

# 5-1

$$\begin{cases} V_m = 480 \text{ V (rms)} \\ f = 60 \text{ Hz} \\ R_L = 50 \Omega \\ \alpha = 60^\circ \end{cases}$$

a) rms Load voltage?  $V_{o,rms} = \frac{V_m}{\sqrt{2}} \left[ 1 - \frac{\alpha}{\pi} + \frac{\sin(2\alpha)}{2\pi} \right]^{\frac{1}{2}} = V_{rms} \left[ 1 - \frac{\alpha}{\pi} + \frac{\sin(2\alpha)}{2\pi} \right]^{\frac{1}{2}}$

$V_m = 480\sqrt{2}$ ,  $\alpha = 60^\circ$ ,  $V_{o,rms} = 431 \text{ V} \Rightarrow I_{o,rms} = \frac{V_{o,rms}}{R} = \frac{431}{50} = 8.61 \text{ A}$

b)  $P_L = \frac{V_{o,rms}^2}{R} = \frac{(431)^2}{50} = 3708 \text{ W}$

c)  $PF = \frac{P}{S} = \frac{P}{V_{rms} I_{rms}} = \frac{3708}{480(8.61)} = 0.897$

d)  $I_{avg, SCR} = \frac{V_m}{2\pi R} (1 + \cos \alpha) = \frac{480\sqrt{2}}{2\pi(50)} (1 + \cos 60) = 3.24 \text{ A}$

$I_{rms, SCR} = \frac{I_{o,rms}}{\sqrt{2}} = \frac{8.61}{\sqrt{2}} = 6.1 \text{ A}$

e)  $I_{i,rms} \approx 0.84 \left( \frac{480}{50} \right) = 8 \text{ A} \Rightarrow THD_i = \frac{\sqrt{I_{rms}^2 - I_{i,rms}^2}}{I_{i,rms}} = \frac{\sqrt{(8.61)^2 - 8^2}}{8} = 38\%$

# 5-6 for  $P = 750 \text{ W} \Rightarrow V_{o,rms} = \sqrt{PR} = \sqrt{750(32)} = 154.9 \text{ V}$

$\Rightarrow 154.9 - 240 \sqrt{1 - \frac{\alpha}{\pi} + \frac{\sin(2\alpha)}{2\pi}} = 0 \Rightarrow \alpha = 1.703 \text{ rad} = 97.6^\circ$

for  $P = 1500 \text{ W} \Rightarrow V_{o,rms} = \sqrt{PR} = \sqrt{1500(32)} = 219 \text{ V}$

$\Rightarrow 219 - 240 \sqrt{1 - \frac{\alpha}{\pi} + \frac{\sin(2\alpha)}{2\pi}} = 0 \Rightarrow \alpha = 0.986 \text{ rad} = 56.5^\circ$

$I_{SCR, rms} = \frac{I_o}{\sqrt{2}} = \frac{\frac{219}{32}}{\sqrt{2}} = 4.84 \text{ A}$ ,  $I_{SCR, avg} = \frac{V_m}{2\pi R} (1 + \cos \alpha) = \frac{240\sqrt{2}}{2\pi(32)} (1 + \cos(56.5^\circ))$

$$= 2.62^A$$

$$\Rightarrow V_{max} = 240\sqrt{2} = 340V$$

# 5-9

$$\text{for } \begin{cases} S_1: 0V & ; (\alpha, \pi) \\ D_2: 0V & ; (\alpha, 2\pi) \end{cases}$$

$$V_o(\omega t) = V_m \sin \omega t \quad ; \quad \alpha < \omega t < 2\pi \quad \Rightarrow \quad V_{o,rms} = \left[ \frac{1}{2\pi} \int_{\alpha}^{2\pi} (V_m \sin \omega t)^2 d\omega t \right]^{\frac{1}{2}}$$

$$= V_m \left[ \frac{1}{2} - \frac{\alpha}{4\pi} + \frac{\sin(2\alpha)}{8\pi} \right]^{\frac{1}{2}} = \frac{V_m}{\sqrt{2}} \left[ 1 - \frac{\alpha}{2\pi} + \frac{\sin(2\alpha)}{4\pi} \right]^{\frac{1}{2}} \xrightarrow{0 \leq \alpha \leq \pi} \frac{V_m}{2} \leq V_{o,rms} \leq \frac{V_m}{\sqrt{2}}$$

# 5-13

$$\begin{cases} Z = 15^{\Omega} \\ \theta = 0.646^{\text{rad}} \\ \omega\tau = 0.754 \end{cases}$$

$$i(\omega t) = 11.3 \sin(\omega t - 0.646) - 15.8 e^{\frac{-\omega t}{0.754}} A$$

$$\alpha = 115^\circ = 2.01 \text{ Rad} \quad , \quad \beta = 3.681^{\text{rad}} = 211^\circ$$

$$I_{rms} = 2.95^A$$

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