

## PBHS 43010: Homework #5

Based on the data “log.txt”, perform a model selection based on RJMCMC. The models under consideration are

$$\begin{aligned} m = 1 & : \log(\lambda(x)) = \beta_0 + \beta_1 x \\ m = 2 & : \log(\lambda(x)) = \beta_0 + \beta_1 x + \beta_2 x^2 \end{aligned}$$

In the data file, the first column is  $x$ , a continuous covariate, and the second column is  $y$ , the Poisson outcome where  $y \sim \text{Poi}(\lambda(x))$ .

Consider parameter space  $\{m = 1, \beta_0, \beta_1\}$  and  $\{m = 2, \beta_0, \beta_1, \beta_2\}$ . Use RJMCMC to estimate the posterior of  $m$ ,  $\beta_0$ ,  $\beta_1$ , and  $\beta_2$ . Draw the trace plots for them and make a conclusion if  $m = 1$  or  $m = 2$  is a better model by comparing their marginal posterior probabilities.