Belief Propagation in Genotype-Phenotype Networks using the `geneNetBP` package

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`geneNetBP` version 2.0.0 as of 2016-05-05

Contents

1   Introduction

The `geneNetBP` package leverages belief propagation methods in genotype-phenotype networks inferred from Quantitative Trait Loci (QTL) data. The network structure can be perturbed by absorbing phenotypic evidence and the system-wide effects on the network are quantified in a nodewise manner. The package implements methods specifically to fit Conditional Gaussian Bayesian Network (CG-BN) or Discrete Bayesian Network to QTL data, absorb phenotype evidence and quantify and visualize the changes in network beliefs. For detailed description of methods, refer to our SAGMB publication. To cite "geneNetBP", use:

Janhavi Moharil, Paul May, Daniel P. Gaile, Rachael Hageman Blair (2016). "Belief Propagation in Genotype-Phenotype Networks.", Stat Appl Genet Mol Biol, 15(1):39-53.

For belief propagation in CG-BN, the package makes extensive use of the package `RHugin` that provides an R interface for the Hugin Decision Engine, a commercial software for building and infering Bayesian belief networks. The `RHugin` is currently not available on CRAN and is hosted on R-Forge. `geneNetBP` requires both Hugin and RHugin to be installed. `RHugin` can be downloaded from `http://rhugin.r-forge.r-project.org`. The Hugin Decision Engine can be downloaded from `http://www.hugin.com`. Detailed installation instructions of the `geneNetBP` package and package dependencies are available on the geneNetBP project homepage. Note that `RHugin` is required for the functioning of CG-BN implementation of `geneNetBP`. The package `RHugin` will not automatically load upon loading `geneNetBP` package. Use `library(RHugin)` or `require(RHugin) to load RHugin before using geneNetBP`.

For belief propagation in discrete bayesian networks where both the genotypes and phenotypes are categorical data, the structural learning in `geneNetBP` version 2.0.0 is implemented using the package `bnlearn` while belief propagation is implemented using the package `gRain`. Both the packages are available on CRAN. `HuginLite` can also be used to infer networks from discrete data, however the demo version is restricted to 50 states and 500 cases. For larger datasets, the discrete bayesian network learning and inference using functions that implement `bnlearn` and `gRain` is recommended.

Load the package before running examples from the vignette.

```
> library(geneNetBP)
> library(RHugin) ## Needed for CG-BN implementation
```

2   Datasets

There are 4 datasets provided with this package.

2.1   mouse

The *Mus Musculus* Kidney eQTL data (`mouse`) was obtained from a F2 inner-cross between inbred MRL/MpJ and SM/J strains of mice [1]. The original data consists of 33,872 gene expression traits for 173 males. After linkage analysis and filtering based on location and significance of QTL, the data consists of 14 genes and their SNP markers corresponding to their QTL. Thus the final dataset `mouse` is a data frame of 173 observations of 19 variables (5 genotypes - SNP markers and 14 genes - normalized gene expression values).

Load the dataset and view the first 3 observations:

```
> data(mouse)
> head(mouse,n=3)

  Qchr4 Qchr17 Qchr15 Qchr11 Qchr2    Cyp4a31      Slc5a9     Slc6a9       Hmgcl
1     2      3      2      2     2 -0.8581591 -1.1433976 2.1143808 -0.3683079
3     3      2      2      2     2  0.2622828  0.3683079 0.6476036  0.1155036
4     2      2      2      3     1  0.1445610  0.6476036 0.3993231  0.5951785
       Ptp4a2        Ak2      Zbtb8a       Stx12    Trspap1       Mecr      Wdtc1
1  1.2006550  0.4149740   0.5443409  0.02881581 -1.0144987 -0.4625623 -0.3224307
3 -0.2177984  0.8581591  -1.0389014  0.66547438 -1.6851791 -0.7582926  0.9906857
4 -0.1737411 -0.8172368   1.0389014 -0.81723682 -0.7972819 -0.2030698  0.5611245
        Atpif1      Rbbp4       Tlr12
1 -1.14339756 1.3644887 -0.52770925
3 -1.32881793 1.2308184 -0.83752265
4  0.08654337 0.3683079 -0.01440641
```

There are 3 possible genotype states MM (homozygous) denoted by 1, H (heterozygous) by 2 and SS (homozygous) by 3. The genotypes are categorical variables and hence first 5 columns in the data frame `mouse` have to be of class factor while the phenotypes are continuous variables with 14 columns in data frame `mouse` of class numeric.

2.2   hdl

The *Mus Musculus* HDL QTL data (`hdl`) was obtained from a F2 inner-cross between inbred MRL/MpJ and SM/J strains of mice [2]. The original data consists of 33,872 gene expression traits for 280 males and females. After linkage analysis and filtering based on

location and significance of QTL, the data consists of 10 phenotypes (9 genes and HDL level) and their 5 SNP markers corresponding to their QTL. Thus the final dataset `hdl` is a data frame of 280 observations of 15 variables (5 SNP markers and 10 phenotypes (9 normalized gene expression and HDL levels).

Load the dataset and view the first 3 observations:

```
> data(hdl)
> head(hdl,n=3)

  c1 c2 c4 c7 c12        HDL     Pla2g4a        Nr1i3     Cyp2b10      Ppap2a
1  2  1  2  1    3 -0.1601137  0.67171243  -0.5748821  0.96978138   0.6606545
2  3  3  3  2    2 -0.8365833 -0.75159139   1.1396864 -0.05760458   0.4145857
3  3  1  2  2    1 -1.1655010 -0.08424431  -0.5233845 -0.30585203  -1.0132221
       Kdsr       Degs1       Neu1        Spgl1      Apoa2
1 0.3762732   0.4049526  0.6940793   1.35105303  1.1396864
2 1.9645187  -0.9011827  0.7398946  -1.37345382  2.1935392
3 0.3667830   0.6065198  1.4451709  -0.02657516  0.7873186
```

Note that there are 3 possible genotype states MM (homozygous) denoted by 1, H (heterozygous) by 2 and SS (homozygous) by 3.

2.3 toy

The `toy` is a simulated eQTL dataset from the network shown below, of 500 observations, 3 genotypes (Q1,Q2,Q3) each having 2 possible states and 6 phenotypes, X1-X6.
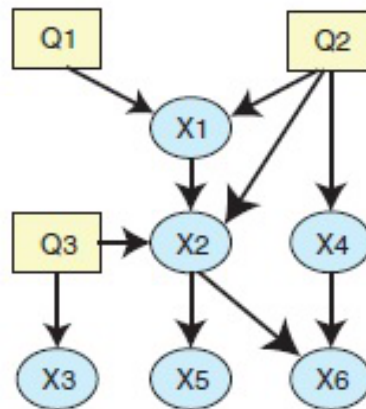

Figure 1. Toy network example.

2.4 yeast

The `yeast` dataset is a subset of the widely studied yeast expression dataset comprising of 112 F1 segregants from a cross between BY4716 and RM11-1a strains of *Saccharomyces Cerevisiae* [3, 4]. The original dataset consists of expression values reported as log2(sample/ BY reference) for 6216 genes. The data can be accessed in Gene Expression Omnibus (GEO) by accession number (GSE1990). After linkage analysis and filtering based on location and significance of QTL, a final set of 38 genes and their corresponding 12 SNP markers were identified and included in the yeast dataset. The gene expression values are discretized around the median, 1(above or equal to median) and -1 (below median).

Thus the final dataset `yeast` is a data frame of 112 observations of 50 variables (12 SNP markers and 38 genes - normalized and discretized gene expression values).

Load the dataset and view the first 3 observations:

```
> data(yeast)
> head(yeast,n=3)
```

Note that there are 2 possible genotype states denoted by 1 and 2. The genotypes are categorical variables and hence all genotype columns in data frame `yeast` have to be of class factor. The phenotypes are also discrete variables and phenotype columns in data frame `yeast` of class factor.

3 Infering network structure

3.1 Fit a CG-BN to QTL data

3.1.1 Model

The graphical model is represented by a Directed Acyclic Graph (DAG). The nodes in the graph represent the model variables, which may be discrete (QTL) or continuous (phenotypes). The phenotypes (e.g., metabolites, gene-expression, or clinical traits etc) are assumed to be continuous and follow a normal distribution. The data consists of n phenotypes (X) and m genotypes at Single Nucleotide Polymorphism (SNP) markers and is defined as: $D = \{X_1, \ldots, X_n, Q_1, \ldots, Q_m\}$ [5].

Model Assumptions:

1. Discrete variables precede the continuous variables.
2. No relationships between discrete variables (no edges between them).

Local relationships between continuous child nodes and parents are described using Homogeneous Conditional Gaussian Models (HCGM). The conditional distribution for a phenotype $Y = X_j$ with discrete parent Q_i with genotype states (g) and continuous parent X_i $(i \neq j)$ is modeled as:

$$P\left(Y \mid Q_i = g, X_i = x_i\right) = N\left(\alpha(g) + \beta(g)^T x_i, \gamma(g)\right), \tag{1}$$

where the mean is a regression that depends on both discrete and continuous parents, but the variance depends only on the discrete parents (genotype states). The parameters of the CG-BN and subsequently the marginal distributions are inferred from the data under the constraints of the topology and the Markov condition using the PC-algorithm [6–8] in `RHugin` package.

3.1.2 Mouse kidney eQTL Example

We will use the function `fit.gnbp` to learn the structure of a genotype-phenotype network from `mouse` dataset. This function uses the PC algorithm and the EM algorithm [6–8] implemented in the `RHugin` package to learn the network structure and and the conditional probability tables for each node in the network. You will need both HuginLite and `RHugin` installed. Refer to Section 1 for installation instructions.

Load the `mouse` dataset and extract the genotype and phenotype data. The first five columns are genotype (categorical) and the next 14 columns are phenotypes (continuous).

```
> data(mouse)
> mousegeno<-mouse[,1:5]
> mousepheno<-mouse[,6:19]
```

The simplest example of fitting a CG-BN to mouse QTL data is given below. This example uses default parameters.

```
> data(mouse)
> fit.gnbp(mousegeno,mousepheno)

$gp
A Hugin domain: there are 19 nodes and 17 edges

$marginal
```

```
$marginal$pheno
$marginal$pheno$mean
                [,1]
Cyp4a31 -4.877280e-17
Slc5a9  -4.813106e-17
Slc6a9  -5.133979e-18
Hmgcl   -3.784939e-17
Ptp4a2  -6.930872e-17
Ak2     -7.153821e-03
Zbtb8a  -3.698069e-17
Stx12    2.657651e-17
Trspap1 -3.200715e-17
Mecr    -8.794206e-02
Wdtc1   -7.604707e-17
Atpif1  -5.615290e-17
Rbbp4    1.067939e-17
Tlr12   -5.534668e-18

$marginal$pheno$var
             [,1]
Cyp4a31 0.9551227
Slc5a9  0.9573564
Slc6a9  0.7425429
Hmgcl   0.7020575
Ptp4a2  0.9584933
Ak2     0.7696464
Zbtb8a  0.9551227
Stx12   0.9575380
Trspap1 0.9551227
Mecr    0.5043761
Wdtc1   0.9551227
Atpif1  0.9572220
Rbbp4   0.9557443
Tlr12   0.7471877


$marginal$geno
$marginal$geno$freq
          state1    state2    state3
Qchr4  0.2312139 0.4682081 0.3005780
Qchr17 0.2647062 0.4588229 0.2764709
```

```
Qchr15 0.1802326 0.5988372 0.2209303
Qchr11 0.2163744 0.5380114 0.2456142
Qchr2  0.2500000 0.5000000 0.2500000


$gp_nodes
node       class      levels type
[1,] "Cyp4a31" "numeric" "0"    "pheno"
[2,] "Slc5a9"  "numeric" "0"    "pheno"
[3,] "Slc6a9"  "numeric" "0"    "pheno"
[4,] "Hmgcl"   "numeric" "0"    "pheno"
[5,] "Ptp4a2"  "numeric" "0"    "pheno"
[6,] "Ak2"     "numeric" "0"    "pheno"
[7,] "Zbtb8a"  "numeric" "0"    "pheno"
[8,] "Stx12"   "numeric" "0"    "pheno"
[9,] "Trspap1" "numeric" "0"    "pheno"
[10,] "Mecr"    "numeric" "0"    "pheno"
[11,] "Wdtc1"   "numeric" "0"    "pheno"
[12,] "Atpif1"  "numeric" "0"    "pheno"
[13,] "Rbbp4"   "numeric" "0"    "pheno"
[14,] "Tlr12"   "numeric" "0"    "pheno"
[15,] "Qchr4"   "factor"  "3"    "geno"
[16,] "Qchr17"  "factor"  "3"    "geno"
[17,] "Qchr15"  "factor"  "3"    "geno"
[18,] "Qchr11"  "factor"  "3"    "geno"
[19,] "Qchr2"   "factor"  "3"    "geno"


$gp_flag
[1] "cg"

attr(,"class")
[1] "gpfit"
```

The learnt network structure is returned as RHugin domain in the first element `gp` of the list. RHugin domain is an external pointer and hence cannot be saved in R workspace. The `RHugin` package provides functions `read.rhd` and `write.rhd` for loading and saving Hugin domains. The domains that are not saved will be lost when quitting R. The use of assignment operator such as <- or = will only return the pointer. Refer to the RHugin help manual for more information. The other elements in the list are for internal use with other functions.

The inferred network structure is very sensitive to the significance level (specified as `alpha`) and hence it is recommended to try out different values of the argument `alpha`. The argument `alpha` is for use with RHugin package i.e. the function `fit.gnbp` will pass on `alpha` to RHugin functions. For example,

```
> fit.gnbp(mousegeno,mousepheno,alpha = 0.1)
```

```
$gp
  A Hugin domain: there are 19 nodes and 31 edges
```

```
$marginal
$marginal$pheno
$marginal$pheno$mean
                [,1]
Cyp4a31  1.914642e-02
Slc5a9   2.471620e-02
Slc6a9  -1.957688e-02
Hmgcl   -7.136515e-03
Ptp4a2   3.519799e-03
Ak2     -7.153821e-03
Zbtb8a  -2.003327e-17
Stx12    4.433032e-17
Trspap1  4.239712e-03
Mecr    -1.551256e-16
Wdtc1    2.514671e-17
Atpif1   2.190113e-03
Rbbp4    2.317482e-17
Tlr12    5.888329e-02
```

```
$marginal$pheno$var
             [,1]
Cyp4a31 0.8965621
Slc5a9  0.8538129
Slc6a9  0.7939058
Hmgcl   0.8509102
Ptp4a2  0.8550665
Ak2     0.7696464
Zbtb8a  0.9551227
Stx12   0.9575380
Trspap1 0.8530483
Mecr    0.9550281
```

```
Wdtc1   0.9574396
Atpif1  0.9027874
Rbbp4   0.9557443
Tlr12   0.7295634


$marginal$geno
$marginal$geno$freq
          state1    state2    state3
Qchr4  0.2312139 0.4682081 0.3005780
Qchr17 0.2647062 0.4588229 0.2764709
Qchr15 0.1800768 0.5975270 0.2223963
Qchr11 0.2171277 0.5379791 0.2448932
Qchr2  0.2500000 0.5000000 0.2500000




$gp_nodes
        node       class      levels type
 [1,] "Cyp4a31"  "numeric"  "0"    "pheno"
 [2,] "Slc5a9"   "numeric"  "0"    "pheno"
 [3,] "Slc6a9"   "numeric"  "0"    "pheno"
 [4,] "Hmgcl"    "numeric"  "0"    "pheno"
 [5,] "Ptp4a2"   "numeric"  "0"    "pheno"
 [6,] "Ak2"      "numeric"  "0"    "pheno"
 [7,] "Zbtb8a"   "numeric"  "0"    "pheno"
 [8,] "Stx12"    "numeric"  "0"    "pheno"
 [9,] "Trspap1"  "numeric"  "0"    "pheno"
[10,] "Mecr"     "numeric"  "0"    "pheno"
[11,] "Wdtc1"    "numeric"  "0"    "pheno"
[12,] "Atpif1"   "numeric"  "0"    "pheno"
[13,] "Rbbp4"    "numeric"  "0"    "pheno"
[14,] "Tlr12"    "numeric"  "0"    "pheno"
[15,] "Qchr4"    "factor"   "3"    "geno"
[16,] "Qchr17"   "factor"   "3"    "geno"
[17,] "Qchr15"   "factor"   "3"    "geno"
[18,] "Qchr11"   "factor"   "3"    "geno"
[19,] "Qchr2"    "factor"   "3"    "geno"

$gp_flag
[1] "cg"
```

```
attr(,"class")
[1] "gpfit"
```

The inferred network structure can be visualized by the generic plot method for objects of class "gpfit".

```
> mouse.cgbn<-fit.gnbp(mousegeno,mousepheno,alpha = 0.1)
> ## plot method for graph objects
> plot.cgbn(mouse.cgbn)
```
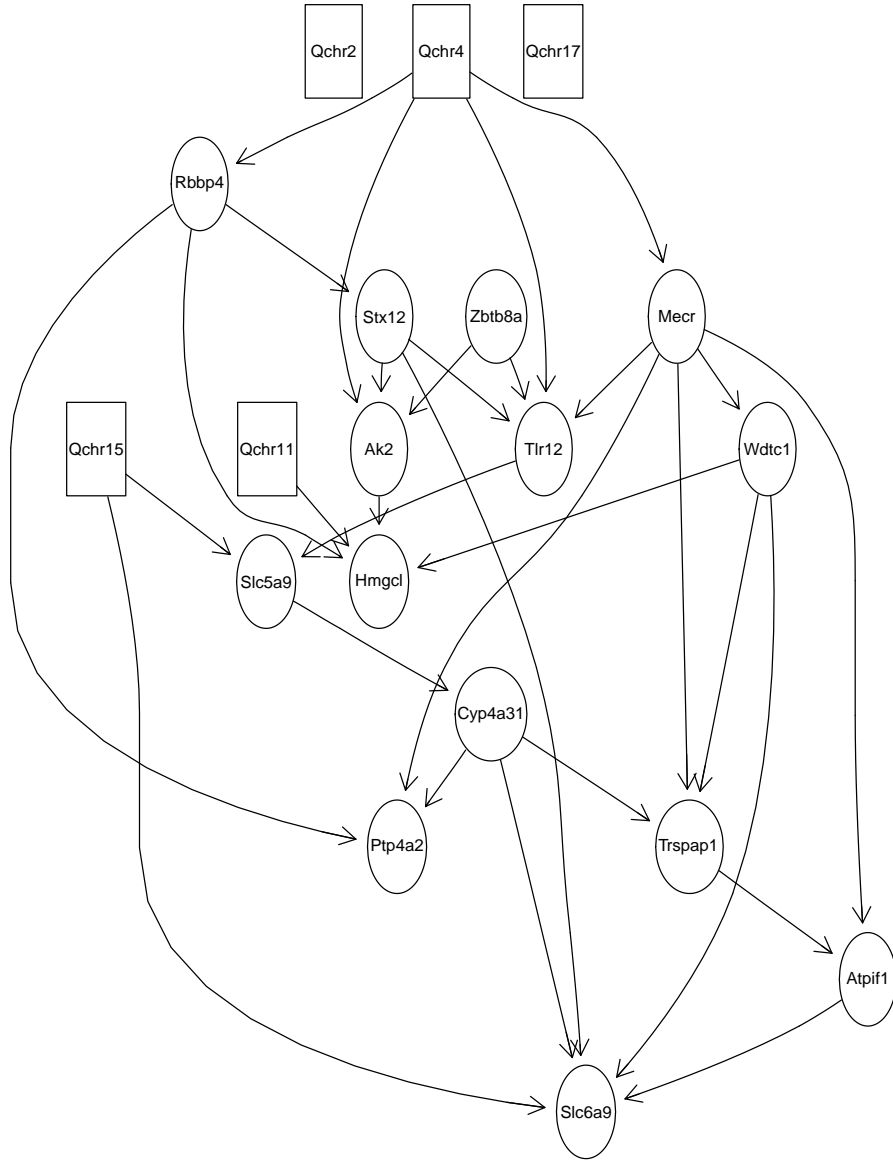
Figure 2. Conditional Gaussian network learnt from mouse kidney eQTL data

The genotypes are represented by boxes and the phenotypes are represented by elliptical nodes. Notice that the network now has 31 edges. Also, Qchr17 and Qchr2 are not included in the network. Any additional domain knowledge can be provided through a list of constraints. See Section 6 for details.

13

3.2 Fit a Discrete Bayesian Network to QTL data

3.2.1 Model

The model for a Discrete Bayesian Network is very similar to the CG-BN. The graphical model is still represented by a Directed Acyclic Graph (DAG). The QTL variables are discrete. The **phenotypes** however are also **discrete** and not continuous unlike in the CG-BN representation. The data consists of n phenotypes (X) and m genotypes at Single Nucleotide Polymorphism (SNP) markers and is defined as: $D = \{X_1, \ldots, X_n, Q_1, \ldots, Q_m\}$.

Model Assumptions are restated as:
1. Genotypes precede the phenotypes.
2. No relationships between genotypes (no edges between them).

3.2.2 Yeast Example

A discrete bayesian network can be learnt by 2 approaches: 1. `fit.gnbp` that implements the PC algorithm as described above or 2. `fit.dbn` that implements several score-based and constraint-based learning methods algorithms from `bnlearn`.

Load the `yeast` dataset and extract the genotype and phenotype data. The first 12 columns are genotypes (categorical, 2 states each) and the next 38 columns are phenotypes (categorical, 2 levels each).

```
> data(yeast)
> yeastgeno<-yeast[,1:12]
> yeastpheno<-yeast[,13:50]
```

1. fit.gnbp
A discrete bayesian network can be learnt using `fit.gnbp` by setting `type = "db"`. Since the demo version of Hugin allows for only 50 states, use a subset of the data.

```
> yeast.gnbp<-fit.gnbp(yeastgeno[,1:9], yeastpheno[,1:16],type="db",alpha=0.1)
```

The RHugin pointer to the inferred network structure is returned in the variable `gp` of the list. It consists of 25 nodes and 22 edges. Here is a plot of the network structure.

```
> plot(yeast.gnbp)
```

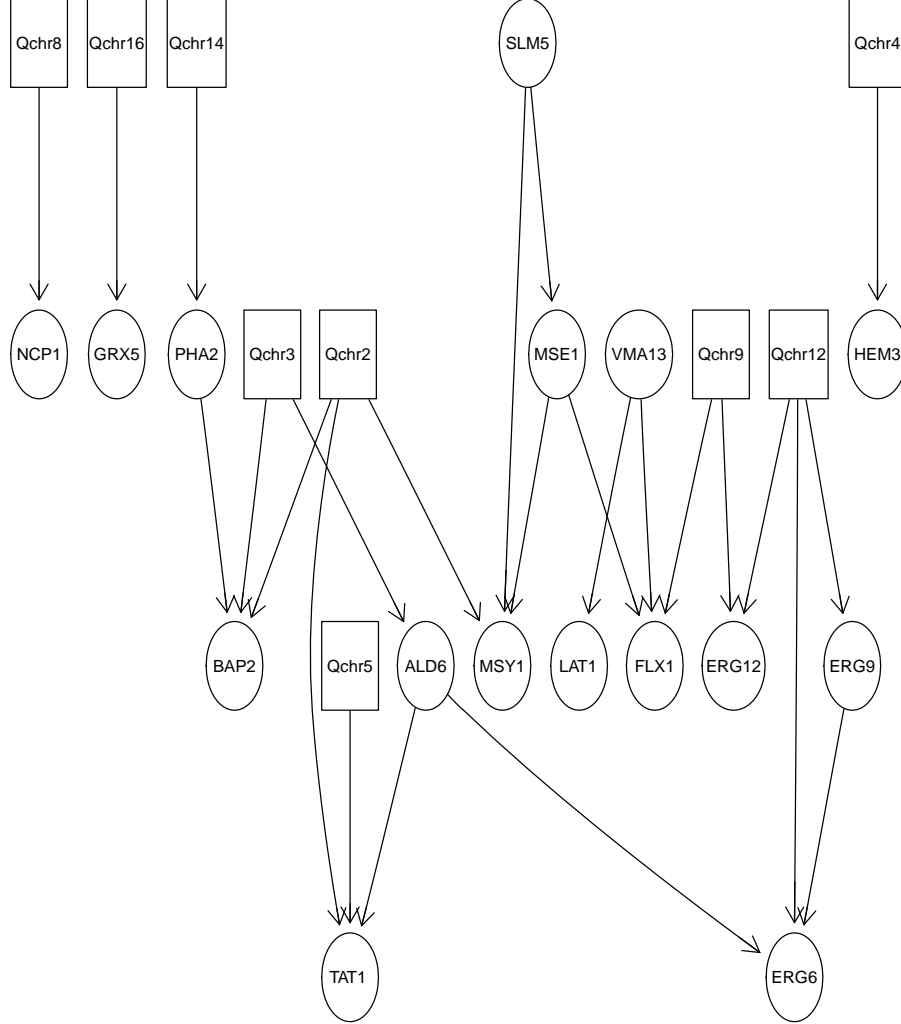**Figure 3.** Discrete Bayesian Network learnt from Yeast data using (`fit.gnbp`)

2. fit.dbn

The second approach to infer the network structure is by using `fit.dbn` that can implement several score-based and constraint-based learning methods from the package `bn-learn`. The default method is *Hill-Climbing* (`method = "hc"`).There is no limit on the number of states or cases, so plug in the complete dataset.

```
> yeast.dbn<-fit.dbn(yeastgeno,yeastpheno)
> plot(yeast.dbn)
```
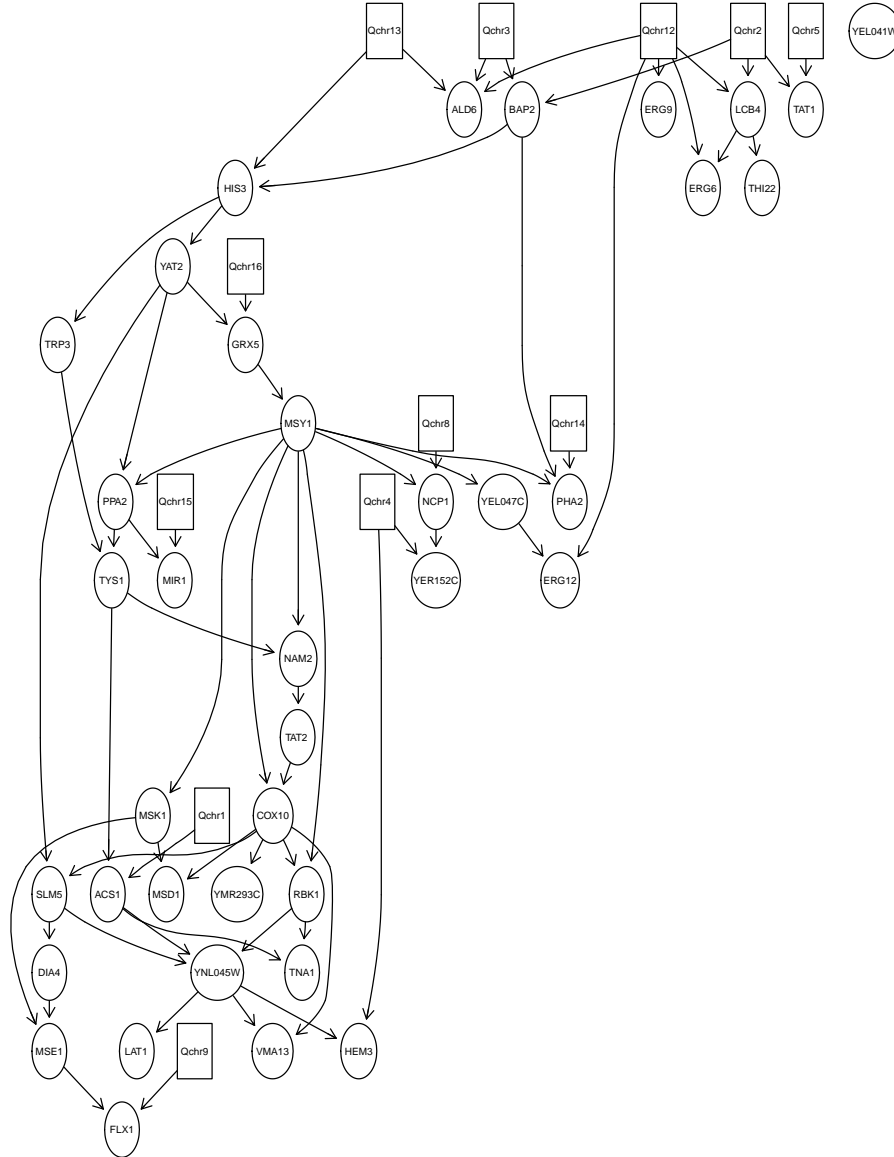

Figure 4. Discrete Bayesian Network learnt from Yeast data using (`fit.dbn`)

`fit.dbn` return an object of class `dbnfit` which is a list of several elements. The inferred network is returned as a "bn.fit" object in `dbn` variable of the list. The conditional prob-

abilities are returned in the `marginal` element of the list. Rest of the variables in the list are for internal use with other functions.

To choose a different learning method, specify `method`. For example, to fit the network by *Grow-Shrink* method,

```
> yeast.dbn<-fit.dbn(yeastgeno,yeastpheno_dis,method="gs")
```

3.3   Extracting Conditional Probability Distributions

In both CG-BN and discrete Bayesian networks, there are conditional probability tables associated with each node in the network. The marginal distributions are returned in the second element `marginal` of the list in both `dbnfit` and `gpfit` objects.

In addition, the conditional distributions can also be accessed by using the package specific functions. For example, `get.marginal` from the package `RHugin` can be used to compute the marginal distributions in an RHugin domain. Another useful function is `get.table` to extract the CPT, experience or fading table associated with any node in an RHugin domain. Refer to `RHugin` manual for more help on these functions.

4   Absorbing evidence and Network Comparison

4.1   Conditional Gaussian Bayesian Networks

4.1.1   Belief propagation

In a CG-BN, new evidence can be entered by setting phenotypes in the network to a particular value, $X_i = x_i^*$. The evidence can pertain to a single node or multiple nodes in the network.

Through message passing, the probability distributions are updated (called as beliefs) after taking into account new evidence. Updated beliefs for discrete nodes (genotypes) are simply updated estimated frequencies under the new evidence. For continuous nodes (phenotypes), the updated beliefs are in terms of revised parameters for the Gaussian distribution. The original and absorbed network are compared node-wise by quantifying the change in marginals [5].

4.1.2   Jeffrey's Signed Information (JSI)

A symmetric version of the Kullback-Leibler information, known as Jeffrey's information is calculated to compare the marginal belief in the original network $X_i^0 \sim N(\mu_0, \sigma_0^2)$ to

the absorbed network $X_i^{\text{abs}} \sim N(\mu_{\text{abs}}, \sigma_{\text{abs}}^2)$. Jeffrey's information, which is computed for all continuous unabsorbed nodes in the network, is given as:

$$J\left(X_i^0, X_i^{\text{abs}}\right) = I^{\text{KL}}\left(X_i^0, X_i^{\text{abs}}\right) + I^{\text{KL}}\left(X_i^{\text{abs}}, X_i^0\right)$$

where

$$I^{\text{KL}}\left(X_i^0, X_i^{\text{abs}}\right) = \frac{1}{2}\left\{\frac{(\mu_0 - \mu_{\text{abs}})^2}{\sigma_0^2} + \frac{\sigma_0^2}{\sigma_{\text{abs}}^2} - \log\left(\frac{\sigma_0^2}{\sigma_{\text{abs}}^2}\right) - 1\right\}.$$

For ease of interpretation, the signed Jeffrey's information

$$\text{sign}(\mu_0 - \mu_{\text{abs}}) \cdot J\left(X_i^0, X_i^{\text{abs}}\right)$$

is used to demonstrate the direction of change after the absorption of evidence.

The changes in belief are measured only for the nodes that are d-connected (conditionally dependent) to the entered evidence. Nodes that are d-separated from absorbed evidence are not influenced, and, consequently, do not change beliefs [5].

4.1.3 Mouse Kidney eQTL Example

Suppose the marginal mean of the node `Tlr12` is known to be -0.99 and we wish to enter this new information in the mouse network and compute the updated states of other nodes. New evidence for single or multiple nodes can be entered using the function `absorb.gnbp` which absorbs evidence and propagates the beliefs. The input to `absorb.gnbp` is an object of class `gpfit`, that is the output returned by the function `fit.gnbp`.

The function `absorb.gnbp` uses the `RHugin` package to absorb evidence in the specified nodes and update the beliefs of all nodes and then calculates Jeffrey's signed information for all d-connected nodes. The following example illustrates how to absorb evidence in a genotype-phenotype network.

1. Absorb a single evidence for a single node

```
> mouse.cgbn<-fit.gnbp(mousegeno,mousepheno,alpha=0.1)
> ## Absorb evidence
> absorb.gnbp(mouse.cgbn,node="Tlr12",evidence=matrix(-0.99))

$gp
  A Hugin domain: there are 19 nodes and 31 edges
```

```
$gp_flag
[1] "cg"

$gp_nodes
          node       class      levels type
 [1,] "Cyp4a31" "numeric" "0"    "pheno"
 [2,] "Slc5a9"  "numeric" "0"    "pheno"
 [3,] "Slc6a9"  "numeric" "0"    "pheno"
 [4,] "Hmgcl"   "numeric" "0"    "pheno"
 [5,] "Ptp4a2"  "numeric" "0"    "pheno"
 [6,] "Ak2"     "numeric" "0"    "pheno"
 [7,] "Zbtb8a"  "numeric" "0"    "pheno"
 [8,] "Stx12"   "numeric" "0"    "pheno"
 [9,] "Trspap1" "numeric" "0"    "pheno"
[10,] "Mecr"    "numeric" "0"    "pheno"
[11,] "Wdtc1"   "numeric" "0"    "pheno"
[12,] "Atpif1"  "numeric" "0"    "pheno"
[13,] "Rbbp4"   "numeric" "0"    "pheno"
[14,] "Tlr12"   "numeric" "0"    "pheno"
[15,] "Qchr4"   "factor"  "3"    "geno"
[16,] "Qchr17"  "factor"  "3"    "geno"
[17,] "Qchr15"  "factor"  "3"    "geno"
[18,] "Qchr11"  "factor"  "3"    "geno"
[19,] "Qchr2"   "factor"  "3"    "geno"

$evidence
      [,1]
[1,] -0.99

$node
[1] "Tlr12"

$marginal
$marginal$pheno
$marginal$pheno$mean
                [,1]
Rbbp4    2.317482e-17
Atpif1   2.190113e-03
Wdtc1    2.514671e-17
Mecr    -1.551256e-16
Trspap1  4.239712e-03
```

```
Stx12    4.433032e-17
Zbtb8a  -2.003327e-17
Ak2     -7.153821e-03
Ptp4a2   3.519799e-03
Hmgcl   -7.136515e-03
Slc6a9  -1.957688e-02
Slc5a9   2.471620e-02
Cyp4a31  1.914642e-02


$marginal$pheno$var
            [,1]
Rbbp4   0.9557443
Atpif1  0.9027874
Wdtc1   0.9574396
Mecr    0.9550281
Trspap1 0.8530483
Stx12   0.9575380
Zbtb8a  0.9551227
Ak2     0.7696464
Ptp4a2  0.8550665
Hmgcl   0.8509102
Slc6a9  0.7939058
Slc5a9  0.8538129
Cyp4a31 0.8965621



$marginal$geno
$marginal$geno$freq
        state1    state2    state3
Qchr4 0.2312139 0.4682081 0.300578



$belief
$belief$pheno
$belief$pheno$mean
        ev= -0.99
Rbbp4    0.8776457
Atpif1  -0.6538109
Wdtc1    0.6669131
Mecr    -0.8791569
```

```
Trspap1 -0.6613503
Stx12    0.8676931
Zbtb8a  -0.1222389
Ak2      0.6720433
Ptp4a2  -0.6969352
Hmgcl    0.6855139
Slc6a9   0.5667517
Slc5a9  -0.6510656
Cyp4a31 -0.5043484


$belief$pheno$var
        ev= -0.99
Rbbp4   0.4859803
Atpif1  0.6226163
Wdtc1   0.6627283
Mecr    0.4428854
Trspap1 0.5679888
Stx12   0.4933635
Zbtb8a  0.8083572
Ak2     0.5327134
Ptp4a2  0.5448964
Hmgcl   0.5628789
Slc6a9  0.5718937
Slc5a9  0.5254673
Cyp4a31 0.6995273



$belief$geno
$belief$geno$state1
        ev= -0.99
Qchr4 0.007944801

$belief$geno$state2
      ev= -0.99
Qchr4 0.2152284

$belief$geno$state3
      ev= -0.99
Qchr4 0.7768268
```

```
$JSI
          ev= -0.99
Rbbp4    0.71650239
Atpif1  -0.32687548
Wdtc1    0.31813768
Mecr    -0.79365404
Trspap1 -0.36674950
Stx12    0.69209864
Zbtb8a  -0.01550701
Ak2      0.40056441
Ptp4a2  -0.42017671
Hmgcl    0.39734466
Slc6a9   0.28567820
Slc5a9  -0.41106696
Cyp4a31 -0.18983139


$FC
NULL


attr(,"class")
[1] "gnbp"
```

Note that the function `absorb.gnbp` requires the argument `evidence` to be of class matrix. If only a single value of evidence is to be entered, this can be done by simply using the function matrix(), as above.

`absorb.gnbp` returns an object of class "gnbp" which is a list of several variables. The Jeffrey's signed information is returned as a matrix `JSI` that gives the quantified comparison of beliefs of the continuous nodes (phenotypes) before and after evidence absorption. Since we absorbed only a single value of evidence, `JSI` is a column vector.In addition to Jeffrey's signed information, the marginal distributions (mean and variance for continuous nodes in and genotype frequencies for SNP markers) before evidence absorption and the updated beliefs (after evidence absorption) are also returned. The variable `FC` is for discrete bayesian networks (see Section 4.2) and is returned with a NULL value for CG-BN.

Since Qchr15 is d-separated when evidence is absorbed in `Tlr12`, it's marginal distribution is not affected and hence the beliefs are not calculated. Qchr4, on the other hand is d-connected and a list returns the updated frequencies of all 3 genotype states of the SNP marker Qchr15.

2. Absorb a sequence of evidence for a single node

```
> mouse.cgbn<-fit.gnbp(mousegeno,mousepheno,alpha=0.1)
> ##Absorb evidence
> absorb.gnbp(mouse.cgbn,node="Tlr12",evidence=t(matrix(c(2.5,3,3.5,4))))
```

A function `gen.evidence` is useful to generate evidence for a node based on it's marginal distribution. This is particularly useful when network perturbation to assess the network behaviour is of interest.

To generate a spectrum of evidence for `Tlr12` within ± 2 standard deviations of it's marginal distribution, we input the inferred network to `gen.evidence`.

```
> mouse.cgbn<-fit.gnbp(mousegeno,mousepheno,alpha = 0.1)
> ##Generate evidence
> ev<-gen.evidence(mouse.cgbn,node="Tlr12",std=2,length.out=20)
> ##absorb evidence
> absorb.gnbp(mouse.cgbn,node="Tlr12",evidence=ev)
```

Note that `JSI` is a matrix whose number of rows are the d-connected phenotype nodes to `Tlr12` and the number of columns is the length of evidence absorbed in `Tlr12`.

When a sequence of evidence is absorbed for a single node in the network, `absorb.gnbp` also plots the JSI of the d-connected nodes vs the evidence absorbed.
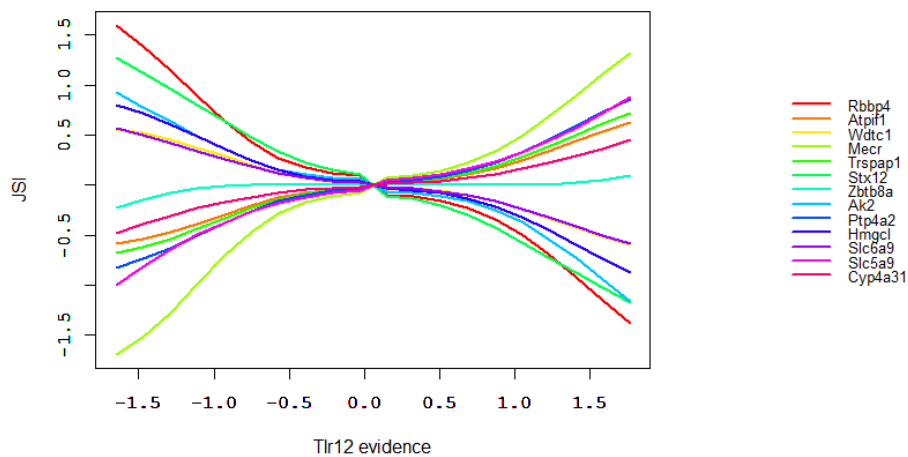

Figure 5. Plot produced by `absorb.gnbp`

23

4.2 Discrete Bayesian Networks

4.2.1 Belief propagation and Fold change (FC)

In Discrete Bayesian Networks, phenotype nodes are represented as $\{X_1, X_2, \ldots, X_p\}$. A node X_i, has the states, $X_i \in \{s_1, s_2, \ldots, s_n\}$, where $\sum_{k=1}^{n} s_k = 1$. Let $X_i^0 = \{s_1^0, s_2^0, \ldots s_n^0\}$ denote the states of X_i in the initial network, and $X_i^{pert} \in \{s_1^{pert}, s_2^{pert}, \ldots s_n^{pert}\}$ denotes the states of X_i in the perturbed network.

The node-wise change in marginals is quantified simply by the Fold Change (FC) as a measure of effect size for the state of maximal probability in the perturbed network. Let I^* be an indicator for the state of X_i^{pert} with maximum probability. That is, $I^* = 1$ if $s_k^{pert} = \max P(s_k^{pert})$, and 0 otherwise. The node-wise change in marginals is:

$$FC(X_i) = I^* \cdot \frac{P(s_k^{pert})}{P(s_k^0)}.$$

Note that $FC \in [0, 1)$ when the node is inhibited, $FC = 1$ when the node stays the same, and $FC > 1$ when the node is activated.

4.2.2 Yeast example

Consider the yeast network inferred in Section 3.2. The phenotypes are discrete variables with 2 states (1,-1) in `yeast` dataset. Suppose we want to evaluate the system wide changes if *COX10* values are known. Like fit methods, there are two ways to absorb the phenotypic evidence in discrete bayesian networks, the function `absorb.dbn` that implements `gRain` or `absorb.gnbp` that implements `RHugin`. `absorb.gnbp` can be used with objects of class `gpfit` that are output from `fit.gnbp`. The implementation is similar to the CG-BN example (refer to Section 4.1.), the only difference being `FC` returned as a matrix of fold changes and `JSI` is returned with a NULL value. This section focuses on abosorbing evidence using `absorb.dbn`.

```
> ## Fit the network
> yeast.dbn<-fit.dbn(yeastgeno,yeastpheno)
> ##Absorb evidence
> yeast.dbn.abs<-absorb.dbn(yeast.dbn,"COX10",matrix(c("-1","1"),ncol=2))

> yeast.dbn.abs
$gp
Independence network: Compiled: FALSE Propagated: FALSE
  Nodes: chr [1:50] "HEM3" "BAP2" "ERG9" "PHA2" "ERG6" "ERG12" "TAT1" "FLX1" "MSY1"
```

24

```
$gp_flag
[1] "db"


$gp_nodes
        node       class     levels  type
 [1,] "HEM3"     "factor" "2"     "pheno"
 [2,] "BAP2"     "factor" "2"     "pheno"
 [3,] "ERG9"     "factor" "2"     "pheno"
 [4,] "PHA2"     "factor" "2"     "pheno"
 [5,] "ERG6"     "factor" "2"     "pheno"
 [6,] "ERG12"    "factor" "2"     "pheno"
 [7,] "TAT1"     "factor" "2"     "pheno"
 [8,] "FLX1"     "factor" "2"     "pheno"
 [9,] "MSY1"     "factor" "2"     "pheno"
[10,] "GRX5"     "factor" "2"     "pheno"
[11,] "VMA13"    "factor" "2"     "pheno"
[12,] "LAT1"     "factor" "2"     "pheno"
[13,] "NCP1"     "factor" "2"     "pheno"
[14,] "SLM5"     "factor" "2"     "pheno"
[15,] "MSE1"     "factor" "2"     "pheno"
[16,] "ALD6"     "factor" "2"     "pheno"
[17,] "HIS3"     "factor" "2"     "pheno"
[18,] "NAM2"     "factor" "2"     "pheno"
[19,] "ACS1"     "factor" "2"     "pheno"
[20,] "YNL045W"  "factor" "2"     "pheno"
[21,] "RBK1"     "factor" "2"     "pheno"
[22,] "YMR293C"  "factor" "2"     "pheno"
[23,] "LCB4"     "factor" "2"     "pheno"
[24,] "PPA2"     "factor" "2"     "pheno"
[25,] "DIA4"     "factor" "2"     "pheno"
[26,] "MIR1"     "factor" "2"     "pheno"
[27,] "YEL047C"  "factor" "2"     "pheno"
[28,] "MSK1"     "factor" "2"     "pheno"
[29,] "TRP3"     "factor" "2"     "pheno"
[30,] "THI22"    "factor" "2"     "pheno"
[31,] "TNA1"     "factor" "2"     "pheno"
[32,] "MSD1"     "factor" "2"     "pheno"
[33,] "YER152C"  "factor" "2"     "pheno"
[34,] "TAT2"     "factor" "2"     "pheno"
[35,] "TYS1"     "factor" "2"     "pheno"
```

```
[36,] "YAT2"    "factor" "2"    "pheno"
[37,] "YEL041W" "factor" "2"    "pheno"
[38,] "COX10"   "factor" "2"    "pheno"
[39,] "Qchr4"   "factor" "2"    "geno"
[40,] "Qchr3"   "factor" "2"    "geno"
[41,] "Qchr12"  "factor" "2"    "geno"
[42,] "Qchr14"  "factor" "2"    "geno"
[43,] "Qchr2"   "factor" "2"    "geno"
[44,] "Qchr5"   "factor" "2"    "geno"
[45,] "Qchr9"   "factor" "2"    "geno"
[46,] "Qchr16"  "factor" "2"    "geno"
[47,] "Qchr8"   "factor" "2"    "geno"
[48,] "Qchr13"  "factor" "2"    "geno"
[49,] "Qchr1"   "factor" "2"    "geno"
[50,] "Qchr15"  "factor" "2"    "geno"

$evidence
     [,1] [,2]
[1,] "-1" "1"

$node
[1] "COX10"

$marginal
$marginal$pheno
$marginal$pheno$freq
       state1 state2
HEM3    0.504  0.496
BAP2    0.500  0.500
PHA2    0.494  0.506
ERG6    0.500  0.500
ERG12   0.492  0.508
TAT1    0.492  0.508
FLX1    0.484  0.516
MSY1    0.499  0.501
GRX5    0.495  0.505
VMA13   0.485  0.515
LAT1    0.489  0.511
NCP1    0.498  0.502
SLM5    0.489  0.511
MSE1    0.480  0.520
```

```
ALD6     0.507  0.493
HIS3     0.480  0.520
NAM2     0.499  0.501
ACS1     0.504  0.496
YNL045W  0.470  0.530
RBK1     0.497  0.503
YMR293C  0.502  0.498
LCB4     0.503  0.497
PPA2     0.499  0.501
DIA4     0.493  0.507
MIR1     0.492  0.508
YEL047C  0.500  0.500
MSK1     0.499  0.501
TRP3     0.489  0.511
THI22    0.499  0.501
TNA1     0.496  0.504
MSD1     0.493  0.507
YER152C  0.503  0.497
TAT2     0.500  0.500
TYS1     0.499  0.501
YAT2     0.490  0.510


$marginal$geno
$marginal$geno$freq
      state1 state2
Qchr3   0.464  0.536
Qchr2   0.571  0.429
Qchr16  0.527  0.473
Qchr13  0.491  0.509



$belief
$belief$pheno
$belief$pheno$state1
       ev= -1  ev= 1
HEM3    0.525 0.4826
BAP2    0.492 0.5080
PHA2    0.562 0.4244
ERG6    0.500 0.5002
```

```
ERG12     0.463 0.5203
TAT1      0.493 0.4911
FLX1      0.545 0.4220
MSY1      0.903 0.0902
GRX5      0.611 0.3785
VMA13     0.269 0.7030
LAT1      0.431 0.5475
NCP1      0.418 0.5788
SLM5      0.880 0.0943
MSE1      0.712 0.2463
ALD6      0.510 0.5040
HIS3      0.465 0.4953
NAM2      0.783 0.2125
ACS1      0.540 0.4662
YNL045W   0.308 0.6330
RBK1      0.212 0.7851
YMR293C   0.893 0.1071
LCB4      0.502 0.5032
PPA2      0.758 0.2377
DIA4      0.758 0.2247
MIR1      0.596 0.3881
YEL047C   0.356 0.6463
MSK1      0.802 0.1927
TRP3      0.479 0.4988
THI22     0.499 0.4990
TNA1      0.581 0.4098
MSD1      0.795 0.1887
YER152C   0.471 0.5353
TAT2      0.672 0.3259
TYS1      0.389 0.6101
YAT2      0.462 0.5187

$belief$pheno$state2
       ev= -1 ev= 1
HEM3     0.4750 0.517
BAP2     0.5079 0.492
PHA2     0.4379 0.576
ERG6     0.4996 0.500
ERG12    0.5367 0.480
TAT1     0.5074 0.509
FLX1     0.4552 0.578
```

```
MSY1    0.0971 0.910
GRX5    0.3889 0.621
VMA13   0.7312 0.297
LAT1    0.5686 0.452
NCP1    0.5818 0.421
SLM5    0.1204 0.906
MSE1    0.2879 0.754
ALD6    0.4904 0.496
HIS3    0.5350 0.505
NAM2    0.2166 0.787
ACS1    0.4595 0.534
YNL045W 0.6919 0.367
RBK1    0.7875 0.215
YMR293C 0.1071 0.893
LCB4    0.4979 0.497
PPA2    0.2419 0.762
DIA4    0.2424 0.775
MIR1    0.4045 0.612
YEL047C 0.6439 0.354
MSK1    0.1978 0.807
TRP3    0.5215 0.501
THI22   0.5007 0.501
TNA1    0.4194 0.590
MSD1    0.2051 0.811
YER152C 0.5288 0.465
TAT2    0.3281 0.674
TYS1    0.6110 0.390
YAT2    0.5383 0.481


$belief$geno
$belief$geno$state1
       ev= -1 ev= 1
Qchr3   0.471 0.458
Qchr2   0.573 0.570
Qchr16  0.603 0.450
Qchr13  0.490 0.492

$belief$geno$state2
       ev= -1 ev= 1
Qchr3   0.529 0.542
```

```
Qchr2   0.427 0.430
Qchr16  0.397 0.550
Qchr13  0.510 0.508



$FC
$FC$FC
        ev= -1 ev= 1
HEM3     1.042 1.043
BAP2     1.016 1.016
PHA2     1.139 1.137
ERG6     1.000 1.000
ERG12    1.056 1.058
TAT1     0.999 1.002
FLX1     1.126 1.120
MSY1     1.811 1.815
GRX5     1.234 1.232
VMA13    1.419 1.450
LAT1     1.113 1.119
NCP1     1.159 1.162
SLM5     1.799 1.772
MSE1     1.482 1.450
ALD6     1.006 0.994
HIS3     1.029 0.971
NAM2     1.569 1.573
ACS1     1.073 1.075
YNL045W  1.305 1.348
RBK1     1.567 1.579
YMR293C  1.778 1.793
LCB4     0.999 1.001
PPA2     1.519 1.522
DIA4     1.538 1.528
MIR1     1.210 1.205
YEL047C  1.289 1.291
MSK1     1.608 1.611
TRP3     1.020 0.980
THI22    1.000 1.000
TNA1     1.171 1.170
MSD1     1.611 1.601
YER152C  1.064 1.064
```

```
TAT2      1.344 1.348
TYS1      1.220 1.223
YAT2      1.056 1.058

$FC$pheno_state
        ev= -1 ev= 1
HEM3          1      2
BAP2          2      1
PHA2          1      2
ERG6          1      1
ERG12         2      1
TAT1          2      2
FLX1          1      2
MSY1          1      2
GRX5          1      2
VMA13         2      1
LAT1          2      1
NCP1          2      1
SLM5          1      2
MSE1          1      2
ALD6          1      1
HIS3          2      2
NAM2          1      2
ACS1          1      2
YNL045W       2      1
RBK1          2      1
YMR293C       1      2
LCB4          1      1
PPA2          1      2
DIA4          1      2
MIR1          1      2
YEL047C       2      1
MSK1          1      2
TRP3          2      2
THI22         2      2
TNA1          1      2
MSD1          1      2
YER152C       2      1
TAT2          1      2
TYS1          2      1
YAT2          2      1
```

31

```
attr(,"class")
[1] "dbn"
```

The output of `absorb.dbn` is an object of class "dbn" list of several variables similar to that of `absorb.gnbp`. Variables of interest are `marginal`, `belief` and `FC`. The conditional probabilities before absorbing evidence are returned in `marginal` while updated beliefs after evidence absorption are returned in `belief`. `FC` is a list of two variables: 1.`FC` - matrix of fold changes of phenotypes 2. `state` - the phenotype state with maximum probability (the index of `belief` with higher value is returned).

5 Visualizing network changes

The most important aspect of the package is visualizing the effect of node perturbations or evidence absorption on the network. To visualize the changes, a generic plot method for plotting the genotype-phenotype network in which evidence has been absorbed and propagated is available. The plot method will convert network into an object of class "graphNEL" by using `Rgraphviz` package. The argument `nodeAttrs` to plot method for graph objects in `Rgraphviz` package is then used to customize the plot.

5.1 A complete example of CG-BN

For CG-BN, a generic plot method `plot.gnbp` will be called for objects of class "gnbp". A complete example that fits a CG-BN, absorbs evidence and plots the network:

```
> mouse.cgbn<-fit.gnbp(mousegeno,mousepheno,alpha=0.1)
> mouse.cgbn<-absorb.gnbp(mouse.cgbn,node="Tlr12",evidence=matrix(-0.99))
> plot(mouse.cgbn)
```
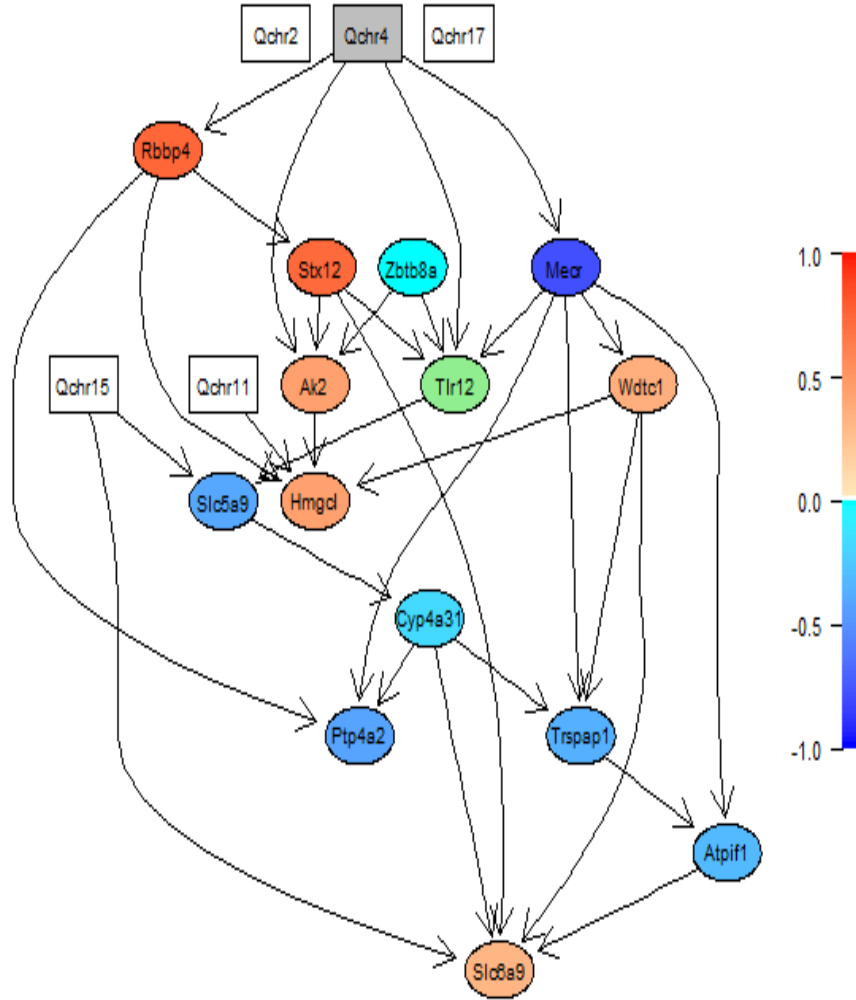
Figure 6. Evidence absorption in single node

The plot method will draw the network with Jeffrey's signed information mapped onto it by a colormap. There is an option to plot beliefs (updated marginal means) which can be entered through the argument `y` (see help for `plot.gnbp`).

The *d*-separated nodes are white while the colored nodes are *d*-connected, with the color indicating the strength and direction of change . By default, the continuous nodes are of shape "ellipse" and a "box" shape is used for discrete nodes. The node for which evidence is absorbed is colored green (default color).

5.1.1 Plot options in plot.gnbp

Colormap options such as end colors for the positive and negative gradients and the resolution can be customized. The resolution of the colormap can be specified by `col.length`. The argument `col.palette` can be used to specify the end colors.

```
> col.palette<-list(pos_high="darkgreen", pos_low= "palegreen2",
                    neg_high="wheat1", neg_low = "red",
                    dsep_col="white",qtl_col="grey",node_abs_col="yellow")
> plot(network,col.palette=col.palette)
```
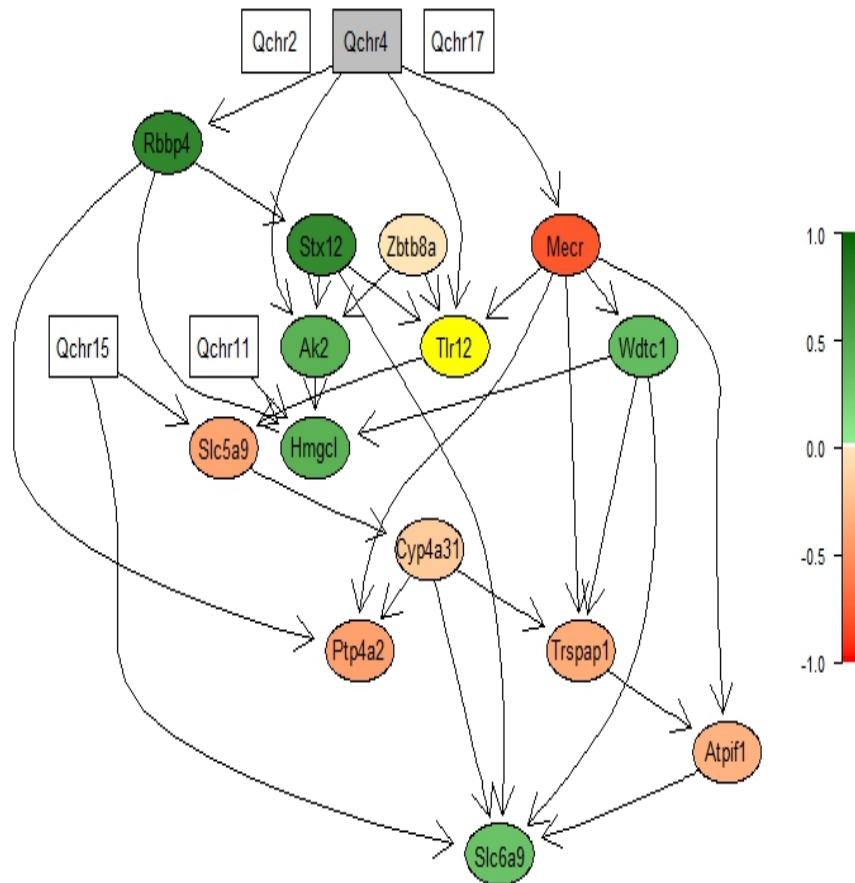

Figure 7. Mouse network with custom color palette

The plot method will always map the JSI or beliefs onto the network for a single piece of evidence. Incase a spectrum of evidence is absorbed for a single/multiple node(s), then

34

the evidence for which we wish to visualize the network changes can be chosen by specifying the corresponding column number of JSI or belief matrix through the argument `ncol`.

For example if we absorbed a sequence of evidence for `Tlr12` and we wish to visualize the belief changes for evidence = 1.767, we can do this as follows.

```
> network<-fit.gnbp(mousegeno,mousepheno,alpha = 0.1)
> ##Generate evidence
> evidence<-gen.evidence(network,node="Tlr12",std=2,length.out=20)
> network<-absorb.gnbp(network,node="Tlr12",evidence=evidence)
> plot(x=network,y="belief",ncol=20)
```

5.2   A complete example of discrete networks

For discrete bayesian networks, a generic plot method is available for both "gnbp" and "dbn" objects. This section focuses on plotting "dbn" objects. A complete example that fits a CG-BN, absorbs evidence and plots the network:

```
> ##load data
> data(yeast)
> ## get genotype and phenotype data
> yeastgeno<-yeast[,1:12]
> yeastpheno<-yeast[,13:50]
> ## Fit discrete network
> yeast.dbn<-fit.dbn(yeastgeno,yeastpheno)
> ## Absorb evidence
> yeast.dbn.abs<-absorb.dbn(yeast.dbn,"COX10",matrix(c("-1","1"),ncol=2))
> ## Plot the network
> plot(yeast.dbn.abs,ncol=2)
```
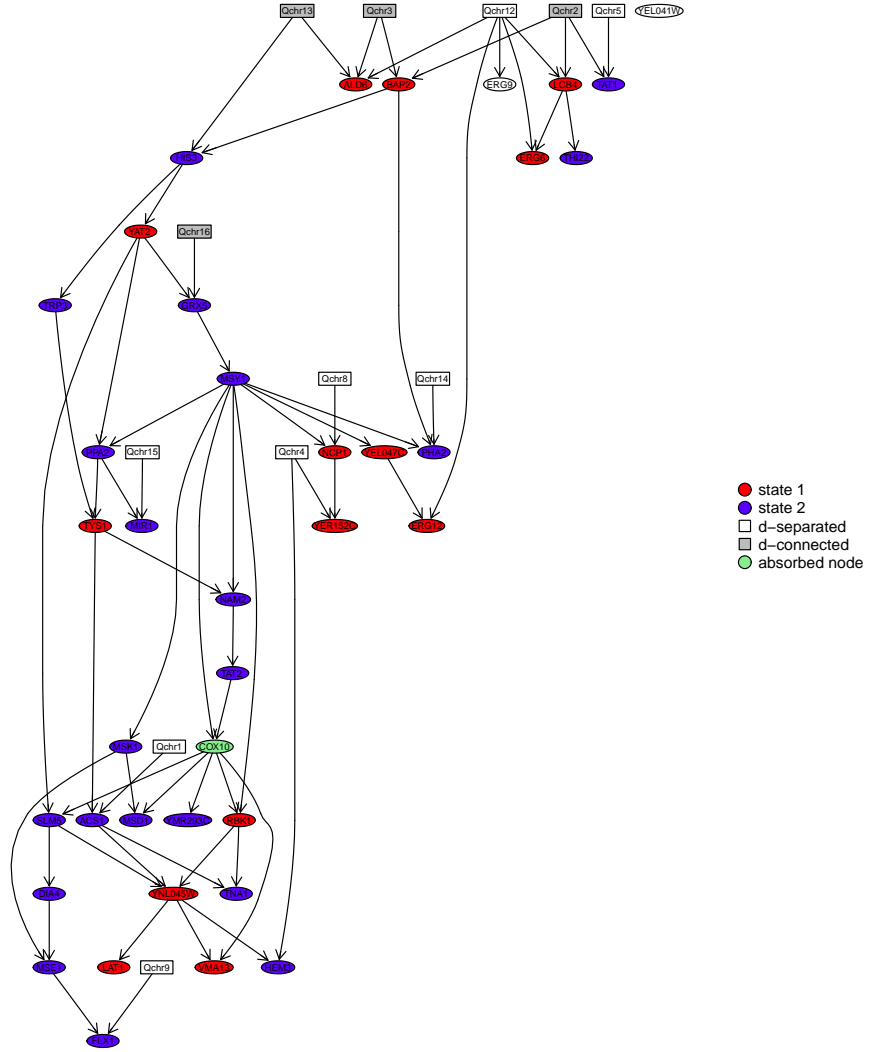
Figure 8. Yeast network after absorbing evidence ($COX10$="1")

The plot method will map the phenotype states with maximum probability on the network by a colormap. The d-separated nodes are white while the colored nodes are d-connected, with the color indicating the direction of change . By default, the continuous nodes are of shape "ellipse" and a "box" shape is used for discrete nodes. The node for which evidence is absorbed is colored green (default color).

There is also an option to plot Fold Changes (FC) which can be entered through the argument y (see help for `plot.gnbp`).
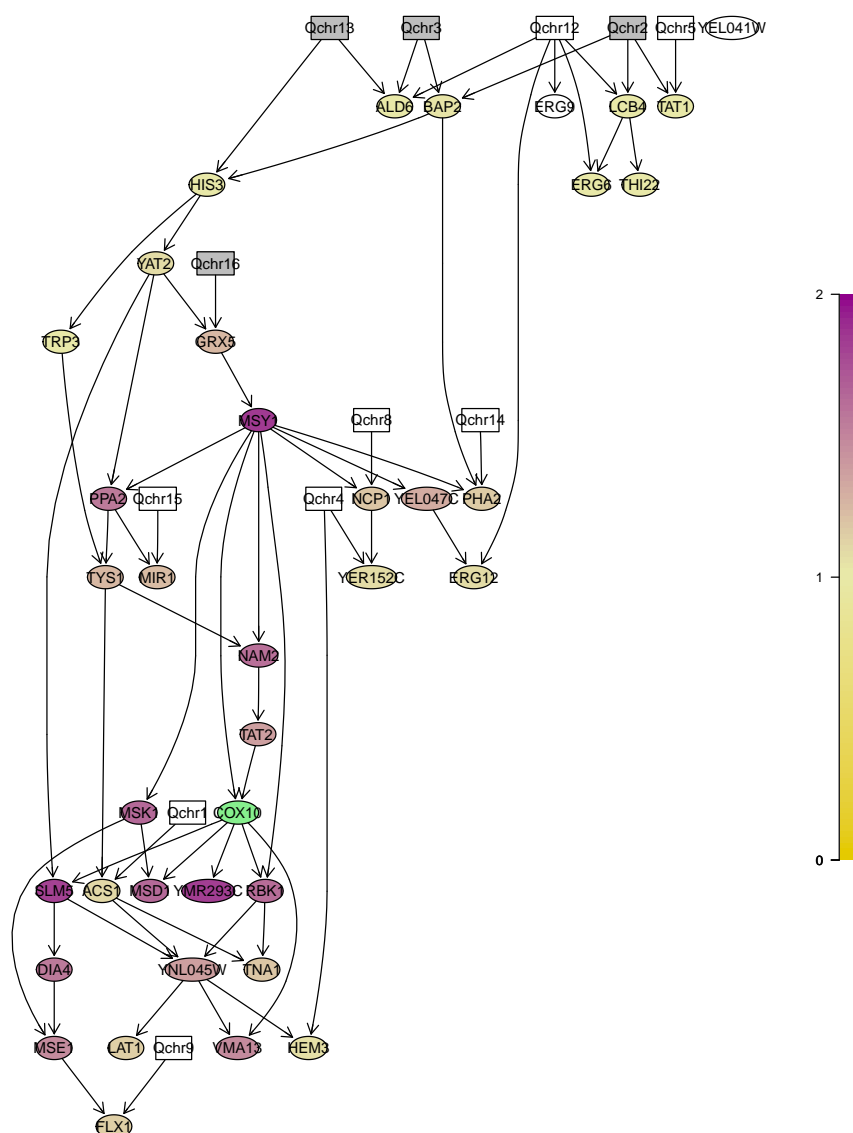
```
> plot.dbn(yeast.dbn.abs,y="FC",ncol=2)
```


Figure 9. Fold Changes in Yeast network after absorbing evidence (*COX10*="1")

When y="FC" is specified, the fold changes for the specified column (evidence) are mapped on the network. FC are positive values. FC of 1 indicates no change from the marginal, greater than 1 indicates the updated mean is higher than the marginal mean while less than 1 indicates vice-versa.

6 Specifying Additional Biological Information

If additional biological information is known such as known or forbidden interactions between variables or the network hierarchy, it can be incorporated into the learning process. Such information can be provided in the `constraints` option of `fit.gnbp` and as `whitelist` and/or `blacklist` in `fit.dbn`. An example illustrating this:

Fit a CG-BN to `hdl` data using `fit.gnbp`. To do this, load the data.

```
> ## load data
> data(hdl)
> ##get the genotype and phenotype data
> hdlgeno<-hdl[,1:5]
> hdlpheno<-hdl[,6:15]
```

This dataset has 5 SNP markers and 10 phenotypes that include HDL levels and 9 genes. Since HDL levels is the observed characteristic, the genes should precede HDL in the network. In other words, HDL should be downstream and cannot be a parent of other variables in the network. This information can be included in the learning process by providing a list of constraints that defines the edges **from** HDL **to** genes as forbidden.

```
> ## create an empty vector for the blacklist
> blackL<-c()
> # fill in the forbidden edges. For example :"HDL"->"Nr1i3"
> for(i in 2:dim(hdlpheno)[2])
+ blackL=rbind(blackL,cbind(colnames(hdlpheno)[1],colnames(hdlpheno)[i]))
> ## Form a list
> directed.forbidden <- vector("list", nrow(blackL))
> for (i in 1:nrow(blackL))
+    directed.forbidden[[i]] <- blackL[i,]
> constraints<-list(directed=list(forbidden=directed.forbidden,
+                                 required=NULL), undirected=NULL)
> ## Fit a CG-BN
> hdl.cgbn<-fit.gnbp(hdlgeno,hdlpheno,constraints=constraints,alpha=0.08)
> ## Plot the network
> plot(hdl.cgbn)
```
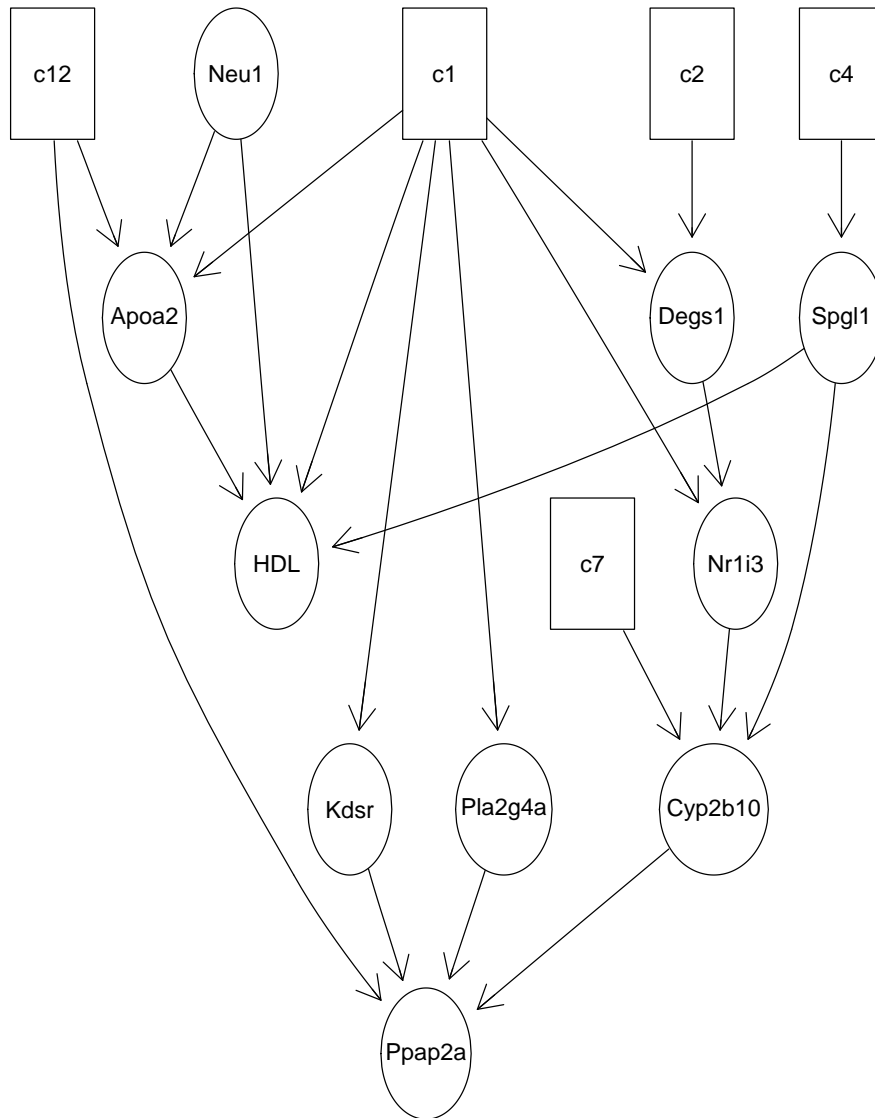
Figure 10. HDL network

As desired, HDL is downstream of the genes in the network. More help about the structure of the constraints list can be found in RHugin documentation. For `fit.dbn`, the `whitelist` option can be used to specify the required edges while the `blacklist` option can be used to specify forbidden edges.

7 Belief propagation in known networks

Belief propagation can be implemented in known genotype-phenotype networks. If the network structure is known apriori from a knowledge database, then learning step can be skipped in `fit.gnbp` by setting `learn = FALSE`. The conditional probabilities will still need to be learnt. This section demonstrates how to specify known networks and subsequent belief propagation.

7.1 Specifying graphNEL objects

One way to specify a known network is to provide the graph structure directly as an input (a graphNEL object) to the fit methods. The following example illustrates how to input a known graph structure using the `fit.dbn` function. Consider a discrete bayesian network implementation of HDL network. Assume that the HDL network structure is known. We will input the structure that we learnt in the previous section to `fit.dbn`.

```
> ## Convert the RHugindomain to a graphNEL object
> bngraph<-RHugin::as.graph.RHuginDomain(hdl.cgbn$gp)
```

For discrete bayesian network, discretize the phenotypes around median. To fit the network parameters, set `learn==FALSE` and specify the graph.

```
> ## discretize the data around median
> hdlpheno_dis<-hdlpheno
> for (i in 1:dim(hdlpheno)[2])
+ {
+   hdlpheno_dis[which(hdlpheno[,i]>=median(hdlpheno[,i])),i]<-"1"
+   hdlpheno_dis[which(hdlpheno[,i]<median(hdlpheno[,i])),i]<-"-1"
+   hdlpheno_dis[,i]<-as.factor(hdlpheno_dis[,i])
+ }
> ## fit dbn
> hdl.dbn<-fit.dbn(hdlgeno,hdlpheno_dis,graph=bngraph,learn ="FALSE")
```

7.2 Specifying edges

The second way to specify an existing network is by providing a data frame of edges. Consider the `toy` network in Section 2. The interactions between the variables in the `toy` dataset are known. To specify the toy network as a CG-BN and learn the conditional probabilities:

First create a data frame of known edges from parent to child.

```
>   ## Load the toy dataset
>   data(toy)
> ## Create a matrix of edges ("from (parent)", "to (child)")
> edgelist=data.frame(matrix(NA,ncol=2,nrow=10))
> edgelist[1,]<-cbind("Q1","X1")
> edgelist[2,]<-cbind("Q2","X1")
> edgelist[3,]<-cbind("Q2","X2")
> edgelist[4,]<-cbind("Q2","X4")
> edgelist[5,]<-cbind("X1","X2")
> edgelist[6,]<-cbind("Q3","X2")
> edgelist[7,]<-cbind("Q3","X3")
> edgelist[8,]<-cbind("X2","X5")
> edgelist[9,]<-cbind("X2","X6")
> edgelist[10,]<-cbind("X4","X6")
> ## label the columns
> colnames(edgelist)<-c("from","to")
```

In `fit.gnbp` provide the edgelist by setting `graph=edgelist` and set `learn = FALSE`. This will skip the learning and only conditional probabilities will be calculated for each node in the network based on the given network structure and data. Absorbing evidence and propagating the beliefs subsequently is then straightforward.

```
> ## Specify the network and learn conditional probabilities
> toy.cgbn<-fit.gnbp(toygeno,toypheno,learn=FALSE,graph=edgelist)
> ##Generate evidence
> evidence<-gen.evidence(toy.cgbn,node="X2",std=2,length.out=20)
> toy.cgbn.abs<-absorb.gnbp(toy.cgbn,node="X2",evidence=evidence)
> plot(x=toy.cgbn.abs,y="JSI",ncol=17,fontsize = 5)
```
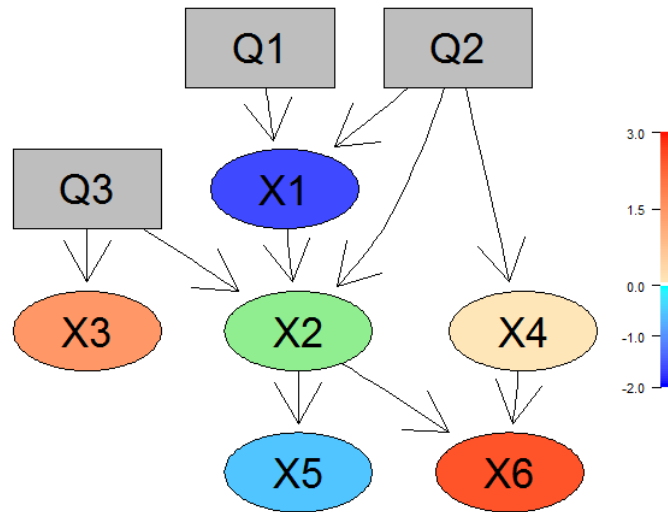
Figure 11. Belief propagation in known network

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