STATISTICAL DATA ANALYSIS: RECURRENCE PLOT

GÜNTHER SAWITZKI

Recurrence Plot: chirpneighs 20 40 80 100 120 Dimensions: 125 x 125

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2

1. Setup

	_ Input
save.RNGseed <- 87149 #.Random.seed	- Input
<pre>save.RNGkind <- RNGkind() # save.RNGseed</pre>	
save.RNGkind	
	Output
[1] "Mersenne-Twister" "Inversion"	- 000900
	_ Input
set.seed(save.RNGseed, save.RNGkind[1])	_ input
	_ Input
<pre>laptime <- function(){</pre>	
	k.time.start, class = "proc_time")[3],3))
<pre>chunk.time.start <<- proc.time() }</pre>	
# install.packages("sintro",repos="http:/	_ Input
library(sintro)	
We use	
1:1	_ Input
library(nonlinearTseries)	
To display state space, we us a variant of pai	rs().
	()
	_ Input
statepairs <- function(states, rank=FALSE	7){
main <- paste("Takens states:",de	<pre>pparse(substitute(states))) ukens,2,rank,ties.method="random")</pre>
main <- paste(main, " ranked")}	rens,2,1ank,tres.method-landom /
pairs(states,	
main=main,	
col=rgb(0,0,0,0.2)) }	
11 T 15 (1 1 m 1)	
1.1. Local Bottleneck. To allow experiment are aliased here.	ntal implementations, functions from nonlinearTseries
are anased nere.	
	Touris
local.buildTakens <- buildTakens	_ Input
	÷ .
local.findAllNeighbours <- nonlinearTseri	_ Input les:::findAllNeighbours

minor cosmetics added to recurrence-PlotAux

2. Test Cases

We set up a small series of test signals.

For convenience, some source code from other libraries is included to make this self-contained.

As a global constant, we set up the length of the series to be used.

```
nsignal <- 128
system.time.start <- proc.time()
```

For representation, we use a common layout.

```
sin10 <- function(n=nsignal) {sin( (1:n)/n* 2*pi*10)}
plotsignal(sin10())</pre>
```

See Figure 1 on the following page,

```
unif <- function(n=nsignal) {runif(n)}
xunif<-unif()
plotsignal(xunif)
```

See Figure 2 on the next page,

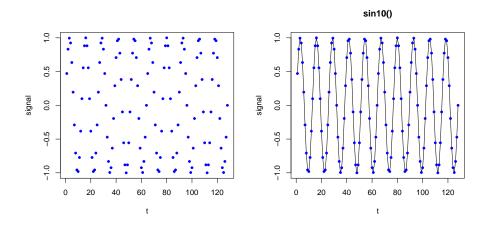


FIGURE 1. Test case: sin10. Signal and linear interpolation.

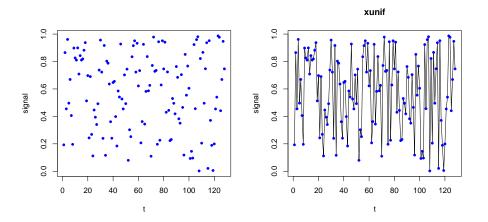
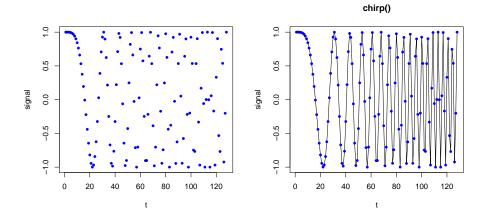


Figure 2. Test case: unif - uniform random numbers. Signal and linear interpolation.

```
Input
chirp <- function(n=nsignal) {</pre>
# this is copied from library(signal)
signal.chirp \leftarrow function(t, f0 = 0, t1 = 1, f1 = 100,
                   form = c("linear", "quadratic", "logarithmic"), phase = 0){
  form <- match.arg(form)</pre>
  phase <- 2*pi*phase/360</pre>
  switch(form,
    "linear" = {
         a \leftarrow pi*(f1 - f0)/t1
         b <- 2*pi*f0
         cos(a*t^2 + b*t + phase)
    },
    "quadratic" = {
         a <- (2/3*pi*(f1-f0)/t1/t1)
        b <- 2*pi*f0
         cos(a*t^3 + b*t + phase)
    },
```

See Figure 3,



 ${\tt Figure}$ 3. Test case: chirp signal. Signal and linear interpolation.

ToDo: doppler way

3. Recurrence States

Recurrence plots have been introduced in an attempt to understand near periodic in hydrodynamics. On the one hand, and etended theory on dynamical systems was available, covering deterministic models. A fundamental concept is that at a certain time a system is in some state, and developing from this. Defining the proper state space is a critical step in modelling.

The other toolkit ist that of stochastics processes, in particular Markov models. Classical time series assumes stationarity, and this is obviously not the way to go. A fundamental idea for Markov models is that the system state is seen in a temporal context: you have a Markov process, if you can define a (non-anticpating) state that has sufficient information for prediction: given this state, the future is independent from the past.

Recurrence, coming back to some state, is often a key to understand a near periodic system.

Hydrodynamics is a challenging problem. Understanding planetary motion is a historical challenge, and may be useful as an illustration.

As a simple illustration, let $x = (x_i)$ be a sequence, maybe near periodic. For now, think of i as a time index.

Recurrency plots have two steps. The first was a bold step by Floris Takens. If you do not know the state space of a system, for a choice of "dimension" d, take the sequence of d tuples taken from your

data to define the states.

$$u_i = (x_i, \dots, x_{i+d})$$

As a mere technical refinement: you may know that your data are a flattenened representation of t dimensional data. So you take

$$u_i = (x_i, \dots, x_{i+d*m}).$$

We ignore this detail here and take m = 1.

Conceptually, you define states by observed histories. For classical Markov setup, the state is defined by the previous information x_{i-1} , but for more combes situations you may have to step back in the past. Finding the appropriate d is the challenge. So it may be appropriate to view the Takens states as a family, indexed by the time scope d. The rest is structural information how to arrange items.

Of course it is possible to compress information here, sorting states and removing duplicates. Keeping the original definition as the advantage that we have the index i, so that u_i is the state at index position i.

But the states may have an inherent structure, which we may take into account or ignore. Since for this example, we are just in 4-dimensional space, marginal scatterplots may give enough information.

```
Input ________ Input ______ sintakens <- local.buildTakens( time.series=sin10(),embedding.dim=4, time.lag=1) statepairs(sintakens)
```

See Figure 4 on the next page.

```
uniftakens <- local.buildTakens( time.series=xunif,embedding.dim=4,time.lag=1)
statepairs(uniftakens)</pre>
```

See Figure 5 on page 8.

```
Input _______chirptakens <- local.buildTakens( time.series=chirp(),embedding.dim=4,time.lag=1) statepairs(chirptakens)
```

See Figure 6 on page 9

4. Recurrence Plots

The next step, taken in Eckmann *et al.* [1987] was to use a two dimensional display. Take a scatterplot with the Taken's staes a marginal. Take a sliding window of your process data, and for each i, find the "distance" of u_i from and to any of the collected states. If the distance is below some chosen threshold, mark the point (i, j) for which u(j) is in the ball of radius r(i) centred at u(i).

The original publication Eckmann $et\ al.\ [1987]$ actually used a nearest neighbourhood evnironment to cover about 10 data points.

The construction has considerable arbitrary choices. The critical radius may depend on the point *i*. In practical applications, using a constant radius is a common first step. Using a dichotomous marking was what presumably was necessary when the idea was introduced. With todays technology, we can allow a markup on a finer scale, as has been seen in Orion-1.

Takens states: sintakens

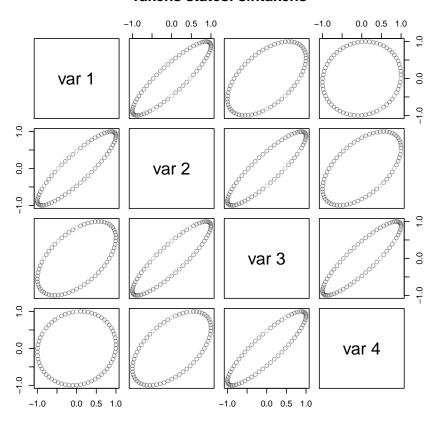


FIGURE 4. Test case: sinus. Note that marginal views of 1-dimensional circles in d space may appear as ellipses. Time used: 0.208 sec.

We can gain additional freedom by using a correlation view: instead of looking from one axis, we can walk along the diagonal, using two reference axis.

4.1. **Sinus.**

load(file="sin10neighs.RData")
local.recurrencePlotAux(sin10neighs)

4.2. Uniform random.

load(file="unifneighs.RData")
local.recurrencePlotAux(unifneighs)

4.3. Chirp Signal.

 $_$ Input $_$

Takens states: uniftakens

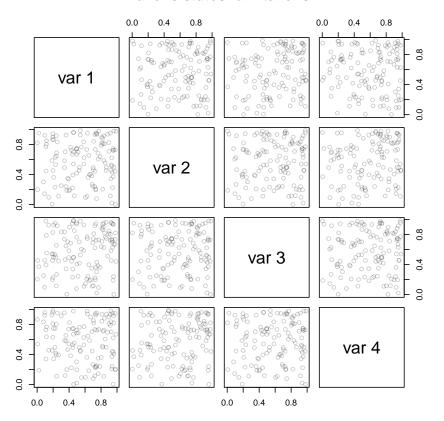


FIGURE 5. Test case: uniform random numbers. Time used: 0.211 sec.

chirpneighs<-local.findAllNeighbours(chirptakens,radius=0.6)#0.4
save(chirpneighs, file="chirpneighs.RData")</pre>

load(file="chirpneighs.RData")
local.recurrencePlotAux(chirpneighs)

5. Case Study: Geyser data

ToDo: extend to This is a classical data set with a two dimensional structure, waiting and waiting. two-dimensional

library(MASS)
data(faithful)

5.1. Geyser Eruptions.

data

Takens states: chirptakens

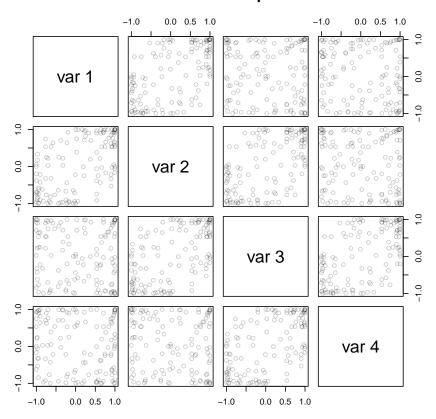


Figure 6. Test case: chirp signal. Time used: $0.185~{\rm sec.}$

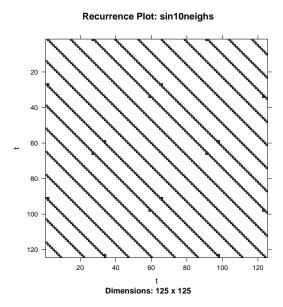


FIGURE 7. Recurrence Plot. Test case: sinus curves. Time used: 4.139 sec.

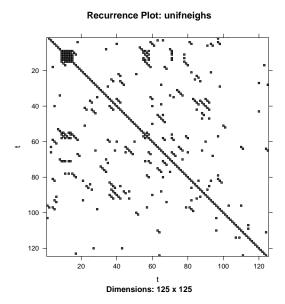


FIGURE 8. Recurrence Plot. Test case: uniform random numbers. Time used: 1.584 sec.

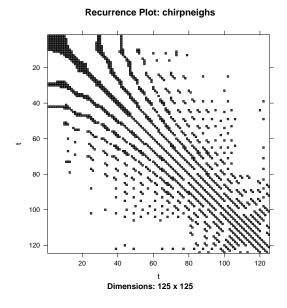


FIGURE 9. Recurrence Plot. Test case: chirp signal. Time used: 4.791 sec.

See Figure 10 on the facing page,

```
Input ______ Input _____ eruptionstakens4 <- local.buildTakens( time.series=faithful$eruptions, embedding.dim=4, time.lag=1) statepairs(eruptionstakens4)
```

See Figure 11 on the next page

```
Input ______eruptionsneighs4<-local.findAllNeighbours(eruptionstakens4, radius=0.8)
save(eruptionsneighs4, file="eruptionsneighs4.RData")
```

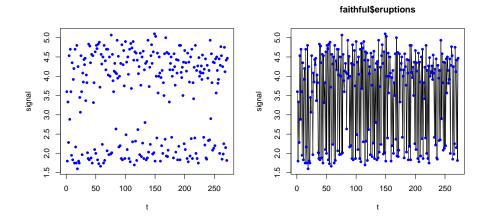


FIGURE 10. Example case: Old Faithful Geyser eruptions. Signal and linear interpolation.

Takens states: eruptionstakens4

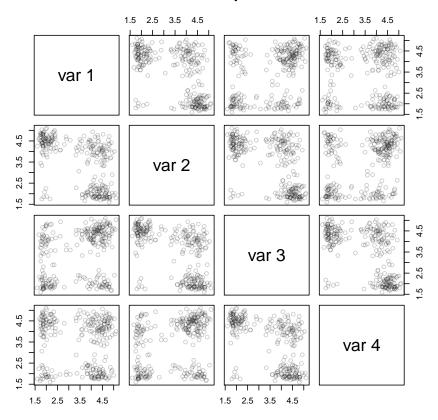


FIGURE 11. Example case: Old Faithful Geyser eruptions. Time used: 0.289 sec.

Recurrence Plot: eruptionsneighs4

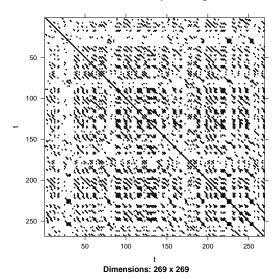


FIGURE 12. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=4. Time used: 21.304 sec.

5.1.1. Dim=2.

Input ______ Input _____ eruptionstakens2 <- local.buildTakens(time.series=faithful\$eruptions, embedding.dim=2, time.lag=1) statepairs(eruptionstakens2)

See Figure 13 on the facing page

Input eruptionsneighs2<-local.findAllNeighbours(eruptionstakens2, radius=0.8) save(eruptionsneighs2, file="eruptionsneighs2.RData")

load(file="eruptionsneighs2.RData")
local.recurrencePlotAux(eruptionsneighs2)

5.1.2. Dim=6.

Input _____eruptionstakens6 <- local.buildTakens(time.series=faithful\$eruptions,embedding.dim=6,time.lag=1) statepairs(eruptionstakens6)

See Figure 15 on page 14

Input eruptionsneighs6<-local.findAllNeighbours(eruptionstakens6, radius=0.8)
save(eruptionsneighs6, file="eruptionsneighs6.RData")

Takens states: eruptionstakens2

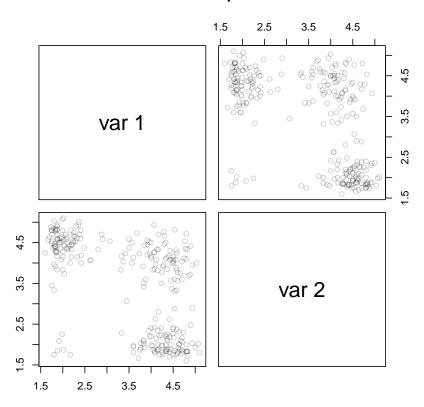


FIGURE 13. Example case: Old Faithful Geyser eruptions. Dim=2. Time used: $0.136~{\rm sec}.$

Recurrence Plot: eruptionsneighs2

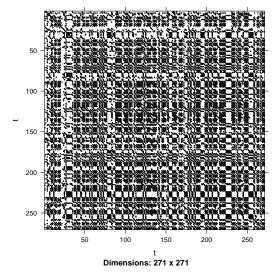


FIGURE 14. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=2. Time used: $67.43~{\rm sec}$.

Takens states: eruptionstakens6

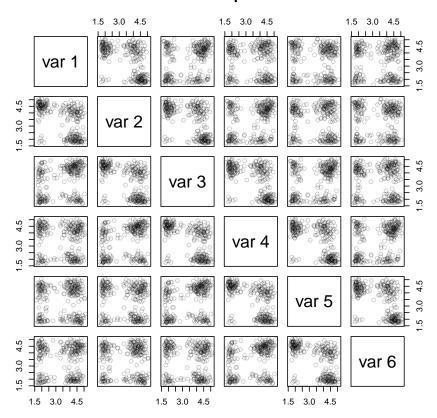


FIGURE 15. Example case: Old Faithful Geyser eruptions. Dim=6. Time used: $0.535~{\rm sec}.$

load(file="eruptionsneighs6.RData")
local.recurrencePlotAux(eruptionsneighs6)

5.1.3. Dim=8.

______Input _____eruptionstakens8 <- local.buildTakens(time.series=faithful\$eruptions,embedding.dim=8,time.lag=1) statepairs(eruptionstakens8)

See Figure 17 on the facing page

eruptionsneighs8<-local.findAllNeighbours(eruptionstakens8, radius=0.8)
save(eruptionsneighs8, file="eruptionsneighs8.RData")

Recurrence Plot: eruptionsneighs6

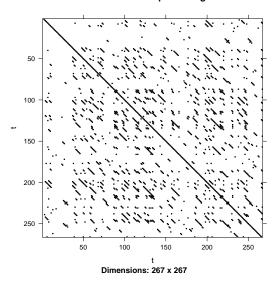


FIGURE 16. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=6. Time used: 7.062 sec.

Takens states: eruptionstakens8

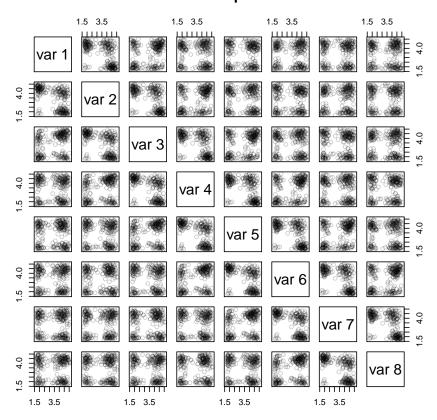


FIGURE 17. Example case: Old Faithful Geyser eruptions. Dim=8. Time used: $0.871~{\rm sec.}$

load(file="eruptionsneighs8.RData")
local.recurrencePlotAux(eruptionsneighs8)

Recurrence Plot: eruptionsneighs8

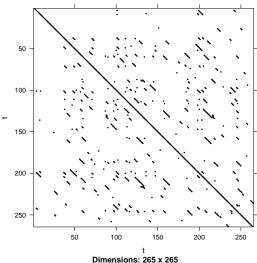


FIGURE 18. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=8. Time used: 2.711 sec.

- 5.2. **Geyser Eruptions: Comparison by Dimension.** For comparison, recurrence plots for the Geyser data with varying dimension are in Figure 19 on the next page
- 5.3. Geyser Waiting.

plotsignal(faithful\$waiting)

See Figure 20 on the facing page,

See Figure 21 on page 18

waitingneighs <-local.findAllNeighbours (waitingtakens, radius=16) save (waitingneighs, file="waitingneighs.Rdata")

load(file="waitingneighs.RData")
local.recurrencePlotAux(waitingneighs)

_ Input

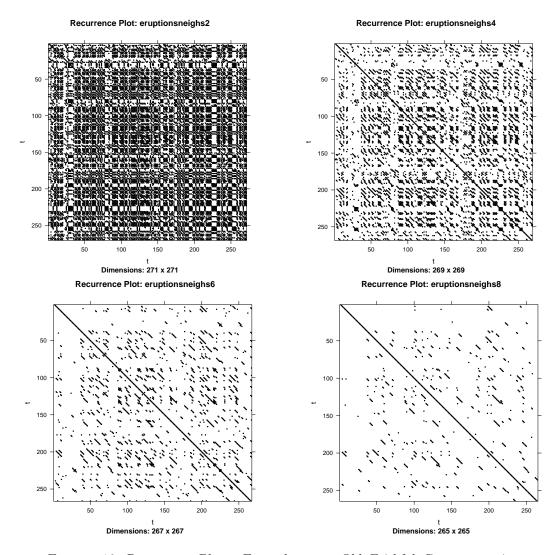


FIGURE 19. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=2, 4, 6, 8.

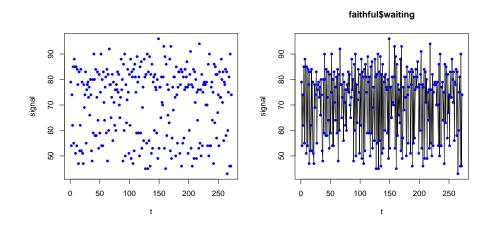


FIGURE 20. Example case: Old Faithful Geyser waiting. Signal and linear interpolation. Time used: $2.94~{\rm sec.}$

Takens states: waitingtakens

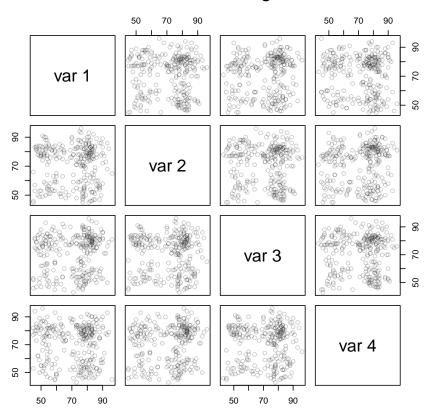


Figure 21. Example case: Old Faithful Geyser waiting. Time used: $0.277~{\rm sec.}$

Recurrence Plot: waitingneighs

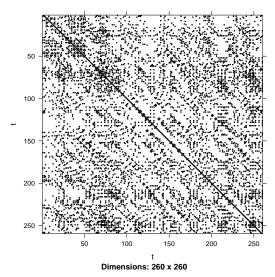


FIGURE 22. Recurrence Plot. Example case: Old Faithful Geyser waiting. Time used: 22.328 sec.

Only 128 da used in this

out too m pulses?

6. Case Study: HRV data

	Input	
library(RHRV)		
<pre>load("/data/pulse/rhrv/pkg/data/HRVData.rd</pre>		
<pre>load("/data/pulse/rhrv/pkg/data/HRVProcess</pre>		
#######################################	#########	
### code chunk number 1: creation		
#######################################	########	
<pre>hrv.data = CreateHRVData()</pre>		
<pre>hrv.data = SetVerbose(hrv.data, TRUE)</pre>		
#######################################	########	
### code chunk number 3: loading		
#######################################	########	
<pre>hrv.data = LoadBeatAscii(hrv.data, "example")</pre>	le.beats",	
<pre>RecordPath = "/data/pulse/rhrv/tuto</pre>	orial/beatsFolder")	
·		
	Output	
** Loading beats positions for record: exam	mple.beats **	
Path: /data/pulse/rhrv/tutorial/beatsFol	Lder	
Scale: 1		
Date: 01/01/1900		
Time: 00:00:00		
Number of beats: 17360		
1.411.501 01 504051 1.000		
	Input	
<pre># RecordPath = "beatsFolder")</pre>		
#######################################	########	
### code chunk number 4: derivating		
#######################################	########	
<pre>hrv.data = BuildNIHR(hrv.data)</pre>		
	Output	
** Calculating non-interpolated heart rate	**	
Number of beats: 17360		
	Input	
	Input	
plotsignal(hrv.data\$Beat\$RR)	при при	
See Figure 23 on the following page,		<u>ToDo:</u> We
		lies at appro
		2*RR. Coul
	Input	
hrvRRtakens4 <- local.buildTakens(time.se	Input	time.lag=1)
statenairs(hryRRtakens4)		processing,

See Figure 24 on the next page

statepairs(hrvRRtakens4)

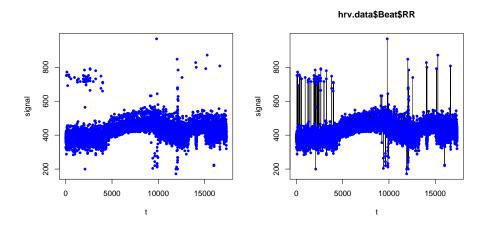


FIGURE 23. Example case: RHRV tutorial. Signal and linear interpolation.

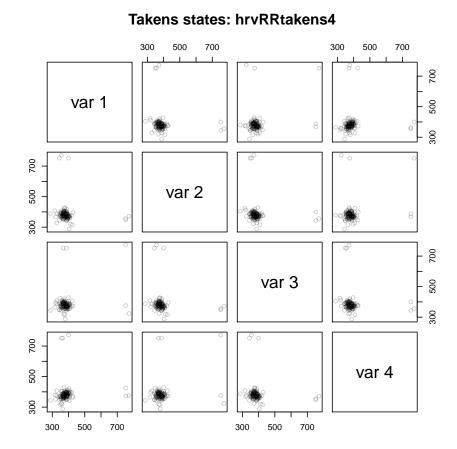


FIGURE 24. Example case: RHRV tutorial. Time used: 0.206 sec.

Takens states: hrvRRtakens4 ranked

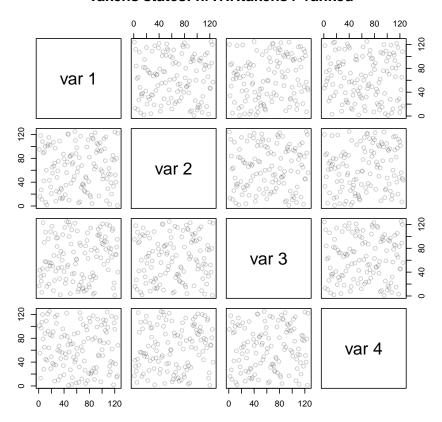


FIGURE 25. Example case: RHRV tutorial. Ranked data. Time used: 0.442 sec.

Input

hrvRRneighs4 <-local.findAllNeighbours(hrvRRtakens4, radius=16)
save(hrvRRneighs4, file="hrvRRneighs4.Rdata")

Time used: 0.024 sec.

load(file="hrvRRneighs4.RData")
local.recurrencePlotAux(hrvRRneighs4)

$6.1.\ RHRV:$ Comparison by Dimension.

We should the breathin so a time la order of 10 expected.

Input _______ Input _______ Input _______ Input _______ time.lag=1) hrvRRtakens2 <- local.buildTakens(time.series=hrv.data\$Beat\$RR[1:nsignal],embedding.dim=2,time.lag=1) hrvRRneighs2 <-local.findAllNeighbours(hrvRRtakens2, radius=16) save(hrvRRneighs2, file="hrvRRneighs2.Rdata")

Time used: 0.058 sec.

Recurrence Plot: hrvRRneighs4

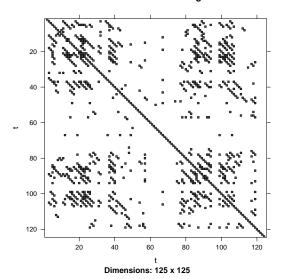


FIGURE 26. Recurrence Plot. Example case: RHRV tutorial. Dim=4. Time used: 3.289 sec.

```
load(file="hrvRRneighs2.RData")
local.recurrencePlotAux(hrvRRneighs2)
```

Time used: 10.709 sec.

```
hrvRRtakens6 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=6,time.lag=1)
hrvRRneighs6 <-local.findAllNeighbours(hrvRRtakens6, radius=16)
save(hrvRRneighs6, file="hrvRneighs6.Rdata")
```

Time used: 0.042 sec.

```
load(file="hrvRRneighs6.RData")
local.recurrencePlotAux(hrvRRneighs6)
```

Dim=6. Time used: 1.132 sec.

```
Input hrvRRtakens8 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=8,time.lag=1) hrvRRneighs8 <-local.findAllNeighbours(hrvRRtakens8, radius=32) save(hrvRRneighs8, file="hrvRRneighs8.Rdata")
```

Time used: 0.043 sec.

```
load(file="hrvRRneighs8.RData")
local.recurrencePlotAux(hrvRRneighs8)
```

Dim=8. Time used: 8.082 sec.

Time used: 1.908 sec.

ToDo: Coning difference

```
Input ______ Input _____ hrvRRtakens12 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=2,time.lag=1)
 hrvRRneighs12 <-local.findAllNeighbours(hrvRRtakens12, radius=16)
 save(hrvRRneighs12, file="hrvRRneighs12.Rdata")
Time used: 8.133 sec.
                                            _ Input _
 load(file="hrvRRneighs12.RData")
 local.recurrencePlotAux(hrvRRneighs12)
Time used: 10.824 sec.
                                             Input
hrvRRtakens16 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=16,time.lag=1)
 hrvRRneighs16 <-local.findAllNeighbours(hrvRRtakens16, radius=32)</pre>
 save(hrvRRneighs16, file="hrvRRneighs16.Rdata")
Time used: 10.866 sec.
                                            _ Input _
 load(file="hrvRRneighs16.RData")
 local.recurrencePlotAux(hrvRRneighs16)
```

6.2. Hart Rate Variation. Since we are not interested in heart rate (or pulse), but in heart rate variation, a proposal is to use scaled differences.

```
# source('/data/pulse/rhrv/pkg/R/BuildNIHR2.R', chdir = TRUE)
BuildNIDHR <-
function(HRVData, verbose=NULL) {
# Obtains instantaneous heart rate variation from beats positions
# D for difference
       if (!is.null(verbose)) {
               cat(" --- Warning: deprecated argument, using SetVerbose() instead ---\n
                                                                                          --- See hel
               SetVerbose(HRVData, verbose)
        7
       if (HRVData$Verbose) {
               cat("** Calculating non-interpolated heart rate differences **\n")
        if (is.null(HRVData$Beat$Time)) {
               cat(" --- ERROR: Beats positions not present... Impossible to calculate Heart Rate!! -
               return(HRVData)
        }
       NBeats=length(HRVData$Beat$Time)
       if (HRVData$Verbose) {
               cat(" Number of beats:",NBeats,"\n");
```

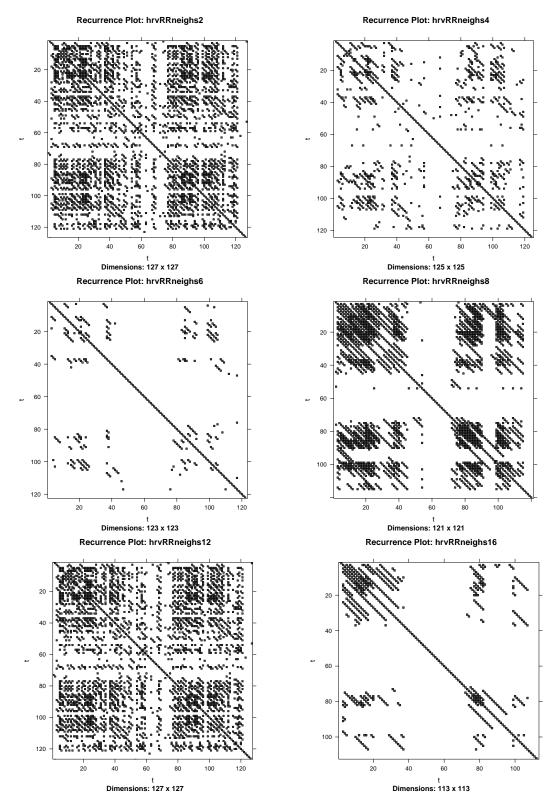


FIGURE 27. Recurrence Plot. Example case: RHRV tutorial. Dim=2, 4, 6, 8, 12, 16. Time used: 1.908 sec.

differences f

These are the displays we used before, now for HRRV:

```
______ Input ______ Input _____
```

Input -

See Figure 28,

HRRV <- hrv.data\$Beat\$HRRV

addition gs

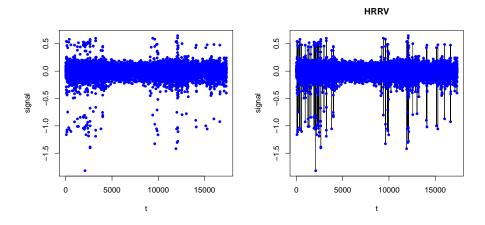


FIGURE 28. Example case: RHRV tutorial. HRRV Signal and linear interpolation.

Only 128 da used in this

See Figure 29

Takens states: hrvRRVtakens4

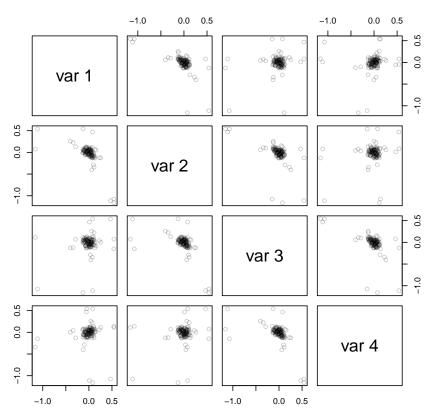


FIGURE 29. Example case: RHRV tutorial. HRRV Time used: 0.2 sec.

_____ Input _____

ToDo: findAll-Neighbours does not handle NAs See Figure 30 on the next page

statepairs(hrvRRVtakens4, rank=TRUE)

#use hack: findAllNeighbours does not handle NAs}
hrvRRVneighs4 <-local.findAllNeighbours(hrvRRVtakens4[-(1:2),],, radius=0.25)
save(hrvRRVneighs4, file="hrvRRVneighs4.Rdata")

Time used: 0.028 sec.

load(file="hrvRRVneighs4.RData")
local.recurrencePlotAux(hrvRRVneighs4)

<u>ToDo:</u> check. There seem to be strange artefacts.

We should expect the breathing rhythm, so a time lag in the order of 10 is to be expected.

ToDo: fix default setting for radius.

6.3. RHRV: Variation: Comparison by Dimension.

Takens states: hrvRRVtakens4 ranked

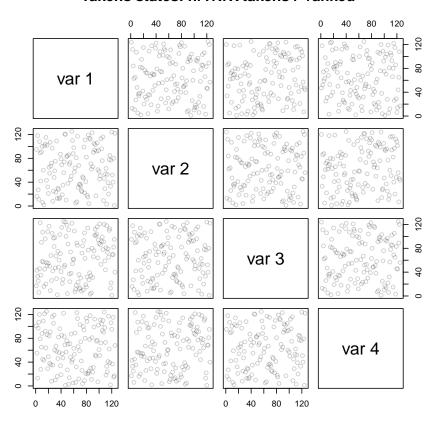


FIGURE 30. Example case: RHRV tutorial. Ranked HRRV data. Time used: $0.422~{\rm sec.}$

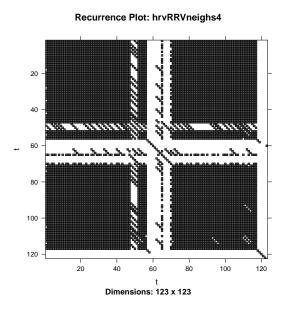


FIGURE 31. Recurrence Plot. Example case: RHRV tutorial. HRRV Dim=4. Time used: 36.025 sec.

```
hrvRRVneighs2 <-local.findAllNeighbours(hrvRRVtakens2[-(1:2),], radius=0.25)
save(hrvRRVneighs2, file="hrvRRVneighs2.Rdata")
Time used: 0.045 sec.
                                     _ Input _
load(file="hrvRRVneighs2.RData")
local.recurrencePlotAux(hrvRRVneighs2)
Time used: 42.818 sec.
                                      Input
hrvRRVtakens6 <- local.buildTakens( time.series=HRRV[1:nsignal],embedding.dim=6,time.lag=1)
hrvRRVneighs6 <-local.findAllNeighbours(hrvRRVtakens6[-(1:2),], radius=0.25)
save(hrvRRVneighs6, file="hrvRRVneighs6.Rdata")
Time used: 0.054 sec.
                                      Input
load(file="hrvRRVneighs6.RData")
local.recurrencePlotAux(hrvRRVneighs6)
Dim=6. Time used: 31.328 sec.
                                     Input
hrvRRVtakens8 <- local.buildTakens( time.series=HRRV[1:nsignal],embedding.dim=8,time.lag=1)
hrvRRVneighs8 <-local.findAllNeighbours(hrvRRVtakens8[-(1:2),], radius=0.25)
save(hrvRRVneighs8, file="hrvRRVneighs8.Rdata")
Time used: 0.05 sec.
                                     _ Input -
load(file="hrvRRVneighs8.RData")
local.recurrencePlotAux(hrvRRVneighs8)
Dim=8. Time used: 28.557 sec.
hrvRRVneighs12 <-local.findAllNeighbours(hrvRRVtakens12[-(1:2),], radius=0.25)
save(hrvRRVneighs12, file="hrvRRVneighs12.Rdata")
Time used: 28.61 sec.
                                     Input -
load(file="hrvRRVneighs12.RData")
local.recurrencePlotAux(hrvRRVneighs12)
```

Time used: 42.68 sec.

Time used: 42.73 sec.

load(file="hrvRRVneighs16.RData")

load(file="hrvkKVneighs16.KData")
local.recurrencePlotAux(hrvRRVneighs16)

Time used: 18.329 sec.

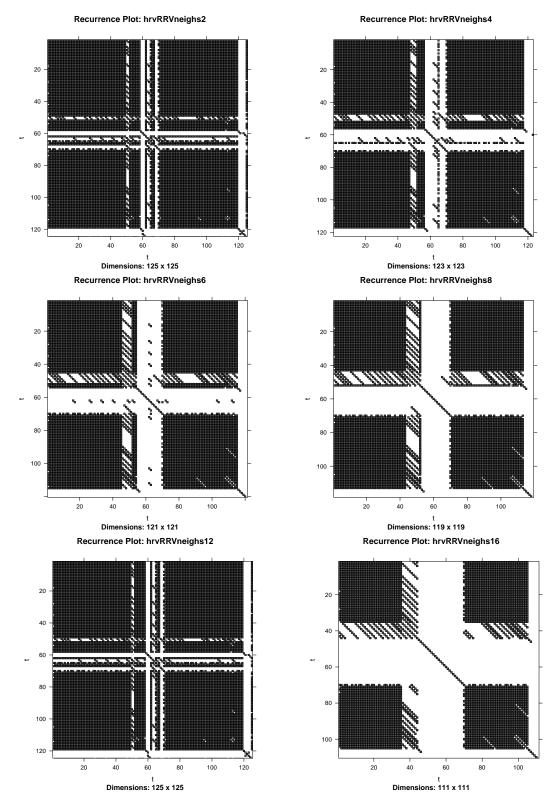


FIGURE 32. Recurrence Plot. Example case: RHRV tutorial. Dim=2, 4, 6, 8, 12, 16. Time used: 18.329 sec.

References

ECKMANN, JEAN-PIERRE, KAMPHORST, S OLIFFSON, & RUELLE, DAVID. 1987. Recurrence plots of dynamical systems. $Europhys.\ Lett,\ 4(9),\ 973-977.$

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R session info:

Total Sweave time used: 376.045 sec. at Sun Feb 9 17:41:09 2014.

- R version 3.0.2 (2013-09-25), x86_64-apple-darwin10.8.0
 Locale: en_GB.UTF-8/en_GB.UTF-8/en_GB.UTF-8/c/en_GB.UTF-8
 Base packages: base, datasets, graphics, grDevices, methods, stats, tcltk, utils
 Other packages: leaps 2.9, locfit 1.5-9.1, MASS 7.3-29, Matrix 1.1-2, mgcv 1.7-27, nlme 3.1-113, nonlinearTseries 0.2, rgl 0.93.996, RHRV 4.0, sintro 0.1-3, tkrplot 0.0-23, TSA 1.01, tseries 0.10-32, waveslim 1.7.3
 Loaded via a namespace (and not attached): grid 3.0.2, lattice 0.20-25, quadprog 1.5-5, tools 3.0.2, zoo 1.7-11

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CVS/Svn repository information:

 $\tt \$Source: /u/math/j40/cvsroot/lectures/src/data analysis/Rnw/recurrence.Rnw,v \$$ \$HeadURL: /u/math/j40/cvsroot/lectures/src/dataanalysis/Rnw/recurrence.Rnw,v \$

\$Revision: 1.2 \$

\$Date: 2014/02/05 20:05:07 \$

\$name: \$ \$Author: j40 \$

 $E\text{-}mail\ address:\ \texttt{gs@statlab.uni-heidelberg.de}$

GÜNTHER SAWITZKI STATLAB HEIDELBERG IM NEUENHEIMER FELD 294 D 69120 Heidelberg