# TREE

### **Depth-First Traversals**

• **Pre-order**: Root – Left – Right



• In-order: Left - Root - Right



• **Post-order**: Left – Right – Root



### **Breadth-First Traversal (Level Order Traversal)**

Visit every node on a level before moving to a lower level.

### **Depth-First Traversals**

Use a recursive algorithm to traverse according to the order

if (!root) return; • **Pre-order**: Root – Left – Right doSomething(); visit(node->left); visit(node->right); if (!root) return; • In-order: Left – Root – Right visit(node->left); doSomething(); visit(node->right); if (!root) return; • **Post-order**: Left – Right – Root visit(node->left); visit(node->right);

doSomething();

### **Example of pre-order and in-order**

```
struct TreeNode {
    int val;
    TreeNode *left, *right;
    TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
};
// Pre-order traversal
void preorderTraversal(TreeNode* root) {
    if (root == nullptr) return;
    cout << root->val << " ";</pre>
    preorderTraversal(root->left);
    preorderTraversal(root->right);
// In-order traversal
void inorderTraversal(TreeNode* root) {
    if (root == nullptr) return;
    inorderTraversal(root->left);
    cout << root->val << " ";</pre>
    inorderTraversal(root->right);
```

### **Example of post-order and level-order**

```
struct TreeNode {
    int val;
    TreeNode *left, *right;
    TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
};
// Post-order traversal
void postorderTraversal(TreeNode* root) {
    if (root == nullptr) return;
    postorderTraversal(root->left);
    postorderTraversal(root->right);
    cout << root->val << " ";</pre>
// Level-order traversal using a queue
void levelOrderTraversal(TreeNode* root) {
    if (root == nullptr) return;
    queue<TreeNode*> q;
    q.push(root);
    while (!q.empty()) {
        TreeNode* current = q.front();
        q.pop();
        cout << current->val << " ";</pre>
        if (current->left != nullptr) q.push(current->left);
        if (current->right != nullptr) q.push(current->right);
```

# **BFS Using Stack**

#### **BFS** with std::stack

 This might be useful for problems when you want to return and resume (for example, <u>872. Leaf-Similar Trees</u>)

```
struct TreeNode {
    int val;
    TreeNode *left, *right;
    TreeNode(int x) : val(x), left(nullptr), right(nullptr) {}
};

// Pre-order traversal
void bfs(std::stack<TreeNode*>& tree) {
    while(!tree.empty()) {
        TreeNode* root = tree.top();
        tree.pop();
        // do something ...
        if (root->right) tree.push(root->right);
        if (root->left) tree.push(root->left);
    }
}
```





LeetCode https://leetcode.com/problems/maximum-depth-of-binary-tree

#### **Problem Statement**

- Given the root of a binary tree, find the <u>maximum depth</u>
- Example:

Output: 4



# Solution – Maximum Depth of Binary Tree



LeetCode https://leetcode.com/problems/maximum-depth-of-binary-tree

### **Solution**

- Perform post-order traversal: left right root
- Recursively go left and right to find each value
- Return the max of each one

# Code – Maximum Depth of Binary Tree

LeetCode https://leetcode.com/problems/maximum-depth-of-binary-tree

```
int maxDepth(TreeNode* root) {
   if (!root) return 0;
   // find max left
   int maxLeft = maxDepth(root->left);
   // find max right
   int maxRight = maxDepth(root->right);
   // return max +1 (account for root)
   return max(maxLeft, maxRight) + 1;
```



leetcode.com/problems/same-tree

### **Problem**

- You are given the root of two trees
- Write a function to check if they are the same
- Example:

$$p = [1,2,3], q = [1,2,3]$$

Output: true



leetcode.com/problems/same-tree

#### **Solution**

- Traverse both trees (**p** and **q**) recursively and check if the nodes are the same
- Start by the base case:are **p** and **q** null? return true
- One of them are null? return false, because they should be the same
- Finally, check if p->val is equal to q->val and also for both and left, recursively

# Code - 100. Same Tree



leetcode.com/problems/same-tree

Code

Time: O(n) where n is the number of nodes Space: O(h) where h is the height of the tree. Best case is usually O(log n) for balanced trees, but skewed trees is usually O(n)

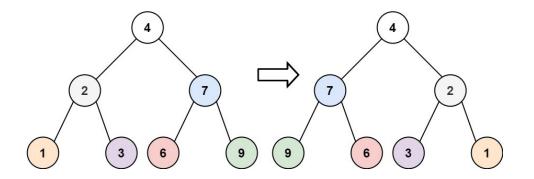
```
bool isSameTree(TreeNode* p, TreeNode* q) {
    // base case: leaf is null. If both are null, then return true
    if (!p && !q) return true;
    // if both are not NULL, then they must have value.
    // If one of them doesn't have value, then they're different, return false
    if (!p || !q) return false;
    // they must have the same value
    // as any other nodes in the tree
    return p->val == q->val &&
        isSameTree(p->left, q->left) &&
        isSameTree(p->right, q->right);
}
```



leetcode.com/problems/invert-binary-tree

### **Problem**

- You are given the root of a binary tree
- Invert the tree and return the root
- Example:







leetcode.com/problems/invert-binary-tree

#### **Solution**

- Recursively traverse the tree
- Create a new pointer temp that points to left node
- Set left node to right
- Set right node to temp
- Call the function recursively for left and right
- Return root

# Code - 226. Invert Binary Tree

```
E LeetCode
```

leetcode.com/problems/invert-binary-tree

```
Time: O(n) Space: O(h) where h is the height of the tree
Code
TreeNode* invertTree(TreeNode* root) {
    // base case
    if (!root) return nullptr;
    // create a new pointer to left
    TreeNode* temp = root->left;
    // invert
    root->left = root->right;
    root->right = temp;
    // recursively invert left and right
    invertTree(root->left);
    invertTree(root->right);
    return root;
```



https://leetcode.com/problems/path-sum

#### **Problem Statement**

- It is given the root of a binary tree and an integer target sum
- Example:



Output: true

Node 
$$1 + Node 7 + Node 2 = 10$$





https://leetcode.com/problems/path-sum

### **Solution**

- Start from root node (1)
- Subtract from target number (example 10 1 = 9)
- Continue going down the tree, until the target is 0, return true
- After visiting all nodes, if the target is not zero, return false



# Code – Path Sum

```
E LeetCode
```

https://leetcode.com/problems/path-sum

```
bool hasPathSum(TreeNode* root, int targetSum) {
    if (!root) {
        return false;
    // we want targetSum to be zero
   targetSum -= root->val;
   // if there is no left, no right, we've reached the end of the path
    // so if the targetSum is zero, then the nodes summed up to the targetSum
    if (!root->left && !root->right && targetSum == 0) {
        return true;
    // propagate to left and right
    return hasPathSum(root->left, targetSum) || hasPathSum(root->right, targetSum);
```

Also, a small performance tweak can be made by avoiding writing targetSum: targetSum -= root->val

This will avoid a memory write access, making the calculation directly in the CPU, but also at a cost of readability

```
if (!root->left && !root->right && targetSum - root->val == 0) {
    ...
return hasPathSum(root->left, targetSum - root->val) || hasPathSum(root->right, targetSum - root->val);
```

# Problem – 102. Binary Tree Level Order Traversal



**LeetCode** 

leetcode.com/problems/binary-tree-level-order-traversal

### Problem Statement / Solution / Code Time: O(-) Space: O(-)

• ..

# Problem - 297. Serialize and Deserialize Binary Tree



leetcode.com/problems/serialize-and-deserialize-binary-tree

#### **Problem**

- Design an algorithm to serialize and deserialize a binary tree
- You have to build two interfaces: serialize that returns a string, and deserialize that returns the whole tree as TreeNode pointer
- The string can be represented at any format (comma-separated, space separated etc)

# Solution – 297. Serialize and Deserialize Binary Tree



leetcode.com/problems/serialize-and-deserialize-binary-tree

#### **Solution**

• Serialize: traverse the tree pre-order, and append its value to a string

Null value should also be represented

Example: [1,2,null,null,3 ...]

Call "traverse" to do it recursively

Deserialize: split the string into tokens

read each token and re-build the tree by adding a new node

Call "buildTree" to do it recursively

# Code - 297. Serialize and Deserialize Binary Tree

```
E LeetCode
```

leetcode.com/problems/serialize-and-deserialize-binary-tree

```
Code Time: O() Space: O()
string serialize(TreeNode* root) {
    // traverse the tree in pre-order: root, left, right
    // generate a string with comma separator,
    // example: 1,2,N,N,3 ...
    string result;
    traverse(root, result);
    return result;
TreeNode* deserialize(string data) {
   // split the input data
   vector<string> tokens = split(data);
   // index to be used to access the elements from tokens recursively.
   // Hence, we need to create it here to pass by reference.
   // Note that index is bounded by the number of tokens, so it won't overflow
   int index = 0:
   TreeNode* root = buildTree(tokens, index);
   return root;
```

#### continue...

# Code - 297. Serialize and Deserialize Binary Tree

```
E LeetCode
```

leetcode.com/problems/serialize-and-deserialize-binary-tree

```
TreeNode* buildTree(vector<string>& tokens, int& index) {
    // read the current token based on the index
    const string& token = tokens[index];
    // increment index before checking for null
    ++index;
    // base case: null node
    if (token == "N") {
        return nullptr;
    }
    // build root
    TreeNode* node = new TreeNode(stoi(token));
    // build left
    node->left = buildTree(tokens, index);
    // build right
    node->right = buildTree(tokens, index);
    return node;
}
```

```
// traverse in pre-order (root, left, right)
// and append the values to the string 's'
// append 'N' if it is NULL
void traverse(TreeNode* root, string& s) {
    if (!s.empty()) s += ",";
    // base case, we need to append null
    if (!root) {
        s += "N";
        return;
    // visit root
    s += to string(root->val);
    // visit left
    traverse(root->left, s);
    // visit right
    traverse(root->right, s);
// helper function in C++ to split string
vector<string> split(const string& s) {
    vector<string> result;
    stringstream ss(s);
    string token;
    while(getline(ss, token, ',')) {
        result.push back(token);
    return result;
```

Hard

# Code - 297. Serialize and Deserialize Binary Tree



leetcode.com/problems/serialize-and-deserialize-binary-tree

### Some interesting alternative to split

C++ 23 have an interesting way to split using std::views::split

```
vector<string> split(string s) {
    auto result = s |
        views::split(',') |
        views::transform([](auto&& subRange) {
            return string(subRange.start(), subRange.end());
        });
}
```

To understand, this follow a structure similar to unix pipes:

```
echo "123,N,556" | split | transform
```

std::views::split returns ranges, something like:

```
[ range("123"), range("N"), range("556") ]
```

std::views::transform converts each subrange into an actual string



leetcode.com/problems/subtree-of-another-tree

#### **Problem**

- You are given the root of a binary tree root and the root of another binary tree subRoot
- Determine whether subRoot is a subtree of root.
- A subtree of a binary tree is a node in the tree along with all of its descendants
- The tree itself is also considered a subtree.



leetcode.com/problems/subtree-of-another-tree

#### **Solution**

- Define a helper function isSameTree(a, b) that checks if two trees rooted at a and b are identical in both structure and node values.
- Traverse the root tree, and for each node:
- Use isSameTree(node, subRoot) to check if a matching subtree starts at that node.
- Return true if any such match is found; otherwise, return false.

# Problem - 572. Subtree of Another Tree

**E** LeetCode

leetcode.com/problems/subtree-of-another-tree

Code Time: O(m \* n) Space: O(h) where n is the number of nodes of the tree and m the number of nodes of the subtree, and h the height of the tree.

```
bool isSame(TreeNode* q, TreeNode* r) {
   // both are null, so they're the same
   if (!q && !r) return true;
   // if they're not null, both must be not null
    if (!q || !r) return false;
   // now check the values
    if (q->val != r->val) return false;
   // check left and right
    return isSame(q->left, r->left) && isSame(q->right, r->right);
bool isSubtree(TreeNode* root, TreeNode* subRoot) {
    if (!root) return false;
   // Check starting from the root first
    if (isSame(root, subRoot)) {
        return true;
   // they are not the same starting from the root,
    // but still subRoot may be in the middle of root. So check it recursively
    return isSubtree(root->left, subRoot) || isSubtree(root->right, subRoot);
```



leetcode.com/problems/construct-binary-tree-from-preorder-and-inorder-traversal

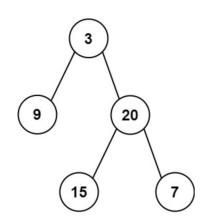
#### **Problem**

- You are given two array of integers: preorder and inorder
- preoder is the pre-order traversal of a binary tree
- inorder is the in-order traversal of a binary tree
- Based on those two arrays, construct the binary tree
- Example

Input: preorder = [3,9,20,15,7]

inorder = [9,3,15,20,7]

Output: the head pointer of the binary tree



# Solution - 105. Construct Binary Tree from Preorder and Inorder Traversal





leetcode.com/problems/construct-binary-tree-from-preorder-and-inorder-traversal

### **Solution**

**2** 

# Code - 105. Construct Binary Tree from Preorder and Inorder Traversal



**LeetCode** 

leetcode.com/problems/construct-binary-tree-from-preorder-and-inorder-traversal

Code Time: O(-) Space: O(-)

- '
- **2**

# Problem – 98. Validate Binary Search Tree





leetcode.com/problems/validate-binary-search-tree

#### **Problem**

- You are given the root of a binary tree
- Determine if the tree is a valid binary search tree according to the following:
- The left subtree contains all elements less than the node's key
- The right subtree contains all elements greater than the node's key
- Both left and right must also be binary search trees

# Solution – 98. Validate Binary Search Tree





leetcode.com/problems/validate-binary-search-tree

#### **Solution**

- For each node, there is a maximum and a minimum value where node lies
- The range of the root is  $(-\infty, \infty)$
- Traverse from top to bottom
- If you are checking the right subtree, all the elements must be higher than a minimum value
- When traversing right, make sure to update the minimum value
- The same is true for the left subtree all the elements must be less than the maximum value





leetcode.com/problems/validate-binary-search-tree

### **Solution (example)**



- The minimum of all elements at the right of "5" should be greater than 5
- So this tree is invalid
- For each node, the values must range between a min and a max:

```
node = (max, min)
```

node  $5 = (-\infty, +\infty)$  can be any value

node  $1 = (-\infty, 5)$  must be any value less than 5

node  $6 = (5, +\infty)$  this node can be any value greater than 5

node 3 = (5, 6) must be greater than the subtree the node belongs and less than the immediate parent

# Code – 98. Validate Binary Search Tree

**LeetCode** 

leetcode.com/problems/validate-binary-search-tree

```
Time: O(n) Space: O(n) where n is the number of the nodes in the tree
Code
// Use long long for min/max due the constraints
bool isValid(TreeNode* root, long long min, long long max) {
    // base case: if we reach the bottom, that means we've
    // checked all nodes along the way and everything is fine
    if (!root) return true;
    // compare the min/max values
    if (root->val <= min || root->val >= max) return false;
    // go right and left. When going right, the minimum should be updated and
    // when going left, the maximum should be updated by its immediate parent
    return isValid(root->right, root->val, max) && isValid(root->left, min, root->val);
bool isValidBST(TreeNode* root) {
    return isValid(root, LONG_MIN, LONG_MAX);
```



LeetCode leetcode.com/problems/kth-smallest-element-in-a-bst

#### **Problem Statement / Solution**

- You are given the root of a binary search tree and an integer k
- Find the k<sup>th</sup> smallest value

### Example

From all values in the tree: 1,2,3,4,5,6

 $\mathbf{k} = \mathbf{3}$  so find the  $3^{th}$  smallest value

**Output** is 3: 1,2,**3**,4,5,6 (3th)





leetcode.com/problems/kth-smallest-element-in-a-bst

### **Solution**

- Note that the smallest element is in the left leaf.
- Therefore, there is an order from small  $\rightarrow$  big values from left  $\rightarrow$  root  $\rightarrow$  right
- Perform in-order traversal k times and stop in the desired node



```
LeetCode
```

LeetCode leetcode.com/problems/kth-smallest-element-in-a-bst

### Time: O(k) Space: O(h) where h is the height of the tree // in-order traversal: left, node: right void traverse(TreeNode\* node, int& k, int& result) { // base case if (!node) return; // visit left first traverse(node->left, k, result); // visit node k--; if (k == 0) { result = node->val; return; // visit right traverse(node->right, k, result); int kthSmallest(TreeNode\* root, int k) { // perform pre-order traversal int result; traverse(root, k, result); return result;



leetcode.com/problems/binary-tree-maximum-path-sum

### **Problem**

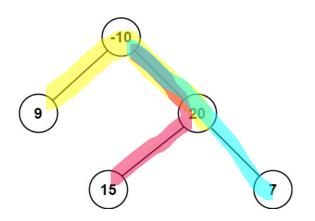
- You are given the root node of a binary tree
- Return the max path sum of any path
- A path can be linear (from the root all the way down to the leaf) or the three node: root, left and right)
- A path can start at any node
- **Example:**

$$9 \rightarrow -10 \rightarrow 20$$
 is a valid path

$$9 \rightarrow -10 \rightarrow 20 \rightarrow 7$$
 is **NOT** a valid path  $20 \rightarrow 7$  is a valid path

$$-10 \rightarrow 20 \rightarrow 15$$
 is a valid path

$$20 \rightarrow 7$$
 is a valid path



# Solution - 124. Binary Tree Maximum Path Sum



leetcode.com/problems/binary-tree-maximum-path-sum

### **Solution**

- Use post-order traversal (bottom-up recursion)
- At each node:
  - Recursively compute left and right max path gains
  - Consider all 3 possible paths:
    - 1. Turn path: left + root + right
  - 2. Linear path: root + left
  - 3. Linear path: root + right
  - Also consider just the root (if the children is negative)
- Track the maximum path seen so far
- Only return linear path (root + one child) upward to maintain the valid structure
- Also, prune negative gain before returning

# Problem - 124. Binary Tree Maximum Path Sum



leetcode.com/problems/binary-tree-maximum-path-sum

int findMaxSum(TreeNode\* root, int& maxSum) {

### Code Time: O(n) Space: O(h) where n is the number of nodes and h is the height of the tree.

```
if (!root) return 0;
   int left = findMaxSum(root->left, maxSum);
   int right = findMaxSum(root->right, maxSum);
   // 1st possible path: exactly the only 3 nodes: root, right and left
   int threeNodes = left + right + root->val;
   // 2nd possible path, linear recursive path: root + left
   int secondPath = root->val + left;
   // 3rd possible path, linear recurrsive path: root + right
   int thirdPath = root->val + right;
   // check if we should consider left, right or only root itself
   int bestPath = max({root->val, secondPath, thirdPath});
   // maxSum can be the accumulated 2nd and 3rd (linear path)
   // or the threeNodes path
   maxSum = max({maxSum, bestPath, threeNodes});
   // Prune subtree: we start from the bottom, so we can set 0
   // to ignore left or right path
   return max(0, bestPath);
int maxPathSum(TreeNode* root) {
   int maxSum = INT MIN;
   findMaxSum(root, maxSum);
   return maxSum;
```

# Problem - 124. Binary Tree Maximum Path Sum

**LeetCode** 

leetcode.com/problems/binary-tree-maximum-path-sum

Code (compact) Time: O(n) Space: O(h) where n is the number of nodes and h is the height of the tree.

```
int find(TreeNode *node, int& totalMax) {
    if (!node) return 0;
    int leftGain = max(0, find(node->left, totalMax));
    int rightGain = max(0, find(node->right, totalMax));
    int currentMax = node->val + leftGain + rightGain;
    totalMax = max(totalMax, currentMax);
    return node->val + max(leftGain, rightGain);
}

int maxPathSum(TreeNode* root) {
    int totalMax = INT_MIN;
    find(root, totalMax);
    return totalMax;
}
```



leetcode.com/problems/leaf-similar-trees

#### **Problem Statement**

- You are given two trees
- The goal is to compare if they have the same leaves
- The leaves should be in the same order
- Example:

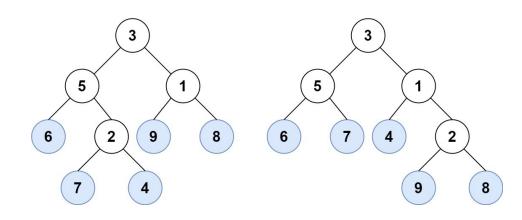
First tree:

**leaves = 6,7,4,9,8** (blue nodes)

Second tree:

leaves = 
$$6,7,4,9,8$$

Return true if the leaves are the same





leetcode.com/problems/leaf-similar-trees

### **Solution**

- Get the first leaf value from tree 1
- Get the first leaf value from tree 2
- Compare, if they are different, return false immediately
- Otherwise, continue finding the next leaf value for tree 1 and 2

### **Implementation**

- Create two stacks stack<TreeNode\*> left and stack<TreeNode\*> right
- Add the

## Code – Leaf-Similar Trees

**LeetCode** 

leetcode.com/problems/leaf-similar-trees

Code Time: O(n + m) where n and m are the numbers of nodes for trees 1 and 2 Space: O(h1 + h2) where h1 and h2 represents the height of the tree

```
// returns the value of the leaf, or -1 if empty
int getLeaf(stack<TreeNode*>& tree) {
   // tree is a reference, we will always pop an element from it
   while(!tree.empty()) {
       // get the top element from the stack
       TreeNode* node = tree.top();
       // already visited, so remove from stack
       tree.pop();
       // is this a leaf?
       if (!node->left && !node->right) {
           // yes, return the value
           return node->val;
        // push the right FIRST to the stack
       if (node->right) tree.push(node->right);
        // left should be on top of the stack
       if (node->left) tree.push(node->left);
   return -1;
```

```
bool leafSimilar(TreeNode* root1, TreeNode* root2) {
   // initialize the stacks, add root1 and root2
   std::stack<TreeNode*> leftTree, rightTree;
   leftTree.push(root1);
   rightTree.push(root2);
   while(true) {
       // get the leaves to compare
       int leaf1 = getLeaf(leftTree);
       int leaf2 = getLeaf(rightTree);
       // exit immediately if one leaf is different
       if (leaf1 != leaf2) return false;
       // stop when there are no leaves left
       if (leaf1 == -1 | leaf2 == -1) break;
   return true;
```

## Code – Leaf-Similar Trees



leetcode.com/problems/leaf-similar-trees

Code (another approach) Time: O(n + m) where n and m are the numbers of nodes for trees 1 and 2 Space: O(h1 + h2) where h1 and h2 represents the height of the tree

```
void extractLeafs(TreeNode* node, vector<int>& leafValues) {
   // base case, return
   if (!node) return;
   // if it looks like a leaf, no left child
   // like a leaf, no right child like a leaf,
   // then it's probably a leaf
   // add to the vector
   if (!node->left && !node->right) {
       leafValues.push back(node->val);
   // continue looking at left and right
    extractLeafs(node->left, leafValues);
    extractLeafs(node->right, leafValues);
bool leafSimilar(TreeNode* root1, TreeNode* root2) {
   vector<int> tree1Values;
   vector<int> tree2Values;
   // extract all leafs from tree 1
    extractLeafs(root1, tree1Values);
   // extract all leafs from tree 2
    extractLeafs(root2, tree2Values);
   // compare
    return tree1Values == tree2Values;
```





leetcode.com/problems/count-good-nodes-in-binary-tree

#### **Problem Statement**

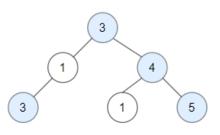
- You are given a binary tree and have to find "good" nodes
- A good node is a node where the values in the path are always than the node
- The root node is always a good node
- Example:
  - root 3 is a good node

### left side:

- left leaf 1 is not a good node because 1 < 3
- leaf 3 is a good node because 3 > 1 and 3 == 3

### right side:

- leaf 4 is a good node because 4 > 3
- **leaf 1** is not a good node because **1 < 4**
- leaf 5 is a good node because 5 > 4 > 3



## Solution – 1448. Count Good Nodes in Binary Tree





leetcode.com/problems/count-good-nodes-in-binary-tree

### **Solution**

- Use DFS traversal to explore the tree from the root to all leaf nodes
- As you traverse, keep track of the maximum value along the path from root to node
- Update max value once you find a node value greater than the max value

## Recursive logic

Base case: if the node is *nullptr*, return 0

### At each node:

- Compare its value to max so far
- If it is a good node, increase a local count
- Recursively repeat this process for the left and right children, passing along the updated max value

```
LeetCode
```

leetcode.com/problems/count-good-nodes-in-binary-tree

```
Code Time: O(n) Space: O(h)
int traverse(TreeNode* root, int maxValue) {
    if (!root) return 0;
   // is this a good node?
    int count = 0;
    if (root->val >= maxValue) {
        maxValue = root->val;
        count = 1;
    count += traverse(root->left, maxValue);
    count += traverse(root->right, maxValue);
    return count;
int goodNodes(TreeNode* root) {
    if (!root) return 0;
    return traverse(root, root->val);
```