biomvRCNS: Copy Number study and Segmentation for multivariate biological data.

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Abstract

With high throughput experiments like tiling array and NGS, researchers are looking for continuous homogeneous segments or signal peaks, which would represent chromatin states, methylation ratio, transcripts or genome regions of deletion and amplification. While in a normal experimental set-up, these profiles would be generated for multiple samples or conditions with replicates. In the package biomvRCNS, a Hidden Semi Markov Model and one homogeneous segmentation model are implemented and tailored to handle multiple genomic profiles, with the aim of assisting in transcripts detection using high throughput technology like RNA-seq or tiling array, and copy number analysis using aCGH or targeted sequencing.

1 Introduction

To begin with biomvRCNS, load the package and read the manual page.

> library(biomvRCNS)

In the package, 3 main functions are provided for the batch processing of multiple chromosome regions across samples: biomvRhsmm, a hidden semi Markov model (HSMM); biomvRseg, a maximum likelihood based homogeneous segmentation model; and a third biomvRmgmr, custom batch function using max-gap-min-run algorithm. In the following sections we will illustrate their functionalities using example data. Currently the package does not deal with data correction, so input should be normalized by reference or paired sample and corrected for factor of interest before passing down.

2 Example of array CGH data set of Coriell cell lines

Extracted from packge *DNACopy*, the coriel1 data contains two aCGH studies (GM05296 and GM13330) of Corriel cell lines taken from Snijders et~al. [2001]. In particular, with 2271 mapped features in total across 22 autosomes and chromosome X.

All three main functions accept common data matrix plus positional information as input or a *GRanges* object with data matrix stored in the meta columns. To get started, we first build a *GRanges* object from *data.frame*.

```
> data('coriell', package='biomvRCNS')
```

> head(coriell, n=3)

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```
Clone Chromosome Position Coriell.05296 Coriell.13330
1 GS1-232B23
                       1
                                        0.000359
                                1
                                                       0.207470
2 RP11-82d16
                       1
                               469
                                        0.008824
                                                       0.063076
3 RP11-62m23
                       1
                                       -0.000890
                                                       0.123881
                              2242
> xgr<-GRanges(seqnames=paste('chr', coriell[,2], sep=''),
          IRanges(start=coriell[,3], width=1, names=coriell[,1]))
> values(xgr)<-DataFrame(coriell[,4:5], row.names=NULL)</pre>
> xgr<-xgr[order(xgr)]</pre>
> head(xgr, n=3)
GRanges with 3 ranges and 2 metadata columns:
              seqnames
                             ranges strand | Coriell.05296
                 <Rle>
                           <IRanges>
                                      <Rle> |
                                                   <numeric>
  GS1-232B23
                  chr1 [
                                                    0.000359
                           1,
                                  1]
                                          * |
  RP11-82d16
                               469]
                  chr1 [ 469,
                                            - 1
                                                    0.008824
                  chr1 [2242, 2242]
                                                    -0.00089
  RP11-62m23
             Coriell.13330
                  <numeric>
  GS1-232B23
                    0.20747
  RP11-82d16
                   0.063076
  RP11-62m23
                   0.123881
  seqlengths:
    chr1 chr10 chr11 chr12 chr13 ...
                                        chr5
                                               chr6
                                                     chr7
                                                            chr8
                                                                  chr9
      NΑ
            NA
                   NΑ
                         NA
                                NA ...
                                          NΑ
                                                 NA
                                                       NΑ
                                                              NΑ
                                                                    NΑ
```

Please be sure that the data is sorted with respect to their positions before feeding to the models.

2.1 Genomic segmentation with Hidden-semi Markov model

First we use the hidden-semi Markov model with the batch function biomvRhsmm, which will sequentially process each chromosome identified by the seqnames (using dummy name when no GRanges supplied in x or xRange), thus for non-continuous regions on the same chromosome user should give different seqnames to each part of the data. Within this package, there is one argument grp, for all main batch functions, which is used to assign data columns to groups according to the experimental design, say technical replicates or biological replicates. Sample columns within the same group could be treated simultaneously in the modelling process as well as iteratively. ¹ In this example, the two profiles are considered independent and not similar, thus been given different values in the grp vector. Additionally there is a built-in automatic grouping method, given a valid clustering method cluster.m and grp set to NULL. By default, all data columns are assumed to be from the same group.

```
> rhsmm<-biomvRhsmm(x=xgr, maxbp=4E4, J=3, soj.type='gamma',
+ emis.type='norm', grp=c(1,2))

> show(rhsmm)

Object is of class: 'biomvRCNS'
List of parameters used in the model:
J, maxk, maxbp, maxgap, soj.type, emis.type, q.alpha, r.var,
```

 $^{^{1} \}text{Simultaneous treatment within group is currently available for } \textit{emis.type} \text{ equals 'mvnorm' or 'mvt' in } \textbf{biomvRhsmm}, \textit{poolGrp} = TRUE \text{ in biomvRmgmr} \text{ and } \textit{twoStep} = FALSE \text{ in biomvRseg}.$

iterative, cMethod, maxit, tol, group, cluster.m, avg.m, trim, na.rm

The segmented ranges:

GRanges with 197 ranges and 3 metadata columns:

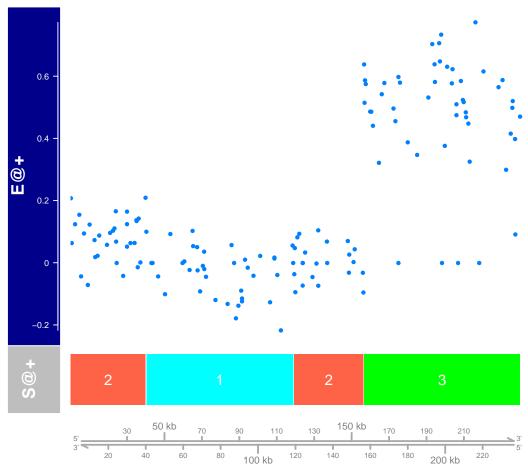
| O | segnames | O | ranges | strand | 1 | SAM | PLE | |
|-------------|--------------|---------------------------------------------------------------------------------|----------|-------------|--------------------------------------------------------|--------|------|------|
| | <rle></rle> | < | IRanges> | <rle></rle> | <c< td=""><td>haract</td><td>er></td><td></td></c<> | haract | er> | |
| [1] | chr1 | _ | _ | * | Cori | ell.05 | 296 | |
| [2] | chr1 | [40327, | | * | | ell.05 | | |
| [3] | | [91001, | | * | | ell.05 | 296 | |
| [4] | | [147954, | | * | Cori | ell.05 | 296 | |
| [5] | | [203907, | | * | • | ell.05 | | |
| [6] | | [35106, | | * | - | ell.05 | | |
| [7] | | [132171, | | * | | ell.05 | | |
| [8] | | [194308, | | * | | ell.05 | | |
| [9] | | [87215, | | * | | ell.05 | | |
| | | | | | | | | |
| [189] | chr9 | [34523, | _ | * | Cori | ell.05 | 296 | |
| [190] | chr9 | [82001, | | * | | ell.05 | | |
| [191] | chr9 | | 6113] | * | | ell.13 | | |
| [192] | chr9 | [15348, | | * | | ell.13 | | |
| [193] | chr9 | | 75244] | * | | ell.13 | | |
| [194] | chr9 | | 115001] | * | | ell.13 | | |
| [195] | chr9 | [8639, | | * | | ell.13 | | |
| [196] | chr9 | [24326, | | * | | ell.13 | | |
| [197] | chr9 | [75733, | | * | | ell.13 | | |
| [| | ATE | AVG | | , 0011 | | | |
| | | er> <nume< td=""><td></td><td></td><td></td><td></td><td></td><td></td></nume<> | | | | | | |
| [1] | | 2 0.004 | | | | | | |
| [2] | | 2 0.012 | | | | | | |
| [3] | | 2 0.006 | | | | | | |
| [4] | | 2 -0.00 | | | | | | |
| [5] | | 2 -0.002 | | | | | | |
| [6] | | 3 0.132 | | | | | | |
| [7] | 3 0.1421530 | | | | | | | |
| [8] | 3 0.1094320 | | | | | | | |
| [9] | 1 -0.1010400 | | | | | | | |
| | | | | | | | | |
| [189] | | | 22070 | | | | | |
| [190] | | 3 0.072 | 26115 | | | | | |
| [191] | | 2 -0.018 | 32800 | | | | | |
| [192] | | | 00075 | | | | | |
| [193] | | 2 -0.028 | 32400 | | | | | |
| [194] | | 2 -0.010 | | | | | | |
| [195] | | 1 -0.190 | | | | | | |
| [196] | | 1 -0.166 | | | | | | |
| [197] | | 3 0.093 | 10200 | | | | | |
| | | | | | | | | |
| seqlengths: | | | | | | | | |
| chr | 1 chr10 ch | nr11 chr12 | chr13 | chr5 | chr6 | chr7 | chr8 | chr9 |
| NA | A NA | NA NA | A NA | NA | NA | NA | NA | NA |
| | | | | | | | | |

In the above run, we limit the model complexity by setting the maxbp to 4E4, which will restrict the maximum sojourn time to maxbp. J is the number of states in the HSMM model, this argument can be given explicitly or estimated from prior information provided in xAnno. Argument soj.type defines the type of sojourn distribution; with Gamma distributed sojourn, the neighbouring position will tend to have the same state, and transit to other states if far apart. In this way the sojourn distribution fully incorporate the positional information into the proba-

bilistic framework. Argument emis.type controls the distribution of emission probability, in this case the log2 ratio of aCGH data is considered to follow Normal distribution. The function will then call C codes and estimate the most likely state sequence, with either cMethod='F-B' or cMethod='Viterbi'. The F-B method uses a forward-backward algorithm described in Guédon [2003], which gives a smooth state sequences, whereas the Viterbi algorithm with cMethod='Viterbi' will use the states profile estimated by the forward-backward algorithm and rebuild the most likely state sequence. The function returns an object of class biomvRCNS, in which the res slot is a GRanges object contain the summary of each estimated segments. There are three meta columns: column SAMPLE gives the column name of which sample this segment belongs to; column STATE, the estimated state for each segments, the lower state number represents state with lower mean value, thus in this example, a state of 1 could represent region of deletion and 3 for region of duplication, whereas state 2 could be considered copy neutral; column AVG, gives the segment average value.

A plot method has been implemented for biomvRCNS object using package Gviz, by default the plot method tries to output graphics to multiple EPS/PDF files for each chromosome region and sample. Here we set tofile=FALSE to output graphics to the current device, and only show resulting graphics for chromosome 1 from sample Coriell.13330.





2.2 Using other methods provided in the package

In this section, we use the other two batch functions to process the coriell data. First we use biomvRseg, in which a similar segmentation method like in the package tillingArray Huber et~al., 2006 is implemented and

extended to handle Poison and Negative binomial distributed data. The function shares several argument with biomvRhsmm, like maxbp and grp. The maxseg gives the maximum number of segment per chromosome region, while the optimal number of segment per chromosome region is determined internally by assessing the likelihood with optional penalty terms, by default penalty='BIC' is used. Another option is to use modified Bayes information criterion penalty='mBIC' Zhang and Siegmund, 2007, as in the CBS algorithm used in DNAcopy. The function proceed in the following manner: assuming within each group sample columns exhibit similar patterns, and thus be processed simultaneously in the first step. By maximizing the likelihood the optimal number of segments is selected for each group. And in a second step if twoStep=TRUE or merging is necessary, the candidate segments produced in the first step are merged with respect to each sample, thus forcing sample columns in the same group to have a more unified segmentation result yet keeping it possible to have sample specific pattern.

```
> rseg<-biomvRseg(x=xgr, maxbp=4E4, maxseg=10, family='norm', grp=c(1,2))</pre>
> head(rseg@res)
GRanges with 6 ranges and 3 metadata columns:
      seqnames
                           ranges strand |
                                                    SAMPLE
                                                                   AVG
          <Rle>
                        <IRanges>
                                   <Rle>
                                               <character>
                                                             <numeric>
  [1]
                           35001]
          chr1 [
                                            Coriell.05296
                                                             0.0045915
  [2]
          chr1 [ 35106,
                           36207]
                                            Coriell.05296
                                                             0.1335200
  [3]
          chr1 [ 37117,
                           85833]
                                        * |
                                            Coriell.05296
                                                             0.0129660
          chr1 [ 87215,
  [4]
                           89493]
                                          | Coriell.05296 -0.1010400
  [5]
          chr1 [ 91001, 132148]
                                         | Coriell.05296
                                                             0.0066565
          chr1 [132171, 136942]
  [6]
                                            Coriell.05296
                                                             0.1421530
             STATE
      <character>
  [1]
               LOW
  [2]
             HIGH
  [3]
              HIGH
  [4]
               LOW
  [5]
               LOW
  [6]
              HIGH
  seqlengths:
    chr1 chr10 chr11 chr12 chr13 ...
                                         chr5
                                                chr6
                                                             chr8
                                                                   chr9
                                                      chr7
      NA
             NA
                   NA
                          NA
                                NA ...
                                           NA
                                                  NA
                                                        NA
                                                               NA
                                                                     NA
```

After the example run, the function returns a biomvRCNS object, containing similar information as the previous biomvRhsmm run, except that the STATE column now only have a binary state value of either "HIGH" or "LOW", which is simply graded as 'HIGH' if the segment mean is higher than the grand mean of the whole region, and 'LOW' otherwise.

It is also possible to use the simple max-gap-min-run algorithm to segment aCGH profiles, by calling biomvRmgmr. But due to the binary nature of the algorithm, one have to run twice in order to get both extremely high and low segments, then combine the resulting *GRanges* manually.

```
> rmgmrh<-biomvRmgmr(xgr, q=0.9, high=T, maxgap=1000, minrun=2500, grp=c(1,2))
> rmgmrl<-biomvRmgmr(xgr, q=0.1, high=F, maxgap=1000, minrun=2500, grp=c(1,2))
> res<-c(rmgmrh@res, rmgmrl@res)</pre>
```

3 Example of RNA-seq data from ENCODE

The data contains gene expressions and transcript annotations in the region of the human TP53 gene (chr17:7,560,001-7,610,000 from the Human February 2009 (GRCh37/hg19) genome assembly), which is part of the long RNA-seq

data generated by ENCODE/Cold Spring Harbor Lab, containing 2 cell types (GM12878 and K562) with 2 replicates each. The libraries were sequenced on the Illumina GAIIx platform as paired-ends for 76 or 101 cycles for each read. The average depth of sequencing was ~200 million reads (100 million paired-ends). The data were mapped against hg19 using Spliced Transcript Alignment and Reconstruction (STAR).

To generate local read counts, alignment files were pulled from UCSC (http://hgdownload.cse.ucsc.edu/goldenPath/hg19/encodeDCC/wgEncodeCshlLongRnaSeq/) using package Rsamtools. And subsequently reads were counted in each non-overlapping unit sized window for the region (chr17:7,560,001-7,610,000). In the pre-compiled data encodeTP53, a window size of 25bp was used with the chunk of code below.

The pre-compiled data encodeTP53 also includes the regional annotation of TP53 RNAs isoforms, gmgr, which were derived from the ENCODE Gene Annotations (GENCODE), http://hgdownload.cse.ucsc.edu/goldenPath/hg19/encodeDCC/wgEncodeGencodeV4/wgEncodeGencodeManualV4.gtf.gz), and subset to only isoforms of TP53 gene. The annotation object gmgr could be rebuilt with the following lines using the included file under extdata.

```
> af<-system.file("extdata", "gmodTP53.csv", package = "biomvRCNS")
> gtfsub<-read.table(af, fill=T, stringsAsFactors=F)
> idx<-gtfsub[,3]=='CDS' | gtfsub[,3]=='UTR'
> gmgr<-GRanges("chr17", IRanges(start=gtfsub[idx, 4], end=gtfsub[idx, 5],
+ names=gtfsub[idx, 13]), strand='-', TYPE=gtfsub[idx, 3])</pre>
```

3.1 Transcript detection with Hidden-semi Markov model

We first load the encodeTP53 data, poll the read counts for each cell type and add 1 to the base count to increase stability.

For count data from sequencing, the emis.type could be set to either 'pois' or 'nbinom', though 'pois' is preferred for sharp boundary detection. For the sojourn settings, instead of using the uninformative flat prior, we here use estimates from other data source as a prior. We load the TxDb.Hsapiens.UCSC.hg19.knownGene known gene database, and pass the TranscriptDb object to xAnno. Then internally sojourn parameters and state number J will be estimated from xAnno by calling function sojournAnno. When given a TranscriptDb object to xAnno, state number would be set to 3 and each represents 'intergenic', 'intron', 'exon'.

```
> library(TxDb.Hsapiens.UCSC.hg19.knownGene)
> txdb<-TxDb.Hsapiens.UCSC.hg19.knownGene
> rhsmm<-biomvRhsmm(x=cgr, xAnno=txdb, maxbp=1E3, soj.type='gamma',
+ emis.type='pois', cMethod='F-B', q.alpha=0.01)</pre>
```

As in the ENCODE guide Consortium, 2011, the study identified the p53 isoform observed in K562 cells has a longer 3'UTR region than the isoform seen in the GM12878 cell line. So here we plot our model estimates and consider the third state, namely 'exon', to represent detected transcripts. And the HSMM model clearly picked up the extra transcripts of the K562 cell line at the 3'UTR region.

> rhsmm@res[mcols(rhsmm@res)[, 'STATE']=='exon']

GRanges with 51 ranges and 3 metadata columns:

[49]

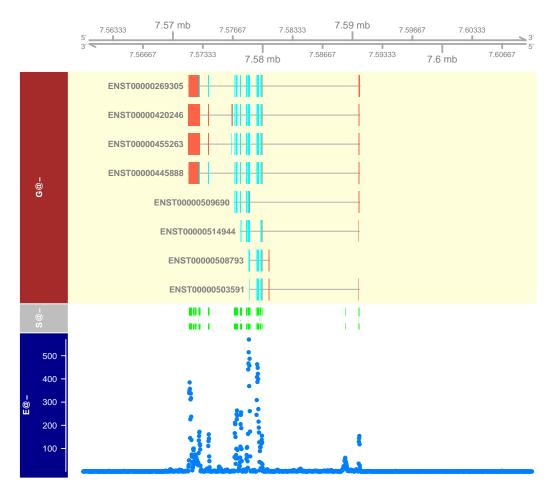
[50] [51] 6.0 9.0

14.5

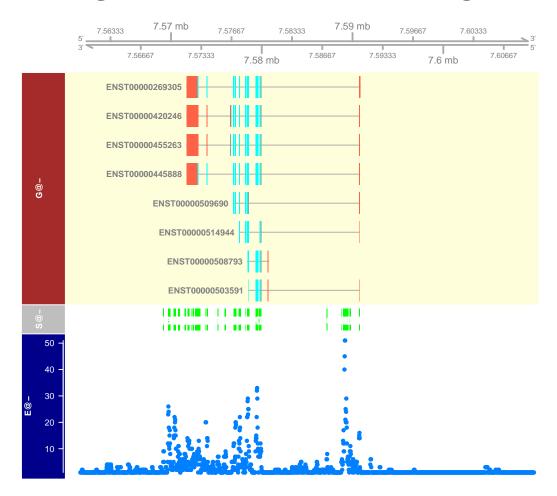
| <u> </u> | 0 W I OII O I | 1 am 600 am | ia o modaa | 404 00± | ****** | • | |
|----------|---------------------|-------------|---------------------|-------------|--------|-------------------------|-------------------------|
| | seqnames | | ranges | strand | - 1 | SAMPLE | STATE |
| | <rle></rle> | | <iranges></iranges> | <rle></rle> | - 1 | <character></character> | <character></character> |
| [1] | chr17 | [7571801, | 7572125] | - | - 1 | Gm12878 | exon |
| [2] | chr17 | [7572251, | 7572350] | - | - 1 | Gm12878 | exon |
| [3] | chr17 | [7572426, | 7572550] | - | - 1 | Gm12878 | exon |
| [4] | chr17 | [7572601, | 7572625] | - | - 1 | Gm12878 | exon |
| [5] | chr17 | [7572851, | 7573050] | - | - 1 | Gm12878 | exon |
| [6] | chr17 | [7573926, | 7574050] | - | - 1 | Gm12878 | exon |
| [7] | chr17 | [7576851, | 7576975] | - | - 1 | Gm12878 | exon |
| [8] | chr17 | [7577001, | 7577225] | - | - 1 | Gm12878 | exon |
| [9] | chr17 | [7577476, | 7577650] | - | - 1 | Gm12878 | exon |
| | | | | | | • • • | |
| [43] | | | 7579625] | - | I | | exon |
| [44] | | | 7579950] | - | I | K562 | exon |
| [45] | chr17 | [7587126, | 7587175] | - | I | K562 | exon |
| [46] | | | 7587225] | - | I | K562 | exon |
| [47] | | | 7588850] | - | I | K562 | exon |
| [48] | | - | 7589400] | - | I | K562 | exon |
| [49] | | | 7589525] | - | I | K562 | exon |
| [50] | | | 7589825] | - | I | K562 | exon |
| [51] | | | 7590800] | - | I | K562 | exon |
| | AVC | Ĭ | | | | | |
| | <numeric></numeric> | | | | | | |
| [1] | 312 | | | | | | |
| [2] | 96 | | | | | | |
| [3] | 61 | | | | | | |
| [4] | 60 | | | | | | |
| [5] | 127 | | | | | | |
| [6] | 132 | | | | | | |
| [7] | 166 | | | | | | |
| [8] | 99 | | | | | | |
| [9] | 188 | 3 | | | | | |
| | | | | | | | |
| [43] | 14.0 | | | | | | |
| [44] | 9.0 | | | | | | |
| [45] | 6.0 | | | | | | |
| [46] | 8.0 | | | | | | |
| [47] | 6.0 | | | | | | |
| [48] | 20.0 |) | | | | | |

seqlengths: chr17

33@chr17.7560000-7610000@Gm128



TP53@chr17.7560000-7610000@K562



Now we can locate those novel detected fragments in K562 cell line comparing to the annotation and those detected in Gm12878 cell line. One can then follow up those findings either by gene structure prediction using local nucleotides composition or by experimental validation.

- > nK2gm<-findOverlaps(rhsmm@res[k], gmgr)@queryHits</pre>
- > nK2G<-findOverlaps(rhsmm@res[k], rhsmm@res[g])@queryHits</pre>
- > rhsmm@res[k][setdiff(seq_len(sum(k)), unique(c(nK2G, nK2gm)))]

GRanges with 18 ranges and 3 metadata columns:

| | seqnames | | ranges | strand | SAMPLE | STATE |
|------|-------------|-----------|---------------------|---------------|-------------------------|-------------------------|
| | <rle></rle> | | <iranges></iranges> | <rle> </rle> | <character></character> | <character></character> |
| [1] | chr17 | [7569151, | 7569225] | - | K562 | exon |
| [2] | chr17 | [7569651, | 7569925] | - | K562 | exon |
| [3] | chr17 | [7570301, | 7570550] | - | K562 | exon |
| [4] | chr17 | [7570751, | 7570850] | - | K562 | exon |
| [5] | chr17 | [7570901, | 7571000] | - | K562 | exon |
| [6] | chr17 | [7571476, | 7571500] | - | K562 | exon |
| [7] | chr17 | [7571551, | 7571575] | - | K562 | exon |
| [8] | chr17 | [7571601, | 7571650] | - | K562 | exon |
| [9] | chr17 | [7573801, | 7573875] | - | K562 | exon |
| [10] | chr17 | [7575151, | 7575175] | - | K562 | exon |

```
[11]
        chr17 [7575201, 7575250]
                                                    K562
                                                                  exon
[12]
        chr17 [7575826, 7575875]
                                                    K562
                                                                  exon
[13]
        chr17 [7575976, 7576075]
                                                    K562
                                                                  exon
        chr17 [7587126, 7587175]
                                         - |
[14]
                                                    K562
                                                                  exon
[15]
        chr17 [7587201, 7587225]
                                         - |
                                                    K562
                                                                  exon
[16]
        chr17 [7588826, 7588850]
                                                    K562
                                                                  exon
[17]
        chr17 [7589426, 7589525]
                                         - 1
                                                    K562
                                                                  exon
        chr17 [7589676, 7589825]
[18]
                                                    K562
                                                                  exon
           AVG
     <numeric>
 [1]
           9.0
 [2]
          15.0
 [3]
          16.0
 [4]
          10.0
 [5]
           8.0
 [6]
           8.0
 [7]
           8.0
 [8]
           7.0
 [9]
          20.0
[10]
           7.0
[11]
           7.0
[12]
           7.0
           7.5
[13]
[14]
           6.0
[15]
           8.0
[16]
           6.0
[17]
           6.0
[18]
           9.0
seqlengths:
chr17
    NA
```

The other 2 batch functions could also be similarly applied here.

```
> rseg<-biomvRseg(x=cgr, maxbp=1E3, maxseg=20, family='pois')
> rmgmr<-biomvRmgmr(x=cgr, q=0.99, maxgap=50, minrun=100)</pre>
```

4 More

To be continued ...

5 Session information

```
> sessionInfo()

R Under development (unstable) (2013-02-28 r62089)
Platform: x86_64-unknown-linux-gnu (64-bit)
locale:
```

```
[1] LC_CTYPE=en_US.UTF-8
                                LC_NUMERIC=C
 [3] LC_TIME=en_US.UTF-8
                                LC_COLLATE=C
 [5] LC_MONETARY=en_US.UTF-8
                                LC_MESSAGES=en_US.UTF-8
 [7] LC_PAPER=C
                                LC_NAME=C
 [9] LC_ADDRESS=C
                                LC_TELEPHONE=C
[11] LC_MEASUREMENT=en_US.UTF-8 LC_IDENTIFICATION=C
attached base packages:
              parallel
[1] grid
                                  graphics grDevices utils
                        stats
[7] datasets
             methods
                        base
other attached packages:
[1] TxDb.Hsapiens.UCSC.hg19.knownGene_2.8.0
[2] GenomicFeatures_1.11.13
[3] AnnotationDbi_1.21.12
[4] Biobase_2.19.3
[5] biomvRCNS_0.99.3
[6] Gviz_1.3.13
[7] GenomicRanges_1.11.35
[8] IRanges_1.17.35
[9] BiocGenerics_0.5.6
loaded via a namespace (and not attached):
 [1] BSgenome_1.27.1
                        Biostrings_2.27.11 DBI_0.2-5
 [4] Hmisc_3.10-1
                        RColorBrewer_1.0-5 RCurl_1.95-3
 [7] RSQLite_0.11.2
                        Rsamtools_1.11.21 XML_3.95-0.1
[10] biomaRt_2.15.0
                        biovizBase_1.7.6
                                            bitops_1.0-5
```

colorspace_1.2-1

lattice_0.20-13

plyr_1.8

stats4_3.0.0

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