

5. Find the equivalent partition of the following machine.

Present State	Next State, z	
	$X = 0$	$X = 1$
A	C, 1	D, 0
B	D, 1	E, 0
C	B, 1	E, 1
D	B, 1	A, 0
E	D, 1	B, 1

Solution: The partitions are

$$P_0 = (ABCDEF)$$

$$P_1 = (AD)(BCE) \text{ (Depending on o/p for i/p 1)}$$

$$P_2 = (AD)(BE)(C) \text{ (For i/p 0, the next state of C goes to another set)}$$

$$P_3 = (A)(D)(BE)(C) \text{ (For i/p 0, the next state of A and D goes to a different set)}$$

$$P_4 = (A)(D)(BE)(C)$$

As P_3 and P_4 are the same, P_3 is the equivalent partition.

Minimization: We know that the equivalent partition is unique. So, $P_4 = (A)(D)(BE)(C)$ is the unique combination. Here, every single set represents one state of the minimized machine.

Let us rename these partitions for simplification.

Rename (A) as S_1 , (BE) as S_2 , (C) as S_3 , and (D) as S_4

The minimized machine becomes

Present State	Next State,z	
	$X = 0$	$X = 1$
$S_1(A)$	$S_3, 1$	$S_4, 1$
$S_2(BE)$	$S_4, 1$	$S_2, 0$
$S_3(C)$	$S_2, 1$	$S_2, 1$
$S_4(D)$	$S_2, 1$	$S_1, 0$

6, Simplify the following incompletely specified machine.

Present State	Next State,z		
	I_1	I_2	I_3
A	D, 1	E, 1	—
B	B, 0	E, -	C, -
C	C, —	C, 0	B, -
D	B, 0	D, -	E, -
E	—	B, 0	A, -

Solution: Put a temporary state T in the next state place, where the next states are not specified. If the output is not mentioned, there is no need to put any output.

As a temporary state T is considered, T is put in the present state column with the next state T for all inputs with no output.

The simplified machine becomes

Present State	Next State,z		
	I_1	I_2	I_3
A	D, 1	E, 1	T, -
B	B, 0	E, -	C, -
C	C, -	C, 0	B, -
D	B, 0	D, -	E, -
E	T, -	B, 0	A, -
T	T, 0	T, 0	T, 0