

#1 a)
$$\begin{cases} N_D = 2 \times 10^{14} \text{ cm}^{-3} \\ T = 300 \text{ K} \\ n_i = 1.66 \times 10^{15} \times T^{\frac{3}{2}} \times e^{\frac{-E_g}{2kT}} \text{ cm}^{-3} \end{cases}$$

$$\Rightarrow n_i = 1.66 \times 10^{15} \times 300^{\frac{3}{2}} \times e^{\frac{0.66 \times 1.6 \times 10^{-19}}{2(1.38 \times 10^{-23}) \times 300}} = 2.5 \times 10^{13} \text{ cm}^{-3}$$

$$\Rightarrow n = n_i + N_D = 0.25 \times 10^{14} + 2 \times 10^{14} = 2.25 \times 10^{14}$$

$$n_p = n_i^2 \Rightarrow p = \frac{n_i^2}{n} = \frac{(2.5 \times 10^{13})^2}{2.25 \times 10^{14}} = 2.7 \times 10^{12} \text{ cm}^{-3}$$

b) $\sigma_I = q n_i (\mu_n + \mu_p)$, $\sigma_N = q \left(n \mu_n + \left(\frac{n_i^2}{n} \right) \mu_p \right)$

$$\Rightarrow \frac{\sigma_N}{\sigma_I} = \frac{n \mu_n + \left(\frac{n_i^2}{n} \right) \mu_p}{n_i (\mu_n + \mu_p)} = \frac{2.25 \times 10^{14} \times 3800 + 2.7 \times 10^{12} \times 1800}{2.5 \times 10^{13} (1800 + 3800)} = 6.12$$

#2
$$\begin{cases} I_s = ? \\ \eta = 2 \\ I_0 = 5 \end{cases} \Rightarrow I_0 = I_s \left(e^{\frac{V_D}{\eta V_T}} - 1 \right) \Rightarrow 5 = I_s \left(e^{\frac{100}{2 \times 26}} - 1 \right)$$

$$\Rightarrow I_s = 0.86 \text{ mA}$$

#3 a)
$$n_i = (1.66 \times 10^{15}) \times 400^{\frac{3}{2}} \times e^{\frac{1.1 \times 1.6 \times 10^{-19}}{2(1.38 \times 10^{-23}) \times 400}} = 3 \times 10^{13} \text{ cm}^{-3}$$

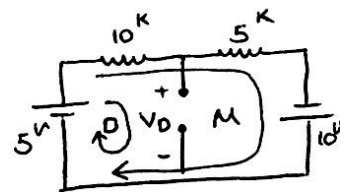
$$n = N_D = 10^{17} , n_p = n_i^2 \Rightarrow p = \frac{n_i^2}{N_D} = \frac{(3 \times 10^{13})^2}{10^{17}} = 9 \times 10^9 \text{ cm}^{-3}$$

b)
$$\rho = \frac{1}{q(\mu_n n + \mu_p p)} = \frac{1}{1.66 \times 10^{-19} (1300 \times 10^{17} + 500 \times 9 \times 10^9)} \approx 0.5$$

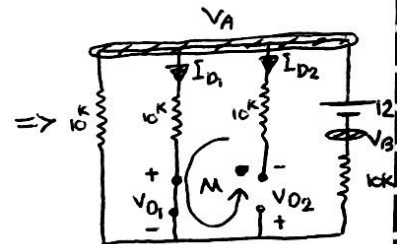
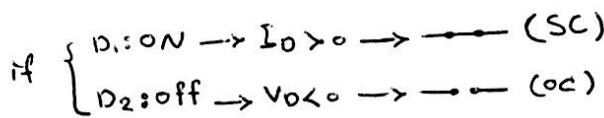
c)
$$R_2 = \frac{L}{h \omega q (\mu_n n + \mu_p p)} = \frac{0.1}{10^3 \times 10^{-2} \times 1.66 \times 10^{-19} (1300 \times 10^{17} + 500 \times 9 \times 10^9)} \approx 5 \times 10^3 \Omega$$

$$R_T = R_1 + R_2 = 6 \text{ k}\Omega , V_0 = 10 \text{ V} \Rightarrow I = \frac{V_0}{R_T} = \frac{10}{6 \times 10^3} = 1.6 \times 10^{-3} \text{ A}$$

a) ideal diodes :



$$\Rightarrow V_D = -5^V < 0 \quad \checkmark, \quad \underline{I_D = 0}$$



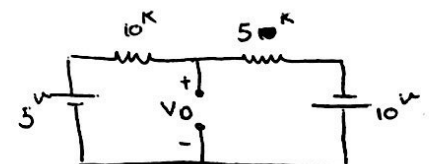
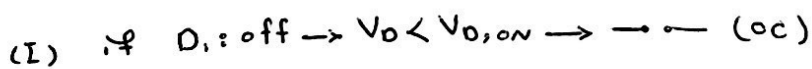
$$\text{KCL @ } V_A, V_B: \frac{V_A}{10} + \frac{V_A}{10} + \frac{V_A}{10} + \frac{V_B}{10} = 0 \Rightarrow \frac{V_A}{5} + \frac{V_B}{10} = 0 \quad (I)$$

$$V_A - V_B = 12 \quad \text{(II)} \xrightarrow{\text{(II) in (I)}} \frac{V_A}{5} + \frac{V_A - 12}{10} = 0 \Rightarrow \underline{V_A = \frac{12}{3} = 4^V}, \quad \underline{V_B = V_A - 12 = 4 - 12 = -8}$$

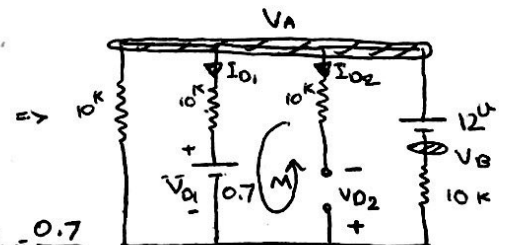
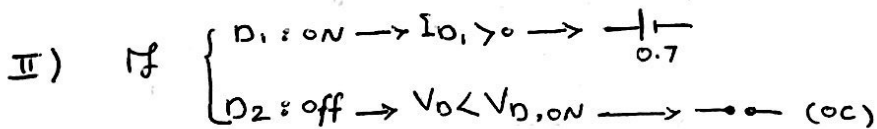
$$\Rightarrow I_{D1} = \frac{V_A}{10^k} = \frac{4}{10^k} = \frac{2}{5} \text{ mA} > 0 \quad \checkmark, \quad \underline{I_{D2} = 0}, \quad \text{KVL @ M: } I_{D1} \times 10^k + V_{D2} + \cancel{I_{D2} \times 10^k} = 0$$

$$\Rightarrow \underline{V_{D2} = -4 < 0} \checkmark$$

b) Constant voltage source : ($V_{0,on} = 0.7^v$)



ایده آل : $V_D = -5V < V_{D,ON}$ ✓ , $I_{D1} = 0A$



$$\text{KCL @ } V_A, V_B: \frac{V_A}{10} + \frac{V_A - 0.7}{10} + \frac{V_A}{10} + \frac{V_B}{10} = 0 \Rightarrow \frac{V_A}{5} + \frac{V_B}{10} = \frac{0.7}{10} \quad (I)$$

$$V_A - V_B = 12 \text{ (II)} \quad \xrightarrow{\text{(II) in (I)}} \quad \frac{V_A}{5} + \frac{V_A - 12}{10} = \frac{0.7}{10} \Rightarrow \frac{3V_A}{10} = \frac{12.7}{10} \Rightarrow V_A = \frac{12.7}{3} \approx 4.23$$

$$V_B = 4.23 - 12 = -7.76 \quad , \quad I_{D1} = \frac{V_A - 0.7}{10} = \frac{4.23 - 0.7}{10} = 0.353 > 0 \quad \checkmark$$

$$I_{D2} = 0 \rightarrow \text{KVL @ M: } 10I_{D1} + 0.7 + V_{D2} + 10I_{D2} = 0 \Rightarrow V_{D2} = -4.23 \text{ V} < V_{D1, \text{on}} \checkmark$$

#6 nalsl : input-output characteristic = ?

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$$\therefore V_{in} < 8.8 \rightarrow I_{D1} > 0 \rightarrow D_1 : \text{ON} \rightarrow V_{out} = 2.2$$

∴ $D_1: \text{off} \rightarrow V_{O_1} < 0 \rightarrow \text{---} \bullet \text{---} (OC)$

$$\text{KVL @ ①: } +V_{in} + 1 \times I_{in} + 3 \times I_{in} = 0 \Rightarrow I_{in} = \frac{-1}{4} V_{in} \quad (I)$$

$$\text{KVL @ (2)}: +V_{in} - 3 + V_{01} + 3 \times I_{in} = 0 \quad (\text{II})$$

$$\underline{\text{(I) in (II)}} \rightarrow V_{in} - 3 + V_{O1} + 3\left(\frac{-V_{in}}{4}\right) = 0 \Rightarrow V_{O1} = 3 - \frac{1}{4}V_{in} < 0 \Rightarrow V_{in} > 12$$

$$\text{KCL @ } V_{out} : \frac{V_{out}-0}{1} + \frac{V_{out}-V_{in}}{3} = 0 \Rightarrow 4V_{out} = V_{in} \Rightarrow V_{out} = \frac{1}{4}V_{in}$$

$$\Rightarrow \boxed{V_{in} > 12 \rightarrow V_{D1} < 0 \rightarrow D_1: \text{off} \rightarrow V_{out} = \frac{1}{4} V_{in}}$$

