

<i>PresentState</i>	<i>I/P</i> = 0		<i>I/P</i> = 1	
	<i>NextState</i>	<i>O/P</i>	<i>NextState</i>	<i>O/P</i>
$q_20$	$q_11$	1	$q_21$	1
$q_21$	$q_11$	1	$q_21$	1
$q_3$	$q_20$	1	$q_0$	1

The converted Moore machine is

<i>State</i>	<i>NextState</i>		
	<i>I/P</i> = 0	<i>I/P</i> = 1	<i>O/P</i>
$\rightarrow q_0$	$q_0$	$q_10$	1
$q_10$	$q_3$	$q_3$	0
$q_11$	$q_3$	$q_3$	1
$q_20$	$q_11$	$q_21$	0
$q_21$	$q_11$	$q_21$	1
$q_3$	$q_20$	$q_0$	1

To get rid of the problem of occurrence of a null string, we need to include another state,  $q_a$ , with the same transactions as that of  $q_0$  but with output 0.

The modified final Moore machine equivalent to the given Mealy machine is

<i>State</i>	<i>NextState</i>		
	<i>I/P</i> = 0	<i>I/P</i> = 1	<i>O/P</i>
$\rightarrow q_a$	$q_0$	$q_10$	0
$q_0$	$q_0$	$q_10$	1
$q_10$	$q_3$	$q_3$	0
$q_11$	$q_3$	$q_3$	1
$q_20$	$q_11$	$q_21$	0
$q_21$	$q_11$	$q_21$	1
$q_3$	$q_20$	$q_0$	1

17. Convert the following Mealy Machine to a Moore Machine. [WBUT 2008]

<i>PresentState</i>	Next State $I/P = 0$		Next State $I/P = 1$	
	State	Output	State	Output
$Q_1$	$q_2$	1	$q_1$	0
$Q_2$	$q_3$	0	$q_4$	1
$Q_3$	$q_1$	0	$q_4$	0
$Q_4$	$q_3$	1	$q_2$	1

**Solution:**  $Q_3$  and  $Q_4$  as next states produce outputs 0 and 1, and so the states are divided into  $Q_30$ ,  $Q_31$  and  $Q_40$ ,  $Q_41$ . Thus, the constructing Moore machine contains six states. The Moore machine becomes

State	NextState		Output
	$I/P = 0$	$I/P = 1$	
$Q_1$	$Q_2$	$Q_1$	0
$Q_2$	$Q_30$	$Q_41$	1
$Q_30$	$Q_1$	$Q_40$	0
$Q_31$	$Q_1$	$Q_40$	1
$Q_40$	$Q_31$	$Q_2$	0
$Q_41$	$Q_31$	$Q_2$	1

18. From the following Mealy machine, find the equivalent Moore machine. Check whether the Mealy machine is a minimal one or not. Give proper justification to your answer. [WBUT 2007]

PresentState	$I/P = 0$		$I/P = 1$	
	NextState	O/P	NextState	O/P
$S_1$	$S_2$	0	$S_1$	0
$S_2$	$S_2$	0	$S_3$	0
$S_3$	$S_4$	0	$S_1$	0
$S_4$	$S_2$	0	$S_5$	0
$S_5$	$S_2$	0	$S_1$	1

**Solution:**

i) In the Mealy machine,  $S_1$  as the next state produces output 0 for some cases and produces output 1 for one case. For this reason, the state  $S_1$  is divided

into two parts:  $S_10$  and  $S_11$ . All the other states produce output 0.

To get rid of the problem of occurrence of a null string, we need to include another state,  $S_a$ , with the same transactions as that of  $S_10$  but with output 0.

The modified final Moore machine equivalent to the given Mealy machine will be as follows.

The converted Moore machine is

<i>State</i>	<i>NextState</i>		<i>Output</i>
	<i>I/P = 0</i>	<i>I/P = 1</i>	
$S_a$	$S_2$	$S_10$	0
$S_10$	$S_2$	$S_10$	0
$S_11$	$S_2$	$S_10$	1
$S_2$	$S_2$	$S_3$	0
$S_3$	$S_4$	$S_10$	0
$S_4$	$S_2$	$S_5$	0
$S_5$	$S_2$	$S_11$	0

ii) All the states are 0 equivalents.

$$P_0 = \{S_1S_2S_3S_4S_5\}$$

For string length 1, all the states produce output 0 except  $S_5$ .

$$P_1 = \{S_1S_2S_3S_4\}\{S_5\}$$

The next states of all the states (belong to the first subset) for all inputs belong to one set except  $S_4$ . The modified partition is

$$P_2 = \{S_1S_2S_3\}\{S_4\}\{S_5\}$$

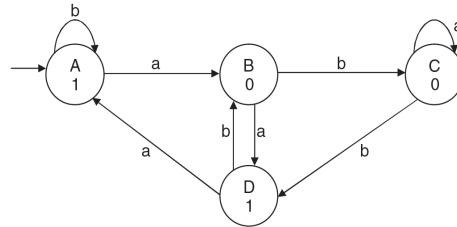
By this process,  $P_3 = \{S_1S_2\}\{S_3\}\{S_4\}\{S_5\}$

$$P_4 = \{S_1\}\{S_2\}\{S_3\}\{S_4\}\{S_5\}$$

The machine is a reduced machine as the number of subsets of the machine is the same as the number of states of the original Mealy machine. Hence, the machine is a minimal machine.

19. Convert the following Moore machine into an equivalent Mealy machine by the transitional format.

## 1 picture



### Solution:

i) In this machine, A is the beginning state. So start from A. For A, there are three incoming arcs, from A to A with input b, one in the form of start-state indication with no input, and the last is from D to A with input a. State A is labelled with output 1. As the start-state indication contains no input, it is useless and, therefore, keep it as it is.

Modify the label of the incoming edge from D to A and from A to A including the output of state A. So, the label of the incoming state will be D to A with label a/1 and A to A with label b/1.

ii) State B is labelled with output 0. The incoming edges to the state B are from A to B with input a and from D to B with input b.

Modify the labels of the incoming edges including the output of state B. So, the labels of the incoming states will be A to B with label a/0 and from D to B with label b/0.

iii) State C is labelled with output 0. There are two incoming edges to this state, from B to C with input b and from C to C with input a.

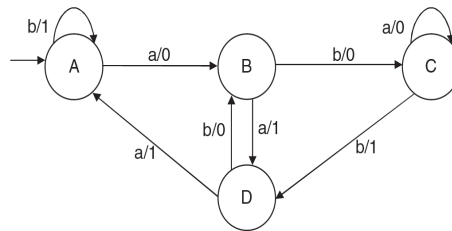
The modified label will be B to C with label b/0 and C to C with label a/0.

iv) State D is labelled with output 1. There are two incoming edges to this state, from B to D with input a and from C to D with input b.

The modified label will be B to D with label a/1, and C to D with label b/1.

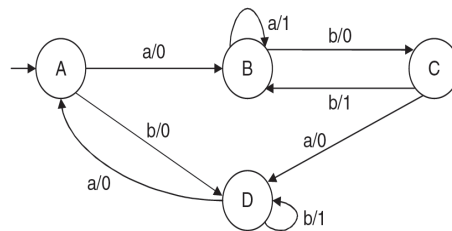
The converted Mealy machine will be

## 2 picture



20. Convert the following Mealy machine into an equivalent Moore machine by the transitional format.

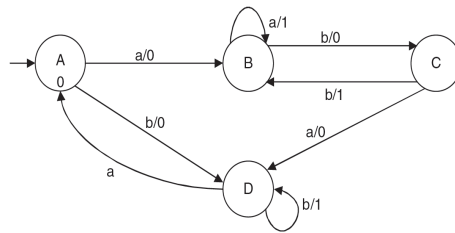
## 3 picture



**Solution:** The machine contains four states. Let us start from the state A. The incoming edges to this state are from D to A with label a/0. There is

no difference in the outputs of the incoming edges to this state, and so in the constructing Moore machine the output for this state will be 0.

## 4 picture



For the state B, the incoming edges are B to B with label a/1, from A to B with label a/0, and from C to B with label b/1.

We get two different outputs for two incoming edges (B to B output 1, A to B output 0). So, the state B will be divided into two, namely, B0 and B1. The outgoing edges are duplicated for both the states generated from B. The modified machine is