# Métodos para resolución de sistemas de ecuaciones lineales LU

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# 1 Metodo Lu

### 1.1 Caso de matrices de $2 \times 2$

$$\begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} = \begin{pmatrix} l_{11} & 0 \\ l_{21} & l_{22} \end{pmatrix} \cdot \begin{pmatrix} 1 & u_{12} \\ 0 & 1 \end{pmatrix}$$
$$\begin{pmatrix} l_{11} & u_{12} \\ l_{21} & l_{22} \end{pmatrix}$$

$$a_{11} = l_{11}$$
  $l_{11} = a_{11}$   $l_{21} = a_{21}$   $l_{21} = a_{21}$   $l_{21} = a_{21}$   $l_{22} = l_{21}u_{12} + l_{22}$   $u_{12} = \frac{a_{12}}{l_{11}}$   $l_{22} = a_{22} - l_{21}u_{12}$ 

# 1.2 Caso de matrices de $3 \times 3$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 \\ l_{21} & l_{22} & 0 \\ l_{31} & l_{32} & l_{33} \end{pmatrix} \cdot \begin{pmatrix} 1 & u_{12} & u_{13} \\ 0 & 1 & u_{23} \\ 0 & 0 & 1 \end{pmatrix}$$
 
$$\begin{pmatrix} l_{11} & u_{12} & u_{13} \\ l_{21} & l_{22} & u_{23} \\ l_{31} & l_{32} & l_{33} \end{pmatrix}$$

$$a_{11} = l_{11}$$

$$a_{21} = l_{21}$$

$$a_{31} = l_{31}$$

$$a_{12} = l_{11}u_{12}$$

$$a_{22} = l_{21}u_{12} + l_{22}$$

$$a_{32} = l_{31}u_{12} + l_{32}$$

$$a_{13} = l_{11}u_{13}$$

$$a_{23} = l_{21}u_{13} + l_{22}u_{23}$$

$$a_{33} = l_{31}u_{13} + l_{32}u_{23} + l_{33}$$

$$l_{11} = a_{11}$$

$$l_{11} = a_{11}$$

$$l_{21} = a_{21}$$

$$l_{21} = a_{21}$$

$$l_{22} = a_{22} - l_{21}u_{12}$$

$$l_{32} = a_{32} - l_{31}u_{12}$$

$$u_{13} = \frac{a_{13}}{l_{11}}$$

$$u_{23} = \frac{a_{23} - l_{21}u_{13}}{l_{22}}$$

$$l_{33} = a_{33} - l_{31}u_{13} - l_{32}u_{23}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} \end{pmatrix} \cdot \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} \\ 0 & 1 & u_{23} & u_{24} \\ 0 & 0 & 1 & u_{34} \\ 0 & 0 & 0 & 1 \end{pmatrix}$$
 
$$\begin{pmatrix} l_{11} & u_{12} & u_{13} & u_{14} \\ l_{21} & l_{22} & u_{23} & u_{24} \\ l_{31} & l_{32} & l_{33} & u_{34} \\ l_{41} & l_{42} & l_{43} & l_{44} \end{pmatrix}$$

$$\begin{array}{c} a_{11} = l_{11} \\ a_{21} = l_{21} \\ a_{31} = l_{31} \\ a_{31} = l_{31} \\ a_{41} = l_{41} \\ a_{12} = l_{11}u_{13} \\ a_{23} = l_{21}u_{13} + l_{22}u_{23} \\ a_{41} = l_{41} \\ a_{12} = l_{11}u_{12} \\ a_{22} = l_{21}u_{12} + l_{22} \\ \end{array}$$

$$a_{24} = l_{21}u_{14} + l_{22}u_{24}$$

$$a_{34} = l_{31}u_{14} + l_{32}u_{24} + l_{33}u_{34}$$

$$l_{21} = a_{21}$$

$$l_{31} = a_{31}$$

$$l_{41} = a_{41}$$

$$u_{12} = \frac{a_{12}}{l_{11}}$$

$$l_{22} = a_{22} - l_{21}u_{12}$$

$$l_{32} = a_{32} - l_{31}u_{12}$$

$$l_{42} = a_{42} - l_{41}u_{12}$$

$$u_{13} = \frac{a_{13}}{l_{11}}$$

$$u_{23} = \frac{a_{23} - l_{21}u_{13}}{l_{22}}$$

$$l_{33} = a_{33} - l_{31}u_{13} - l_{32}u_{23}$$

 $l_{43} = a_{43} - l_{41}u_{13} - l_{42}u_{23}$ 

 $u_{14} = \frac{a_{14}}{l_{11}}$ 

 $u_{24} = \frac{a_{24} - l_{21}u_{14}}{l_{22}}$ 

 $u_{34} = \frac{a_{34} - l_{31}u_{14} - l_{32}u_{24}}{l_{33}}$ 

 $l_{44} = a_{44} - l_{41}u_{14} - l_{42}u_{24} - l_{43}u_{34}$ 

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & l_{55} \end{pmatrix} \cdot \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} & u_{15} \\ 0 & 1 & u_{23} & u_{24} & u_{25} \\ 0 & 0 & 1 & u_{34} & u_{35} \\ 0 & 0 & 0 & 1 & u_{45} \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\begin{array}{c} a_{11}=l_{11} \\ a_{21}=l_{21} \\ a_{31}=l_{31} \\ a_{21}=l_{21} \\ a_{41}=l_{41} \\ a_{51}=l_{51} \\ a_{12}=l_{11}u_{12} \\ a_{22}=l_{21}u_{12}+l_{22} \\ a_{32}=l_{31}u_{12}+l_{32} \\ a_{42}=l_{41}u_{12}+l_{42} \\ a_{52}=l_{51}u_{12}+l_{52} \\ a_{13}=l_{11}u_{13} \\ a_{23}=l_{21}u_{13}+l_{22}u_{23} \\ a_{33}=l_{31}u_{13}+l_{32}u_{23}+l_{33} \end{array}$$

$$l_{11} = a_{11}$$

$$l_{21} = a_{21}$$

$$l_{31} = a_{31}$$

$$l_{41} = a_{41}$$

$$l_{51} = a_{51}$$

$$u_{12} = \frac{a_{12}}{l_{11}}$$

$$l_{22} = a_{22} - l_{21}u_{12}$$

$$l_{32} = a_{32} - l_{31}u_{12}$$

$$l_{42} = a_{42} - l_{41}u_{12}$$

$$l_{52} = a_{52} - l_{51}u_{12}$$

$$u_{13} = \frac{a_{13}}{l_{11}}$$

$$u_{23} = \frac{a_{23} - l_{21}u_{13}}{l_{22}}$$

$$l_{33} = a_{33} - l_{31}u_{13} - l_{32}u_{23}$$

$$l_{43} = a_{43} - l_{41}u_{13} - l_{42}u_{23}$$

$$l_{53} = a_{53} - l_{51}u_{13} - l_{52}u_{23}$$

$$u_{14} = \frac{a_{14}}{l_{11}}$$

$$u_{24} = \frac{a_{24} - l_{21}u_{14}}{l_{22}}$$

$$u_{34} = \frac{a_{34} - l_{31}u_{14} - l_{32}u_{24}}{l_{33}}$$

$$l_{44} = a_{44} - l_{41}u_{14} - l_{42}u_{24} - l_{43}u_{34}$$

$$l_{54} = a_{54} - l_{51}u_{14} - l_{52}u_{24} - l_{53}u_{34}$$

$$u_{15} = \frac{a_{15}}{l_{11}}$$

$$u_{25} = \frac{a_{25} - l_{21}u_{15}}{l_{22}}$$

$$u_{35} = \frac{a_{35} - l_{31}u_{15} - l_{32}u_{25}}{l_{33}}$$

$$u_{45} = \frac{a_{45} - l_{41}u_{15} - l_{42}u_{25} - l_{43}u_{35}}{l_{44}}$$

$$l_{55} = a_{55} - l_{51}u_{15} - l_{52}u_{25} - l_{53}u_{35} - l_{54}u_{45}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & a_{16} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} & a_{26} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} & a_{36} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} & a_{46} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} & a_{56} \\ a_{61} & a_{62} & a_{63} & a_{64} & a_{65} & a_{66} \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 & 0 & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 & 0 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} & 0 & 0 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & l_{55} & 0 & 0 \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & l_{66} \end{pmatrix} \cdot \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ 0 & 1 & u_{23} & u_{24} & u_{25} & u_{26} \\ 0 & 0 & 1 & u_{34} & u_{35} & u_{36} \\ 0 & 0 & 0 & 1 & u_{45} & u_{46} \\ 0 & 0 & 0 & 0 & 1 & u_{56} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\begin{pmatrix} l_{11} & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ l_{21} & l_{22} & u_{23} & u_{24} & u_{25} & u_{26} \\ l_{31} & l_{32} & l_{33} & u_{34} & u_{35} & u_{36} \\ l_{41} & l_{42} & l_{43} & l_{44} & u_{45} & u_{46} \\ l_{51} & l_{52} & l_{53} & l_{54} & l_{55} & u_{56} \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & l_{66} \end{pmatrix}$$

$$a_{11} = l_{11}$$

$$a_{21} = l_{21}$$

$$a_{31} = l_{31}$$

$$a_{41} = l_{41}$$

$$a_{41} = l_{41}$$

$$a_{51} = l_{51}$$

$$a_{12} = l_{11}u_{12}$$

$$a_{61} = l_{61}$$

$$a_{12} = l_{11}u_{12}$$

$$a_{22} = l_{21}u_{12} + l_{22}u_{24} + l_{31}u_{34} + l_{44}$$

$$a_{61} = l_{61}$$

$$a_{12} = l_{11}u_{12}$$

$$a_{32} = l_{31}u_{12} + l_{32}$$

$$a_{42} = l_{21}u_{14} + l_{22}u_{24} + l_{31}u_{34} + l_{44}$$

$$a_{61} = l_{61}$$

$$a_{12} = l_{11}u_{12}$$

$$a_{64} = l_{61}u_{14} + l_{62}u_{24} + l_{63}u_{34} + l_{64}$$

$$a_{22} = l_{21}u_{12} + l_{22}$$

$$a_{42} = l_{41}u_{12} + l_{42}$$

$$a_{43} = l_{41}u_{12} + l_{42}$$

$$a_{51} = l_{51}u_{15} + l_{52}u_{25}$$

$$a_{42} = l_{41}u_{12} + l_{42}$$

$$a_{52} = l_{51}u_{15} + l_{52}u_{25}$$

$$a_{43} = l_{61}u_{15} + l_{62}u_{25} + l_{63}u_{35} + l_{64}u_{45} + l_{55}$$

$$a_{13} = l_{11}u_{13}$$

$$a_{23} = l_{21}u_{13} + l_{22}u_{23}$$

$$a_{33} = l_{31}u_{13} + l_{32}u_{23} + l_{33}$$

$$a_{26} = l_{21}u_{16} + l_{22}u_{26}$$

$$a_{33} = l_{31}u_{15} + l_{32}u_{25} + l_{33}u_{36}$$

$$a_{46} = l_{41}u_{16} + l_{42}u_{26} + l_{43}u_{36} + l_{44}u_{46}$$

$$a_{56} = l_{51}u_{16} + l_{52}u_{26} + l_{53}u_{36} + l_{54}u_{46} + l_{55}u_{56}$$

$$a_{66} = l_{61}u_{16} + l_{62}u_{26} + l_{63}u_{36} + l_{64}u_{46} + l_{65}u_{56} + l_{66}$$

$$\begin{split} I_{11} &= a_{11} \\ I_{21} &= a_{21} \\ I_{31} &= a_{31} \\ I_{41} &= a_{41} \\ I_{51} &= a_{51} \\ I_{61} &= a_{61} \\ u_{12} &= \frac{a_{12}}{I_{11}} \\ I_{22} &= a_{22} - I_{21} u_{12} \\ I_{32} &= a_{32} - I_{31} u_{12} \\ I_{42} &= a_{42} - I_{41} u_{12} \\ I_{52} &= a_{52} - I_{51} u_{12} \\ I_{62} &= a_{62} - I_{61} u_{12} \\ u_{13} &= \frac{a_{13}}{I_{11}} \\ u_{23} &= \frac{a_{23} - I_{21} u_{13}}{I_{22}} \\ I_{33} &= a_{33} - I_{31} u_{13} - I_{32} u_{23} \\ I_{43} &= a_{43} - I_{41} u_{13} - I_{42} u_{23} \\ I_{53} &= a_{53} - I_{51} u_{13} - I_{52} u_{23} \\ I_{63} &= a_{63} - I_{61} u_{13} - I_{62} u_{23} \\ u_{14} &= \frac{a_{14}}{I_{11}} \\ u_{24} &= \frac{a_{24} - I_{21} u_{14}}{I_{22}} \\ u_{34} &= \frac{a_{34} - I_{31} u_{14} - I_{32} u_{24}}{I_{33}} \\ I_{44} &= a_{44} - I_{41} u_{14} - I_{42} u_{24} - I_{43} u_{34} \\ I_{54} &= a_{54} - I_{51} u_{14} - I_{52} u_{24} - I_{53} u_{34} \\ I_{64} &= a_{64} - I_{61} u_{14} - I_{62} u_{24} - I_{63} u_{35} \\ u_{15} &= \frac{a_{15}}{I_{11}} \\ u_{25} &= \frac{a_{25} - I_{21} u_{15}}{I_{22}} \\ u_{35} &= \frac{a_{35} - I_{31} u_{15} - I_{32} u_{25}}{I_{33}} \\ u_{45} &= \frac{a_{45} - I_{41} u_{15} - I_{42} u_{25} - I_{43} u_{35}}{I_{44}} \\ I_{55} &= a_{55} - I_{51} u_{15} - I_{52} u_{25} - I_{63} u_{35} - I_{64} u_{45} \\ u_{16} &= \frac{a_{16}}{I_{11}} \\ u_{26} &= \frac{a_{26} - I_{21} u_{16}}{I_{22}} \\ u_{36} &= \frac{a_{36} - I_{31} u_{16} - I_{32} u_{26}}{I_{33}} \\ u_{46} &= \frac{a_{36} - I_{31} u_{16} - I_{32} u_{26}}{I_{33}} \\ u_{46} &= \frac{a_{36} - I_{51} u_{16} - I_{52} u_{26} - I_{53} u_{36} - I_{54} u_{46}}{I_{45}} \\ u_{56} &= \frac{a_{66} - I_{61} u_{16} - I_{62} u_{26} - I_{63} u_{36} - I_{64} u_{46} - I_{65} u_{56}}{I_{55}} \\ I_{66} &= a_{66} - I_{61} u_{16} - I_{62} u_{26} - I_{63} u_{36} - I_{64} u_{46} - I_{65} u_{56} \\ I_{65} &= a_{66} - I_{61} u_{16} - I_{62} u_{26} - I_{63} u_{36} - I_{64} u_{46} - I_{65} u_{56} \\ I_{66} &= a_{66} - I_{61} u_{16} - I_{62} u_{26} - I_{63} u_{36} - I_{64} u_{46} - I_{65} u_{56} \\ I_{66} &= a_{66} - I_{61} u_{16} - I_{62} u_{26} - I_{63} u_{36} - I_{64} u_{46} - I_{65} u_{56} \\ I_{66$$

### 2 Metodo lU

### 2.1 Caso de matrices de $2 \times 2$

$$\begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ l_{21} & 1 \end{pmatrix} \cdot \begin{pmatrix} u_{11} & u_{12} \\ 0 & u_{22} \end{pmatrix}$$
 
$$\begin{pmatrix} u_{11} & u_{12} \\ l_{21} & u_{22} \end{pmatrix}$$

$$a_{11} = u_{11}$$
  $u_{11} = a_{11}$ 
 $a_{21} = l_{21}u_{11}$ 
 $a_{12} = u_{12}$ 
 $a_{22} = l_{21}u_{12} + u_{22}$ 
 $u_{12} = a_{12}$ 
 $u_{12} = a_{12}$ 
 $u_{22} = a_{22} - l_{21}u_{12}$ 

### 2.2 Caso de matrices de $3 \times 3$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ l_{21} & 1 & 0 \\ l_{31} & l_{32} & 1 \end{pmatrix} \cdot \begin{pmatrix} u_{11} & u_{12} & u_{13} \\ 0 & u_{22} & u_{23} \\ 0 & 0 & u_{33} \end{pmatrix}$$
 
$$\begin{pmatrix} u_{11} & u_{12} & u_{13} \\ l_{21} & u_{22} & u_{23} \\ l_{31} & l_{32} & u_{33} \end{pmatrix}$$

$$a_{11} = u_{11}$$

$$a_{21} = l_{21}u_{11}$$

$$a_{31} = l_{31}u_{11}$$

$$a_{12} = u_{12}$$

$$l_{31} = \frac{a_{31}}{u_{11}}$$

$$l_{31} = \frac{a_{31}}{u_{11}}$$

$$l_{31} = a_{12}$$

$$u_{12} = a_{12}$$

$$u_{13} = u_{13}$$

$$a_{23} = l_{21}u_{13} + u_{23}$$

$$u_{13} = a_{13}$$

$$u_{23} = a_{23} - l_{21}u_{13}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 \\ l_{41} & l_{42} & l_{43} & 1 \end{pmatrix} \cdot \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} \\ 0 & u_{22} & u_{23} & u_{24} \\ 0 & 0 & u_{33} & u_{34} \\ 0 & 0 & 0 & u_{44} \end{pmatrix}$$
 
$$\begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} \\ l_{21} & u_{22} & u_{23} & u_{24} \\ l_{31} & l_{32} & u_{33} & u_{34} \\ l_{41} & l_{42} & l_{43} & u_{44} \end{pmatrix}$$

$$a_{32} = l_{31}u_{12} + l_{32}u_{22}$$

$$a_{11} = u_{11}$$

$$a_{21} = l_{21}u_{11}$$

$$a_{31} = l_{31}u_{11}$$

$$a_{41} = l_{41}u_{11}$$

$$a_{12} = u_{12}$$

$$a_{22} = l_{21}u_{12} + u_{22}$$

$$a_{32} = l_{31}u_{12} + l_{42}u_{22}$$

$$a_{13} = u_{13}$$

$$a_{23} = l_{21}u_{13} + u_{23}$$

$$a_{33} = l_{31}u_{13} + l_{32}u_{23} + u_{33}$$

$$a_{43} = l_{41}u_{13} + l_{42}u_{23} + l_{43}u_{33}$$

$$a_{14} = u_{14}$$

$$a_{24} = l_{21}u_{14} + u_{24}$$

$$a_{34} = l_{31}u_{14} + l_{32}u_{24} + u_{34}$$

$$a_{44} = l_{41}u_{14} + l_{42}u_{24} + l_{43}u_{34} + u_{44}$$

$$u_{11} = a_{11}$$

$$l_{21} = \frac{a_{21}}{u_{11}}$$

$$l_{31} = \frac{a_{31}}{u_{11}}$$

$$l_{41} = \frac{a_{41}}{u_{11}}$$

$$u_{12} = a_{12}$$

$$u_{22} = a_{22} - l_{21}u_{12}$$

$$l_{32} = \frac{a_{32} - l_{31}u_{12}}{u_{22}}$$

$$l_{42} = \frac{a_{42} - l_{41}u_{12}}{u_{22}}$$

$$u_{13} = a_{13}$$

$$u_{23} = a_{23} - l_{21}u_{13}$$

$$u_{33} = a_{33} - l_{31}u_{13} - l_{32}u_{23}$$

$$l_{43} = \frac{a_{43} - l_{41}u_{13} - l_{42}u_{23}}{u_{33}}$$

$$u_{14} = a_{14}$$

$$u_{24} = a_{24} - l_{21}u_{14}$$

$$u_{34} = a_{34} - l_{31}u_{14} - l_{32}u_{24}$$

$$u_{44} = a_{44} - l_{41}u_{14} - l_{42}u_{24} - l_{43}u_{34}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & 1 & 0 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & 1 & 0 \end{pmatrix} \cdot \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} \\ 0 & u_{22} & u_{23} & u_{24} & u_{25} \\ 0 & 0 & u_{33} & u_{34} & u_{35} \\ 0 & 0 & 0 & 0 & u_{44} & u_{45} \\ 0 & 0 & 0 & 0 & 0 & u_{55} \end{pmatrix}$$

$$a_{11} = u_{11}$$

$$a_{21} = l_{21}u_{11}$$

$$a_{31} = l_{31}u_{11}$$

$$a_{41} = l_{41}u_{11}$$

$$a_{41} = l_{41}u_{11}$$

$$a_{51} = l_{51}u_{11}$$

$$a_{12} = u_{12}$$

$$a_{22} = l_{21}u_{12} + u_{22}$$

$$a_{32} = l_{31}u_{12} + l_{32}u_{22}$$

$$a_{42} = l_{41}u_{12} + l_{42}u_{22}$$

$$a_{42} = l_{41}u_{12} + l_{42}u_{22}$$

$$a_{42} = l_{41}u_{12} + l_{42}u_{22}$$

$$a_{43} = l_{31}u_{14} + l_{42}u_{23} + l_{43}u_{33}$$

$$a_{43} = l_{31}u_{14} + u_{24}$$

$$a_{24} = l_{21}u_{14} + u_{24}$$

$$a_{44} = l_{41}u_{14} + l_{42}u_{24} + l_{43}u_{34} + u_{44}$$

$$a_{54} = l_{51}u_{14} + l_{52}u_{24} + l_{53}u_{34} + l_{54}u_{44}$$

$$a_{54} = l_{51}u_{14} + l_{52}u_{24} + l_{53}u_{34} + l_{54}u_{44}$$

$$a_{54} = l_{51}u_{14} + l_{52}u_{24} + l_{53}u_{34} + l_{54}u_{44}$$

$$a_{55} = l_{51}u_{15} + l_{52}u_{25} + u_{35}$$

$$a_{45} = l_{41}u_{15} + l_{42}u_{25} + l_{43}u_{35} + u_{45}$$

$$a_{55} = l_{51}u_{15} + l_{52}u_{25} + l_{53}u_{35} + l_{54}u_{45} + u_{55}$$

$$a_{23} = l_{21}u_{13} + u_{23}$$

$$a_{33} = l_{31}u_{13} + l_{32}u_{23} + u_{33}$$

$$u_{11} = a_{11}$$

$$l_{21} = \frac{a_{21}}{u_{11}}$$

$$l_{31} = \frac{a_{31}}{u_{11}}$$

$$l_{41} = \frac{a_{41}}{u_{11}}$$

$$l_{51} = \frac{a_{51}}{u_{11}}$$

$$u_{12} = a_{12}$$

$$u_{22} = a_{22} - l_{21}u_{12}$$

$$l_{32} = \frac{a_{32} - l_{31}u_{12}}{u_{22}}$$

$$l_{42} = \frac{a_{42} - l_{41}u_{12}}{u_{22}}$$

$$l_{52} = \frac{a_{52} - l_{51}u_{12}}{u_{22}}$$

$$u_{13} = a_{13}$$

$$u_{23} = a_{23} - l_{21}u_{13}$$

$$u_{33} = a_{33} - l_{31}u_{13} - l_{32}u_{23}$$

$$l_{43} = \frac{a_{43} - l_{41}u_{13} - l_{42}u_{23}}{u_{33}}$$

$$l_{53} = \frac{a_{53} - l_{51}u_{13} - l_{52}u_{23}}{u_{33}}$$

$$u_{14} = a_{14}$$

$$u_{24} = a_{24} - l_{21}u_{14}$$

$$u_{34} = a_{34} - l_{31}u_{14} - l_{32}u_{24}$$

$$u_{44} = a_{44} - l_{41}u_{14} - l_{42}u_{24} - l_{43}u_{34}$$

$$l_{54} = \frac{a_{54} - l_{51}u_{14} - l_{52}u_{24} - l_{53}u_{34}}{u_{44}}$$

$$u_{15} = a_{15}$$

$$u_{25} = a_{25} - l_{21}u_{15}$$

$$u_{35} = a_{35} - l_{31}u_{15} - l_{32}u_{25}$$

$$u_{45} = a_{45} - l_{41}u_{15} - l_{42}u_{25} - l_{43}u_{35}$$

$$u_{55} = a_{55} - l_{51}u_{15} - l_{52}u_{25} - l_{53}u_{35} - l_{54}u_{45}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & a_{16} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} & a_{26} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} & a_{36} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} & a_{46} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} & a_{56} \\ a_{61} & a_{62} & a_{63} & a_{64} & a_{65} & a_{66} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 & 0 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 & 0 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & 1 & 0 & 0 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & 1 & 0 & 0 \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & 1 \end{pmatrix} \cdot \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ 0 & u_{22} & u_{23} & u_{24} & u_{25} & u_{26} \\ 0 & 0 & u_{33} & u_{34} & u_{35} & u_{36} \\ 0 & 0 & 0 & u_{44} & u_{45} & u_{46} \\ 0 & 0 & 0 & 0 & 0 & u_{55} & u_{56} \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{pmatrix}$$

$$\begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ l_{21} & u_{22} & u_{23} & u_{24} & u_{25} & u_{26} \\ l_{31} & l_{32} & u_{33} & u_{34} & u_{35} & u_{36} \\ l_{41} & l_{42} & l_{43} & u_{44} & u_{45} & u_{46} \\ l_{51} & l_{52} & l_{53} & l_{54} & u_{55} & u_{56} \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & u_{66} \end{pmatrix}$$

$$\begin{array}{c} a_{11}=u_{11} & a_{53}=l_{51}u_{13}+l_{52}u_{23}+l_{53}u_{33} \\ a_{21}=l_{21}u_{11} & a_{14}=u_{14} \\ a_{31}=l_{31}u_{11} & a_{24}=l_{21}u_{14}+u_{24} \\ a_{41}=l_{41}u_{11} & a_{34}=l_{31}u_{14}+l_{32}u_{24}+u_{34} \\ a_{51}=l_{51}u_{11} & a_{44}=l_{41}u_{14}+l_{42}u_{24}+l_{43}u_{34}+u_{44} \\ a_{61}=l_{61}u_{11} & a_{54}=l_{51}u_{14}+l_{52}u_{24}+l_{53}u_{34}+l_{54}u_{44} \\ a_{12}=u_{12} & a_{64}=l_{61}u_{14}+l_{62}u_{24}+l_{63}u_{34}+l_{64}u_{44} \\ a_{22}=l_{21}u_{12}+u_{22} & a_{15}=u_{15} \\ a_{32}=l_{31}u_{12}+l_{32}u_{22} & a_{25}=l_{21}u_{15}+u_{25} \\ a_{42}=l_{41}u_{12}+l_{42}u_{22} & a_{35}=l_{31}u_{15}+l_{32}u_{25}+u_{35} \\ a_{52}=l_{51}u_{12}+l_{52}u_{22} & a_{45}=l_{41}u_{15}+l_{42}u_{25}+l_{43}u_{35}+u_{45} \\ a_{62}=l_{61}u_{12}+l_{62}u_{22} & a_{55}=l_{51}u_{15}+l_{52}u_{25}+l_{53}u_{35}+l_{54}u_{45}+u_{55} \\ a_{13}=u_{13} & a_{65}=l_{61}u_{15}+l_{62}u_{25}+l_{63}u_{35}+l_{64}u_{45}+l_{65}u_{55} \\ a_{23}=l_{21}u_{13}+u_{23} & a_{66}=l_{61}u_{15}+l_{62}u_{25}+l_{63}u_{35}+l_{64}u_{45}+l_{65}u_{55} \\ a_{33}=l_{31}u_{13}+l_{32}u_{23}+u_{33} & a_{26}=l_{21}u_{16}+u_{26} \\ a_{43}=l_{41}u_{13}+l_{42}u_{23}+l_{43}u_{33} & a_{36}=l_{31}u_{16}+l_{32}u_{26}+u_{36} \\ \end{array}$$

$$a_{46} = l_{41}u_{16} + l_{42}u_{26} + l_{43}u_{36} + u_{46}$$
 
$$a_{56} = l_{51}u_{16} + l_{52}u_{26} + l_{53}u_{36} + l_{54}u_{46} + u_{56}$$
 
$$a_{66} = l_{61}u_{16} + l_{62}u_{26} + l_{63}u_{36} + l_{64}u_{46} + l_{65}u_{56} + u_{66}$$

$$u_{11} = a_{11}$$

$$l_{21} = \frac{a_{21}}{u_{11}}$$

$$l_{31} = \frac{a_{31}}{u_{11}}$$

$$l_{41} = \frac{a_{41}}{u_{11}}$$

$$l_{41} = \frac{a_{41}}{u_{11}}$$

$$l_{51} = \frac{a_{51}}{u_{11}}$$

$$l_{61} = \frac{a_{61}}{u_{11}}$$

$$u_{12} = a_{12}$$

$$u_{22} = a_{22} - l_{21}u_{12}$$

$$l_{32} = \frac{a_{32} - l_{31}u_{12}}{u_{22}}$$

$$l_{42} = \frac{a_{42} - l_{41}u_{12}}{u_{22}}$$

$$l_{52} = \frac{a_{52} - l_{51}u_{12}}{u_{22}}$$

$$l_{62} = \frac{a_{62} - l_{61}u_{12}}{u_{22}}$$

$$u_{13} = a_{13}$$

$$u_{23} = a_{23} - l_{21}u_{13}$$

$$u_{33} = a_{33} - l_{31}u_{13} - l_{32}u_{23}$$

$$l_{43} = \frac{a_{43} - l_{41}u_{13} - l_{42}u_{23}}{u_{33}}$$

$$l_{53} = \frac{a_{53} - l_{51}u_{13} - l_{52}u_{23}}{u_{33}}$$

$$l_{63} = \frac{a_{63} - l_{61}u_{13} - l_{62}u_{23}}{u_{33}}$$

$$u_{14} = a_{14}$$

$$u_{24} = a_{24} - l_{21}u_{14}$$

$$u_{34} = a_{34} - l_{31}u_{14} - l_{32}u_{24}$$

$$u_{44} = a_{44} - l_{41}u_{14} - l_{42}u_{24} - l_{43}u_{34}$$

$$l_{54} = \frac{a_{54} - l_{51}u_{14} - l_{52}u_{24} - l_{53}u_{34}}{u_{44}}$$

$$l_{64} = \frac{a_{64} - l_{61}u_{14} - l_{62}u_{24} - l_{63}u_{34}}{u_{44}}$$

$$u_{15} = a_{15}$$

$$u_{25} = a_{25} - l_{21}u_{15}$$

$$u_{35} = a_{35} - l_{31}u_{15} - l_{32}u_{25}$$

$$u_{45} = a_{45} - l_{41}u_{15} - l_{42}u_{25} - l_{43}u_{35}$$

$$u_{55} = a_{55} - l_{51}u_{15} - l_{52}u_{25} - l_{53}u_{35} - l_{54}u_{45}$$

$$l_{65} = \frac{a_{65} - l_{61}u_{15} - l_{62}u_{25} - l_{63}u_{35} - l_{64}u_{45}}{u_{55}}$$

$$u_{16} = a_{16}$$

$$u_{26} = a_{26} - l_{21}u_{16}$$

$$u_{36} = a_{36} - l_{31}u_{16} - l_{32}u_{26}$$

$$u_{46} = a_{46} - l_{41}u_{16} - l_{42}u_{26} - l_{43}u_{36}$$

$$u_{56} = a_{56} - l_{51}u_{16} - l_{52}u_{26} - l_{53}u_{36} - l_{54}u_{46}$$

$$u_{66} = a_{66} - l_{61}u_{16} - l_{62}u_{26} - l_{63}u_{36} - l_{64}u_{46} - l_{65}u_{56}$$

$$u_{66} = a_{66} - l_{61}u_{16} - l_{62}u_{26} - l_{63}u_{36} - l_{64}u_{46} - l_{65}u_{56}$$

$$u_{66} = a_{66} - l_{61}u_{16} - l_{62}u_{26} - l_{63}u_{36} - l_{64}u_{46} - l_{65}u_{56}$$

# 3 Metodo uL

### 3.1 Caso de matrices de $2 \times 2$

$$\begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} = \begin{pmatrix} 1 & u_{12} \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} l_{11} & 0 \\ l_{21} & l_{22} \end{pmatrix}$$
$$\begin{pmatrix} l_{11} & u_{12} \\ l_{21} & l_{22} \end{pmatrix}$$

$$a_{22} = l_{22}$$
  $l_{22} = a_{22}$ 
 $a_{12} = u_{12}l_{22}$   $u_{12} = \frac{a_{12}}{l_{22}}$ 
 $a_{21} = l_{21}$   $l_{21} = a_{21}$ 
 $l_{21} = a_{21}$ 
 $l_{11} = a_{11} - u_{12}l_{21}$ 

# 3.2 Caso de matrices de $3 \times 3$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} \\ 0 & 1 & u_{23} \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} l_{11} & 0 & 0 \\ l_{21} & l_{22} & 0 \\ l_{31} & l_{32} & l_{33} \end{pmatrix}$$
 
$$\begin{pmatrix} l_{11} & u_{12} & u_{13} \\ l_{21} & l_{22} & u_{23} \\ l_{31} & l_{32} & l_{33} \end{pmatrix}$$

$$\begin{array}{c} a_{33} = l_{33} & l_{33} = a_{33} \\ a_{23} = u_{23}l_{33} & u_{23} = \frac{a_{23}}{l_{33}} \\ a_{13} = u_{13}l_{33} & u_{13} = \frac{a_{13}}{l_{33}} \\ a_{32} = l_{32} & u_{13} = \frac{a_{13}}{l_{33}} \\ a_{22} = l_{22} + u_{23}l_{32} & l_{32} = a_{32} \\ a_{12} = u_{12}l_{22} + u_{13}l_{32} & l_{22} = a_{22} - u_{23}l_{32} \\ a_{31} = l_{31} & u_{12} = \frac{a_{12} - u_{13}l_{32}}{l_{22}} \\ a_{21} = l_{21} + u_{23}l_{31} & u_{12} = \frac{a_{12} - u_{13}l_{32}}{l_{22}} \\ a_{11} = l_{11} + u_{12}l_{21} + u_{13}l_{31} & l_{21} = a_{21} - u_{23}l_{31} \\ \end{array}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} \\ 0 & 1 & u_{23} & u_{24} \\ 0 & 0 & 1 & u_{34} \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} l_{11} & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} \end{pmatrix}$$
 
$$\begin{pmatrix} l_{11} & u_{12} & u_{13} & u_{14} \\ l_{21} & l_{22} & u_{23} & u_{24} \\ l_{31} & l_{32} & l_{33} & u_{34} \\ l_{41} & l_{42} & l_{43} & l_{44} \end{pmatrix}$$

$$a_{23} = u_{23}l_{33} + u_{24}l_{43}$$

$$a_{34} = u_{34}l_{44}$$

$$a_{24} = u_{24}l_{44}$$

$$a_{14} = u_{14}l_{44}$$

$$a_{25} = l_{25}l_{25}$$

$$a_{16} = l_{16}l_{25}$$

$$a_{17} = u_{11}l_{17}l_{17}$$

$$a_{18} = l_{18}l_{18}$$

$$a_{19} = l_{19}l_{19}l_{19}$$

$$a_{11} = u_{11}l_{19}l_{19}$$

$$a_{12} = u_{12}l_{19}l_{19} + u_{11}l_{19}l_{19}$$

$$a_{11} = u_{11}l_{19}l_{19}$$

$$a_{12} = u_{11}l_{19}l_{19}$$

$$a_{13} = l_{14}l_{19}$$

$$a_{31} = l_{31} + u_{34}l_{41}$$

$$a_{21} = l_{21} + u_{23}l_{31} + u_{24}l_{41}$$

$$a_{11} = l_{11} + u_{12}l_{21} + u_{13}l_{31} + u_{14}l_{41}$$

$$u_{24} = \frac{a_{34}}{l_{44}}$$

$$u_{14} = \frac{a_{14}}{l_{44}}$$

$$l_{43} = a_{43}$$

$$l_{33} = a_{33} - u_{34}l_{43}$$

$$u_{23} = \frac{a_{23} - u_{24}l_{43}}{l_{33}}$$

$$u_{13} = \frac{a_{13} - u_{14}l_{43}}{l_{33}}$$

$$l_{42} = a_{42}$$

$$l_{32} = a_{32} - u_{34}l_{42}$$

$$l_{22} = a_{22} - u_{23}l_{32} - u_{24}l_{42}$$

$$u_{12} = \frac{a_{12} - u_{13}l_{32} - u_{14}l_{42}}{l_{22}}$$

$$l_{41} = a_{41}$$

$$l_{31} = a_{31} - u_{34}l_{41}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} & u_{15} \\ 0 & 1 & u_{23} & u_{24} & u_{25} \\ 0 & 0 & 1 & u_{34} & u_{35} \\ 0 & 0 & 0 & 1 & u_{45} \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} l_{11} & 0 & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & l_{55} \end{pmatrix}$$

 $l_{21} = a_{21} - u_{23}l_{31} - u_{24}l_{41}$  $l_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41}$ 

$$a_{55} = l_{55}$$

$$a_{45} = u_{45}l_{55}$$

$$a_{25} = u_{25}l_{55}$$

$$a_{25} = u_{25}l_{55}$$

$$a_{15} = u_{15}l_{55}$$

$$a_{44} = l_{44} + u_{45}l_{54}$$

$$a_{34} = u_{34}l_{44} + u_{35}l_{54}$$

$$a_{24} = u_{24}l_{44} + u_{25}l_{54}$$

$$a_{14} = u_{14}l_{44} + u_{15}l_{54}$$

$$a_{33} = l_{33} + u_{34}l_{43} + u_{35}l_{53}$$

$$a_{33} = l_{33} + u_{34}l_{43} + u_{35}l_{53}$$

$$a_{31} = l_{31} + u_{34}l_{41} + u_{45}l_{51}$$

$$a_{21} = l_{21} + u_{23}l_{31} + u_{24}l_{41} + u_{25}l_{51}$$

$$a_{21} = l_{21} + u_{23}l_{31} + u_{24}l_{41} + u_{25}l_{51}$$

$$a_{21} = l_{21} + u_{23}l_{31} + u_{24}l_{41} + u_{25}l_{51}$$

$$a_{11} = l_{11} + u_{12}l_{21} + u_{13}l_{31} + u_{14}l_{41} + u_{15}l_{51}$$

$$l_{55} = a_{55}$$

$$u_{45} = \frac{a_{45}}{l_{55}}$$

$$u_{35} = \frac{a_{35}}{l_{55}}$$

$$u_{25} = \frac{a_{25}}{l_{55}}$$

$$u_{15} = \frac{a_{15}}{l_{55}}$$

$$l_{54} = a_{54}$$

$$l_{44} = a_{44} - u_{45}l_{54}$$

$$u_{34} = \frac{a_{34} - u_{35}l_{54}}{l_{44}}$$

$$u_{24} = \frac{a_{24} - u_{25}l_{54}}{l_{44}}$$

$$u_{14} = \frac{a_{14} - u_{15}l_{54}}{l_{44}}$$

$$l_{43} = a_{43} - u_{45}l_{53}$$

$$l_{33} = a_{33} - u_{34}l_{43} - u_{35}l_{53}$$

$$u_{23} = \frac{a_{23} - u_{24}l_{43} - u_{25}l_{53}}{l_{33}}$$

$$u_{13} = \frac{a_{13} - u_{14}l_{43} - u_{15}l_{53}}{l_{33}}$$

$$l_{52} = a_{52}$$

$$l_{42} = a_{42} - u_{45}l_{52}$$

$$l_{32} = a_{32} - u_{34}l_{42} - u_{35}l_{52}$$

$$l_{22} = a_{22} - u_{23}l_{32} - u_{24}l_{42} - u_{25}l_{52}$$

$$u_{12} = \frac{a_{12} - u_{13}l_{32} - u_{14}l_{42} - u_{15}l_{52}}{l_{22}}$$

$$l_{51} = a_{51}$$

$$l_{41} = a_{41} - u_{45}l_{51}$$

$$l_{31} = a_{31} - u_{34}l_{41} - u_{35}l_{51}$$

$$l_{21} = a_{21} - u_{23}l_{31} - u_{24}l_{41} - u_{25}l_{51}$$

$$l_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41} - u_{15}l_{51}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & a_{16} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} & a_{26} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} & a_{36} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} & a_{46} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} & a_{56} \\ a_{61} & a_{62} & a_{63} & a_{64} & a_{65} & a_{66} \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ 0 & 1 & u_{23} & u_{24} & u_{25} & u_{26} \\ 0 & 0 & 1 & u_{34} & u_{35} & u_{36} \\ 0 & 0 & 0 & 1 & u_{45} & u_{46} \\ 0 & 0 & 0 & 1 & u_{56} \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} l_{11} & 0 & 0 & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} & 0 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & l_{55} & 0 \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & l_{66} \end{pmatrix}$$

$$a_{66} = l_{66}$$

$$a_{56} = u_{56}l_{66}$$

$$a_{46} = u_{46}l_{66}$$

$$a_{36} = u_{36}l_{66}$$

$$a_{26} = u_{26}l_{66}$$

$$a_{16} = u_{16}l_{66}$$

$$a_{65} = l_{65}$$

$$a_{55} = l_{55} + u_{56}l_{65}$$

$$a_{45} = u_{45}l_{55} + u_{46}l_{65}$$

$$a_{35} = u_{35}l_{55} + u_{36}l_{65}$$

$$a_{25} = u_{25}l_{55} + u_{26}l_{65}$$

$$a_{15} = u_{15}l_{55} + u_{16}l_{65}$$

$$a_{64} = l_{64}$$

$$a_{54} = l_{54} + u_{56}l_{64}$$

$$a_{44} = l_{44} + u_{45}l_{54} + u_{46}l_{64}$$

$$a_{34} = u_{34}l_{44} + u_{35}l_{54} + u_{36}l_{64}$$

$$a_{24} = u_{24}l_{44} + u_{25}l_{54} + u_{26}l_{64}$$

$$a_{14} = u_{14}l_{44} + u_{15}l_{54} + u_{16}l_{64}$$

$$a_{63} = l_{63}$$

$$a_{53} = l_{53} + u_{56}l_{63}$$

$$a_{43} = l_{43} + u_{45}l_{53} + u_{46}l_{63}$$

$$a_{33} = l_{33} + u_{34}l_{43} + u_{35}l_{53} + u_{36}l_{63}$$

$$a_{23} = u_{23}l_{33} + u_{24}l_{43} + u_{25}l_{53} + u_{26}l_{63}$$

$$a_{13} = u_{13}l_{33} + u_{14}l_{43} + u_{15}l_{53} + u_{16}l_{63}$$

$$a_{62} = l_{62}$$

$$a_{52} = l_{52} + u_{56}l_{62}$$

$$a_{42} = l_{42} + u_{45}l_{52} + u_{46}l_{62}$$

$$a_{32} = l_{32} + u_{34}l_{42} + u_{35}l_{52} + u_{36}l_{62}$$

$$a_{22} = l_{22} + u_{23}l_{32} + u_{24}l_{42} + u_{25}l_{52} + u_{26}l_{62}$$

$$a_{12} = u_{12}l_{22} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{61} = l_{61}$$

$$a_{51} = l_{51} + u_{56}l_{61}$$

$$a_{41} = l_{41} + u_{45}l_{51} + u_{46}l_{61}$$

$$a_{31} = l_{31} + u_{34}l_{41} + u_{35}l_{51} + u_{36}l_{61}$$

$$a_{21} = l_{21} + u_{23}l_{31} + u_{24}l_{41} + u_{25}l_{51} + u_{26}l_{61}$$

$$a_{11} = l_{11} + u_{12}l_{21} + u_{13}l_{31} + u_{14}l_{41} + u_{15}l_{51} + u_{16}l_{61}$$

$$l_{66} = a_{66}$$

$$u_{56} = \frac{a_{56}}{l_{66}}$$

$$u_{46} = \frac{a_{46}}{l_{66}}$$

$$u_{46} = \frac{a_{46}}{l_{66}}$$

$$u_{36} = \frac{a_{36}}{l_{66}}$$

$$u_{26} = \frac{a_{26}}{l_{66}}$$

$$u_{16} = \frac{a_{16}}{l_{66}}$$

$$u_{16} = \frac{a_{16}}{l_{66}}$$

$$l_{55} = a_{55} - u_{56}l_{65}$$

$$u_{45} = \frac{a_{45} - u_{46}l_{65}}{l_{55}}$$

$$u_{35} = \frac{a_{35} - u_{36}l_{55}}{l_{55}}$$

$$u_{25} = \frac{a_{25} - u_{26}l_{65}}{l_{55}}$$

$$u_{15} = \frac{a_{15} - u_{16}l_{65}}{l_{55}}$$

$$l_{64} = a_{64}$$

$$l_{54} = a_{54} - u_{56}l_{64}$$

$$l_{44} = a_{44} - u_{45}l_{54} - u_{46}l_{64}$$

$$u_{34} = \frac{a_{34} - u_{35}l_{54} - u_{36}l_{64}}{l_{44}}$$

$$u_{14} = \frac{a_{14} - u_{15}l_{54} - u_{16}l_{64}}{l_{44}}$$

$$u_{14} = \frac{a_{14} - u_{15}l_{54} - u_{16}l_{64}}{l_{44}}$$

$$u_{14} = \frac{a_{14} - u_{15}l_{54} - u_{16}l_{64}}{l_{44}}$$

$$u_{13} = \frac{a_{13} - u_{14}l_{43} - u_{35}l_{53} - u_{36}l_{63}}{l_{33}}$$

$$u_{13} = \frac{a_{13} - u_{14}l_{43} - u_{15}l_{53} - u_{16}l_{63}}{l_{33}}$$

$$u_{13} = \frac{a_{13} - u_{14}l_{43} - u_{15}l_{53} - u_{16}l_{63}}{l_{33}}$$

$$u_{13} = \frac{a_{13} - u_{14}l_{43} - u_{15}l_{53} - u_{16}l_{63}}{l_{33}}$$

$$u_{14} = \frac{a_{14} - u_{15}l_{54} - u_{16}l_{64}}{l_{44}}$$

$$u_{15} = a_{63}$$

$$u_{15} = a_{63}$$

$$u_{15} = a_{63}$$

$$u_{16} = a_{64}$$

$$l_{15} = a_{62}$$

$$l_{15} = a_{62}$$

$$l_{12} = a_{42} - u_{23}l_{32} - u_{24}l_{42} - u_{25}l_{52} - u_{26}l_{62}$$

$$u_{12} = \frac{a_{12} - u_{13}l_{32} - u_{14}l_{42} - u_{15}l_{52} - u_{16}l_{62}}{l_{22}}$$

$$l_{61} = a_{61}$$

$$l_{61} = a_{61}$$

$$l_{61} = a_{61}$$

$$l_{11} = a_{61} - u_{15}l_{61}$$

$$l_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41} - u_{25}l_{51} - u_{26}l_{61}$$

$$l_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41} - u_{15}l_{51} - u_{16}l_{61}$$

$$l_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41} - u_{15}l_{51} - u_{16}l_{61}$$

### 4 Metodo Ul

### 4.1 Caso de matrices de $2 \times 2$

$$\begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} \\ 0 & u_{22} \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 \\ l_{21} & 1 \end{pmatrix}$$
 
$$\begin{pmatrix} u_{11} & u_{12} \\ l_{21} & u_{22} \end{pmatrix}$$

$$a_{22} = u_{22}$$
  $u_{22} = a_{22}$ 
 $a_{12} = u_{12}$   $u_{12} = a_{12}$ 
 $a_{21} = u_{22}l_{21}$   $l_{21} = \frac{a_{21}}{u_{22}}$ 
 $u_{11} = a_{11} - u_{12}l_{21}$ 
 $u_{11} = a_{11} - u_{12}l_{21}$ 

# 4.2 Caso de matrices de $3 \times 3$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} \\ 0 & u_{22} & u_{23} \\ 0 & 0 & u_{33} \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 \\ l_{21} & 1 & 0 \\ l_{31} & l_{32} & 1 \end{pmatrix}$$
 
$$\begin{pmatrix} u_{11} & u_{12} & u_{13} \\ l_{21} & u_{22} & u_{23} \\ l_{31} & l_{32} & u_{33} \end{pmatrix}$$

$$a_{33} = u_{33}$$

$$a_{23} = u_{23}$$

$$a_{13} = u_{13}$$

$$a_{32} = u_{33}l_{32}$$

$$a_{22} = u_{22} + u_{23}l_{32}$$

$$a_{12} = u_{12} + u_{13}l_{32}$$

$$a_{31} = u_{33}l_{31}$$

$$a_{21} = u_{22}l_{21} + u_{23}l_{31}$$

$$a_{11} = u_{11} + u_{12}l_{21} + u_{13}l_{31}$$

$$u_{12} = a_{12} - u_{13}l_{32}$$

$$u_{12} = a_{12} - u_{13}l_{32}$$

$$u_{13} = a_{31}l_{33}$$

$$u_{12} = a_{12} - u_{13}l_{32}$$

$$u_{13} = a_{31}l_{33}$$

$$u_{14} = a_{11} - u_{12}l_{21} - u_{13}l_{31}$$

$$u_{15} = a_{15}l_{15}l_{15}$$

$$u_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} \\ a_{21} & a_{22} & a_{23} & a_{24} \\ a_{31} & a_{32} & a_{33} & a_{34} \\ a_{41} & a_{42} & a_{43} & a_{44} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} \\ 0 & u_{22} & u_{23} & u_{24} \\ 0 & 0 & u_{33} & u_{34} \\ 0 & 0 & 0 & u_{44} \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 \\ l_{41} & l_{42} & l_{43} & 1 \end{pmatrix}$$
 
$$\begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} \\ l_{21} & u_{22} & u_{23} & u_{24} \\ l_{31} & l_{32} & u_{33} & u_{34} \\ l_{41} & l_{42} & l_{43} & u_{44} \end{pmatrix}$$

$$a_{23} = u_{23} + u_{24}l_{43}$$

$$a_{13} = u_{13} + u_{14}l_{43}$$

$$a_{34} = u_{34}$$

$$a_{24} = u_{24}$$

$$a_{14} = u_{14}$$

$$a_{43} = u_{44}l_{43}$$

$$a_{42} = u_{44}l_{42}$$

$$a_{32} = u_{33}l_{32} + u_{34}l_{42}$$

$$a_{22} = u_{22} + u_{23}l_{32} + u_{24}l_{42}$$

$$a_{43} = u_{44}l_{43}$$

$$a_{12} = u_{12} + u_{13}l_{32} + u_{14}l_{42}$$

$$a_{33} = u_{33} + u_{34}l_{43}$$

$$a_{41} = u_{44}l_{41}$$

$$a_{31} = u_{33}l_{31} + u_{34}l_{41}$$

$$a_{21} = u_{22}l_{21} + u_{23}l_{31} + u_{24}l_{41}$$

$$a_{11} = u_{11} + u_{12}l_{21} + u_{13}l_{31} + u_{14}l_{41}$$

$$u_{34} = a_{34}$$

$$u_{24} = a_{24}$$

$$u_{14} = a_{14}$$

$$l_{43} = \frac{a_{43}}{u_{44}}$$

$$u_{33} = a_{33} - u_{34}l_{43}$$

$$u_{23} = a_{23} - u_{24}l_{43}$$

$$u_{13} = a_{13} - u_{14}l_{43}$$

$$l_{42} = \frac{a_{42}}{u_{44}}$$

$$l_{32} = \frac{a_{32} - u_{34}l_{42}}{u_{33}}$$

$$u_{22} = a_{22} - u_{23}l_{32} - u_{24}l_{42}$$

$$u_{12} = a_{12} - u_{13}l_{32} - u_{14}l_{42}$$

$$l_{41} = \frac{a_{41}}{u_{44}}$$

$$l_{31} = \frac{a_{31} - u_{34}l_{41}}{u_{33}}$$

$$l_{21} = \frac{a_{21} - u_{23}l_{31} - u_{24}l_{41}}{u_{22}}$$

 $a_{33} = u_{33} + u_{34}l_{43} + u_{35}l_{53}$ 

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} \\ 0 & u_{22} & u_{23} & u_{24} & u_{25} \\ 0 & 0 & u_{33} & u_{34} & u_{35} \\ 0 & 0 & 0 & u_{44} & u_{45} \\ 0 & 0 & 0 & 0 & u_{55} \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & 1 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & 1 \end{pmatrix}$$

 $u_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41}$ 

$$a_{23} = u_{23} + u_{24}l_{43} + u_{25}l_{53}$$

$$a_{45} = u_{45}$$

$$a_{35} = u_{35}$$

$$a_{25} = u_{25}$$

$$a_{25} = u_{25}$$

$$a_{15} = u_{15}$$

$$a_{54} = u_{55}l_{54}$$

$$a_{44} = u_{44} + u_{45}l_{54}$$

$$a_{34} = u_{34} + u_{35}l_{54}$$

$$a_{24} = u_{24} + u_{25}l_{54}$$

$$a_{14} = u_{14} + u_{15}l_{54}$$

$$a_{53} = u_{55}l_{53}$$

$$a_{43} = u_{44}l_{43} + u_{45}l_{53}$$

$$a_{41} = u_{11} + u_{12}l_{21} + u_{13}l_{31} + u_{14}l_{41} + u_{15}l_{51}$$

$$a_{21} = u_{22}l_{21} + u_{23}l_{31} + u_{24}l_{41} + u_{25}l_{51}$$

$$a_{11} = u_{11} + u_{12}l_{21} + u_{13}l_{31} + u_{14}l_{41} + u_{15}l_{51}$$

$$u_{55} = a_{55}$$

$$u_{45} = a_{45}$$

$$u_{35} = a_{35}$$

$$u_{25} = a_{25}$$

$$u_{15} = a_{15}$$

$$l_{54} = \frac{a_{54}}{u_{55}}$$

$$u_{44} = a_{44} - u_{45}l_{54}$$

$$u_{34} = a_{34} - u_{35}l_{54}$$

$$u_{24} = a_{24} - u_{25}l_{54}$$

$$u_{14} = a_{14} - u_{15}l_{54}$$

$$l_{53} = \frac{a_{53}}{u_{55}}$$

$$l_{43} = \frac{a_{43} - u_{45}l_{53}}{u_{44}}$$

$$u_{33} = a_{33} - u_{34}l_{43} - u_{35}l_{53}$$

$$u_{23} = a_{23} - u_{24}l_{43} - u_{25}l_{53}$$

$$u_{13} = a_{13} - u_{14}l_{43} - u_{15}l_{53}$$

$$l_{52} = \frac{a_{52}}{u_{55}}$$

$$l_{42} = \frac{a_{42} - u_{45}l_{52}}{u_{44}}$$

$$l_{32} = \frac{a_{32} - u_{34}l_{42} - u_{35}l_{52}}{u_{33}}$$

$$u_{22} = a_{22} - u_{23}l_{32} - u_{24}l_{42} - u_{25}l_{52}$$

$$u_{12} = a_{12} - u_{13}l_{32} - u_{14}l_{42} - u_{15}l_{52}$$

$$l_{51} = \frac{a_{51}}{u_{55}}$$

$$l_{41} = \frac{a_{41} - u_{45}l_{51}}{u_{44}}$$

$$l_{31} = \frac{a_{31} - u_{34}l_{41} - u_{35}l_{51}}{u_{33}}$$

$$l_{21} = \frac{a_{21} - u_{23}l_{31} - u_{24}l_{41} - u_{25}l_{51}}{u_{22}}$$

$$u_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41} - u_{15}l_{51}$$

$$\begin{pmatrix} a_{11} & a_{12} & a_{13} & a_{14} & a_{15} & a_{16} \\ a_{21} & a_{22} & a_{23} & a_{24} & a_{25} & a_{26} \\ a_{31} & a_{32} & a_{33} & a_{34} & a_{35} & a_{36} \\ a_{41} & a_{42} & a_{43} & a_{44} & a_{45} & a_{46} \\ a_{51} & a_{52} & a_{53} & a_{54} & a_{55} & a_{56} \\ a_{61} & a_{62} & a_{63} & a_{64} & a_{65} & a_{66} \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ 0 & u_{22} & u_{23} & u_{24} & u_{25} & u_{26} \\ 0 & 0 & u_{33} & u_{34} & u_{35} & u_{36} \\ 0 & 0 & 0 & u_{44} & u_{45} & u_{46} \\ 0 & 0 & 0 & 0 & u_{55} & u_{56} \\ 0 & 0 & 0 & 0 & 0 & u_{66} \end{pmatrix} \cdot \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & 1 & 0 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & 1 & 0 \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & 1 \end{pmatrix}$$

$$\begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ l_{21} & u_{22} & u_{23} & u_{24} & u_{25} & u_{26} \\ l_{31} & l_{32} & u_{33} & u_{34} & u_{35} & u_{36} \\ l_{41} & l_{42} & l_{43} & u_{44} & u_{45} & u_{46} \\ l_{51} & l_{52} & l_{53} & l_{54} & u_{55} & u_{56} \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & u_{66} \end{pmatrix}$$

$$a_{24} = u_{24} + u_{25}l_{54} + u_{26}l_{64}$$

$$a_{66} = u_{66}$$

$$a_{56} = u_{56}$$

$$a_{63} = u_{66}l_{63}$$

$$a_{46} = u_{46}$$

$$a_{36} = u_{36}$$

$$a_{36} = u_{36}$$

$$a_{26} = u_{26}$$

$$a_{16} = u_{16}$$

$$a_{65} = u_{66}l_{65}$$

$$a_{45} = u_{45} + u_{46}l_{65}$$

$$a_{45} = u_{45} + u_{46}l_{65}$$

$$a_{35} = u_{35}l_{52} + u_{56}l_{62}$$

$$a_{35} = u_{35}l_{52} + u_{56}l_{62}$$

$$a_{35} = u_{35} + u_{36}l_{65}$$

$$a_{45} = u_{45} + u_{46}l_{65}$$

$$a_{25} = u_{25} + u_{26}l_{65}$$

$$a_{15} = u_{15} + u_{16}l_{65}$$

$$a_{26} = u_{26}l_{62}$$

$$a_{15} = u_{15} + u_{16}l_{65}$$

$$a_{26} = u_{26}l_{62}$$

$$a_{25} = u_{25} + u_{26}l_{65}$$

$$a_{26} = u_{26}l_{62}$$

$$a_{25} = u_{25} + u_{26}l_{65}$$

$$a_{26} = u_{26}l_{62}$$

$$a_{26} = u_{26}l_{62}$$

$$a_{27} = u_{27} + u_{23}l_{32} + u_{24}l_{42} + u_{25}l_{52} + u_{26}l_{62}$$

$$a_{29} = u_{22} + u_{23}l_{32} + u_{24}l_{42} + u_{25}l_{52} + u_{26}l_{62}$$

$$a_{21} = u_{12} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{21} = u_{12} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{24} = u_{24}l_{44} + u_{45}l_{54} + u_{46}l_{63}$$

$$a_{31} = u_{31}l_{31} + u_{41}l_{41} + u_{45}l_{52} + u_{46}l_{63}$$

$$a_{21} = u_{12} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{15} = u_{15}l_{15} + u_{16}l_{63}$$

$$a_{26} = u_{66}l_{61}$$

$$a_{26} = u_{66}l_{61}$$

$$a_{26} = u_{66}l_{61}$$

$$a_{26} = u_{66}l_{61}$$

$$a_{27} = u_{27} + u_{23}l_{32} + u_{24}l_{42} + u_{25}l_{52} + u_{26}l_{62}$$

$$a_{29} = u_{22} + u_{23}l_{32} + u_{24}l_{42} + u_{25}l_{52} + u_{26}l_{62}$$

$$a_{29} = u_{21} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{29} = u_{21} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{21} = u_{12} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{21} = u_{12} + u_{13}l_{32} + u_{14}l_{42} + u_{15}l_{52} + u_{16}l_{62}$$

$$a_{21} = u_{22} + u_{23}l_{23} + u_{24}l_{44} + u_{45}l_{54} + u_{46}l_{64}$$

$$a_{21} = u_{22} + u_{23}l_{23} + u_{24}l_{44} + u_{45}l_{54} + u_{46}l_{64}$$

$$a_{21} = u_{22} + u_{23}l_{23} + u_{24}l_{44} + u_{25}l$$

$$a_{31} = u_{33}l_{31} + u_{32}l_{21} + u_{32}l_{31} + u_{34}l_{41}$$

$$a_{21} = u_{22}l_{21} + u_{23}l_{31} + u_{24}l_{41} + u_{23}l_{51} + u_{24}l_{61}$$

$$u_{11} = u_{11} + u_{12}l_{22} + u_{13}l_{31} + u_{14}l_{41} + u_{13}l_{51} + u_{16}l_{61}$$

$$u_{15} = u_{15}$$

$$u_{25} = u_{25}$$

$$u_{25} = u_{25}$$

$$u_{25} = u_{25}$$

$$u_{25} = u_{35}$$

$$u_{25} = u_{35}$$

$$u_{35} = u_{35}l_{65}$$

$$u_{15} = u_{15}l_{44} + u_{45}l_{54} + u_{46}l_{65}$$

$$l_{64} = \frac{u_{66}}{u_{66}}$$

$$l_{54} = \frac{u_{64} + u_{45}l_{54} + u_{46}l_{65}}{u_{55}}$$

$$u_{44} = u_{44} + u_{45}l_{54} + u_{46}l_{64}$$

$$u_{24} = u_{44} + u_{45}l_{54} + u_{46}l_{64}$$

$$u_{44} = u_{44} + u_{45}l_{54} + u_{46}l_{64}$$

$$u_{44} = u_{44} - u_{45}l_{54} + u_{56}l_{65}$$

$$u_{55} = \frac{u_{55}u_{55}u_{55}}{u_{55}}$$

$$l_{43} = \frac{u_{45}u_{45}u_{55}u_{55}u_{55}u_{55}}{u_{44}}$$

$$u_{43} = u_{43}u_{45}v_{53}u_{44}u_{45}u_{54}u_{54}u_{54}u_{54}$$

$$u_{44} = u_{44}u_{45}l_{44}u_{45}u_{45}u_{46}u_{54}$$

$$u_{44} = u_{45}u_{44}u_{45}u_{45}u_{45}u_{54$$

 $u_{11} = a_{11} - u_{12}l_{21} - u_{13}l_{31} - u_{14}l_{41} - u_{15}l_{51} - u_{16}l_{61}$ 

# 5 Resolución de matrices triangulares L

### 5.1 Caso de matrices de $2 \times 2$

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} l_{11} & 0 \\ l_{21} & l_{22} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

$$y_1 = l_{11}x_1$$

$$y_2 = l_{21}x_1 + l_{22}x_2$$

$$x_2 = \frac{y_2 - l_{21}x_1}{l_{22}}$$

## 5.2 Caso de matrices de $3 \times 3$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 \\ l_{21} & l_{22} & 0 \\ l_{31} & l_{32} & l_{33} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$$

$$y_1 = l_{11}x_1 \qquad x_1 = \frac{y_1}{l_{11}}$$

$$y_2 = l_{21}x_1 + l_{22}x_2$$

$$y_3 = l_{31}x_1 + l_{32}x_2 + l_{33}x_3$$

$$x_2 = \frac{y_2 - l_{21}}{l_{22}}$$

$$x_2 = \frac{y_2 - l_{21}x_1}{l_{22}}$$
$$x_3 = \frac{y_3 - l_{31}x_1 - l_{32}x_2}{l_{33}}$$

# 5.3 Caso de matrices de $4 \times 4$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix}$$

$$y_{1} = l_{11}x_{1}$$

$$y_{2} = l_{21}x_{1} + l_{22}x_{2}$$

$$y_{3} = l_{31}x_{1} + l_{32}x_{2} + l_{33}x_{3}$$

$$y_{4} = l_{41}x_{1} + l_{42}x_{2} + l_{43}x_{3} + l_{44}x_{4}$$

$$x_{3} = \frac{y_{3} - l_{31}x_{1} - l_{32}x_{2}}{l_{33}}$$

$$x_{4} = \frac{y_{4} - l_{41}x_{1} - l_{42}x_{2} - l_{43}x_{3}}{l_{44}}$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ v_5 \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & l_{55} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{pmatrix}$$

$$y_{1} = l_{11}x_{1}$$

$$y_{2} = l_{21}x_{1} + l_{22}x_{2}$$

$$y_{3} = l_{31}x_{1} + l_{32}x_{2} + l_{33}x_{3}$$

$$y_{4} = l_{41}x_{1} + l_{42}x_{2} + l_{43}x_{3} + l_{44}x_{4}$$

$$y_{5} = l_{51}x_{1} + l_{52}x_{2} + l_{53}x_{3} + l_{54}x_{4} + l_{55}x_{5}$$

$$x_{4} = \frac{y_{4} - l_{41}x_{1} - l_{42}x_{2} - l_{43}x_{3}}{l_{44}}$$

$$x_{5} = \frac{y_{5} - l_{51}x_{1} - l_{52}x_{2} - l_{53}x_{3} - l_{54}x_{4}}{l_{55}}$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \\ y_6 \end{pmatrix} = \begin{pmatrix} l_{11} & 0 & 0 & 0 & 0 & 0 \\ l_{21} & l_{22} & 0 & 0 & 0 & 0 \\ l_{31} & l_{32} & l_{33} & 0 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & l_{44} & 0 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & l_{55} & 0 \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & l_{66} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{pmatrix}$$

$$y_1 = l_{11}x_1$$

$$y_2 = l_{21}x_1 + l_{22}x_2$$

$$y_3 = l_{31}x_1 + l_{32}x_2 + l_{33}x_3$$

$$y_4 = l_{41}x_1 + l_{42}x_2 + l_{43}x_3 + l_{44}x_4$$

$$y_5 = l_{51}x_1 + l_{52}x_2 + l_{53}x_3 + l_{54}x_4 + l_{55}x_5$$

$$y_6 = l_{61}x_1 + l_{62}x_2 + l_{63}x_3 + l_{64}x_4 + l_{65}x_5 + l_{66}x_6$$

$$x_{1} = \frac{y_{1}}{l_{11}}$$

$$x_{2} = \frac{y_{2} - l_{21}x_{1}}{l_{22}}$$

$$x_{3} = \frac{y_{3} - l_{31}x_{1} - l_{32}x_{2}}{l_{33}}$$

$$x_{4} = \frac{y_{4} - l_{41}x_{1} - l_{42}x_{2} - l_{43}x_{3}}{l_{44}}$$

$$x_{5} = \frac{y_{5} - l_{51}x_{1} - l_{52}x_{2} - l_{53}x_{3} - l_{54}x_{4}}{l_{55}}$$

$$x_{6} = \frac{y_{6} - l_{61}x_{1} - l_{62}x_{2} - l_{63}x_{3} - l_{64}x_{4} - l_{65}x_{5}}{l_{66}}$$

# 6 Resolución de matrices triangulares l

### 6.1 Caso de matrices de $2 \times 2$

$$\left(\begin{array}{c} y_1 \\ y_2 \end{array}\right) = \left(\begin{array}{cc} 1 & 0 \\ l_{21} & 1 \end{array}\right) \cdot \left(\begin{array}{c} x_1 \\ x_2 \end{array}\right)$$

$$y_1 = x_1 y_2 = l_{21}x_1 + x_2$$

$$x_1 = y_1$$

$$x_2 = y_2 - l_{21}x_1$$

### 6.2 Caso de matrices de $3 \times 3$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ l_{21} & 1 & 0 \\ l_{31} & l_{32} & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$$

$$y_1 = x_1$$

$$y_2 = l_{21}x_1 + x_2$$

$$y_3 = l_{31}x_1 + l_{32}x_2 + x_3$$

$$x_1 = y_1$$

$$x_2 = y_2 - l_{21}x_1$$

$$x_3 = y_3 - l_{31}x_1 - l_{32}x_2$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 \\ l_{41} & l_{42} & l_{43} & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix}$$

$$y_1 = x_1$$

$$y_2 = l_{21}x_1 + x_2$$

$$y_3 = l_{31}x_1 + l_{32}x_2 + x_3$$

$$y_4 = l_{41}x_1 + l_{42}x_2 + l_{43}x_3 + x_4$$

$$x_1 = y_1$$

$$x_2 = y_2 - l_{21}x_1$$

$$x_3 = y_3 - l_{31}x_1 - l_{32}x_2$$

$$x_4 = y_4 - l_{41}x_1 - l_{42}x_2 - l_{43}x_3$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ v_5 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & 1 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{pmatrix}$$

$$y_1 = x_1$$

$$y_2 = l_{21}x_1 + x_2$$

$$y_3 = l_{31}x_1 + l_{32}x_2 + x_3$$

$$y_4 = l_{41}x_1 + l_{42}x_2 + l_{43}x_3 + x_4$$

$$y_5 = l_{51}x_1 + l_{52}x_2 + l_{53}x_3 + l_{54}x_4 + x_5$$

$$x_1 = y_1$$

$$x_2 = y_2 - l_{21}x_1$$

$$x_3 = y_3 - l_{31}x_1 - l_{32}x_2$$

$$x_4 = y_4 - l_{41}x_1 - l_{42}x_2 - l_{43}x_3$$

$$x_5 = y_5 - l_{51}x_1 - l_{52}x_2 - l_{53}x_3 - l_{54}x_4$$

### 6.5 Caso de matrices de $6 \times 6$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \\ y_6 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 \\ l_{21} & 1 & 0 & 0 & 0 & 0 \\ l_{31} & l_{32} & 1 & 0 & 0 & 0 \\ l_{41} & l_{42} & l_{43} & 1 & 0 & 0 \\ l_{51} & l_{52} & l_{53} & l_{54} & 1 & 0 \\ l_{61} & l_{62} & l_{63} & l_{64} & l_{65} & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{pmatrix}$$

$$y_1 = x_1$$

$$y_2 = l_{21}x_1 + x_2$$

$$y_3 = l_{31}x_1 + l_{32}x_2 + x_3$$

$$y_4 = l_{41}x_1 + l_{42}x_2 + l_{43}x_3 + x_4$$

$$y_5 = l_{51}x_1 + l_{52}x_2 + l_{53}x_3 + l_{54}x_4 + x_5$$

$$y_6 = l_{61}x_1 + l_{62}x_2 + l_{63}x_3 + l_{64}x_4 + l_{65}x_5 + x_6$$

$$x_1 = y_1$$

$$x_2 = y_2 - l_{21}x_1$$

$$x_3 = y_3 - l_{31}x_1 - l_{32}x_2$$

$$x_4 = y_4 - l_{41}x_1 - l_{42}x_2 - l_{43}x_3$$

$$x_5 = y_5 - l_{51}x_1 - l_{52}x_2 - l_{53}x_3 - l_{54}x_4$$

$$x_6 = y_6 - l_{61}x_1 - l_{62}x_2 - l_{63}x_3 - l_{64}x_4 - l_{65}x_5$$

# 7 Resolución de matrices triangulares U

#### 7.1 Caso de matrices de $2 \times 2$

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} \\ 0 & u_{22} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

$$y_2 = u_{22}x_2$$

$$y_1 = u_{11}x_1 + u_{12}x_2$$

$$x_1 = \frac{y_1 - u_{12}x_2}{u_{11}}$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} \\ 0 & u_{22} & u_{23} \\ 0 & 0 & u_{33} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$$

$$y_3 = u_{33}x_3$$

$$y_2 = u_{22}x_2 + u_{23}x_3$$

$$y_1 = u_{11}x_1 + u_{12}x_2 + u_{13}x_3$$

$$x_2 = \frac{y_2 - u_{23}x_3}{u_{22}}$$

$$x_1 = \frac{y_1 - u_{12}x_2 - u_{13}x_3}{u_{11}}$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ v_4 \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} \\ 0 & u_{22} & u_{23} & u_{24} \\ 0 & 0 & u_{33} & u_{34} \\ 0 & 0 & 0 & u_{44} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix}$$

$$y_{4} = u_{44}x_{4}$$

$$y_{3} = u_{33}x_{3} + u_{34}x_{4}$$

$$y_{2} = u_{22}x_{2} + u_{23}x_{3} + u_{24}x_{4}$$

$$y_{1} = u_{11}x_{1} + u_{12}x_{2} + u_{13}x_{3} + u_{14}x_{4}$$

$$x_{2} = \frac{y_{2} - u_{23}x_{3} - u_{24}x_{4}}{u_{22}}$$

$$x_{1} = \frac{y_{1} - u_{12}x_{2} - u_{13}x_{3} - u_{14}x_{4}}{u_{11}}$$

### 7.4 Caso de matrices de $5 \times 5$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} \\ 0 & u_{22} & u_{23} & u_{24} & u_{25} \\ 0 & 0 & u_{33} & u_{34} & u_{35} \\ 0 & 0 & 0 & u_{44} & u_{45} \\ 0 & 0 & 0 & 0 & u_{55} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{pmatrix}$$

$$y_{5} = u_{55}x_{5}$$

$$y_{4} = u_{44}x_{4} + u_{45}x_{5}$$

$$y_{3} = u_{33}x_{3} + u_{34}x_{4} + u_{35}x_{5}$$

$$y_{2} = u_{22}x_{2} + u_{23}x_{3} + u_{24}x_{4} + u_{25}x_{5}$$

$$y_{1} = u_{11}x_{1} + u_{12}x_{2} + u_{13}x_{3} + u_{14}x_{4} + u_{15}x_{5}$$

$$x_{2} = \frac{y_{2} - u_{23}x_{3} - u_{24}x_{4} - u_{25}x_{5}}{u_{22}}$$

$$x_{1} = \frac{y_{1} - u_{12}x_{2} - u_{13}x_{3} - u_{14}x_{4} - u_{15}x_{5}}{u_{11}}$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \\ y_6 \end{pmatrix} = \begin{pmatrix} u_{11} & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ 0 & u_{22} & u_{23} & u_{24} & u_{25} & u_{26} \\ 0 & 0 & u_{33} & u_{34} & u_{35} & u_{36} \\ 0 & 0 & 0 & u_{44} & u_{45} & u_{46} \\ 0 & 0 & 0 & 0 & u_{55} & u_{56} \\ 0 & 0 & 0 & 0 & 0 & u_{66} \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{pmatrix}$$

$$y_6 = u_{66}x_6$$

$$y_5 = u_{55}x_5 + u_{56}x_6$$

$$y_4 = u_{44}x_4 + u_{45}x_5 + u_{46}x_6$$

$$y_3 = u_{33}x_3 + u_{34}x_4 + u_{35}x_5 + u_{36}x_6$$

$$y_2 = u_{22}x_2 + u_{23}x_3 + u_{24}x_4 + u_{25}x_5 + u_{26}x_6$$

$$y_1 = u_{11}x_1 + u_{12}x_2 + u_{13}x_3 + u_{14}x_4 + u_{15}x_5 + u_{16}x_6$$

$$x_{6} = \frac{y_{6}}{u_{66}}$$

$$x_{5} = \frac{y_{5} - u_{56}x_{6}}{u_{55}}$$

$$x_{4} = \frac{y_{4} - u_{45}x_{5} - u_{46}x_{6}}{u_{44}}$$

$$x_{3} = \frac{y_{3} - u_{34}x_{4} - u_{35}x_{5} - u_{36}x_{6}}{u_{33}}$$

$$x_{2} = \frac{y_{2} - u_{23}x_{3} - u_{24}x_{4} - u_{25}x_{5} - u_{26}x_{6}}{u_{22}}$$

$$x_{1} = \frac{y_{1} - u_{12}x_{2} - u_{13}x_{3} - u_{14}x_{4} - u_{15}x_{5} - u_{16}x_{6}}{u_{11}}$$

# 8 Resolución de matrices triangulares u

### 8.1 Caso de matrices de $2 \times 2$

$$\begin{pmatrix} y_1 \\ y_2 \end{pmatrix} = \begin{pmatrix} 1 & u_{12} \\ 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \end{pmatrix}$$

$$y_2 = x_2$$

$$y_1 = x_1 + u_{12}x_2$$

$$x_1 = y_1 - u_{12}x_2$$

### 8.2 Caso de matrices de $3 \times 3$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} \\ 0 & 1 & u_{23} \\ 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix}$$

$$v_3 = x_3$$

$$y_3 = x_3$$

$$y_2 = x_2 + u_{23}x_3$$

$$y_1 = x_1 + u_{12}x_2 + u_{13}x_3$$

$$x_1 = y_1 - u_{12}x_2 - u_{13}x_3$$

### 8.3 Caso de matrices de $4 \times 4$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} \\ 0 & 1 & u_{23} & u_{24} \\ 0 & 0 & 1 & u_{34} \\ 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{pmatrix}$$

$$y_4 = x_4$$

$$y_3 = x_3 + u_{34}x_4$$

$$y_2 = x_2 + u_{23}x_3 + u_{24}x_4$$

$$y_1 = x_1 + u_{12}x_2 + u_{13}x_3 + u_{14}x_4$$

$$x_4 = y_4$$

$$x_3 = y_3 - u_{34}x_4$$

$$x_2 = y_2 - u_{23}x_3 - u_{24}x_4$$

$$x_1 = y_1 - u_{12}x_2 - u_{13}x_3 - u_{14}x_4$$

### 8.4 Caso de matrices de $5 \times 5$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} & u_{15} \\ 0 & 1 & u_{23} & u_{24} & u_{25} \\ 0 & 0 & 1 & u_{34} & u_{35} \\ 0 & 0 & 0 & 1 & u_{45} \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \end{pmatrix}$$

$$y_5 = x_5$$

$$y_4 = x_4 + u_{45}x_5$$

$$y_3 = x_3 + u_{34}x_4 + u_{35}x_5$$

$$y_2 = x_2 + u_{23}x_3 + u_{24}x_4 + u_{25}x_5$$

$$y_1 = x_1 + u_{12}x_2 + u_{13}x_3 + u_{14}x_4 + u_{15}x_5$$

$$x_1 = y_1 - u_{12}x_2 - u_{13}x_3 - u_{14}x_4 - u_{15}x_5$$

$$x_1 = y_1 - u_{12}x_2 - u_{13}x_3 - u_{14}x_4 - u_{15}x_5$$

$$\begin{pmatrix} y_1 \\ y_2 \\ y_3 \\ y_4 \\ y_5 \\ y_6 \end{pmatrix} = \begin{pmatrix} 1 & u_{12} & u_{13} & u_{14} & u_{15} & u_{16} \\ 0 & 1 & u_{23} & u_{24} & u_{25} & u_{26} \\ 0 & 0 & 1 & u_{34} & u_{35} & u_{36} \\ 0 & 0 & 0 & 1 & u_{45} & u_{46} \\ 0 & 0 & 0 & 0 & 1 & u_{56} \\ 0 & 0 & 0 & 0 & 0 & 1 \end{pmatrix} \cdot \begin{pmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \\ x_5 \\ x_6 \end{pmatrix}$$

$$y_6 = x_6$$

$$y_5 = x_5 + u_{56}x_6$$

$$y_4 = x_4 + u_{45}x_5 + u_{46}x_6$$

$$y_3 = x_3 + u_{34}x_4 + u_{35}x_5 + u_{36}x_6$$

$$y_2 = x_2 + u_{23}x_3 + u_{24}x_4 + u_{25}x_5 + u_{26}x_6$$

$$y_1 = x_1 + u_{12}x_2 + u_{13}x_3 + u_{14}x_4 + u_{15}x_5 + u_{16}x_6$$

$$x_6 = y_6$$

$$x_5 = y_5 - u_{56}x_6$$

$$x_4 = y_4 - u_{45}x_5 - u_{46}x_6$$

$$x_3 = y_3 - u_{34}x_4 - u_{35}x_5 - u_{36}x_6$$

$$x_2 = y_2 - u_{23}x_3 - u_{24}x_4 - u_{25}x_5 - u_{26}x_6$$

$$x_1 = y_1 - u_{12}x_2 - u_{13}x_3 - u_{14}x_4 - u_{15}x_5 - u_{16}x_6$$