

# Taking uncertainty seriously

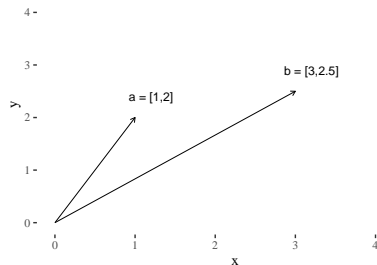
A Bayesian approach to word embedding bias estimation

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Boston, April Fools' Day

# Cosine similarity

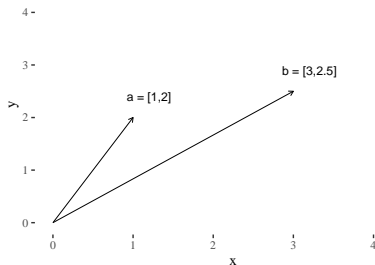
## Vectors



$$a = [1, 2]$$

$$b = [3, 2]$$

# Cosine similarity



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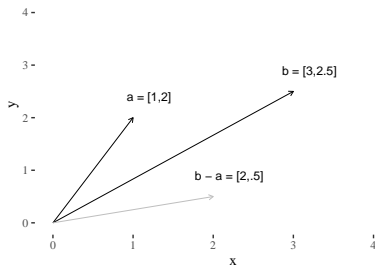
## Dot product

$$a \cdot b = a_1 b_1 + a_2 b_2$$

$$a \cdot a = a_1^2 + a_2^2$$

$$\|a\| = \sqrt{a \cdot a}$$

# Cosine similarity



## Vectors

$$a = [1, 2]$$

$$b = [4, 4]$$

## Dot product

$$a \cdot b = a_1 b_1 + a_2 b_2$$

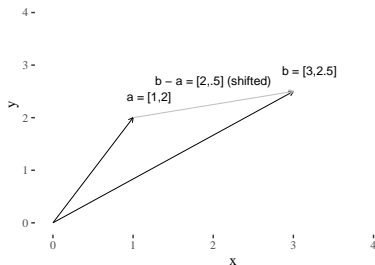
$$a \cdot a = a_1^2 + a_2^2$$

$$\|a\| = \sqrt{a \cdot a}$$

## Vector difference

$$b - a = [b_1 - a_1, b_2 - a_2]$$

# Cosine similarity



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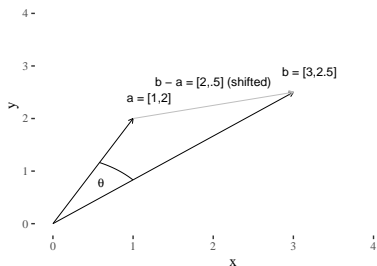
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# Cosine similarity



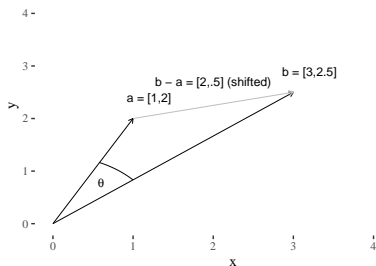
## Angle

$$\|b - a\|^2 = \|b\|^2 + \|a\|^2 - 2\|b\|\|a\| \cos \theta$$

$$b \cdot a = \|b\|\|a\| \cos \theta$$

$$\cos \theta = \frac{b \cdot a}{\|b\|\|a\|}$$

# Cosine similarity



## Angle

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## Orthogonality

$$\cos(90^\circ) = 0$$

$$\frac{b \cdot a}{\|b\|\|a\|} = 0$$

$$b \cdot a = 0$$