Model selection using GAMM with MuMIn

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1 Extending MuMIn's functionality to support gamm

This document describes how to implement the interface between the routines performing model selection and averaging in MuMIn and a class of models not supported by default, using gamm from package mgcv as an example.

The two principal functions in MuMIn, model.avg and dredge rely on the availability of methods for several generic functions for the class of the given fitted model object. These generic functions include the ones defined in package stats (logLik, formula, nobs, and optionally deviance which may simply return NULL), as well as ones defined in MuMIn itself (coeffs, getAllTerms and coefTable). In some cases the default methods may work as well.

In the case of gamm and gamm4, the returned object has no special class, and it is a list with two items: lme or mer, and gam (with some information stripped from it). Therefore no specific methods can be applied.

The solution is to provide a 'wrapper' function for gamm that evaluates the model and adds a class attribute onto it, e.g.:

```
> gamm <- function(...) structure(c(mgcv::gamm(...), list(call = match.call(mgcv::gamm))),
+    class = c("gamm", "list"))
similarly for gamm4 (but assign the same class gamm):
> gamm4 <- function(...) structure(c(gamm4::gamm4(...), list(call = match.call(gamm4::gamm4))),
+    class = c("gamm", "list"))</pre>
```

As these wrappers have the same names as the actual functions, use of them is invisible for the user, and they mask the original functions on the level of .GlobalEnv.

In addition, these wrappers add a call element, containing the original call to the wrapper function. It is not necessary, but makes things easier later on for dredge.

Once we have an object of class gamm, it is possible to provide methods for it. First let us define the generic methods from stats.

```
> logLik.gamm <- function(object, ...) logLik(object[[if (is.null(object$lme)) "mer" else "lme"]],
+ ...)
> formula.gamm <- function(x, ...) formula(x$gam, ...)
> nobs.gamm <- function(object, ...) nobs(object$gam, ...)</pre>
```

It should be noted here that the issue of what the log-likelihood for GAMM should be is not entirely clear. The documentation for gamm states that the log-likelihood of lme is not the one of the fitted GAMM. However, comparing alternative models presents some evidence that it may be still appropriate for gamm. Namely both the log-likelihood of fitted lme, and one of the lme part of gamm (including only linear terms to make the comparison adequate) have identical values.

```
> dat <- gamSim(6, n = 100, scale = 0.2, dist = "normal")</pre>
4 term additive + random effectGu & Wahba 4 term additive model
> fm1 < -gamm(y ~x0 + x1 + x2 + x3, data = dat, random = list(fac = ~1),
      method = "ML")
> fm2 < -lme(y ~x0 + x1 + x2 + x3, data = dat, random = list(fac = ~1),
      method = "ML")
> logLik(fm1$lme)
'log Lik.' -224.2712 (df=7)
> logLik(fm2)
'log Lik.' -224.2712 (df=7)
  Likewise is in the generalised case of gamm4 and lmer:
> dat <- gamSim(6, n = 100, scale = 0.2, dist = "poisson")</pre>
4 term additive + random effectGu & Wahba 4 term additive model
> fmg1 <- gamm4(y \sim x0 + x1 + x2 + x3, family = poisson, data = dat,
      random = ~(1 | fac))
> fmg2 <- lmer(y ~x0 + x1 + x2 + x3 + (1 | fac), family = poisson,
      data = dat)
> logLik(fmg1$mer)
'log Lik.' -703.5312 (df=6)
> logLik(fmg2)
'log Lik.' -703.5312 (df=6)
```

A comparison of gamm4 including a smooth term with fixed two degrees of freedom gives log-likelihood which is very close to that of lmer including a linear and quadratic term.

```
> fmgs1 <- gamm4(y \sim x0 + s(x1, k = 3, fx = TRUE) + x2 + x3, family = poisson,
+ data = dat, random = \sim (1 \mid fac))
> fmgs2 <- lmer(y \sim x0 + x1 + I(x1^2) + x2 + x3 + (1 \mid fac), family = poisson,
+ data = dat)
> logLik(fmgs1$mer)
```

```
'log Lik.' -676.0842 (df=7)
> logLik(fmgs2)
'log Lik.' -661.7715 (df=7)
```

Normally, the object returned by gam inherits also from glm, so the nobs method for glm is called, but in case of gamm the gam element has only class gam, so we need to define the method directly (it just calls nobs.glm):

```
> nobs.gam <- function(object, ...) stats:::nobs.glm(object, ...)
    Methods for generic functions defined in MuMIn:
> coeffs.gamm <- function(model) coef(model$gam)
> getAllTerms.gamm <- function(x, ...) getAllTerms(x$gam, ...)
> coefTable.gamm <- function(model, ...) coefTable(model$gam, ...)</pre>
Two columns are obligatory in the data.frame returned by coefTable: 'Estimate' and 'Std. Error').
```

2 Model selection

Now we have all the prerequisites to proceed with the model selection:

```
> set.seed(0)
> dat <- gamSim(6, n = 100, scale = 5, dist = "normal")
4 term additive + random effectGu & Wahba 4 term additive model
> fmgs2 <- gamm(y \tilde{1} + s(x0) + s(x3) + s(x2), family = gaussian,
      data = dat, random = list(fac = ~1))
This model fits poorly, but this is deliberate, to justify the model averaging.
> head(dd2 <- dredge(fmgs2))</pre>
Global model call: gamm(formula = y ~1 + s(x0) + s(x3) + s(x2), random = list(fac = ~1),
    family = gaussian, data = dat)
Model selection table
  (Intercept) s(x0) s(x2) s(x3) df logLik
                                             AICc delta weight
3 16.58
                                 5 -325.830 662.3 0.00 0.480
7 16.58
                                 7 -323.916 663.0 0.75 0.330
4 16.58
                                7 -325.016 665.2 2.95 0.110
8 16.58
                                 9 -323.507 667.0 4.72 0.045
1 16.58
                                 3 -331.043 668.3 6.04 0.023
5 16.58
                                 5 -329.624 669.9 7.59 0.011
```

(Note that we get quite different results using gamm4)

```
> summary(model.avg(dd2, subset = cumsum(weight) <= 0.95))</pre>
Call:
model.avg.model.selection(object = dd2, subset = cumsum(weight) <=</pre>
    0.95)
Component models:
   df logLik
                AICc Delta Weight
    5 -325.83 662.30
                      0.00
                              0.52
23 7 -323.92 663.05
                      0.75
                              0.36
12 7 -325.02 665.25 2.95
                              0.12
Term codes:
s(x0) s(x2) s(x3)
          2
    1
Model-averaged coefficients:
              Estimate Std. Error z value Pr(>|z|)
                                     9.545
(Intercept)
             1.658e+01 1.737e+00
                                              <2e-16 ***
s(x2).1
            -4.393e+00 2.983e+00
                                     1.472
                                              0.1409
s(x2).2
            -1.208e+01
                        7.979e+00
                                     1.513
                                             0.1302
                                     0.544
s(x2).3
            -1.157e+00 2.126e+00
                                             0.5863
s(x2).4
            -2.318e+00 5.211e+00
                                     0.445
                                             0.6564
s(x2).5
            -1.129e+00 1.606e+00
                                     0.703
                                             0.4820
s(x2).6
            -3.211e+00 4.609e+00
                                     0.697
                                             0.4860
s(x2).7
            -1.581e+00 1.707e+00
                                     0.926
                                              0.3544
s(x2).8
             1.426e+01
                        1.169e+01
                                     1.219
                                              0.2227
s(x2).9
             3.243e+00
                        4.770e+00
                                     0.680
                                              0.4965
            -4.985e-09
                        1.669e-04
                                     0.000
                                              1.0000
s(x3).1
s(x3).2
            -6.610e-09
                        2.326e-04
                                     0.000
                                              1.0000
             1.033e-09 5.467e-05
                                     0.000
s(x3).3
                                              1.0000
                                     0.000
s(x3).4
            -8.233e-09
                        1.359e-04
                                              1.0000
            -1.724e-09
                        3.452e-05
                                     0.000
                                              1.0000
s(x3).5
            -8.022e-09 1.284e-04
                                     0.000
                                              1.0000
s(x3).6
s(x3).7
             4.433e-09
                        6.862e-05
                                     0.000
                                              0.9999
             4.255e-08 4.185e-04
s(x3).8
                                     0.000
                                             0.9999
s(x3).9
            -1.149e+00 5.834e-01
                                     1.969
                                             0.0489 *
s(x0).1
             1.278e-08 1.489e-04
                                     0.000
                                             0.9999
s(x0).2
            -1.051e-08 2.333e-04
                                     0.000
                                              1.0000
s(x0).3
             1.635e-09
                        5.412e-05
                                     0.000
                                              1.0000
            -7.340e-09
                                     0.000
                                              1.0000
s(x0).4
                        1.410e-04
s(x0).5
             1.691e-09
                        4.206e-05
                                     0.000
                                              1.0000
                                     0.000
s(x0).6
            -7.870e-09
                        1.285e-04
                                              1.0000
s(x0).7
            -3.062e-09
                        5.340e-05
                                     0.000
                                              1.0000
s(x0).8
             3.200e-08
                                     0.000
                        4.384e-04
                                              0.9999
```

0.2011

1.278

s(x0).9

7.461e-01 5.836e-01

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Full model-averaged coefficients (with shrinkage):

(Intercept)	s(x2).1	s(x2).2	s(x2).3	s(x2).4	s(x2).5
1.6583e+01	-4.3927e+00	-1.2075e+01	-1.1568e+00	-2.3180e+00	-1.1290e+00
s(x2).6	s(x2).7	s(x2).8	s(x2).9	s(x3).1	s(x3).2
-3.2112e+00	-1.5809e+00	1.4258e+01	3.2433e+00	-1.7880e-09	-2.3708e-09
s(x3).3	s(x3).4	s(x3).5	s(x3).6	s(x3).7	s(x3).8
3.7056e-10	-2.9532e-09	-6.1827e-10	-2.8775e-09	1.5900e-09	1.5263e-08
s(x3).9	s(x0).1	s(x0).2	s(x0).3	s(x0).4	s(x0).5
-4.1208e-01	1.5258e-09	-1.2551e-09	1.9519e-10	-8.7648e-10	2.0188e-10
s(x0).6	s(x0).7	s(x0).8	s(x0).9		
-9.3974e-10	-3.6567e-10	3.8213e-09	8.9094e-02		

Relative variable importance:

(Intercept)	s(x0)	s(x2)	s(x3)
1.00	0.12	1.00	0.36