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a) The all elements in A also exist in A', though they may be in a different order

- b) Loop Invariant 1) The subarray $A[j...n]$ consists of elements of $A[j...n]$ from before the loop, possibly in a different order
 2) $A[j]$ is the smallest of those elements

Initialization: Must hold, because there is only one element and it is the very last element in the array

Maintenance: (1) holds because at each step, we replace $A[j]$ with $A[j-1]$, and we're only adding the previous element and possibly swapping two values. (2) since the loop invariant states that $A[j]$ is the smallest of $A[j...n]$ and $A[j-1]$ becomes the smallest of $A[j]$ and $A[j-1]$

Termination: When the loop terminates, $j=i$, which implies the $A[i]$ is the smallest element of the subarray $A[i...n]$ and contains the original elements in the same order

c) Loop Invariant: At the beginning of each iteration, $A[1...i-1]$ consists of sorted elements, all of which are less than or equal to the ones in $A[i...n]$

Initialization: Array is empty initially

Maintenance: Inner loop invariant states that at each iteration, $A[i]$ becomes the smallest element of $A[i...n]$, while the rest get shuffled around. At the end of the loop, $A[i] < A[k]$, for $i < k$

Termination: At termination, $i=n$, where n is the length of the array. If we substitute I for n in the loop invariant, we can state the $A[1...n]$ consists of the original elements, but they are sorted. At termination, this is the entire array, so the whole array is sorted.

d) $\theta(n^2)$, which is the same as Insertion Sort

e)

- i. If every other element is out of order, such as $[1, 3, 2, 4]$
- ii. There is no permutation where Insertion Sort takes $\theta(n^2)$, but Bubble Sort takes $\theta(n)$