

* حل سوال اول :

$$KVL: -V_{BE,ref} + R_p I_{B,ref} + V_{BE1} = 0$$

$$\Rightarrow V_T \ln \frac{I_1}{I_s} - V_T \ln \frac{I_{B,ref}}{I_s} = R_p \frac{I_{B,ref}}{\beta}$$

$$\Rightarrow V_T \ln \frac{I_{ref}}{I_{B,ref}} = R_p \frac{I_{B,ref}}{\beta} \quad (1)$$

$$KCL: I_{ref} = I_{C,ref} + I_{B1} + I_{B,ref} = I_{C,ref} + \frac{I_{C,ref}}{\beta} + \frac{I_{ref}}{\beta}$$

$$\Rightarrow I_{ref} \left(1 - \frac{1}{\beta}\right) = I_{C,ref} \left(1 + \frac{1}{\beta}\right) \Rightarrow I_{C,ref} = \frac{\beta-1}{\beta+1} I_{ref} \quad (2)$$

$$(1), (2) \Rightarrow V_T \ln \frac{I_{ref}}{\frac{\beta-1}{\beta+1} I_{ref}} = R_p \times \frac{\beta-1}{\beta+1} I_{ref} \times \frac{1}{\beta}$$

$$\Rightarrow \left(V_T \ln \frac{\beta+1}{\beta-1}\right) \times \frac{\beta+1}{\beta-1} \times \frac{\beta}{I_{ref}} = R_p$$

* حل سوال دوم :

$$I_{M9} = \frac{1}{2} \mu_p C_{ox} \left(\frac{W}{L}\right)_9 (V_{SG9} - |V_{TH1}|)^2 = \frac{1}{2} \times 0.1 \times 5 (V_{SG9} - 1)^2$$

$$\Rightarrow V_{SG9} = V_{DD} - 7 I_{M9} = 10 - 7 I_{M9} \Rightarrow \frac{1}{2} \times 0.1 \times 5 (10 - 7 I_{M9} - 1)^2 \Rightarrow I_{M9} = 1^{mA}$$

$$\Rightarrow V_{SG9} = 3 > V_{TH1} \quad \checkmark$$

$$I_{D8} = I_{D9} = I_{D7} = 1^{mA}, \quad I_{M6,5} = 4 \times I_{M7} = 4^{mA}$$

$$\Rightarrow I_{M6,M2} = \frac{1}{2} I_{M6,5} = 2^{mA}$$

$$\min \{V_{G1}\} = V_{GS5} + V_{DSSAT6} \quad (1)$$

$$I_{M5} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_5 (V_{GS5} - V_{TH1})^2 \Rightarrow 4 = \frac{1}{2} \times 0.4 \times 20 (V_{GS5} - 1)^2 \Rightarrow V_{GS5} = 2^V$$

$$(1), (2) \Rightarrow \min \{V_{G1}\} = 2 + 1 = 3^V \quad \Rightarrow V_{eff5,6} = 2 - 1 = 1^V \quad (2)$$

$$I_{M1} = I_{M3} + I_0 \Rightarrow I_{M3} = I_{M1} - I_0 = 2 - 1.5 = 0.5 \text{ mA}$$

(1)

$$|V_{eff3}| = V_{SG3} - |V_{TH}| \Rightarrow 1^V = V_{SG3} - 1 \Rightarrow V_{SG3} = 2^V$$

$$V_{in, max} = \min \{ V_{DD} - V_{SG3} - V_{eff1} + V_{GS1}, V_{DD} - V_{I_0, min} - V_{eff1} + V_{GS1} \}$$

$$= \min \{ 9, 10 \} = 9^V$$

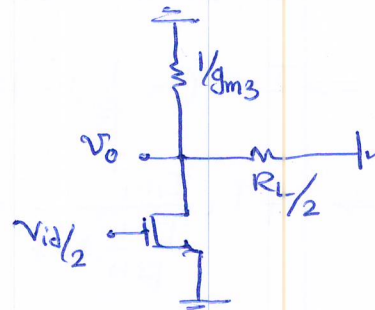
$$V_{in, min} = V_{GS1} + 2V_{eff5} = 4^V$$

$$A_d = \frac{1}{2} g_{m1} \alpha (1/g_{m3} \parallel R_L/2)$$

$$g_{m1} = 2I_{D1}/V_{eff1} = 4 \text{ mA/V},$$

$$g_{m3} = 2I_{D3}/V_{eff3} = \frac{2 \times 0.5}{1} = 1 \text{ mA/V}$$

$$\Rightarrow A_d = \frac{1}{2} \times 4^m (1/1^m \parallel 1^k) = 1^V/V$$



(2)

$$A_{cm} = \frac{1/g_{m3}}{1/g_{m1} + 2R_{EE}} = \frac{1/g_{m3}}{1/g_{m1} + 2r_{ds}(1 + g_{m5}r_{ds6})}$$

$$r_{ds5} = r_{ds6} = \frac{1}{0.1 \times 4} = 2.5^k\Omega$$

$$g_{m5} = \frac{2 \times 4}{1} = 8 \text{ mA/V}$$

$$\Rightarrow A_{cm} = \frac{1^k}{1/4^m + 2 \times 2.5^k \times 8 \times 2.5} \approx 0.01$$

