Robust Regression with Particle Swarm Optimisation and Differential Evolution

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1 Introduction

We provide a code example for a robust regression problem. The purpose of this vignette is to provide the code in a convenient way; for more details, please see Gilli et al. [2011]. (The vignette builds on the script comparisonLMS.R.)

2 Data and settings

We start by attaching the package.

```
> require("NMOF")
> require("MASS")
> set.seed(11223344)
```

We will use the function lqs from the MASS package [Venables and Ripley, 2002]. We will use an artificial data set with n observations and p regressors, created with the function createData.

We start by creating some artifial data. We collect X and y in the list data. We also add the scalar h which gives the order statistic of the squared residuals to be minimised. Note that we put as .vector(y) into data so that the vector gets 'recycled' in the objective function.

```
> n <- 100L  ## number of observations
> p <- 10L  ## number of regressors
> constant <- TRUE; sigma <- 3; oFrac <- 0.1
> h <- 75L  ## ... or use something like floor((n+1)/2)
> aux <- createData(n, p, constant, sigma, oFrac)
> X <- aux$X; y <- aux$y
> data <- list(y = as.vector(y), X = X, h = h)
The outliers are visible.
> par(bty = "n", las = 1)
> plot(X[ ,2L], type = "b", ylab = "X values")
> abline(h = 0)
```



Two example objective functions, Least Trimmed Squares (LTS) and Least Quantile of Squares (LQS). Note that they are almost identical.

```
> OF <- function(param,data) {
    X <- data$X; y <- data$y
    aux <- y - X %*% param
    aux <- aux * aux
    aux <- apply(aux, 2L, sort, partial = data$h)
    colSums(aux[1:data$h, ]) ## LTS
}
> OF <- function(param, data) {
    X <- data$X; y <- data$y
    aux <- y - X %*% param
    aux <- aux * aux
    aux <- apply(aux, 2L, sort, partial = data$h)
    aux[data$h, ] ## LQS
}</pre>
```

Both functions are vectorised. They work with a single solution (param would be a vector) or a whole population (param would be a matrix; each column would be one solution).

3 Using DE and PSO

We run DE and PSO. We compare the result with lqs.

```
> popsize <- 100L; generations <- 500L
> ps <- list(min = rep(-10,p),
            max = rep(10,p),
            c1 = 0.5,
            c2 = 1.1,
            iner = 0.9,
            initV = 1,
            nP = popsize,
            nG = generations,
            \max V = 5,
            loopOF = FALSE,
            printBar = FALSE,
            printDetail = FALSE)
> de <- list(min = rep(-10,p),
            max = rep(10,p),
            nP = popsize,
```

```
nG = generations,
             F = 0.7,
             CR = 0.9,
             loopOF = FALSE,
             printBar = FALSE,
             printDetail = FALSE)
> system.time(solPS <- PSopt(OF = OF, algo = ps, data = data))
          system elapsed
  1.404
           0.008
                    1.414
> system.time(solDE <- DEopt(OF = OF, algo = de, data = data))
          system elapsed
    user
   1.400
           0.012
                    1.414
> if (require("MASS", quietly = TRUE)) {
     system.time(test1 <- lqs(y ~ X[ ,-1L],</pre>
                                adjust = TRUE,
                                nsamp = 100000L,
                                method = "lqs",
                                 quantile = h))
     res1 <- sort((y - X %*% as.matrix(coef(test1)))^2)[h]</pre>
 } else res1 <- NA
> (res2 <- sort((y - X %*% as.matrix(solPS$xbest))^2)[h])</pre>
[1] 0.26335
> (res3 <- sort((y - X %*% as.matrix(solDE$xbest))^2)[h])</pre>
[1] 0.27989
> cat("lqs:
              ", res1, "\n",
     "PSopt: ", res2, "\n",
     "DEopt: ", res3, "\n", sep = "")
lqs: 0.38073
PSopt: 0.26335
DEopt: 0.27989
   To demonstrate the advantage of a vectorised objective function, we can compare it with looping over
the solutions. We first set loopOF to TRUE, so we actually loop over the solutions. (We also reduce the
number of objective function evaluations.)
> popsize <- 20L; generations <- 100L
> de$nP <- popsize; de$nG <- generations</pre>
> ps$nP <- popsize; ps$nG <- generations
> de$loopOF <- TRUE; ps$loopOF <- TRUE</pre>
> (t1ps <- system.time(solPS <- PSopt(OF = OF, algo = ps, data = data)))
    user system elapsed
           0.004
  0.184
                    0.189
> (t1de <- system.time(solDE <- DEopt(OF = OF, algo = de, data = data)))</pre>
    user system elapsed
           0.000
  0.180
                    0.181
To evaluate the objective function in one step, we loopOF to FALSE.
> de$loopOF <- FALSE; ps$loopOF <- FALSE</pre>
> (t2ps <- system.time(solPS <- PSopt(OF = OF, algo = ps, data = data)))
    user system elapsed
  0.064
           0.000
                    0.064
```

```
> (t2de <- system.time(solDE <- DEopt(OF = OF, algo = de, data = data)))</pre>
```

```
user system elapsed
0.064 0.000 0.065
```

Speedup:

> t1ps[[3L]]/t2ps[[3L]]

```
[1] 2.9531
```

> t1de[[3L]]/t2de[[3L]]

```
[1] 2.7846
```

References

Manfred Gilli, Dietmar Maringer, and Enrico Schumann. *Numerical Methods and Optimization in Finance*. Elsevier, 2011.

William N. Venables and Brian D. Ripley. *Modern Applied Statistics with S.* Springer, 4th edition, 2002. URL http://www.stats.ox.ac.uk/pub/MASS4.