

Date:

تاریخ:

Subject: 06 - 99527361

موضوع:

1) a) i) there are  $n$   $\alpha$  scores which represent the probabilities associated with each element in the sequence. these scores are normalized so they sum up to 1.

ii)  $k_j \gg k_i \{i \in \{1, \dots, n\}, i \neq j\}$   
so the dot product of  $k_j$  and query will be large that means the softmax will put most of the probability on this.

iii)  $\alpha_j \gg \alpha_i \rightarrow C = \sum_{i=1}^n v_i \alpha_i \sim v_j \alpha_j \sim v_j$

iv) if one of the key is similar to given query, the attention weight will be its value. so the output sense we copied the keys value

$$b) i) \quad \left. \begin{aligned} v_a &= c_1 a_1 + c_2 a_2 + \dots + c_n a_n = A c \\ v_b &= d_1 b_1 + d_2 b_2 + \dots + d_p b_p = B d \\ M v_a + M v_b &= v_a \end{aligned} \right\} M A c + M B d = v_a$$

we want  $M v_a = v_a$  and  $M v_b = 0$

$$a_j^T b_k = 0, \quad a_j^T a_i = 0 \rightarrow i \neq j, \quad a_j^T a_i = 1 \rightarrow i = j$$

$$\text{if } M = A^T \rightarrow A^T A c + A^T B d = I c + 0 = c$$

and we know  $v_a$  is a collection of constants  $c$  in terms of  $Rd$

$$\text{so } \rightarrow M = A^T$$

$$ii) \quad k_a^T q \sim k_b^T q \gg k_i^T q \quad (i \neq a, b)$$

so the probability mass will be big on  $a$  and  $b$

$$q \sim \beta (k_a + k_b) \rightarrow \beta = k_a^T q = k_b^T q$$

$$(\beta \gg 0)$$

$$\alpha_a = \alpha_b = \frac{\exp(\beta)}{n-2 + 2\exp(\beta)} \sim \frac{\exp(\beta)}{2\exp(\beta)} = \frac{1}{2} \quad (\beta \gg 0)$$

$$c = \sum_{i=1}^n v_i \alpha_i = 0 + \frac{1}{2} v_a + \frac{1}{2} v_b$$



c) i) variances are vanishingly small so  $\kappa_i \sim \mu_i$ .  
 thus we can write equations like part b  
 and we have:  $q = \beta(\mu_a + \mu_b)$  ( $\beta \gg 0$ )

ii)  $\Sigma_a = \alpha I + \frac{1}{2}(\mu_a \mu_a^T)$  and  $\mu_a \mu_a^T = 1$

$$\Rightarrow \kappa_a \in [0, 0.5\mu_a, 1, 0.5\mu_a]$$

$$\kappa_a \sim Y\mu_a \quad (Y \sim N(\mu_a, \alpha I (\mu_a \mu_a^T))) \rightarrow Y \sim N(1, 1/2)$$

$$\kappa_i \sim \mu_i \quad (i \neq a)$$

$$\kappa_a^T q \sim Y\mu_a^T \beta(\mu_a + \mu_b) \quad (\beta \gg 0)$$

$$\kappa_b^T q \sim \mu_b^T \beta(\mu_a + \mu_b) \quad (\beta \gg 0)$$

$$\kappa_i^T q \sim \mu_i^T \beta(\mu_a + \mu_b) = 0 \quad (\beta \gg 0)$$

$$\alpha_a \sim \frac{\exp(Y\beta)}{\exp(Y\beta) + \exp(\beta)} \sim \frac{1}{1 + \exp(\beta(1-Y))}$$

$$\alpha_b \sim \frac{\exp(\beta)}{\exp(Y\beta) + \exp(\beta)} \sim \frac{1}{1 + \exp(\beta(Y-1))}$$

$$\rightarrow Y = 0.5 \rightarrow \alpha_a \sim 0, \alpha_b \sim 1$$

$$\rightarrow Y = 1.5 \rightarrow \alpha_a \sim 1, \alpha_b \sim 0$$

So  $C = \alpha_a \mu_a + \alpha_b \mu_b$  oscillates between  $\mu_a$  and  $\mu_b$

$$d) i) \quad q_1 = q_2 = \beta(u_a + u_b)$$

$$\begin{aligned} \rightarrow C &= \frac{1}{2}(C_1 + C_2) = \frac{1}{2} \left( \frac{1}{2}(u_a + u_b) + \frac{1}{2}(u_a + u_b) \right) \\ &= \frac{1}{2}(u_a + u_b) \end{aligned}$$

ii) As  $q_1 = q_2 = \beta(u_a + u_b)$  so like part c(ii),

$$C = \frac{1}{1 + \exp(\beta(1-\gamma))} u_a + \frac{1}{1 + \exp(\beta(\gamma-1))} u_b.$$

$$\gamma \rightarrow 1 \Rightarrow C = \frac{1}{2}u_a + \frac{1}{2}u_b = \frac{1}{2}(u_a + u_b)$$

2)d) Correct: 100 out of 500.0: 2.0%.  
London: Correct: 25.0 out of 500.0: 5.0%.

f) Correct: 72.0 out of 500.0: 14.39%



g) i) Correct: 94.0 out of 500.0 : 8.79%

ii) In the perceiver approach, the attention layer has important rule in which it reduces the complexity to  $O(m \times d)$  ( $d$  is input dimensionality) (cross-attention)

In Latent transformer blocks the complexity reduces to  $O(m^2)$  (self-attention)

So, the complexity of multi-headed is  $O(L^2 d + Ld)$  and the perceiver complexity is  $O(dn + Lm^2)$

3) a) because the pretrained model had more knowledge about relation of words and patterns. so, it can generalize better on new examples.

b) 1) it can cause to the spread of misinformation so this leads to confusion.

2) it can cause users to use false information in their works or some researches. so it's a legal impact.

c) the model try to find correlations and patterns based on other information of people with similar names. so, the prediction may be false and it cause concern as mentioned in 3b.