

```

1  #!/usr/bin/env lua
2  local b4={}; for k,v in pairs(_ENV) do b4[k]=v end;
3
4  --
5  --
6  -- a little lite
7  -- ZVA learning
8  -- library
9  --
10 --
11 --
12 --
13 --
14 --
15 --
16 --
17 --
18 --
19 --
20
21 local options={
22
23 what = "Small sample multi-objective optimizer.",
24 usage= "(c) 2021 Tim Menzies <timm@ieee.org> unlicense.org",
25 about= [[
26 Sort N examples on multi-goals using a handful of 'hints'; i.e.
27
28 - Evaluate and rank, a few examples (on their y-values);
29 - Sort other examples by x-distance to the ranked ones;
30 - Recurse on the better half (so we sample more and more
31   from the better half, then quarter, then eighth...).
32
33 A regression tree learner then explores the examples (sorted
34 left to right, worst to best). By finding branches that
35 reduce the variance of the index of those examples, this
36 tree reports what attribute ranges select for the better (or
37 worse) examples. ]],
38
39 how= {{"file",      "-f",      ".", "data/auto93.csv",    "read data from file"},
40       {"cull",      "-c",      .5,  "cuts per repeat"},
41       {"help",      "-h",      false, "show help"},
42       {"hints",     "-H",      4,    "hints per generation"},
43       {"p",         "-p",      2,    "distance calc exponent"},
44       {"small",     "-s",      .5,    "div list into 'small'"},
45       {"seed",      "-S",      10019, "random number seed"},
46       {"train",     "-t",      .5,    "size of training set"},
47       {"trivial",   "-T",      .35,   "small delta=trivial*sd"},
48       {"todo",     "-I",      "all",  "run unit test, or 'all'"},
49       {"wild",     "-W",      false, "run tests, no protection" }},
50
51 local Seed,cli,the
52 Seed=10019
53 -- If '-x X' appears on command line and '-x default' is in 'how'
54 -- then update default from the command line (and if 'default')
55 -- is false, then set it to true. Also, maybe
56 -- set random number seed and maybe show help string.
57 function cli(opt, u)
58   u={}
59   for _,t in pairs(opt.how) do
60     u[t[1]] = t[3]
61     for n,word in ipairs(arg) do if word==t[2] then
62       u[t[1]] = t[3] and (tonumber(arg[n+1]) or arg[n+1]) or true end end end
63   if u.help
64   then print(string.format("\n%s [OPTIONS]n%s\n%s\n\nOPTIONS:n",
65     arg[0],opt.usage,opt.what))
66     for _,t in pairs(opt.how) do print(string.format("%4s %-9s%W%s %s",
67       t[2], t[3] and t[1] or "", t[4], t[3] and "" or "", t[3] or "")) end
68     print("\n"..opt.about)
69     os.exit()
70   end
71   if u.seed then Seed = u.seed end
72   return u end
73
74 -- Make a global for our options e.g. the = {seed=10019, help=false, p=2...}
75 the = cli(options)
76
77 --
78 --
79 --
80 --
81 --
82 -- ## Table Stuff
83 local randi -- defined later, needed now in "shuffle"
84 local cat,map,lap,keys, last,copy,pop,push,sort,firsts,first,second,shuffle,bchop
85 -- Table to string.
86 cat = table.concat
87 -- Return a sorted table.
88 sort = function(t,f) table.sort(t,f); return t end
89 -- Add to end, pull from end.
90 push = table.insert
91 pop = table.remove
92 -- Return first,second, last item.
93 first = function(t) return t[1] end
94 second = function(t) return t[2] end
95 last = function(t) return t[#t] end
96 -- Function for sorting pairs of items.
97 firsts = function(a,b) return first(a) < first(b) end
98
99 -- Random order of items in a list (sort in place).
100 function shuffle(t, j)
101   for i=#t,2,-1 do j=randi(1,i); t[i],t[j]=t[j],t[i] end; return t end
102
103 -- Collect values, passed through 'f'.
104 function lap(t,f) return map(t,f,1) end
105 -- Collect key,values, passed through 'f'.
106 -- If 'f' returns two values, store as key,value.
107 -- If 'f' returns one values, store at index value.
108 -- If 'f' return nil then add nothing (so 'map' is also 'select').
109 function map(t,f,one, u)
110   u={}; for x,y in pairs(t) do
111     if one then x,y=f(y) else x,y=f(x,y) end
112     if x ~= nil then
113       if y then u[x]=y else u[1+#u]=x end end end
114   return u end
115
116 -- Return a table's keys (sorted).
117 function keys(t,u)
118   u={}
119   for k,_ in pairs(t) do if tostring(k):sub(1,1)~="_" then push(u,k) end end
120   return sort(u) end
121
122 -- Binary chop (assumes sorted lists)
123 function bchop(t,val,lt,lo,hi, mid)
124   lt = lt or function(x,y) return x < y end
125   lo,hi = lo or 1, hi or #t
126   while lo <= hi do
127     mid = (lo+hi) // 2
128     if lt(t[mid],val) then lo=mid+1 else hi= mid-1 end end
129   return math.min(lo,#t) end
130
131 -----
132 -- ## Maths Stuff
133 local abs,norm,sum,rnd,rnds,Seed,rand
134 abs = math.abs
135 -- Round 'x' to 'd' decimal places.
136 function rnd(x,d, n) n=10^(d or 0); return math.floor(x*n+0.5) / n end
137 -- Round list of items to 'd' decimal places.
138 function rnds(t,d) return lap(t, function(x) return rnd(x,d or 2) end) end
139
140 -- Sum items, filtered through 'f'.
141 function sum(t,f)
142   f = f or function(x) return x end
143   out=0; for _,x in pairs(f) do out = out + f(x) end; return out end
144
145 -- Pseudo-random number generator for integers ('randi') or floats ('rand').
146 Seed=937162211
147 function randi(lo,hi) return math.floor(0.5 + rand(lo,hi)) end
148 function rand(lo,hi, mult,mod)
149   lo, hi = lo or 0, hi or 1
150   Seed = (16807 * Seed) % 2147483647
151   return lo + (hi-lo) * Seed / 2147483647 end
152
153 -----
154 -- ## Printing Stuff
155 local out,shout,red,green,yellow,blue,color,fmt
156 fmt = string.format
157 -- Print as red, green, yellow, blue.
158 function color(s,n) return fmt("%27[1m%27[27[32m%27[31m",n,s) end
159 function red(s) return color(s,31) end
160 function green(s) return color(s,32) end
161 function yellow(s) return color(s,34) end
162 function blue(s) return color(s,36) end
163
164 -- Printed string from a nested structure.
165 shout = function(x) print(out(x)) end
166 -- Generate string from a nested structures
167 -- (and don't print any contents more than once).
168 function out(t,seen, u,key,value,public)
169   function key(k) return fmt("%s%s",blue(k),out(t[k],seen)) end
170   function value(v) return out(v,seen) end
171   if type(t) == "function" then return "..." end
172   if type(t) ~= "table" then return tostring(t) end
173   seen = seen or {}
174   if seen[t] then return "..." else seen[t] = t end
175   u = #t>0 and lap(t, value) or lap(keys(t), key)
176   return red((t._is or "").."(")..cat(u," ")..red(")") end
177
178 -----
179 -- ## File i/o Stuff
180 -- Return one table per line, split on commas.
181 local csv
182 function csv(file, line)
183   file = io.input(file)
184   line = io.read()
185   return function( t,tmp)
186     if line then
187       t={}
188       for cell in line:gsub("[\r]*",""):gsub("#.*",""):gmatch("[^\,]+") do
189         push(t, tonumber(cell) or cell) end
190       line = io.read()
191       if #t>0 then return t end
192       else io.close(file) end end end
193
194 -----
195 -- ## OO Stuff
196 local has,obj
197 -- Create an instance
198 function has(mt,x) return setmetatable(x,mt) end
199
200 -- Create a class
201 function obj(s, o,new)
202   o = {_is=s, __tostring=out}
203   o._index = o
204   return setmetatable(o,{__call = function(_,...) return o.new(...) end}) end
205

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206 -- ## Stuff for tracking 'Sym'bol Counts.
207 -- 'Sym's track symbol counts and the 'mode' (most frequent symbol).
208 local Sym=obj{"Sym"}
209 function Sym.new(inits, self)
210   self=has(Sym,{has={}, n=0, mode=nil, most=0})
211   for _,one in pairs(inits or {}) do self:add(one) end
212   return self end
213
214 function Sym:add(x)
215   self.n = self.n + 1
216   self.has[x] = 1 + (self.has[x] or 0)
217   if self.has[x] > self.most then self.most, self.mode = self.has[x], x end end
218
219 function Sym:dist(a,b) return a==b and 0 or 1 end
220 function Sym:mid() return self.mode end
221
222 -- ## Stuff for tracking 'Num'bers.
223 -- 'Num's track a list of number, and can report it sorted.
224 local Num=obj{"Num"}
225 function Num.new(inits, self)
226   self=has(Num,{has={}, n=0, lo=1E32, hi=1E-32, ready=true})
227   for _,one in pairs(inits or {}) do self:add(one) end
228   return self end
229
230 function Num:add(x)
231   if x>self.hi then self.hi = x
232   elseif x<self.lo then self.lo = x end
233   push(self.has,x); self.n=self.n+1; self.ready=false end
234
235 -- Ensure that the returned list of numbers is sorted.
236 function Num:all(x)
237   if not self.ready then table.sort(self.has) end
238   self.ready = true
239   return self.has end
240
241 function Num:dist(a,b)
242   if a=="?" then b=self:norm(b); a = b>.5 and 0 or 1
243   elseif b=="?" then a=self:norm(a); b = a>.5 and 0 or 1
244   else a,b = self:norm(a), self:norm(b) end
245   return abs(a-b) end
246
247 -- Combine two 'num's.
248 function Num:merge(other, new)
249   new = Num.new(self.has)
250   for _,x in pairs(other.has) do new:add(x) end
251   return new end
252
253 -- Return a merged item if that combination
254 -- is simpler than its parts.
255 function Num:mergeable(other, new,b4)
256   new = self:merge(other)
257   b4 = (self.n*self:sd() + other.n*other:sd()) / new.n
258   if b4 >= new:sd() then return new end end
259
260 -- The 'mid' is the 50th percentile.
261 function Num:mid() return self:per(.5) end
262
263 -- Return 'x' normalized 0..1, lo..hi.
264 function Num:norm(x, lo,hi)
265   if x=="?" then return x end
266   lo,hi = self.lo, self.hi
267   return abs(hi - lo) < 1E-32 and 0 or (x - lo)/(hi - lo) end
268
269 -- Return the 'p'-th percentile number.
270 function Num:per(p, t)
271   t = self:all()
272   p = p*#t//1
273   return #t<2 and t[1] or t[p < 1 and 1 or p>#t and #t or p] end
274
275 -- The 10th to 90th percentile is 2.56 times the standard deviation.
276 function Num:sd() return (self:per(.9) - self:per(.1))/ 2.56 end
277
278 -- discretization tricks
279 local splits={}
280 function splits.best(sample, best,tmp,xpect,out)
281   best = maths.huge
282   for _,x in pairs(sample.xs) do
283     tmp, xpect = splits.whatif(x.at,self)
284     if xpect < best
285     then out,best = tmp,xpect end end
286   return out end
287
288 function splits.whatif(col,sample, out)
289   out = splits.spans(col,sample)
290   xpect = sum(out, function(x) return x.has.n*x:sd() end)/#sample.egs
291   out = map(out, function(_,x) x.has=x.has:all(); x.col= col end)
292   return out, xpect end
293
294 function splits.spans(col,sample, xs, symbolic,x)
295   xys,xs, symbolic = {}, Num(), sample.numbers[col]
296   for rank,eg in pairs(sample.egs) do
297     x = eg[col]
298     if x ~="?" then
299       xs:add(x)
300       if symbolic
301       then -- in symbolic columns, xys are the indexes seen with each symbol
302         xys[x] = xys[x] or {}
303         push(xys[x], rank)
304       else -- in numeric columns, xys are each number paired with its row id
305         push(xys, {x=x,y=rank}) end end
306   end
307   if symbolic
308   then return map(xys, function(x,t) return {lo=x, hi=x, has=Num(t)} end)
309   else return splits.merge(
310     splits.div(xys, #xs*the.small, sd(sort(xs))*the.trivial)) end end
311
312 -- Generate a new range when
313 -- 1. there is enough left for at least one more range; and
314 -- 2. the lo,hi delta in current range is not boringly small; and
315 -- 3. there are enough x values in this range; and
316 -- 4. there is natural split here
317 -- Fuse adjacent ranges when:
318 -- 5. the combined class distribution of two adjacent ranges
319 -- is just as simple as the parts.
320 function splits.div(xys, tiny, dull, now,out,x,y)
321   xys = sort(xys, function(a,b) return a.x < b.x end)
322   now = {lo=xys[1].x, hi=xys[1].x, has=Num()}
323   out = {now}
324   for j,xy in pairs(xys) do
325     x, y = xy.x, xy.y
326     if j<#xys-tiny and x==xys[j+1].x and now.has.n>tiny and now.hi-now.lo>dull
327     then now = {lo=x, hi=x, has=Num()}
328     push(out, now) end
329     now.hi = x
330     now.has:add(y) end
331   return out end
332
333 function splits.merge(b4, j,tmp,a,n,simpler)
334   j, n, tmp = 0, #b4, {}
335   while j<n do
336     j = j + 1
337     a = b4[j]
338     if j < n-1 then
339       simpler = a.has:mergeable(b4[j+1].has)
340       if simpler then
341         j = j + 1
342         a = {lo=a.lo, hi= b4[j+1].hi, has=simpler} end end
343     push(tmp,a) end
344   return #tmp==#b4 and b4 or merge(tmp) end
345
346
347
348
349

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349 -- Samples store examples. Samples know about
350 -- (a) lo,hi ranges on the numerics
351 -- and (b) what's here, independent 'x' or dependent 'y' columns.
352 local Sample=obj{"Sample"}
353 function Sample.new(src,self)
354   self = has(Sample,{names=nil, all={}, ys={}, xs={}, egs={}})
355   if src then
356     if type(src)=="string" then for x in csv(src) do self:add(x) end end
357     if type(src)=="table" then for _,x in pairs(src) do self:add(x) end end end
358   return self end
359
360 function Sample:clone(inits,out)
361   out = Sample.new():add(self.names)
362   for _,eg in pairs(inits or {}) do out:add(eg) end
363   return out end
364
365 function Sample:add(eg, name,datum)
366   function name(col,new, weight, where, what)
367     if new:find"." then return end
368     weight= new:find"." and -1 or 1
369     what = (col=col, w=weight, seen=(new:match("^([A-Z])",x) and Num() or Sym()))
370     where = (new:find("+") or new:find("-")) and self.ys or self.xs
371     push(self.all, what)
372     push(where, what)
373   end
374   function datum(one,new)
375     if new ~="?" then one.seen:add(new) end
376   end
377   if not self.names
378   then self.names = eg
379   map(eg, function(col,x) name(col,x) end)
380   else push(self.egs, eg)
381   map(self.all, function(_,col) datum(col,eg[col.col]) end)
382   end
383   return self end
384
385 function Sample:better(eg1,eg2, e,n,a,b,s1,s2)
386   n,s1,s2,e = #self.ys, 0, 0, 2.71828
387   for _,num in pairs(self.ys) do
388     a = num.seen:norm(eg1[num.col])
389     b = num.seen:norm(eg2[num.col])
390     s1 = s1 - e^(num.w * (a-b)/n)
391     s2 = s2 - e^(num.w * (b-a)/n) end
392   return s1/n < s2/n end
393
394 function Sample:betters(egs)
395   return sort(egs or self.egs,function(a,b) return self:better(a,b) end) end
396
397 function Sample:dist(eg1,eg2, a,b,d,n,inc)
398   d,n = 0,0
399   for _,x in pairs(self.xs) do
400     a,b = eg1[x.col], eg2[x.col]
401     inc = a=="?" and b=="?" and 1 or x.seen:dist(a,b)
402     d = d + inc*the.p
403     n = n + 1 end
404   return (d/n)^(1/the.p) end
405
406 function Sample:stats(cols)
407   return lap(cols or self.ys,function(col) return col.seen:mid() end) end
408
409 -- bins his
410 -- bins sorts
411
412 function Sample:tree(min, node,min,sub)
413   node = {node=self, kids={}}
414   min = min or (#self.egs)*the.small
415   if #self.egs >= 2*min then
416     -- here
417     for _,span in pairs(splits.best(sample)) do
418       sub = self:clone()
419       for _,at in pairs(span.has) do sub:add(self.egs[at]) end
420       push(node.kids, span)
421       span.has = sub:tree(min) end end
422   return node end
423
424 -- at node
425 function Sample:where(tree,eg, max,x,default)
426   if #kid.has==0 then return tree end
427   max = 0
428   for _,kid in pairs(tree.node) do
429     if #kid.has > max then default,max = kid,#kid.has end
430     x = eg[kid.col]
431     if x ~="?" then
432       if x <= kid.hi and x >= kid.lo then
433         return self:where(kid.has,eg) end end end
434   return self:where(default, eg) end
435
436

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437 -----
438 -- sample sample sorting
439 local hints={}
440 function hints.default(eg) return eg end
441
442 function hints.sort(sample,score, test,train,evals)
443 sample = Sample.new(the.file)
444 train,test = {}, {}
445 for i,eg in pairs(shuffle(sample.egs)) do
446   push(i<= the.train*#sample.egs and train or test, eg) end
447 evals,train = hints.recurse(sample, train,0,
448   score or hints.default, {}, (#train^the.small)
449   return evals,sample:clone(train), sample:clone(test) end
450
451 function hints.recurse(sample, eggs, evals, scorefun, out, small, worker)
452 if #egs < small then
453   for i=1, #egs do push(out, pop(egs)) end
454   return evals,out
455 end
456 local scores = {}
457 function worker(eg) return hints.locate(scores,eg,sample) end
458 for j=1,the.hints do evals=evals+1;
459   push(scores, scorefun(pop(egs))) end
460 scores = sample:betters(scores)
461 eggs = lap(sort(lap(egs, worker),firsts),second)
462 print(the.cull*#egs)
463 for i=1,the.cull*#egs//1 do push(out, pop(egs)) end
464 return hints.recurse(sample, eggs,evals, scorefun, out, small) end
465
466 function hints.locate(scores,eg,sample, closest,rank,tmp)
467 closest, rank, tmp = IE32, IE32, nil
468 for rank0, scored in pairs(scores) do
469   tmp = sample:dist(eg, scored)
470   if tmp < closest then closest,rank = tmp,rank0 end end
471 return {rank, eg} end
472 --return {rank+closest/10^6, eg} end
473
474
475

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476 --
477 -- elene
478 -----
479
480 local eg,fail,example={},0
481 function example(k, f,ok,msg)
482 f= eg[k]; assert(f,"unknown action"..k)
483 the=cli(options)
484 if the.wild then return f() end
485 ok,msg = pcall(f)
486 if ok then print(green("PASS"),k)
487 else print(red("FAIL"), k,msg); fail=fail+1 end end
488
489 function eg.shuffle( t)
490 t={}
491 for i=1,32 do push(t,i) end
492 assert(#t == #shuffle(t) and t[1] ~= shuffle(t)[1]) end
493
494 function eg.lap()
495 assert(3==lap({1,2},function(x) return x+1 end)[2]) end
496
497 function eg.map()
498 assert(3==map({1,2},function(_,x) return x+1 end)[2]) end
499
500 function eg.tables()
501 assert(20==sort(shuffle({{10,20},{30,40},{40,50}}),firsts)[1][2]) end
502
503 function eg.csv( n,z)
504 n=0
505 for eg in csv(the.file) do n=n+1; z=eg end
506 assert(n==399 and z[#z]==50) end
507
508 function eg.rnds( t)
509 assert(10.2 == first(rnds({10.22,81.22,22.33},1))) end
510
511 function eg.sym( s)
512 s=Sym("a","a","a","a","b","b","c")
513 assert("a"==s.mode) end
514
515 function eg.num1( n)
516 n=Num(10,20,30,40,50,10,20,30,40,50,10,20,30,40,50)
517 assert(.375 == n:norm(25))
518 assert(15.625 == n:sd()) end
519
520 function eg.num2( n1,n2,n3,n4)
521 n1=Num(10,20,30,40,50,10,20,30,40,50,10,20,30,40,50)
522 n2=Num(10,20,30,40,50,10,20,30,40,50,10,20,30,40,50)
523 assert(n1:mergeable(n2)==nil)
524 n3=Num(10,20,30,40,50,10,20,30,40,50,10,20,30,40,50)
525 n4=Num(100,200,300,400,500,100,200,300,400,500,100,200,300,400,500)
526 assert(n3:mergeable(n4)==nil) end
527
528 function eg.sample( s,tmp,d1,d2,n)
529 s=Sample(the.file)
530 assert(2110 == last(s.egs)[s.all[3].col])
531 local sortl= s:betters(s.egs)
532 local lo, hi = s:clone(), s:clone()
533 for i=1,20 do lo:add(sortl[i]) end
534 for i=#sortl,#sortl-30,-1 do hi:add(sortl[i]) end
535 shout(s:stats())
536 shout(lo:stats())
537 shout(hi:stats())
538 for m,eg in pairs(sortl) do
539   n = bchop(sortl, eg,function(a,b) return s:better(a,b) end)
540   assert(m-n <=2) end end
541
542 function eg.dists( s,tmp,d1,d2,n)
543 s=Sample(the.file)
544 tmp = sort(lap(shuffle(s.egs),
545   function(eg2) return {s:dist(eg2,s.egs[1]), eg2} end),
546   firsts)
547 d1=s:dist(tmp[1][2], tmp[10][2])
548 d2=s:dist(tmp[1][2], tmp[#tmp][2])
549 assert(d1*10<d2)
550
551 end
552
553 function eg.hints( s,_,_,evals,sortl,train)
554 s=Sample(the.file)
555 --for _,eg in pairs(sortl) do lap(s.ys, function(col) return eg[col.col] end ) end
556 -- assert(s.ys[4].lo==1613)
557 evals, train,test = hints.sort(s)
558 print("=",evals)
559 test.egs = test:betters()
560 for m,eg in pairs(test.egs) do
561   n = bchop(train.egs, eg,function(a,b) return s:better(a,b) end)
562   print(m,n) end
563 end
564
565 if the.todo=="all" then lap(keys(eg),example) else example(the.todo) end
566
567 -----
568 -- trick for checking for rogues.
569 for k,v in pairs(_ENV) do if not b4[k] then print("?rogue: ",k,type(v)) end end
570 os.exit(fail)
571
572
573

```

```
574 --[[
575 --  seems to be  a revers that i  need to do .... but dont
576
577 teaching:
578 - sample is v.useful
579
580
581 --]]
```