# Displaying model fits in Lattice plots

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lattice is an add-on package for R that implements Trellis graphics (originally developed for S and S-PLUS). It is a powerful and elegant high-level data visualization system, with an emphasis on multivariate data, that is sufficient for typical graphics needs, and is also flexible enough to handle most nonstandard requirements.

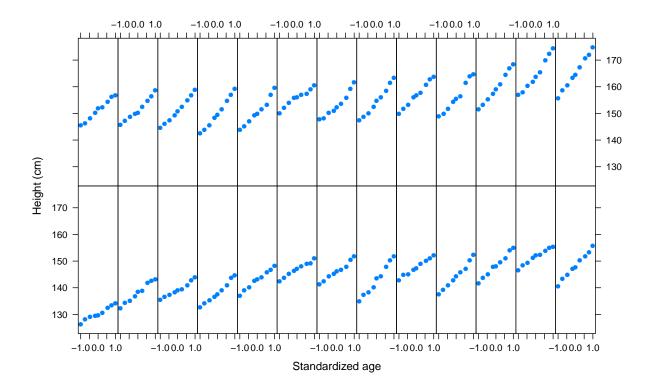
This article discusses the common situation where we want to augment a raw data plot with a model fit. We assume that the reader is familiar with the basic ideas related to model-fiting in R, and in particular the use of summary(), fitted(), predict(), and related methods. We use two datasets for our examples.

The first one is the Oxboys dataset from the nlme package, which records the growth (height) over time of 26 boys from Oxford. Each boy had his height measured on 9 occasions.

- > data(Oxboys, package = "nlme")
  > head(Oxboys, 20)
- age height Occasion Subject 1 -1.0000 140.5 1 2 1 - 0.7479143.4 2 3 1 -0.4630 144.8 3 4 4 1 -0.1643 147.1 5 5 1 -0.0027 147.7 6 6 0.2466 150.2 7 7 0.5562 151.7 8 0.7781 153.3 8 9 9 0.9945 155.8 10 2 -1.0000 136.9 1 2 11 -0.7479139.1 2 -0.4630 3 12 140.1 13 2 - 0.1643142.6 4 14 2 -0.0027 143.2 5 15 0.2466 144.0 6 7 16 2 0.5562 145.8 17 0.7781 146.8 8 9 18 0.9945 148.3 19 3 -1.0000 1 150.0 3 -0.7479 2 20 152.1

A simple Trellis plot of the data can be obtained by

Each panel represents one subject. As the subject identifiers are uninformative, the usual strips on top of each panel is omitted.



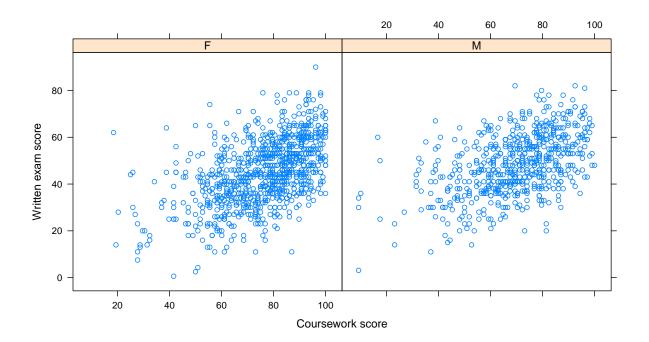
Our objective will be to fit growth curves (possibly nonlinear) to the data and superpose them on the plot.

The second example is the GCSE van dataset from the mlmRev package. This dataset records the GCSE exam scores in a science subject for 1905 students. The marks in two components (course work and written paper) are recorded separately. We are interested in modeling the expected written score based on course work score, taking into account the gender of the student.

```
> data(Gcsemv, package = "mlmRev")
> head(Gcsemv)
```

	school	student	gender	written	course
1		16	М	23	NA
2	20920	25	F	NA	71.2
3	20920	27	F	39	76.8
4	20920	31	F	36	87.9
5	20920	42	М	16	44.4
6	20920	62	F	36	NA

A plot of the raw data is produced by



## Adding to a Lattice display

In both examples, we wish to add to the basic plot of the raw data. In traditional R graphics, one is encouraged to incrementally add components to a plot. The analogue in Lattice graphics is to write panel functions.

## Understanding panel functions

The idea of panel functions may seem intimidating to beginners, but actually they are quite simple. As the name suggests, panel functions are simply R functions (!). They are responsible for drawing the graphical content inside panels. They get executed once for every panel, with the data specific to that panel supplied as arguments. Every high level function has a default panel function, e.g., xyplot() has default panel function panel.xyplot(). Thus, the code that produced the GCSE score plot above is equivalent to

Here "panel.xyplot" is a (predefined) symbol whose value is a function. But creating new functions is not at all difficult in R. Making things a little more complicated, but keeping the results unchanged, we can explicitly define a new inline function, which simply calls panel.xyplot() with exactly the arguments given to it.<sup>1</sup>

Now, to do anything interesting with the data, we need to get access to the raw data for each panel. For each high-level lattice function, such as xyplot(), the raw data is passed to the panel function as specific arguments (which may depend on the high-level function). Looking at the help page for panel.xyplot() tells us that for our example these arguments are x and y. Thus, another equivalent way to create the plot above is

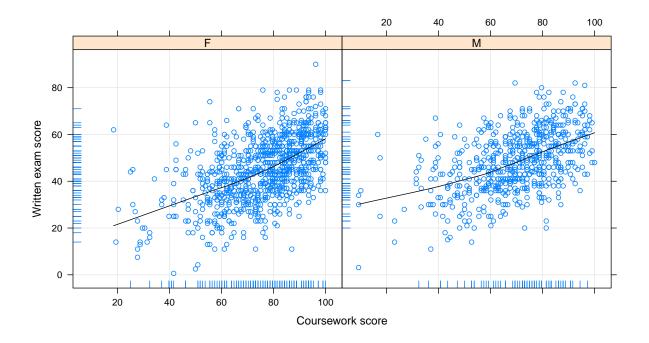
Here, we finally have access to the panel-specific data, but instead of doing anything with it (yet), we have simply called panel.xyplot() with it. Although the sequence of calls so far produce identical results, it is important to understand the concepts that have been introduced to appreciate the next example.

<sup>&</sup>lt;sup>1</sup>The mysterious ... needs some explanation, which we will get to soon.

## A nontrivial panel function

Now that we have access to the data inside the inline panel function we are defining, we can use it to add further elements to the plot. In the following example, we add several elements: a reference grid (which does not really depend on the data), a loess fit, and marginal "rugs" indicating cases where one (but not both) of the score components are missing.

Here the individual elements are added by the component functions panel.grid(), panel.loess(), panel.rug(), etc., which all produce some form of graphical output, based on arguments supplied to it. Together they define a procedure for plotting the data in a panel, encapsulated in the "panel function". Notice that we also needed to include a call to panel.xyplot(), as without it the raw data would not have been plotted. Also notice that panel.grid() is called before it, but panel.loess() after, so that the grid is rendered below the points but the loess fit above. Having the panel function completely control the display allows this kind of fine control.



## Passing arguments through the ... argument

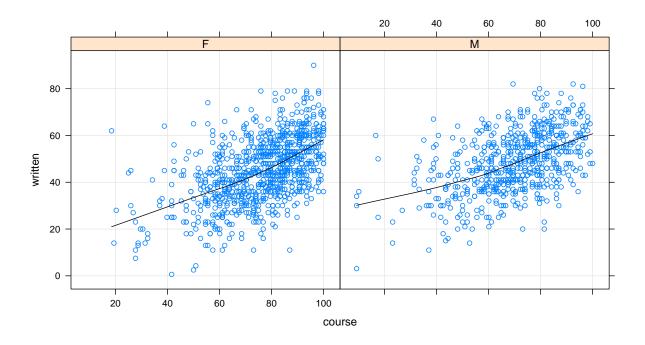
We have used a ... construct in all the panel functions defined above; it is now time to understand how it works. The idea is fairly simple. Functions normally have zero, one, or more named arguments. It can also optionally have a special ... argument. When such a function is called, they can be supplied further arguments not matching the named arguments. These arguments can then be passed on to other functions called by it, where it may match a named argument. The first explicit use of an inline function above provides an example of this:

```
panel = function(...) {
    panel.xyplot(...)
}
```

The panel function is called with arguments named x and y. Although panel itself does not recognize these names, it will dutifully pass them on to panel.xyplot(), which does recognize them.

## Using optional features of predefined panel functions

panel.xyplot() has only two compulsory arguments (x and y), but it has quite a few optional arguments (with appropriate default values) which can modify its behaviour in various ways. In particular, two of its arguments, grid and type, can be used to make it include a background grid and a fitted loess smooth respectively (see help(panel.xyplot) for details). For example, we may write



## Simplifying the call

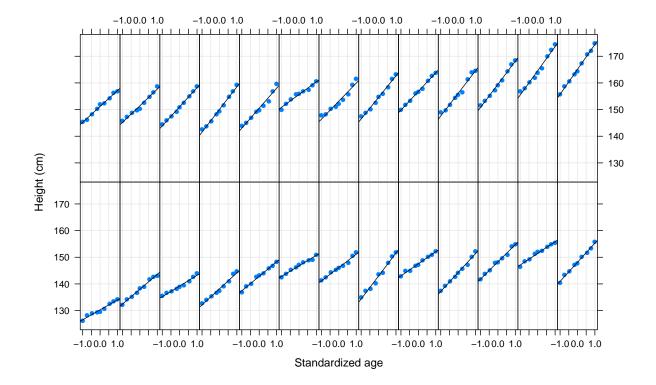
A useful observation is that this is equivalent to

This is a consequence of how xyplot() itself is designed. It has a ... argument, which allows arbitrary additional arguments to be supplied to it. Arguments that are not recognized by xyplot() are passed on to the panel function. Notice how the panel function in the last plot is similar to our initial panel function examples that did nothing special. Following our earlier arguments in reverse, we now see that the above is equivalent to

The end result is thus produced by a call that looks quite simple, and is quite close to the plot produced using the complicated panel function above (except for the rugs). Of course, this approach only works for features already supported by the default panel function (e.g., rugs are not supported by panel.xyplot(), and thus require an explicit panel function), and requires knowledge of what features are available. Still, most of the default panel functions (named as "panel." followed by the high-level function name) do have optional arguments that implement the most common variants, making this a quite useful approach.

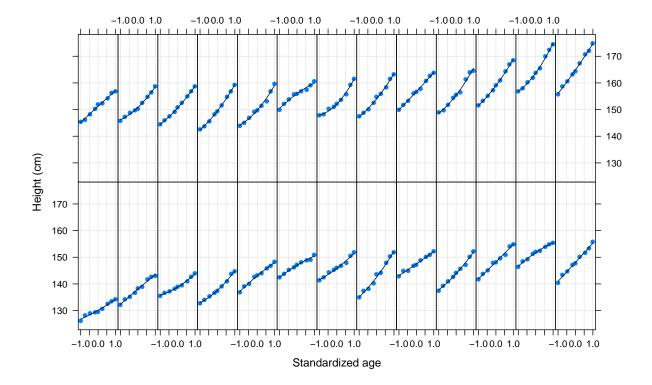
# Back to regression lines

Returning to our original question of how to add model fits, let us next consider the Oxboys dataset. We can of course add a loess smooth to each panel as before, but we wish to stick to parametric models for the remainder of this discussion. The help page for panel.xyplot() tells us that type="r" will add a linear regression line, so we can do



This does not seem completely appropriate though, as we expect growth curves to be nonlinear. Without thinking too much about what kind of nonlinearity would be appropriate, let us start out with a simple quadratic model. We can no longer get away without a panel function, but we can use what we have already learned to come up with

The specific model used here is not important, and we can replace the call to lm() inside the panel function with any other suitable modeling function, provided of course that the model fit uses only the data for that panel. The panel.lines() call draws lines joining its arguments (in the order provided), producing a reasonable approximation of the quadratic curve that we actually want to represent.



## Moving from panel-specific to more general models

The approach taken so far is fundamentally limited in the sense that it can only handle models that are fitted using the within-panel data alone, because that is the only data available to the panel function. In practice, we are often interested in more complex approaches that model the full data. To use such models in a lattice plot, it is simplest to fit the model separately, before attempting to create the plot.

Again, the particular model used is not important for our purposes. For illustration, we will use a mixed effect model that generalizes the quadratic model used above, with common linear and quadratic coefficients, and a subject-specific random intercept. Formally, the model is given by

$$y_{ij} = \alpha_0 + b_i + \alpha_1 x_{ij} + \alpha_2 x_{ij}^2 + \varepsilon_{ij}$$

where i indexes subjects, j indexes repeated measurements (occasion) of a subject,  $x_{ij}$  denotes (standardized) age, and  $y_{ij}$  denotes height. The error terms  $b_i$  and  $\varepsilon_{ij}$  are assumed to be independent, with  $b_i \sim N(0,\tau^2)$  and  $\varepsilon_{ij} \sim N(0,\sigma^2)$ . The parameters in the model are the coefficients  $\alpha_i$  and the variance terms  $\tau^2$  and  $\sigma^2$ . The model can be fit using the lme4 package as follows.

```
> library(lme4)
> fm.mixed <- lmer(height ~ age + I(age^2) + (1 | Subject), data = Oxboys)
```

We might now proceed to view the estimates of the parameters and related numerical quantities; for example, using

```
> summary(fm.mixed)
```

```
Linear mixed model fit by REML
Formula: height ~ age + I(age^2) + (1 | Subject)
  Data: Oxboys
        BIC logLik deviance REMLdev
   AIC
940.7 957.9 -465.3
                         930
                               930.7
Random effects:
Groups
                      Variance Std.Dev.
         Name
Subject (Intercept) 65.570
                               8.0975
Residual
                       1.641
                               1.2810
Number of obs: 234, groups: Subject, 26
Fixed effects:
```

```
Estimate Std. Error t value
(Intercept) 149.0617
                          1.5930
                                   93.57
              6.5152
                          0.1295
                                   50.29
age
I(age^2)
              0.7412
                          0.2264
                                    3.27
```

Correlation of Fixed Effects:

```
(Intr) age
         -0.001
I(age^2) -0.059 -0.020
```

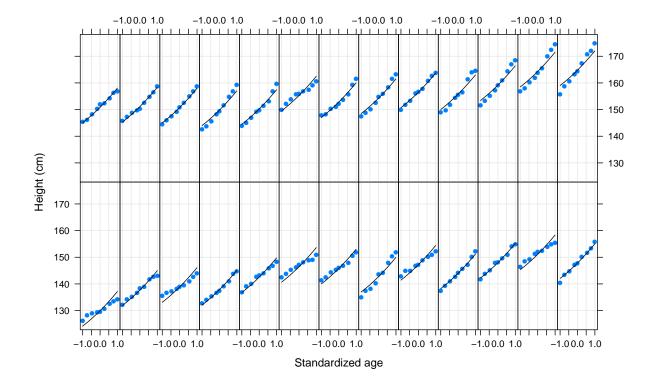
However, our goal is simply to visually incorporate the fitted model in the plot, and all we need for that is the fitted() and predict() (which are closely related) methods for the particular modeling method used. The fitted() function returns the fitted values for the same data that have been used to fit the model. The predict() function can be used to obtain the predicted values for a new set of inputs. If no new data is provided, predict() essentially behaves like fitted().

### Fitted models in panel functions

We now have the fitted model object fm.mixed, and we wish to plot the fitted regression curve in each panel. Two approaches are possible. We can make the fitted model available to the panel function, and then use it as needed. Alternatively, we can augment our dataset with the necessary information before plotting anything. We start with the first approach.

We already know how to make the fitted model available to the panel function: pass it in as an argument not recognized by xyplot(), and it will be passed on to the panel function. Thus, we have

However, this seems unnecessarily complicated. Partly this is due to the use of the lmer() function: as its fitted models do not have a predict() method (for legitimate reasons), we had to manually construct the predictions using the result of coef(). In general, for multipanel plots the current panel will represent some subset of the full dataset, and we would need to somehow figure out the relevant part of the model. Here, for example, we needed to figure out (inside the panel function) which Subject was represented in the panel.

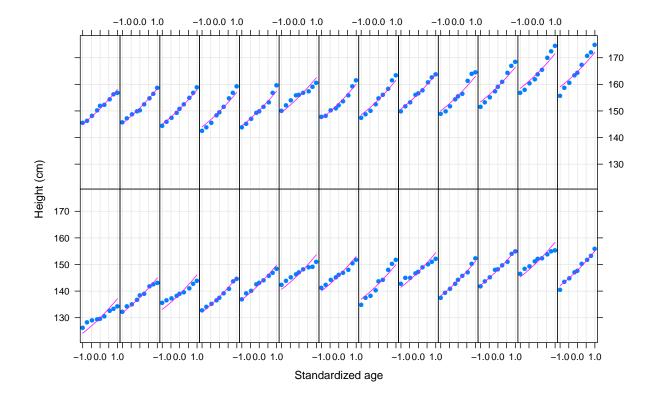


One simpler but fairly general approach works well in this and many other situations. Consider the following example, which produces identical output.

This makes use of two features. First, the fitted() method extracts the fitted values from the model object. This of course corresponds to the full dataset, and is not specific to the panel; it will be a vector with the same length as the number of observation used to fit the model, and will be identical for each panel. The second piece is the subscripts argument, which lattice passes to the panel function, containing the indices of the observations in the original dataset that end up in the panel. This is used to extract the corresponding elements of fitted(fit).

An interesting corollary of this approach is the following trick.

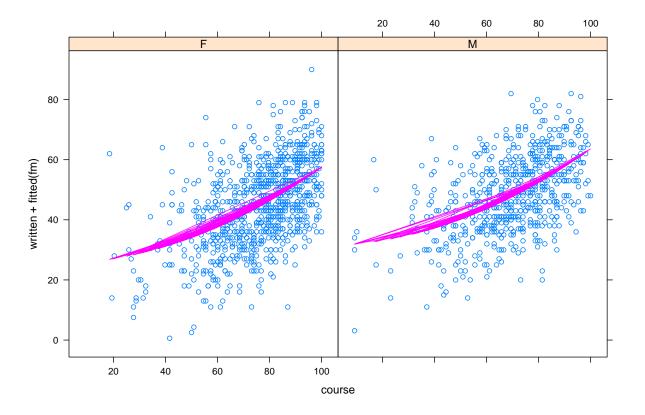
Except for the color of the line, the output is essentially identical. This treats the fitted values as an additional set of y values, and plots them with lines rather than points. See help(panel.superpose) for an explanation of the distribute.type argument.



# Irregular data

Unfortunately, this approach does not work in all situations. For example, in the Gcsemv example, we might try the following.

The na.exclude argument is needed, as otherwise missing values are omitted from fitted(fm) making its length different from that of the other variables. However, as we can see below, the result is a mess because the x values are not ordered (and there are too many of them as well).



We can of course always stick to the built-in solutions; for example,

However, more complex models need more work. Consider the three models

The first model is a quadratic regression model that ignores gender. The second model incorporates gender as an additive term, and the third model further includes interaction terms. Here we have used the "non-missing" subset of <code>Gcsemv</code> in <code>fmO</code> to avoid further grief related to missing values, and used the <code>update()</code> function to simplify the subsequent model fitting calls. Our goal is to compare the fits from <code>fmO</code> and <code>fm1</code> with that from <code>fmO</code>.

All we really need are the fitted values at a sufficiently dense grid covering the range of the predictors. Our approach will be to compute these values separately and then combine them suitably before plotting. This approach generalizes to more models, as well as other types of models. We first define a suitable evaluation grid.

Next we evaluate the corresponding fitted values for each of the three models.

```
> fm0.pred <- cbind(grid, written = predict(fm0, newdata = grid))
> fm1.pred <- cbind(grid, written = predict(fm1, newdata = grid))
> fm2.pred <- cbind(grid, written = predict(fm2, newdata = grid))</pre>
```

Notice that we have done this in a way that each set of predictions comes in the form of a data frame with columns course, gender, and written.

```
> str(fm0.pred)
```

```
'data.frame': 62 obs. of 3 variables:
$ course: num 9.25 12.28 15.3 18.32 ...
$ gender: Factor w/ 2 levels "F","M": 2 2 2 2 2 2 2 2 ...
$ written: num 29.4 29.7 30.1 30.5 ...

We will now transform our original dataset to have the same form.

> orig <- Gcsemv[c("course", "gender", "written")]
> str(orig)

'data.frame': 1905 obs. of 3 variables:
$ course: num NA 71.2 76.8 87.9 44.4 NA 89.8 17.5 ...
$ gender: Factor w/ 2 levels "F","M": 2 1 1 1 2 1 1 2 ...
$ written: num 23 NA 39 36 16 36 49 25 ...
```

and then combine it with the predictions from the models we wish to compare.

```
> combined <- make.groups(original = orig, fm0 = fm0.pred, fm2 = fm2.pred)
```

The make.groups() function combines similarly structured datasets (or simple atomic vectors) with possibly different number of observations into a single dataset, adding a new variable to indicate the origin of each observation in the new dataset.

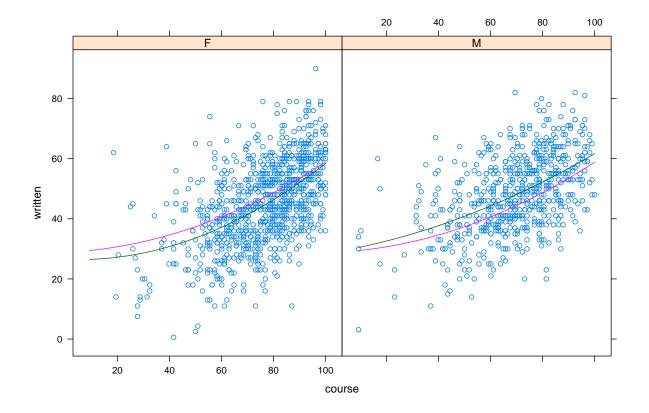
#### > str(combined)

```
'data.frame': 2029 obs. of 4 variables:
$ course : num NA 71.2 76.8 87.9 44.4 NA 89.8 17.5 ...
$ gender : Factor w/ 2 levels "F","M": 2 1 1 1 2 1 1 2 ...
$ written: num 23 NA 39 36 16 36 49 25 ...
$ which : Factor w/ 3 levels "original","fm0",..: 1 1 1 1 1 1 1 1 ...
```

The combined dataset thus consists of the original raw observations (orig), and evaluations of the fitted models fm0 and fm2. All this manipulation finally leads to the call that produces the plot we want.

The raw data are plotted as points, whereas the model fit evaluations are joined by lines to produce a representation of the fitted curves.

A similar comparison of fm0 and fm1 is left a an exercise.



## Summary

The take-home message from all this is that custom panel functions provide finest level of control, but built-in panel functions are also powerful because we can take specify their arguments using argument passing. However, this requires knowledge of arguments (so read documentation!).

For adding regression lines from complex models, it is usually best to obtain a suitable representation of the relevant data *before* the plotting is done. The special function panel.superpose() is useful for grouping, and in particular the distribute.type argument is useful when adding model fits.

#### Session information

- R Under development (unstable) (2011-07-26 r56509), x86\_64-unknown-linux-gnu
- Locale: LC\_CTYPE=en\_IN, LC\_NUMERIC=C, LC\_TIME=en\_IN, LC\_COLLATE=en\_IN, LC\_MONETARY=en\_IN, LC\_MESSAGES=en\_IN, LC\_PAPER=C, LC\_NAME=C, LC\_ADDRESS=C, LC\_TELEPHONE=C, LC\_MEASUREMENT=en\_IN, LC\_IDENTIFICATION=C
- Base packages: base, datasets, graphics, grDevices, methods, stats, tools, utils
- Other packages: lattice 0.19-33, lme4 0.999375-39, Matrix 0.999375-50
- Loaded via a namespace (and not attached): grid 2.14.0, nlme 3.1-101, stats4 2.14.0