STATISTICAL DATA ANALYSIS: RECURRENCE PLOT

GÜNTHER SAWITZKI

Contents

1. Setup	
1.1. Local Bottleneck	2
2. Test Cases	
3. Takens' Recurrence States	
4. Recurrence Plots	7
4.1. Sinus	8
4.2. Uniform random	8
4.3. Chirp Signal	10
5. Case Study: Geyser data	11
5.1. Geyser Eruptions	11
5.2. Geyser Eruptions: Comparison by Dimension	16
5.3. Geyser Waiting	16
6. Case Study: HRV data	17
6.1. RHRV: Comparison by Dimension	21
6.2. Hart Rate Variation	24
6.3. RHRV: Variation: Comparison by Dimension	27
References	31
Index	32

1

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2

1. Setup

	_ Input
save.RNGseed <- 87149 #.Random.seed	- Input
<pre>save.RNGkind <- RNGkind() # save.RNGseed</pre>	
save.RNGkind	
	Output
[1] "Mersenne-Twister" "Inversion"	- 000900
	_ Input
set.seed(save.RNGseed, save.RNGkind[1])	_ input
	_ Input
<pre>laptime <- function(){</pre>	
	k.time.start, class = "proc_time")[3],3))
<pre>chunk.time.start <<- proc.time() }</pre>	
<pre># install.packages("sintro",repos="http:/</pre>	_ Input
library(sintro)	
We use	
1:1	_ Input
library(nonlinearTseries)	
To display state space, we us a variant of pai	rs().
	()
	_ Input
statepairs <- function(states, rank=FALSE	7){
main <- paste("Takens states:",de	eparse(substitute(states))) ukens,2,rank,ties.method="random")
main <- paste(main, " ranked")}	rens,2,1ank,tres.method-landom /
pairs(states,	
main=main,	
col=rgb(0,0,0,0.2)) }	
11 T 15 41 1 T 1	
are aliased here.	ntal implementations, functions from nonlinearTseries
are anased nere.	
	Touris
local.buildTakens <- buildTakens	_ Input
	÷ .
local.findAllNeighbours <- nonlinearTseri	_ Input les:::findAllNeighbours

minor cosmetics added to recurrence-PlotAux

```
_{-} Input _{-}
#non-sparse variant
#local.recurrencePlotAux <- nonlinearTseries:::recurrencePlotAux</pre>
local.recurrencePlotAux=function(neighs){
        neighbourListNeighbourMatrix = function(){
          #neighs.matrix = Diagonal(ntakens)
          for (i in 1:ntakens){
            if (length(neighs[[i]])>0){
              for (j in neighs[[i]]){
                neighs.matrix[i,j] = 1
         # return (neighs.matrix)
 ntakens=length(neighs)
 neighs.matrix <- matrix(nrow=ntakens,ncol=ntakens)</pre>
 #neighbourListNeighbourMatrix()
   #neighs.matrix = Diagonal(ntakens)
         for (i in 1:ntakens){
            if (length(neighs[[i]])>0){
              for (j in neighs[[i]]){
                neighs.matrix[i,j] = 1
  # need no print because it is not a trellis object!!
  #print(
          image(neighs.matrix,xlab="t", ylab="t",
                main=paste("Recurrence Plot:",
                        deparse(substitute(neighs))
          )
```

2. Test Cases

We set up a small series of test signals.

For convenience, some source code from other libraries is included to make this self-contained.

As a global constant, we set up the length of the series to be used.

```
nsignal <- 128
system.time.start <- proc.time()
```

For representation, we use a common layout.

```
sin10 <- function(n=nsignal) {sin( (1:n)/n* 2*pi*10)}
plotsignal(sin10())</pre>
```

See Figure 1,

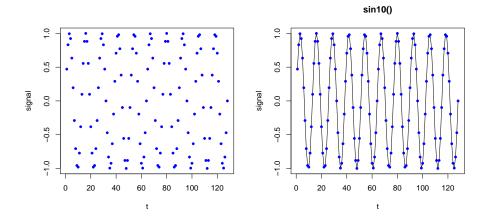


FIGURE 1. Test case: sin10. Signal and linear interpolation.

```
unif <- function(n=nsignal) {runif(n)}
xunif<-unif()
plotsignal(xunif)</pre>
```

See Figure 2 on the next page,

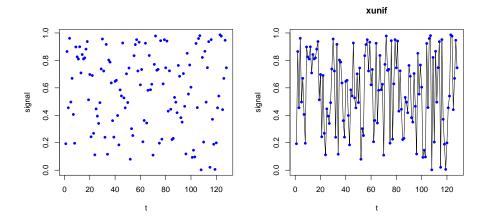


Figure 2. Test case: unif - uniform random numbers. Signal and linear interpolation.

```
},
   "quadratic" = {
        a <- (2/3*pi*(f1-f0)/t1/t1)
        b <- 2*pi*f0
        cos(a*t^3 + b*t + phase)
},
   "logarithmic" = {
        a <- 2*pi * t1 / log(f1 - f0)
        b <- 2*pi * f0
        x <- (f1-f0)^(1/t1)
        cos(a*x^t + b*t + phase)
})
}
signal.chirp(seq(0, 0.6, len=nsignal))
}
plotsignal(chirp())</pre>
```

See Figure 3,

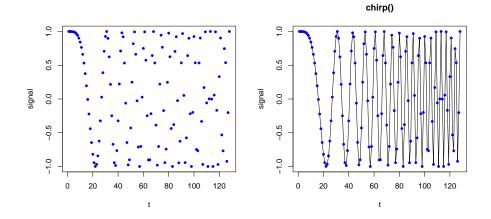


FIGURE 3. Test case: chirp signal. Signal and linear interpolation.

3. Takens' Recurrence States

Recurrence plots have been introduced in an attempt to understand near periodic in hydrodynamics. On the one hand, and etended theory on dynamical systems was available, covering deterministic models. A fundamental concept is that at a certain time a system is in some state, and developing from this. Defining the proper state space is a critical step in modelling.

The other toolkit ist that of stochastics processes, in particular Markov models. Classical time series assumes stationarity, and this is obviously not the way to go. A fundamental idea for Markov models is that the system state is seen in a temporal context: you have a Markov process, if you can define a (non-anticpating) state that has sufficient information for prediction: given this state, the future is independent from the past.

Recurrence, coming back to some state, is often a key to understand a near periodic system.

Hydrodynamics is a challenging problem. Understanding planetary motion is a historical challenge, and may be useful as an illustration.

As a simple illustration, let $x = (x_i)$ be a sequence, maybe near periodic. For now, think of i as a time index.

Recurrency plots have two steps. The first was a bold step by Floris Takens. If you do not know the state space of a system, for a choice of "dimension" d, take the sequence of d tuples taken from your data to define the states.

$$u_i = (x_i, \dots, x_{i+d})$$

As a mere technical refinement: you may know that your data are a flattenened representation of t dimensional data. So you take

$$u_i = (x_i, \dots, x_{i+d*m}).$$

This may be a relict of FORTRAN times, where it was common to flatten two-dimensional structures by case. We ignore this detail here and take m = 1.

Conceptually, you define states by observed histories. For classical Markov setup, the state is defined by the previous information x_{i-1} , but for more combles situations you may have to step back in the past. Finding the appropriate d is the challenge. So it may be appropriate to view the Takens states as a family, indexed by the time scope d. The rest is structural information how to arrange items.

Of course it is possible to compress information here, sorting states and removing duplicates. Keeping the original definition as the advantage that we have the index i, so that u_i is the state at index position i.

But the states may have an inherent structure, which we may take into account or ignore. Since for this example, we are just in 4-dimensional space, marginal scatterplots may give enough information.

sintakens <- local.buildTakens(time.series=sin10(),embedding.dim=4, time.lag=1)
statepairs(sintakens)</pre>

See Figure 4 on the next page.

ToDo: add support for higher dimensional signals

Input _____

uniftakens <- local.buildTakens(time.series=xunif,embedding.dim=4,time.lag=1) statepairs(uniftakens)

Takens states: sintakens

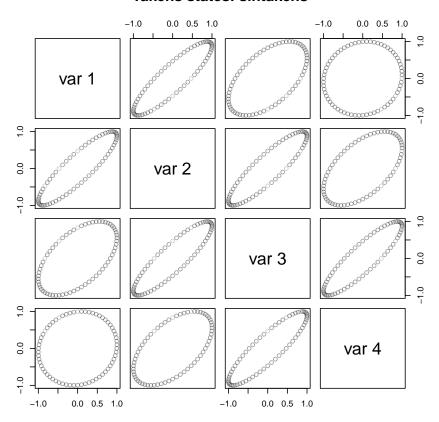


FIGURE 4. Test case: sinus. Note that marginal views of 1-dimensional circles in d space may appear as ellipses. Time used: 0.201 sec.

See Figure 5 on the following page.

See Figure 6 on page 9

4. Recurrence Plots

The next step, taken in Eckmann *et al.* [1987] was to use a two dimensional display. Take a scatterplot with the Taken's staes a marginal. Take a sliding window of your process data, and for each i, find the "distance" of u_i from and to any of the collected states. If the distance is below some chosen threshold, mark the point (i, j) for which u(j) is in the ball of radius r(i) centred at u(i).

The original publication Eckmann *et al.* [1987] actually used a nearest neighbourhood evnironment to cover about 10 data points.

The construction has considerable arbitrary choices. The critical radius may depend on the point i. In practical applications, using a constant radius is a common first step. Using a dichotomous

Takens states: uniftakens

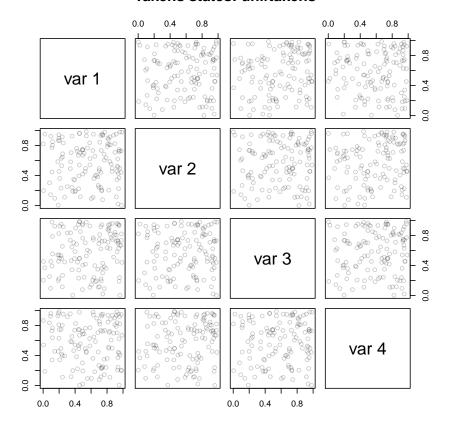


FIGURE 5. Test case: uniform random numbers. Time used: 0.212 sec.

ToDo: support distance instead of 0/1 indicators

marking was what presumably was necessary when the idea was introduced. With todays technology, we can allow a markup on a finer scale, as has been seen in Orion-1.

We can gain additional freedom by using a correlation view: instead of looking from one axis, we can walk along the diagonal, using two reference axis.

Helpful hints how to interpret recurrence plots are in "Recurrence Plots At A Glance" http://www.recurrence-plot.tk/glance.php.

4.1. **Sinus.**

load(file="sin10neighs.RData")
local.recurrencePlotAux(sin10neighs)

4.2. Uniform random.

load(file="unifneighs.RData")
local.recurrencePlotAux(unifneighs)

Takens states: chirptakens

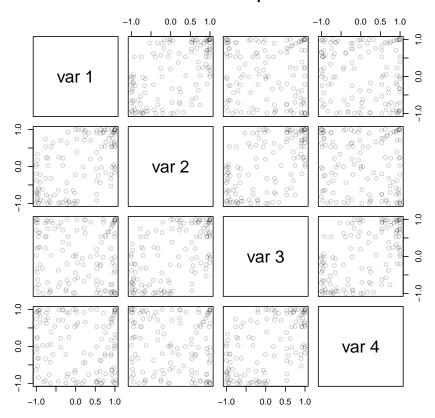


Figure 6. Test case: chirp signal. Time used: $0.192~{\rm sec.}$

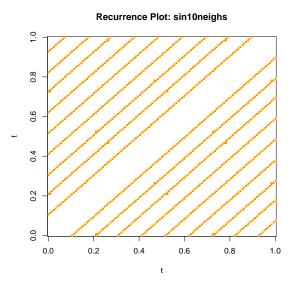


FIGURE 7. Recurrence Plot. Test case: sinus curves. Time used: 0.091 sec.

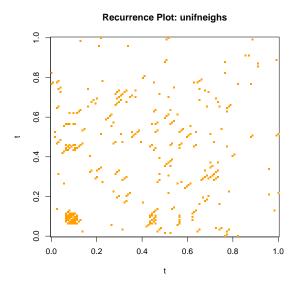


FIGURE 8. Recurrence Plot. Test case: uniform random numbers. Time used: $0.084~{\rm sec.}$

4.3. Chirp Signal.

```
chirpneighs <-local.findAllNeighbours(chirptakens, radius=0.6)#0.4
save(chirpneighs, file="chirpneighs.RData")
```

load(file="chirpneighs.RData")
local.recurrencePlotAux(chirpneighs)



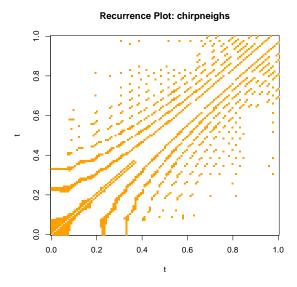


Figure 9. Recurrence Plot. Test case: chirp signal. Time used: $0.082~{\rm sec.}$

5. Case Study: Geyser data

This is a classical data set with a two dimensional structure, waiting and waiting.

ToDo: extend to dimensional

library(MASS)
data(faithful)

_ Input _

5.1. Geyser Eruptions.

plotsignal(faithful\$eruptions)

Input -

See Figure 10,

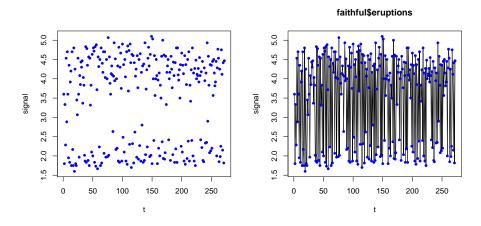


FIGURE 10. Example case: Old Faithful Geyser eruptions. Signal and linear interpolation.

Input ______ Input _____ eruptionstakens4 <- local.buildTakens(time.series=faithful\$eruptions, embedding.dim=4, time.lag=1) statepairs(eruptionstakens4)

See Figure 11 on the next page

eruptionsneighs4<-local.findAllNeighbours(eruptionstakens4, radius=0.8) save(eruptionsneighs4, file="eruptionsneighs4.RData")

Input -

Takens states: eruptionstakens4

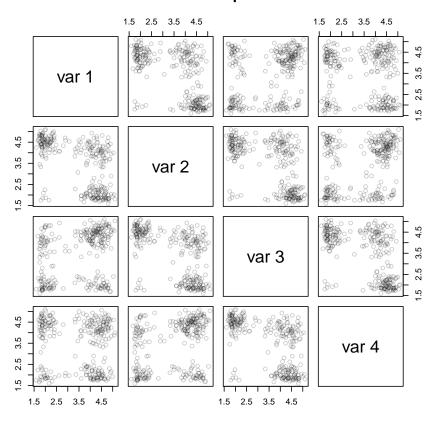


FIGURE 11. Example case: Old Faithful Geyser eruptions. Time used: $0.303~{\rm sec.}$

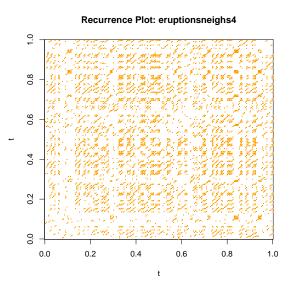


FIGURE 12. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=4. Time used: $0.184~{\rm sec}$.

5.1.1. Dim=2.

See Figure 13

Takens states: eruptionstakens2

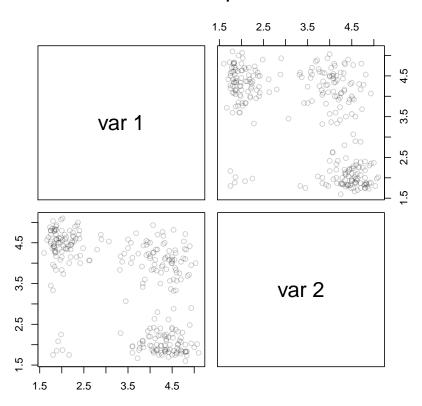


FIGURE 13. Example case: Old Faithful Geyser eruptions. Dim=2. Time used: $0.111~{\rm sec.}$

Input ______eruptionsneighs2<-local.findAllNeighbours(eruptionstakens2, radius=0.8) save(eruptionsneighs2, file="eruptionsneighs2.RData")

Input _

load(file="eruptionsneighs2.RData")
local.recurrencePlotAux(eruptionsneighs2)

Recurrence Plot: eruptionsneighs2

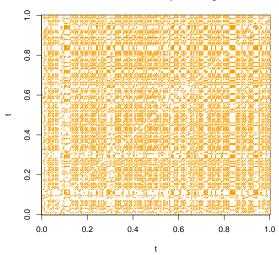


FIGURE 14. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=2. Time used: 0.374 sec.

Input

_ Input -

eruptionsneighs8<-local.findAllNeighbours(eruptionstakens8, radius=0.8)

save(eruptionsneighs8, file="eruptionsneighs8.RData")

Takens states: eruptionstakens6

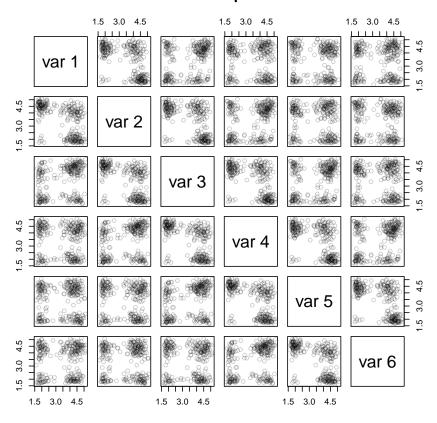


FIGURE 15. Example case: Old Faithful Geyser eruptions. Dim=6. Time used: $0.555~{\rm sec}.$

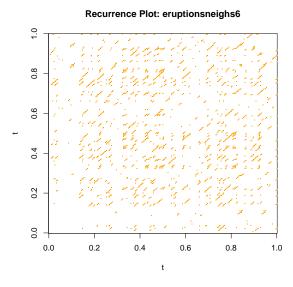


FIGURE 16. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=6. Time used: $0.123~{\rm sec.}$

Takens states: eruptionstakens8

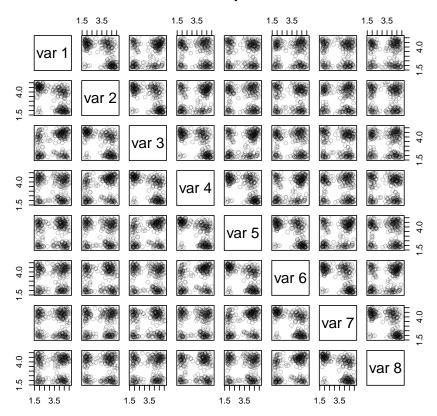


FIGURE 17. Example case: Old Faithful Geyser eruptions. Dim=8. Time used: $0.861~{\rm sec}.$

load(file="eruptionsneighs8.RData")
local.recurrencePlotAux(eruptionsneighs8)

- 5.2. **Geyser Eruptions: Comparison by Dimension.** For comparison, recurrence plots for the Geyser data with varying dimension are in Figure 19 on page 18
- 5.3. Geyser Waiting.

______ Input ______ Input _____

See Figure 20 on page 18,

waitingtakens <- local.buildTakens(time.series=faithful\$waiting,embedding.dim=4,time.lag=4)
statepairs(waitingtakens)</pre>

See Figure 21 on page 19

Recurrence Plot: eruptionsneighs8

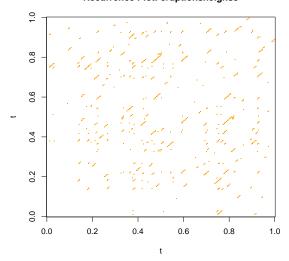


FIGURE 18. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=8. Time used: 0.119 sec.

waitingneighs<-local.findAllNeighbours(waitingtakens, radius=16)
save(waitingneighs, file="waitingneighs.Rdata")

load(file="waitingneighs.RData")

Input -

local.recurrencePlotAux(waitingneighs)

6. Case Study: HRV data

Only 128 da used in this

Output

** Loading beats positions for record: example.beats **

Path: /data/pulse/rhrv/tutorial/beatsFolder

Scale: 1

Date: 01/01/1900

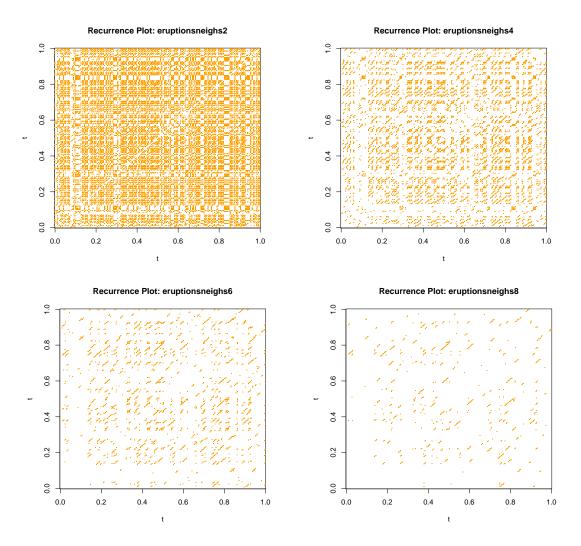


FIGURE 19. Recurrence Plot. Example case: Old Faithful Geyser eruptions. Dim=2, 4, 6, 8.

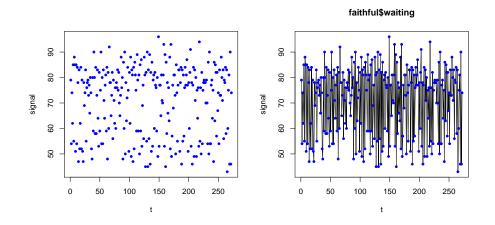


FIGURE 20. Example case: Old Faithful Geyser waiting. Signal and linear interpolation. Time used: $0.324~{\rm sec.}$

Takens states: waitingtakens

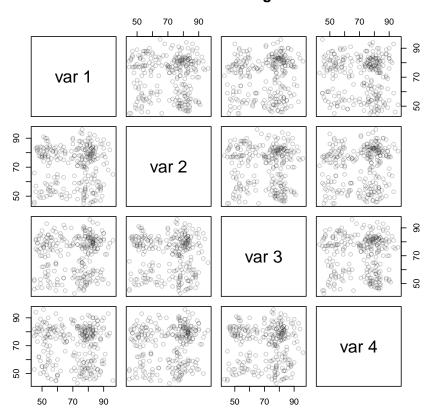


FIGURE 21. Example case: Old Faithful Geyser waiting. Time used: 0.257 sec.

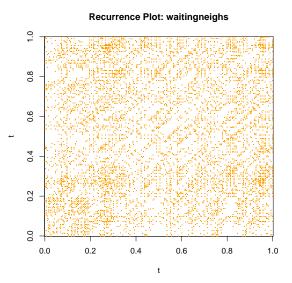


FIGURE 22. Recurrence Plot. Example case: Old Faithful Geyser waiting. Time used: $0.186~{\rm sec.}$

Time: 00:00:00 Number of beats: 17360

ToDo: We have outlies at approximately 2*RR. Could this be an artefact of preprocessing, filtering out too many impulses?

See Figure 23,

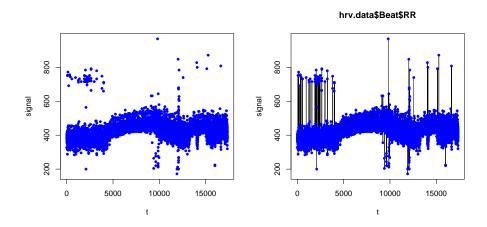


FIGURE 23. Example case: RHRV tutorial. Signal and linear interpolation.

Input ______ Input _____ hrvRRtakens4 <- local.buildTakens(time.series=hrv.data\$Beat\$RR[1:nsignal],embedding.dim=4,time.lag=1) statepairs(hrvRRtakens4)

See Figure 24 on the next page

Takens states: hrvRRtakens4

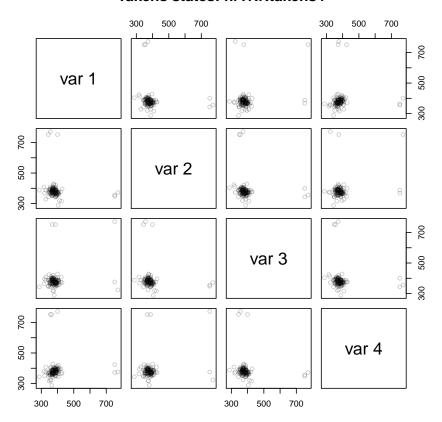


FIGURE 24. Example case: RHRV tutorial. Time used: 0.16 sec.

See Figure 25 on the following page

Time used: 0.036 sec.

```
load(file="hrvRRneighs4.RData")
local.recurrencePlotAux(hrvRRneighs4)
```

6.1. RHRV: Comparison by Dimension.

We should the breathin so a time la order of 10 expected.

```
Input _______ Input _______ hrvRRtakens2 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=2,time.lag=1) hrvRRneighs2 <-local.findAllNeighbours(hrvRRtakens2, radius=16) save(hrvRRneighs2, file="hrvRRneighs2.Rdata")
```

Time used: 0.042 sec.

Takens states: hrvRRtakens4 ranked

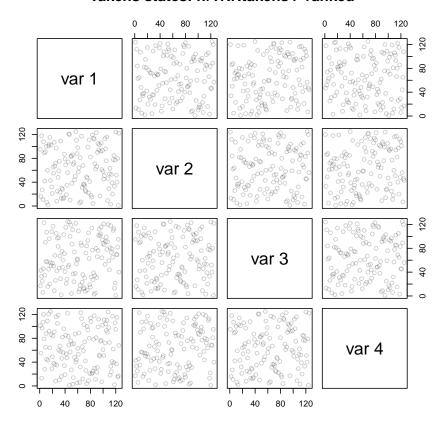


FIGURE 25. Example case: RHRV tutorial. Ranked data. Time used: 0.38 sec.

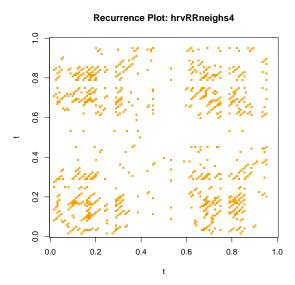


FIGURE 26. Recurrence Plot. Example case: RHRV tutorial. Dim=4. Time used: $0.106~{\rm sec.}$

Time used: 0.188 sec.

```
_ Input _
load(file="hrvRRneighs2.RData")
local.recurrencePlotAux(hrvRRneighs2)
Time used: 0.125 sec.
                                           Input
hrvRRtakens6 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=6,time.lag=1)
hrvRRneighs6 <-local.findAllNeighbours(hrvRRtakens6, radius=16)
save(hrvRRneighs6, file="hrvRRneighs6.Rdata")
Time used: 0.035 sec.
                                           Input -
load(file="hrvRRneighs6.RData")
local.recurrencePlotAux(hrvRRneighs6)
Dim=6. Time used: 0.089 sec.
                                           Input
hrvRRtakens8 <- local.buildTakens( time.series-hrv.data$Beat$RR[1:nsignal],embedding.dim=8,time.lag=1)
hrvRRneighs8 <-local.findAllNeighbours(hrvRRtakens8, radius=32)
save(hrvRRneighs8, file="hrvRRneighs8.Rdata")
Time used: 0.04 sec.
                                          _ Input _
load(file="hrvRRneighs8.RData")
local.recurrencePlotAux(hrvRRneighs8)
Dim=8. Time used: 0.124 sec.
                                           Input
hrvRRtakens12 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=2,time.lag=1)
hrvRRneighs12 <-local.findAllNeighbours(hrvRRtakens12, radius=16)</pre>
save(hrvRRneighs12, file="hrvRRneighs12.Rdata")
Time used: 0.184 sec.
load(file="hrvRRneighs12.RData")
local.recurrencePlotAux(hrvRRneighs12)
Time used: 0.13 sec.
                                           Input
hrvRRtakens16 <- local.buildTakens( time.series=hrv.data$Beat$RR[1:nsignal],embedding.dim=16,time.lag=1)
hrvRRneighs16 <-local.findAllNeighbours(hrvRRtakens16, radius=32)
 save(hrvRRneighs16, file="hrvRRneighs16.Rdata")
```

```
load(file="hrvRRneighs16.RData")
local.recurrencePlotAux(hrvRRneighs16)
```

ToDo: Consider using differences

Time used: 0.107 sec.

6.2. Hart Rate Variation. Since we are not interested in heart rate (or pulse), but in heart rate variation, a proposal is to use scaled differences.

```
# source('/data/pulse/rhrv/pkg/R/BuildNIHR2.R', chdir = TRUE)
BuildNIDHR <-
\verb|function(HRVData, verbose=NULL)| \{ \\
# Obtains instantaneous heart rate variation from beats positions
# D for difference
        if (!is.null(verbose)) {
                cat(" --- Warning: deprecated argument, using SetVerbose() instead ---\n --- See hel
                SetVerbose(HRVData, verbose)
        }
        if (HRVData$Verbose) {
                cat("**\ {\it Calculating\ non-interpolated\ heart\ rate\ differences\ **\n"})
        }
        if (is.null(HRVData$Beat$Time)) {
                cat(" --- ERROR: Beats positions not present... Impossible to calculate Heart Rate!! -
                return(HRVData)
        }
        NBeats=length(HRVData$Beat$Time)
        if (HRVData$Verbose) {
               cat(" Number of beats:",NBeats,"\n");
        }
  # addition gs
   \#using NA, not constant extrapolation as else in RHRV
   #drr=c(NA,NA,1000.0*
                               diff(HRVData$Beat$Time, lag=1 , differences=2))
   HRVData$Beat$dRR=c(NA, NA,
           1000.0*diff(HRVData$Beat$Time, lag=1, differences=2))
   HRVData$Beat$avRR=(c(NA,HRVData$Beat$RR[-1])+HRVData$Beat$RR)/2
   HRVData$Beat$HRRV <- HRVData$Beat$dRR/HRVData$Beat$avRR</pre>
        return(HRVData)
}
```

differences for HRV

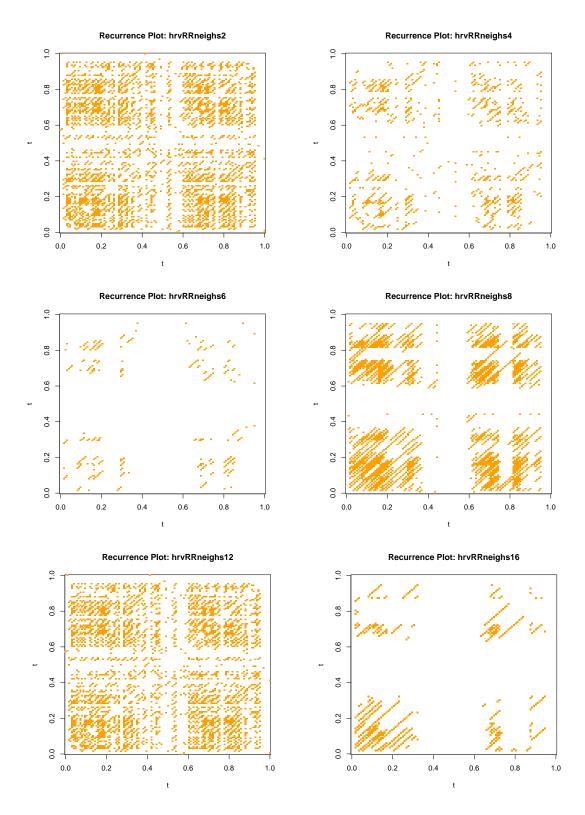


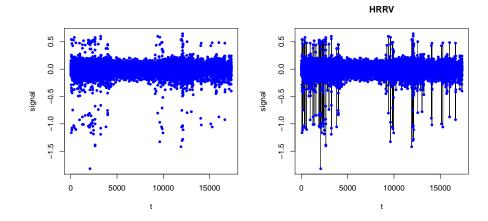
FIGURE 27. Recurrence Plot. Example case: RHRV tutorial. Dim=2, 4, 6, 8, 12, 16. Time used: 0.108 sec.

HRRV <- hrv.data\$Beat\$HRRV

These are the displays we used before, now for HRRV:

plotsignal(HRRV)

See Figure 28,



Input

Only 128 data points used in this section

FIGURE 28. Example case: RHRV tutorial. HRRV Signal and linear interpolation.

See Figure 29 on the facing page

statepairs(hrvRRVtakens4, rank=TRUE)

ToDo: findAll-Neighbours does not handle NAs

See Figure 30 on page 28

#use hack: findAllNeighbours does not handle NAs}
hrvRRVneighs4 <-local.findAllNeighbours(hrvRRVtakens4[-(1:2),],, radius=0.25)
save(hrvRRVneighs4, file="hrvRRVneighs4.Rdata")

Time used: 0.022 sec.

Input _______ Input ______ load(file="hrvRRVneighs4.RData") local.recurrencePlotAux(hrvRRVneighs4)

<u>ToDo:</u> check. There seem to be strange artefacts.

Takens states: hrvRRVtakens4

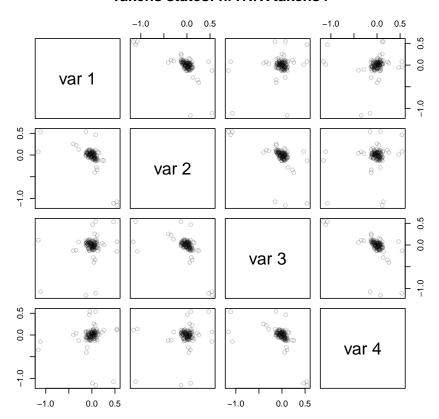


FIGURE 29. Example case: RHRV tutorial. HRRV Time used: 0.204 sec.

6.3. RHRV: Variation: Comparison by Dimension.

Input
hrvRRVtakens2 <- local.buildTakens(time.series=HRRV[1:nsignal],embedding.dim=2,time.lag=1)
hrvRRVneighs2 <-local.findAllNeighbours(hrvRRVtakens2[-(1:2),], radius=0.25)
save(hrvRRVneighs2, file="hrvRRVneighs2.Rdata")

Time used: 0.042 sec.

load(file="hrvRRVneighs2.RData")
local.recurrencePlotAux(hrvRRVneighs2)

Time used: 0.278 sec.

Input
hrvRRVtakens6 <- local.buildTakens(time.series=HRRV[1:nsignal],embedding.dim=6,time.lag=1)
hrvRRVneighs6 <-local.findAllNeighbours(hrvRRVtakens6[-(1:2),], radius=0.25)
save(hrvRRVneighs6, file="hrvRRVneighs6.Rdata")

We should expect the breathing rhythm, so a time lag in the order of 10 is to be expected.

ToDo: fix default setting for radius.

Eckmann uses

NN=10

Takens states: hrvRRVtakens4 ranked

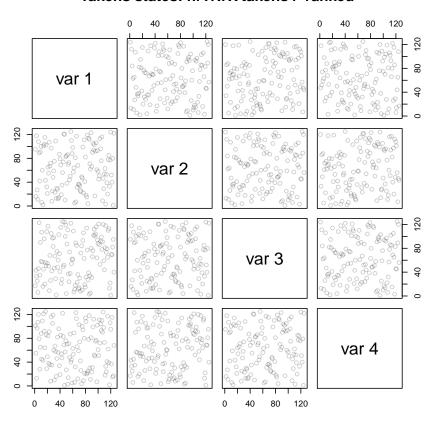


FIGURE 30. Example case: RHRV tutorial. Ranked HRRV data. Time used: 0.451 sec.

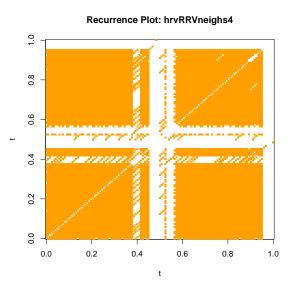


FIGURE 31. Recurrence Plot. Example case: RHRV tutorial. HRRV Dim=4. Time used: $0.219~{\rm sec.}$

Time used: 0.066 sec.

```
Input
 load(file="hrvRRVneighs6.RData")
 local.recurrencePlotAux(hrvRRVneighs6)
Dim=6. Time used: 0.203 sec.
                                            Input
 hrvRRVtakens8 <- local.buildTakens( time.series=HRRV[1:nsignal],embedding.dim=8,time.lag=1)
 hrvRRVneighs8 <-local.findAllNeighbours(hrvRRVtakens8[-(1:2),], radius=0.25)
 save(hrvRRVneighs8, file="hrvRRVneighs8.Rdata")
Time used: 0.048 sec.
                                           _ Input _
load(file="hrvRRVneighs8.RData")
 local.recurrencePlotAux(hrvRRVneighs8)
Dim=8. Time used: 0.206 sec.
                                            Input
hrvRRVtakens12 <- local.buildTakens( time.series=HRRV[1:nsignal],embedding.dim=2,time.lag=1)
 hrvRRVneighs12 <-local.findAllNeighbours(hrvRRVtakens12[-(1:2),], radius=0.25)
 save(hrvRRVneighs12, file="hrvRRVneighs12.Rdata")
Time used: 0.266 sec.
                                            _ Input
 load(file="hrvRRVneighs12.RData")
 local.recurrencePlotAux(hrvRRVneighs12)
Time used: 0.259 sec.
Input ______ Input ______ hrvRRVtakens16 <- local.buildTakens( time.series=HRRV[1:nsignal],embedding.dim=16,time.lag=1)
 hrvRRVneighs16 <-local.findAllNeighbours(hrvRRVtakens16[-(1:2),], radius=0.25)
 save(hrvRRVneighs16, file="hrvRRVneighs16.Rdata")
Time used: 0.305 sec.
                                           \_ Input \_
load(file="hrvRRVneighs16.RData")
 local.recurrencePlotAux(hrvRRVneighs16)
```

Time used: 0.17 sec.

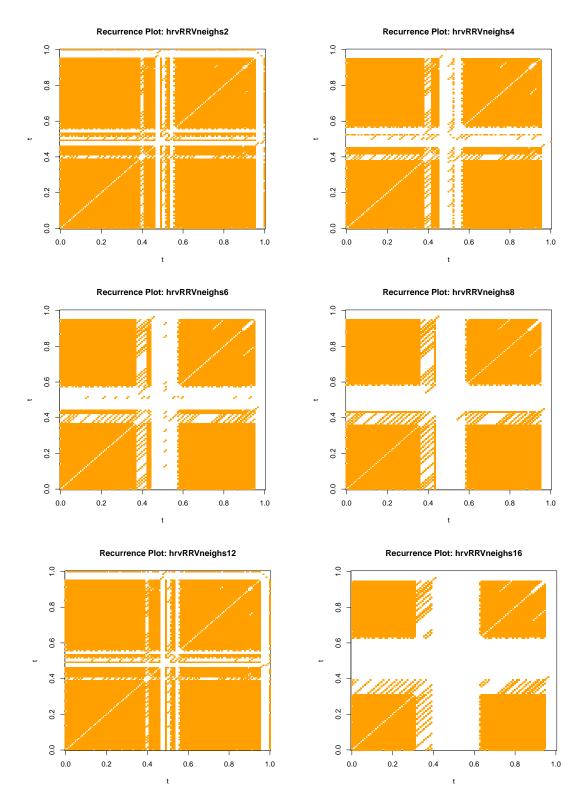


FIGURE 32. Recurrence Plot. Example case: RHRV tutorial. Dim=2, 4, 6, 8, 12, 16. Time used: $0.17~{\rm sec.}$

References

ECKMANN, JEAN-PIERRE, KAMPHORST, S OLIFFSON, & RUELLE, DAVID. 1987. Recurrence plots of dynamical systems. $Europhys.\ Lett,\ 4(9),\ 973-977.$

Index

ToDo

- $2\colon$ include doppler waves lim, 5
- 3: add support for higher dimensional signals, 6
- 4: support distance instead of 0/1 indicators, 8
- 5: Geyser: extend to two-dimensional data, 11
- 6: Consider using differences, 24
- 6: We have outlies at approximately 2*RR. Could this be an artefact of preprocessing, filtering out too many impulses?, 20
- $6\colon\mbox{check}.$ There seem to be strange artefacts., 26
- $6\colon \mathrm{findAllNeighbours}$ does not handle NAs, 26
- 6: fix default setting for radius. Eckmann uses NN=10, 27

Geyser, 11

heart rate, 17

heart rate variation, 26

R session info:

Total Sweave time used: 11.893 sec. at Mon Feb 10 16:49:55 2014.

- R version 3.0.2 (2013-09-25), x86_64-apple-darwin10.8.0
 Locale: en_GB.UTF-8/en_GB.UTF-8/en_GB.UTF-8/c/en_GB.UTF-8
 Base packages: base, datasets, graphics, grDevices, methods, stats, tcltk, utils
 Other packages: leaps 2.9, locfit 1.5-9.1, MASS 7.3-29, Matrix 1.1-2, mgcv 1.7-27, nlme 3.1-113, nonlinearTseries 0.2, rgl 0.93.996, RHRV 4.0, sintro 0.1-3, tkrplot 0.0-23, TSA 1.01, tseries 0.10-32, waveslim 1.7.3
 Loaded via a namespace (and not attached): grid 3.0.2, lattice 0.20-25, quadprog 1.5-5, tools 3.0.2, zoo 1.7-11

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CVS/Svn repository information:

 $\tt \$Source: /u/math/j40/cvsroot/lectures/src/data analysis/Rnw/recurrence.Rnw,v \$$ \$HeadURL: /u/math/j40/cvsroot/lectures/src/dataanalysis/Rnw/recurrence.Rnw,v \$

\$Revision: 1.2 \$

\$Date: 2014/02/05 20:05:07 \$

\$name: \$ \$Author: j40 \$

 $E\text{-}mail\ address:\ \texttt{gs@statlab.uni-heidelberg.de}$

GÜNTHER SAWITZKI STATLAB HEIDELBERG IM NEUENHEIMER FELD 294 D 69120 Heidelberg