



DClusterm: Model-based detection of disease clusters

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Abstract

The detection of regions with unusual high risk plays an important role in disease mapping and the analysis of Public Health data. In particular, the detection of groups of areas (i.e., clusters) where the risk is significantly high is often conducted by Public Health authorities.

Many methods have been proposed for the detection of disease clusters, most of them based on moving windows, such as, Kulldorff's Spatial Scan Statistics (SSS). Here we describe a model-based approach for the detection of disease clusters implemented in the **DClusterm** package. Our model-based approach is based on representing a large number of possible clusters by dummy variables and then fitting many generalized linear models to the data where these covariates are included one at a time. Cluster detection is done by performing a variable or model selection among all fitted models using different criteria.

Because of our model-based approach, cluster detection can be performed using different types of likelihoods and latent effects. We cover the detection of spatial and spatio-temporal clusters, as well as how to account for covariates, deal with zero-inflated datasets and overdispersion in the data.

Keywords: disease cluster, spatial statistics, R.

1. Introduction

**** SOME INTRO TEXT HERE ****

Kulldorff (1997) proposes a test for detecting disease clusters which will find the most likely cluster. This is called the Spatial Scan Statistic and the significance of the test is found via a Monte Carlo test. The test statistic is based on a likelihood ratio test for the following test:

$$\begin{aligned} H_0 : \theta_z &= \theta_{\bar{z}} \\ H_1 : \theta_z &> \theta_{\bar{z}} \end{aligned}$$

Here, z represents a cluster (i.e., a set of contiguous areas), θ_z the relative risk in the cluster and $\theta_{\bar{z}}$ the relative risk outside the cluster. Many different clusters are tested in turn. The most likely cluster is the one with the highest value of the test statistic. Then a Monte Carlo test is used to compute the p-value of the most likely cluster.

{sec:GLM}

2. Generalised Linear Models for cluster detection

Jung (2009); Zhang and Lin (2009) show that the test statistic for a given cluster is equivalent to fitting a Generalised Linear Model using a cluster variable as a predictor. This cluster variable is a dummy variable which is 1 for the areas in the cluster and 0 for the areas outside the cluster.

Firstly, given that we are using GLM's we could include covariates in the model. For example, for a Poisson model with expected counts E_i we could have:

$$O_i \sim Po(E_i \theta_i)$$

$$\log(\theta_i) = \log(E_i) + \alpha + \beta x_i$$

Fitting this model will provide estimates $\hat{\alpha}$ and $\hat{\beta}$. This will account for the (spatial) effects of the covariates. In order to include the cluster variable the effects of the covariates will be kept fixed. Hence, the clusters covariates will be used in a model with fixed coefficients for the covariates:

$$\log(\theta_i) = \log(E_i) + \hat{\alpha} + \hat{\beta} x_i + \gamma CLUSTER_i$$

This means that the offset now is $\log(E_i) + \hat{\alpha} + \hat{\beta} x_i$. γ is a measure of the difference of the risk in the cluster. We are only interested in cluster whose coefficient is higher than 0 (i.e., increased risk).

Testing different clusters will produce many different cluster covariates. We can use model selection techniques to select the most important cluster in the area. In particular, the log-likelihood can be used to compare the model with the cluster variable to the null model (i.e., the one with the covariates only). Note that we are interested in clusters with a high risk, so that

Bilancia and Demarinis (2014); Gómez-Rubio, Moraga, and Molitor (2015)

2.1. Leukemia in upstate New York

The NY8 dataset is available in package *DClusterm* and it provides cases of leukemia in different census tracts in upstate New York. This data set has been analysed by several authors (Waller, Turnbull, Clark, and Nasca 1992; Waller and Gotway 2004).

The location of leukemia is thought to be linked to the use of Trichloroethene (TCE) by several companies in the area. Figure 1 shows the Standardised Mortality Ratios of the census tracts and the locations of the industries using TCE.

In order to measure exposure, the inverse of the distance to the nearest TCE site has been used (PEXPOSURE). In addition, two other socioeconomic covariates have been used: the percentage of people aged 65 or more (PCTAGE65P) and the percentage of people who own their home (PCTOWNHOME).

```
> library(DClusterM)
> library(snowfall)
> library(xts)
> data(NY8)
> NY8$Cases2 <- round(NY8$Cases)
> NY8$Observed <- NY8$Cases2
> NY8$EXP <- NY8$POP8 * sum(NY8$Cases2)/sum(NY8$POP8)
> NY8$Expected <- NY8$EXP
> NY8$SMR <- NY8$Cases2/NY8$EXP
> NY8$x <- coordinates(NY8)[, 1]
> NY8$y <- coordinates(NY8)[, 2]
> NY8st <- STFDF(as(NY8, "SpatialPolygons"), xts(1, as.Date("1972-01-01")),
+   NY8@data, endTime = as.POSIXct(strptime(c("1972-01-01"),
+   "%Y-%m-%d"), tz = "GMT"))
```

2.2. Cluster detection

Cluster detection with no covariates

First of all, a model with no covariates will be fitted and used as a starting point.

```
> m0 <- glm(Cases2 ~ offset(log(EXP)) + 1, family = "poisson",
+   data = NY8)
> idxcl <- c(120, 12, 89, 139, 146)
> cl0 <- DetectClustersModel(NY8st, thegrid = as.data.frame(NY8)[idxcl,
+   c("x", "y")], fractpop = 0.15, alpha = 0.05, radius = Inf,
+   step = NULL, typeCluster = "S", R = NULL, numCPUS = 2, model0 = m0)
```

Below is a summary of the clusters detected with this method. The dates can be ignored as this is a purely spatial cluster.

```
> cl0
```

	x	y	size	minDateCluster	maxDateCluster	statistic
11	424728.9	4661404	39	1972-01-01 01:00:00	1972-01-01 01:00:00	8.044846
88	409430.4	4720092	9	1972-01-01 01:00:00	1972-01-01 01:00:00	6.967107
119	404710.7	4768346	24	1972-01-01 01:00:00	1972-01-01 01:00:00	3.254824
	pvalue	risk	cluster			
11	0.0000604120	0.3916904	TRUE			
88	0.0001893208	0.6455613	TRUE			
119	0.0107290781	0.4445236	TRUE			

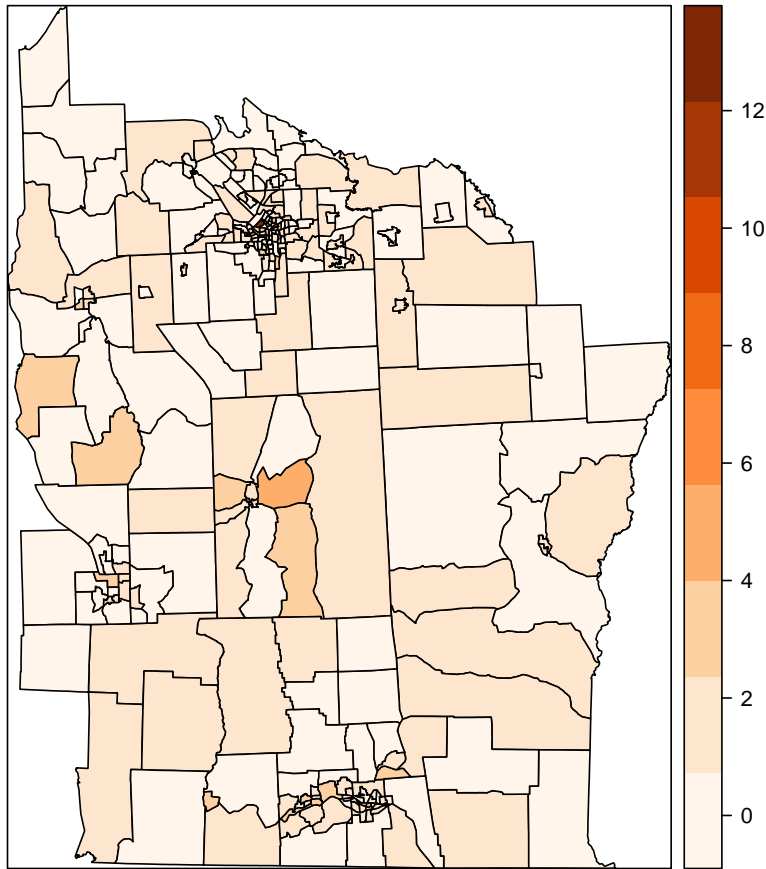


Figure 1: SMR of the incidence of Leukemia in upstate New York.

{fig:NYmap}

The centre of the clusters detected are shown in Figure 2.

Cluster detection after adjusting for covariates

Similarly, clusters can be detected after adjusting for significant risk factors. First we will fit a GLM with the 3 covariates mentioned earlier. As it can be seen, all three are significant:

```
> m1 <- glm(Cases2 ~ offset(log(EXP)) + PCTOWNHOME + PCTAGE65P +
+   PEXPOSURE, family = "poisson", data = NY8)
> summary(m1)
```

Call:

```
glm(formula = Cases2 ~ offset(log(EXP)) + PCTOWNHOME + PCTAGE65P +
    PEXPOSURE, family = "poisson", data = NY8)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.9099	-1.1294	-0.1768	0.6385	3.2426

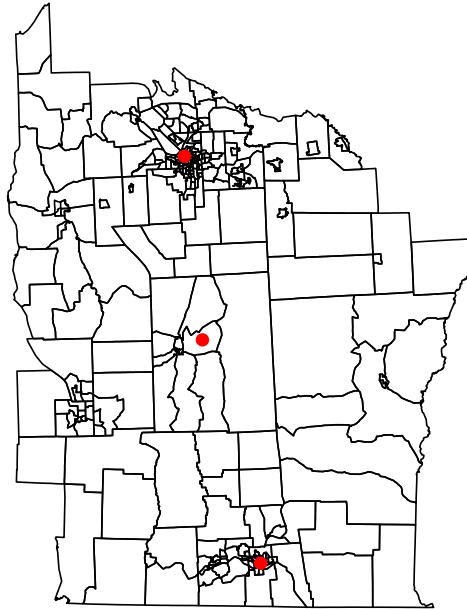


Figure 2: Clusters detected when no covariates are included in the model.

{fig:NYc10}

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)	
(Intercept)	-0.65507	0.18550	-3.531	0.000413	***
PCTOWNHOME	-0.36472	0.19316	-1.888	0.058998	.
PCTAGE65P	4.05031	0.60559	6.688	2.26e-11	***
PEXPOSURE	0.15141	0.03165	4.784	1.72e-06	***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 459.05 on 280 degrees of freedom
 Residual deviance: 384.01 on 277 degrees of freedom
 AIC: 958.97

Number of Fisher Scoring iterations: 5

The cluster detection method is run as before, but now we use the previous model instead:

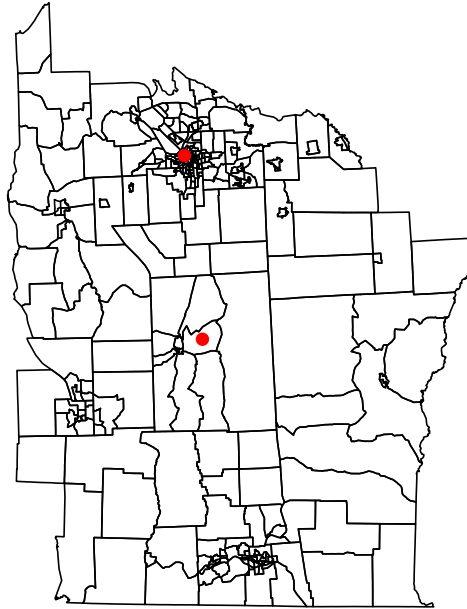
```
> cl1 <- DetectClustersModel(NY8st, thegrid = as.data.frame(NY8)[idxcl,
+   c("x", "y")], fractpop = 0.15, alpha = 0.05, typeCluster = "S",
+   R = NULL, numCPUS = 2, model0 = m1)
```

```
> cl1
```

	x	y	size	minDateCluster	maxDateCluster	statistic
88	409430.4	4720092	9	1972-01-01 01:00:00	1972-01-01 01:00:00	5.861204
119	404710.7	4768346	20	1972-01-01 01:00:00	1972-01-01 01:00:00	3.160591

	pvalue	risk	cluster
88	0.0006175202	0.5869176	TRUE
119	0.0119304026	0.4882633	TRUE

Figure 3 shows the clusters detected after adjusting for covariates.



{fig:NYc11}

Figure 3: Clusters detected after adjusting for covariates.

3. Spatio-temporal clusters

Jung (2009) discusses how to extend model-based approaches for the detection of spatial disease clusters to space and time. Gómez-Rubio *et al.* (2015) propose the following model:

$$\log(\mu_{i,t}) = \log(E_{i,t}) + \gamma_j c_{i,t}^{(j)} \quad (1)$$

where $\mu_{i,t}$ is the mean of area i at time t and $c_{i,t}^{(j)}$ a cluster dummy variable for cluster j .

3.1. Brain Cancer in New Mexico

The `brainNM` data set contains yearly cases of brain cancer in New Mexico from 1973 to 1991 (inclusive). The data set has been taken from the SatScan website and the area boundaries from the U.S. Census Bureau. In addition, the location of Los Alamos National Laboratory has been included (from the Wikipedia). Inverse distance to this site can be used to test for increased risk in the areas around the Laboratory as no other covariates are available.

```
> library(DClusterM)
> library(snowfall)
> data(brainNM)
```

Expected counts have been obtained using age and sex standardisation over the whole period of time. Hence, yearly differences are likely to be seen when plotting the data. The SMR's have been plotted in Figure 3.1.

3.2. Cluster detection

Cluster detection with no covariates

Similarly as in the spatial case, a GLM

```
> m0 <- glm(Observed ~ offset(log(Expected)) + 1, family = "poisson",
+          data = brainst@data)
> summary(m0)
```

Call:

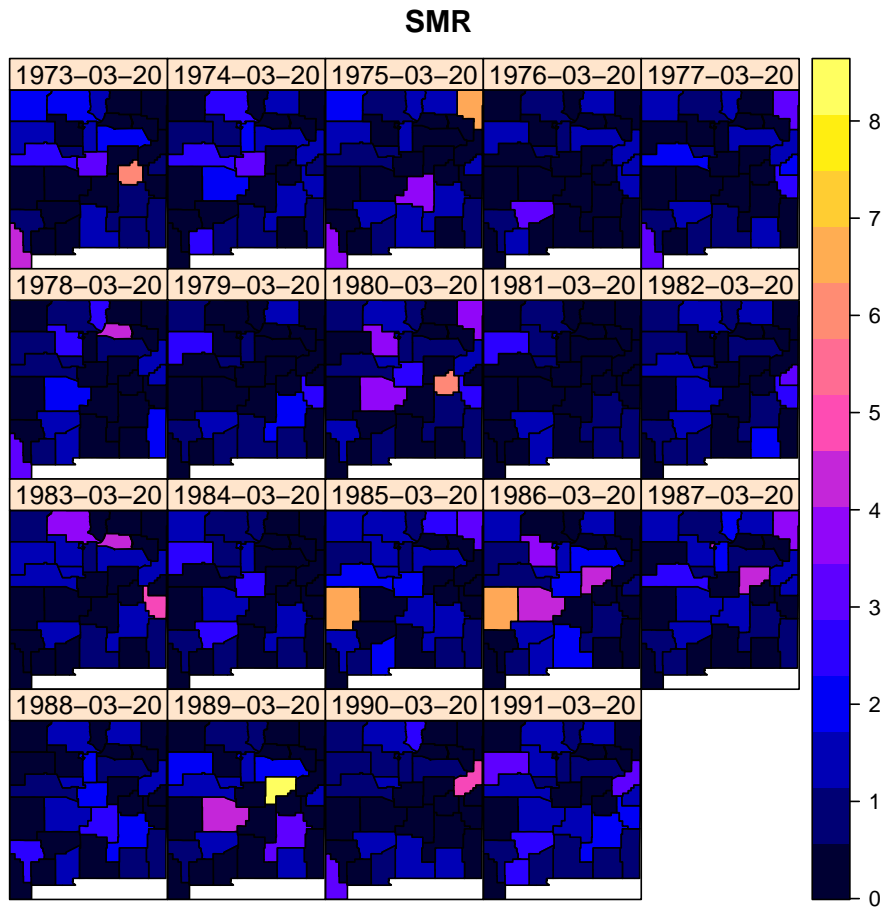
```
glm(formula = Observed ~ offset(log(Expected)) + 1, family = "poisson",
    data = brainst@data)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.4874	-0.9998	-0.4339	0.3773	3.1321

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	2.761e-16	2.917e-02	0	1



{fig:NMSMR}

Figure 4: SMR of brain cancer in New Mexico.

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 631.64 on 607 degrees of freedom
 Residual deviance: 631.64 on 607 degrees of freedom
 AIC: 1585.6

Number of Fisher Scoring iterations: 5

```
> cl0 <- DetectClustersModel(brainst, coordinates(brainst@sp),
+   minDateUser = "1985-01-01", maxDateUser = "1989-01-01", fractpop = 0.15,
+   alpha = 0.05, typeCluster = "ST", R = NULL, numCPUS = 2,
+   model0 = m0)
```

```
> nrow(cl0)
```

```
[1] 180
```

```
> cl0[1:5, ]
```


	x	y	size	minDateCluster		maxDateCluster		statistic
0286	-106.3073	35.86930	3	1986-03-20	01:00:00	1988-03-20	01:00:00	7.493492
0496	-105.9761	35.50684	2	1986-03-20	01:00:00	1988-03-20	01:00:00	6.438221
0531	-106.9303	34.00725	9	1985-03-20	01:00:00	1986-03-20	01:00:00	6.378992
0498	-105.9761	35.50684	2	1987-03-20	01:00:00	1988-03-20	01:00:00	6.331113
0288	-106.3073	35.86930	2	1987-03-20	01:00:00	1988-03-20	01:00:00	6.331113

	pvalue	risk	cluster
0286	0.0001082553	0.6814588	TRUE
0496	0.0003327442	0.6970405	TRUE
0531	0.0003544929	0.3838756	TRUE
0498	0.0003731179	0.8070901	TRUE
0288	0.0003731179	0.8070901	TRUE

Cluster detection after adjusting for covariates

We will use the inverse of the distance to Los Alamos National Laboratory as a covariate.

```
> dst <- spDistsN1(coordinates(brainst@sp), losalamos, TRUE)
> nyears <- length(unique(brainst@data$Year))
> brainst@data$IDLANL <- rep(1/dst, nyears)

> m1 <- glm(Observed ~ offset(log(Expected)) + IDLANL, family = "poisson",
+ data = brainst)
> summary(m1)
```

Call:

```
glm(formula = Observed ~ offset(log(Expected)) + IDLANL, family = "poisson",
    data = brainst)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.4832	-0.9982	-0.4280	0.3775	3.1424

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-0.005721	0.029897	-0.191	0.848
IDLANL	0.338194	0.364900	0.927	0.354

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 631.64 on 607 degrees of freedom
 Residual deviance: 630.84 on 606 degrees of freedom
 AIC: 1586.8

Number of Fisher Scoring iterations: 5

```

> cl1 <- DetectClustersModel(brainst, coordinates(brainst@sp),
+   fractpop = 0.15, alpha = 0.05, minDateUser = "1988-01-01",
+   maxDateUser = "1989-01-01", typeCluster = "ST", R = NULL,
+   numCPUS = 2, model0 = m1)

> nrow(cl1)

[1] 6

> cl1[1:5, ]

```

	x	y	size	minDateCluster	maxDateCluster	statistic
049	-105.9761	35.50684	2	1988-03-20 01:00:00	1988-03-20 01:00:00	2.433451
028	-106.3073	35.86930	2	1988-03-20 01:00:00	1988-03-20 01:00:00	2.433451
057	-105.8508	34.64048	2	1988-03-20 01:00:00	1988-03-20 01:00:00	2.431998
013	-106.8328	32.35265	17	1988-03-20 01:00:00	1988-03-20 01:00:00	2.010047
027	-105.4592	33.74524	3	1988-03-20 01:00:00	1988-03-20 01:00:00	2.007057

	pvalue	risk	cluster
049	0.02737662	0.7122467	TRUE
028	0.02737662	0.7122467	TRUE
057	0.02742274	0.7475794	TRUE
013	0.04496121	0.2594413	TRUE
027	0.04512090	0.7512120	TRUE

We can easily display the most significant cluster as follows:

```

> stcl <- get.stclusters(brainst, cl0)
> brainst$CLUSTER <- 0
> brainst$CLUSTER[stcl[[1]]] <- 1

```

4. Zero-inflated models for cluster detection

[sec:zeroinfl]

Gómez-Rubio and López-Quílez (2010) extend this method to account for zero-inflation. In this case the observed number of cases come from a mixture distribution:

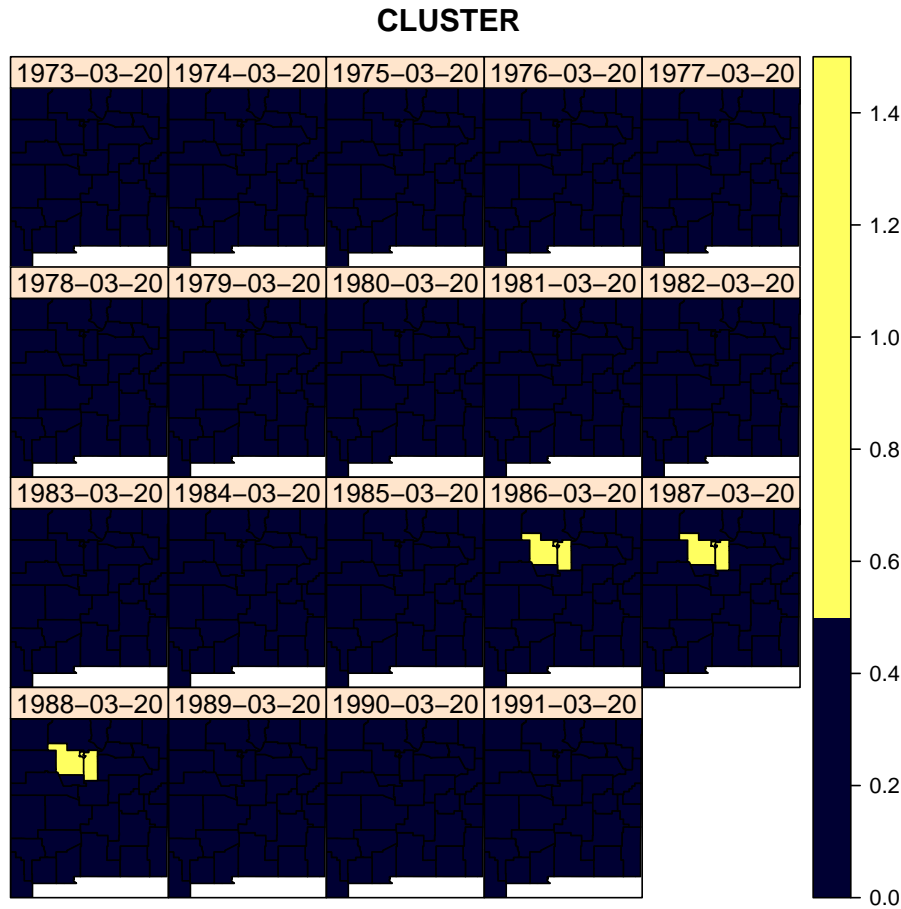
$$Pr(O_i = n_i) = \begin{cases} \pi_i + (1 - \pi_i)Po(0|\theta_i E_i) & n_i = 0 \\ (1 - \pi_i)Po(n_i|\theta_i E_i) & n_i = 1, 2, \dots \end{cases}$$

The relative risk θ_i can be modelled using a log-linear model to depend on some relevant risk factors. Also, it is common that all π_i 's are taken equal to a single value π .

4.1. Brain Cancer in Navarre (Spain)

Ugarte, Ibáñez, and Militino (2006) analyse the incidence of brain cancer in Navarre (Spain). The aggregation level is the health district. Figure 4.1 shows the SMR. As it can be seen there are many areas where the SMR is zero because there are no cases in those areas. Ugarte,

```
> print(stplot(brainst[, , "CLUSTER"], at = c(0, 0.5, 1.5)))
```



```
Fig:NMcluster}
```

Figure 5: Spatio-temporal cluster of brain cancer detected in New Mexico.

Ibáñez, and Militino (2004) also tested for positive zero-inflation of these data compared to a Poisson distribution. The method implemented in this package is similar to the one used in Gómez-Rubio and López-Quílez (2010) for the detection of disease clusters of rare diseases.

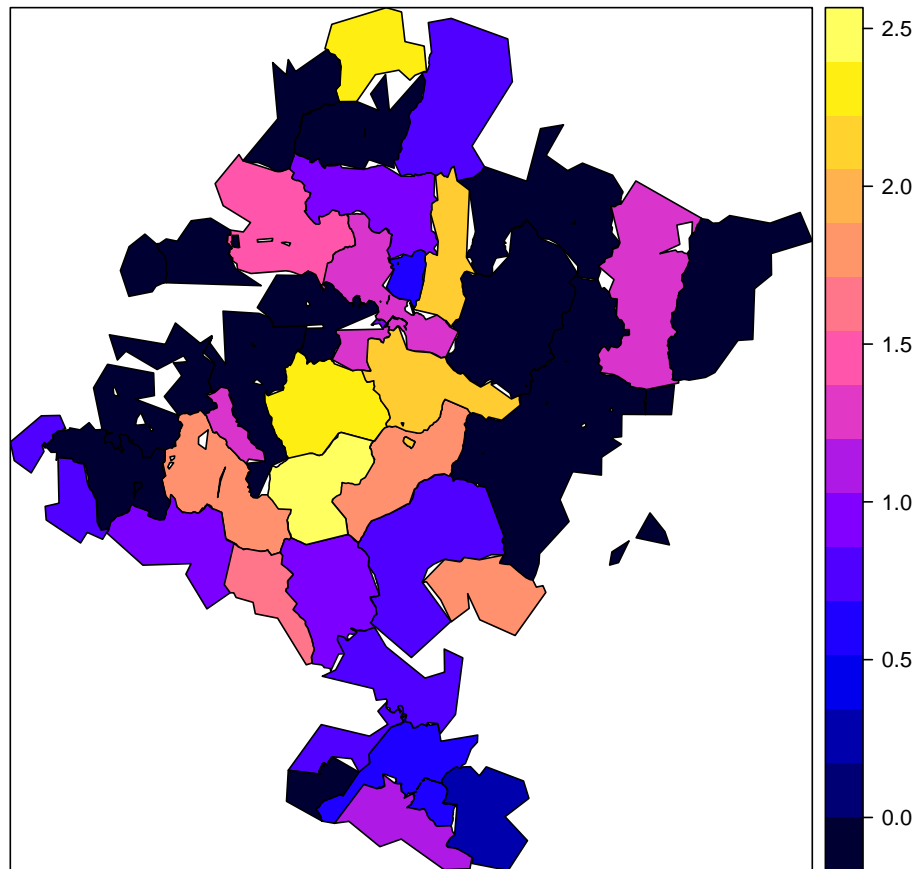
4.2. Cluster detection

Cluster detection with no covariates

Before starting our cluster detection methods, we will check the appropriateness of a Poisson GLM for this data. Fitting a log-linear model (with no covariates) gives the following model:

```
> m0 <- glm(OBSERVED ~ offset(log(EXPECTED)) + 1, family = "poisson",
+ data = brainnav)
> summary(m0)
```

Call:



{fig:Navarre}

Figure 6: SMR of brain cancer in Navarre (Spain).

```
glm(formula = OBSERVED ~ offset(log(EXPECTED)) + 1, family = "poisson",
     data = brainnav)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.5227	-1.4783	-0.3203	0.7042	1.6393

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-7.752e-06	8.805e-02	0	1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 63.733 on 39 degrees of freedom
 Residual deviance: 63.733 on 39 degrees of freedom
 AIC: 145.02

Number of Fisher Scoring iterations: 5

Furthermore, a quasipoisson model has been fit in order to asses any extra-variation in the data:

```
> m0q <- glm(OBSERVED ~ offset(log(EXPECTED)) + 1, family = "quasipoisson",
+ data = brainnav)
> summary(m0q)
```

Call:

```
glm(formula = OBSERVED ~ offset(log(EXPECTED)) + 1, family = "quasipoisson",
    data = brainnav)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-2.5227	-1.4783	-0.3203	0.7042	1.6393

Coefficients:

	Estimate	Std. Error	t value	Pr(> t)
(Intercept)	-7.752e-06	9.703e-02	0	1

(Dispersion parameter for quasipoisson family taken to be 1.214555)

Null deviance: 63.733 on 39 degrees of freedom
 Residual deviance: 63.733 on 39 degrees of freedom
 AIC: NA

Number of Fisher Scoring iterations: 5

The dispersion parameter in the previous model seems to be higher than 1, which may mean that the Poisson distribution is not appropriate.

For this reason, and following [Ugarte *et al.* \(2004\)](#), a zero-inflated Poisson model has been fit. Here is the resulting model:

```
> m0zip <- zeroinfl(OBSERVED ~ offset(log(EXPECTED)) + 1 | 1, data = brainnav,
+ dist = "poisson", x = TRUE)
> summary(m0zip)
```

Call:

```
zeroinfl(formula = OBSERVED ~ offset(log(EXPECTED)) + 1 | 1, data = brainnav,
    dist = "poisson", x = TRUE)
```

Pearson residuals:

Min	1Q	Median	3Q	Max
-1.3585	-0.9137	-0.1378	0.7137	1.8091

```

Count model coefficients (poisson with log link):
      Estimate Std. Error z value Pr(>|z|)
(Intercept)  0.09347    0.09459   0.988   0.323

Zero-inflation model coefficients (binomial with logit link):
      Estimate Std. Error z value Pr(>|z|)
(Intercept) -1.6158     0.6435 -2.511   0.012 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Number of iterations in BFGS optimization: 9
Log-likelihood: -69.08 on 2 Df

```

Hence, the zero-inflated Poisson model will be used now to detect clusters of disease:

```

> brainnav$Expected <- brainnav$EXPECTED
> brainnavst <- STFDF(as(brainnav, "SpatialPolygons"), xts(1, as.Date("1990-01-01")),
+   brainnav@data, endTime = as.POSIXct(strptime(c("1990-01-01"),
+     "%Y-%m-%d"), tz = "GMT"))
> c10 <- DetectClustersModel(brainnavst, coordinates(brainnav),
+   fractpop = 0.25, alpha = 0.05, typeCluster = "S", R = NULL,
+   numCPUS = 2, model0 = m0zip)

```

```

Library spdep loaded.
Library splancs loaded.
Library spacetime loaded.
Library DCluster loaded.
Library pscl loaded.
Library INLA loaded.
Library DClusterm loaded.
[1] 1 1

```

```
> c10
```

	x	y	size	minDateCluster	maxDateCluster	statistic
31	596886.8	4710520	4	1990-01-01 01:00:00	1990-01-01 01:00:00	2.520091
30	611795.5	4713762	3	1990-01-01 01:00:00	1990-01-01 01:00:00	2.016942
	pvalue	risk	cluster			
31	0.02476587	0.5987255	TRUE			
30	0.04459518	0.6139100	TRUE			

As it can be seen, two clusters (with a p-value lower than 0.05) are detected. However, they overlap and we will just consider the one with the lowest p-value, which is shown in [Figure 4.2.1](#)

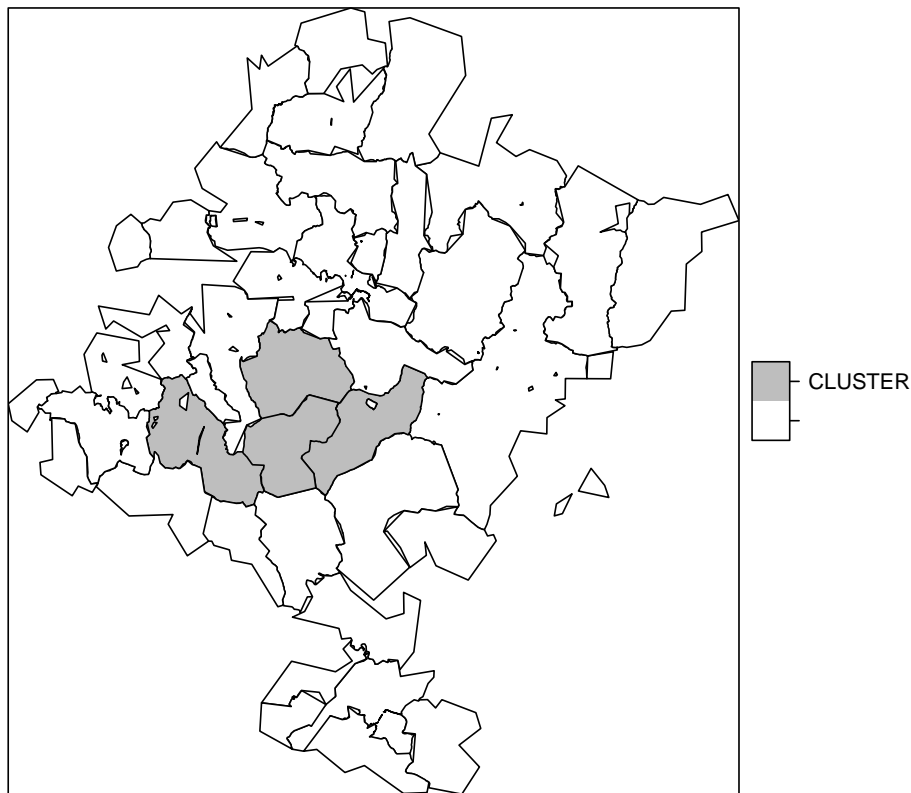
```

> names(c10)[3] <- "size"
> knbinary(brainnav, c10)

```

	CL1	CL2
1	0	0
2	0	0
3	0	0
4	0	0
5	0	0
6	0	0
7	0	0
8	0	0
9	0	0
10	0	0
11	0	0
12	0	0
13	0	0
14	0	0
15	0	0
16	0	0
17	1	0
18	0	1
19	0	0
20	0	0
21	0	0
22	0	0
23	0	0
24	1	0
25	0	0
26	0	0
27	0	0
28	0	0
29	0	0
30	1	1
31	1	1
32	0	0
33	0	0
34	0	0
35	0	0
36	0	0
37	0	0
38	0	0
39	0	0
40	0	0

```
> brainnav$CLUSTER <- as.factor(knbinary(brainnav, c10)[, 1])  
> levels(brainnav$CLUSTER) <- c("", "CLUSTER")
```



{fig:Navarre}

Figure 7: Cluster of brain cancer detected in Navarre (Spain).

5. Mixed-effects models for cluster detection

{sec:mixed}

6. Bivariate models for cluster detection

{sec:bivar}

7. Discussion

{sec:disc}

References

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