

السؤال ٢:

$P(A|y)$

0 A 1

$$y \begin{pmatrix} 0 & 0.75 & 0.25 \\ 1 & 0 & 1 \end{pmatrix}$$

$P(B|y)$

0 B 1

$$\begin{pmatrix} 0.5 & 0.5 \\ 0.33 & 0.66 \end{pmatrix}$$

$P(C|y)$

0 C 1

$$\begin{pmatrix} 0.5 & 0.5 \\ 0.66 & 0.33 \end{pmatrix}$$

$$P(y=0) = \frac{4}{7}$$

$$P(y=1) = \frac{3}{7}$$

$$P(y=0|x_1) \propto P(y=0) P(A=0|y=0) P(B=0|y=0) P(C=0|y=0) = \frac{4}{7} \times 0.75 \times 0.5 \times 0.5 = 0.107$$

$$P(y=1|x_1) \propto P(y=1) P(A=0|y=1) P(B=0|y=1) P(C=0|y=1) = \frac{3}{7} \times 0 \times 0.33 \times 0.66 = 0$$

$$\Rightarrow \hat{y}_1 = 0$$

$$P(y=0|x_2) \propto P(y=0) P(A=1|y=0) P(B=1|y=0) P(C=1|y=0) = \frac{4}{7} \times 0.25 \times 0.5 \times 0.5 = 0.035$$

$$P(y=1|x_2) \propto P(y=1) P(A=1|y=1) P(B=1|y=1) P(C=1|y=1) = \frac{3}{7} \times 1 \times 0.66 \times 0.33 = 0.095$$

$$\Rightarrow \hat{y}_2 = 1$$

$$P(y=0|x_3) \propto P(y=0)P(B=1|y=0)P(C=0|y=0) = \frac{4}{7} \times 0.5 \times 0.5 = 0.142$$

$$P(y=1|x_3) \propto P(y=1)P(B=1|y=1)P(C=0|y=1) = \frac{3}{7} \times 0.66 \times 0.66 = 0.190$$

$$\Rightarrow \hat{y}_3 = 1$$

$$P(y=0|x_4) \propto P(y=0)P(B=0|y=0)P(C=1|y=0) = \frac{4}{7} \times 0.5 \times 0.5 = 0.142$$

$$P(y=1|x_4) \propto P(y=1)P(B=0|y=1)P(C=1|y=1) = \frac{3}{7} \times 0.33 \times 0.33 = 0.047$$

$$\Rightarrow \hat{y}_4 = 0$$