```lua
#!/usr/bin/env lua
-- vim : ft=lua et sts=2 sw=2 ts=2 :
-- ---------------------------------------------------------------------------
--      __                                         __
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--
-- keys0: understand "N" items by peeking at at few (maybe zero) items.
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-- ---------------------------------------------------------------------------

local your = {} -- user settings (may be changes from command-line)
local our  = {} -- system settings (controlled internal to code)
our.help   = [[

./keys0 [OPTIONS]
Understand "N" items by peeking at at few (maybe zero) items.
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  -ample  max items in a 'SAMPLE'       : 512
  -better prune best half of each split : true
  -Debug  one crash, show stackdump     : true
  -dull   small effect if 'dull'*sd     : .35
  -far    for far,  skip after 'far'    : .9
  -file   load data from file           : ../../data/auto93.csv
  -h      show help                     : false
  -goal   smile,frown,xplor, doubt      : smile
  -p      coefficient on distance calcs : 2
  -round  round numbers to 'round'      : 2
  -seed   random number seed            : 10019
  -Some   max number items to explore   : 512
  -Tiny   bin size = #t^'Tiny'          : .5
  -todo   start up action ('all'=every) : -]]

our.b4={}        -- globals known, pre-code. used to find stray globals
for k,_ in pairs(_ENV) do our.b4[k]=k end

local add, any, asserts,coerce, col, copy, csv, defaults, dist
local firsts, fmt, klass, map, main, new,o, push, rand, randi, rnd, rnds
local same, seconds, slots, sort, xpects

function klass(s, it)
  it = {_is=s, __tostring=o}
  it.__index = it
  return setmetatable(it,{__call=function(_,...) return it.new(...) end}) end

local COLS,EG,EGS   = klass"COLS", klass"EG", klass"EGS"
local NUM,RANGE,SAMPLE,SYM = klass"NUM", klass"RANGE", klass"SAMPLE", klass"SYM"

-- TODO:
-- - resorvoir sampler
-- - r.s. added to num
-- - mergabel numbers
-- - add :add(x,y) to range. updates an N
-- - add :div() to range (so now xpect works for those as well)

----------------------------------------------------------------------------
local SAMPLE=klass"SAMPLE"
function SAMPLE.new() return new(SAMPLE,{n=0, all={}, max=your.ample}) end

function SAMPLE.add(i,x,     pos)
  i.n= i.n + 1
  if     #i.all < i.max      then pos= #i.all + 1
  elseif rand() < #i.all/i.n then pos= #i.all * rand() end
  if pos then i.all[pos//1]= x end end

----------------------------------------------------------------------------
function NUM.new(at,s,   i)
  i= new(NUM,{n=0,at=at or 0, txt=s or "",_has=SAMPLE(),
            mu=0,m2=0,lo=math.huge,hi=-math.huge})
  i.w = i.txt:find"-" and -1 or 1
  return i end

function NUM.add(i,x,  d)
  if x~="?" then
    i.n  = i.n + 1
    d    = x    - i.mu
    i.mu = i.mu + d/i.n
    i.m2 = i.m2 + d*(x-i.mu)
    i.has:add(x)
    i.lo = math.min(i.lo,x); i.hi = math.max(i.hi,x) end
  return x end

function NUM.dist(i,x,y)
  if     x=="?" and y=="?" then return 1
  elseif x=="?"            then y= i:norm(y); x=y>.5 and 0 or 1
  elseif y=="?"            then x= i:norm(x); y=x>.5 and 0 or 1
  else   x,y = i:norm(x), i:norm(y) end
  return math.abs(x-y) end

function NUM.div(i) return i.n<2 and 0 or (i.m2/(i.n-1))^0.5 end

function NUM.merged(i,j)
  k= NUM(i.at, i.txt)
  for _,x in pairs(i._has,all) do k:add(x) end
  for _,x in pairs(j._has.akk) do k:add(x) end
  return k end

function NUM.mid(i) return i.mu end

function NUM.norm(i,x) return i.hi-i.lo<1E-9 and 0 or (x-i.lo)/(i.hi-i.lo) end

function NUM.ranges(i,j, yklass)
  local xys, dull, tiny, range,out
  yklass = yklass or SYM
  xys    = {}
  for _,x in pairs(i._has.all) do push(xys, {x=x, y="best"}) end
  for _,x in pairs(j,_has.all) do push(xys, {x=x, y="rest"}) end
  xys    = sort(xys, function(a,b) return a.x < b.x end)
  dull   = xpects{i,j}*your.dull
  tiny   = (#xys)^your.Tiny
  range  = RANGE(i,xys[1].x, xys[1].x, yklass())
  out = {range}
  for k,xy in pairs(xys) do
    if   k < #xys - tiny    and xy.x ~= xys[k+1].x and
         range.has.n > tiny and range.hi - range.lo > dull
    then range = push(out, RANGE(i, range.hi, xy.x, yklass()))
    end
    range:add(xy.x, xy.y) end
  out[1].lo       = -math.huge
  out[#ranges].hi =  math.huge
  return out end

function NUM.superRanges(i,b4)
  local j,tmp,now,after,maybe = 0, {}
  while j < #b4 do
    j = j + 1
    now, after = b4[j], b4[j+1]
    if after then
      maybe = now:merge(after)
      if maybe then now=maybe; j=j+1 end end
    push(tmp,now) end
  return #tmp==#b4 and b4 or i:superRanges(tmp) end

----------------------------------------------------------------------------
function SYM.new(at,s)
  return new(SYM,{n=0, at=at or 0, txt=s or "", has={}, most=0, mode=nil}) end

function SYM.add(i,x,count)
  count = count or 1
  i.has[x] = count + (i.has[x] or 0)
  if i.has[x] > i.most then i.most,i.mode = i.has[x], x end
  return x end

function SYM.dist(i,x,y) return x=="?" and y=="?" and 1 or x==y and 0 or 1 end

function SYM.div(i,   e)
  e=0; for _,n in pairs(i.has) do e=e-n/i.n*math.log(n/i.n,2) end; return e end

function SYM.merged(i,j,     k)
  k= SYM(i.at, i.txt)
  for x,count in pairs(i.has) do k:add(x,count) end
  for x,count in pairs(j.has) do k:add(x,count) end
  return k end

function SYM.mid(i) return i.mode end

function SYM.ranges(i,j,        ranges,t,n,xpect)
  t,out = {},{}
  for x,n in pairs(i.has) do t[x]= t[x] or SYM(); t[x]:add("best",n) end
  for x,n in pairs(j.has) do t[x]= t[x] or SYM(); t[x]:add("rest",n) end
  for x,stats in pairs(t) do push(out, RANGE(i,x,x,stats)) end
  return out end

function SYM.superRanges(i, ranges) return ranges end
```

```lua
-------------------------------------------------------------------------------
function EG.new(t) return new(EG, {cooked={}, has=t}) end

function EG.better(eg1,eg2,egs)
  local s1,s2,e,n,a,b = 0,0,10,#egs.cols.y
  for _,col in pairs(egs.cols.y) do
    a  = col:norm(eg1.has[col.at])
    b  = col:norm(eg2.has[col.at])
    s1 = s1 - e^(col.w * (a-b)/n)
    s2 = s2 - e^(col.w * (b-a)/n) end
  return s1/n < s2/n end

function EG.cols(i,cols) return map(cols,function(x) return i.has[x.at] end) end

function EG.dist(i,j,egs,    a,b,d,n)
  d,n = 0, #egs.cols.x + 1E-31
  for _,col in pairs(egs.cols.x) do
    a,b = i.has[col.at], j.has[col.at]
    d   = d + col:dist(a,b) ^ your.p end
  return (d/n) ^ (1/your.p) end

-------------------------------------------------------------------------------
function RANGE.new(col,lo,hi,has)
  lo = lo or -math.huge
  return new(RANGE, {n=0,score=nil,col=col, lo=lo, hi=hi or lo, has=has or SYM()
}) end

function RANGE.__tostring(i)
  if i.lo == i.hi        then return fmt("%s == %s",i.col.txt,i.lo) end
  if i.lo == -math.huge then return fmt("%s < %s",i.col.txt,i.hi) end
  if i.ho ==  math.huge then return fmt("%s >= %s",i.col.txt,i.lo) end
  return fmt("%s <= %s < %s", i.col.txt, i.lo, i.hi) end

function RANGE.add(i,x,y)
  i.n = n.n+1
  i.hi = math.max(x,i.hi)
  i.lo = math.min(x,i.lo)
  i.has:add(y) end

function RANGE.div(i) return i.has:div() end

function RANGE.select(i,eg,       x)
  x = eg.has[i.col.at]
  return x=="?" or i.lo <= x and x < i.hi end

function RANGE.merge(i,j,      k)
 k = RANGE(i.col, i.lo, j.hi, i.has:merged(j.has))
 k.n = i.n + j.n
 if k.has:div()*1.01 <= xpects{i, j} then return k end end

function RANGE.eval(i,goal)
    local best, rest, goals = 0,0,{}
  if not i.score then
    function goals.smile(b,r) return r>b and 0 or b*b/(b+r +1E-31) end
    function goals.frown(b,r) return b<r and 0 or r*r/(b+r +1E-31) end
    function goals.xplor(b,r) return 1/(b+r              +1E-31) end
    function goals.doubt(b,r) return 1/(math.abs(b-r)    +1E-31) end
    for x,n in pairs(i.has) do
      if x==goal then best = best+n/i.n else rest = rest+n/i.n end end
    i.score = best + rest < 0.01 and 0 or goals[your.goal](best,rest) end
  return i.score end

-------------------------------------------------------------------------------
function COLS.new(eg,     i,now,where)
  i = new(COLS,{all={}, x={}, y={}})
  for at,s in pairs(eg) do    -- First row. Create the right columns
    now   = push(i.all, (s:find"^[A-Z]" and NUM or SYM)(at,s))
    where = (s:find"-" or s:find"+") and i.y or i.x
    if not s:find":" then push(where, now) end end
  return i end

function COLS.add(i,eg)
  return map(i.all, function(col) return col:add(eg[col.at]) end) end

-------------------------------------------------------------------------------
function EGS.new(i) return new(EGS, {rows={}, cols=nil}) end

function EGS.add(i,eg)
  eg = eg.has and eg.has or eg -- If eg has data buried inside, expose it.
  if i.cols then push(i.rows,EG(i.cols:add(eg))) else i.cols=COLS(eg) end end

function EGS.clone(i,inits,    j)
  j = EGS()
  j:add(map(i.cols.all, function(col) return col.txt end))
  for _,x in pairs(inits or {}) do  j:add(x) end
  return j end

function EGS.cluster(i, rows)
  local zero,one,two,ones,twos,both,a,b,c
  zero  = any(rows)
  one   = i:far(zero)
  two,c = i:far(one)
  ones,twos,both = i:clone(), i:clone(),{}
  for _,eg in pairs(rows) do
    a = eg:dist(one, i)
    b = eg:dist(two, i)
    push(both, {(a^2 + c^2 - b^2) / (2*c),eg}) end
  for n,pair in pairs(sort(both, firsts)) do
    (n <= #both//2 and ones or twos):add(pair[2]) end
  if your.better and two:better(one,i) then ones,twos=twos,ones end
  return ones, twos end

function EGS.far(i,eg1,    fun,tmp)
  fun = function(eg2) return {eg2, eg1:dist(eg2,i)} end
  tmp = #i.rows > your.Some and any(i.rows, your.Some) or i.rows
  tmp = sort(map(tmp, fun), seconds)
  return table.unpack(tmp[#tmp*your.far//1] ) end

function EGS.from(t, i)
  i=i or EGS(); for _,eg in pairs(t) do i:add(eg) end; return i end

function EGS.mid(i,cols)
  return map(cols or i.all, function(col) return col:mid() end) end

function EGS.read(file, i)
  i=i or EGS(); for eg in csv(file) do i:add(eg) end; return i end

function EGS.superRanges(i,top)
  local one, two = top:cluster(i.rows)
  local best, out, col2, tmp, ranges = math.huge
  for n,col1 in pairs(one.cols.x) do
    col2   = two.cols.x[n]
    ranges = col1:ranges(col2)
    ranges = col1:superRanges(ranges)
    if #ranges > 1 then
      tmp    = xpects(ranges)
      if tmp < best then best, out = tmp, ranges end end end
  return out, lefts, firsts end
```

```
-------------------------------------------------------------------------
function any(t,  n)
  if not n then return t[randi(1,#t)] end
  u={};for j=1,n do push(u,any(t)) end; return u end

our.fails = 0
function asserts(test,msg)
  msg=msg or ""
  if test then return print(" PASS : "..msg) end
  our.fails = our.fails+1
  print(" FAIL : "..msg)
  if your.Debug then assert(test,msg) end end

function coerce(x)
  if x=="true" then return true elseif x=="false" then return false end
  return tonumber(x) or x end

function copy(t,u)
  u={}; for k,v in pairs(t) do u[k]=v end
  return setmetatable(u, getmetatable(t)) end

function csv(file,   x,row)
  function row(x,  t)
    for y in x:gsub("%s+",""):gmatch"([^,]+)" do push(t,coerce(y)) end
    return t
  end ----------------
  file = io.input(file)
  return function()
    x=io.read(); if x then return row(x,{}) else io.close(file) end end end

function userSettings(help_string,       t,fun)
  function fun(flag,x)
    for n,txt in ipairs(arg) do
      if   txt:sub(1,1)=="-" and flag:match("^"..txt:sub(2)..".*")
      then x = x=="false" and"true" or x=="true" and"false" or arg[n+1] end end
    t[flag] = coerce(x)
  end ----------------
  t = {}
  help_string:gsub("\n  [-]([^%s]+)[^\n]*%s([^%s]+)", fun)
  return t end

function firsts(a,b) return a[1] < b[1] end

function fmt(...) return string.format(...) end

function main(user, system,      todos)
  local function reset()
    for k,v in pairs(userSettings(system.help)) do user[k]=v end end
  reset()
  if   user.h
  then print(system.help)
  else system.fails = 0
       todos = user.todo=="all" and slots(system.go) or {user.todo}
       for _,one in pairs(todos) do
        if type(system.go[one])=="function" then system.go[one]() end
        reset() end end
  for k,v in pairs(_ENV) do
    if not system.b4[k] then print("?rogues",k,type(v)) end end
  return system.fails end

function map(t,f,  u)
  u= {};for k,v in pairs(t) do push(u,(f or same)(v)) end; return u end

our.oid=0
function new(mt,x)
  our.oid = our.oid+1; x._oid = our.oid -- Everyone gets a unique id.
  return setmetatable(x,mt) end         -- Methods now delegate to `mt`.

function o(t)
  local u,key
  key= function(k) return fmt(":%s %s", k, o(t[k])) end
  if type(t) ~= "table" then return tostring(t) end
  u = #t>0 and map(t,o) or map(slots(t),key)
  return (t._is or "").."{"..table.concat(u, " ").."}" end

function push(t,x) table.insert(t,x); return x end

your.seed = your.seed or 10019
function rand(lo,hi)
  your.seed = (16807 * your.seed) % 2147483647
  return (lo or 0) + ((hi or 1) - (lo or 0)) * your.seed / 2147483647 end

function randi(lo,hi) return math.floor(0.5 + rand(lo,hi)) end

function rnd(x,d,  n)
  if type(x)~="number" then return x end
  n=10^(d or your.round)
  return math.floor(x*n+0.5)/n end

function rnds(t,d) return map(t,function(x) return rnd(x,d) end) end

function same(x,...) return x end

function seconds(a,b) return a[2] < b[2] end

function slots(t,   u)
  u={}
  for k,_ in pairs(t) do if tostring(k):sub(1,1) ~= "_" then push(u,k) end end
  return sort(u) end

function sort(t,f) table.sort(t,f);   return t end

function xpects(t)
  local sum,n = 0,0
  for _,z in pairs(t) do n = n + z.n; sum = sum + z.n*z:div() end
  return sum/n end
```

```
-------------------------------------------------------------------------
our.go={}   -- list of enabled tests
our.nogo={} -- list of disabled test
local go, nogo = our.go,our.nogo

function go.settings()
  print("our",o(our))
  print("your",o(your)) end

function go.range(  r)
  r=RANGE(NUM(10,"fred"),"apple")
  assert(tostring(r) == "fred == apple", "print ok") end

function go.num(    m,n)
  m=NUM();   for j=1,10 do m:add(j) end
  n=copy(m); for j=1,10 do n:add(j) end
  asserts(2.95 == rnd(n:div()),"sd ok") end

function go.egs(    egs)
  egs = EGS.read(your.file)
  asserts(egs.cols.y[1].hi==5140,"most seen") end

function go.clone(     egs1,egs2,s1,s2)
  egs1 = EGS.read(your.file)
  s1   = o(egs1.cols.y)
  egs2 = egs1:clone(egs1.rows)
  s2   = o(egs2.cols.y)
  asserts(s1==s2, "cloning works") end

function go.dist()
  local egs,eg1,dist,tmp,j1,j2,d1,d2,d3,one
  egs  = EGS.read(your.file)
  eg1  = egs.rows[1]
  dist = function(eg2) return {eg2,eg1:dist(eg2,egs)} end
  tmp  = sort(map(egs.rows, dist), seconds)
  one  = tmp[1][1]
  for j=1,10 do
    j1 = randi(1,#tmp)
    j2 = randi(1,#tmp)
    if j1>j2 then j1,j2=j2,j1 end
    d1 = tmp[j1][1]:dist(one,egs)
    d2 = tmp[j2][1]:dist(one,egs)
    asserts(d1 <= d2,"distance ") end end

function go.cluster(   top,left,right)
  top = EGS.read(your.file)
  left, right = top:cluster()
  for n,t in pairs{top,left,right} do print(n,o(rnds(t:mid(t.cols.y)))) end
end

-- assuming our.go = demos and our.help==help string and our.fails = 0 then...
os.exit( main(your, our))
```