

```

1  #!/usr/bin/env lua
2  --
3  --
4  --
5  -- a little lite
6  -- ZWA learning
7  -- library
8  --
9  --
10 --
11 --
12 --
13 --
14 --
15 --
16 --
17 --
18 local it=require"options"
19 what = "Small sample multi-objective optimizer.",
20 who = "(c) 2021 Tim Menzies <tim@ieee.org> unlicense.org",
21 why = {}
22 Sort N examples on multi-goals using a handful of 'hints'; i.e.
23
24 - Evaluate and rank, a few examples (on their y-values);
25 - Sort other examples by x-distance to the ranked ones;
26 - Recurse on the better half (so we sample more and more
27   from the better half, then quarter, then eighth...).
28
29 A regression tree learner then explores the examples (sorted
30 left to right, worst to best). By finding branches that
31 reduce the variance of the index of those examples, this
32 tree reports what attribute ranges select for the better (or
33 worse) examples.  ]],
34
35 how={{"FILE",      "-f",      ".data/au93.csv",    "read data from file"},
36       {"CULL",     "-c",      .5,      "cuts per generation"},
37       {"HELP",     "-h",      false,    "show help"},
38       {"HINTS",    "-H",      4,      "hints per generation"},
39       {"P",        "-p",      2,      "distance calc exponent"},
40       {"TINY",     "-t",      .5,      "div list into 'small'"},
41       {"SEED",     "-S",      10019,    "random number seed"},
42       {"TRAIN",    "-i",      .5,      "size of training set"},
43       {"TODO",     "-T",      "all",    "run unit test, or 'all'"},
44       {"TRIVIAL",  "-v",      .35,     "small delta=trivial*sd"},
45       {"WILD",     "-W",      false,   "run tests, no protection"}},
46
47 local _=require"lib"
48 local abs,bchop,cut,copy = _abs, _bchop, _cat, _copy
49 local csv,first,firsts,fmt,has = _csv, _first, _firsts, _fmt, _has
50 local keys,last,lap,map,obj = _keys, _last, _lap, _map, _obj
51 local out,pop,push,rand,shout = _out, _pop, _push, _rand, _shout
52 local rnd,rnds,roques,second = _rnd, _rnds, _roques, _second
53 local shuffle,sort,sum,top = _shuffle, _sort, _sum, _top
54
55 --[[
56 Spans
57   Little languages:
58   - options
59   - data language
60
61 Lesson plan
62 -- w1: ssystems: github. github workplaces. unit tests. doco tools.
63 -- w2: num, sym
64 -- w3: sample
65 -- w4: eval, knn, unfairness
66 -- w5:
67 --]]

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```

68 -- NUM -----
69 --
70 --
71 -- ## Stuff for tracking 'Num'bers.
72 -- 'Num's track a list of number, and can report it sorted.
73 local Num=obj"Num"
74 function Num.new(inits,at,txt, self)
75   self=has(Num,{at=at or 0, txt=txt or "", w=(txt or ""):find"--" and -1 or 1,
76     has={}, n=0, lo=1E32, hi =1E-32, ready=true})
77   for _,one in pairs(inits or {}) do self:add(one) end
78   return self end
79
80 function Num:add(x)
81   if x>self.hi then self.hi = x
82   elseif x<self.lo then self.lo = x end
83   push(self.has,x); self.n=self.n+1; self.ready=false end
84
85 -- Ensure that the returned list of numbers is sorted.
86 function Num:all(x)
87   if not self.ready then table.sort(self.has) end
88   self.ready = true
89   return self.has end
90
91 function Num:dist(a,b)
92   if a=="?" then b=self:norm(b); a = b>.5 and 0 or 1
93   elseif b=="?" then a=self:norm(a); b = a>.5 and 0 or 1
94   else a,b = self:norm(a), self:norm(b) end
95   return abs(a-b) end
96
97 -- Combine two 'num's.
98 function Num:merge(other, new)
99   new = Num()
100   new.at, new.txt = self.at, self.txt
101   for _,x in pairs(self.has) do new:add(x) end
102   for _,x in pairs(other.has) do new:add(x) end
103   return new end
104
105 -- The 'mid' is the 50th percentile.
106 function Num:mid() return self:per(.5) end
107
108 -- Return 'x' normalized 0..1, lo..hi.
109 function Num:norm(x, lo,hi)
110   if x=="?" then return x end
111   lo,hi = self.lo, self.hi
112   return abs(hi - lo) < 1E-32 and 0 or (x - lo)/(hi - lo) end
113
114 -- Return the 'p'-th percentile number.
115 function Num:per(p, t)
116   t = self:all()
117   p = p*#t//1
118   return #t<2 and t[1] or t[p < 1 and 1 or p>#t and #t or p] end
119
120 -- The 10th to 90th percentile range is 2.56 times the standard deviation.
121 function Num:sd() return self:per(.9) - self:per(.1)/ 2.56 end
122 function Num:spread() return self:sd() end
123
124 -- Create one span (each has the row indexes of the rows)
125 -- where each span has at least 'tiny' items and span is more than
126 -- 'trivially' small.
127 local div -- defined below
128 function Num:spans(sample,tiny,trivial)
129   local xys = {}
130   for _,eg in pairs(sample.egs) do
131     local x = eg[self.at]
132     if x == "?" then push(xys, {col=col, x=x, y=eg[sample.klass.at]}) end end
133   return div(xys, tiny, trivial, self, getmetatable(sample.klass)) end
134
135 -- SYM -----
136 --
137 --
138 -- Stuff for tracking 'Sym'bol Counts.
139 -- 'Sym's track symbol counts and the 'mode' (most frequent symbol).
140 local Sym=obj"Sym"
141 function Sym.new(inits,at,txt, self)
142   self=has(Sym,{at=at or 0, txt=txt or "", has={}, n=0, mode=nil, most=0})
143   for _,one in pairs(inits or {}) do self:add(one) end
144   return self end
145
146 function Sym:add(x,n)
147   n = n or 1
148   self.n = self.n + n
149   self.has[x] = n + (self.has[x] or 0)
150   if self.has[x] > self.most then self.most, self.mode = self.has[x], x end end
151
152 function Sym:dist(a,b) return a==b and 0 or 1 end
153
154 function Sym:merge(other)
155   new=Sym()
156   new.at, new.txt = self.at, self.txt
157   for k,n in pairs(self.has) do new:add(k,n) end
158   for k,n in pairs(other.has) do new:add(k,n) end
159   return new end
160
161 function Sym:mid() return self.mode end
162
163 -- Create one span holding row indexes associated with each symbol
164 function Sym:spans(sample,...)
165   local xys,yklass = {}, getmetatable(sample.klass)
166   for pos,eg in pairs(sample.egs) do
167     local x = eg[self.at]
168     if x == "?" then
169       xys[x] = xys[x] or yklass()
170       xys[x]:add(eg[sample.klass.at]) end end
171   return map(xys, function(x,ys) return {col=self, lo=x, hi=x, has=ys} end) end
172
173 function Sym:spread()
174   return sum(self.has,
175     function(nl) return -nl/self.n * math.log(nl/self.n,2) end) end
176
177 -- SKIP -----
178 --
179 -- ## Stuff for skipping all things sent to a column
180 local Skip=obj"Skip"
181 function Skip.new(_,at,txt) return has(Skip,{at=at or 0, txt=txt or "", n=0}) end
182 function Skip:add(x) self.n = self.n + 1; return x end
183 function Skip:mid() return "?" end

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184 -- SAMPLE -----
185 --
186 -- Samples store examples. Samples know about
187 -- (a) lo,hi ranges on the numerics
188 -- and (b) what are independent 'x' or dependent 'y' columns.
189 local Sample = {}
190 function Sample.new( src,self)
191   self = has(Sample,{names=nil, klass=nil, all={}, ys={}, xs={}, eggs={})
192   if src then
193     if type(src)=="string" then for x in csv(src) do self:add(x) end end
194     if type(src)=="table" then for _,x in pairs(src) do self:add(x) end end end
195   return self end
196
197 function Sample:add(eg, ako,what,xy)
198   if not self.names
199   then -- create the column headers
200     self.names = eg
201     for at,x in pairs(eg) do
202       ako = (x:find(".*") and Skip) or
203             (x:match("[A-Z]" and Num) or
204              Sym
205             )
206       what = push(self.all, ako({}, at, x))
207       if not x:find(".*") then
208         if x:find(".*") then self.klass = what end
209         xy = (x:find(".*") or x:find(".*") or x:find(".*") and self.ys or self.xs
210         push(xy, what) end end
211     else -- store another example; update column headers
212       push(self.egs, eg)
213       for at,x in pairs(eg) do if x ~= "?" then self.all[at]:add(x) end end end
214     return self end
215
216 function Sample:better(eg1,eg2, e,n,a,b,s1,s2)
217   n,s1,s2,e = #self.ys, 0, 0, 2.71828
218   for _,num in pairs(self.ys) do
219     a = num:norm(eg1[num.at])
220     b = num:norm(eg2[num.at])
221     s1 = s1 - e^(num.w * (a-b)/n)
222     s2 = s2 - e^(num.w * (b-a)/n) end
223   return s1/n < s2/n end
224
225 function Sample:betters(egs)
226   return sort(egs or self.egs,function(a,b) return self:better(a,b) end) end
227
228 function Sample:clone( inits,out)
229   out = Sample.new({}):add(self.names)
230   for _,eg in pairs(inits or {}) do out:add(eg) end
231   return out end
232
233 function Sample:dist(eg1,eg2, a,b,d,n,inc)
234   d,n = 0,0
235   for _,col in pairs(self.xs) do
236     a,b = eg1[col.at], eg2[col.at]
237     inc = a=="?" and b=="?" and 1 or col:dist(a,b)
238     d = d + inc*it.P
239     n = n + 1 end
240   return (d/n)^(1/it.P) end
241
242 -- Report mid of the columns
243 function Sample:mid(cols)
244   return lap(cols or self.ys,function(col) return col:mid() end) end
245
246 -- Return spans of the column that most reduces variance
247 function Sample:bestSplits(tiny, trivials)
248   local function(x,col, total,xpect,spans,total,xpect)
249     local function xpect1(span) return span.has.n/total * span.has:spread() end
250     spans = col:spans(self, tiny,trivials[col.at])
251     total = sum(spans,function(span) return span.has.n end)
252     xpect = sum(spans, xpect1)
253     return {xpect, spans}
254   end
255   return first(sort(lap(self.xs, column1), firsts))[2] end
256
257 -- Split on column with best span, recurse on each split.
258 function Sample:tree(tiny,trivials,pre, node,new,x)
259   pre=pre or ""
260   print(pre ..".".#self.egs)
261   tiny = tiny or (#self.egs)^it.TINY
262   trivials = trivials or map(self.xs,
263     function(_,x)
264       return x.at,it.TRIVIAL*x:spread() end)
265   node = {node=self, kids={}}
266   if #self.egs <= 2*tiny then print(333333);return node end
267   for _,span in pairs(self:bestSplits(tiny,trivials)) do
268     new = self:clone()
269     for _,eg in pairs(self.egs) do
270       x = eg[span.col.at]
271       if x=="?" or (span.lo <= x and x <= span.hi) then new:add(eg) end end
272     if #new.egs < #self.egs then
273       push(node.kids, {txt = span.col.txt, txt= span.col.at,
274         lo = span.lo, hi = span.hi,
275         sub = new:tree(tiny,trivials,pre..["."..span.col.at]) end end
276       --os.exit()
277       --end end
278     return node end
279
280 -- Find which leaf best matches an example 'eg'.w
281 function Sample:where(tree,eg, max,x,default)
282   if #kid.has==0 then return tree end
283   max = 0
284   for _,kid in pairs(tree.node) do
285     if #kid.has > max then default,max = kid,#kid.has end
286     x = eg[kid.at]
287     if x == "?" then
288       if x <= kid.hi and x >= kid.lo then
289         return self:where(kid.has.eg) end end end
290   return self:where(default, eg) end
291

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292 -- DISCRIMINATION -----
293 --
294 -- Input a list of {(x,y)..} values. Return spans that divide the 'x' values
295 -- to minimize variance on the 'y' values.
296 -- local div -- do not uncommment. 'div' was declared local above for 'Num:spans'.
297 local mergeable,merge
298
299 -- Return a list of 'spans' (lo=hi,col=col).
300 -- Sort the list of pairs 'xys' then split it into 'spans' of cardinality at
301 -- least 'tiny'. Ensure that the max-min of each span is more than 'trivial'.
302 function div(xys, tiny, trivial,col,yklass)
303   xys = sort(xys, function(a,b) return a.x < b.x end)
304   local tenth=#xys/10
305   trivial = trivial or it.TRIVIAL*(xys[9*tenth][1] - xys[tenth][1])/2.56
306   tiny = tiny or it.TINY*#xys
307   yklass = yklass or Num
308   local spans,span
309   span = {col=col,lo=xys[1].x, hi=xys[1].x, has=yklass()}
310   spans = {span}
311   for j,xy in pairs(xys) do
312     local x, y = xy.x, xy.y
313     if j < #xys - tiny and -- enough items remaining after split
314        x ~= xys[j+1].x and -- next item is different (so can split here)
315        span.has.n > tiny and -- span has enough items
316        span.hi - span.lo > trivial -- span is not trivially small
317     then
318       span = push(spans, {col=col, lo=span.hi, hi=x, has=yklass()}) -- then new span
319     end
320     span.hi = x
321     span.has:add(y) end
322   first(spans).lo = -math.huge
323   last(spans).hi = math.huge
324   return merge(spans) end
325
326 function mergeable(a,b, new,b4)
327   new = a:merge(b)
328   b4 = {a.n*a:spread() + b.n*b:sd()} / new.n
329   if new:spread() <= b4 then return new end
330   end
331
332 -- Merge adjacent spans if the combo is simpler than the parts.
333 function merge(b4)
334   local j, tmp = 0, {}
335   while j < #b4 do
336     j = j + 1
337     local now, after = b4[j], b4[j+1]
338     if after then
339       local simpler = mergeable(now.has, after.has)
340       if simpler then
341         now = {col=col, lo=now.lo, hi= after.hi, has=simpler}
342         j = j + 1 end end
343     push(tmp,now) end
344   return #tmp==#b4 and b4 or merge(tmp) -- recurse until nothing merged
345   end
346

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348 -- HINTING
349 --
350 -- Sorting on a few y values
351 local hints={}
352 function hints.default(eg) return eg end
353
354 function hints.sort(sample,scorefun, test,train,egs,scored,small)
355   sample = Sample.new(it.FILE)
356   train,test = {}, {}
357   for i,eg in pairs(shuffle(sample.egs)) do
358     push(i<= it.TRAIN*#sample.egs and train or test, eg) end
359   egs = copy(train)
360   small = (#egs)^it.TINY
361   local i=0
362   scored = {}
363   while #egs >= small do
364     local tmp={}
365     i = i + 1
366     io.stderr:write(fmt("%s",string.char(96+i)))
367     for j=1,it.HINTS do
368       egs[j] = (scorefun or hints.default)(egs[j])
369       push(tmp, push(scored, egs[j]))
370     end
371     egs = hints.ranked(scored,egs,sample)
372     for i=1,it.CULL*#egs//1 do pop(egs) end
373   end
374   io.stderr:write("\n")
375   train=hints.ranked(scored, train, sample)
376   return #scored, sample:clone(train), sample:clone(test) end
377
378 function hints.ranked(scored,egs,sample,worker, some)
379   function worker(eg) return {hints.rankOfClosest(scored,eg,sample),eg} end
380   scored = sample:betters(scored)
381   return lap(sort(lap(egs, worker),firsts),second) end
382
383 function hints.rankOfClosest(scored,egl,sample, worker,closest)
384   function worker(rank,eg2) return {sample:dist(egl,eg2),rank} end
385   closest = first(sort(map(scored, worker),firsts))
386   return closest[2] end --+ closest[1]/10^8 end

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387 -- demos
388 it._eg={}
389 it._no={}
390 function it._eg.shuffle( t,u,v)
391   t={}
392   for i=1,32 do push(t,i) end
393   u = shuffle(copy(t))
394   v = shuffle(copy(t))
395   assert(#t == #u and u[1] ~= v[1]) end
396
397 function it._eg.lap()
398   assert(3==lap({1,2},function(x) return x+1 end)[2]) end
399
400 function it._eg.map()
401   assert(3==map({1,2},function(_,x) return x+1 end)[2]) end
402
403 function it._eg.tables()
404   assert(20==sort(shuffle({{10,20},{30,40},{40,50}}),firsts)[1][2]) end
405
406 function it._eg.csv( n,z)
407   n=0
408   for eg in csv(it.FILE) do n=n+1; z=eg end
409   assert(n==399 and z[#z]==50) end
410
411 function it._eg.rnds( t)
412   assert(10.2 == first(rnds({10.22,81.22,22.33},1))) end
413
414 function it._eg.sym( s)
415   s=Sym{"a","a","a","a","b","b","b","c"}
416   assert("a"==s.mode) end
417
418 function it._eg.numl( n)
419   n=Num(10,20,30,40,50,10,20,30,40,50,10,20,30,40,50)
420   assert(1.375 == n:norm(25))
421   assert(15.625 == n:sd()) end
422
423 function it._eg.sample( s,tmp,d1,d2,n)
424   s=Sample(it.FILE)
425   assert(2110 == last(s.egs)[s.all[4].at])
426   local sortl= s:betters(s.egs)
427   local lo, hi = s:clone(), s:clone()
428   for i=1,20 do lo:add(sortl[i]) end
429   for i=#sortl,#sortl-20,-1 do hi:add(sortl[i]) end
430   shout(s:mid())
431   shout(lo:mid())
432   shout(hi:mid())
433   for m,eg in pairs(sortl) do
434     n = bchop(sortl, eg,function(a,b) return s:better(a,b) end)
435     assert(m-n <=2) end end
436
437 function it._eg.dists( s,tmp,d1,d2,n)
438   s=Sample(it.FILE)
439   tmp = sort(lap(shuffle(s.egs),function(eg2) return (s:dist(eg2,s.egs[1]), eg2) end),firsts)
440   d1=s:dist(tmp[1][2], tmp[10][2])
441   d2=s:dist(tmp[1][2], tmp[#tmp][2])
442   assert(d1*10 < d2) end
443
444 function it._eg.hints( s,_,_,evals,sortl,train,test,n)
445   s = Sample(it.FILE)
446   evals, train,test = hints.sort(s)
447   test.egs = test:betters()
448   for m,eg in pairs(test.egs) do
449     n = bchop(train.egs, eg,function(a,b) return s:better(a,b) end); end end
450
451 function it._eg.dump()
452   shout(it) end
453 function it._eg.tree( s,t,u,egl,evals,ordered,rest)
454   s = Sample(it.FILE)
455   t = copy(s.names)
456   push(t,"Rank")
457   u = Sample.new():add(t)
458   evals, ordered,rest = hints.sort(s)
459   for m,eg in pairs(ordered.egs) do
460     egl = copy(eg)
461     push(egl,m)
462     u:add(egl) end
463   print(1)
464   u:tree() end
465
466 -- START-UP
467 it(demos=it._eg, nervous=true)

```

```
472 --[[
473   |  |  |
474   |  |  |
475
476 Spans
477 Little languages:
478   - options
479   - data language
480
481 Lesson plan
482 - w1: ssystems: github. github workplaces. unit tests. doco tools.
483
484 - w2: num, sym
485 - W3: sample
486 - w4: eval, knn, unfairnessness
487 - W5:
488
489 - seems to be a revers that i need to do .... but dont
490 - check if shuffle is working
491
492 teaching:
493 - sample is v.useful
494 --]]
495
```

```

1  local lib={}
2
3  --- ROGUES ---
4  ---
5  --- Call 'rogues', last thing, to find escaped locals.
6  lib._b4={}; for k,v in pairs(_ENV) do lib._b4[k]=k end
7  function lib.rogues()
8      for k,v in pairs(_ENV) do
9          if not lib._b4[k] then print("?rogue: ",k,type(v)) end end end
10
11  --- OBJECTS ---
12  ---
13  --- Create an instance
14  function lib.has(mt,x) return setmetatable(x,mt) end
15  --- Create a class
16  function lib.obj(s, o,new)
17      o = {__is=s, __tostring=lib.out}
18      o.__index = o
19      return setmetatable(o,{__call = function(_,...) return o.new(...) end}) end
20
21  --- RANDOM ---
22  ---
23  lib.Seed = 10019
24  --- random integers
25  function lib.randi(lo,hi) return math.floor(0.5 + lib.rand(lo,hi)) end
26  --- random floats
27  function lib.rand(lo,hi, mult,mod)
28      lo, hi = lo or 0, hi or 1
29      lib.Seed = (16807 * lib.Seed) % 2147483647
30      return lo + (hi-lo) * lib.Seed / 2147483647 end
31
32  --- MATHS ---
33  ---
34  lib.abs = math.abs
35  --- Round 'x' to 'd' decimal places.
36  function lib.rnd(x,d, n) n=10^(d or 0); return math.floor(x*n+0.5) / n end
37  --- Round list of items to 'd' decimal places.
38  function lib.rnds(t,d)
39      return lib.lap(t, function(x) return lib.rnd(x,d or 2) end) end
40
41  --- Sum items, filtered through 'f'.
42  function lib.sum(t,f, out)
43      f = f or function(x) return x end
44      out=0; for _,x in pairs(t) do out = out + f(x) end; return out end
45
46  --- FILES ---
47  ---
48  --- Return one table per line, split on commas.
49  function lib.csv(file, line)
50      file = io.input(file)
51      line = io.read()
52      return function()
53          if line then
54              t={}
55              for cell in line:gsub("[\r\n]", ""):gsub("#", ""):gmatch("[^\r\n,]+") do
56                  lib.push(t, tonumber(cell) or cell) end
57              line = io.read()
58              if #t>0 then return t end
59              else io.close(file) end end end
60
61  --- PRINTING ---
62  ---
63  lib.fmt = string.format
64  lib.say = function(...) print(lib.fmt(...)) end
65
66  --- Print as red, green, yellow, blue.
67  function lib.color(s,n) return lib.fmt("%27[1m27[%sm%s27[0m",n,s) end
68  function lib.red(s) return lib.color(s,31) end
69  function lib.green(s) return lib.color(s,32) end
70  function lib.yellow(s) return lib.color(s,34) end
71  function lib.blue(s) return lib.color(s,36) end
72
73  --- Printed string from a nested structure.
74  lib.shout = function(x) print(lib.out(x)) end
75  --- Generate string from a nested structures
76  --- (and don't print any contents more than once).
77  function lib.out(t,seen, u,key,value,public)
78      function key(k) return lib.fmt("%s %s", lib.blue(k), lib.out(t[k],seen)) end
79      function value(v) return lib.out(v,seen) end
80      if type(t) == "function" then return "(...)" end
81      if type(t) ~= "table" then return tostring(t) end
82      seen = seen or {}
83      if seen[t] then return "..." else seen[t] = t end
84      u = #t>0 and lib.lap(t, value) or lib.lap(lib.keys(t), key)
85      return lib.red((t._is or "").."["..lib.cat(u,"")..lib.red("]") end
86
87  --- TABLE ---
88  ---
89  --- Table to string.
90  lib.cat = table.concat
91  --- Return a sorted table.
92  lib.sort = function(t,f) table.sort(t,f); return t end
93  --- Return first, second, last item
94  lib.first = function(t) return t[1] end
95  lib.second = function(t) return t[2] end
96  lib.last = function(t) return t[#t] end
97  --- Function for sorting pairs of items.
98  lib.firsts = function(a,b) return a[1] < b[1] end
99  --- Add to end, pull from end.
100 lib.pop = table.remove
101 lib.push = function(t,x) table.insert(t,x); return x end
102
103 --- Random order of items in a list (sort in place).
104 function lib.shuffle(t, j)
105     for i=#t,2,-1 do j=lib.randi(1,i); t[i],t[j]=t[j],t[i] end; return t end
106
107 --- Collect values, passed through 'f'.
108 function lib.lap(t,f) return lib.map(t,f,1) end
109 --- Collect key, values, passed through 'f'.
110 --- If 'f' returns two values, store as key, value.
111 --- If 'f' returns one values, store at index value.
112 --- If 'f' return nil then add nothing (so 'map' is also 'select').
113 function lib.map(t,f,one)
114     u={}; for k,v in pairs(t) do
115         if one then x,y=f(y) else x,y=f(x,y) end
116         if x ~= nil then
117             if y then u[x]=y else u[1+#u]=x end end end
118     return u end
119
120 --- Shallow copy
121 function lib.copy(t, u) u={}; for k,v in pairs(t) do u[k]=v end; return u end
122
123 function lib.top(t,n, u)
124     u={};for k,v in pairs(t) do if k>n then break end; push(u,v) end; return u;end
125
126 --- Return a table's keys (sorted).
127 function lib.keys(t,u)
128     u={}
129     for k,_ in pairs(t) do if tostring(k):sub(1,1)~="_" then lib.push(u,k) end end
130     return lib.sort(u) end
131
132 --- Binary chop (assumes sorted lists)
133 function lib.bchop(t, val, lt, lo, hi, mid)
134     lt = lt or function(x,y) return x < y end
135     lo, hi = lo or 1, hi or #t
136     while lo <= hi do
137         mid = (lo+hi) // 2
138         if lt(t[mid], val) then lo=mid+1 else hi= mid-1 end end
139     return math.min(lo, #t) end
140
141 -----
142 return lib

```