

#6-4

$$\begin{cases} V_s = 24V \\ D = 0.65 \\ L = 25\mu H \\ C = 15\mu F \\ R = 10\Omega \end{cases}$$

a) output Voltage?

b) Max and Min Inductor current?

c) output Voltage ripple?

$$a) V_o = DV_s = 24(0.65) = 15.6V$$

$$b) I_L = I_R = \frac{V_o}{R} = \frac{15.6}{10} = 1.56A \Rightarrow \Delta I_L = \frac{V_o}{L}(1-D)T = \frac{15.6}{25 \times 10^{-6}}(1-0.65) \times \frac{1}{100000} = 2.18A$$

$$I_{L,max} = I_L + \frac{\Delta I_L}{2} = 1.56 + \frac{2.18}{2} = 2.65A, I_{L,min} = I_L - \frac{\Delta I_L}{2} = 1.56 - \frac{2.18}{2} = 0.47A$$

$$c) \Delta V_o = \frac{V_o(1-D)}{8LCf^2} = \frac{15.6(1-0.65)}{8(25 \times 10^{-6}) \times 15 \times 10^{-6}(100000)} = 0.182 \text{ or } \frac{\Delta V_o}{V_o} = 1.17\%$$

#6-7

$$\begin{cases} V_{input} = 6V \\ V_{out} = 1.5V \\ R_L = 3\Omega \\ \text{switching freq} = 400kHz \\ L = 5\mu H, C = 10\mu F \end{cases}$$

a) duty ratio?

b) average, Peak, rms Inductor current

c) average source current?

d) Peak and average Diode current

$$a) D = \frac{V_o}{V_s} = \frac{1.5}{6} = 0.25$$

$$b) \text{ average: } I_L = I_R = \frac{V_o}{R} = \frac{1.5}{3} = 0.5A, \text{ rms: } I_{L,rms} = \left[(0.5)^2 + \left(\frac{0.5625}{\sqrt{3}} \right)^2 \right]^{\frac{1}{2}} = 0.526A$$

$$\Delta I_L = 0.5625$$

$$\text{Peak: } I_{L,max} = V_o \left(\frac{1}{R} + \frac{1-D}{2Lf} \right) = 1.5 \left(\frac{1}{3} + \frac{1-0.25}{2(5 \times 10^{-6})(400000)} \right) = 0.781A$$

$$I_{L,min} = V_o \left(\frac{1}{R} - \frac{1-D}{2Lf} \right) = 0.219A$$

$$c) P_s = P_o = V_s I_s = V_o I_R \Rightarrow I_s = \frac{V_o I_R}{V_s} = \frac{1.5(0.5)}{6} = 0.125 \text{ A}$$

$$d) I_{D, \max} = I_{L, \max} = 0.781 \text{ A} \Rightarrow I_D = I_o - I_s = 0.5 - 0.125 = 0.375 \text{ A}$$

#6-10

$$L_{\min} = \frac{(1-D)R}{2f}$$

$$f = 200 \text{ kHz}$$

$$V_o = 5 \text{ V}$$

| $V_s (\text{V})$ | D | $I (\text{A})$ | $R (\Omega)$ | $L_{\min} (\mu\text{H})$ |
|------------------|---------------|----------------|--------------|--------------------------|
| 10 | 0.5 | 0.5 | 10 | 12.5 |
| 10 | 0.5 | 1 | 5 | 6.25 |
| 15 | $\frac{1}{3}$ | 0.5 | 10 | 16.7 |
| 15 | $\frac{1}{3}$ | 1 | 5 | 8.33 |

$$L = \frac{(1-D_{\min})R_{\max}}{2f}$$

$$L_{\min} = \frac{(1-\frac{1}{3})10}{2(200)} = 16.67 \mu\text{H}$$

#6-15

$$V_n = \frac{\sqrt{2} V_s}{n\pi} \sqrt{1 - \cos(2n\pi D)} \quad n = 1, 2, 3, \dots$$

$$\text{if } n=1 \Rightarrow V_1 = 30.27$$

$$\Rightarrow V_{o1} = 0.048 \text{ V} = 2(0.048) = 0.096 \text{ V}_{\text{p-p}}$$

$$\frac{0.096}{V_o} = \frac{0.096}{20} = 0.48\%$$

$$\Rightarrow \frac{\Delta V_o}{V_o} = 0.469\%$$

#6-19

$$\begin{cases} V_{in} = 5 \text{ V} \\ P_{out} = 25 \text{ W} \\ V_{out} = 15 \text{ V} \end{cases}$$

$$V_o = \frac{V_s}{1-D} \Rightarrow D = 1 - \frac{V_s}{V_o} = 1 - \frac{5}{15} = 0.667$$

$$R = \frac{V_o^2}{25} = \frac{15^2}{25} = 9 \Omega$$

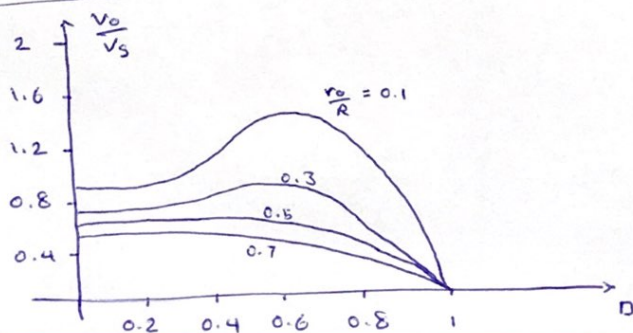
$$I_L = \frac{V_s}{(1-D)^2 R} = \frac{5}{(1-0.667)^2 \cdot 9} = 5 \text{ A}$$

$$I_{L, \min} = 0.5(5) = 2.5 \text{ A} \Rightarrow \Delta I_L = 5 \text{ A}$$

$$\Delta I_L = \frac{V_s D T}{\Delta I_L} = \frac{5(0.667)/300}{5} = 2.22 \mu\text{H}$$

$$\rightarrow C = \frac{0.667}{9(0.01)(300000)} = 24.7 \mu\text{F}$$

#6-22



#6-25

$$\begin{cases} V_s = 24 \text{ V} \\ V_o = -36 \\ R_L = 10 \Omega \\ \text{switching } f_{\text{req.}} = 100 \text{ KHz} \end{cases}$$

a) If Minimum Inductance Current is 40% of the average $\rightarrow L = ?$

b) $C = ? \rightarrow \text{ripple} = 0.5\%$

$$a) D = \frac{|V_o|}{V_s + |V_o|} = \frac{36}{24 + 36} = 0.6$$

$$I_L = \frac{V_s \cdot D}{R(1-D)^2} = \frac{24(0.6)}{10(1-0.6)^2} = 9 \text{ A}$$

$$I_{L, \min} = 0.4(9) = 3.6 \text{ A}, \quad \Delta I_L = 2(9 - 3.6) = 10.8 \text{ A}$$

$$\Rightarrow L = \frac{V_s D T}{\Delta I_L} = \frac{24(0.6)}{10.8(100000)} = 13.3 \mu\text{H}$$

$$b) C = \frac{D}{R \left(\frac{\Delta V_o}{V_o} \right) f} = \frac{0.6}{10(0.005)(100000)} = 12 \mu\text{F}$$

#6-28

$$D = \frac{|V_o|}{V_s + |V_o|}, \quad R = \frac{V_o^2}{P}, \quad I_{\min} = \frac{(1-D)^2 R}{2f}, \quad I_L = \frac{P}{DV_s}$$

$$C = \frac{D}{R \left(\frac{\Delta V_o}{V_o} \right) f} \quad \text{if } f = 100 \text{ KHz}$$

$$V_s = 14 \text{ V}$$

$$P = 10 \text{ W}$$

$$L = 20.9 \mu\text{H}$$

$$C = 56.8 \mu\text{F}$$

| V_s (V) | P (W) | D | R (Ω) | L_{\min} (μH) | I_L (A) | C (μF) |
|-----------|---------|-------|------------------|------------------------------|-----------|-----------------------|
| 10 | 10 | 0.545 | 14.4 | 14.9 | 1.83 | 37.9 |
| 10 | 15 | 0.545 | 9.6 | 9.9 | 2.75 | 56.8 |
| 14 | 10 | 0.462 | 14.4 | 20.9 | 1.55 | 32.1 |
| 14 | 15 | 0.462 | 9.6 | 13.9 | 2.32 | 48.1 |

#6-31

$$\frac{V_o}{V_s} = -\frac{D}{1-D} = \frac{-30}{25} = -1.2 \Rightarrow D = 0.5455$$

$$I_{L2} = \frac{P}{V_o} = \frac{60}{30} = 2 \text{ A}$$

$$i_{L2} = 0.4(2) = 0.8 \text{ A}$$

6-35

$$I_{L1} = I_S = \frac{V_o^2}{V_S R} = \frac{6^2}{15 \times 2} = 1.2 \text{ A}$$

$$D = \frac{V_o}{V_o + V_S} = \frac{6}{6 + 15} = 0.286, \quad L_1 = \frac{V_S D}{(\Delta i_{L1}) f} = \frac{15(0.286)}{0.4(1.2) \cdot 250000}$$

$$= 35.7 \mu\text{H}$$

$$I_{L2} = I_O = \frac{V_o}{R} = \frac{6}{2} = 3 \text{ A}$$

$$L_2 = \frac{V_S D}{(\Delta i_{L2}) f} = \frac{15(0.286)}{0.4(3)(250000)} = 14.3 \mu\text{H}, \quad V_{C2} = V_o = 6 \text{ V}$$

$$\Delta V_{C2} = \Delta V_o = \frac{V_o D}{R C_2 f} \quad \text{or} \quad C = \frac{D}{R \left(\frac{\Delta V_o}{V_o} \right) f} = \frac{0.286}{2(0.2) \cdot 250000} = 28.6 \mu\text{F}$$

$$\Rightarrow C_1 = C_2 = 28.6 \mu\text{F}$$

6-38

$$\text{if switch closed: } V_L = V_S - V_Q$$

$$\text{if switch open: } V_L = V_o - V_o$$

$$\text{avg}\{V_L\} = 0 : (V_S - V_Q)DT + (V_o - V_o)(1-D)T = 0$$

$$V_o = V_o - (V_S - V_Q) \frac{D}{1-D}$$