



Definitions

1. Complexity:

- a. Big O- Tight upper bound. Better than or equal to this in the worst case.
- b. Big Theta- Bound within a constant. This is the exact efficiency.
- c. Big Omega- lower bound. It's this at best case.
- d. Order of growth - unaffected by constants. Normally defined by a big O.
- e. Recurrence Relation - A recurrence relation is **an equation that defines a sequence based on a rule that gives the next term as a function of the previous term(s)**
. for some function f . One such example is $x_{n+1} = 2 - x_n/2$. for some function f with two inputs.
- f. Telescoping - take a large number of terms to a small constant number of terms

2. Dynamic Programming - To make brute force recursive algorithms more efficient:

- a. Memoization - improve recursion by storing results in a table full of -1s. Can increase efficiency in space and time, but not always. Time and space efficiency are NOT always the same.
- b. Tabulation - calculate the results from the bottom up. Something is tabulated if it uses the previous calculation to make the next calculation in ANY way. no recursion used! - requires recursive thinking, but not recursive code.

3. Types of Algorithms

- Brute Force algorithm - do all the work the longest way. By checking all answers.
- Greedy algorithm - go for largest or smallest of something.
- Recursive algorithm - defined in terms of itself
- Divide & Conquer algorithm - call children to do work.

- Dynamic programming algorithm

4. **Graphs:**

- **Graph** - vertices and edges
- **cyclical** - it's possible to get back to an origin point through other vertices.
- **loop**: start at a point, end at the same point
- **complete graph**: on 5 vertices can be shorthand to K4. This is the most dense graph and the most dense simple graph
- **a simple graph** - no loops or double edges
- **tree**: connected acyclical graph
- Also tree: the number of edges is one less than the number of vertices $\rightarrow e = v - 1$ and $v = e + 1$
- **A minimal spanning tree (MST)** tries to find the lowest "cost" path to connect all vertices of a simple weighted graph.
- Degree of a vertex is the number of edges connecting to that vertex
- Connected graph: a path between every pair of vertices
- complete graph \rightarrow every point attaches to every other point directly.