

bn_add.c (original)	bn_add.c (modified)
<pre>+-- 5 lines: Copyright 1995-2018 The OpenSSL Project Authors. All Rights * in the file LICENSE in the source distribution or at * https://www.openssl.org/source/license.html */  #include "internal/cryptlib.h" #include "bn_local.h"  ...  /* signed add of b to a. */ int BN_add(BIGNUM *r, const BIGNUM *a, const BIGNUM *b) {     int ret, r_neg, cmp_res;      ...      if (a-&gt;top &lt; b-&gt;top) {         const BIGNUM *tmp;          tmp = a;         a = b;         b = tmp;     }      r-&gt;top = max;      ap = a-&gt;d;     bp = b-&gt;d;     rp = r-&gt;d;      carry = bn_add_words(rp, ap, bp, min);      ...</pre>	<pre>+-- 5 lines: Copyright 1995-2018 The OpenSSL Project Authors. All Rights * in the file LICENSE in the source distribution or at * https://www.openssl.org/source/license.html */  #include "internal/cryptlib.h" #include "bn_local.h" #include "bn_par.h"  void *bn_add_sub_words_thread(void *ptr) {     BN_ULONG c;     add_sub_args *args = (add_sub_args *) ptr;      const BN_ULONG* ap = args-&gt;a;     const BN_ULONG* bp = args-&gt;b;     BN_ULONG* rp = args-&gt;r;     BN_ULONG min = args-&gt;n;      if (args-&gt;type == '+')         c = bn_add_words(rp, ap, bp, min);     else if (args-&gt;type == '-')         c = bn_sub_words(rp, ap, bp, min);      args-&gt;carry = c;     pthread_exit(NULL); }  void bn_resolve_carry (BN_ULONG carry, add_sub_args* arg) {     int i = 0;     BN_ULONG t;     while (carry &amp;&amp; i &lt; arg-&gt;n) {         t = arg-&gt;r[i];         t = (t + carry) &amp; BN_MASK2;         carry = (t &lt; carry);         arg-&gt;r[i] = t;         i++;     }     if(i == arg-&gt;n) {         arg-&gt;carry += carry;     } }  void bn_resolve_borrow (BN_ULONG borrow, add_sub_args* arg) {     int i = 0;     BN_ULONG t, t1, c = borrow;     while (c &amp;&amp; i &lt; arg-&gt;n) {         t = arg-&gt;r[i];         t1 = (t - c) &amp; BN_MASK2;         arg-&gt;r[i] = t1;          //check overflow         c = (t1 &gt; t);         i++;     }     if(i == arg-&gt;n) {         arg-&gt;carry += c;     } }  /* signed add of b to a. */ int BN_add(BIGNUM *r, const BIGNUM *a, const BIGNUM *b) {     int ret, r_neg, cmp_res;      ...      // a must be longer than b, if otherwise, swap     if (a-&gt;top &lt; b-&gt;top) {         const BIGNUM *tmp;          tmp = a;         a = b;         b = tmp;     }      r-&gt;top = max;      ap = a-&gt;d;     bp = b-&gt;d;     rp = r-&gt;d;      // thread init     pthread_t thr[NUM_THREADS];     int rc;      /* create a thread_data_t argument array */     add_sub_args thr_data[NUM_THREADS];      /* create threads, divide array */     int new_n = min/NUM_THREADS;     int l_idx = 0;      for (int i = 0; i &lt; NUM_THREADS; ++i) {         l_idx = new_n * i;         // printf("l_idx %d, h_idx %d\n", l_idx, l_idx + new_n);         thr_data[i].a = &amp;ap[l_idx];         thr_data[i].b = &amp;bp[l_idx];         thr_data[i].r = &amp;rp[l_idx];         thr_data[i].type = '+';          if (i == (NUM_THREADS - 1))             thr_data[i].n = new_n + min % NUM_THREADS;         else             ...</pre>

	<pre>         thr_data[i].n = new_n;          if ((rc = pthread_create(&amp;thr[i], NULL, bn_add_sub_words_thread, &amp;thr_data[i]),             fprintf(stderr, "error: pthread_create, rc: %d\n", rc);             return EXIT_FAILURE;         )      /* block until all threads complete */     for (int i = 0; i &lt; NUM_THREADS; ++i) {         pthread_join(thr[i], NULL);         // printf("t%d %d\n", i, thr_data[i].carry);     }      /* Resolve Carry */     BN_ULONG tmp_carry;     for (int i = 0; i &lt; NUM_THREADS - 1; ++i) {         tmp_carry = thr_data[i].carry;         bn_resolve_carry(tmp_carry, &amp;thr_data[i+1]);     }     carry = thr_data[NUM_THREADS-1].carry; </pre>
<pre>         rp += min;         ap += min;          while (dif) {             dif--;             t1 = *(ap++); +-- 32 lines: t2 = (t1 + carry) &amp; BN_MASK2;-----             return 0;          ap = a-&gt;d;         bp = b-&gt;d;         rp = r-&gt;d; </pre>	<pre>         rp += min;         ap += min;          while (dif) {             dif--;             t1 = *(ap++); +-- 32 lines: t2 = (t1 + carry) &amp; BN_MASK2;-----             return 0;          ap = a-&gt;d;         bp = b-&gt;d;         rp = r-&gt;d; </pre>
<pre>         borrow = bn_sub_words(rp, ap, bp, min); </pre>	<pre> // create threads pthread_t thr[NUM_THREADS]; int rc;  /* create a thread_data_t argument array */ add_sub_args thr_data[NUM_THREADS];  /* create threads, divide array */ int new_n = min/NUM_THREADS; int l_idx = 0;  for (int i = 0; i &lt; NUM_THREADS; ++i) {     l_idx = new_n * i;     // printf("l_idx %d, h_idx %d\n", l_idx, l_idx + new_n);     thr_data[i].a = &amp;ap[l_idx];     thr_data[i].b = &amp;bp[l_idx];     thr_data[i].r = &amp;rp[l_idx];     thr_data[i].type = '-';      if (i == (NUM_THREADS - 1))         thr_data[i].n = new_n + min % NUM_THREADS;     else         thr_data[i].n = new_n;      if ((rc = pthread_create(&amp;thr[i], NULL, bn_add_sub_words_thread, &amp;thr_data[i]),         fprintf(stderr, "error: pthread_create, rc: %d\n", rc);         return EXIT_FAILURE;     )  }  /* block until all threads complete */ for (int i = 0; i &lt; NUM_THREADS; ++i) {     pthread_join(thr[i], NULL);     // printf("t%d %d\n", i, thr_data[i].carry); }  /* Resolve Carry */ BN_ULONG tmp_carry; for (int i = 0; i &lt; NUM_THREADS - 1; ++i) {     tmp_carry = thr_data[i].carry;     bn_resolve_borrow(tmp_carry, &amp;thr_data[i+1]); } borrow = thr_data[NUM_THREADS-1].carry; </pre>
<pre>         ap += min;         rp += min;          while (dif) {             dif--;             t1 = *(ap++); +-- 8 lines: t2 = (t1 - borrow) &amp; BN_MASK2;-----             r-&gt;top = max;             r-&gt;neg = 0;             bn_pollute(r);              return 1;         } </pre>	<pre>         ap += min;         rp += min;          while (dif) {             dif--;             t1 = *(ap++); +-- 8 lines: t2 = (t1 - borrow) &amp; BN_MASK2;-----             r-&gt;top = max;             r-&gt;neg = 0;             bn_pollute(r);              return 1;         } </pre>

/tmp/yhdaSL_bn_asm.c	crypto/bn/bn_asm.c
<pre>+-- 7 lines: Copyright 1995-2016 The OpenSSL Project Authors. All Rights */  #include &lt;assert.h&gt; #include &lt;openssl/crypto.h&gt; #include "internal/cryptlib.h" #include "bn_local.h"  -----  #if defined(BN_LLONG)    defined(BN_UMULT_HIGH)  BN_ULONG bn_mul_add_words(BN_ULONG *rp, const BN_ULONG *ap, int num,                           BN_ULONG w) {     -----     BN_ULONG c1 = 0;      assert(num &gt;= 0);     if (num &lt;= 0)         return c1;  +-- 17 lines: # ifndef OPENSLL_SMALL_FOOTPRINT----- }  return c1;  BN_ULONG bn_mul_words(BN_ULONG *rp, const BN_ULONG *ap, int num, BN_ULONG {     -----     BN_ULONG c1 = 0;      assert(num &gt;= 0);     if (num &lt;= 0)         return c1;  +-- 42 lines: # ifndef OPENSLL_SMALL_FOOTPRINT----- }  }  #else                                /* !(defined(BN_LLONG)   * defined(BN_UMULT_HIGH)) */  BN_ULONG bn_mul_add_words(BN_ULONG *rp, const BN_ULONG *ap, int num,</pre>	<pre>+-- 7 lines: Copyright 1995-2016 The OpenSSL Project Authors. All Rights */  #include &lt;assert.h&gt; #include &lt;openssl/crypto.h&gt; #include "internal/cryptlib.h" #include "bn_local.h" #include "bn_par.h"  -----  #if defined(BN_LLONG)    defined(BN_UMULT_HIGH)  BN_ULONG bn_mul_add_words(BN_ULONG *rp, const BN_ULONG *ap, int num,                           BN_ULONG w) {     -----     //printf("a\n");     BN_ULONG c1 = 0;      assert(num &gt;= 0);     if (num &lt;= 0)         return c1;  +-- 17 lines: # ifndef OPENSLL_SMALL_FOOTPRINT----- }  return c1;  BN_ULONG bn_mul_words(BN_ULONG *rp, const BN_ULONG *ap, int num, BN_ULONG {     -----     //printf("ai\n");     BN_ULONG c1 = 0;      assert(num &gt;= 0);     if (num &lt;= 0)         return c1;  +-- 42 lines: # ifndef OPENSLL_SMALL_FOOTPRINT----- }  }  #else                                /* !(defined(BN_LLONG)   * defined(BN_UMULT_HIGH)) */  void bn_resolve_carry_mul(BN_ULONG carry, mul_normal_args* arg) {     int i = 0;     BN_ULONG t;     while (carry &amp;&amp; i &lt; arg-&gt;n) {         t = arg-&gt;r[i];         t = (t + carry) &amp; BN_MASK2;         carry = (t &lt; carry);         arg-&gt;r[i] = t;         i++;     }     if(i == arg-&gt;n) {         arg-&gt;carry += carry;     } }  void *bn_mul_add_words_thread(void *ptr) {     mul_normal_args *args = (mul_normal_args *) ptr;      const BN_ULONG* ap = args-&gt;a;     const BN_ULONG w = args-&gt;w;     BN_ULONG* rp = args-&gt;r;     int num = args-&gt;n;      // printf("num %d\n", num);     BN_ULONG c = 0;     BN_ULONG bl, bh;      bl = LBITS(w);     bh = HBITS(w);     # ifndef OPENSLL_SMALL_FOOTPRINT     while (num &amp; ~3) {         mul_add(rp[0], ap[0], bl, bh, c);         mul_add(rp[1], ap[1], bl, bh, c);         mul_add(rp[2], ap[2], bl, bh, c);         mul_add(rp[3], ap[3], bl, bh, c);         ap += 4;         rp += 4;         num -= 4;     }     # endif     while (num) {         mul_add(rp[0], ap[0], bl, bh, c);         ap++;         rp++;         num--;     }     args-&gt;carry = c;      pthread_exit(NULL); }  BN_ULONG bn_mul_add_words_par(BN_ULONG *rp, const BN_ULONG *ap, int num,                               BN_ULONG w) {     -----     //printf("b\n");     BN_ULONG carry = 0;      assert(num &gt;= 0);     if (num &lt;= 0)         return (BN_ULONG) 0;      pthread_t thr[NUM_THREADS];     int rc;</pre>

	<pre> /* create a thread_data_t argument array */ mul_normal_args thr_data[NUM_THREADS];  /* create threads, divide array */ int new_n = num/NUM_THREADS; int l_idx = 0; // printf("%lu\n", w); for (int i = 0; i &lt; NUM_THREADS; ++i) {     l_idx = new_n * i;     thr_data[i].a = &amp;ap[l_idx];     thr_data[i].w = w;     thr_data[i].r = &amp;rp[l_idx];      if (i == (NUM_THREADS - 1))         thr_data[i].n = new_n + num % NUM_THREADS;     else         thr_data[i].n = new_n;     // printf("tot %d n %d\n", num, thr_data[i].n);     if ((rc = pthread_create(&amp;thr[i], NULL, bn_mul_add_words_thread, &amp;thr_data[i])) != 0)         fprintf(stderr, "error: pthread_create, rc: %d\n", rc);     exit(EXIT_FAILURE); }  // printf("\n"); /* block until all threads complete */ for (int i = 0; i &lt; NUM_THREADS; ++i) {     pthread_join(thr[i], NULL);     // printf("t%d %d\n", i, thr_data[i].carry); }  /* Resolve Carry */ BN_ULONG tmp_carry; for (int i = 0; i &lt; NUM_THREADS - 1; ++i) {     tmp_carry = thr_data[i].carry;     bn_resolve_carry_mul(tmp_carry, &amp;thr_data[i+1]); } carry = thr_data[NUM_THREADS-1].carry;  return carry; } </pre>
<pre> BN_ULONG w) {     BN_ULONG c = 0;     BN_ULONG bl, bh;      assert(num &gt;= 0); +-- 20 lines: if (num &lt;= 0) -----     rp++;     num--; } return c; }  BN_ULONG bn_mul_words(BN_ULONG *rp, const BN_ULONG *ap, int num, BN_ULONG </pre>	<pre> BN_ULONG w) {     BN_ULONG c = 0;     BN_ULONG bl, bh;      assert(num &gt;= 0); +-- 20 lines: if (num &lt;= 0) -----     rp++;     num--; } return c; }  BN_ULONG bn_mul_add_words(BN_ULONG *rp, const BN_ULONG *ap, int num, BN_ULONG w) {     if (num &gt; BN_MUL_ADD_NUM_THRESHOLD) {         return bn_mul_add_words_par(rp, ap, num, w);     } else {         return bn_mul_add_words_original(rp, ap, num, w);     } }  void *bn_mul_words_thread(void *ptr) {     mul_normal_args *args = (mul_normal_args *) ptr;      const BN_ULONG* ap = args-&gt;a;     const BN_ULONG w = args-&gt;w;     BN_ULONG* rp = args-&gt;r;     int num = args-&gt;n;      BN_ULONG bl, bh, carry = 0;      bl = LBITS(w);     bh = HBITS(w);     // printf("w %lx, bh %lx, bl %lx\n", w, bh, bl);  #ifdef OPENSSSL_SMALL_FOOTPRINT     while (num &amp; ~3) {         mul(rp[0], ap[0], bl, bh, carry);         mul(rp[1], ap[1], bl, bh, carry);         mul(rp[2], ap[2], bl, bh, carry);         mul(rp[3], ap[3], bl, bh, carry);         ap += 4;         rp += 4;         num -= 4;     } #endif     while (num) {         mul(rp[0], ap[0], bl, bh, carry);         ap++;         rp++;         num--;     }      args-&gt;carry = carry;     pthread_exit(NULL); }  BN_ULONG bn_mul_words_par(BN_ULONG *rp, const BN_ULONG *ap, int num, BN_ULONG {     BN_ULONG carry = 0;      assert(num &gt;= 0);     if (num &lt;= 0)         return (BN_ULONG) 0; </pre>

	<pre> pthread_t thr[NUM_THREADS]; int rc;  /* create a thread_data_t argument array */ mul_normal_args thr_data[NUM_THREADS];  /* create threads, divide array */ int new_n = num/NUM_THREADS; int l_idx = 0;  for (int i = 0; i &lt; NUM_THREADS; ++i) {     l_idx = new_n * i;     thr_data[i].a = &amp;(ap[l_idx]);     thr_data[i].w = w;     thr_data[i].r = &amp;(rp[l_idx]);      if (i == (NUM_THREADS - 1))         thr_data[i].n = new_n + num % NUM_THREADS;     else         thr_data[i].n = new_n;     // printf("tot %d l_idx %d, h_idx %d\n", num, l_idx, l_idx + thr_n);     if ((rc = pthread_create(&amp;thr[i], NULL, bn_mul_words_thread, &amp;thr_data[i])) != 0)         fprintf(stderr, "error: pthread_create, rc: %d\n", rc);     exit(EXIT_FAILURE); }  // printf("\n"); /* block until all threads complete */ for (int i = 0; i &lt; NUM_THREADS; ++i) {     pthread_join(thr[i], NULL);     // printf("t%d %lx\n", i, thr_data[i].carry); }  /* Resolve Carry */ BN_ULONG tmp_carry; for (int i = 0; i &lt; NUM_THREADS - 1; ++i) {     tmp_carry = thr_data[i].carry;     bn_resolve_carry_mul(tmp_carry, &amp;thr_data[i+1]); } carry = thr_data[NUM_THREADS-1].carry;  return carry; } BN_ULONG bn_mul_words_original(BN_ULONG *rp, const BN_ULONG *ap, int num, </pre>
<pre> {     BN_ULONG carry = 0;     BN_ULONG bl, bh;      assert(num &gt;= 0);     if (num &lt;= 0) +-- 17 lines: return (BN_ULONG)0;-----         mul(rp[0], ap[0], bl, bh, carry);         ap++;         rp++;         num--;     }     return carry; }  void bn_sqr_words(BN_ULONG *r, const BN_ULONG *a, int n) {     assert(n &gt;= 0);     if (n &lt;= 0) +--868 lines: return;----- } </pre>	<pre> {     BN_ULONG carry = 0;     BN_ULONG bl, bh;      assert(num &gt;= 0);     if (num &lt;= 0) +-- 17 lines: return (BN_ULONG)0;-----         mul(rp[0], ap[0], bl, bh, carry);         ap++;         rp++;         num--;     }     return carry; }  BN_ULONG bn_mul_words(BN_ULONG *rp, const BN_ULONG *ap, int num, BN_ULONG w) {     if (num &gt; BN_MUL_NUM_THRESHOLD) {         return bn_mul_words_par(rp, ap, num, w);     } else {         return bn_mul_words_original(rp, ap, num, w);     } }  void bn_sqr_words(BN_ULONG *r, const BN_ULONG *a, int n) {     assert(n &gt;= 0);     if (n &lt;= 0) +--868 lines: return;----- } </pre>

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/tmp/FGsasW_bn_mul.c
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4 lines: Copyright 1995-2018 The OpenSSL Project Authors. All Rights
* this file except in compliance with the License. You can obtain a copy
* in the file LICENSE in the source distribution or at
* https://www.openssl.org/source/license.html
*/

#include <assert.h>
-----
#include "internal/cryptlib.h"
#include "bn_local.h"
-----
#if defined(OPENSSL_NO_ASM) || !defined(OPENSSL_BN_ASM_PART_WORDS)
/*
 * Here follows specialised variants of bn_add_words() and bn_sub_words()
 * They have the property performing operations on arrays of different size
 * The sizes of those arrays is expressed through cl, which is the common
 * length ( basically, min(len(a),len(b)) ), and dl, which is
 * the length of the result array.
 */
#ifdef BN_RECURSION
/*
 * Karatsuba recursive multiplication algorithm (cf. Knuth, The Art of
 * Computer Programming, Vol. 2)
 */
-----
pthread_mutex_t thr_count_lock;

void *bn_mul_recursive_thread(void *ptr) {
    recursive_args *args = (recursive_args *) ptr;
    BN_ULONG *r = args->r;
    BN_ULONG *a = args->a;
    BN_ULONG *b = args->b;
    int n2 = args->n2;
    int dna = args->dna;
    int dnb = args->dnb;
    BN_ULONG *t = args->t;
    int *used_thr = args->used_thr;

    bn_mul_recursive(r, a, b, n2, dna, dnb, t, used_thr);
    pthread_exit(NULL);
}

void *bn_mul_part_recursive_thread(void *ptr) {
    recursive_args *args = (recursive_args *) ptr;
    BN_ULONG *r = args->r;
    BN_ULONG *a = args->a;
    BN_ULONG *b = args->b;
    int n = args->n2;
    int tna = args->dna;
    int tnb = args->dnb;
    BN_ULONG *t = args->t;
    int *used_thr = args->used_thr;

    bn_mul_part_recursive(r, a, b, n, tna, tnb, t, used_thr);
    pthread_exit(NULL);
}

void start_mul_recursive_thread(pthread_t *thr, recursive_args *arg, BN_ULONG *r,
int rc;

pthread_mutex_lock(&thr_count_lock);
(*used_thr)++;
pthread_mutex_unlock(&thr_count_lock);
set_recursive_arg((*arg), r, a, b, n2, dna, dnb, tmp_thr, used_thr);

// printf("thread_created %d\n", *(arg->used_thr));
if ((rc = pthread_create(thr, NULL, bn_mul_recursive_thread, arg))) {
    fprintf(stderr, "error: pthread_create, rc: %d\n", rc);
    exit(EXIT_FAILURE);
} else {
    // printf("create%d success\n", *used_thr);
}
}

void start_mul_part_recursive_thread(pthread_t *thr, recursive_args *arg,
int rc;

pthread_mutex_lock(&thr_count_lock);
(*used_thr)++;
pthread_mutex_unlock(&thr_count_lock);
set_recursive_arg((*arg), r, a, b, n2, dna, dnb, tmp_thr, used_thr);

// printf("thread_created %d\n", *(arg->used_thr));
if ((rc = pthread_create(thr, NULL, bn_mul_part_recursive_thread, arg))) {
    fprintf(stderr, "error: pthread_create, rc: %d\n", rc);
    exit(EXIT_FAILURE);
} else {
    // printf("create%d success\n", *used_thr);
}
}

int get_used_thread(int* used_thr) {
    pthread_mutex_lock(&thr_count_lock);
    int u = *used_thr;
    pthread_mutex_unlock(&thr_count_lock);
    return u;
}

/*
 * r is 2*n2 words in size,
 * a and b are both n2 words in size.
 * n2 must be a power of 2.
 * We multiply and return the result.
 * t must be 2*n2 words in size
 * We calculate

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* a[0]*b[0]
* a[0]*b[0]+a[1]*b[1]+(a[0]-a[1])*(b[1]-b[0])
* a[1]*b[1]
-----
*/
/* dnX may not be positive, but n2/2+dnX has to be */
void bn_mul_recursive(BN_ULONG *r, BN_ULONG *a, BN_ULONG *b, int n2,
                     int dna, int dnb, BN_ULONG *t)
{
    int n = n2 / 2, c1, c2;
    int tna = n + dna, tnb = n + dnb;
    unsigned int neg, zero;
    BN_ULONG ln, lo, *p;

+-- 19 lines: # ifdef BN_MUL_COMBA-----
    if ((dna + dnb) < 0)
        memset(&r[2 * n2 + dna + dnb], 0,
               sizeof(BN_ULONG) * -(dna + dnb));

    return;
}
/* r=(a[0]-a[1])*(b[1]-b[0]) */
c1 = bn_cmp_part_words(a, &(a[n]), tna, n - tna);
c2 = bn_cmp_part_words(&(b[n]), b, tnb, tnb - n);
zero = neg = 0;
switch (c1 * 3 + c2) {
case -4:
    bn_sub_part_words(t, &(a[n]), a, tna, tna - n); /* - */
    bn_sub_part_words(&(t[n]), b, &(b[n]), tnb, n - tnb); /* - */
    break;
case -3:
    zero = 1;
    break;
case -2:
    bn_sub_part_words(t, &(a[n]), a, tna, tna - n); /* - */
    bn_sub_part_words(&(t[n]), &(b[n]), b, tnb, tnb - n); /* + */
    neg = 1;
    break;
case -1:
case 0:
case 1:
    zero = 1;
    break;
case 2:
    bn_sub_part_words(t, a, &(a[n]), tna, n - tna); /* + */
    bn_sub_part_words(&(t[n]), b, &(b[n]), tnb, n - tnb); /* - */
    neg = 1;
    break;
case 3:
    zero = 1;
    break;
case 4:
    bn_sub_part_words(t, a, &(a[n]), tna, n - tna);
    bn_sub_part_words(&(t[n]), &(b[n]), b, tnb, tnb - n);
    break;
}

# ifdef BN_MUL_COMBA
+-- 16 lines: if (n == 4 && dna == 0 && dnb == 0) { XXX: bn_mul_comba4 con
    bn_mul_comba8(r, a, b);
    bn_mul_comba8(&(r[n2]), &(a[n]), &(b[n]));
} else
/* BN_MUL_COMBA */
{
-----
    p = &(t[n2 * 2]);
    if (!zero)
        bn_mul_recursive(&(t[n2]), t, &(t[n]), n, 0, 0, p);
    else
-----
    memset(&(t[n2]), 0, sizeof(*t) * n2);
    bn_mul_recursive(r, a, b, n, 0, 0, p);
    bn_mul_recursive(&(r[n2]), &(a[n]), &(b[n]), n, dna, dnb, p);
-----
}

/*-

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* a[0]*b[0] a_low*b_low
* a[0]*b[0]+a[1]*b[1]+(a[0]-a[1])*(b[1]-b[0])
* a_low*b_low + a_high*b_high + (a_low-a_high)*(b_high-b_low)
* a[1]*b[1] a_high*b_high
-----
*/
/* dnX may not be positive, but n2/2+dnX has to be */
void bn_mul_recursive(BN_ULONG *r, BN_ULONG *a, BN_ULONG *b, int n2,
                     int dna, int dnb, BN_ULONG *t, int *used_thr)
{
    int n = n2 / 2, c1, c2;
    int tna = n + dna, tnb = n + dnb;
    unsigned int neg, zero;
    BN_ULONG ln, lo, *p;

+-- 19 lines: # ifdef BN_MUL_COMBA-----
    if ((dna + dnb) < 0)
        memset(&r[2 * n2 + dna + dnb], 0,
               sizeof(BN_ULONG) * -(dna + dnb));

    return;
}
/* r=(a[0]-a[1])*(b[1]-b[0]) */
c1 = bn_cmp_part_words(a, &(a[n]), tna, n - tna); // a[0] > a[1] ? 1
c2 = bn_cmp_part_words(&(b[n]), b, tnb, tnb - n); // b[1] > b[0] ? 1
zero = neg = 0;
switch (c1 * 3 + c2) {
case -4: // a[0] < a[1], b[1] < b[0]
    bn_sub_part_words(t, &(a[n]), a, tna, tna - n); /* - */
    bn_sub_part_words(&(t[n]), b, &(b[n]), tnb, n - tnb); /* - */
    break;
case -3: // a[0] < a[1], b[1] == b[0]
    zero = 1;
    break;
case -2: // a[0] < a[1], b[1] > b[0]
    bn_sub_part_words(t, &(a[n]), a, tna, tna - n); /* - */
    bn_sub_part_words(&(t[n]), &(b[n]), b, tnb, tnb - n); /* + */
    neg = 1;
    break;
case -1: // a[0] == a[1], b[1] < b[0]
case 0: // a[0] == a[1], b[1] == b[0]
case 1: // a[0] == a[1], b[1] > b[0]
    zero = 1;
    break;
case 2: // a[0] > a[1], b[1] < b[0]
    bn_sub_part_words(t, a, &(a[n]), tna, n - tna); /* + */
    bn_sub_part_words(&(t[n]), b, &(b[n]), tnb, n - tnb); /* - */
    neg = 1;
    break;
case 3: // a[0] > a[1], b[1] == b[0]
    zero = 1;
    break;
case 4: // a[0] > a[1], b[1] > b[0]
    bn_sub_part_words(t, a, &(a[n]), tna, n - tna);
    bn_sub_part_words(&(t[n]), &(b[n]), b, tnb, tnb - n);
    break;
}

# ifdef BN_MUL_COMBA
+-- 16 lines: if (n == 4 && dna == 0 && dnb == 0) { XXX: bn_mul_comba4 con
    bn_mul_comba8(r, a, b);
    bn_mul_comba8(&(r[n2]), &(a[n]), &(b[n]));
} else
/* BN_MUL_COMBA */
{
    pthread_t thr[3];
    recursive_args arg[3];
    int running_cnt = 0, rc;
    BN_ULONG * tp[3];
    p = &(t[n2 * 2]);
    if (!zero) {
        if (get_used_thread(used_thr) < NUM_THREADS) {
            tp[0] = (BN_ULONG *) calloc(n2*2, sizeof(BN_ULONG));
            start_mul_recursive_thread(&(thr[0]), &(arg[0]), &(t[n2]),
                                     running_cnt++);
        } else
            bn_mul_recursive(&(t[n2]), t, &(t[n]), n, 0, 0, p, used_thr);
    } else
        memset(&(t[n2]), 0, sizeof(*t) * n2);

    if (get_used_thread(used_thr) < NUM_THREADS) {
        tp[1] = (BN_ULONG *) calloc(n2*2, sizeof(BN_ULONG));
        start_mul_recursive_thread(&(thr[1]), &(arg[1]), r, a, b, n,
                                   running_cnt++);
    } else
        bn_mul_recursive(r, a, b, n, 0, 0, p, used_thr);

    if (get_used_thread(used_thr) < NUM_THREADS) {
        tp[2] = (BN_ULONG *) calloc(n2*2, sizeof(BN_ULONG));
        start_mul_recursive_thread(&(thr[2]), &(arg[2]), &(r[n2]), &(a[n]),
                                   &(b[n]), n, dna, dnb, p,
                                   running_cnt++);
    } else
        bn_mul_recursive(&(r[n2]), &(a[n]), &(b[n]), n, dna, dnb, p,
                           used_thr);

    /* block until all threads complete */
    // printf("running_cnt %d\n", running_cnt);
    for (int i = 0; i < running_cnt; i++) {
        // printf("i %d\n", i);
        if ((rc = pthread_join(thr[i], NULL))) {
            fprintf(stderr, "error: pthread_join, rc: %d\n", rc);
            exit(EXIT_FAILURE);
        } else {
            // printf("join%d success\n", i);
        }
        // printf("t%d %d\n", i, thr_data[i].carry);
        free(tp[i]);
    }
}

/*-

```

<pre> * t[32] holds (a[0]-a[1])*(b[1]-b[0]), c1 is the sign * r[10] holds (a[0]*b[0]) * r[32] holds (b[1]*b[1]) */  c1 = (int)(bn_add_words(t, r, &amp;(r[n2]), n2));  if (neg) { /* if t[32] is negative */     c1 -= (int)(bn_sub_words(&amp;(t[n2]), t, &amp;(t[n2]), n2)); } else {     /* Might have a carry */     c1 += (int)(bn_add_words(&amp;(t[n2]), &amp;(t[n2]), t, n2)); }  /*- * t[32] holds (a[0]-a[1])*(b[1]-b[0])+(a[0]*b[0])+(a[1]*b[1]) * r[10] holds (a[0]*b[0]) * r[32] holds (b[1]*b[1]) * c1 holds the carry bits */ c1 += (int)(bn_add_words(&amp;(r[n]), &amp;(r[n]), &amp;(t[n2]), n2)); </pre>	<pre> * t[n2] holds (a[0]-a[1])*(b[1]-b[0]), c1 is the sign * r[0] holds (a[0]*b[0]) * r[n2] holds (b[1]*b[1]) */  c1 = (int)(bn_add_words(t, r, &amp;(r[n2]), n2));  if (neg) { /* if t[n2] is negative */     c1 -= (int)(bn_sub_words(&amp;(t[n2]), t, &amp;(t[n2]), n2)); } else {     /* Might have a carry */     c1 += (int)(bn_add_words(&amp;(t[n2]), &amp;(t[n2]), t, n2)); }  /*- * t[n2] holds (a[0]-a[1])*(b[1]-b[0])+(a[0]*b[0])+(a[1]*b[1]) * r[0] holds (a[0]*b[0]) * r[n2] holds (b[1]*b[1]) * c1 holds the carry bits */ c1 += (int)(bn_add_words(&amp;(r[n]), &amp;(r[n]), &amp;(t[n2]), n2)); </pre>
<pre> // resolve carry on r[n + n2] to last elmt if (c1) {     p = &amp;(r[n + n2]);     lo = *p;     ln = (lo + c1) &amp; BN_MASK2;     *p = ln; </pre>	<pre> // resolve carry on r[n + n2] to last elmt if (c1) {     p = &amp;(r[n + n2]);     lo = *p;     ln = (lo + c1) &amp; BN_MASK2;     *p = ln; </pre>
<pre> +-- 14 lines: The overflow will stop before we over write words we should </pre>	<pre> +-- 14 lines: The overflow will stop before we over write words we should </pre>
<pre> /* * n+tn is the word length t needs to be n*4 is size, as does r */ /* tnX may not be negative but less than n */ void bn_mul_part_recursive(BN_ULONG *r, BN_ULONG *a, BN_ULONG *b, int n,                            int tna, int tnb, BN_ULONG *t) {     int i, j, n2 = n * 2;     int c1, c2, neg;     BN_ULONG ln, lo, *p;      if (n &lt; 8) { +-- 45 lines: bn_mul_normal(r, a, n + tna, b, n + tnb);-----     if (n == 8) {         bn_mul_comba8(&amp;(t[n2]), t, &amp;(t[n]));         bn_mul_comba8(r, a, b);         bn_mul_normal(&amp;(r[n2]), &amp;(a[n]), tna, &amp;(b[n]), tnb);         memset(&amp;(r[n2 + tna + tnb]), 0, sizeof(*r) * (n2 - tna - tnb));     } else {          p = &amp;(t[n2 * 2]);         bn_mul_recursive(&amp;(t[n2]), t, &amp;(t[n]), n, 0, 0, p);         bn_mul_recursive(r, a, b, n, 0, 0, p);          i = n / 2;         /*         * If there is only a bottom half to the number, just do it         */         if (tna &gt; tnb)             j = tna - i;         else             j = tnb - i;         if (j == 0) {             bn_mul_recursive(&amp;(r[n2]), &amp;(a[n]), &amp;(b[n]),                             i, tna - i, tnb - i, p);              memset(&amp;(r[n2 + i * 2]), 0, sizeof(*r) * (n2 - i * 2));         } else if (j &gt; 0) { /* eg, n == 16, i == 8 and tn == 11 */             bn_mul_part_recursive(&amp;(r[n2]), &amp;(a[n]), &amp;(b[n]),                                 i, tna - i, tnb - i, p);              memset(&amp;(r[n2 + tna + tnb]), 0,                     sizeof(BN_ULONG) * (n2 - tna - tnb));         } else { /* (j &lt; 0) eg, n == 16, i == 8 and tn == 9 */             memset(&amp;(r[n2]), 0, sizeof(*r) * n2);             if (tna &lt; BN_MUL_RECURSIVE_SIZE_NORMAL +-- 4 lines: &amp;&amp; tnb &lt; BN_MUL_RECURSIVE_SIZE_NORMAL) {-----                 i /= 2;                 /*                 * these simplified conditions work exclusively because                 * difference between tna and tnb is 1 or 0                 */ </pre>	<pre> /* * n+tn is the word length t needs to be n*4 is size, as does r */ /* tnX may not be negative but less than n */ void bn_mul_part_recursive(BN_ULONG *r, BN_ULONG *a, BN_ULONG *b, int n,                            int tna, int tnb, BN_ULONG *t, int *used_thr) {     int i, j, n2 = n * 2;     int c1, c2, neg;     BN_ULONG ln, lo, *p;      if (n &lt; 8) { +-- 45 lines: bn_mul_normal(r, a, n + tna, b, n + tnb);-----     if (n == 8) {         bn_mul_comba8(&amp;(t[n2]), t, &amp;(t[n]));         bn_mul_comba8(r, a, b);         bn_mul_normal(&amp;(r[n2]), &amp;(a[n]), tna, &amp;(b[n]), tnb);         memset(&amp;(r[n2 + tna + tnb]), 0, sizeof(*r) * (n2 - tna - tnb));     } else {         pthread_t thr[3];         recursive_args arg[3];         int running_cnt = 0, rc;         BN_ULONG* tp[3];         p = &amp;(t[n2 * 2]);          if (get_used_thread(used_thr) &lt; NUM_THREADS) {             tp[0] = (BN_ULONG *) calloc(n2*4, sizeof(BN_ULONG));             start_mul_recursive_thread(&amp;(thr[0]), &amp;(arg[0]), &amp;(t[n2]), t,                                      running_cnt++);         } else             bn_mul_recursive(&amp;(t[n2]), t, &amp;(t[n]), n, 0, 0, p, used_thr);          if (get_used_thread(used_thr) &lt; NUM_THREADS) {             tp[1] = (BN_ULONG *) calloc(n2*4, sizeof(BN_ULONG));             start_mul_recursive_thread(&amp;(thr[1]), &amp;(arg[1]), r, a, b, n,                                      running_cnt++);         } else             bn_mul_recursive(r, a, b, n, 0, 0, p, used_thr);          i = n / 2;         /*         * If there is only a bottom half to the number, just do it         */         if (tna &gt; tnb)             j = tna - i;         else             j = tnb - i;         if (j == 0) {             if (get_used_thread(used_thr) &lt; NUM_THREADS) {                 tp[2] = (BN_ULONG *) calloc(n2*2, sizeof(BN_ULONG));                 start_mul_recursive_thread(&amp;(thr[2]), &amp;(arg[2]), &amp;(r[n2]),  i, tna - i, tnb - i, tp[2], used_thr);                 running_cnt++;             } else                 bn_mul_recursive(&amp;(r[n2]), &amp;(a[n]), &amp;(b[n]),                                 i, tna - i, tnb - i, p, used_thr);             memset(&amp;(r[n2 + i * 2]), 0, sizeof(*r) * (n2 - i * 2));         } else if (j &gt; 0) { /* eg, n == 16, i == 8 and tn == 11 */             if (get_used_thread(used_thr) &lt; NUM_THREADS) {                 tp[2] = (BN_ULONG *) calloc(n2*2, sizeof(BN_ULONG));                 start_mul_recursive_thread(&amp;(thr[2]), &amp;(arg[2]), &amp;(r[n2]),  i, tna - i, tnb - i, tp[2], used_thr);                 running_cnt++;             } else                 bn_mul_recursive(&amp;(r[n2]), &amp;(a[n]), &amp;(b[n]),                                 i, tna - i, tnb - i, p, used_thr);             memset(&amp;(r[n2 + tna + tnb]), 0,                     sizeof(BN_ULONG) * (n2 - tna - tnb));         } else { /* (j &lt; 0) eg, n == 16, i == 8 and tn == 9 */             memset(&amp;(r[n2]), 0, sizeof(*r) * n2);             if (tna &lt; BN_MUL_RECURSIVE_SIZE_NORMAL +-- 4 lines: &amp;&amp; tnb &lt; BN_MUL_RECURSIVE_SIZE_NORMAL) {-----                 i /= 2;                 /*                 * these simplified conditions work exclusively because                 * difference between tna and tnb is 1 or 0                 */ </pre>



```

        if (i < tna || i < tnb) {
            bn_mul_part_recursive(&(r[n2]),
                                &(a[n]), &(b[n]),
                                i, tna - i, tnb - i, p);
        }

        break;
    } else if (i == tna || i == tnb) {
        bn_mul_recursive(&(r[n2]),
                        &(a[n]), &(b[n]),
                        i, tna - i, tnb - i, p);
    }

    break;
}

}

}

/*
 * t[32] holds (a[0]-a[1])*(b[1]-b[0]), c1 is the sign
 * r[10] holds (a[0]*b[0])
 * r[32] holds (b[1]*b[1])
+-- 41 lines: -----
 * r needs to be n2 words and t needs to be n2*2
 */
void bn_mul_low_recursive(BN_ULONG *r, BN_ULONG *a, BN_ULONG *b, int n2,
                        BN_ULONG *t)
{
    int n = n2 / 2;

    bn_mul_recursive(r, a, b, n, 0, 0, &(t[0]));
    if (n >= BN_MUL_LOW_RECURSIVE_SIZE_NORMAL) {
        bn_mul_low_recursive(&(t[0]), &(a[0]), &(b[n]), n, &(t[n2]));
        bn_add_words(&(r[n]), &(r[n]), &(t[0]), n);
        bn_mul_low_recursive(&(t[0]), &(a[n]), &(b[0]), n, &(t[n2]));
        bn_add_words(&(r[n]), &(r[n]), &(t[0]), n);
    } else {
+-- 47 lines: bn_mul_low_normal(&(t[0]), &(a[0]), &(b[n]), n);-----
        goto err;
    } else
        rr = r;

#ifdef BN_MUL_COMBA || defined(BN_RECURSION)
    i = al - bl;
    -----
#endif
#ifdef BN_MUL_COMBA
    if (i == 0) {
# if 0
        if (al == 4) {
            if (bn_wexpand(rr, 8) == NULL)
                goto err;
            rr->top = 8;
            bn_mul_comba4(rr->d, a->d, b->d);
            goto end;
        }
    }
# endif

    if (al == 8) {
        if (bn_wexpand(rr, 16) == NULL)
            goto err;
        rr->top = 16;
        bn_mul_comba8(rr->d, a->d, b->d);
        goto end;
    }
}

#endif /* BN_MUL_COMBA */
#ifdef BN_RECURSION
    if ((al >= BN_MULL_SIZE_NORMAL) && (bl >= BN_MULL_SIZE_NORMAL)) {
        if (i >= -1 && i <= 1) {
            -----
            /*
             * Find out the power of two lower or equal to the longest of
             * two numbers
             */
            if (i >= 0) {
                j = BN_num_bits_word((BN_ULONG)al);
            }
            if (i == -1) {
                j = BN_num_bits_word((BN_ULONG)bl);
            }
            j = 1 << (j - 1);
            -----

```

```

        if (i < tna || i < tnb) {
            if (get_used_thread(used_thr) < NUM_THREADS) {
                tp[2] = (BN_ULONG *) calloc(n2*2, sizeof(BN_ULONG));
                start_mul_part_recursive_thread(&(thr[2]), &(a[n]), &(b[n]),
                                                i, tna - i, tnb - i, tp[2], &(used_thr));
                running_cnt++;
            } else
                bn_mul_part_recursive(&(r[n2]),
                                    &(a[n]), &(b[n]),
                                    i, tna - i, tnb - i, p, used_thr);
        }

        break;
    } else if (i == tna || i == tnb) {
        if (get_used_thread(used_thr) < NUM_THREADS) {
            tp[2] = (BN_ULONG *) calloc(n2*2, sizeof(BN_ULONG));
            start_mul_recursive_thread(&(thr[2]), &(a[n]), &(b[n]),
                                      i, tna - i, tnb - i, tp[2], &(used_thr));
            running_cnt++;
        } else
            bn_mul_recursive(&(r[n2]),
                            &(a[n]), &(b[n]),
                            i, tna - i, tnb - i, p, used_thr);
    }

    break;
}

}

}

/* block until all threads complete */
// printf("running_cnt %d\n", running_cnt);
for (int i = 0; i < running_cnt; i++) {
    // printf("i %d\n", i);
    if ((rc = pthread_join(thr[i], NULL))) {
        fprintf(stderr, "error: pthread_join, rc: %d\n", rc);
        exit(EXIT_FAILURE);
    } else {
        // printf("join %d success\n", i);
    }
    // printf("t %d %d\n", i, thr_data[i].carry);
    free(tp[i]);
}

}

/*
 * t[32] holds (a[0]-a[1])*(b[1]-b[0]), c1 is the sign
 * r[10] holds (a[0]*b[0])
 * r[32] holds (b[1]*b[1])
+-- 41 lines: -----
 * r needs to be n2 words and t needs to be n2*2
 */
void bn_mul_low_recursive(BN_ULONG *r, BN_ULONG *a, BN_ULONG *b, int n2,
                        BN_ULONG *t)
{
    int n = n2 / 2;
    int u = 99;
    bn_mul_recursive(r, a, b, n, 0, 0, &(t[0]), &u);
    if (n >= BN_MUL_LOW_RECURSIVE_SIZE_NORMAL) {
        bn_mul_low_recursive(&(t[0]), &(a[0]), &(b[n]), n, &(t[n2]));
        bn_add_words(&(r[n]), &(r[n]), &(t[0]), n);
        bn_mul_low_recursive(&(t[0]), &(a[n]), &(b[0]), n, &(t[n2]));
        bn_add_words(&(r[n]), &(r[n]), &(t[0]), n);
    } else {
+-- 47 lines: bn_mul_low_normal(&(t[0]), &(a[0]), &(b[n]), n);-----
        goto err;
    } else
        rr = r;

#ifdef BN_MUL_COMBA || defined(BN_RECURSION)
    i = al - bl;
    // printf("i %d, al %d, bl %d\n", i, al, bl);
    -----
#endif
#ifdef BN_MUL_COMBA
    if (i == 0) {
# if 0
        if (al == 4) {
            if (bn_wexpand(rr, 8) == NULL)
                goto err;
            rr->top = 8;
            bn_mul_comba4(rr->d, a->d, b->d);
            goto end;
        }
    }
# endif

    // printf("comba\n");
    if (al == 8) {
        if (bn_wexpand(rr, 16) == NULL)
            goto err;
        rr->top = 16;
        bn_mul_comba8(rr->d, a->d, b->d);
        goto end;
    }
}

#endif /* BN_MUL_COMBA */
#ifdef BN_RECURSION
    if ((al >= BN_MULL_SIZE_NORMAL) && (bl >= BN_MULL_SIZE_NORMAL)) {
        if (i >= -1 && i <= 1) {
            // printf("recursion\n");
            -----
            /*
             * Find out the power of two lower or equal to the longest of
             * two numbers
             */
            if (i >= 0) {
                j = BN_num_bits_word((BN_ULONG)al);
            }
            if (i == -1) {
                j = BN_num_bits_word((BN_ULONG)bl);
            }
            j = 1 << (j - 1);
            // printf("j %d\n", j);
            -----

```

```

assert(j <= al || j <= bl);
k = j + j;
t = BN_CTX_get(ctx);
if (t == NULL)
    goto err;
if (al > j || bl > j) {
    if (bn_wexpand(t, k * 4) == NULL)
        goto err;
    if (bn_wexpand(rr, k * 4) == NULL)
        goto err;
    bn_mul_part_recursive(rr->d, a->d, b->d,
                          j, al - j, bl - j, t->d);
} else { /* al <= j || bl <= j */

    if (bn_wexpand(t, k * 2) == NULL)
        goto err;
    if (bn_wexpand(rr, k * 2) == NULL)
        goto err;
    bn_mul_recursive(rr->d, a->d, b->d, j, al - j, bl - j, t->d);

    rr->top = top;
    goto end;
}
}
#endif /* BN_RECURSION */
if (bn_wexpand(rr, top) == NULL)
    goto err;
rr->top = top;

bn_mul_normal(rr->d, a->d, al, b->d, bl);

#if defined(BN_MUL_COMBA) || defined(BN_RECURSION)
end:
#endif
rr->neg = a->neg ^ b->neg;
+-- 9 lines: rr->flags |= BN_FLG_FIXED_TOP;-----
}

void bn_mul_normal(BN_ULONG *r, BN_ULONG *a, int na, BN_ULONG *b, int nb)
{
    BN_ULONG *rr;

    if (na < nb) {
        int itmp;
        BN_ULONG *ltmp;

        itmp = na;
        na = nb;
+-- 53 lines: nb = itmp;-----
    }

```

```

assert(j <= al || j <= bl);
k = j + j;
t = BN_CTX_get(ctx);
if (t == NULL)
    goto err;
if (al > j || bl > j) {
    // printf("mul-part-rec\n");
    if (bn_wexpand(t, k * 4) == NULL)
        goto err;
    if (bn_wexpand(rr, k * 4) == NULL)
        goto err;

    int used_thread = 1;
    bn_mul_part_recursive(rr->d, a->d, b->d,
                          j, al - j, bl - j, t->d, &used_thread);
} else { /* al <= j && bl <= j */
    // al or bl is exactly the power of two
    if (bn_wexpand(t, k * 2) == NULL)
        goto err;
    if (bn_wexpand(rr, k * 2) == NULL)
        goto err;

    int used_thread = 1;
    bn_mul_recursive(rr->d, a->d, b->d, j, al - j, bl - j, t->d, &used_thread);

    rr->top = top;
    goto end;
}
}
#endif /* BN_RECURSION */
if (bn_wexpand(rr, top) == NULL)
    goto err;
rr->top = top;
// printf("normal\n");
bn_mul_normal(rr->d, a->d, al, b->d, bl);

#if defined(BN_MUL_COMBA) || defined(BN_RECURSION)
end:
#endif
rr->neg = a->neg ^ b->neg;
+-- 9 lines: rr->flags |= BN_FLG_FIXED_TOP;-----
}

void bn_mul_normal(BN_ULONG *r, BN_ULONG *a, int na, BN_ULONG *b, int nb)
{
    BN_ULONG *rr;

    // a must be longer than b, switch if otherwise
    if (na < nb) {
        int itmp;
        BN_ULONG *ltmp;

        itmp = na;
        na = nb;
+-- 53 lines: nb = itmp;-----
    }

```