

1

a)

ii. The sub-array $A[1 \dots j]$ contains the original contents of sub-array $A[(n + 1 - j) \dots n]$ in reverse order.

v. The sub-array $A[(n+1-j) \dots n]$ contains the original contents of sub-array $A[1 \dots j]$ in reverse order.

b) $2n-1$ c) $2(r-p)+1$

Proof: The total number of calls to MergeSort is 2 times the difference between r and p , plus 1

Base Case: For MergeSort($A, 1, 1$), $r = p = 1$. This means that the total number of calls to MergeSort is $2(1-1)+1=1$ call.

Induction Hypothesis: Let $k, l \in \mathbb{Z}$. Assume $2(k-l)+1$ is true.

Induction Step: a) $k=2, l=1$ (simplest case)

$$2(2-1)+1 = 3$$

b) $k=3, l=2$

$$2(3-2)+1 = 3$$

c) $k=3, l=1$

$$2(3-1)+1 = 5$$

Therefore, by Induction Rule, we can say the MergeSort is called $2(r-p)+1$ times