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rezo.lua

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9  --
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25 -- LIABILITY, WHETHER IN AN ACTION OF CONTRACT, TORT OR OTHERWISE, ARISING FROM,
26 -- OUT OF OR IN CONNECTION WITH THE SOFTWARE OR THE USE OR OTHER DEALINGS IN THE
27 -- SOFTWARE
28 local help = [[
29 lua rezo.lua [OPTIONS]
30 Tree learner (binary splits on numerics using Gaussian approximation)
31 (c)2021 Tim Menzies <timm@ieee.org> MIT license.
32
33 OPTIONS:
34 -best      X   Best examples are in 1..best*size(all)      = .2
35 -debug     X   run one test, show stackdumps on fail      = pass
36 -epsilon   X   ignore differences under epsilon*stdev     = .35
37 -Far       X   How far to look for remove items           = .9
38 -file      X   Where to read data                          = ../../data/auto93.csv
39 -h         X   Show help                                    = false
40 -little    X   size of subset of a list                    = 256
41 -p         X   distance calc coefficient                   = 2
42 -seed      X   Random number seed;                        = 10019
43 -Stop      X   Create subtrees while at least 2*stop eggs = 4
44 -Tiny      X   Min range size = size(eggs)^tiny           = .5
45 -todo      X   Pass/fail tests to run at start time       = pass
46               If "X=all", then run all.
47               If "X=s" then list all.
48
49 Data read from "-file" is a csv file whose first row contains column
50 names (and the other row contain data. If a name contains ":",
51 that column will get ignored. Otherwise, names starting with upper
52 case denote numerics (and the other columns are symbolic). Names
53 containing "!" are class columns and names containing "+" or "-"
54 are goals to be maximized or minimized. --]] --[[
55
56 Internally, columns names are read by a COLS object where numeric,
57 symbolic, and ignored columns generate NUM, SYM, and SKIP instances
58 (respectively). After row1, all the other rows are examples ('EG')
59 which are stored in a SAMPLE. As each example is added to a sample,
60 they are summarized in the COLS' objects.
61
62 Note that SAMPLES can be created from disk data, or at runtimes from
63 lists of examples (see SAMPLE:clone()). --]]
64
65 local b4={}; for k,_ in pairs(_ENV) do b4[k]=k end
66 local THE = {} -- The THE global stores the global config for this software.
67 -- any line of help text starting with " -" has flag,default as first,last word
68 help:gsub("\n [-]([%s]+)[^\n]*%s([%s]+)",
69 function(flag,x)
70   for n,word in ipairs(arg) do -- check for any updated to "flag" on command line
71     -- use any command line "word" that matches the start of "flag"
72     if flag:match("^"..word:sub(2)..".*") then
73       -- command line "word"s for booleans flip the default value
74       x=(x=="false" and "true") or (x=="true" and "false") or arg[n+1] end end
75   if x=="true" then x=true elseif x=="false" then x=false else x=tonumber(x) or x end
76   THE[flag] = x end)
77
78 THE.seed = THE.seed or 10019
79 if THE.h then return print(help) end

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79 --
80 --
81 --
82 --
83 -- meta
84 local same
85 function same(x,...) return x end
86
87 -- sorting
88 local push,sort,ones
89 function push(t,x) table.insert(t,x); return x end
90 function sort(t,f) table.sort(t,f); return t end
91 function ones(a,b) return a[1] < b[1] end
92
93 -- tables
94 local copy,keys,map,sum
95 function copy(t, u) u={};for k,v in pairs(t) do u[k]=v end; return u end
96 function keys(t, u) u={};for k,_ in pairs(t) do u[1+#u]=k end; return sort(u) end
97 function map(t,f, u) u={};for k,v in pairs(t) do u[1+#u]=f(k,v) end; return u end
98 function sum(t,f, n) n=0;for _,v in pairs(t) do n=n+(f or same)(v) end;return n end
99
100 -- printing utils
101 local hue,shout,out,say,fmt
102 fmt = string.format
103 function say(...) print(string.format(...)) end
104 function hue(n,s) return string.format("%27[1m%27[31m%27[0m",n,s) end
105 function shout(x) print(out(x)) end
106 function out(t, u,key,val) -- convert nested tables to a string
107   function key(_,k) return string.format(":%s%s", k, out(t[k])) end
108   function val(_,v) return out(v) end
109   if type(t) ~= "table" then return tostring(t) end
110   u = #t>0 and map(t, val) or map(keys(t), key)
111   return {"..table.concat(u," ").."} end
112
113 -- reading from file
114 local coerce,csv
115 function coerce(x)
116   if x=="true" then return true elseif x=="false" then return false end
117   return tonumber(x) or x end
118
119 function csv(file, x)
120   file = io.input(file)
121   return function() t,tmp)
122     x = io.read()
123     if x then
124       t={};for y in x:gsub("[\n]*",""):gmatch("[^\n]+") do push(t,coerce(y)) end
125       if #t>0 then return t end
126     else io.close(file) end end end
127
128 -- maths
129 local log,sqrt,rnd,rnds
130 log = math.log
131 sqrt= math.sqrt
132 function rnd(x,d, n) n=10^(d or 2); return math.floor(x*n+0.5) / n end
133 function rnds(t,d) return map(t, function(_,x) return rnd(x,d or 2) end) end
134
135 -- random stuff (LUA's built-in randoms give different results on different platfors)
136 local randi,rand,any,some,shuffle
137 function randi(lo,hi) return math.floor(0.5 + rand(lo,hi)) end
138 function rand(lo,hi)
139   lo, hi = lo or 0, hi or 1
140   THE.seed = (16807 * THE.seed) % 2147483647
141   return lo + (hi-lo) * THE.seed / 2147483647 end
142
143 function any(t) return t[randi(1,#t)] end
144 function some(t,n, u)
145   if n >= #t then return shuffle(copy(t)) end
146   u={}; for i=1,n do push(u,any(t,i)) end; return u end
147
148 function shuffle(t, j)
149   for i=#t,2,-1 do j=randi(1,i); t[i],t[j]=t[j],t[i] end; return t end
150
151 -- objects
152 local ako,has,obj
153 ako= getmetatable
154 function has(mt,x) return setmetatable(x,mt) end
155 function obj(s, o,new)
156   o = {__is=s, __tostring=out}
157   o.__index = o
158   return setmetatable(o, {__call=function(_,...) return o.new(...) end}) end

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159 --
160 -- NUM
161 --
162 --
163 local NUM=obj"NUM"
164 function NUM.new(inits,at,txt, self)
165     self = has(NUM,{n=0, at=at or 0, txt=txt or "",
166                     w=(txt or ""):find"- " and -1 or 1,
167                     mu=0, m2=0, lo=math.huge, hi=-math.huge})
168     for _,x in pairs(inits or {}) do self:add(x) end
169     return self end
170
171 -- summarizing
172 function NUM:mid() return self.mu end
173 function NUM:spread() return (self.m2/(self.n-1))^0.5 end
174
175 -- updating
176 function NUM:add(x, d)
177     if x ~= "?" then
178         self.n=self.n+1
179         d=x-self.mu
180         self.mu= self.mu+d/self.n
181         self.m2= self.m2+d*(x-self.mu)
182         self.lo = math.min(x, self.lo)
183         self.hi = math.max(x, self.hi) end
184     return x end
185
186 -- querying
187 function NUM:norm(x)
188     local lo,hi = self.lo,self.hi
189     return math.abs(hi - lo) < 1E-9 and 0 or (x-lo)/(hi-lo) end
190
191 function NUM:dist(x,y)
192     if x=="?" then y=self:norm(y); x=y>0.5 and 0 or 1
193     elseif y=="?" then x=self:norm(x); y=x>0.5 and 0 or 1
194     else x, y = self:norm(x), self:norm(y) end
195     return math.abs(x-y) end
196
197 -- discretization
198 function NUM:splits(other)
199     function cuts(x,s,at) return {
200         {val=x, at=at, txt=fmt("%s<=$s",s,x), when=function(z) return z<=x end},
201         {val=x, at=at, txt=fmt("%s>$s",s,x), when=function(z) return z>x end}}
202     end
203     local i,j,e = self, other, 2.71828
204     local a,b,c,root1,root2
205     local sd=function(x) return x:spread() end
206     a = 1/(2*sd(i)^2) - 1/(2*sd(j)^2)
207     b = j.mu/(sd(j)^2) - i.mu/(sd(i)^2)
208     c = i.mu^2/(2*sd(i)^2) - j.mu^2/(2*sd(j)^2) - mat
209     root1 = (-b - sqrt(b*b - 4*a*c))/2*a
210     root2 = (-b + sqrt(b*b - 4*a*c))/2*a
211     if i.mu<=root1 and root1<=j.mu
212     then return cuts(root1,self.txt,self.at)
213     else return cuts(root2,self.txt,self.at) end end
214
215 --
216 -- SYM
217 --
218 local SYM=obj"SYM"
219 function SYM.new(inits,at,txt,sample, self)
220     self= has(SYM,{n=0, at=at or 0, txt=txt or "", sample=sample,
221                  seen={}, mode=nil, most=0})
222     for _,x in pairs(inits or {}) do self:add(x) end
223     return self end
224
225 -- Summarizing
226 function SYM:mid() return self.mode end
227 function SYM:spread()
228     return sum(self.seen, function(n) return -n/self.n*log(n/self.n,2) end) end
229
230 -- update
231 function SYM:add(x)
232     self.seen[x] = (self.seen[x] or 0) + 1
233     if self.seen[x] > self.most then self.mode, self.most = x, self.seen[x] end
234     return x end
235
236 -- querying
237 function SYM:dist(x,y) return x==y and 0 or 1 end
238
239 -- discretization
240 function SYM:splits(other)
241     function cut(_,x) return
242         {val=x, at=self.at, txt=fmt("%s===$s",self.txt,x),
243          when = function(z) return z==x end} end
244     local out={}
245     for k,_ in pairs(self.seen) do push(out,k) end
246     for k,_ in pairs(other.seen) do push(out,k) end
247     return map(sort(out),cut) end
248

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249 --
250 -- SKIP
251 --
252 --
253 -- Columns for values we want to ignore.
254 local SKIP=obj"SKIP"
255 function SKIP.new(inits,at,txt)
256     return has(SKIP,{n=0, at=at or 0, txt=txt or ""}) end
257
258 function SKIP:mid() return "?" end
259 function SKIP:spread() return 0 end
260 function SKIP:add(x) return x end
261 function SKIP:splits(_) return {} end
262
263 -- EG
264 --
265 -- One example
266 local EG=obj"EG"
267
268 function EG.new(cells) self.cells = cells end
269
270 -- Sumamrizing
271 function EG:mid(cols) return map(cols, function(_,c) return c:mid() end) end
272 function EG:spread(cols) return map(cols, function(_,c) return c:spread() end) end
273
274 -- Queries
275 function EG:dist(other,cols, a,b,d,n,inc)
276     d,n = 0,0
277     for _,col in pairs(cols) do
278         a,b = self.cells[col.at], other.cells[col.at]
279         inc = a=="?" and b=="?" and 1 or col:dist(a,b)
280         d = d + inc^THE.p
281         n = n + 1 end
282     return (d/n)^(1/THE.p) end
283
284 -- Sorting
285 function EG:better(other,cols, e,n,a,b,s1,s2)
286     n,s1,s2,e = #cols, 0, 0, 2.71828
287     for _,num in pairs(cols) do
288         a = num:norm(self.cells[ num.at])
289         b = num:norm(other.cells[num.at])
290         s1 = s1 - e^(num.w * (a-b)/n)
291         s2 = s2 - e^(num.w * (b-a)/n) end
292     return s1/n < s2/n end
293
294 --
295 -- COLS
296 --
297 -- Convert column headers into NUMs and SYMs, etc.
298 local COLS=obj"COLS"
299 function COLS.new(names, self, new,what)
300     self = has(COLS, {names=names, xs={}, all={}, ys={}})
301     for n,x in pairs(names) do
302         new = (x:find"." and SKIP or x:match"^[A-Z]" and NUM or SYM)({},{},n,x)
303         push(self.all, new)
304         if not x:find"." then
305             if x:find"!" then self.klass = new
306             what = (x:find"- " or x:find"+") and self.ys or self.xs
307             push(what, new) end end end
308     return self end
309
310 -- Updates
311 function COLS:add(eg)
312     return map(eg, function(n,x) self.all[n]:add(x); return x end) end
313
314

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315 --
316 -- SAMPLE
317 --
318 -- SAMPLEs hold many examples
319 local SAMPLE=obj"SAMPLE"
320 function SAMPLE:new(inits, self)
321     self = has(SAMPLE, {cols=nil, eggs={}})
322     if type(inits)=="string" then for eg in csv(inits) do self:add(eg) end end
323     if type(inits)=="table" then for eg in pairs(inits) do self:add(eg) end end
324     return self end
325
326 -- Create a new sample with the same structure as this one
327 function SAMPLE:clone(inits, out)
328     out = SAMPLE:new(self.cols.names)
329     for _,eg in pairs(inits or {}) do out:add(eg) end
330     return out end
331
332 -- Updates
333 function SAMPLE:add(eg)
334     eg = eg.cells and eg.cells or eg
335     if self.cols
336     then push(self.egs, eg); self.cols:add(eg)
337     else self.cols = COLS(eg) end end
338
339 -- Distance queries
340 function SAMPLE:neighbors(eg1, eggs, cols)
341     local dist_eg2 = function(_, eg2) return {eg1:dist(eg2, cols or self.xls), eg2} end
342     return sort(map(egs or self.egs, dist_eg2), firsts) end
343
344 function SAMPLE:distance_farExample(eg1, eggs, cols, tmp)
345     tmp = self:neighbors(eg1, eggs, cols)
346     return table.unpack(tmp[#tmp*self.Far//1]) end
347
348 -- Discretization
349 function SAMPLE:twain(egs, cols)
350     local eggs, north, south, a, b, c, lo, hi
351     eggs = some(egs or self.egs, self.little)
352     _, north = self:distance_farExample(any(self.egs), eggs, cols)
353     c, south = self:distance_farExample(north, eggs, cols)
354     for _, eg in pairs(self.egs) do
355         a = eg:dist(north, cols)
356         b = eg:dist(south, cols)
357         eg.x = (a^2 + c^2 - b^2)/(2*c) end
358     lo, hi = self:clone(), self:clone()
359     for n, eg in pairs(sort(self.egs, function(a, b) return a.x < b.x end)) do
360         if n < .5*#eg then lo:add(eg) else hi:add(eg) end end
361     return lo, hi end
362
363 function SAMPLE:mid(cols)
364     return map(cols or self.cols.all, function(_, col) return col:mid() end) end
365 function SAMPLE:spread(cols)
366     return map(cols or self.cols.all, function(_, col) return col:spread() end) end
367
368

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369 --
370 -- SAMPLE TREE
371 --
372 --
373 -- need to sort first
374
375 -- how to score
376 function SAMPLE:splits(other, both, cuts, unplaced, place, score)
377     function guess(todos, cuts)
378         for _, todo in pairs(todos) do
379             local f=function(_, cut)
380                 return {Row(cut.has:mid()):dist(todo, both.cols.xls), cut} end
381             sort(map(cuts, f), firsts)[1][2].has:add(todo) end
382         return cuts end
383     function divide(cuts, todos, placed)
384         todos = {}
385         for _, eg in pairs(both.egs) do
386             placed = false
387             for _, cut in pairs(cuts) do
388                 if cut.what(eg.cells[cut.at])
389                 then cut.has = cut.has or self:clone()
390                     cut.has:add(eg)
391                     placed = true
392                     break end end
393             if not placed then push(todos, eg) end end
394         return guess(todos, cuts) end
395     function score(cut, m, n)
396         m, n = #cut.has.egs, both.egs; return -m/n*log(m/n, 2) end
397     local best, cutsx, tmp = math.huge
398     for pos, col in pairs(both.cols.xls) do
399         cutsx = col:splits(other.cols.xls[pos])
400         tmp = sum(divide(cutsx), score)
401         if tmp < best then best, cuts = tmp, cutsx end end
402     return cuts end
403
404 function SAMPLE:tree(top)
405     top = top or self
406     one, two = self:twain(self.egs, top.cols.xls)
407     for _, cut in pairs(one:splits(two, self)) do
408         if cut.stats.n > (#top.egs)^THE.Tiny then
409             cut.sub= cut.has:tree(top) end end end
410
411 function SAMPLE:show(tree)
412     local vals=function(a, b) return a.val < b.val end
413     local function show1(tree, pre)
414         if #tree.kids==0 then io.write(fmt("==> %s[%s]", tree.mode, tree.n)) end
415         for _, kid in pairs(sort(tree.kids, vals)) do
416             io.write("\n"..fmt("%s%s", pre, showDiv(i, kid.at, kid.val)))
417             show1(kid.sub, pre.."|..") end
418     end -----
419     show1(tree, ""); print("") end
420

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421 -----
422 --
423 --   EXAMPLES
424 --
425 --
426 local go={}
427 function go.ls()
428   print("\nlua " ..arg[0] .. "-todo ACTION\n\nACTIONS:")
429   for _,k in pairs(keys(go)) do print("-todo",k) end end
430
431 function go.pass() return true end
432 function go.the() shout(TH) end
433 function go.bad( s) assert(false) end
434
435 function go.sort( u,t)
436   t={}; for i=100,1,-1 do push(t,i) end
437   t=sort(t,function(x,y)
438     if x+y<20 then return x>y else return x<y end end)
439   assert(sum(t,function(x) return x*100 end)==505000)
440   assert(t[1] == 10)
441   assert(t[#t]==100)
442   u=copy(t)
443   t[1] = 99
444   assert(u[1] ~= 99) end
445
446 function go.out( s)
447   assert("[:age 21 :milestones {1 2 3 4} :name tim]"==out(
448     {name='tim', age=21, milestones={1,2,3,4}}))end
449
450 function go.file( n)
451   for _,t in pairs({{"true",true,"boolean"}, {"false",false,"boolean"},
452     {"42.1",42.1,"number"}, {"32zz","32zz","string"},
453     {"nil","nil","string"}}) do
454     assert(coerce(t[1])==t[2])
455     assert(type(coerce(t[1]))==t[3]) end
456   n = 0
457   for row in csv(TH.file) do
458     n = n + 1
459     assert(#row==8)
460     assert(n==1 or type(row[1])=="number")
461     assert(n==1 or type(row[8])=="number") end end
462
463 function go.rand( t,u)
464   t,u={},{}; for i=1,20 do push(u,push(t,100*rand())) end
465   t= sort(rnds(t,0))
466   assert(t[1]==3 and t[#t]==88)
467   t= sort(some(t,4))
468   assert(#t==4)
469   assert(t[1]==7)
470   assert(79.5 == rnds(shuffle(u))[1])
471 end
472
473 function go.num( cut,min)
474   local xnum, ynum = NUM(), NUM()
475   for i=1,400 do xnum:add(rand()^3) end
476   for i=401,500 do ynum:add(rand()^.25) end
477   print(xnum:mid(), xnum:spread())
478   print(ynum:mid(), ynum:spread())
479   print(xnum:splits(ynum))
480 end
481
482 function go.ordered( s,n)
483   s = ordered(slurp())
484   n = #s.egs
485   shout(s.heads)
486   for i=1,15 do shout(s.egs[i].cells) end
487   print("#")
488   for i=n,n-15,-1 do shout(s.egs[i].cells) end
489 end
490
491 function go.symcuts( s,xpect,cuts)
492   s=ordered(slurp())
493   print(out(s.xs),out(s.ys))
494   xpect,cuts = symcuts(7,s.egs, "origin")
495   for _,cut in pairs(cuts) do print(xpect, out(cut)) end end
496
497 function go.numcuts( s,xpect,cuts)
498   s=ordered(slurp())
499   xpect,cuts = numcuts(s,2,s.egs,"Displment")
500   if xpect then
501     for _,cut in pairs(cuts) do print(xpect, out(cut)) end end end
502
503 function go.atcuts(s,cuts,at,ynum)
504   s=ordered(slurp())
505   ynum=NUM(a); map(s.egs,function(_,eg) add(ynum, eg.klass) end)
506   at,cuts = at_cuts(s,egs,sd(ynum)*THE.epsilon, (#s.egs)^THE.Tiny)
507   for _,cut in pairs(cuts) do print(at, out(cut)) end end
508

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```

509 --
510 --   START-UP
511 --
512 --
513 local fails, defaults = 0, copy(TH)
514 go[ THE.debug ]()
515 local todos = THE.todo == "all" and keys(go) or {THE.todo}
516 for _,todo in pairs(todos) do
517   THE = copy(defaults)
518   local ok,msg = pcall( go[todo] )
519   if ok then io.write(hue(32,"PASS")..todo.."\n")
520     else io.write(hue(31,"FAIL")..todo.." ".msg.."\n")
521     fails=fails+1 end end
522
523 for k,v in pairs(_ENV) do if not b4[k] then print("?:",k,type(v)) end end
524 os.exit(fails)

```