# BINARY

# Bit Manipulation in C

#### Operators

```
& AND OR ^ XOR ~ NOT << LEFT SHIFT >> RIGHT SHIFT
```

#### Common Operations

```
set bit: num |= (1 << pos)

clear bit: num &= ~(1 << pos)

toggle bit: num ^= (1 << pos)

check bit: (num & (1 << pos)) != 0

extract bit: (num >> pos) & 1

extract a range of bits: (num >> pos) & ((1 << length) - 1)</pre>
```

#### Example

```
void copyBit(int *dst, int src, int srcPos, int dstPos) {
    int bit = (src >> srcPos) & 1; // extract bit
    *dst &= ~(1 << dstPos); // clear destination bit
    *dst |= (bit << dstPos); // set destination bit
}</pre>
```

### Binary

- In C++, **std::bitset** represents a fixed-size sequence of N bits
- Example:

```
std::bitset<8> bitmap;
bitmap.reset(1)
bitmap.set(1)
if (bitmap.test(1)) { // true
...
```

- reset : set bit to false
- **set** : set a specific bit
- **test** : check a specific bit
- **count**: return the number of bits set to true
- **flip**: toggle the value of the bits (if true, set to false and vice-versa)

# **Problem – 371. Sum of Two Integers**





leetcode.com/problems/sum-of-two-integers

#### **Problem**

- Sum two integer numbers a and b
- You can't use + or -





leetcode.com/problems/sum-of-two-integers

#### **Solution**

• Example:

$$a = 101 \text{ and } b = 110$$
  
expected result = 101 + 110 = 1011

• Find the position where carry occurs using and operation:

Sum without carry using XOR:

Shift left the carry:

Add the previous sum to the carry

Check the carry from the previous operation:

Now if it is zero, the result is 1011. Otherwise, repeat the process

### Code - 371. Sum of Two Integers

```
E LeetCode
```

leetcode.com/problems/sum-of-two-integers

```
int getSum(int a, int b) {
    while (b!= 0) {
        // find which bits produce a carry
        // e.g. 101 & 111 = 101
        int carry = static_cast<unsigned>(a & b);
        // adds without carry (XOR)
        // 101 ^ 111 = 010
        a = a ^ b;
        // move carry to the left
        // b = 110
        b = carry << 1;
    }
    return a;
}</pre>
```



leetcode.com/problems/number-of-1-bits

#### **Problem**

- You are given a positive integer n
- Return the number of set bits
- Example:

n = 11

output: 3

Binary is 1011, hence three set bits "1"



leetcode.com/problems/number-of-1-bits

#### **Solution**

- Use Brian Kernighan's Bit Counting Algorithm
- removes the rightmost 1-bit from n in each iteration
- Example:

```
n = 12 (1100)
```

**First iteration**: n=1100, n-1=1011, so 1100 & 1011 = 1000 (removed rightmost 1)

**Second iteration**: n=1000, n-1=0111, so 1000 & 0111 = 0000 (removed last 1)

**Result**: 2 iterations = 2 ones counted



leetcode.com/problems/number-of-1-bits

#### Code

```
// Brian Kernighan's algorithm
int hammingWeight(int n) {
    // return std::popcount(n);
    int count = 0;
    while (n) {
        n &= (n - 1);
        ++count;
    }
    return count;
}
```



leetcode.com/problems/counting-bits

#### **Problem**

- You are given an integer n representing n different numbers starting from 0
- Return an array with the number of 1 for each integer

#### • Example:

```
n = 3
0 → 0 (zero '1's)
1 → 1 (one '1')
2 → 10 (one '1')
3 → 11 (two '1's)
Output: [0,1,1,2]
```



leetcode.com/problems/counting-bits

#### **Solution**

- One solution is to code Brian Kernighan's algorithm and then call it multiple times; or
- Use previously calculated results: the bit count of any number i equals the bit count of i/2 plus
   1 if the last bit is 1
- res[i] = res[i >> 1] + (i & 1)
  - i >> 1 removes the rightmost bit (divides by 2)
  - i & 1 checks if the rightmost bit is 1

## Code – 338. Counting Bits

**LeetCode** 

leetcode.com/problems/counting-bits

```
Code Time: O(n) Space: O(n)
```

```
vector<int> countBits(int n) {
    vector<int> res(n + 1, 0);
    for (int i = 1; i <= n; ++i) {
        // i >> 1 = i is divided by 2 (i with the last bit removed)
        // i & 1 is 1 if the last bit is set
        // number of set bits in i = number of set bits in i / 2 + 1 if last bit is 1.
        res[i] = res[i >> 1] + (i & 1);
    }
    return res;
}
```

### Problem - 190. Reverse Bits





leetcode.com/problems/reverse-bits

#### **Problem**

- You are given a 32 bits unsigned integer
- Reverse its bits
- Example:

 $00110 \rightarrow 01100$ 

Do not confuse this with "bit flipping"!

### Solution - 190. Reverse Bits



**LeetCode** 

leetcode.com/problems/reverse-bits

#### **Solution**

• ..

```
E LeetCode
```

leetcode.com/problems/reverse-bits

```
Code Time: O(-) Space: O(-)
```

```
uint32_t reverseBits(uint32_t n) {
   int result = 0;
   for (int i = 0; i < 32; ++i) {
      // shift to left
      result = result << 1;
      // extract the right-most bit from n
      int bit = n & 1;
      // set bit
      result = result | bit;
      // shift to right to check the next bit
      n = n >> 1;
    }
    return result;
}
```

# Negabinary

- Non-standard positional numeral system that uses base of -2
- Allow representing negative numbers in binary
- Example:

$$1101_{-2}$$

$$(-2)^3 + (-2)^2 + 0 + (-2)^0 = -8 + 4 + 0 + 1 = -3$$

#### **Summing Negabinary**

Add as a regular binary number, but with negative carry

$$0 + 0 = 0$$
  
 $1 + 0 = 1$   
 $1 + 1 = 0$  with a negative carry 1  
 $1 + 1 = 0$  (subtract)  
 $1 + 0 = 1$  with a positive carry 1

# Negabinary

#### **Example 1**

#### **Example 2**

$$\begin{array}{r}
 1111 \\
 101010 \\
 + 101100 \\
\hline
 = 11110110
 \end{array}$$

#### Reference

### Problem – 1073. Adding Two Negabinary Numbers



**E** LeetCode

leetcode.com/problems/adding-two-negabinary-numbers

Problem / Solution / Code Time: O(-) Space: O(-)

TODO