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Coimbatore – 112.

19CSE302 - Design and Analysis of Algorithms

Academic Year : June 2024 – Dec 2024

Semester: V

Comprehensive Evaluation - 1

Float Date: 10th Aug, 2024; Due Date: 20th Aug, 2024.

Course Instructor: Ramraj

For the ensuing questions, you are permitted to collaborate in pairs for the assignment submission. It is essential to distinctly specify each participant's contributions. Moreover, a minimum of two problems must be tackled utilizing either C++ or Java.

- Q.1 | Commence the initial stage by coding the core sorting algorithms, namely:
 - In-Place Quick Sort(Pick the pivot as the last element)
 - 3-Way Merge Sort
 - In-Place Heap Sort
 - Bucket Sort
 - Radix Sort (For this, the input is a linked list and it max. size is 25, in which one node of the linked list possess exactly one element)

Afterward, create a series of random input test cases in diverse sizes, starting with a minimum of 100, and including 500 and 1000. Proceed to assess the efficiency of these algorithms using the criteria listed below:

- Number of comparisons (where applicable)
- Number of swaps (where applicable)
- Number of basic operations (other than the ones mentioned above)
- Execution time in milliseconds
- Memory usage

Upon completing this evaluation, articulate your findings and deduce conclusions.

Submission Requirements:

- Submit code files with clear, succinct comments. It's important to note that code embedded within document files (such as Word documents) is not permissible.
- Include input data files that contain the test cases used for the assessment.
- Provide a detailed report that encapsulates your analysis, complemented by pertinent screenshots.
- Q.2 Optimizations and strategic data structure applications can significantly refine each algorithm's performance. For guidance on implementation, consider consulting "Algorithm Design" by Goodrich et al., along with other pertinent scholarly texts viz., CLRS book.

Detail the refinements applied to the algorithms and expound on how these modifications have elevated their efficiency. This should be substantiated both in theory and through empirical comparison, employing extensive and varied input test cases, against the algorithms' initial versions.

- Q.3 In "Algorithm Design" by Goodrich et al., a variety of algorithms are explicated, along with suggested modifications for enhanced efficiency:
 - a. Chapter 6 addresses the algorithm for detecting strongly connected components, articulation points, and bridges, incorporating both elementary and sophisticated improvements.

- b. Chapter 7 provides a detailed exposition of Dijkstra's algorithm for determining the shortest path from a singular source, inclusive of the path's cost (that includes negative edge weights) and the actual route to all other vertices, as well as its variant algorithms.
- c. The text also explores Boruvka's algorithm for calculating the minimum spanning tree, presenting both the MST's cost and its structure, in addition to different implementation methods.

For each algorithm, undertake an analysis of performance across various implementations—those delineated in the textbook and your selected alternatives—emphasizing the count of primitive operations, duration of execution, and memory consumption. Inputs should include expansive graphs of varied configurations, with at least 20 nodes. Clarify the implementations, inclusive of their modifications, and rationalize the design decisions made, as well as the resultant effects of the diverse algorithms.

Instructions for Submission:

- Supply code files with explicit commentary. It is important to note that code inserted into text documents, such as Word files, will be deemed unacceptable.
- Append input data files that encompass the test cases employed for the performance evaluation.
- Present a thorough report that outlines the alterations, integrates an analytical perspective, and is supplemented with illustrative screenshots.
- Q.4 "Snakes and Ladders," a venerable board game with origins tracing back to no later than the 16th century in India, is played on a board that forms an n X n grid. This grid is sequentially numbered from 1 to n^2, commencing at the lower left corner and advancing row by row from the bottom to the top, with each row alternating direction. Within this grid, specific square pairs, always situated in distinct rows, are interconnected by "snakes" (descending) or "ladders" (ascending). No square may serve as the terminal point for more than one snake or ladder. The objective is to be the swiftest to arrive at the final square, n X n, also known as the paramapatam.

Play begins with a token placed on square 1, located at the bottom left. Each turn allows the player to move their token forward by up to k spaces ($k \le 6$), where k is a predetermined constant. Should the token conclude its move on a snake's head, it must descend to the snake's tail. Conversely, landing on the base of a ladder means the token ascends to the ladder's top.

The tasks at hand are as follows:

You are presented with a board characterized by a) its size n X n (with n being no less than 8), b) the count of snakes and ladders, and c) the starting and ending grid positions of each snake and ladder. Your task is to confirm that the board adheres to these stipulations:

- There exists at least one viable path to the goal.
- No pair of snakes or ladders share the same starting or ending grid position.
- The arrangement of snakes and ladders does not create any loops.

Directly from the starting position, there is no ladder that leads straight to the destination.

Points to Ponder:

Kindly ensure that you submit an individual zip file for every distinct problem. It is crucial to comply with the anti-plagiarism rules set for this task. Reproducing content from fellow students, online sources, or Al-generated content will result in the nullification of the entire

assignment. Should you refer to any external resources, they must be accurately referenced in your report, along with a detailed account of how they informed your work.