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                                                   rezon.lua
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   local help = [[
   lua rezon.lua [OPTIONS]
   Tree learner (binary splits on numerics using Gaussian approximation)
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                    Best examples are in 1..best*size(all)
     -best
                    run one test, show stackdumps on fail
     -debug
     -epsilon X
                     ignore differences under epsilon*stdev
                                                                   = .35
     -Far
                     How far to look for remove items
                                                                    = .9
     -file
                X
                    Where to read data
                                                                    = ../../data/auto93.csv
                     Show help
     -h
                                                                    = false
     -little
               X size of subset of a list
                                                                  = 256
                     distance calc coefficient
     -p
                                                                   = 2
      -seed
                     Random number seed;
                                                                   = 10019
      -Stop
                     Create subtrees while at least 2*stop egs =
                                                                      4
     -Tiny
                     Min range size = size(egs)^tiny
                     Pass/fail tests to run at start time
      -todo
                    If "X=all", then run all.
If "X=ls" then list all.
  Data read from "-file" is a csv file whose first row contains column names (and the other row contain data. If a name contains ":", that column will get ignored. Otherwise, names starting with upper
   case denote numerics (and the other columns are symbolic). Names
   containing "!" are class columns and names containing "+" or "-"
   are goals to be maximized or minimized. --]] --[[
   Internally, columns names are read by a COLS object where numeric,
   symbolic, and ignored columns generate NUM, SYM, and SKIP instances
   (respectively). After row1, all the other rows are examples ('EG')
  which are stored in a SAMPLE. As each example is added to a sample, they are summarized in the COLS' objects.
   Note that SAMPLEs can be created from disk data, or at runtimes from
   lists of examples (see SAMPLE:clone()). -- 11
   local b4={}; for k,_ in pairs(_ENV) do b4[k]=k end
   function (flag, x)
       for n, word in ipairs (arg) do -- check for any updated to "flag" on command line
            - use any command line "word" that matches the start of "flag"
          if flag:match("^"..word:sub(2)..".*") then
       -- command line "word"s for booleans flip the default value x=(x=="false" and "tnue") or (x=="tnue" and "false") or arg[n+1] end end if x=="tnue" then x=true elseif x=="false" then x=false else x=tonumber(x) or x end
```

THE[flag] = x end)

77 THE seed = THE seed or 10019

78 if THE.h then return print (help) end

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```
-- meta
   local same
   function same (x,...) return x end
   -- sorting
   local push, sort, ones
    function push (t,x) table.insert(t,x); return x end
   function sort(t,f) table.sort(t,f); return t end
function ones(a,b) return a[1] < b[1] end
   -- tables
   local copy, keys, map, sum
   end: return 11
   function keys(t, u) u={}; for k, in pairs(t) do u[1+#u]=k
function map(t, f, u) u={}; for k, v in pairs(t) do u[1+#u] = f(k, v)
                                                                                end: return sort(u) end
                                                                                end: return u
                                                                                                       end
   function sum(t, f, n) n=0; for _, v in pairs(t) do n=n+(f or same)(v) end; return n
                                                                                                       end
101 local hue, shout, out, say, fmt
102 fmt = string.format
   function say(...) print(string.format(...)) end
function hue(n,s) return string.format("\27[lm\27[%sm\%\27[0m",n,s) end
   function shout (x) print (out (x)) end
function out(t, u,key,val) -- convert nested tables to a string
function key(_,k) return string.format(":%s %s", k, out(t[k])) end
     function val(_,v) return out(v) end

if type(t) ~= "table" then return tostring(t) end
     return "{"..table.concat(u,"").."}" end
   -- reading from file
   local coerce, csv
115 function coerce(x)
     if x=="true" then return true elseif x=="false" then return false end
     return tonumber(x) or x end
     file = io.input(file)
      return function ( t,tmp)
        x = io.read()
        if x then
123
          t=\{\}; for y in x:gsub("[t]*",""):gmatch"([^,]+)" do push(t,coerce(y)) end
124
          if #t>0 then return t end
125
        else in close (file) end end end
126
128 -- maths
129 local log, sgrt, rnd, rnds
130 log = math.log
   sgrt= math.sgrt
   function rnd(x,d, n) n=10^(d or 0); return math.floor(x*n+0.5) / n end
133 function rnds(t,d)
                            return map(t, function(_,x) return rnd(x,d or 2) end) end
135 -- random stuff (LUA's built-in randoms give different results on different platfors)
   local randi, rand, any, some
   function randi(lo,hi) return math.floor(0.5 + rand(lo,hi)) end
   function rand(lo,hi)
     lo, hi = lo or 0, hi or 1
THE.seed = (16807 * THE.seed) % 2147483647
     return lo + (hi-lo) * THE.seed / 2147483647 end
143 function anv(t)
                            return t[randi(1, #t)] end
144 function some (t,n,
                           u)
     if n >= #t then return copy(t) end
     u={}; for i=1,n do push(u,any(t)) end; return u end
149 local ako, has, obj
150 ako= getmetatable
   function has (mt,x) return setmetatable (x, mt) end
152 function obj(s, o,new)
   o = {_is=s, __tostring=lib.out}
     o index = o
     return setmetatable(o,{ call=function(,...) return o.new(...) end}) end
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```
157 --
158 --
   local NUM=obj"NUM"
   function NUM.new(inits,at,txt,
     mu=0, m2=0, lo=math.huge, hi=-math.huge})
      for _, x in pairs(inits or {}) do self:add(x) end
     return self end
169 function NUM:mid()
                          return self.mu end
   function NUM:spread() return (self.m2/(self.n-1))^0.5 end
172 -- updating
173 function NUM:add(x, d)
    if x ~= "?" then
        self.n=self.n+1
        d=x-self.mu
        self.mu= self.mu+d/self.n
        self.m2= self.m2+d*(x-self.mu)
        self.lo = math.min(x, self.lo)
        self.hi = math.max(x, self.hi) end
     return x end
183 -- querving
184 function NUM:norm(x)
     local lo,hi = self.lo,self.hi
      return math.abs(hi - lo) < 1E-9 and 0 or (x-lo)/(hi-lo) end
   function NUM:dist(x,y)
     if x=="?" then y=self:norm(y); x=y>0.5 and 0 or 1
elseif y=="?" then x=self:norm(x); y=x>0.5 and 0 or 1
     else x, y = self:norm(x), self:norm(y) end
     return (x-y) end
   -- discretization
194
   function NUM:splits(other)
     function cuts (x, s, at) return {
        \{val=x, at=at, txt=fmt("%s <= $s", s, x), when=function(z) return z <= x end\},
        {val=x, at=at, txt=fmt("%s>$s",s,x), when=function(z) return z >x end}}
     end 1 local i, j, e, a, b, c, x1, x2 = self, other, 2.71828 a = 1/(2*sd(i)^2) - 1/(2*sd(j)^2) b = j.mu/(sd(j)^2) - i.mu/(sd(i)^2) c = i.mu^2 / (2*sd(i)^2) - j.mu^2 / (2*sd(j)^2) - mat x1 = (-b - sqrt(b*b - 4*a*c))/2*a
     x2 = (-b + sqrt(b*b - 4*a*c))/2*a
      if i.mu<=x1 and x1<=j.mu
      then return cuts(x1, self.txt, self.at)
      else return cuts (x2, self.txt, self.at) end end
210
211
212
   local SYM=obi"SYM"
   function SYM.new(inits,at,txt,sample, self)
self= has(SYM,(n=0, at=at or 0, txt=txt or "", sample=sample,
seen={}, mode=nil, most=0})
      for ,x in pairs(inits or {}) do self:add(x) end
     return self end
   -- Summarizing
221 function SYM:mid() return self.mode end
222 function SYM:spread()
    return sum(self.seen, function(n) return -n/self.n*log(n/self.n,2) end) end
225
   function SYM:add(x)
     self.seen[x] = (self.seen[x] or 0) + 1
      if self.seen[x] > self.most then self.mode, self.most = x, self.seen[x] end
232 function SYM:dist(x,y) return x==y and 0 or 1 end
   -- discretization
234
   function SYM:splits(other)
235
     function cut( ,x) return
        {val=x, at=self.at, txt=fmt("%s==$s", self.txt,x),
         when = function(z) return z==x end end
      local out={}
      for k,_ in pairs(self.seen) do push(out,k) end
      for k, _ in pairs (other.seen) do push (out, k) end
      return map (sort (out), cut) end
```

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```
(__)
245 --
247 --
248 -- Columns for values we want to ignore.
249 local SKIP=obj"SKIP"
function SKIP.new(inits,at,txt)
   return has(SKIP, {n=0, at=at or 0, txt=txt or ""}) end
253 function SKIP:mid()
                               return "?" end
   function SKIP:spread() return 0 end
   function SKIP:add(x) return x
256 function SKIP:splits(_) return {} end
259 --
   -- One example
262 local EG=obi"EG"
function EG.new(cells) self.cells = cells end
function EG:mid(cols) return map(cols, function(_,c) return c:mid() end) end
function EG:spread(cols) return map(cols, function(_,c) return c:spread() end) end
function EG:dist(other,cols, a,b,d,n,inc)
      d.n = 0.0
      for _, col in pairs (cols) do
        a,b = self.cells[col.at], other.cells[col.at]
inc = a == "?" and b == "?" and 1 or col:dist(a,b)
        d = d + inc^THE.p
        n = n + 1 end
      return (d/n)^(1/THE.p) end
280 -- Sorting
281 function EG:better(other, cols,
                                           e.n.a.b.s1.s2)
     n, s1, s2, e = \#cols, 0, 0, 2.71828
      for .num in pairs(cols) do
       a = num:norm(self.cells[ num.at])
        b = num:norm(other.cells[num.at])
        s1 = s1 - e^{(num.w * (a-b)/n)}
     s2 = s2 - e^(num.w * (b-a)/n) end
return s1/n < s2/n end
289
200 --
291 --
293 -- Convert column headers into NUMs and SYMs, etc.
   local COLS=obj"COLS"
   function COLS.new(names, self, new,what)
      self = has(COLS, {names=names, xs={}}, all={}, ys={}})
      for n, x in pairs(names) do
  new = (x:find":" and SKIP or x:match"^[A-Z]" and NUM or SYM)({},n,x)
        push(self.all, new)
if not x:find":" then
          if x:find"!" then self.klass = new
what = (x:find"-" or x:find"+") and self.ys or self.xs
          push (what, new) end end end
     return self end
307 function COLS:add(eq)
     return map(eg, function(n,x) self.all[n]:add(x); return x end) end
```

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```
311 --
   -- SAMPLEs hold many examples local SAMPLE=obj"SAMPLE"
    function SAMPLE-GOJ SAMPLE, self)
self = has(SAMPLE, {cols=nil, egs={}})
if type(inits)=="kming" then for eg in csv(inits) do self:add(eg) end end
if type(inits)=="table" then for eg in pairs(inits) do self:add(eg) end end
    -- Create a new sample with the same structure as this one
    function SAMPLE:clone(inits, out)
       out = SAMPLE:new{self.cols.names}
       for _,eg in pairs(inits or {}) do out:add(eg) end
return out end
    function SAMPLE:add(eq)
       eg = eg.cells and eg.cells or eg
if self.cols
       then push(self.egs,eg); self.cols:add(eg)
       else self.cols = COLS(eg) end end
    -- Distance gueries
    function SAMPLE:neighbors(eq1,eqs,cols)
       local dist_eq2 = function(_,eq2) return {eq1:dist(eq2,cols or self.xs),eq2} end
       return sort (map (egs or self.egs, dist_eg2), firsts) end
    function SAMPLE:distance_farExample(eg1,egs,cols,
       tmp = self:neighbors(eg1, egs, cols)
       return table.unpack(tmp[#tmp*self.Far//1]) end
    -- Discretization
function SAMPLE:twain(egs.cols)
      local egs, north, south, a,b,c, lo,hi
egs = nany(egs or self.egs, self.little)
_,north = self:distance_farExample(any(self.egs), egs, cols)
       c, south = self:distance_farExample(north,
                                                                          egs, cols)
       for _,eg in pairs(self.egs) do
      a = eg:dist(north, cols)
b = eg:dist(south, cols)
eg.x = (a^2 + c^2 - b^2)/(2*c) end
lo, ho = self:clone(), self:clone()
       for n,eg in pairs(sort(self.egs, function(a,b) return a.x < b.x end)) do
  if n < .5*#eg then lo:add(eg) else hi:add(eq) end end</pre>
       return lo. hi end
    function SAMPLE:mid(cols)
       return map(cols or self.cols.all,function(,col) return col:mid() end) end
    function SAMPLE:spread(cols)
       return map(cols or self.cols.all, function(_,col) return col:spread() end) end
```

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```
SAMPLE TREE
368 -- need to sort first
  -- how to score
function SAMPLE:splits(other.both.
                                            cuts, unplaced, place, score)
     function guess (todos, cuts)
        for _, todo in pairs (todos) do
          local f=function(_, cut)
                     return {Row(cut.has:mid()):dist(todo, both.cols.xs),cut} end
          sort (map(cuts, f), firsts) [1] [2].has:add(todo) end
        return cuts end
     function divide (cuts, todos, placed)
       todos = {}
for _,eg in pairs(both.egs) do
          placed = false
          for _, cut in pairs(cuts) do
            if cut.what(eg.cells[cut.at])
            then cut.has = cut.has or self.clone()
                  cut.has:add(eg)
                  placed = true
                  break end end
          if not placed then push(todos, eg) end end
        return guess (todos, cuts) end
     function score(cut, m,n)
m,n = #cut.has.eqs,both.eqs; return -m/n*log(m/n,2) end
     local best, cutsx, tmp = math.huge
for pos,col in pairs(both.cols.xs) do
       cutsx = col:splits(other.cols.xs[pos])
        tmp = sum(divide(cutsx), score)
        if tmp < best then best, cuts = tmp, cutsx end end
     return cuts end
   function SAMPLE: tree (top)
     top = top or self
     one, two = self:twain(self.eqs, top.cols.xs)
     for _, cut in pairs (one:splits (two, self)) do
       if cut.stats.n > (#top.egs) THE.Tiny then
cut.sub= cut.has:tree(top) end end end
   function SAMPLE: show(tree)
     local vals=function(a,b) return a.val < b.val end</pre>
      local function show1(tree,pre)
        if #tree.kids==0 then io.write(fmt("==> %s[%s]",tree.mode, tree.n)) end
       for _,kid in pairs(sort(tree.kids,vals)) do
io.write("\u"..fmt("%%%",pre, showDiv(i, kid.at, kid.val)))
showl(kid.sub, pre.."|..") end
     show1(tree, ""); print("") end
```

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```
416
417 --
418 --
419 --
421 local go={}
function go.ls()
print("inlua"..arg[0].."-todo ACTION\n\nACTIONS:")
for _,k in pairs(keys(go)) do print("-todo",k) end end
function go.the() shout(THE) end
   function go.bad( s) assert(false) end
   function go.ordered( s,n)
      s = ordered(slurp())
      n = #s.egs
      shout (s.heads)
      for i=1,15 do shout(s.egs[i].cells) end
print("#")
      for i=n, n-15, -1 do shout (s.egs[i].cells) end
434 end
function go.num( cut,min)
local xy, xnum, ynum = {}, NUM(), NUM()
      for i=1,400     do push(xy, {add(xnum,i), add(ynum, rand()^3 )}) end
for i=401,500     do push(xy, {add(xnum,i), add(ynum, rand()^2.25)}) end
      cut, min= minXpect(xy, ynum, .35*sd(xnum), (#xy)^the.Tiny)
      shout{cut=cut, min=min} end
443 function go.symcuts( s,xpect,cuts)
      s=ordered(slurp())
      print (out (s.xs), out (s.ys))
      xpect, cuts = symcuts(7, s.egs, "origin")
      for _, cut in pairs (cuts) do print (xpect, out (cut)) end end
    function go.numcuts( s,xpect,cuts)
      s=ordered(slurp())
      xpect, cuts = numcuts(s, 2, s.egs, "Dsiplcment")
      if xpect then
        for _, cut in pairs(cuts) do print(xpect, out(cut)) end end end
455 function go.atcuts(s,cuts,at,ynum)
      s=ordered(slurp())
      ynum=NUM(a); map(s.egs, function(_,eg) add(ynum, eg.klass) end)
      at, cuts = at_cuts(s, egs, sd(ynum) *THE.epsilon, (#s.egs) THE.Tiny)
      for _,cut in pairs(cuts) do print(at, out(cut)) end end
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