

# MA 415: Assignment 4

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Problem 1: Warm Up a. Write a function which takes a numeric vector  $x$  and returns a named list containing the mean, median and variance of the values in  $x$

```
stats <- function(x, plot = FALSE)
{
  if(is.numeric(x)==FALSE) # need to filter out character vectors!\
    stop("Invalid Input. summ() only accepts numeric vectors")
  st = list(Mean=mean(x), Median=median(x), Variance =var(x))
  if(plot==TRUE)
  {
    plot(x)
    abline(h=st[["Mean"]])
  }
  return (st)
}

stats(1:9)
```

```
## $Mean
## [1] 5
##
## $Median
## [1] 5
##
## $Variance
## [1] 7.5
```

b. Write a function with arguments  $x$  and  $n$  which evaluates  $\sum_{i=0}^n ((e^{-x})^x i) / (i!)$

```
partb <- function(x,n)
{
  for(i in 0:n){
    s <- sum(((exp(-x)*(x^i))/ (factorial(i))))
    return(s)
  }
}

partb(2,2)
```

```
## [1] 0.1353353
```

c. Write a function which goes through every entry in a list, checks whether it is a character vector

```
is.char <- function(l)
{
  if (is.list(l)==FALSE)
    stop("Invalid Input. Must enter a list")
  for (x in l){
    if(is.character(x)==TRUE)
      print(x)
  }
}
```

```

}
list <- list(c(4:6), "cat", "dog", 6, "pie")
is.char(list)

```

```

## [1] "cat"
## [1] "dog"
## [1] "pie"

```

```

list <- list("cat", 5, 7, "dog")
is.char(list)

```

```

## [1] "cat"
## [1] "dog"

```

- d. Write a function with an argument  $k$  which stimulates a symmetric walk on the integers, stopping when the walk reaches  $k$  (or  $-k$ ). A random walk on the integers is a sequence  $X_1, X_2, \dots$ , with  $X_0 = 0$  and  $X_i = X_{i+1} + D_i$  where  $D_i$  are independent with  $P(D_i=1)=P(D_i=-1)=0.5$

```

r.walk <- function(k)
{
  r=0
  print(r)
  x <- c(-1,1)
  while (abs(r)<k){
    y <- sample(x,1)
    r <- r + y
    print(r)
  }
}
r.walk(4)

```

```

## [1] 0
## [1] 1
## [1] 2
## [1] 1
## [1] 2
## [1] 1
## [1] 2
## [1] 1
## [1] 0
## [1] -1
## [1] 0
## [1] -1
## [1] -2
## [1] -1
## [1] 0
## [1] -1
## [1] 0
## [1] 1
## [1] 2
## [1] 1
## [1] 0
## [1] 1
## [1] 2
## [1] 3

```

```
## [1] 4
r.walk(2)
```

```
## [1] 0
## [1] 1
## [1] 2
```

## Problem 2. Moving Averages

- a. Write a function to calculate the moving averages of length 3 of a vector  $(x_1, \dots, x_n)^T$ . (The function returns  $(z_1, \dots, z_n)^T$  where  $z_i = (1/3)(x_i + x_{i+1} + x_{i+2})$ ,  $i=1, \dots, n-2$ ) Call this function `ma3`

```
ma3 <- function(xVec){
  if (is.numeric(xVec)==FALSE){
    stop("Invalid Input. Please enter a numeric vector")}
  n <- length(xVec)
  z <- ( xVec[1:(n-2)]+xVec[2:(n-1)]+xVec[3:n])/3
  return(z)
}
ma3(c(1:5,6:1))
```

```
## [1] 2.000000 3.000000 4.000000 5.000000 5.333333 5.000000 4.000000 3.000000
## [9] 2.000000
```

- b. Write a function which takes two arguments, `x` and `k`, and calculates the moving average of `x` for length `k`

```
ma.k <- function(x,k){
  if (is.numeric(x)==FALSE){
    stop("Invalid Input. Please enter a numeric vector")}
  z <- filter(x,rep(1/k,k))
  if (k==1){
    stop("Invalid Input. K must be greater than 1.")
  }
  if ((length(k)<length(x))==TRUE){
    stop("Invalid Input. K cannot be larger than or equal to x.")
  }
  return(z)
}
#ma.k(c(1,2,3,4,5,6),3)
#ma.k(c(1:3),1)
```

- c. How does your function behave if `k` is larger than (or equal to) the length of `x`? There is an error message that says: Error in `filter(x, rep(1/k, k))` : 'filter' is longer than time series.
- d. You should return an error, use the `stop()` function. Are there other choices? Error message included.
- e. How does your function behave if `k=1`? What should you do? Fit it if necessary? If `k=1`, then the error message pops up saying that `k` cannot be larger than or equal to `x`. To fix it, we should say that `k` must be greater than 1.

## Problem 3. Optional Plot

Continuous functions:  $f(x) = x^2 + 2x + 3$  if  $x < 0$  =  $x + 3$  if  $0 \leq x < 2$  =  $x^2 + 4x - 7$  if  $x \geq 2$

Write a function which takes a vector and returns a vector of the values  $f(x)$ . The function should be valid for inputs where  $-4 < x < 4$ . The function should check the input for validity and offer the user the option of plotting the values the function returns

```

prob2 <- function(x, plot = FALSE)
{
  if (-4 < x & x < 0){
    z = ((x^2)+2*x+3)
    return(z)
  }
  if (0 <= x & x < 2){
    z = (x+3)
    return(z)
  }
  if (2 <= x & x < 4){
    z = ((x^2)+4*x-7)
    return(z)
  }
  if(plot==TRUE){
    plot(x)
  }
  else{
    stop("Input Invalid. Please enter a number between -4 and 4.")
  }
}
prob2(0)

```

```
## [1] 3
```

```

#prob2(-4)
prob2(2,TRUE)

```

```
## [1] 5
```

```
prob2(1)
```

```
## [1] 4
```

```
prob2(3)
```

```
## [1] 14
```

```
#prob2(5)
```

#### Problem 4. Matrix Input

Write a function which takes a single argument, a matrix or an arguments that can be coerced into a matrix and return a matrix which is the same as the function of the argument, but every odd number is doubled

```

double <- function(mat)
{
  x = nrow(mat)
  y = ncol(mat)
  for(i in 1:x){
    for(j in 1:y){
      if(mat[i,j]%%2==1){
        mat[i,j] = mat[i,j]*2
      }
    }
  }
  return(mat)
}

```

```
}  
matrix1 <- matrix(c(2,-4,-5,7), nrow = 4,ncol = 4 ,byrow = TRUE)  
double(matrix1)
```

```
##      [,1] [,2] [,3] [,4]  
## [1,]    2   -4  -10   14  
## [2,]    2   -4  -10   14  
## [3,]    2   -4  -10   14  
## [4,]    2   -4  -10   14
```