

Tutorial for the **dcglm** package

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Abstract

This tutorial package demonstrates the capabilities of data cloning algorithm via the infrastructure provided by the **dclone** package. The functions developed here reproduce main features of the **glm** base function in R by using data cloning.

Keywords: Bayesian statistics, data cloning, maximum likelihood inference, generalized linear models, R.

1. Introduction

Data cloning is a statistical computing method introduced by [Lele *et al.* \(2007\)](#). It exploits the computational simplicity of the Markov chain Monte Carlo (MCMC) algorithms used in the Bayesian statistical framework, but it provides valid frequentist inferences such as the maximum likelihood estimates and their standard errors for complex hierarchical models. The use of the data cloning algorithm is especially straightforward for complex models, where the number of unknowns increases with sample size (i.e. mixed models), because inference and prediction procedures are often hard to implement in such situations.

The **dclone** R package ([Sólymos 2009](#)) aims to provide low level functionality to easily implement more specific higher level procedures based on data cloning for users familiar with the Bayesian methodology. This tutorial, we develop high level functions to reproduce the **glm** base function of R by using the data cloning algorithm building on the infrastructure of the **dclone** package.

2. Data generation

We generate random data for Poisson and Binomial GLMs. First we define the number of locations (**n**) and the independent covariate (**x**). **X** represents the design matrix:

```
R> library(dclone)
R> set.seed(1234)
R> n <- 20
R> x <- runif(n, -1, 1)
R> X <- model.matrix(~x)
```

Parameters (**beta1**), linear predictor (**mu1**) and random response (**Y1**) for the Poisson case (log link function):

```
R> beta1 <- c(2, -1)
```

```
R> mu1 <- X %*% beta1
R> Y1 <- rpois(n, exp(mu1))
```

Parameters (**beta2**), linear predictor (**mu2**) and random response (**Y2**) for the Binomial (Bernoulli) case (logistic link function):

```
R> beta2 <- c(0, -1)
R> mu2 <- X %*% beta2
R> Y2 <- rbinom(n, 1, exp(mu2) / (1 + exp(mu2)))
```

3. GLM based on the glm function

Now we fit the Poisson and Binomial GLM by using the `glm` base function and inspect their summaries:

```
R> m1 <- glm(Y1 ~ x, family=poisson)
R> summary(m1)
```

Call:

```
glm(formula = Y1 ~ x, family = poisson)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.6336	-0.8138	-0.2134	0.5154	2.0309

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	1.94162	0.09482	20.478	< 2e-16 ***
x	-1.27648	0.16017	-7.969	1.60e-15 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 90.897 on 19 degrees of freedom
 Residual deviance: 19.060 on 18 degrees of freedom
 AIC: 99.543

Number of Fisher Scoring iterations: 4

```
R> m2 <- glm(Y2 ~ x, family=binomial)
R> summary(m2)
```

Call:

```
glm(formula = Y2 ~ x, family = binomial)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.7850	-0.8787	-0.5794	1.0077	1.5424

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
--	----------	------------	---------	----------

```

(Intercept)  -0.3388      0.5021  -0.675   0.500
x             -1.7377      1.0186  -1.706   0.088 .
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 27.526  on 19  degrees of freedom
Residual deviance: 24.097  on 18  degrees of freedom
AIC: 28.097

Number of Fisher Scoring iterations: 4

```

4. The full Bayesian model for GLM and data cloning

Here is the JAGS model for the Poisson case, with flat Normal priors for the regression coefficients:

```

R> glm.pois <- function() {
+   for (i in 1:n) {
+     Y[i] ~ dpois(lambda[i])
+     log(lambda[i]) <- inprod(X[i,], beta[1,])
+   }
+   for (j in 1:np) {
+     beta[1,j] ~ dnorm(0, 0.001)
+   }
+ }

```

The data will be represented as a list (if we want to use data cloning consistently, we have to use the list format instead of the global environment):

```

R> dat1 <- list(n = length(Y1), Y = Y1, X = X, np = ncol(X))
R> str(dat1)

```

```

List of 4
 $ n : int 20
 $ Y : num [1:20] 14 3 2 4 5 6 25 22 3 9 ...
 $ X : num [1:20, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
 .. attr(*, "dimnames")=List of 2
 .. ..$ : chr [1:20] "1" "2" "3" "4" ...
 .. ..$ : chr [1:2] "(Intercept)" "x"
 .. attr(*, "assign")= int [1:2] 0 1
 $ np: int 2

```

Now let's clone the data set (note that `n` should be multiplied, while `np` must remain unchanged):

```

R> n.clones <- 5
R> dcdat1 <- dclone(dat1, n.clones, multiply = "n", unchanged = "np")
R> str(dcdat1)

```

```

List of 4
 $ n : atomic [1:1] 100

```

```

..- attr(*, "n.clones")= atomic [1:1] 5
.. ..- attr(*, "method")= chr "multi"
$ Y : atomic [1:100] 14 3 2 4 5 6 25 22 3 9 ...
..- attr(*, "n.clones")= atomic [1:1] 5
.. ..- attr(*, "method")= chr "rep"
$ X : num [1:100, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
..- attr(*, "dimnames")=List of 2
.. ..$ : chr [1:100] "1_1" "2_1" "3_1" "4_1" ...
.. ..$ : chr [1:2] "(Intercept)" "x"
..- attr(*, "n.clones")= atomic [1:1] 5
.. ..- attr(*, "method")= chr "rep"
$ np: int 2

```

To fit the model to the data with data cloning is as easy as this:

```
R> mod1 <- jags.fit(dcdat1, "beta", glm.pois)
```

```
R> summary(mod1)
```

```

Iterations = 1001:6000
Thinning interval = 1
Number of chains = 3
Sample size per chain = 5000
Number of clones = 5

```

1. Empirical mean and standard deviation for each variable,
plus standard error of the mean:

	Mean	SD	DC SD	Naive SE	Time-series SE	R hat
beta[1]	1.940	0.04185	0.09357	0.0003417	0.0006906	1.002
beta[2]	-1.278	0.07105	0.15886	0.0005801	0.0011818	1.002

2. Quantiles for each variable:

	2.5%	25%	50%	75%	97.5%
beta[1]	1.857	1.912	1.940	1.969	2.020
beta[2]	-1.418	-1.326	-1.278	-1.230	-1.140

Let's compare this `mcmc.list` (more accurately an `mcmc.list.dc`) object with the `glm` results:

```

R> cbind(true.values=beta1,
+        glm.estimates=coef(m1), glm.se=summary(m1)$coefficients[,2],
+        dc.estimates=coef(mod1), dc.se=dcsd(mod1))

```

	true.values	glm.estimates	glm.se	dc.estimates	dc.se
(Intercept)	2	1.941624	0.09481704	1.939911	0.0935704
x	-1	-1.276479	0.16017431	-1.277835	0.1588650

Here is the JAGS model for the Binomial (Bernoulli, because only one trial) case:

```

R> glm.bin <- function() {
+   for (i in 1:n) {
+     Y[i] ~ dbin(p[i], k)
+     logit(p[i]) <- inprod(X[i,], beta[1,])
+   }
+ }

```

```

+      }
+      for (j in 1:np) {
+        beta[1,j] ~ dnorm(0, 0.001)
+      }
+    }

```

Putting together the data set is similar to the Poisson case:

```

R> dat2 <- list(n = length(Y2), Y = Y2, k = 1, X = X, np = ncol(X))
R> str(dat2)

```

```

List of 5
 $ n : int 20
 $ Y : num [1:20] 1 0 0 1 0 1 0 1 0 0 ...
 $ k : num 1
 $ X : num [1:20, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
  ..- attr(*, "dimnames")=List of 2
  .. ..$ : chr [1:20] "1" "2" "3" "4" ...
  .. ..$ : chr [1:2] "(Intercept)" "x"
  ..- attr(*, "assign")= int [1:2] 0 1
 $ np: int 2

```

but data cloning setup is a bit different. We don't have to repeat the data vectors or columns in the design matrix `n.clones` times, because there is an easier way. We multiply `Y` and `k` with `n.clones` and leave the other elements unchanged:

```

R> dcdat2 <- dclone(dat2, n.clones, multiply = c("Y", "k"), unchanged = c("n", "np", "X"))
R> str(dcdat2)

```

```

List of 5
 $ n : int 20
 $ Y : atomic [1:20] 5 0 0 5 0 5 0 5 0 0 ...
  ..- attr(*, "n.clones")= atomic [1:1] 5
  .. ..- attr(*, "method")= chr "multi"
 $ k : atomic [1:1] 5
  ..- attr(*, "n.clones")= atomic [1:1] 5
  .. ..- attr(*, "method")= chr "multi"
 $ X : num [1:20, 1:2] 1 1 1 1 1 1 1 1 1 1 ...
  ..- attr(*, "dimnames")=List of 2
  .. ..$ : chr [1:20] "1" "2" "3" "4" ...
  .. ..$ : chr [1:2] "(Intercept)" "x"
  ..- attr(*, "assign")= int [1:2] 0 1
 $ np: int 2

```

Now fit the model to the data with data cloning:

```

R> mod2 <- jags.fit(dcdat2, "beta", glm.bin)

R> summary(mod2)

```

```

Iterations = 1001:6000
Thinning interval = 1
Number of chains = 3
Sample size per chain = 5000

```

Number of clones = 5

1. Empirical mean and standard deviation for each variable,
plus standard error of the mean:

	Mean	SD	DC SD	Naive SE	Time-series SE	R hat
beta[1]	-0.3442	0.2241	0.5012	0.001830	0.002424	1.000
beta[2]	-1.7853	0.4560	1.0196	0.003723	0.005041	1.000

2. Quantiles for each variable:

	2.5%	25%	50%	75%	97.5%
beta[1]	-0.7931	-0.4941	-0.3416	-0.1884	0.08299
beta[2]	-2.7199	-2.0783	-1.7706	-1.4731	-0.92225

and compare results with `glm` results:

```
R> cbind(true.values=beta2,
+        glm.estimates=coef(m2), glm.se=summary(m2)$coefficients[,2],
+        dc.estimates=coef(mod2), dc.se=dcstd(mod2))
```

	true.values	glm.estimates	glm.se	dc.estimates	dc.se
(Intercept)	0	-0.3388286	0.5020926	-0.3442398	0.5012107
x	-1	-1.7377202	1.0185540	-1.7853345	1.0196158

5. The 'custommodel' function

The `custommodel` function enables us to reuse the same JAGS model with minor modifications. For example we combine the above Poisson and Binomial model into one.

```
R> glm.model <- function() {
+   for (i in 1:n) {
+     Y[i] ~ dpois(lambda[i])
+     Y[i] ~ dbin(p[i], k)
+     log(lambda[i]) <- inprod(X[i,], beta[1,])
+     logit(p[i]) <- inprod(X[i,], beta[1,])
+   }
+   for (j in 1:np) {
+     beta[1,j] ~ dnorm(0, 0.001)
+   }
+ }
```

If we want to use this in the `jags.fit` function, it would give the error message about the attempt to define the nodes more than once. To avoid this, we tell the function which line(s) should be excluded:

```
R> custommodel(glm.model, c(4,6))
```

```
[1] "model {"
[2] "   for (i in 1:n) {"
[3] "       Y[i] ~ dpois(lambda[i])"
[4] "       log(lambda[i]) <- inprod(X[i,], beta[1,])"
```

```

[5] "    }"
[6] "    for (j in 1:np) {"
[7] "        beta[1,j] ~ dnorm(0, 0.001)"
[8] "    }"
[9] "}"
attr(,"class")
[1] "custommodel"

R> custommodel(glm.model, c(3,5))

[1] "model {"
[2] "    for (i in 1:n) {"
[3] "        Y[i] ~ dbin(p[i], k)"
[4] "        logit(p[i]) <- inprod(X[i,], beta[1,])"
[5] "    }"
[6] "    for (j in 1:np) {"
[7] "        beta[1,j] ~ dnorm(0, 0.001)"
[8] "    }"
[9] "}"
attr(,"class")
[1] "custommodel"

```

so eventually we get back our original models. But these are not functions, but character vectors of the class ‘custommodel’. `jags.fit` will recognize this.

Why do we want to complicate our lives with the `custommodel`? Because `dpois`, `dbin`, and `inprod` are not recognised as valid R objects or functions. This is, however, a requisite of building a valid R package that that passes R CMD check. A way to overcome this is to define fake objects as e.g. `inprod <- function() NULL`, but this option should be regarded as ugly and inefficient (unnecessary) as compared to a clean `custommodel` approach that will be presented in the next section.

6. The main function `dcglm`

Here is our main function for the data cloning based estimating procedure for the Poisson and Binomial GLMs:

```

R> dcglm <-
+   function(formula, data = parent.frame(),
+   family=c("poisson", "binomial"), n.clones=5, ...)
+   {
+       glm.model <- c("model {",
+       "    for (i in 1:n) {",
+       "        Y[i] ~ dpois(lambda[i])",
+       "        Y[i] ~ dbin(p[i], k)",
+       "        log(lambda[i]) <- inprod(X[i,], beta[1,])",
+       "        logit(p[i]) <- inprod(X[i,], beta[1,])",
+       "    }",
+       "    for (j in 1:np) {",
+       "        beta[1,j] ~ dnorm(0, 0.001)",
+       "    }",
+       "}")
+   }

```

```

+   family <- match.arg(family)
+   lhs <- formula[[2]]
+   formula.orig <- formula
+   Y <- eval(lhs, data)
+   formula[[2]] <- NULL
+   rhs <- model.frame(formula, data)
+   X <- model.matrix(attr(rhs, "terms"), rhs)
+   if (family == "poisson") {
+     dat <- list(n = length(Y), Y = Y, X = X, np = ncol(X))
+     dcdat <- dclone(dat, n.clones, multiply = "n", unchanged = "np")
+     model <- dclone:::custommodel(glm.model, c(4,6))
+   } else {
+     dat <- list(n = length(Y), Y = Y, X = X, np = ncol(X), k = 1)
+     dcdat <- dclone(dat, n.clones, multiply = c("Y","k"), unchanged = c("n", "np", "X"))
+     model <- dclone:::custommodel(glm.model, c(3,5))
+   }
+   mod <- jags.fit(dcdat, "beta", model, ...)
+   COEF <- coef(mod)
+   SE <- dcsd(mod)
+   names(COEF) <- names(SE) <- colnames(X)
+   mu <- X %*% COEF
+   if (family == "poisson") {
+     fitval <- drop(exp(mu))
+     ll <- sum(dpois(Y, fitval, log=TRUE))
+   } else {
+     fitval <- drop(exp(mu) / (1 + exp(mu)))
+     ll <- sum(dbinom(Y, 1, fitval, log=TRUE))
+   }
+   rval <- list(call=match.call(),
+     mcmc = mod,
+     y = Y,
+     x = rhs,
+     model = X,
+     fitted.values = fitval,
+     linear.predictors = mu,
+     formula = formula.orig,
+     coefficients = COEF,
+     std.error = SE,
+     loglik = ll,
+     family = family,
+     df.residual = length(Y) - length(COEF),
+     df.null = length(Y) - 1)
+   class(rval) <- c("dcglm")
+   rval
+ }

```

Let's go through this function step-by-step as pseudo-code:

1. `glm.model` is the `custommodel` version of the BUGS model, unifying the Poisson and Binomial cases, as we have seen before.
2. The `family` argument is recognized, and as a result, it can be given not only in full (e.g. `family = "p"` is equivalent of `family = "poisson"`).

3. **lhs** is the left-hand-side of the formula, **Y** is the value as a result of evaluating **lhs** in **data** (that is the parent frame, which is usually the global environment if not called from inside of a function).
4. **formula[[2]] <- NULL** removes the left-hand-side from the formula (that's why we keep a copy of it named as **formula.orig**).
5. **rhs** is the right-hand-side, that is a model frame with variables defined in **data**.
6. The design matrix **X** is a result of using the "**terms**" attribute of **rhs** and evaluated in **rhs**.
7. The the Bayesian (**dat**) and data cloned (**dcdat**) data representation, and **model** depends on the **family** argument.
8. **mod** is the fitted **mcmc.list** object. Dots (...) represents all the additional arguments that can be passed, including **n.update**, **n.iter**, and **n.chains**.
9. **COEF** is the **coef** method evaluated on the **mcmc.list** object **mod**. **SD** is the data cloned standard error (scaled by \sqrt{k}). Names of **COEF** and **SD** follow column names of **X**.
10. **mu** is the linear predictor (on log/logit scale), while **fitval** is the fitted value (response scale after using the appropriate inverse link function) and **ll** is the log-likelihood calculated from the probability mass function.
11. **rval** is the return value, that is a list with elements commonly applied in objects representing model fit (cf. for example element names with **names(m1)**):

call the function call,

mcmc the fitted **mcmc.list** object,

y the response,

x the model frame (right-hand-side),

model the design matrix,

fitted.values fitted values,

linear.predictors linear predictors,

formula the formula argument of the call,

coefficients means of the joint posterior distribution (maximum likelihood estimates),

std.error standard errors of the MLE,

loglik log-likelihood,

family family argument of the call,

df.residual residual degrees of freedom,

df.null degrees of freedom in the null model.

12. Finally, we attach the class attribute and return **rval**.

Fun, isn't it? See if it is actually working:

```
R> dcm1 <- dcglm(Y1 ~ x)
R> dcm2 <- dcglm(Y2 ~ x, family = "binomial")
```

If we are about to inspect these objects, well, it is a mess without some additional helper functions. The most basic such functions (called methods in R jargon) are `print` and `summary`. For our convenience, we also define some other methods, too. These are based on the so called S3 method dispatch system. That is, if a generic function is defined, we can add class specific methods to it.

In our case, the most simple methods are the `coef` and `fitted`, because these only extract an element from the objects¹:

```
R> coef.dcglm <- function(object, ...) object$coefficients
R> fitted.dcglm <- function(object, ...) object$fitted.values
```

Compare with the `glm` results:

```
R> rbind(glm=coef(m1), dcglm=coef(dcm1))
```

	(Intercept)	x
glm	1.941624	-1.276479
dcglm	1.939725	-1.277473

```
R> rbind(glm=coef(m2), dcglm=coef(dcm2))
```

	(Intercept)	x
glm	-0.3388286	-1.737720
dcglm	-0.3508279	-1.790707

```
R> rbind(glm=fitted(m1), dcglm=fitted(dcm1))
```

	1	2	3	4	5	6	7
glm	18.68691	5.100808	5.273269	5.086763	2.773811	4.871574	24.38239
dcglm	18.66579	5.089894	5.262122	5.075869	2.766564	4.860977	24.35987
	8	9	10	11	12	13	14
glm	13.79645	4.561353	6.721032	4.252018	6.214003	12.13746	2.364617
dcglm	13.77761	4.551198	6.708092	4.242320	6.201661	12.11967	2.358146
	15	16	17	18	19	20	
glm	11.84414	2.946219	12.02980	12.64069	15.50880	13.80789	
dcglm	11.82655	2.938659	12.01209	12.62256	15.48903	13.78904	

```
R> rbind(glm=fitted(m2), dcglm=fitted(dcm2))
```

	1	2	3	4	5	6	7
glm	0.7317898	0.3178060	0.3276999	0.3169928	0.1689386	0.3043920	0.7967153
dcglm	0.7374313	0.3124194	0.3225263	0.3115891	0.1620009	0.2987331	0.8031138
	8	9	10	11	12	13	14
glm	0.6435203	0.2857649	0.4041127	0.2666583	0.3786844	0.6025899	0.1405842
dcglm	0.6472606	0.2797620	0.4008638	0.2603484	0.3747479	0.6052271	0.1338523
	15	16	17	18	19	20	
glm	0.5945881	0.1807789	0.5996819	0.6157557	0.6791673	0.643779	
dcglm	0.5969987	0.1738156	0.6022371	0.6187588	0.6837690	0.647526	

¹Note that these are identical to the `coef.default` and `fitted.default` functions, but shown here for didactic purposes.

For the `logLik` method, it is necessary to follow the standard rules, because AIC calculations depend on this method (this means, that we don't have to define a method for AIC if the `logLik` method exists for a class):

```
R> logLik.dcgmlm <- function (object, ...)
+   structure(object$loglik,
+             df = object$df.null + 1 - object$df.residual,
+             nobs = object$df.null + 1,
+             class = "logLik")
```

Compare with the `glm` results:

```
R> logLik(m1)

'log Lik.' -47.77174 (df=2)

R> logLik(dcm1)

'log Lik.' -47.77197 (df=2)

R> logLik(m2)

'log Lik.' -12.04875 (df=2)

R> logLik(dcm2)

'log Lik.' -12.05018 (df=2)

R> AIC(m1, dcm1, m2, dcm2)
```

	df	AIC
m1	2	99.54347
dcm1	2	99.54394
m2	2	28.09749
dcm2	2	28.10036

Now it is possible to write the `print` method:

```
R> print.dcgmlm <- function(x, digits = max(3, getOption("digits") - 3), ...) {
+   cat("\nCall: ", deparse(x$call), "\n\n")
+   cat("Coefficients:\n")
+   print.default(format(x$coefficients, digits = digits), print.gap = 2, quote = FALSE)
+   cat("\nDegrees of Freedom:", x$df.null, "Total (i.e. Null); ", x$df.residual, "Residual\n")
+   cat("Log Likelihood:\t\t\t", format(signif(x$loglik, digits)), "\n")
+   invisible(x)
+ }
```

Let's have a look at the resulting objects of our `dcgmlm` function:

```
R> dcm1

Call:  dcgmlm(formula = Y1 ~ x)

Coefficients:
```

```

(Intercept)          x
      1.940        -1.277

Degrees of Freedom: 19 Total (i.e. Null);  18 Residual
Log Likelihood:      -47.77

R> dcm2

Call:  dcglm(formula = Y2 ~ x, family = "binomial")

Coefficients:
(Intercept)          x
    -0.3508        -1.7907

Degrees of Freedom: 19 Total (i.e. Null);  18 Residual
Log Likelihood:      -12.05

Well done so far!

```

7. Methods for inference

The `summary` method returns the ML estimates, data cloning standard errors, and Wald-type z statistics and p -values:

```

R> summary.dcglm <- function(object, ...){
+   COEF <- coef(object)
+   SE <- object$std.error
+   z <- COEF / SE
+   p <- 2 * pnorm(-abs(z))
+   stab <- cbind("Estimate" = COEF, "Std. Error" = SE,
+     "z value" = z, "Pr(>|z|)" = p)
+   rval <- list(call = object$call,
+     coefficients = stab,
+     loglik = object$loglik,
+     df.residual = object$df.residual,
+     df.null = object$df.null)
+   class(rval) <- "summary.dcglm"
+   rval
+ }

```

The return value here is also a list, repeating some of the elements of the fitted `object`. To appropriately format the summary, we use the `print` method for the object class `'summary.dcglm'`:

```

R> print.summary.dcglm <-
+   function (x, digits = max(3, getOption("digits") - 3),
+     signif.stars = getOption("show.signif.stars"), ...)
+   {
+     cat("\nCall:\n")
+     cat(paste(deparse(x$call), sep = "\n", collapse = "\n"), "\n", sep = "")
+     cat("\nCoefficients:\n")
+     printCoefmat(x$coefficients, digits = digits, signif.stars = signif.stars, na.print = "NA",
+       cat("\nDegrees of Freedom:", x$df.null, "Total (i.e. Null); ", x$df.residual, "Residual\n"),
+       cat("Log Likelihood:\t    ", format(signif(x$loglik, digits)), "\n")
+     )
+   }

```

```
+ invisible(x)
+ }
```

Summaries of the `glm()` results and our models:

```
R> summary(m1)
```

Call:

```
glm(formula = Y1 ~ x, family = poisson)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.6336	-0.8138	-0.2134	0.5154	2.0309

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	1.94162	0.09482	20.478	< 2e-16 ***
x	-1.27648	0.16017	-7.969	1.60e-15 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for poisson family taken to be 1)

Null deviance: 90.897 on 19 degrees of freedom
 Residual deviance: 19.060 on 18 degrees of freedom
 AIC: 99.543

Number of Fisher Scoring iterations: 4

```
R> summary(dcm1)
```

Call:

```
dcglm(formula = Y1 ~ x)
```

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	1.93973	0.09415	20.603	< 2e-16 ***
x	-1.27747	0.15912	-8.029	9.86e-16 ***

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Degrees of Freedom: 19 Total (i.e. Null); 18 Residual
 Log Likelihood: -47.77

```
R> summary(m2)
```

Call:

```
glm(formula = Y2 ~ x, family = binomial)
```

Deviance Residuals:

Min	1Q	Median	3Q	Max
-1.7850	-0.8787	-0.5794	1.0077	1.5424

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-0.3388	0.5021	-0.675	0.500
x	-1.7377	1.0186	-1.706	0.088 .

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

Null deviance: 27.526 on 19 degrees of freedom

Residual deviance: 24.097 on 18 degrees of freedom

AIC: 28.097

Number of Fisher Scoring iterations: 4

R> *summary*(dcm2)

Call:

dcglm(formula = Y2 ~ x, family = "binomial")

Coefficients:

	Estimate	Std. Error	z value	Pr(> z)
(Intercept)	-0.3508	0.5093	-0.689	0.4910
x	-1.7907	1.0349	-1.730	0.0836 .

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Degrees of Freedom: 19 Total (i.e. Null); 18 Residual

Log Likelihood: -12.05

Piece of cake!

For the *confint*, we use the asymptotic normality result of the data cloning theory ([Lele et al. 2007](#)), and the *confint* method defined for the data cloned *mcmc.list* part of the fitted model object:

```
R> confint.dcglm <- function(object, parm, level = 0.95, ...) {
+   rval <- confint(object$mcmc, parm, level, ...)
+   rownames(rval) <- names(coef(object))
+   rval
+ }
```

The 95% confidence intervals for the model estimates are:

R> *confint*(m1)

	2.5 %	97.5 %
(Intercept)	1.748410	2.120651
x	-1.596540	-0.968007

R> *confint*(dcm1)

	2.5 %	97.5 %
(Intercept)	1.755200	2.1242506
x	-1.589334	-0.9656121

```
R> confint(m2)
```

```

                2.5 %    97.5 %
(Intercept) -1.404579 0.62478977
x            -4.014429 0.09589234
```

```
R> confint(dcm2)
```

```

                2.5 %    97.5 %
(Intercept) -1.349128 0.6474719
x            -3.819111 0.2376974
```

Differences are due to the fact, that `confint` for `glm` uses profile likelihood, while `dcglm` confidence intervals are based on the asymptotic normality assumption. Profile likelihood can be computed based on data cloning (Ponciano *et al.* 2009) but that procedure is not covered here.

8. Prediction based on the joint posterior distribution

In the prediction, we use MCMC. The likelihood part of the BUGS model for the prediction is the same as for the estimation. The only difference is in the prior specification:

```
R> glm.pred <- function() {
+   for (i in 1:n) {
+     Y[i] ~ dpois(z[i])
+     Y[i] ~ dbin(z[i], k)
+     log(z[i]) <- mu[i]
+     logit(z[i]) <- mu[i]
+     mu[i] <- inprod(X[i,], beta[1,])
+   }
+   beta[1,1:np] <- mvn[1:np]
+   mvn[1:np] ~ dmnorm(coefs[], prec[,])
+ }
```

Note that we denote `lambda` or `p` as `z`, this will make life easier later. We use again the `custommodel` approach to differentiate between the Poisson and Binomial cases:

```
R> custommodel(glm.pred, c(4,6))
```

```

[1] "model {"
[2] "   for (i in 1:n) {"
[3] "       Y[i] ~ dpois(z[i])"
[4] "       log(z[i]) <- mu[i]"
[5] "       mu[i] <- inprod(X[i,], beta[1,])"
[6] "   }"
[7] "   beta[1,1:np] <- mvn[1:np]"
[8] "   mvn[1:np] ~ dmnorm(coefs[], prec[,])"
[9] "}"
attr(,"class")
[1] "custommodel"
```

```
R> custommodel(glm.pred, c(3,5))
```

```

[1] "model {"
[2] "   for (i in 1:n) {"
[3] "       Y[i] ~ dbin(z[i], k)"
[4] "       logit(z[i]) <- mu[i]"
[5] "       mu[i] <- inprod(X[i,], beta[1,])"
[6] "   }"
[7] "   beta[1,1:np] <- mvn[1:np]"
[8] "   mvn[1:np] ~ dmnorm(coefs[], prec[,])"
[9] "}"
attr(,"class")
[1] "custommodel"

```

Let's consider the Poisson case only (the Binomial differs from it only by the specification of the `model` argument based on the `custommodel` approach, and the fitted model used). The prediction can be done by `jags.fit`, only the data specification is somewhat different. We will define the model parameters based on the MLE (`coefs`) and the variance-covariance matrix. We define a Multivariate Normal node for all the model parameters, by using the inverse of the variance-covariance matrix as a precision matrix (`prec`). Be careful, the check for symmetry in JAGS is stricter than the usual numerical precision in R, consequently we ensure that this condition is met by using the `make.symmetric` function. The data specification will look like (note, we are using the observed data in `X`, but algorithmically, this doesn't make any difference):

```

R> prec <- make.symmetric(solve(vcov(mod1)))
R> coefs <- coef(mod1)
R> prdat <- list(n = nrow(X), X = X,
+             np = ncol(X), k = 1, coefs = coefs, prec = prec)

```

We use the `jags.fit` function. One chain is usually enough:

```

R> prval <- jags.fit(prdat, "z", custommodel(glm.pred, c(4,6)), n.chains = 1)

```

The resulting `mcmc.list` object contains the conditional posterior distribution for our Poisson GLM based prediction with prediction intervals.

9. Methods for prediction

For our convenience, we can write a `vcov` method. We simply use the `vcov` method defined for the `mcmc.list` part of the fitted model object and do some cosmetics on the names:

```

R> vcov.dcglm <- function(object, ...) {
+   rval <- vcov(object$mcmc, ...)
+   rownames(rval) <- colnames(rval) <- names(coef(object))
+   rval
+ }

```

Comparison of the `glm` and `dcglm` approaches:

```

R> vcov(m1)

              (Intercept)              x
(Intercept) 0.008990272 0.009590252
x            0.009590252 0.025655809

```



```
R> vcov(dcm1)
```

```
      (Intercept)      x
(Intercept) 0.008863699 0.009371742
x           0.009371742 0.025317779
```

```
R> vcov(m2)
```

```
      (Intercept)      x
(Intercept)  0.2520969 0.1053385
x           0.1053385 1.0374523
```

```
R> vcov(dcm2)
```

```
      (Intercept)      x
(Intercept)  0.2594333 0.1043506
x           0.1043506 1.0710576
```

Quite similar as we expected.

The `predict` function will look like:

```
R> predict.dcgglm <-
+   function(object, newdata = NULL,
+     type = c("link", "response"), se = FALSE, ...)
+   {
+     glm.pred <- c("model {",
+       "   for (i in 1:n) {",
+       "       Y[i] ~ dpois(z[i])",
+       "       Y[i] ~ dbin(z[i], k)",
+       "       log(z[i]) <- mu[i]",
+       "       logit(z[i]) <- mu[i]",
+       "       mu[i] <- inprod(X[i,], beta[1,])",
+       "   }",
+       "   beta[1,1:np] <- mvn[1:np]",
+       "   mvn[1:np] ~ dmnorm(coefs[], prec[,])",
+       " }")
+     prec <- make.symmetric(solve(vcov(object)))
+     coefs <- coef(object)
+     if (is.null(newdata)) {
+       X <- object$model
+     } else {
+       formul <- object$formula
+       formul[[2]] <- NULL
+       rhs <- model.frame(formul, newdata)
+       X <- model.matrix(attr(rhs, "terms"), rhs)
+     }
+     type <- match.arg(type)
+     params <- switch(type,
+       "link" = "mu",
+       "response" = "z")
+     model <- switch(object$family,
+       "poisson" = custommodel(glm.pred, c(4,6)),
+       "binomial" = custommodel(glm.pred, c(3,5)))
```

```

+   prdat <- list(n = nrow(X), X = X,
+   np = ncol(X), coefs = coefs, prec = prec)
+   if (object$family == "binomial")
+     prdat[["k"]] <- 1
+   prval <- jags.fit(prdat, params, model, ...)
+   if (!se) {
+     rval <- coef(prval)
+   } else {
+     rval <- list(fit = coef(prval),
+       se.fit = mcmcapply(prval, sd))
+   }
+   rval
+ }

```

The pseudo-code for `predict` is:

1. `glm.predict` is the familiar `custommodel` specification.
2. `prec` and `coefs` are needed for the data specification.
3. If `newdata` is `NULL`, we use the extracted design matrix of our fitted model (`object`). Else, we create the design matrix corresponding to our model from `newdata` (a data frame, containing the same covariates, but possibly with different values). For this extraction, we use the `formula` of the fitted model `object`.
4. Based on the `type` argument, we will monitor (sample) the nodes `mu` (if `type = "link"`) or `z` (if `type = "response"`). `mu` corresponds to the values on the scale of the linear predictors, while `z` corresponds to the values on the response scale.
5. `model` is determined by the `family` of the fitted model `object`.
6. `prdat` is the data, `prmod` is the fitted MCMC object (we use `k` only in case of the Binomial family, otherwise `rjags` warns us that `k` is unused for the Poisson case).
7. If the `se` argument is `FALSE`, the return value will be the point estimate vector of the prediction. If the `se` argument is `TRUE`, the return value will be a list including point estimates (`fit`) and standard errors (`se.fit`). Then, return the value.

Now let's do the prediction for a range of `x` values from -1 to 1 (call it `px`):

```

R> px <- data.frame(x=seq(-1, 1, len = 10))
R> px

```

```

      x
1 -1.000000
2 -0.777778
3 -0.555556
4 -0.333333
5 -0.111111
6  0.111111
7  0.333333
8  0.555556
9  0.777778
10 1.000000

```

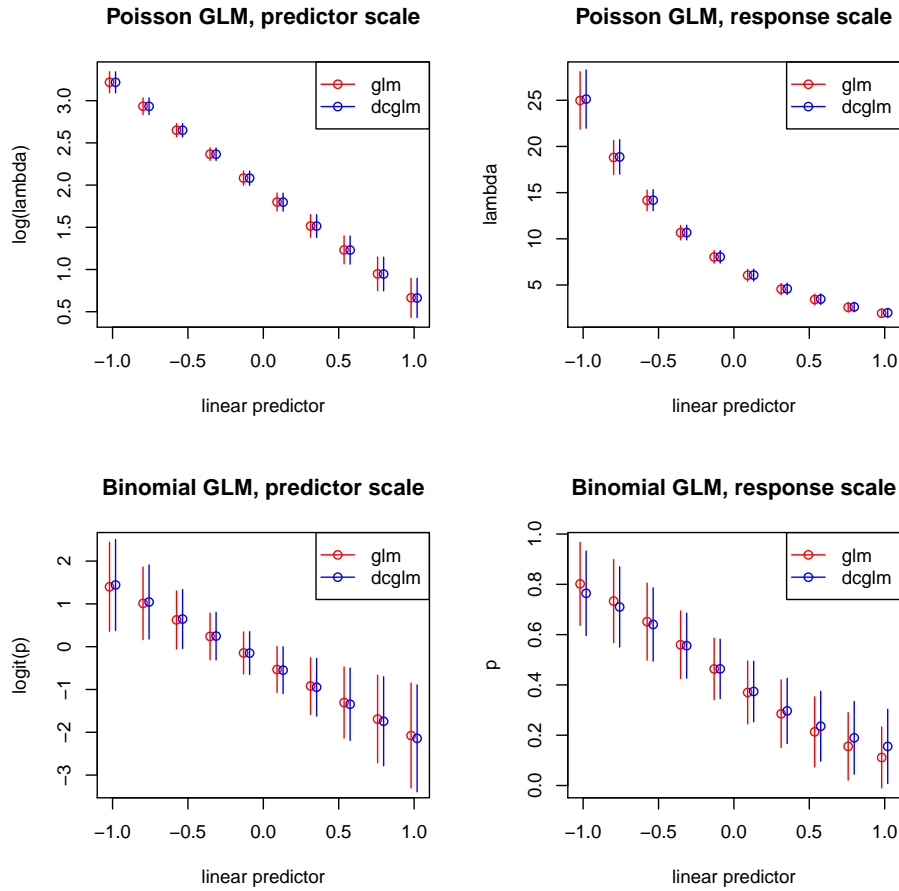


Figure 1: Prediction results based on the `glm` and `dcglm` approaches for the Poisson GLM. Points are prediction estimates, whiskers are prediction standard errors.

The `glm` based predictions are:

```
R> pm1link <- predict(m1, newdata=px, type="link", se=TRUE)
R> pm1resp <- predict(m1, newdata=px, type="response", se=TRUE)
R> pm2link <- predict(m2, newdata=px, type="link", se=TRUE)
R> pm2resp <- predict(m2, newdata=px, type="response", se=TRUE)
```

The `dcglm` based predictions are:

```
R> pdcm1link <- predict(dcm1, newdata=px, type="link", se=TRUE)
R> pdcm1resp <- predict(dcm1, newdata=px, type="response", se=TRUE)
R> pdcm2link <- predict(dcm2, newdata=px, type="link", se=TRUE)
R> pdcm2resp <- predict(dcm2, newdata=px, type="response", se=TRUE)
```

Fig. 1 shows prediction results.

10. Making the *dcglm* package

The easiest part now comes:

```
R> package.skeleton("dcglm", c("coef.dcglm", "confint.dcglm", "dcglm",
+   "fitted.dcglm", "logLik.dcglm", "predict.dcglm",
+   "print.dcglm", "print.summary.dcglm", "summary.dcglm", "vcov.dcglm"))
```

Follow this workflow for your own model and estimating procedure, then edit the files (read the *Writing R Extensions* manual) in the package directory, run R CMD check and R CMD build, distribute your package, and go out for a walk!

References

- Lele SR, Dennis B, Lutscher F (2007). “Data cloning: easy maximum likelihood estimation for complex ecological models using Bayesian Markov chain Monte Carlo methods.” *Ecology Letters*, **10**, 551–563.
- Ponciano JM, Taper ML, Dennis B, Lele SR (2009). “Hierarchical models in ecology: confidence intervals, hypothesis testing, and model selection using data cloning.” *Ecology*, **90**, 356–362.
- Sólymos P (2009). *dclone: Data Cloning and MCMC Tools for Maximum Likelihood Methods*. R package version 1.0-0, URL <http://cran.r-project.org/packages=dclone>.

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