Tips

- When to build an adjacency list from the input data?
 - When the graph is **sparse**
 - When working with **non-grid graphs**
 - When you want to perform multiple or complex traversals and need fast neighbour lookups.

DFS Boilerplate

Recursive DFS

Time Complexity: **O(N + E)** Space Complexity: **O(N)**

N = Number of nodes E = Number of edges

Iterative DFS

Time Complexity: **O(N + E)** Space Complexity: **O(N)**

```
void runDFS(int n, const vector<vector<int>>& graph) {
   vector<bool> visited(n, false);
   stack<int> stk;
   stk.push(0); // start from node 0
   while (!stk.empty()) {
       int node = stk.top();
        stk.pop();
       if (visited[node]) continue;
       visited[node] = true;
       for (int neighbor : graph[node]) {
            if (!visited[neighbor]) {
                stk.push(neighbor);
```

BFS Boilerplate

Iterative BFS

Time Complexity: **O(N + E)** Space Complexity: **O(N)**

```
void runBFS(int n, const vector<vector<int>>& graph) {
    vector<bool> visited(n, false);
    queue<int> q;
    q.push(0); // start from node 0
    visited[0] = true;
    while (!q.empty()) {
        int node = q.front();
        q.pop();
        for (int neighbor : graph[node]) {
            if (!visited[neighbor]) {
                visited[neighbor] = true;
                q.push(neighbor);
```

Time Complexity notes

- Every node is enqueued/dequeued once
- Every edge is checked once

N = Number of nodes E = Number of edges

Problem – 841. Keys and Rooms



leetcode.com/problems/keys-and-rooms

Problem

- You are given an array of array rooms, example:
 - [[1,2], [2],[0]]
- Each element in the outer array represents a room
- Each array inside the array represents a set of keys that open the rooms
- Rooms are the index of the array
- In the example, room 0 have the keys for room 1 and 2
- Room 1 have the keys for room 2
- Room 2 have the key for room 0
- **Room 0** is the only room unlocked. You start by visiting room 0, grab the key and unlock other rooms
- **Return true** if you can unlock all rooms

Solution – 841. Keys and Rooms





leetcode.com/problems/keys-and-rooms

- This is a graph problem that can be solved using DFS
- Treat each room as a node
- Treat each set of keys as edges the goes from room A to B
- Visit room 0, and then start visiting the neighbours
- Once you visited all rooms/nodes, check if the visited size is the same as the number of exiting rooms

Code – 841. Keys and Rooms

```
LeetCode
```

leetcode.com/problems/keys-and-rooms

```
Void dfs(int room, vector<vector<int>>& rooms, unordered_set<int>& visited) {
   if (visited.count(room)) return;
   visited.insert(room);
   for (const auto& roomNumber : rooms[room]) {
      dfs(roomNumber, rooms, visited);
   }
}
bool canVisitAllRooms(vector<vector<int>>& rooms) {
   unordered_set<int> visited;
   dfs(0, rooms, visited);
   return rooms.size() == visited.size();
}
```



https://leetcode.com/problems/clone-graph

Problem Statement

- Given a node reference, create a deep copy of the graph
- The class node has two variables: val and neighbours

```
class Node {
  public int val;
  public List<Node> neighbors;
}
```

Output is the node reference of the copy



https://leetcode.com/problems/clone-graph

- First check the edge cases (is the node null?)
- Create a hash map to store the nodes that is already created unordered<int, Node*> graph;
- Check if the current node already exists in the graph
- If not, create a new Node object and store in the hashmap
- Visit all the neighbors and add the neighbors to this current node

Code - Clone Graph

```
E LeetCode
```

https://leetcode.com/problems/clone-graph

```
std::unordered_map<int, Node*> graph;
Node* cloneGraph(Node* node) {
   if (node == NULL) {
        return NULL;
    // does this node object exists?
   if (graph.find(node->val) == graph.end()) {
        // node wasn't visited yet, store in the hashmap
        graph[node->val] = new Node(node->val);
        // visit all neighnours
        for (const auto& n : node->neighbors) {
            graph[node->val]->neighbors.push_back(cloneGraph(n));
   return graph[node->val];
```

Problem - 207. Course Schedule



LeetCode

leetcode.com/problems/course-schedule

Problem

- You are given the number of courses and a course pre-requisite array
- Course pre-requisite indicates the dependency between courses

• Example:

```
numCourses = 2, prerequisites = [[1,0],[0,1]]
To take course 1, you must take course 0 first
to take course 0, you must take course 1 first
```

- In this example, this schedule is not possible since one course depends on the other
- Return if the schedule is valid or not

Solution - 207. Course Schedule





leetcode.com/problems/course-schedule

- Model as a graph problem
- Create a dependency graph between courses: course A depends on course B
- If there is a cycle, **A** to **B** and **B** to **A**, the schedule is invalid
- For the implementation: first convert the schedule to adjacency list
- Use DFS and track two status: VISITING and VISITED
- Go over each node in the adjacency list, and perform a DFS
- Once you find a node which status is VISITING, you've detected a cycle

Code - 207. Course Schedule



leetcode.com/problems/course-schedule

Code Time: O(n + p) Space: O(n + p) where n is the number of courses and p the number of edges in the graph

```
enum class VisitState {
   NOT VISITED,
   VISITING,
    VISITED
};
bool hasCycle(int node, const unordered map<int, vector<int>>& adjList,
              unordered map<int, VisitState>& visited) {
   // if we are revisiting a node in the current path, there's a cycle
   if (visited[node] == VisitState::VISITING) return true;
   // if we've already completed visiting this node, no need to check again
   if (visited[node] == VisitState::VISITED) return false;
   // mark the node as being visited
   visited[node] = VisitState::VISITING;
   for (int neighbor : adjList.at(node)) {
        if (hasCycle(neighbor, adjList, visited)) return true;
   // mark the node as fully visited
   visited[node] = VisitState::VISITED;
   return false:
```

```
bool canFinish(int numCourses, const vector<vector<int>>& prerequisites) {
    // build the adjacency list: course -> list of its prerequisites
    unordered_map<int, vector<int>> adjList;
    for (const auto& dependencyPair : prerequisites) {
        int course = dependencyPair[0];
        int prerequisite = dependencyPair[1];
        adjList[course].push_back(prerequisite);
    }
    unordered_map<int, VisitState> visited;

    // check each course for cycles
    for (int course = 0; course < numCourses; ++course) {
        if (adjList.count(course)) {
            if (hasCycle(course, adjList, visited)) return false;
        }
    }
    return true; // no cycles detected
}</pre>
```

Code - 207. Course Schedule

LeetCode

leetcode.com/problems/course-schedule

Code (simplified) Time: O(n + p) Space: O(n + p) where n is the number of courses and p the number of edges in the graph

```
bool canFinish(int numCourses, vector<vector<int>>& prerequisites) {
    // construct the graph
   vector<vector<int>> adjList(numCourses);
    // states:
    // unvisited = 0, visiting = -1, visited = 1
   vector<int> visited(numCourses, 0);
    for (const auto& pre : prerequisites) {
        adjList[pre[1]].push back(pre[0]);
    for (int n = 0; n < adjList.size(); ++n) {</pre>
        if (hasCycle(adjList, visited, n /* starting node */)) {
            return false;
    return true;
bool hasCycle(vector<vector<int>>& adjList, vector<int>& visited, int node) {
   if (visited[node] == -1) return true;
   if (visited[node] == 1) return false;
   // visiting
   visited[node] = -1;
    for (const auto& n: adjList[node]) {
        if (hasCycle(adjList, visited, n)) {
            return true;
    // already visited
    visited[node] = 1;
```

Problem – 417. Pacific Atlantic Water Flow





leetcode.com/problems/pacific-atlantic-water-flow

Problem

- You are given a matrix heights[m][n] representing elevations on an island
- Pacific Ocean borders the top and left, Atlantic Ocean borders the bottom and right
- Rainwater can flow from a cell to its north, south, east, or west neighbor if the neighbor's height is ≤ current
- Find all coordinates (r, c) from which water can flow to both oceans
- Return a list of such coordinates: [[r1, c1], [r2, c2], ...]

	Pacific Ocean						
	1	2	2	3	5		
Pacific	3	2	3	4	4	Atlantic Ocean	
	2	4	5	3	1		
Ocean	6	7	1	4	5	Ocean	
	5	1	1	2	4		
Atlantic Ocean							

Solution - 417. Pacific Atlantic Water Flow





leetcode.com/problems/pacific-atlantic-water-flow

Solution 1 (inneficient)

- Iterate the whole matrix and perform a DFS
- Visit the neighbour if the value is less or equal the current value
- If it reaches some ocean, mark either atlantic or pacific as true
- Return true once both are true or false after finishing DFS

Code - 417. Pacific Atlantic Water Flow

```
LeetCode
```

leetcode.com/problems/pacific-atlantic-water-flow

Code Time: $O((m \times n)^2)$ Space: $O(m \times n)$

```
private:
vector<vector<int>> directions = {{0,1},{0,-1},{1,0},{-1,0}};
public:
vector<vector<int>> pacificAtlantic(vector<vector<int>>& heights) {
    int m = heights.size();
    int n = heights[0].size();
    vector<vector<int>> result;
    for (int row = 0; row < m; ++row) {
        for (int col = 0; col < n; ++col) {
            bool pacific = false;
            bool atlantic = false;
            vector<vector<bool>> visited(m, vector<bool>(n, false));
            if (dfs(make_pair(row, col), heights, visited, pacific,
atlantic)) {
                result.push_back({row, col});
    return result;
```

```
bool dfs(pair<int, int> coordinates, vector<vector<int>>& heights,
        vector<vector<bool>>& visited, bool& pacific, bool& atlantic) {
   if (pacific && atlantic) return true;
   int row = coordinates.first;
   int col = coordinates.second;
   if (visited[row][col]) return false;
   if (col == 0 | row == 0) pacific = true;
   if (col == heights[0].size() - 1 || row == heights.size() - 1)
         atlantic = true;
   visited[row][col] = true;
   for (const auto& d : directions) {
        int nextRow = row + d[0];
        int nextCol = col + d[1];
        if (nextRow < 0 || nextCol < 0 || nextRow >= heights.size() ||
            nextCol >= heights[0].size()) continue;
        if (heights[nextRow][nextCol] <= heights[row][col]) {</pre>
            if (dfs(make_pair(nextRow, nextCol), heights,
                    visited, pacific, atlantic)) {
                    return true;
   return pacific && atlantic;
```

Solution - 417. Pacific Atlantic Water Flow





leetcode.com/problems/pacific-atlantic-water-flow

Solution 2 (better)

- Start from the border of pacific ocean and find all reachable squares using DFS
- Then, start from the border of atlantic ocean and find all reachable squares using DFS
- Check the squares where both are accessible

Code - 417. Pacific Atlantic Water Flow



leetcode.com/problems/pacific-atlantic-water-flow

Code Time: $O(m \times n)$ Space: $O(m \times n)$

```
private:
vector<vector<int>> directions = {{0,1},{0,-1},{1,0},{-1,0}};
public:
vector<vector<int>> pacificAtlantic(vector<vector<int>>& heights) {
    int m = heights.size();
    int n = heights[0].size();
   // squares where pacific is reachable
    vector<vector<bool>> pacific(m, vector<bool>(n, false));
   // squares where atlantic is reachable
    vector<vector<bool>> atlantic(m, vector<bool>(n, false));
   // check pacific and atlantic
    for (int row = 0; row < m; ++row) {
        dfs(row, 0, heights, pacific);
        dfs(row, n - 1, heights, atlantic);
    for (int col = 0; col \langle n; ++col) {
        dfs(0, col, heights, pacific);
        dfs(m - 1, col, heights, atlantic);
    // check where both are reachable
    vector<vector<int>> result;
    for (int row = 0; row < m; ++row) {
        for (int col = 0; col < n; ++col) {
            if (pacific[row][col] && atlantic[row][col]) {
                result.push_back({row,col});
    return result;
```



leetcode.com/problems/number-of-islands

Problem

- You are given a matrix m x n
- The matrix represents a map where "1" is land and "0" is water
- Return the total number of island: "connected" ones form one island
- Example:

Input:

Output: 2

Solution - 200. Number of Islands





leetcode.com/problems/number-of-islands

- Loop through each element in the matrix
- Once you find "1", count the land and;
- Perform a DFS (or BFS) around each '1' cell
- When traversing, mark "0" after visited
- Continue until you finish processing all elements in the matrix

Code - 200. Number of Islands

E LeetCode

leetcode.com/problems/number-of-islands

Code Time: O(m × n) Space: O(m × n) As we visit each cell only once, time complexity is the size of the matrix. The space complexity comes from the DFS recursion stack.

```
int numIslands(vector<vector<char>>& grid) {
    int m = grid.size(), n = grid[0].size();
    int count = 0;
    for (int i = 0; i < m; i++) {
       for (int j = 0; j < n; j++) {
           if (grid[i][j] == '1') {
                count++;
                dfs(grid, i, j);
    return count;
void dfs(vector<vector<char>>& grid, int i, int j) {
    int m = grid.size(), n = grid[0].size();
    if (i < 0 || i >= m || j < 0 || j >= n || grid[i][j] == '0')
       return;
    grid[i][j] = '0';
    dfs(grid, i + 1, j);
    dfs(grid, i - 1, j);
    dfs(grid, i, j + 1);
    dfs(grid, i, j - 1);
```

Problem – 128. Longest Consecutive Sequence





leetcode.com/problems/longest-consecutive-sequence

Problem

- You are given an unsorted array of integers nums
- Return the length of the longest consecutive elements sequence
- Algorithm must run on O(n) time





leetcode.com/problems/longest-consecutive-sequence

Solution

- Create a set with the same elements of nums
- Loop through this set and check if it is the beginning of a sequence
- Example:

```
[4,100,3,2,101]
```

4: Look up 3 (found) \rightarrow 4 is **NOT** the beginning (skip it)

100: Look up 99 (not found) \rightarrow 100 **IS** the beginning \rightarrow count 100, 101 \rightarrow length = 2

3: Look up 2 (found) \rightarrow 3 is **NOT** the beginning (skip it)

2: Look up 1 (not found) \rightarrow 2 **IS** the beginning \rightarrow count 2, 3, 4 \rightarrow length = 3

101: Look up 100 (found) \rightarrow 101 is **NOT** the beginning (skip it)

Track the maximum length

Code - 128. Longest Consecutive Sequence

```
E LeetCode
```

leetcode.com/problems/longest-consecutive-sequence

```
Code Time: O(n) Space: O(n)
```

```
int longestConsecutive(vector<int>& nums) {
    unordered_set<int> seq(nums.begin(), nums.end());
   int maxStreak = 0;
    for (const auto& n : seq) {
       // is beginning of sequence?
       // previous exist?
       int streak = 0;
       if (seq.find(n - 1) == seq.end()) {
           // check next
           int currNum = n;
           while (seq.find(currNum) != seq.end()) {
                streak++;
               currNum++;
       maxStreak = max(maxStreak, streak);
    return maxStreak;
```





leetcode.com/problems/number-of-connected-components-in-an-undirected-graph

Problem

- You are given a graph of n nodes, and an array of edges (source, destination)
- Edges indicates the edge between node source and destination
- Find the total number of isolated components (subgraphs)

• Example:

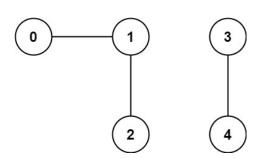
Input:

$$n = 5$$
, edges = [[0,1],[1,2],[3,4]]

Output: 2

0 is connected to 1, 1 is connected to 2

3 is a new subgraph connected to 4



Solution – 323. Number of Connected Components





leetcode.com/problems/number-of-connected-components-in-an-undirected-graph

- Build an adjacency list from edges
- From each node, check if its visited
- If it is not visited, mark as a new "component" or subgraph
- Perform a DFS from that node

Code – 323. Number of Connected Components

E LeetCode

leetcode.com/problems/number-of-connected-components-in-an-undirected-graph

Code Time: O(n + E) Space: O(n + E) where n is the number of nodes and E is edges size

```
int countComponents(int n, vector<vector<int>>& edges) {
   vector<bool> visited(n, false);
   vector<vector<int>> adjList(n);
   // build adjancency list
   for (const auto& edge: edges) {
        adjList[edge[0]].push back(edge[1]);
        adjList[edge[1]].push_back(edge[0]);
   int totalComponents = 0;
   for (int i = 0; i < n; ++i) {
       if (!visited[i]) {
           dfs(adjList, visited, i);
           totalComponents++;
   return totalComponents;
void dfs(vector<vector<int>>& adjList, vector<bool>& visited, int node) {
   if (visited[node]) return;
   visited[node] = true;
   for (const auto& neighbour : adjList[node]) {
        dfs(adjList, visited, neighbour);
```





https://leetcode.com/problems/maximum-level-sum-of-a-binary-tree

Problem Statement

- Given the root of a binary tree, find the smallest level with the maximum sum
- For example, the tree below has the follow sums for each level:

level
$$1 \text{ (root)} = 1$$

level
$$2 = 7 + 0 = 7$$

$$|eve| 3 = 7 - 8 = -1$$

Therefore, level 2 has the maximum sum



Solution – Maximum Level Sum of a Binary Tree





https://leetcode.com/problems/maximum-level-sum-of-a-binary-tree

- Have a queue with the nodes for the current level
- Sum the values from that level by taking the nodes from the queue
- Example, we know that level 1 has one node. Hence, pop the first node from the queue
 If level 2 has 2 nodes, pop two nodes, sum the values
- In addition, add left and right to the end of the queue to process the next level

Code – Maximum Level Sum of a Binary Tree

```
E LeetCode
```

https://leetcode.com/problems/maximum-level-sum-of-a-binary-tree

```
int maxLevelSum(TreeNode* root) {
    std::queue<TreeNode*> nodes;
    int currentLevel = 0;
    int maxLevel = 1;
    int maxSum = INT MIN;
    nodes.push(root);
    // traverse the graph
    while(!nodes.empty()) {
        int levelSum = 0;
        int levelSize = nodes.size();
        currentLevel++;
        // sum the values in current level
        for (int i = 0; i < levelSize; ++i) {</pre>
            TreeNode* node = nodes.front();
            levelSum += node->val;
            nodes.pop();
            if (node->left) nodes.push(node->left);
            if (node->right) nodes.push(node->right);
        if (levelSum > maxSum) {
            maxLevel = currentLevel;
            maxSum = levelSum;
    return maxLevel;
```

Problem - 1236. Web Crawler





https://leetcode.com/problems/web-crawler

Problem

- You are given a starting URL startURL and an interface HtmlParser with a method getUrls(url)
- getUrls(url) returns a vector of strings with the URLs found on the given page
- Start crawling from startUrl and recursively visit all reachable URLs
- Only visit URLs that share the same hostname as startUrl
- Return a list of all visited URLs (in any order)

Solution - 1236. Web Crawler





https://leetcode.com/problems/web-crawler

- This is a graph problem framed as an object
- Both BFS and DFS are valid options
- Each url represent a node, and getUrls retrieve the neighbours
- Visit each node and add to the result if they have the same hostname

Code - 1236. Web Crawler



https://leetcode.com/problems/web-crawler

Code (BFS) Time: O(n + m) Space: O(n + w) where n is the number of unique URLs, m the number of links (edges), w is the explicit queue

```
vector<string> crawl(string startUrl, HtmlParser htmlParser) {
    string hostname = getHostname(startUrl);
   queue<string> urls;
   unordered set<string> visited;
   vector<string> result;
   urls.push(startUrl);
   visited.insert(startUrl);
   result.push back(startUrl);
   while(!urls.empty()) {
        string url = urls.front();
       urls.pop();
       for (const auto& u : htmlParser.getUrls(url)) {
           // is it the same hostname?
           // have I already visited this one?
           if (visited.count(u)) continue;
           if (getHostname(u) != hostname) continue;
           urls.push(u);
           result.push back(u);
           visited.insert(u);
   return result;
```

```
string getHostname(const string& url) {
   int start = url.find("://") + 3;
   int end = url.find("/", start);
   return url.substr(start, end - start);
}
```

```
LeetCode
```

https://leetcode.com/problems/web-crawler

Code (DFS) Time: O(n + m) Space: O(n + h) where n is the number of unique URLs, m the number of links (edges), h is the recursive stack

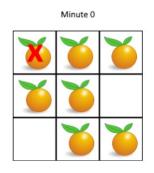
```
string getHostname(const string& url) {
    int start = url.find("://") + 3;
    int end = url.find("/", start);
    return url.substr(start, end - start);
void dfs(const string& hostname, const string& url, HtmlParser& htmlParser,
unordered set<string>& visited, vector<string>& result) {
    if (visited.count(url)) return;
    result.push_back(url);
    visited.insert(url);
    for (const auto& u: htmlParser.getUrls(url)) {
        if (getHostname(u) == hostname) {
            dfs(hostname, u, htmlParser, visited, result);
vector<string> crawl(string startUrl, HtmlParser htmlParser) {
    string hostname = getHostname(startUrl);
    unordered set<string> visited;
    vector<string> result;
    dfs(hostname, startUrl, htmlParser, visited, result);
    return result;
```

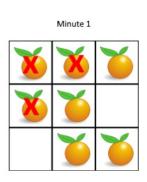


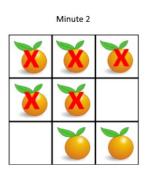
leetcode.com/problems/rotting-oranges

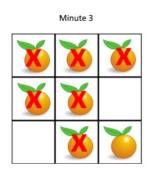
Problem

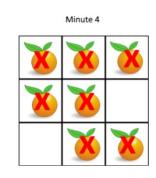
- You are given a m x n grid
- Each cell represents the following:
- 0 is an empty cell
- 1 is a fresh orange
- 2 is a rotten orange
- Every minute (snapshot), any fresh orange is contaminated by adjacent oranges
- Return the minimum number of minutes required for all fresh oranges to become rotten
- If it is **impossible** to rot all fresh oranges, return -1













leetcode.com/problems/rotting-oranges

- This is another BFS problem: for each rotten orange, visit adjacent fresh oranges
- Start by finding all rotten oranges in the grid. No need to convert grid to adjacent list
- Initialize a queue<pair<int, int>> to perform the BFS. Add the rotten oranges to this queue
- Start the traversal while (!q.empty()) { ... }
- This part is important! you want to calculate the "minutes". So you have to first go over the current size of the queue and "process" all the elements, meaning, rot the adjacent fresh oranges
- Use directions vector to calculate the adjacent positions:
 const vector<pair<int, int>> directions = {{0, 1}, {0, -1}, {1, 0}, {-1, 0}};
- Keep track of the number of fresh oranges
- By the end, check if the number of fresh oranges is zero. If so, return minutes, or -1 otherwise.

Code - 994. Rotting Oranges



leetcode.com/problems/rotting-oranges

Code Time: O(m * n) Space: O(m * n)

```
int orangesRotting(vector<vector<int>>& grid) {
    // go over the grid, find the rotten ones
    // count the number of fresh oranges
    // add to a queue
    // queue should contain the positions x,y
    int fresh = 0;
    // we'll increase the minutes before visiting
    int minutesElapsed = -1;
    queue<pair<int, int>> q;
    int m = grid.size();
    int n = grid[0].size();
    for (int row = 0; row < m; ++row) {
        for (int col = 0; col < n; ++col) {</pre>
            if (grid[row][col] == 1) ++fresh;
            if (grid[row][col] == 2) q.push({row, col});
    // no fresh oranges
    if (fresh == 0) return 0;
```

```
// at each minute: pop all the queue, visit the neighbours
// set a fresh one to rotten
// decrease the number of fresh
vector<pair<int, int>> directions = {{0,1},{0,-1},{1,0},{-1,0}};
while(!q.empty()) {
    int qSize = q.size();
   // at each minute, it rottens all oranges
   // therefore, fully consumes the queue
    minutesElapsed++;
    for (int i = 0; i < qSize; ++i) {
        auto [row, col] = q.front();
        q.pop();
       // visit neighbours, check boundaries
       // and if its not visited yet
        for (const auto& [dRow, dCol] : directions) {
            int nRow = row + dRow;
           int nCol = col + dCol;
            if (nRow >= 0 \& nCol >= 0 \& nRow < m \& nCol < n \& grid[nRow][nCol] == 1) {
                grid[nRow][nCol] = 2;
                fresh--;
                q.push({nRow, nCol});
// once you reach the end, count if rotten == fresh
return (fresh == 0) ? minutesElapsed : -1;
```

Backtracking

Common pattern in backtracking

- Useful for problems like: generating all permutations / combinations
- N-Queens
- Sudoku
- Letter combinations

```
void backtrack(/* problem-specific args */) {
    if (/* base case */) {
        // store result
        return;
    }

    for (/* each choice */) {
        // make choice
        state.push_back(choice);

        // explore further
        backtrack(/* updated args */);

        // undo choice (backtrack)
        state.pop_back();
    }
}
```

Problem – 46. Permutations





leetcode.com/problems/permutations

Problem

• You are given an array of numbers, **Example**:

```
nums = [1,2]
```

• Return all possible the permutations:

```
output = [[1,2], [2,1]]
```



leetcode.com/problems/permutations

Solution

- Permutations problem can be solved using backtracking
- Create a function following the template:

```
backtrack(path, result, nums) {
  if path.size == nums.size()
      add to the result and return
    for i in nums
       continue if already used this i
       mark i as used
       add to the current path
       backtrack(...)
       mark i as unused
       remove from the current path
```

LeetCode

leetcode.com/problems/permutations

Code Time: O(n! * n) Space: O(n) Time: there are n! permutations. Each permutation takes O(n) time to construct. Space: the path and used vector grow as n grows. n represents the size of nums

```
void backtrack(vector<int>& path, vector<int>& nums, vector<bool>& used, vector<vector<int>>& result) {
    if (path.size() == nums.size()) {
        result.push back(path);
        return;
    for (int i = 0; i < nums.size(); ++i) {</pre>
        if (used[i]) continue;
        used[i] = true;
       path.push back(nums[i]);
        backtrack(path, nums, used, result);
        path.pop back();
        used[i] = false;
vector<vector<int>> permute(vector<int>& nums) {
    vector<int> path;
    vector<vector<int>> result;
    vector<bool> used(nums.size(), false);
    backtrack(path, nums, used, result);
    return result;
```

Problem – 17. Letter Combinations of a Phone Number





leetcode.com/problems/letter-combinations-of-a-phone-number

Problem

- You are given a string digits containing numbers such as "2" or "234" etc
- Each digit correspond to a digit of a phone number
- The digits map to a group of characters from the phone. For example, $2 \rightarrow$ "abc", $3 \rightarrow$ "def" ...
- Return all possible letter combinations from the digits
- Example

Input: 23

Output: ["ad","ae","af","bd","be","bf","cd","ce","cf"]

2 maps to "abc" and 3 maps to "def", so generate all combinations



Solution – 17. Letter Combinations of a Phone Number



```
E LeetCode
```

leetcode.com/problems/letter-combinations-of-a-phone-number

Solution

Map the keyboard to a vector of strings:

```
std::vector<string> = { "", "", "abc", "def", "ghi", "jkl", "mno", "pqrs", "tuv", "wxyz"}
First 2 characters are empty to map exactly the phone digit position
```

- Use backtracking to generate all combinations
- **Example**: digits "2" and "3" maps to "abc" and "def":

```
visit "a"
visit "d"
reached the end of the digits, add "ad"
backtrack to "a"
visit "e"
reached the end of the digits, add "ae"
```

Problem – 17. Letter Combinations of a Phone Number

E LeetCode

leetcode.com/problems/letter-combinations-of-a-phone-number

```
Time: O(4^n) Space: O(n * 4^n) where n is the number of digits.
Code
For each digit, you have to generate a combination of max 4 characters (the maximum phone digits, for example, 7 represents "pgrs")
void backtrack(vector<string>& result, string& current,
              const vector<string>& phone, string& digits, int index) {
    if (index == digits.size()) {
        result.push back(current);
        return;
    // retrieve current digit
    char currentDigit = digits[index];
    // retrieve chars from that digit
    string chars = phone[currentDigit - '0'];
    // go over each char to backtrack
    for (const char& c : chars) {
        current.push back(c);
        backtrack(result, current, phone, digits, index + 1);
        current.pop back();
vector<string> letterCombinations(string digits) {
    if (digits.empty()) return {};
    const vector<string> phone = {
        "", "", "abc", "def", "ghi",
        "jkl", "mno", "pqrs", "tuv", "wxyz"
    };
    vector<string> result;
    string current;
    backtrack(result, current, phone, digits, 0);
    return result;
```

SHORTEST PATH

Shortest Path Algorithms

Algorithm	Use Case	Graph Type	Time Complexity	Notes
BFS	When all edges have equal weight	Unweighted / same-weighted edges	O(V + E)	Simplest and fastest when all weights are equal.
Dijkstra	When edge weights are non-negative	Weighted, no negative weights	O((V + E) log V) with heap	Greedy, efficient for SSSP (Single Source Shortest Path).
Bellman-Ford	When edge weights can be negative	Weighted, allows negative weights	O(V * E)	Slower, but handles negative weights and detects negative cycles.
Floyd-Warshall	For all-pairs shortest paths	Dense graphs, small number of nodes	O(V ³)	Easy to implement; handles negative weights (but not negative cycles).
A* Search	For shortest path with a goal node and heuristic	Weighted, heuristic needed	Depends on heuristic quality	Often used in pathfinding (e.g. maps, games); faster than Dijkstra if heuristic is good.
Johnson's Algorithm	All-pairs shortest paths in sparse graphs with negative weights	Weighted, allows negative weights	$O(V^2 \log V + V * E)$	Reweights graph with Bellman-Ford, then runs Dijkstra from each node.
SPFA	Practical variant of Bellman-Ford, often faster	Weighted, allows negative weights	Avg: O(E), Worst: O(VE)	Queue-based; faster in practice, not guaranteed. Handles negative weights.
Bidirectional Search	When you know start and target , speeds up search in undirected graphs	Unweighted or uniformly weighted	O(b^(d/2)) in best case	Runs two simultaneous searches (from start and end); fast when goal is known.





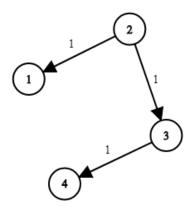
leetcode.com/problems/network-delay-time

Problem

- You are given a network of nodes n with destination and time to reach that node
- \blacksquare You are given a starting node **k** and the number of nodes in the network **n**
- lacktriangle A signal is sent from node **k** to all nodes in the network
- lacktriangle Find the minimum time required for all nodes to receive the signal from lacktriangle
- Example:

$$k = 2 \quad n = 4$$

Output: 3





```
LeetCode
```

leetcode.com/problems/network-delay-time

Solution

- This is solved using Djikstra algorithm
- Build the graph by storing in the destination node and the time from a source node:

```
graph[node] = [[node, distance]]
graph[2] = [[1,1], [2,3]]
```

- Set up a min-heap for Djikstra (priority_queue) with distance and node
- Perform Djikstra algorithm and store the shortest paths
- Check if all nodes were reached
- Return the longest distance among shortest paths