Tutorial 2

COMP 355: Introduction to Theoretical Computer Science

Mohammad Reza Davari

Concordia University



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Outline

1 Languages

2 DFA



Contents of the section

Languages

2 DFA



Operations

Let
$$\Sigma = \{0,1\}$$

Example 1: Σ^1



Operations

Let
$$\Sigma = \{0,1\}$$

Example 1:
$$\Sigma^1 = \{0,1\}$$



Operations

Let $\Sigma = \{0, 1\}$

Example 1: $\Sigma^1 = \{0,1\}$

Example 2: Σ^2



Operations

Let
$$\Sigma = \{0,1\}$$

Example 1:
$$\Sigma^1 = \{0, 1\}$$

Example 2:
$$\Sigma^2 = \{00, 01, 10, 11\}$$



Operations

```
Let \Sigma = \{0, 1\}
```

Example 1: $\Sigma^1 = \{0, 1\}$

Example 2: $\Sigma^2 = \{00, 01, 10, 11\}$

Example 3: |01|



Operations

```
Let \Sigma = \{0, 1\}
```

Example 1: $\Sigma^1 = \{0, 1\}$

Example 2: $\Sigma^2 = \{00, 01, 10, 11\}$

Example 3: |01| = 2



Operations

```
Let \Sigma = \{0, 1\}
```

Example 1: $\Sigma^1 = \{0, 1\}$

Example 2: $\Sigma^2 = \{00, 01, 10, 11\}$

Example 3: |01| = 2

Example 4: $|\epsilon|$



Operations

```
Let \Sigma = \{0,1\}
```

Example 1:
$$\Sigma^1 = \{0, 1\}$$

Example 2:
$$\Sigma^2 = \{00, 01, 10, 11\}$$

Example 3:
$$|01| = 2$$

Example 4:
$$|\epsilon| = 0$$



Concatenation

Let x = 01101 and y = 110, then:



1 xy



Concatenation

Let x = 01101 and y = 110, then:

$$y = 01101110$$



Concatenation

Let x = 01101 and y = 110, then:

- y = 01101110
- 2 yx



Concatenation

Let x = 01101 and y = 110, then:

- y = 01101110
- yx = 11001101



Language

Example 1: The language of all words consisting of n 0's followed by n 1's, for some n > 0:



Language

Example 1: The language of all words consisting of n 0's followed by n 1's, for some $n \ge 0$: $\{\epsilon, 01, 0011, 000111, \dots\}$



Language

Example 1: The language of all words consisting of n 0's followed by n 1's, for some $n \ge 0$: $\{\epsilon, 01, 0011, 000111, \dots\}$

Example 2: The empty language:



Language

Example 1: The language of all words consisting of n 0's followed by n 1's, for some $n \ge 0$: $\{\epsilon, 01, 0011, 000111, \dots\}$

Example 2: The empty language: \emptyset



Language

- Example 1: The language of all words consisting of n 0's followed by n 1's, for some $n \ge 0$: $\{\epsilon, 01, 0011, 000111, \dots\}$
- Example 2: The empty language: \emptyset
- Example 3: The language consisting of only the empty string:



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Language

- Example 1: The language of all words consisting of n 0's followed by n 1's, for some $n \ge 0$: $\{\epsilon, 01, 0011, 000111, \dots\}$
- Example 2: The empty language: \emptyset
- Example 3: The language consisting of only the empty string: $\{\epsilon\}$



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Contents of the section

1 Languages

2 DFA



Example 1

For the following DFA determine:

• The alphabet set.



Example 1

For the following DFA determine:

- The alphabet set.
- Its transition table.



Example 1

For the following DFA determine:

- The alphabet set.
- Its transition table.
- Its Language.



Example 1

For the following DFA determine:

- The alphabet set.
- Its transition table.
- Its Language.

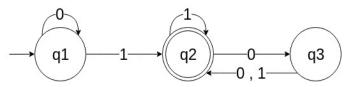


Figure: Example 1 DFA



Example 2

Build a DFA that identifies the non-negative multiples of 3.

• What is the set of alphabet?



Example 2

Build a DFA that identifies the non-negative multiples of 3.

- What is the set of alphabet?
- What is the transition diagram?



Example 2

Build a DFA that identifies the non-negative multiples of 3.

- What is the set of alphabet?
- What is the transition diagram?
- What is the transition table?



Example 3

Build a DFA that identifies the non-negative multiples of 5.

• What is the set of alphabet?



Example 3

Build a DFA that identifies the non-negative multiples of 5.

- What is the set of alphabet?
- What is the transition diagram?



Example 3

Build a DFA that identifies the non-negative multiples of 5.

- What is the set of alphabet?
- What is the transition diagram?
- What is the transition table?



Example 4

Build a DFA that identifies the non-negative powers of 2.

• What is the set of alphabet?



Example 4

Build a DFA that identifies the non-negative powers of 2.

- What is the set of alphabet?
- What is the transition diagram?



Example 4

Build a DFA that identifies the non-negative powers of 2.

- What is the set of alphabet?
- What is the transition diagram?
- What is the transition table?



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