

# Package ‘MuMIn’

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**Title** Multi-model inference

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**Description** Functions for model selection and model averaging based on information criteria (AICc and alikes).

**License** GPL

**Suggests** lme4

**LazyLoad** yes

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MuMIn-package

*Multi model inference*

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## Description

The package MuMIn contains functions for model selection and model averaging, based on information criteria (AIC alike).

## Details

User level functions include:

`model.avg` - does model averaging.

`get.models` - evaluates models from the table returned by `dredge`.

`dredge` - runs models with combinations of terms of the supplied 'global' model.

`AICc` - calculates second-order Akaike information criterion for one or several fitted model objects.

## Author(s)

Kamil Bartoń <kamil.barton@go2.pl>

## References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

## See Also

[AIC, step](#)

## Examples

```
fml <- lm(Fertility ~ . , data = swiss)

dd <- dredge(fml)
dd
#list of models with delta.aicc < 4
top.models.1 <- get.models(dd, subset = delta < 4)
model.avg(top.models.1) # get averaged coefficients

#or as a 95% confidence set:
top.models.2 <- get.models(dd, cumsum(weight) <= .95)

model.avg(top.models.2) # get averaged coefficients

# Mixed models:

data(Orthodont, package="nlme")

require(nlme)
fm2 <- lme(distance ~ age + Sex, data = Orthodont, random = ~ 1 | Subject, method="ML")
dredge(fm2)
```

```
require(lme4)
fm3 <- lmer(distance ~ age + Sex + (1 | Subject), data = Orthodont, REML=FALSE)
dd3 <- dredge(fm3)

# Get top-most models, but fitted by REML:
(top.models.3 <- get.models(dd3, subset = delta < 4, REML=TRUE))
# use: method = "REML" for older versions of lme4
```

AICc

*Second-order Akaike Information Criterion***Description**

Calculates second-order Akaike information criterion for one or several fitted model objects (AIC for small samples).

**Usage**

```
AICc(object, ..., k = 2)
```

**Arguments**

<code>object</code>	a fitted model object
<code>...</code>	optionally more fitted model objects
<code>k</code>	the “penalty” per parameter to be used; the default $k = 2$ is the classical <a href="#">AIC</a>

**Value**

If just one object is provided, returns a numeric value with the corresponding AICc; if more than one object are provided, returns a data.frame with rows corresponding to the objects and columns representing the number of parameters in the model (df), AICc and the [AIC](#).

**Author(s)**

Kamil Bartoń

**References**

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

**See Also**

Akaike’s An Information Criterion: [AIC](#)

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Cement

*Cement hardening data*


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### Description

Cement hardening data from Woods et al (1939).

### Usage

```
data(Cement)
```

### Format

`cement` is a data frame with 5 variables. `x1-x4` are four predictor variables expressed as a percentage of weight.

**x1** calcium aluminate

**x2** tricalcium silicate

**x3** tetracalcium alumino ferrite

**x4** dicalcium silicate

**y** calories of heat evolved per gram of cement after 180 days of hardening

### Author(s)

Kamil Bartoń

### Source

Woods H., Steinour H.H., Starke H.R. (1932) Effect of composition of Portland cement on heat evolved during hardening. *Industrial & Engineering Chemistry* 24, 1207-1214

### References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

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dredge

*data dredging*


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### Description

runs models with all possible combinations of the explanatory variables in the supplied model.

### Usage

```
dredge(global.model, beta = FALSE, eval = TRUE, rank = "AICc",
       fixed = NULL, m.max = NA, ...)
```

## Arguments

<code>global.model</code>	a fitted ‘global’ model object. Currently, it can be a <code>lm</code> , <code>glm</code> , <code>gam</code> , <code>lme</code> , <code>lmer</code> , <code>sarlm</code> or <code>spautolm</code> .
<code>beta</code>	logical should standardized coefficients be returned rather than normal ones?
<code>eval</code>	whether to evaluate and rank the models. If set to <code>FALSE</code> only a list of all possible model formulas is returned
<code>rank</code>	custom rank function (information criterion) to use instead AICc, e.g. <code>QAIC</code> or <code>BIC</code> , See ‘Details’
<code>fixed</code>	optional, either a single sided formula or a character vector giving names of terms to be included in all models
<code>m.max</code>	maximum number of terms to be included in single model, defaults to the number of terms in <code>global.model</code>
<code>...</code>	optional arguments for the <code>rank</code> function

## Details

Models are run one by one by calling `update` with modified `formula` argument. While is robust in, it is not very efficient, so may be time (and memory) consuming.

Handling interactions, `dredge` respects marginality constraints, so “all possible combinations” do not include models containing interactions without their respective main effects.

`rank` is found by a call to `match.fun` and typically is specified as a function or a symbol (e.g. a backquoted name) or a character string specifying a function to be searched for from the environment of the call to `lapply`.

Function `rank` must be able to accept model as a first argument and must always return a scalar.

## Value

`dredge` returns a `data.frame` of class `model.selection` with models’ coefficients, k, deviance/RSS, r-squared, AIC, AICc, etc. This depends on a type of model. Models are ordered according to `AICc` (lowest on top), or by `rank` function if specified. It has also a `formulas` attribute - a list containing all the model formulas.

## Note

Use the `lmer` from **lme4** library rather than the old `lmer` from **Matrix** package. Complex expressions (like `log(y)`) cannot be used as the response variable, the response must be specified as simple variable name. They may be used on the right side of the formula, though. Make sure there is no `na.action` set to `na.omit` in `global.model`. This can result with models fitted to different data sets, if there are NA’s present. `dredge` cannot handle nested model designs (formulas such as `y ~ a/b`).

## Author(s)

Kamil Bartoń

## References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

**See Also**

[get.models](#), [model.avg](#). [QAIC](#) has examples of using custom rank function.

**Examples**

```
# Example from Burnham and Anderson (2002), page 100:
data(Cement)
lm1 <- lm(y ~ ., data = Cement)
dd <- dredge(lm1)
dd

#models with delta.aicc < 4
model.avg(get.models(dd, subset = delta < 4)) # get averaged coefficients

#or as a 95% confidence set:
top.models <- get.models(dd, cumsum(weight) <= .95)

model.avg(top.models) # get averaged coefficients

#topmost model:
top.models[[1]]
```

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dRedging.functions *Helper functions for package dRedging*

---

**Description**

`beta.weights` - computes standardized coefficients (beta weights) for the model; `coeffs` - gets model coefficients; `getAllTerms` - extracts independent variables' names from a fitted model; `tTable` - returns [summary](#) table of a fitted model with coefficients, standard errors, and p-values.

**Usage**

```
beta.weights(model)
coeffs(model)
getAllTerms(x, ...)
tTable(model, ...)
```

**Arguments**

<code>model</code>	a fitted model object
<code>x</code>	a fitted model object or a <a href="#">formula</a>
<code>...</code>	other arguments, not used

**Author(s)**

Kamil Bartoń

**See Also**

[dredge](#)

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get.models	<i>Get models</i>
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## Description

Gets list of models from a `model.selection` object

## Usage

```
get.models(dd, subset = delta <= 4, ...)
```

## Arguments

<code>dd</code>	object returned by <a href="#">dredge</a>
<code>subset</code>	subset of models
<code>...</code>	additional parameters passed to <code>update</code> , for example, in <code>lme/lmer</code> one may want to use <code>method = "REML"</code> while using "ML" for model selection

## Value

[list](#) of models.

## Author(s)

Kamil Bartoń

## See Also

[dredge](#), [model.avg](#)

## Examples

```
# Mixed models:

require(nlme)
fm2 <- lme(distance ~ age + Sex, data = Orthodont, random = ~ 1 | Subject, method="ML")
dd2 <- dredge(fm2)

# Get top-most models, but fitted by REML:
(top.models.2 <- get.models(dd2, subset = delta < 4, method = "REML"))
```

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model.avg

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*Model averaging*


---

## Description

averages models according to an information criterion

## Usage

```
model.avg(m1, ..., beta = FALSE, method = c("0", "NA"), rank = NULL, rank.args =

## S3 method for class 'averaging':
coef(object, ...)

## S3 method for class 'averaging':
predict(object, newdata, se.fit = NULL, interval = NULL,
type=NULL, ...)
```

## Arguments

m1	A fitted model object or a list of such objects.
beta	Logical, should standardized coefficients be returned rather than normal ones?
method	If set to "0" (default), terms missing in one model are assumed to be 0's, otherwise they are omitted from the weighted average.
rank	Custom rank function (information criterion) to use instead of AICc, e.g. QAIC or BIC, may be omitted if m1 is a list returned by dredge. See 'Details'.
rank.args	Optional list of arguments for the rank function.
alpha	Significance level for calculating confidence intervals.
object	An object returned by model.avg.
newdata	An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used.
se.fit, interval	Currently not used.
type	Ignored. Only predictions on the link scale are allowed. Warning is given if user tries something else here.
...	for model.avg - more fitted model objects, for predict - arguments to be passed to respective predict method

## Details

rank is found by a call to match.fun and typically is specified as a function or a symbol (e.g. a backquoted name) or a character string specifying a function to be searched for from the environment of the call to lapply.

Function rank must be able to accept model as a first argument and must always return a scalar. \ Apart from predict and coef, other default methods, such as formula and residuals may be used.



**Value**

`model.avg` returns a list with elements:

<code>summary</code>	Model table with deviance, AICc, Delta and weight.
<code>coefficients</code>	the model coefficients
<code>variance</code>	variance of coefficients
<code>avg.model</code>	averaged model summary ( <code>data.frame</code> with columns: <code>coef</code> - averaged coefficients, <code>var</code> - unconditional variance estimator, <code>ase</code> - adjusted standard error estimator, <code>lci</code> , <code>uci</code> - unconditional confidence intervals)
<code>relative.importance</code>	relative variable importances
<code>variable.codes</code>	Variable names with numerical codes used in the summary
<code>relative.importance</code>	Relative importance of variables
<code>weights</code>	
<code>beta</code>	(logical) were standardized coefficients used?
<code>model</code>	the model matrix, analogical to one that would be used in a single model.
<code>residuals</code>	the residuals (response minus fitted values).

**Author(s)**

Kamil Bartoń

**References**

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

**See Also**

`dredge`, `get.models`. [QAIC](#) has examples of using custom rank function.

**Examples**

```
# Example from Burnham and Anderson (2002), page 100:
data(Cement)
lm1 <- lm(y ~ ., data = Cement)
dd <- dredge(lm1)
dd

#models with delta.aicc < 4
model.avg(get.models(dd, subset = delta < 4)) # get averaged coefficients

#or as a 95% confidence set:
top.models <- get.models(dd, cumsum(weight) <= .95)

model.avg(top.models) # get averaged coefficients

#topmost model:
top.models[[1]]
```

```
## Not run:
# using BIC (Schwarz's Bayesian criterion) to rank the models
BIC <- function(x) AIC(x, k = log(length(residuals(x))))
mav <- model.avg(top.models, rank=BIC)
## End(Not run)

# Predicted values

nseq <-
function(x, len=length(x)) seq(min(x, na.rm=TRUE), max(x, na.rm=TRUE), length=len)

# New predictors: X1 along the range of original data, other variables held
# constant at their means
newdata <- as.data.frame(lapply(lapply(Cement[1:5], mean), rep, 25))
newdata$X1 <- nseq(Cement$X1, 25)

# Predictions from each of the models in a set:
pred <- sapply(top.models, predict, newdata=newdata)
# Add predictions from the averaged model:
pred <- cbind(pred, averaged=predict(model.avg(top.models), newdata))

matplot(x = newdata$X1, y = pred, type="l", lwd=c(rep(1,ncol(pred)-1), 2))

legend("topleft", legend=c(lapply(top.models, formula), "Averaged model"),
      col=seq(ncol(pred)), lty=1:5, lwd=c(rep(1,ncol(pred)-1), 2))
```

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par.avg

---

*Parameter averaging*


---

## Description

averages single parameter based on given weights

## Usage

```
par.avg (x, se, npar, weight, alpha = 0.05)
```

## Arguments

x	vector of parameters
se	vector of standard errors
npar	vector giving numbers of estimated parameters
weight	vector of weights
alpha	significance level for calculating confidence intervals

**Value**

`par.avg` returns a vector with named elements:

Coefficient	model coefficients
Variance	unconditional variance of coefficients
Unconditional SE	
Lower CI, Upper CI	relative variable importances

**Author(s)**

Kamil Barton

**References**

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

**See Also**

[model.avg](#) for averaging models.

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QAIC	<i>Quasi AIC</i>
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**Description**

Calculates “quasi AIC” for one or several fitted model objects. This function is provided just as an example of custom rank function for use with [model.avg](#) and [dredge](#)

**Usage**

```
QAIC(object, ..., chat)
```

**Arguments**

<code>object</code>	a fitted model object.
<code>...</code>	optionally more fitted model objects.
<code>chat</code>	c - hat

**Details**

`rank` is specified as a function or a symbol (e.g. a backquoted name) or a character string specifying a function.

Function `rank` must be able to accept `model` as a first argument and must always return a scalar.

**Value**

If just one object is provided, returns a numeric value with the corresponding QAIC; if more than one object are provided, returns a data.frame with rows corresponding to the objects.

**Author(s)**

Kamil Bartoń

**Examples**

```
budworm <- data.frame(ldose = rep(0:5, 2), numdead = c(1, 4, 9, 13, 18, 20, 0, 2, 6, 10,
budworm$SF <- cbind(budworm$numdead, 20 - budworm$numdead)
budworm.qlg <- glm(SF ~ sex*ldose, family = quasibinomial, data = budworm)

ddl <- dredge(budworm.qlg, rank = "QAIC", chat = summary(budworm.qlg)$dispersion)
gml <- get.models(ddl, 1:4)

model.avg(gml)

model.avg(gml[[1]], gml[[2]], rank = "QAIC", rank.args = list(chat = 1))
```

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