

Package ‘MuMIn’

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R topics documented:

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MuMIn-package

Multi-model inference

Description

The package `MuMIn` contains functions for (automated) model selection and model averaging based on information criteria (AIC alike).

Details

User level functions include:

`model.avg` - does model averaging.

`get.models` - evaluates models from the table returned by `dredge`.

`dredge` - runs models with combinations of terms of the supplied 'global' model.

`AICc` - calculates second-order Akaike information criterion for one or several fitted model objects.

Author(s)

Kamil Bartoń <kamil.barton@go2.pl>

References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

See Also

[AIC](#), [step](#)

Examples

```
fml <- lm(Fertility ~ . , data = swiss)

dd <- dredge(fml)
dd
#list of models with delta.aicc < 4
top.models.1 <- get.models(dd, subset = delta < 4)
model.avg(top.models.1) # get averaged coefficients

#or as a 95% confidence set:
top.models.2 <- get.models(dd, cumsum(weight) <= .95)

model.avg(top.models.2) # get averaged coefficients

# Mixed models:

data(Orthodont, package="nlme")

require(nlme)
fm2 <- lme(distance ~ age + Sex, data = Orthodont, random = ~ 1 | Subject,
method="ML")
```

```
dredge(fm2)

require(lme4)
fm3 <- lmer(distance ~ age + Sex + (1 | Subject), data = Orthodont, REML=FALSE)
dd3 <- dredge(fm3)

# Get top-most models, but fitted by REML:
(top.models.3 <- get.models(dd3, subset = delta < 4, REML=TRUE))
# use: method = "REML" for older versions of lme4
```

AICc

*Second-order Akaike Information Criterion***Description**

Calculates second-order Akaike information criterion for one or several fitted model objects (AIC for small samples).

Usage

```
AICc(object, ..., k = 2)
```

Arguments

<code>object</code>	a fitted model object
<code>...</code>	optionally more fitted model objects
<code>k</code>	the “penalty” per parameter to be used; the default <code>k = 2</code> is the classical AIC

Value

If just one object is provided, returns a numeric value with the corresponding AICc; if more than one object are provided, returns a `data.frame` with rows corresponding to the objects and columns representing the number of parameters in the model (`df`), AICc and the [AIC](#).

Author(s)

Kamil Barton

References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

See Also

Akaike’s An Information Criterion: [AIC](#)

Cement

Cement hardening data

Description

Cement hardening data from Woods et al (1939).

Usage

```
data(Cement)
```

Format

Cement is a data frame with 5 variables. x1-x4 are four predictor variables expressed as a percentage of weight.

X1 calcium aluminate

X2 tricalcium silicate

X3 tetracalcium alumino ferrite

X4 dicalcium silicate

y calories of heat evolved per gram of cement after 180 days of hardening

Author(s)

Kamil Bartoń

Source

Woods H., Steinour H.H., Starke H.R. (1932) Effect of composition of Portland cement on heat evolved during hardening. *Industrial & Engineering Chemistry* 24, 1207-1214

References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

dredge

Evaluate "all possible" models

Description

runs models with all possible combinations of the explanatory variables in the supplied model.

Usage

```
dredge(global.model, beta = FALSE, eval = TRUE, rank = "AICc",
fixed = NULL, m.max = NA, ...)
```

Arguments

<code>global.model</code>	a fitted ‘global’ model object. Currently, it can be a <code>lm</code> , <code>glm</code> , <code>gam</code> , <code>lme</code> , <code>lmer</code> , <code>sarlm</code> or <code>spautolm</code> , but also other types are likely to work (untested).
<code>beta</code>	logical should standardized coefficients be returned rather than normal ones?
<code>eval</code>	whether to evaluate and rank the models. If <code>FALSE</code> , a list of all possible model formulas is returned
<code>rank</code>	optional custom rank function (information criterion) to be used instead <code>AICc</code> , e.g. <code>QAIC</code> or <code>BIC</code> , See ‘Details’
<code>fixed</code>	optional, either a single sided formula or a character vector giving names of terms to be included in all models
<code>m.max</code>	optional, maximum number of terms to be included in single model, defaults to the number of terms in <code>global.model</code>
<code>...</code>	optional arguments for the <code>rank</code> function

Details

Models are run one by one by calling `update` with modified `formula` argument. This method, while robust in that it can be applied to a variety of different models, is not very efficient, so may be time (and memory) consuming.

Handling interactions, `dredge` respects marginality constraints, so “all possible combinations” do not include models containing interactions without their respective main effects.

`rank` is found by a call to `match.fun` and typically is specified as a function or a symbol (e.g. a backquoted name) or a character string specifying a function to be searched for from the environment of the call to `lapply`.

Function `rank` must be able to accept `model` as a first argument and must always return a scalar.

Value

`dredge` returns a `data.frame` of class `model.selection` with models’ coefficients, k, deviance/RSS, r-squared, AIC, `AICc`, etc. This depends on a type of model. Models are ordered according to `AICc` (lowest on top), or by `rank` function if specified. It has also a `formulas` attribute - a list containing all the model formulas.

Note

Use the `lmer` from **lme4** library rather than the old `lmer` from **Matrix** package. Make sure there is no `na.action` set to `na.omit` in `global.model`. This can result with models fitted to different data sets, if there are NA’s present. `dredge` cannot handle nested model designs (formulas such as `y ~ a/b`) properly.

Author(s)

Kamil Bartoń

References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

See Also

[get.models](#), [model.avg](#). [QAIC](#) has examples of using custom rank function.

Examples

```
# Example from Burnham and Anderson (2002), page 100:
data(Cement)
lm1 <- lm(y ~ ., data = Cement)
dd <- dredge(lm1)
dd

#models with delta.aicc < 4
model.avg(get.models(dd, subset = delta < 4)) # get averaged coefficients

#or as a 95% confidence set:
top.models <- get.models(dd, cumsum(weight) <= .95)

model.avg(top.models) # get averaged coefficients

#topmost model:
top.models[[1]]
```

get.models

Get models

Description

Gets list of models from a `model.selection` object

Usage

```
get.models(dd, subset = delta <= 4, ...)
```

Arguments

dd	object returned by dredge
subset	subset of models
...	additional parameters passed to <code>update</code> , for example, in <code>lme/lmer</code> one may want to use <code>method = "REML"</code> while using "ML" for model selection

Value

[list](#) of models.

Author(s)

Kamil Bartoń

See Also

[dredge](#), [model.avg](#)

Examples

```
# Mixed models:

require(nlme)
fm2 <- lme(distance ~ age + Sex, data = Orthodont,
random = ~ 1 | Subject, method="ML")
dd2 <- dredge(fm2)

# Get top-most models, but fitted by REML:
(top.models.2 <- get.models(dd2, subset = delta < 4, method = "REML"))
```

miscellaneous

Helper functions

Description

`beta.weights` - computes standardized coefficients (beta weights) for a model;
`coeffs` - extracts model coefficients;
`getAllTerms` - extracts independent variable names from a model object;
`tTable` - extracts a table of coefficients, standard errors, and p-values from a model object;
`Weights` - calculates Akaike weights (normalized relative likelihoods)

Usage

```
beta.weights(model)
coeffs(model)
getAllTerms(x, ...)
tTable(model, ...)
Weights(aic, ...)

cbindDataFrameList(x)
rbindDataFrameList(x)
```

Arguments

<code>model</code>	a fitted model object
<code>x</code>	a fitted model object or a formula . for <code>*bindDataFrameList</code> , a list of <code>data.frames</code>
<code>...</code>	other arguments, not used
<code>aic</code>	a vector of AIC (or other information criterion) values

Note

`coeffs`'s value is in most cases identical to that returned by `coef`, the only difference is that it returns fixed effects' coefficients for mixed models.

Functions `*bindDataFrameList` are not exported from the name space, use e.g. `MuMIn:::cbindDataFrameList` to access them.

Author(s)

Kamil Bartoń

See Also[dredge](#)

model.avg

Model averaging

Description

Model averaging based on an information criterion.

Usage

```
model.avg(m1, ..., beta = FALSE, method = c("0", "NA"), rank = NULL,
rank.args = NULL, alpha = 0.05)

## S3 method for class 'averaging':
coef(object, ...)

## S3 method for class 'averaging':
predict(object, newdata, se.fit = NULL, interval = NULL,
type=NULL, ...)
```

Arguments

m1	A fitted model object or a list of such objects.
beta	Logical, should standardized coefficients be returned rather than normal ones?
method	If set to “0” (default), terms missing in one model are assumed to be 0’s, otherwise they are omitted from the weighted average.
rank	Custom rank function (information criterion) to use instead of AICc, e.g. QAIC or BIC, may be omitted if m1 is a list returned by dredge. See ‘Details’.
rank.args	Optional list of arguments for the rank function.
alpha	Significance level for calculating confidence intervals.
object	An object returned by model.avg.
newdata	An optional data frame in which to look for variables with which to predict. If omitted, the fitted values are used.
se.fit, interval	Currently not used.
type	Ignored. Only predictions on the link scale are allowed. Warning is given if user tries something else here.
...	for model.avg - more fitted model objects, for predict - arguments to be passed to respective predict method

Details

`rank` is found by a call to `match.fun` and typically is specified as a function or a symbol (e.g. a backquoted name) or a character string specifying a function to be searched for from the environment of the call to `lapply`.

Function `rank` must be able to accept `model` as a first argument and must always return a scalar. \ Apart from `predict` and `coef`, other default methods, such as `formula` and `residuals` may be used.

Value

`model.avg` returns a list with elements:

<code>summary</code>	Model table with deviance, AICc, Delta and weight.
<code>coefficients</code>	the model coefficients
<code>variance</code>	variance of coefficients
<code>avg.model</code>	averaged model summary (<code>data.frame</code> with columns: <code>coef</code> - averaged coefficients, <code>var</code> - unconditional variance estimator, <code>ase</code> - adjusted standard error estimator, <code>lci</code> , <code>uci</code> - unconditional confidence intervals)
<code>relative.importance</code>	relative variable importances
<code>variable.codes</code>	Variable names with numerical codes used in the summary
<code>relative.importance</code>	Relative importance of variables
<code>weights</code>	
<code>beta</code>	(logical) were standardized coefficients used?
<code>model</code>	the model matrix, analogical to one that would be used in a single model.
<code>residuals</code>	the residuals (response minus fitted values).

Author(s)

Kamil Bartoń

References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

See Also

[dredge](#), [get.models](#). [QAIC](#) has examples of using custom rank function.

Examples

```
# Example from Burnham and Anderson (2002), page 100:
data(Cement)
lm1 <- lm(y ~ ., data = Cement)
dd <- dredge(lm1)
dd

#models with delta.aicc < 4
```

```

model.avg(get.models(dd, subset = delta < 4)) # get averaged coefficients

#or as a 95% confidence set:
top.models <- get.models(dd, cumsum(weight) <= .95)

model.avg(top.models) # get averaged coefficients

#topmost model:
top.models[[1]]

## Not run:
# using BIC (Schwarz's Bayesian criterion) to rank the models
BIC <- function(x) AIC(x, k = log(length(residuals(x))))
mav <- model.avg(top.models, rank=BIC)

## End(Not run)

# Predicted values
nseq <- function(x, len=length(x)) seq(min(x, na.rm=TRUE), max(x, na.rm=TRUE),
length=len)

# New predictors: X1 along the range of original data, other variables held
# constant at their means
newdata <- as.data.frame(lapply(lapply(Cement[1:5], mean), rep, 25))
newdata$X1 <- nseq(Cement$X1, 25)

# Predictions from each of the models in a set:
pred <- sapply(top.models, predict, newdata=newdata)
# Add predictions from the averaged model:
pred <- cbind(pred, averaged=predict(model.avg(top.models), newdata))

matplot(x = newdata$X1, y = pred, type="l", lwd=c(rep(1,ncol(pred)-1), 2))

legend("topleft", legend=c(lapply(top.models, formula), "Averaged model"),
      col=seq(ncol(pred)), lty=1:5, lwd=c(rep(1,ncol(pred)-1), 2))

```

par.avg

Parameter averaging

Description

Averages single parameter based on provided weights

Usage

```
par.avg(x, se, npar, weight, alpha = 0.05)
```

Arguments

x	vector of parameters
se	vector of standard errors
npar	vector giving numbers of estimated parameters

weight	vector of weights
alpha	significance level for calculating confidence intervals

Value

par.avg returns a vector with named elements:

Coefficient	model coefficients
Variance	unconditional variance of coefficients
Unconditional SE	
Lower CI, Upper CI	relative variable importances

Author(s)

Kamil Bartoń

References

Burnham, K. P. and Anderson, D. R (2002) *Model selection and multimodel inference: a practical information-theoretic approach*. 2nd ed.

See Also

[model.avg](#) for averaging models.

QAIC

Quasi AIC

Description

Calculates “quasi AIC” for one or several fitted model objects. This function is provided just as an example of custom rank function for use with [model.avg](#) and [dredge](#)

Usage

```
QAIC(object, ..., chat)
```

Arguments

object	a fitted model object.
...	optionally more fitted model objects.
chat	c - hat

Details

rank is specified as a function or a symbol (e.g. a backquoted name) or a character string specifying a function.

Function rank must be able to accept model as a first argument and must always return a scalar.

Value

If just one object is provided, returns a numeric value with the corresponding QAIC; if more than one object are provided, returns a data.frame with rows corresponding to the objects.

Author(s)

Kamil Bartoń

Examples

```
budworm <- data.frame(ldose = rep(0:5, 2), numdead = c(1, 4, 9, 13, 18, 20, 0,
2, 6, 10, 12, 16), sex = factor(rep(c("M", "F"), c(6, 6))))

budworm$SF <- cbind(budworm$numdead, 20 - budworm$numdead)

budworm.qlg <- glm(SF ~ sex*ldose, family = quasibinomial, data = budworm)

ddl <- dredge(budworm.qlg, rank = "QAIC",
chat = summary(budworm.qlg)$dispersion)
gml <- get.models(ddl, 1:4)

model.avg(gml)

model.avg(gml[[1]], gml[[2]], rank = "QAIC", rank.args = list(chat = 1))
```

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