

# Journal of Statistical Software

MMMMMM YYYY, Volume VV, Issue II.

doi: 10.18637/jss.v000.i00

# DClusterm: Model-based Detection of Disease Clusters

Virgilio Gómez-Rubio

Universidad de Castilla-La Mancha

Paula Moraga
Queensland University of Technology

John Molitor
Oregon State University

Barry Rowlingson Lancaster University

#### Abstract

The detection of regions with unusually high risk plays an important role in disease mapping and the analysis of public health data. In particular, the detection of groups of areas (i.e., clusters) where the risk is significantly high is often conducted by Public Health authorities.

Many methods have been proposed for the detection of these disease clusters, most of them based on moving windows, such as Kulldorff's Spatial Scan Statistics. Here we describe a model-based approach for the detection of disease clusters implemented in the **DClusterm** package. Our model-based approach is based on representing a large number of possible clusters by dummy variables and then fitting many generalized linear models to the data where these covariates are included one at a time. Cluster detection is done by performing a variable or model selection among all fitted models using different criteria.

Because of our model-based approach, cluster detection can be performed using different types of likelihoods and latent effects. We cover the detection of spatial and spatio-temporal clusters, as well as how to account for covariates, zero-inflated datasets and overdispersion in the data.

Keywords: disease cluster, spatial statistics, R.

## 1. Introduction

The analysis of epidemiological data at small area level often involves accounting for possible risk factors and other important covariates using different types of regression models. However, it is not uncommon that after a number of covariates have been accounted for, residuals

still show a spatial distribution that defines some groups of areas with unusual high epidemiological risk. Hence, in many occasions it is not clear whether all spatial risk factors have been included in our model.

Public health data are often aggregated over small administrative areas due to issues of confidentiality. However, individual data are often available as well, and Generalized Linear Models (GLM, McCullagh and Nelder 1989) are a common framework used in disease mapping for modeling aggregated and individual-level information. GLMs not only model Poisson or binomial responses, but they can also link the outcome to a linear predictor on the covariates (and, possibly, other effects). However, until recently, it was not clear how to use GLMs to detect clusters of disease, a group of contiguous areas with significant high risk.

In order to detect disease clusters, the most widely used method is probably the Spatial Scan Statistic (SSS) proposed by Kulldorff (1997). Given a possible cluster z, the SSS will compare the relative risk in the cluster  $\theta_z$  to the relative risk outside the cluster  $\theta_{\overline{z}}$  using the following test:

$$H_0: \quad \theta_z = \theta_{\overline{z}} H_1: \quad \theta_z > \theta_{\overline{z}}$$
 (1)

This test is performed via the use of a likelihood ratio statistic, where many different possible clusters are tested in turn by changing the areas in z and the most likely cluster (i.e., the one with the highest value of the test statistic) is selected. Significance of this cluster is assessed with a Monte Carlo test that also provides the p-value.

Several R packages include an implementation of the SSS. **DCluster** (Gómez-Rubio, Ferrándiz-Ferragud, and López-Quílez 2005) implements the orginal version of the SSS for spatial binomial and Poisson data and can compute cluster significancy by means of bootstrap or a Gumbel distribution. Package **SpatialEpi** (Kim and Wakefield 2016) also implements the SSS for binomial or Poisson data and assesses significancy using a Monte Carlo test. **rsatscan** (Kleinman 2015) provides a set of functions to create the necessary data files and run the SaTScan<sup>TM</sup> software (for Windows) from R. Hence, spatio-temporal detection of disease clusters can also be performed. Package **scanstatistics** (Kjellson 2016) implements a number of space-time scan statistics, that includes spatio-temporal versions of the SSS. Similarly as the original SSS, these implementations lack of a general way of adjusting for covariates and assessing the significancy of non-primary clusters.

In this paper we describe a novel approach to disease cluster detection that provides a link between GLMs and SSS. We have implemented this approach via the free and open source **DClusterm** package for the R statistical software (R Core Team 2016). This approach involves fitting many different GLMs for which dummy variables that represent possible clusters are included one at a time. Cluster detection is based on selecting a number of dummy cluster variables using variable selection methods.

This paper is organized as follows. Section 2 will introduce the link between GLM and SSS. Next, in Section 3 we show how to include random effects in the detection of disease clusters to account for over-dispersion. The detection of disease clusters for zero-inflated data is discussed in Section 4. Section 5 describes how to extend these ideas to detect clusters in space and time. Finally, a discussion and some final remarks are provided in Section 6.

# 2. Generalized linear models for cluster detection

# 2.1. General description

An explicit link between GLM's and the SSS is provided by Jung (2009); Zhang and Lin (2009) who show that the test statistic for a given cluster is equivalent to fitting a GLM using a cluster variable as predictor. This cluster variable is a dummy variable which is 1 for the areas in the cluster and 0 for the areas outside the cluster. By including cluster covariates in the model we obtain an estimate of the increased risk (as measured by its associated coefficient) and its significance (by means of the associated p-value, for example).

We demonstrate our approach by first considering a Poisson model with expected counts  $E_i$  and observed cases  $O_i$  modeled as:

$$O_i \sim Po(E_i \theta_i)$$
$$\log(\mu_i) = \log(E_i) + \alpha + \beta x_i \tag{2}$$

Here  $\log(E_i)$  denotes an offset to account for the population "exposure" (age, gender, etc.) and  $\theta_i$  is the relative risk and it measures any deviation (increase or decrease) in the incidence of the disease from the expected number of cases. Finally,  $x_i$  represents a covariate associated with the outcome of interest.

After fitting this model, we obtain estimates  $\hat{\alpha}$  and  $\hat{\beta}$  which account for the effects of non-cluster covariates in the model. We include the cluster covariates as follows:

$$\log(\mu_i) = \log(E_i) + \hat{\alpha} + \hat{\beta}x_i + \gamma_j c_i^{(j)}$$
(3)

The overall intercept is now  $\log(E_i) + \hat{\alpha} + \hat{\beta}x_i$  and  $c_i^{(j)}$  denotes a dummy variable associated with cluster j, with j denoting an index over the list of all possible clusters being tested, defined as

$$c_i^{(j)} = \begin{cases} 1 & \text{if area } i \text{ belongs to cluster } j \\ 0 & \text{otherwise} \end{cases}$$
 (4)

Here,  $\gamma_j$  is a measure of the risk within cluster j. We are only interested in clusters whose coefficient is significantly higher than 0 (i.e., increased risk). Hence those with a significant negative coefficient will be ignored. We use model selection techniques to select the most important cluster in the study region. As such, the log-likelihood can be used to compare the model with the cluster variables to the null model (i.e., the one with no cluster covariates at all).

It is possible to perform cluster detection without considering non-cluster based covariates in the model. Here, cluster detection accounting for the non-cluster based covariates will likely provide a different number of clusters than models fit without these variables. By comparing the clusters detected in both models (with and without non-cluster based covariates), we will be able to find which clusters are linked to underlying risk factors included in the model and which clusters remain unexplained by these other variables. In the examples that we include in this paper, we will consider both scenarios to better understand how cluster detection works.

Similar approaches to detection of disease clusters have been proposed by Bilancia and Demarinis (2014); Gómez-Rubio, Moraga, and Molitor (2017) who describe a similar approach to the detection of disease clusters using Bayesian hierarchical models. The Integrated Nested Laplace Approximation (INLA) is used in both cases for model fitting as it provides computational benefits over other computationally expensive methods, such as Markov Chain Monte Carlo.

## 2.2. Leukemia in upstate New York

We first consider an example where we model counts of leukemia cases in upstate New York. These data are provided in the NY8 dataset, available in package DClusterm. It provides cases of leukemia in different census tracts in upstate New York. This data set has been analyzed by several authors (Waller, Turnbull, Clark, and Nasca 1992; Waller and Gotway 2004). The location of leukemia is thought to be linked to the use of Trichloroethene (TCE) by several companies in the area. Figure 1 shows the Standardized Mortality Ratios of the census tracts and the locations of the industries using TCE.

In order to measure exposure, the inverse of the distance to the nearest TCE site has been used (variable PEXPOSURE in the dataset). In addition, two other socioeconomic covariates have been used: the percentage of people aged 65 or more (variable PCTAGE65P) and the percentage of people who own their home (variable PCTOWNHOME).

Hence, our first action is to load some required packages, such as **xts** (Ryan and Ulrich 2014), and the dataset itself.

```
R> library("DClusterm")
R> library("xts")
R> data("NY8")
```

A number of cases could not be linked to their actual location and they were distributed uniformly over the study area, making the counts real numbers instead of integers. We have rounded these values as we intend to use a Poisson likelihood for the analysis. Furthermore, expected counts are computed using the overall incidence ratio (i.e., total number of cases divided by the total population). Age-sex standardization is not possible in this case as this information is not available in our dataset.

```
R> NY8$Observed <- round(NY8$Cases)
R> NY8$Expected <- NY8$POP8 * sum(NY8$Observed) / sum(NY8$POP8)
R> NY8$SMR <- NY8$Observed / NY8$Expected
```

The centres of the areas will be stored in columns named x and y. This will be used later when ordering the areas by increasing distance to the putative cluster centre. If the location of the main populated cities are available these could be used but here we will use function coordinates() instead:

```
R> NY8$x <- coordinates(NY8)[, 1]
R> NY8$y <- coordinates(NY8)[, 2]
```

As **DClusterm** is designed to detect clusters in space and time, it will always expect data to be from one of the classes in package **spacetime** (Pebesma 2012) to store all the data, even if they are available for a single period of time. In this case, a STFDF object is created to store all the data but note that in this case we do not have a truly space-time dataset. Hence, the time series in the data is made of a single date entry ("1972-01-01") and that it is just a convenient way of having our data in a STFDF object.

```
R> NY8st <- STFDF(as(NY8, "SpatialPolygons"), xts(1, as.Date("1972-01-01")),
+ NY8@data, endTime = as.POSIXct(strptime(c("1972-01-01"), "%Y-%m-%d"),
+ tz = "GMT"))</pre>
```

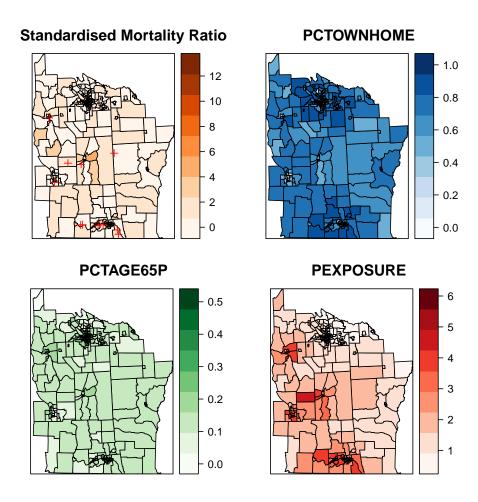


Figure 1: Standardised Mortality Ratios and covariates of the incidence of Leukemia in upstate New York dataset. PEXPOSURE is the inverse of the distance to the nearest TCE site, PCTAGE65P is the percentage people aged 65 or more, and PCTOWNHOME is the percentage of people who own their home. The red crosses in the top-left map mark the locations of the TCE sites.

#### 2.3. Cluster detection

Cluster detection with no covariates

First of all, a model with no covariates will be fitted and used as a baseline, so that other models can be compared to this one (for example, using the AIC or the log–likelihood) to assess whether they provide a better fit.

Function DetectClustersModel() will take this baseline model (using argument model0), create the cluster dummy variables and test them in turn. Then, those clusters with a highest significance will be reported.

Argument thegrid will take a 2-column data.frame (with names x and y) with the centres of possible clusters. If the grid of cluster centres is not defined, then a rectangular grid is used with a distance between adjacent points defined by argument step. Dummy cluster variables are created around these points by adding areas to the cluster until a certain percentage of the population (defined by argument fractpop), with the column to be used to compute the population at risk in the cluster defined by parameter ClusterSizeContribution, or until a certain distance about the centre (defined by argument radius) has been reached. When testing for significant cluster variables, argument alpha defines the significance level.

DetectClustersModel() can detect spatial and spatio-temporal clusters, which is why its first argument is a space-time object. The type of clusters that are investigated is defined by argument typeCluster. In the example we have used typeCluster = "S".

Other options include the number of replicates for Monte Carlo tests (argument R) if cluster assessment is done by simulation. By default, Monte Carlo tests are not used. **DClusterm** allows for parallel computing using several cores as implemented in package **parallel**. The number of cores to use is defined in option mc.cores (now 4 cores are used):

```
R> options(mc.cores = 4)
```

In the following example, to reduce the computational burden, we have only looked for clusters around 5 areas (whose rows in NY8 are defined in variable idxcl). In a real application we advise the use of all locations (area centroids or actual locations of individual data).

Below is a summary of the clusters detected. Dates can be ignored as this is a purely spatial cluster analysis. In the case of spatio-temporal clusters, dates shown define the temporal range of the cluster. Values x and y defined the cluster centre, size is the number of areas in

the cluster, statistic is the value of the test statistic and risk represents the point estimate of the associated cluster coefficient. Also, note that only clusters with a lower pvalue than argument alpha are returned. cluster indicates whether the cluster is a significant one. Finally, note how detected clusters are ordered by increasing value of pvalue, so that the most significant clusters are reported first.

```
R> ny.c10
```

```
y size
                               minDateCluster
                                                    maxDateCluster
           X
                       39 1972-01-01 01:00:00 1972-01-01 01:00:00
   424728.9 4661404
11
                        9 1972-01-01 01:00:00 1972-01-01 01:00:00
88 409430.4 4720092
119 404710.7 4768346
                       24 1972-01-01 01:00:00 1972-01-01 01:00:00
   statistic
                    pvalue
                                risk cluster
11
    8.044846 0.0000604120 0.3916904
                                         TRUE
    6.967107 0.0001893208 0.6455613
88
                                         TRUE
119 3.254824 0.0107290781 0.4445236
                                        TRUE
```

Function get.knclusters() can be used to extract the indices of the areas in the different clusters detected. In the next lines, we show how to write a new function called get.allknclusters() to obtain all the clusters detected together in a single variable:

The areas and centers of the clusters detected are shown in Figure 2. Because of the lack of adjustment for covariates these clusters show regions of high risk based on the raw data (observed and expected counts) alone.

Cluster detection after adjusting for covariates

Similarly, clusters can be detected after adjusting for significant risk factors. First of all, we will fit a Poisson regression with the 3 covariates mentioned earlier. As it can be seen, all three are significant:

```
Call:
glm(formula = Observed ~ offset(log(Expected)) + PCTOWNHOME +
    PCTAGE65P + PEXPOSURE, family = "poisson", data = NY8)
Deviance Residuals:
    Min
             1Q Median
                               3Q
                                       Max
-2.9099 -1.1294 -0.1768
                           0.6385
                                    3.2426
Coefficients:
           Estimate Std. Error z value Pr(>|z|)
                     0.18550 -3.531 0.000413 ***
(Intercept) -0.65507
PCTOWNHOME -0.36472
                       0.19316 -1.888 0.058998 .
PCTAGE65P
            4.05031
                       0.60559
                                 6.688 2.26e-11 ***
PEXPOSURE
            0.15141
                       0.03165
                                4.784 1.72e-06 ***
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
(Dispersion parameter for poisson family taken to be 1)
    Null deviance: 459.05 on 280 degrees of freedom
Residual deviance: 384.01 on 277 degrees of freedom
AIC: 958.97
```

Number of Fisher Scoring iterations: 5

R> ny.cl1 <- DetectClustersModel(NY8st,

As the three covariates are significant, the expected number of cases will be different now and the detected clusters may be different in this case. Cluster detection is performed as in the previous example, but now we use the model that adjusts for covariates instead:

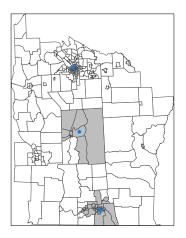
the grid = as.data.frame(NY8)[idxcl, c("x", "y")], fract pop = 0.15,

```
alpha = 0.05, typeCluster = "S", R = NULL, model0 = ny.m1,
    ClusterSizeContribution = "POP8")
R> ny.cl1
                               minDateCluster
                                                   maxDateCluster
                   y size
88 409430.4 4720092
                        9 1972-01-01 01:00:00 1972-01-01 01:00:00
119 404710.7 4768346
                       20 1972-01-01 01:00:00 1972-01-01 01:00:00
   statistic
                    pvalue
                                risk cluster
88
    5.861204 0.0006175202 0.5869176
                                        TRUE.
119 3.160591 0.0119304026 0.4882633
                                        TRUE.
```

Similarly as in the previous example, we can use function get.allkncluster() to get the indices of the areas in the clusters and add a new variable to the SpatialPolygonsDataFrame:

```
R> NY8$CLUSTER1 <- get.allknclusters(NY8, ny.cl1)
```

Figure 2 shows the clusters detected after adjusting for covariates. Compared to the example with no covariate adjustment, one cluster has disappeared. Hence, that cluster has been explained by the effect of the covariates. Another cluster is a bit smaller in size, which means that covariates only explain a small part of it. The most significant cluster remains the same. In all cases, cluster significance has been reduced by the effect of the covariates.



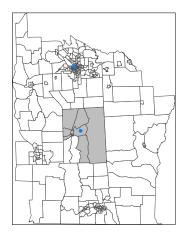


Figure 2: Clusters detected with no covariate adjustment (left) and after adjusting for covariates (right). Areas in clusters are shaded in gray and cluster centres are represented by blue dots.

# 3. Mixed-effects models for cluster detection

Random effects can be incorporated into our models to account for unmeasured risk factors. Cluster detection will be performed as usual, but we should keep in mind that by including random effects and dummy cluster covariates there may be a clash between the two. By using dummy variables we are intentionally looking for unexplained spatial variation in the data. Hence, random effects should aim at modelling a different structure in the data.

Random effects are particularly useful to model over-dispersion in count data. For the Poisson case, this will mean that the relative risk can be modelled as:

$$\log(\mu_i) = \log(E_i) + \alpha + \beta x_i + \gamma_j c_i^{(j)} + u_i$$

$$u_i \sim N(0, \sigma_u^2)$$
(5)

where  $u_i$  represents a random effect normally distributed with zero mean and variance  $\sigma_u^2$ . Note that random effects can be defined to be spatially correlated, as suggested by Bilancia and Demarinis (2014). However, this can produce a clash between the dummy cluster variables and the random effects.

# 3.1. Leukemia in upstate New York

We go back to the example on the leukemia incidence in upstate New York to show how models can include random effects and, at the same time, detect disease clusters. In this particular example, random effects will be important in order to reflect any over-dispersion present in the data. For this reason, our first step here is to test the data for over-dispersion using Dean's  $P_B$  and  $P_B'$  score tests (see, Dean 1992, for details). These two tests have been implemented in functions DeanB() and DeanB2() in the **DCluster** (Gómez-Rubio *et al.* 2005) package. They both take a glm object and perform the score tests:

```
R> DeanB(ny.m0)

Dean's P_B test for overdispersion

data: ny.m0
P_B = 5.5755, p-value = 1.234e-08
alternative hypothesis: greater

R> DeanB2(ny.m0)

Dean's P'_B test for overdispersion

data: ny.m0
P'_B = 5.6233, p-value = 9.368e-09
alternative hypothesis: greater
```

From the results, it is clear that when no covariates are included data are clearly overdispersed. Hence, a Poisson distribution will not be appropriate to model the observed counts in each tract.

The same tests applied to the model with covariates produce a similar result:

Although p-values have increased, they are both small and we may still consider that data are over-dispersed. Hence, we will aim at detecting clusters using a Poisson regression with independent random effects to account for census tract-level heterogeneity.

#### 3.2. Cluster detection

Cluster detection with no covariates

The baseline model with no covariate will now be fitted with function glmer() from package lme4 (Bates, Mächler, Bolker, and Walker 2015). This function is similar to glm() for GLMs but it will allow us to include random effects in the model as part of the formula argument.

```
R> library("lme4")
R> ny.mm0 <- glmer(Observed ~ offset(log(Expected)) + (1 | AREANAME),</pre>
     data = as(NY8, "data.frame"), family = "poisson")
R> summary(ny.mm0)
Generalized linear mixed model fit by maximum likelihood (Laplace
  Approximation) [glmerMod]
 Family: poisson (log)
Formula: Observed ~ offset(log(Expected)) + (1 | AREANAME)
   Data: as(NY8, "data.frame")
     AIC
                    logLik deviance df.resid
              BIC
  1010.8
           1018.1
                   -503.4
                            1006.8
                                         279
Scaled residuals:
            1Q Median
                            3Q
                                   Max
-2.1185 -0.8799 -0.2617 0.7784 5.0263
Random effects:
 Groups
        Name
                     Variance Std.Dev.
 AREANAME (Intercept) 0.2111
                               0.4594
Number of obs: 281, groups: AREANAME, 64
Fixed effects:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.2410
                        0.1051 -2.293 0.0219 *
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
R> ny.clmm0 <- DetectClustersModel(NY8st,</pre>
     the grid = as.data.frame(NY8)[idxcl, c("x", "y")], fractpop = 0.15,
     alpha = 0.05, typeCluster = "S", R = NULL, model0 = ny.mm0,
     ClusterSizeContribution = "POP8")
R> ny.clmm0
                  y size
                              minDateCluster
                                                  maxDateCluster
88 409430.4 4720092
                      9 1972-01-01 01:00:00 1972-01-01 01:00:00
119 404710.7 4768346 24 1972-01-01 01:00:00 1972-01-01 01:00:00
```

```
statistic pvalue risk cluster
88 7.577766 9.900781e-05 0.7880056 TRUE
119 2.415960 2.793750e-02 0.7862091 TRUE
```

After accounting for overdispersion, the number of clusters detected is 2. These are shown in Figure 3. The largest cluster detected before has now disappeared and only the two smallest clusters remain. This may be due to the fact that the first cluster has the smallest SMR and risk. Hence, allowing for extra-variation will make the discrepancy between observed and expected less extreme and this cluster will be the first one to be declared as non-significant. The two remaining clusters have the same size and a very similar risk than in the previous case.

Cluster detection with covariates

```
R> ny.mm1 <- glmer(Observed ~ offset(log(Expected)) + PCTOWNHOME +
     PCTAGE65P + PEXPOSURE + (1 | AREANAME),
     data = as(NY8, "data.frame"), family = "poisson")
R> summary(ny.mm1)
Generalized linear mixed model fit by maximum likelihood (Laplace
  Approximation) [glmerMod]
 Family: poisson (log)
Formula:
Observed ~ offset(log(Expected)) + PCTOWNHOME + PCTAGE65P + PEXPOSURE +
    (1 | AREANAME)
   Data: as(NY8, "data.frame")
     AIC
              BIC
                    logLik deviance df.resid
   959.8
                    -474.9
            978.0
                              949.8
                                         276
Scaled residuals:
             1Q Median
-2.1451 -0.8697 -0.1932 0.6963 4.0848
Random effects:
          Name
 Groups
                      Variance Std.Dev.
 AREANAME (Intercept) 0.01532 0.1238
Number of obs: 281, groups: AREANAME, 64
Fixed effects:
            Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.73898
                        0.21947
                                -3.367
                                         0.00076 ***
PCTOWNHOME -0.38390
                        0.21622 -1.776 0.07582 .
PCTAGE65P
             4.04222
                        0.62575
                                  6.460 1.05e-10 ***
                        0.03662
                                  4.413 1.02e-05 ***
PEXPOSURE
             0.16159
```

```
Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
Correlation of Fixed Effects:
           (Intr) PCTOWN PCTAGE
PCTOWNHOME -0.734
PCTAGE65P -0.465 0.145
PEXPOSURE -0.567 0.211 -0.023
R> ny.clmm1 <- DetectClustersModel(NY8st,</pre>
     the grid = as.data.frame(NY8)[idxcl, c("x", "y")], fract pop = 0.15,
     alpha = 0.05, typeCluster = "S", R = NULL, model0 = ny.mm1,
     ClusterSizeContribution = "POP8")
R> ny.clmm1
                  y size
                              minDateCluster
                                                   maxDateCluster
88 409430.4 4720092
                       1 1972-01-01 01:00:00 1972-01-01 01:00:00
                               risk cluster
   statistic
                  pvalue
   4.051264 0.004420356 0.03289885
                                        TRUF.
```

When overdispersion and covariates are included in the model, only one of the clusters remains with size 1 and a slightly reduced estimate of the cluster coefficient. This should not come as a surprise given that we have already seen how including covariates explains some of the extra-variation and that by including random effects the significance of the clusters is also reduced. A summary of the clusters detected can be found in Figure 3.

As in the example in Section 2.2, we have created two cluster variables to display the clusters obtained:

```
R> NY8$CLUSTERMM0 <- get.allknclusters(NY8, ny.clmm0)
R> NY8$CLUSTERMM1 <- get.allknclusters(NY8, ny.clmm1)</pre>
```

## 4. Zero-inflated models for cluster detection

The analysis of rare diseases often involves datasets where there are many areas with zero counts, leading to zero-inflated data. In this situation the Poisson or binomial likelihoods may not be suitable to fit a model and other distributions for the data should be used. Gómez-Rubio and López-Quílez (2010) discuss this issue and they have extended model-based cluster detection methods to account for zero-inflation.

For count data, a zero-inflated Poisson model could be used. In this case, observed number of cases come from a mixture distribution of a Poisson and a distribution with all mass at zero. Probabilities are as follows:

$$Pr(O_i = n_i) = \begin{cases} \pi_i + (1 - \pi_i) Po(0|\theta_i E_i) & n_i = 0\\ (1 - \pi_i) Po(n_i|\theta_i E_i) & n_i = 1, 2, \dots \end{cases}$$
 (6)

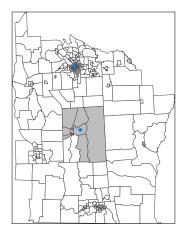




Figure 3: Clusters detected with no covariate adjustment (left) and after adjusting for covariates (right) using a mixed-effects model to account for overdispersion of the data. Areas in clusters are shaded in gray and cluster centers are represented by blue dots.

Here  $Po(O_i|\theta_i E_i)$  represents the probability of observing  $O_i$  cases using a Poisson distribution with mean  $\theta_i E_i$ .  $\pi_i$  represents the proportion of zeroes observed that do not come from the Poisson distribution.

Relative risks  $\theta_i$  can be modeled using a log-linear model to depend on some relevant risk factors. Also, it is common that all  $\pi_i$ 's are taken equal to a single value  $\pi$ .

# 4.1. Brain cancer in Navarre (Spain)

Ugarte, Ibáñez, and Militino (2006) analyze the incidence of brain cancer in Navarre (Spain) at the health district level. Figure 4 shows the Standardized Mortality Ratios. As it can be seen there are many areas where the SMR is zero because there are no cases in those areas. Ugarte, Ibáñez, and Militino (2004) have also reported a significant zero-inflation of these data compared to a Poisson distribution. For cluster detection, the method implemented in DClusterm is similar to the one used in Gómez-Rubio and López-Quílez (2010) for the detection of disease clusters of rare diseases.

#### 4.2. Cluster detection

Before starting our cluster detection methods, we will check the appropriateness of a Poisson distribution for this data. Fitting a log-linear model (with no covariates) gives the following model:

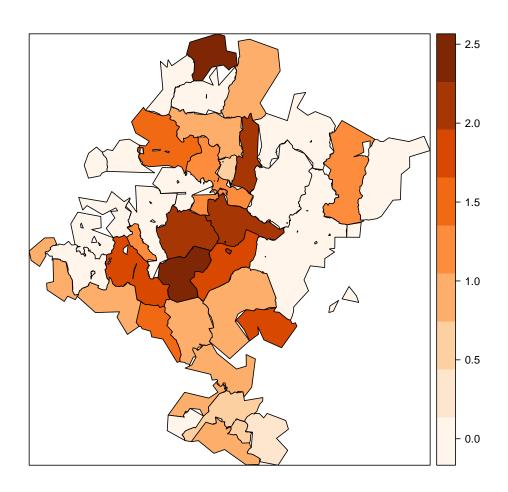


Figure 4: SMR of brain cancer in Navarre (Spain).

#### Deviance Residuals:

Min 1Q Median 3Q Max -2.5227 -1.4783 -0.3203 0.7042 1.6393

## Coefficients:

Estimate Std. Error z value Pr(>|z|) (Intercept) -7.752e-06 8.805e-02 0 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 63.733 on 39 degrees of freedom Residual deviance: 63.733 on 39 degrees of freedom

AIC: 145.02

Number of Fisher Scoring iterations: 5

Furthermore, a quasipoisson model has been fitted in order to assess any extra-variation in the data:

```
R > \text{nav.mOq} \leftarrow \text{glm}(OBSERVED \sim \text{offset}(\log(EXPECTED)) + 1, data = brainnav,}
     family = "quasipoisson")
R> summary(nav.m0q)
Call:
glm(formula = OBSERVED ~ offset(log(EXPECTED)) + 1, family = "quasipoisson",
    data = brainnav)
Deviance Residuals:
    Min
              10
                  Median
                              30
                                         Max
-2.5227 -1.4783 -0.3203 0.7042 1.6393
Coefficients:
              Estimate Std. Error t value Pr(>|t|)
(Intercept) -7.752e-06 9.703e-02
(Dispersion parameter for quasipoisson family taken to be 1.214555)
    Null deviance: 63.733 on 39 degrees of freedom
Residual deviance: 63.733 on 39 degrees of freedom
AIC: NA
Number of Fisher Scoring iterations: 5
```

The dispersion parameter in the previous model seems to be higher than 1, which may mean that the Poisson distribution is not appropriate.

For this reason, and following Ugarte *et al.* (2004), a zero-inflated Poisson model has been fitted using function <code>zeroinfl()</code> from package <code>pscl</code> (Zeileis, Kleiber, and Jackman 2008). Here is the resulting model:

```
Count model coefficients (poisson with log link):

Estimate Std. Error z value Pr(>|z|)

(Intercept) 0.09347 0.09459 0.988 0.323

Zero-inflation model coefficients (binomial with logit link):

Estimate Std. Error z value Pr(>|z|)

(Intercept) -1.6158 0.6435 -2.511 0.012 *

---

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Number of iterations in BFGS optimization: 9

Log-likelihood: -69.08 on 2 Df
```

Hence, the zero-inflated Poisson model will be used now to detect clusters of disease. As in the example on the New York leukemia dataset, a **spacetime** object will store all the information. The column for the expected counts must be named **Expected**, and this is our first step. Note also that, because only one time period is considered, data will have a single value and it is the 1st of January of 1990.

```
R> brainnav$Expected <- brainnav$EXPECTED
R> brainnavst <- STFDF(as(brainnav, "SpatialPolygons"),
+ xts(1,as.Date("1990-01-01")), as(brainnav, "data.frame"),
+ endTime = as.POSIXct(strptime(c("1990-01-01"), "%Y-%m-%d"), tz = "GMT"))</pre>
```

Function DetectClustersModel() will perform the cluster detection using a zeroinfl model. This provides a very flexible way of handling different types of models in R for cluster detection.

```
R> nav.c10 <- DetectClustersModel(brainnavst, coordinates(brainnav),
+ fractpop = 0.25, alpha = 0.05, typeCluster = "S", R = NULL,
+ model0 = nav.mOzip, ClusterSizeContribution = "EXPECTED")</pre>
```

The output will show the following clusters:

R> nav.cl0

```
x y size minDateCluster maxDateCluster
31 596886.8 4710520 4 1990-01-01 01:00:00 1990-01-01 01:00:00
30 611795.5 4713762 3 1990-01-01 01:00:00 1990-01-01 01:00:00
statistic pvalue risk cluster
31 2.520092 0.02476587 0.5987255 TRUE
30 2.016942 0.04459518 0.6139100 TRUE
```

As it can be seen, two clusters (with a p-value lower than 0.05) are detected. However, they overlap and we will just consider the one with the lowest p-value, which is shown in Figure 5. An index for the areas in each of the detected cluster can be obtained with function knbinary(). This function will return a data.frame with all the dummy cluster variables, i.e., the returned

data.frame will have as many columns as clusters and a number of rows equal to the number of areas. Entries will be 1 if the corresponding areas are in a cluster and 0 otherwise. These indices can be used for a number of analyses, such as checking whether two clusters overlap or computing the number of times an area is included in a cluster. In the following example we obtain the representation of all the clusters detected and the first one, the most significant, is added as a new column to the original SpatialPolygonsDataFrame to be displayed in Figure 5.

```
R> nav.clusters <- get.knclusters(brainnav, nav.cl0)
R> brainnav$CLUSTER <- ""
R> brainnav$CLUSTER [ nav.clusters[[1]] ] <- "CLUSTER"
R> brainnav$CLUSTER <- as.factor(brainnav$CLUSTER)</pre>
```

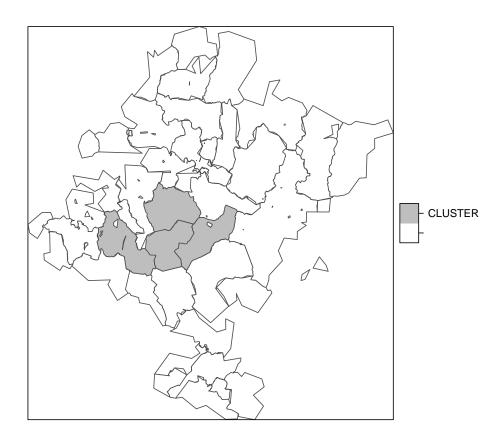


Figure 5: Cluster of brain cancer detected in Navarre (Spain).

# 5. Spatio-temporal clusters

Jung (2009) discusses how to extend model-based approaches for the detection of spatial disease clusters to space and time. Gómez-Rubio et al. (2017) propose the following model:

$$\log(\mu_{i,t}) = \log(E_{i,t}) + \gamma_j c_{i,t}^{(j)}$$
(7)

where  $\mu_{i,t}$  is the mean of area i at time t and  $c_{i,t}^{(j)}$  a cluster dummy variable for spatio-temporal cluster j. Random effects can also be included in Equation 7 as described in Section 3 and zero-inflated distributions can also be considered as in Section 4.

Note how now data are indexed according to space and time. Dummy cluster variables are defined as in the spatial case, by considering areas in the cluster according to their distance to the cluster center, for data within a particular time period. When defining a temporal cluster, areas are aggregated using all possible temporal windows up to a predefined temporal range.

#### 5.1. Brain cancer in New Mexico

The brainNM dataset (included in **DClusterm**) contains yearly cases of brain cancer in New Mexico from 1973 to 1991 (inclusive) in a **spacetime** object. The data set has been taken from the SaTScan website and the area boundaries from the U.S. Census Bureau. In addition, the location of Los Alamos National Laboratory (LANL) has been included (from Wikipedia). Inverse distance to this site can be used to test for increased risk in the areas around the Laboratory as no other covariates are available.

## R> data("brainNM")

Expected counts have been obtained using age and sex standardization over the whole period of time. Hence, yearly differences are likely to be seen when plotting the data. Standardized Mortality Ratios have been plotted in Figure 6.

## 5.2. Cluster detection

Cluster detection with no covariates

Similarly as in the purely spatial case, a Poisson model with no covariates will be fitted first:

```
R> nm.m0 <- glm(Observed ~ offset(log(Expected)) + 1, family = "poisson",
     data = brainst)
R> summary(nm.m0)
Call:
glm(formula = Observed ~ offset(log(Expected)) + 1, family = "poisson",
    data = brainst)
Deviance Residuals:
    Min
              10
                   Median
                                 30
                                         Max
-2.4874 -0.9998 -0.4339
                            0.3773
                                      3.1321
Coefficients:
```

Estimate Std. Error z value Pr(>|z|)

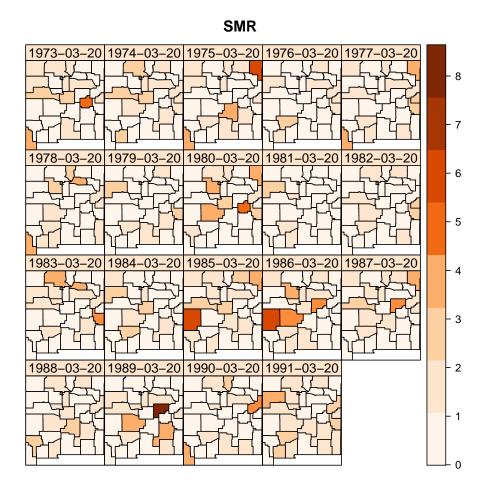


Figure 6: Standardized Mortality Ratios of brain cancer in New Mexico.

(Intercept) 2.834e-16 2.917e-02 0

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 631.64 on 607 degrees of freedom Residual deviance: 631.64 on 607 degrees of freedom

AIC: 1585.6

Number of Fisher Scoring iterations: 5

Before proceeding to disease cluster detection, we have extracted the centroids of the counties in New Mexico by using function coordinates() from the sp slot in the STIDF object that stores the data.

R> NM.coords <- coordinates(brainst@sp)</pre>

Cluster detection with function DetectClustersModel() takes arguments minDateUser and maxDateUser to define the minimum and maximum times that are considered when looking

for clusters. In this example the time period has been constrained to 1985–1989. Furthermore, typeCluster = "ST" is used to look for spatio-temporal clusters.

```
R> nm.cl0 <- DetectClustersModel(brainst, NM.coords,
+ minDateUser = "1985-01-01", maxDateUser = "1989-01-01",
+ fractpop = 0.15, alpha = 0.05, typeCluster = "ST", R = NULL,
+ model0 = nm.m0, ClusterSizeContribution = "Expected")</pre>
```

180 possible clusters have been found this time. However, note that most of them overlap and may be different configurations of the same cluster. The first 5 are summarized below:

```
R> nm.cl0[1:5,]
```

```
minDateCluster
                      y size
                                                      maxDateCluster
                           3 1986-03-20 01:00:00 1988-03-20 01:00:00
0286 -106.3073 35.86930
0496 -105.9761 35.50684
                           2 1986-03-20 01:00:00 1988-03-20 01:00:00
0531 -106.9303 34.00725
                           9 1985-03-20 01:00:00 1986-03-20 01:00:00
0498 -105.9761 35.50684
                           2 1987-03-20 01:00:00 1988-03-20 01:00:00
0288 -106.3073 35.86930
                           2 1987-03-20 01:00:00 1988-03-20 01:00:00
                                 risk cluster
    statistic
                    pvalue
0286 7.493492 0.0001082553 0.6814588
                                         TRUE
0496 6.438221 0.0003327442 0.6970405
                                         TRUE
0531 6.378992 0.0003544929 0.3838756
                                         TRUE
0498 6.331113 0.0003731179 0.8070901
                                         TRUE
0288 6.331113 0.0003731179 0.8070901
                                         TRUE
```

Cluster detection after adjusting for covariates

In this case, we will use the inverse of the distance to LANL as a covariate as no other information about the areas is available. Distances have been computed using function spDistsN1() from package sp (Pebesma and Bivand 2005). Given that coordinates are expressed in longitude and latitude great circle distances are used.

```
R> dst <- spDistsN1(pts = NM.coords, pt = losalamos, longlat = TRUE)</pre>
```

Distances need to be put together in a way that values are available for all time periods. In this case, given that distances do not change over time, a vector is created by repeating the vector of distances as many times as time slots (years) we have in the dataset.

```
R> nyears <- length(unique(brainst$Year))
R> brainst$IDLANL <- rep(1 / dst, nyears)</pre>
```

With all these data we are now able to fit a baseline model.

```
R> nm.m1 <- glm(Observed ~ offset(log(Expected)) + IDLANL,
+ family = "poisson", data = brainst)
R> summary(nm.m1)
```

```
Call:
```

```
glm(formula = Observed ~ offset(log(Expected)) + IDLANL, family = "poisson",
    data = brainst)
```

#### Deviance Residuals:

```
Min 1Q Median 3Q Max -2.4832 -0.9982 -0.4280 0.3775 3.1424
```

#### Coefficients:

```
Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.005721  0.029897  -0.191  0.848
IDLANL  0.338467  0.365200  0.927  0.354
```

(Dispersion parameter for poisson family taken to be 1)

```
Null deviance: 631.64 on 607 degrees of freedom Residual deviance: 630.84 on 606 degrees of freedom
```

AIC: 1586.8

Number of Fisher Scoring iterations: 5

Note how now the included covariate is not significant. For illustrative purposes, we will still keep the covariate in our model for the cluster detection. However, non-significant covariates will have a tiny impact on the clusters detected as they will not produce a change in the expected number of cases.

```
R> nm.cl1 <- DetectClustersModel(brainst, NM.coords, fractpop = 0.15,
+ alpha = 0.05, minDateUser = "1985-01-01", maxDateUser = "1989-01-01",
+ typeCluster = "ST", R = NULL, model0 = nm.m1,
+ ClusterSizeContribution = "Expected")</pre>
```

The number of clusters detected in this case is 179, very similar to the 180 found when no covariates where included in the model. This was expected as the included covariate was not significant. By inspecting the five most significant clusters we can observe that they are very similar to the ones detected before:

#### R> nm.cl1[1:5,]

```
y size
                                  minDateCluster
                                                      maxDateCluster
0286 -106.3073 35.86930
                           3 1986-03-20 01:00:00 1988-03-20 01:00:00
0531 -106.9303 34.00725
                           9 1985-03-20 01:00:00 1986-03-20 01:00:00
0533 -106.9303 34.00725
                          10 1985-03-20 01:00:00 1988-03-20 01:00:00
0498 -105.9761 35.50684
                           2 1987-03-20 01:00:00 1988-03-20 01:00:00
                           2 1987-03-20 01:00:00 1988-03-20 01:00:00
0288 -106.3073 35.86930
    statistic
                     pvalue
                                 risk cluster
0286 6.857035 0.0002128539 0.6487021
                                         TRUE
```

```
0531 6.468803 0.0003220466 0.3867416 TRUE
0533 6.127874 0.0004638274 0.2581940 TRUE
0498 5.789493 0.0006670128 0.7673277 TRUE
0288 5.789493 0.0006670128 0.7673277 TRUE
```

Note how these clusters only cover a few areas, but over several years.

In order to exploit the output from DetectClustersModel(), function get.stclusters() will take the data and this output to return a list with the indices of the areas in the clusters. The next example shows how to add a new variable to brainst with the space-time regions in the most significant cluster, which is displayed in Figure 7.

```
R> stcl <- get.stclusters(brainst, nm.cl0)
R> brainst$CLUSTER <- ""
R> brainst$CLUSTER[ stcl[[1]] ] <- "CLUSTER"</pre>
```

#### **CLUSTER**

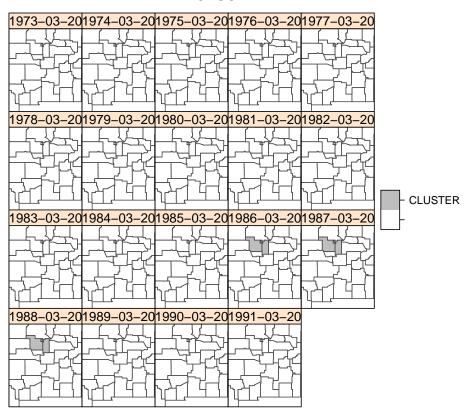


Figure 7: Most significant spatio-temporal cluster of brain cancer detected in New Mexico.

# 6. Discussion

In this paper we have introduced **DClusterm**, a new package for the R statistical computing software for the detection of disease clusters using a model-based approach, following recent developments by several authors. Clusters are represented by dummy variables that are introduced into a generalized linear model and different likelihoods can be used to account for different types of data. Because of this model-based approach, fixed effects (to consider relevant risk factors) and random effects (to account for other non-spatial unmeasured risk factors) can be put in the linear predictor as well.

In our examples we have considered well-known datasets to show how the functions in the **DClusterm** package tackle the problem of cluster detection. The results are similar to those found in relevant papers where the same datasets have been analyzed using a similar methodology. In particular, we have considered the case of the detection of clusters in space and space-time, zero-inflated data and over-dispersed data.

# 7. Acknowledgments

This package was initially developed by Paula Moraga as a Google Summer of Code project. Virgilio Gómez-Rubio has been supported by grant PPIC-2014-001, funded by Consejería de Educación, Cultura y Deportes (JCCM) and FEDER, and grant MTM2016-77501-P, funded by Ministerio de Economía y Competitividad.

# References

- Auguie B (2016). *gridExtra:* Miscellaneous Functions for "Grid" Graphics. R Package Version 2.2.1, URL https://CRAN.R-project.org/package=gridExtra.
- Bates D, Mächler M, Bolker B, Walker S (2015). "Fitting Linear Mixed-Effects Models Using lme4." *Journal of Statistical Software*, **67**(1), 1–48. doi:10.18637/jss.v067.i01.
- Bilancia M, Demarinis G (2014). "Bayesian Scanning of Spatial Disease Rates with Integrated Nested Laplace Approximation (INLA)." Statistical Methods & Applications, 23(1), 71–94. ISSN 1618-2510. URL http://dx.doi.org/10.1007/s10260-013-0241-8.
- Dean CB (1992). "Testing for Overdispersion in Poisson and Binomial Regression Models." Journal of the American Statistical Association, 87(418), 451–457.
- Gómez-Rubio V, López-Quílez A (2010). "Statistical Methods for the Geographical Analysis of Rare Diseases." Advances in Experimental Medicine and Biology, **686**, 151–171.
- Gómez-Rubio V, Moraga P, Molitor J (2017). "Fast Bayesian Classification for Disease Mapping and the Detection of Disease Clusters." *Under Review*.
- Gómez-Rubio V, Ferrándiz-Ferragud J, López-Quílez A (2005). "Detecting Clusters of Disease with R." *Journal of Geographical Systems*, **7**(2), 189–206.
- Jung I (2009). "A Generalized Linear Models Approach to Spatial Scan Statistics for Covariate Adjustment." *Statistics in Medicine*, **28**(7), 1131–1143.

- Kim AY, Wakefield J (2016). *SpatialEpi: Methods and Data for Spatial Epidemiology*. R Package Version 1.2.2, URL https://CRAN.R-project.org/package=SpatialEpi.
- Kjellson B (2016). scanstatistics: Space-Time Anomaly Detection using Scan Statistics. R Package Version 0.1.0, URL https://CRAN.R-project.org/package=scanstatistics.
- Kleinman K (2015). rsatscan: Tools, Classes, and Methods for Interfacing with SaTScan Stand-Alone Software. R Package Version 0.3.9200, URL https://CRAN.R-project.org/package=rsatscan.
- Kulldorff M (1997). "A Spatial Scan Statistic." Communications in Statistics Theory and Methods, **26**(6), 1481–1496.
- McCullagh P, Nelder J (1989). Generalized Linear Models. 2nd edition. Chapman and Hall, London.
- Neuwirth E (2014). *RColorBrewer:* ColorBrewer Palettes. R Package Version 1.1-2, URL https://CRAN.R-project.org/package=RColorBrewer.
- Pebesma E (2012). "spacetime: Spatio-Temporal Data in R." Journal of Statistical Software, 51(1), 1-30. ISSN 1548-7660. doi:10.18637/jss.v051.i07. URL https://www.jstatsoft.org/index.php/jss/article/view/v051i07.
- Pebesma E, Bivand R (2005). "Classes and Methods for Spatial Data in R." R News, 5(2). URL https://cran.r-project.org/doc/Rnews/.
- R Core Team (2016). R: A Language and Environment for Statistical Computing. R Foundation for Statistical Computing, Vienna, Austria. URL https://www.R-project.org/.
- Ryan JA, Ulrich JM (2014). *xts:* eXtensible Time Series. R Package Version 0.9-7, URL https://CRAN.R-project.org/package=xts.
- Sarkar D, Andrews F (2016). *latticeExtra*: Extra Graphical Utilities Based on Lattice. R Package Version 0.6-28, URL https://CRAN.R-project.org/package=latticeExtra.
- Ugarte MD, Ibáñez B, Militino AF (2004). "Testing for Poisson Zero Inflation in Disease Mapping." *Biometrical Journal*, **46**(5), 526–539.
- Ugarte MD, Ibáñez B, Militino AF (2006). "Modelling Risks in Disease Mapping." Statistical Methods in Medical Research, 15, 21–35.
- Waller L, Turnbull B, Clark L, Nasca P (1992). "Chronic Disease Surveillance and Testing of Clustering of Disease and Exposure: Application to Leukemia Incidence in TCE-contamined Dumpsites in Upstate New York." Environmetrics, 3, 281–300.
- Waller LA, Gotway CA (2004). Applied Spatial Statistics for Public Health Data. John Wiley & Sons, Hoboken, New Jersey.
- Zeileis A, Kleiber C, Jackman S (2008). "Regression Models for Count Data in R." *Journal of Statistical Software*, **27**(1), 1–25. ISSN 1548-7660. doi:10.18637/jss.v027.i08. URL https://www.jstatsoft.org/index.php/jss/article/view/v027i08.

Zhang T, Lin G (2009). "Spatial Scan Statistics in Loglinear Models." Computational Statistics and Data Analysis, 53(8), 2851–2858.

#### **Affiliation:**

Virgilio Gómez-Rubio Department of Mathematics School of Industrial Engineering University of Castilla-La Mancha 02071 Albacete, Spain

E-mail: virgilio.gomez@uclm.es

URL: http://www.uclm.es/profesorado/vgomez

Paula Moraga
School of Mathematical Sciences
Queensland University of Technology
GPO Box 2434, Brisbane, QLD 4001, Australia
E-mail: paula.moragaserrano@qut.edu.au

URL: http://staff.qut.edu.au/staff/moragase/

John Molitor
College of Public Health and Human Sciences
Oregon State University
Corvallis, Oregon 97331, United States
E-mail: John.Molitor@oregonstate.edu

URL: http://health.oregonstate.edu/people/molitor-john

Barry Rowlingson
Lancaster Medical School
Furness Building
Lancaster University
Bailrigg, Lancaster LA1 4YG, United Kingdom
E-mail: b.rowlingson@lancaster.ac.uk

URL: http://www.lancaster.ac.uk/fhm/about-us/people/barry-rowlingson

Journal of Statistical Software published by the Foundation for Open Access Statistics MMMMMM YYYY, Volume VV, Issue II

MMMMMM YYYY, Volume VV, Issue II doi:10.18637/jss.v000.i00

http://www.foastat.org/ Submitted: yyyy-mm-dd Accepted: yyyy-mm-dd

http://www.jstatsoft.org/