

R Notebook

If one SNP has a marginal effect on a phenotype, it is known as an SNP interaction displaying marginal effects. In some cases, however, each individual SNP has no effect on the phenotype, but the combination has a strong effect; this is known as SNP interactions displaying no marginal effects (INME)

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minor allele frequency (MAF)

```
#####simulate SNPs from a latent multivariate Gaussian variable with
##### a CS(rho) correlation structure.
```

```
#####Input:
```

```
#          ORs: association in OR between the causal SNPs and outcome;
#          implicitly, # of causal SNPs = length(ORs);
#          n0: # of controls;
#          n1: # of cases ;
#          nSNP: # of noise/marker SNPs to be generated;
#          rho: the parameter in CS(rho) for the latent multivariate
#          Gaussian variable to be discretized to SNPs;
#          rho=0 means all SNPs are independent;
```

```
#          MAF0slow, MAF0sup: MAFs for the causal SNPs from
#          Unif(MAF0slow, MAF0sup);
#          MAFslow, MAFsup: MAF's of the noise SNPs are drawn from
#          Unif(MAFslow, MAFsup);
```

```
#          p0: background disease prevalence; i.e. true logistic reg model's intercept=log(p0/(1-p0))
```

```
#####Output: a list of the binary outcome Y (=0 or 1) and SNPs (=0, 1 or 2);
```

```
#          Y is a vector of length n=n1+n0; X is a matrix of n by nSNP;
#          and location indices for causal SNPs.
```

```
simRareSNP<-function(ORs, n0=500, n1=500, nSNP=0, rho=0,
                     MAF0slow=0.001, MAF0sup=0.01,
                     MAFslow=0.001, MAFsup=0.01, p0=0.05){
```

```
nSNP0<-length(ORs)
```

```
q<-nSNP+nSNP0
```

```
#####index for causal SNPs; mix causal and noise SNPs:
```

```
##### SNP j is causal iff SNP0index[j]=1 or -1; =0 o/w
```

```
signORs<-rep(1, nSNP0)
```

```
signORs[ORs<1]<-0-1
```

```
SNP0indx<-sample(c(signORs, rep(0, nSNP)), q, replace = FALSE)
```

```
R<-matrix(1, nrow=q, ncol=q)
```

```
for(i in 1:q)
```

```
  for(j in 1:q)
```

```
    if (i!=j) R[i, j]<-rho
```

```
svd.R<-svd(R)
```

```
R1<-svd.R$u %*% diag(sqrt(svd.R$d))
```

```

##background disease prev = p0
b0<-log(p0/(1-p0))
logORs<-log(ORs)

MAF0s<-runif(nSNP0, MAF0slow, MAF0sup)
MAFs1<-runif(nSNP, MAFslow, MAFsup)
cutoff0<-qnorm(MAF0s)
cutoff1<-qnorm(MAFs1)

cutoff<-rep(0, q)
cutoff[SNP0indx!=0]=cutoff0
cutoff[SNP0indx==0]=cutoff1

X<-matrix(0, nrow=n0+n1, ncol=q)
Y<-rep(0, n0+n1); Y[(n0+1):(n0+n1)]<-1
i<-1
#sampling controls:
while ( i <= n0){
  X0<-rnorm(q, 0, 1) #:  $X_0 \sim MVN(0, I)$ 
  X1<-R1 %*% X0 #:  $X_1 \sim MVN(0, R)$ 
  X2<-ifelse(X1<cutoff, 1, 0)
  X0<-rnorm(q, 0, 1) #:  $X_0 \sim MVN(0, I)$ 
  X1<-R1 %*% X0 #:  $X_1 \sim MVN(0, R)$ 
  X3<-ifelse(X1<cutoff, 1, 0)
  X4<-X2+ X3
  pr<-1/(1 + exp(-(b0 + sum(logORs * X4[SNP0indx!=0]))))
  Y1<-sample(c(0, 1), 1, prob=c(1-pr, pr))
  if (Y1==0){
    X[i, ]<-X4
    i<-i+1
  }
}
#sampling cases:
while ( i <= n0+n1){
  X0<-rnorm(q, 0, 1) #:  $X_0 \sim MVN(0, I)$ 
  X1<-R1 %*% X0 #:  $X_1 \sim MVN(0, R)$ 
  X2<-ifelse(X1<cutoff, 1, 0)
  X0<-rnorm(q, 0, 1) #:  $X_0 \sim MVN(0, I)$ 
  X1<-R1 %*% X0 #:  $X_1 \sim MVN(0, R)$ 
  X3<-ifelse(X1<cutoff, 1, 0)
  X4<-X2+ X3
  pr<-1/(1 + exp(-(b0 + sum(logORs * X4[SNP0indx!=0]))))
  Y1<-sample(c(0, 1), 1, prob=c(1-pr, pr))
  if (Y1==1){
    X[i, ]<-X4
    i<-i+1
  }
}

list(Y=Y, X=X, SNP0indx=SNP0indx)
}

```

```

now <- Sys.time()
### but how to pick false pos correlated to a gene??
#-----
## There is a coef for each gene plus the intercept
coef.pvalues.naive<-NULL
coef.pvalues.labeled<-NULL
num.iter<-5
ORs<-sample(c(.25,.5,2,4),100,replace = TRUE)
ORs<-rep(10,20)

for(i in 1:num.iter){

naive.rupture<-c(rep(0,300),rep(1,300))

foo<-simRareSNP(ORs=ORs
               , n0=285
               , n1=315
               , nSNP=200
               , rho=0,
               MAF0slow=0.001, MAF0sup=0.05,
               MAFslow=0.001, MAFsup=0.05, p0=0.05)

labeled.rupture<-foo$Y
predisposition<-foo$X

df<-data.frame(predisposition=predisposition
               ,naive.rupture=naive.rupture
               ,labeled.rupture=labeled.rupture)

m.naive<- glm(naive.rupture ~ predisposition, family="binomial",data=df)

m.labeled<- glm(labeled.rupture ~ predisposition, family="binomial",data=df)

coef.pvalues.naive<-c(coef.pvalues.naive,coef(summary(m.naive))[,4])
coef.pvalues.labeled<-c(coef.pvalues.labeled,coef(summary(m.labeled))[,4])

} #end loop

pvalues.diff<-(coef.pvalues.labeled<0.05)==
               (coef.pvalues.naive<0.05)

sum(pvalues.diff)/length(pvalues.diff)

## [1] 0.5833
difftime(Sys.time(),now)

## Time difference of 3.511 secs

```

```
Sys.sleep(2)
```

Time for this code chunk to run: 2.05122303962708