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## ABSTRACT

**Summary:** Numerous methods have been proposed to find the optimal partition of a signal in a given number of segments, but very few address the question of the quality of the segmentation. In many biological data-sets (CGH-array, NGS, ...), each segment is assumed to be related to a biological event so that the certainty of their location and the number of segments is crucial. EBS is an R package that provides through a Bayesian framework exact quantities such as the posterior distribution of a change-point position, and an efficient ICL criterion for the selection of the total number of change-points. All quantities are computed in a quadratic time.

**Availability:** EBS is available as an R package from CRAN repositories (e.g. <http://cran.r-project.org/web/packages>).

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## 1 INTRODUCTION

Most change-point detection strategies do not address crucial questions like the quality of the segmentation or the uncertainty on the localisation of breakpoints that are useful when choosing the number of segments, or comparing the segmentation of different profiles.

Among the few are the implementation of Bardy and Hartigan's Bayesian approach (bcp) that uses MCMC approximation, (Barry and Hartigan, 1993; Erdman and Emerson, 2007), and the frequentist forward-backward algorithm of Guedon (2008) and constrained-HMM framework of Luong *et al* (2012). Those two later approaches compute those useful quantities for fixed values of the segment parameters.

EBS is an implementation of the framework described in Rigaill *et al.* (2010) which derives **exact** posterior probabilities of quantities such as the number of segments, the entropy of a segmentation, or the localisation of the change-points.

## 2 AVAILABLE FUNCTIONALITY

The package has been developed for the analysis of biological data. For this matter, the Normal Heteroscedastic model, relevant for CGH-arrays, and the Poisson and Negative Binomial (with known overdispersion parameter) models, relevant for NGS-data have been implemented.

Table 1 gives the list of the functions available in the EBS Package. This section describes and illustrates their use with a continued example.

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**Table 1.** Functions provided by EBS package

Function Name	Output
EBSegmentation	Initializes matrix $A$ and its $K_{max}$ first powers
EBSBIC	Computes BIC and chooses optimal value of $K$
EBSICL	Computes ICL and chooses optimal value of $K$
EBSPostK	Returns the posterior probability of the number of segments
EBSDistrib	Computes the distribution of a change-point
EBSPlotProba	Plots distribution of all change-points for a given $K$

### 2.1 Initialization

All quantities of interest can be computed using simple operations on the elements of the matrix  $A$  of segment probabilities. The function `EBSegmentation` initializes this matrix with the data according to the user's choice of maximum number of segments and data-model. Each of them is associated with a prior distribution on the parameters (for instance, Gamma for the Poisson model), and the result depends on the value of the hyperparameters. By default `EBSegmentation` uses values such that the prior is non-informative, but the user has the possibility of giving his own hyperparameters.

The function returns an object of class `EBS` which contains the prior information, matrix  $A$  and the two following matrices:  $Li$  and  $Col$  are matrices which  $k^{th}$  row (respectively column) is the first row (resp last column) of the  $k^{th}$  power of  $A$  ( $1 \leq k \leq K_{max}$ ). Thus  $Li_{i,j} = P(\|Y_0, Y_j\|, i)$  and  $Col_{i,j} = P(\|Y_i, Y_{n+1}\|, j)$ .

```
> set.seed(1)
> require(EBS)
> x<-c(rpois(125,1),rpois(100,5),rpois(50,1),
      rpois(75,5),rpois(50,1))
> out <- EBSegmentation(x,Kmax=20)
```

### 2.2 Model Selection

EBS Package provides two model selection criteria:

- an exact BIC criterion
- an ICL criterion

These criteria can be called with functions `EBSBIC` and `EBSICL`.

Considering the segmentation as an unobserved variable, we can use the ICL criterion introduced by Biernacki *et al.* (2000) in the context of incomplete data models to select the number of segments. Written as

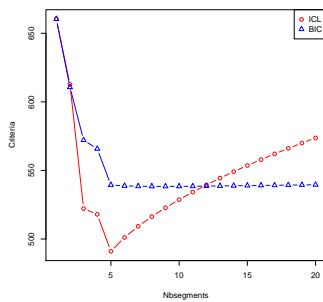
$ICL(K) = -\log P(Y, K) + \mathcal{H}(K)$  where

$$\mathcal{H}(K) = -\log \sum_{m \in \mathcal{M}_K} p(m|Y, K) \log p(m|Y, K) \quad (1)$$

the entropy  $\mathcal{H}(K)$  (computed in a quadratic time) can be viewed as a penalty term. Even though in this context the Bayesian Information Criterion is exact, it overestimates the number of segments while the ICL performs better (Rigaill *et al.*, 2010). However, the computation of the BIC (through function `EBSPostK`) can be useful for later analysis such as Bayesian Model Averaging (BMA).

```
> bic <- EBSBIC(out)
> print(bic$NbBIC)
[1] 9
> icl <- EBSICL(out)
> print(icl$NbICL)
[1] 5
```

figure 1 plots the value of the BIC and ICL depending on  $K$ .



**Fig. 1.** BIC and ICL criteria as a function of the number of segments

### 2.3 Change-point location distribution

Once the number of segments is chosen, one might be interested in the distribution of the location of each change-points. Two functions are implemented to address this question. `EBSDistriB` returns the distribution of the  $k^{th}$  changepoint of a segmentation in  $K$  segments. `EBSPlotProba` plots the distribution of all  $K - 1$  change-points of a segmentation in  $K$  segments. The user has the option to plot those distributions on top of the data.

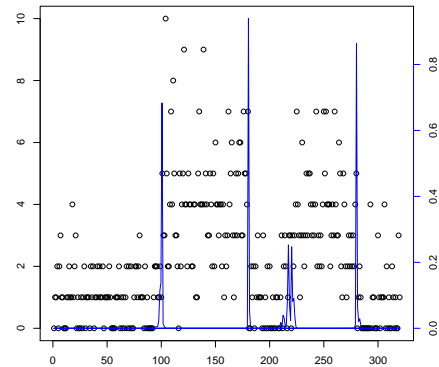
```
> EBSPlotProba(out, Kicl, data=TRUE,
  file="my-segmentation.pdf")
```

Figure 2 shows the output.

## 3 IMPLEMENTATION

The preprocessing of the input data is handled by the R language, giving the user easier access to a large amount of data. The model fitting, computation of probabilities and other time consuming operations are implemented in a versatile C++ code, and dynamically loaded into R. Several methods are available for further analysis of the results. The package offers various diagnostic tools

and functions for visualization, for example, plotting the breakpoint location distributions for a given number of segments.



**Fig. 2.** file `my-segmentation.pdf`, output of function `EBSPlotProba`

## 4 CONCLUSION

This note introduces the EBS package for the analysis of NGS and CGH-array data. It allows a complete analysis of the segmentation space for biological profiles in an exact Bayesian framework. It provides an efficient criterion for the selection of the number of segments and allows further analysis of variables such as the entropy or the location of a change-point. Future improvements of the package include the analysis of other quantities of interest such as the posterior mean of the signal.

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