The "InclusionZone" Class

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1 Introduction

Inclusion zones in general are the area surrounding an object in which the sample point (e.g., the fixed-radius plot center) can land and sample the object. Therefore, they have a clearly defined area and perimeter. In addition, for PPS methods, they depend on some attribute of the object, such as length in the case of a down log. This class and its subclasses bring together objects from the "ArealSampling" class and the "Stem" class, to define the more useful subclasses corresponding to actual sampling methods for standing trees or down logs.

The "InclusionZone" object that will be defined through its subclasses will eventually instantiate an object that therefore contains both the inclusion zone and the stem itself. These components will be stored in separate slots in the object, so they can be accessed individually as needed, but for plotting and summary purposes, the object will be treated as the union of the two component objects that define the inclusion zone and stem.

Figure 1 presents an overview of the class hierarchy arrangement. Round-cornered boxes represent virtual classes, while the "standingTreeIZ" class does not exist yet. A container class ("downLogIZs") for "downLogIZ" objects is also shown, it will handle collections of objects of any of the "downLogIZs" subclasses.

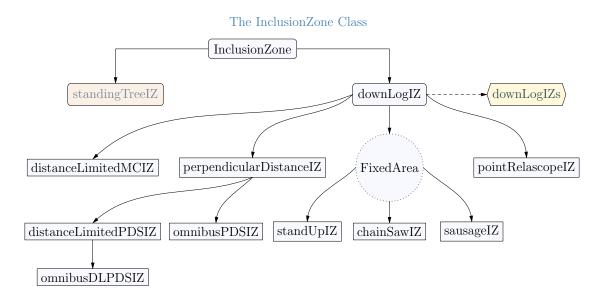


Figure 1: An overview of the "InclusionZone" class. "FixedArea" is not part of the class structure, but simply a subheading for the three subclasses following.

2 The "InclusionZone" Class

This is a virtual class which simply defines the main attributes of the subclasses. Note that this class is extremely basic, and it will have two direct subclasses, much like the "Stem" class, for standing tree- and down log-based sampling methods.

The base class is defined with the slots...

```
R> showClass('InclusionZone')
Virtual Class "InclusionZone" [package "sampSurf"]
Slots:
Name:
        description
                           units
                                          bbox
                                                    spUnits
                                                               puaBlowup
Class:
          character
                                                        CRS
                                                                 numeric
                       character
                                        matrix
       puaEstimates
Name:
                       userExtra
Class:
                             ANY
Known Subclasses:
Class "downLogIZ", directly
Class "standUpIZ", by class "downLogIZ", distance 2
Class "chainSawIZ", by class "downLogIZ", distance 2
Class "sausageIZ", by class "downLogIZ", distance 2
Class "pointRelascopeIZ", by class "downLogIZ", distance 2
Class "perpendicularDistanceIZ", by class "downLogIZ", distance 2
Class "omnibusPDSIZ", by class "perpendicularDistanceIZ", distance 3
Class "distanceLimitedMCIZ", by class "downLogIZ", distance 2
Class "distanceLimitedPDSIZ", by class "perpendicularDistanceIZ", distance 3
Class "omnibusDLPDSIZ", by class "distanceLimitedPDSIZ", distance 4
```

2.1 Class slots

- description: Some descriptive text about this class.
- units: A character string specifying the units of measure. Legal values are "English" and "metric."
- bbox: The bounding box enclosing the overall object and its inclusion zone. Since the inclusion zone may not include the entire object (as in the "standup" method for down logs), we require

it here. Most of the time, it is actually redundant as the "SpatialPolygons" slot containing the inclusion zone in the subclasses will have this same information.

- spUnits: A valid string of class "CRS" denoting the spatial units coordinate system ("?CRS" for more information) as in package sp.
- puaBlowup: The per unit area blowup or expansion factor, based on an acre or hectare depending upon the units of measure.
- puaEstimates: A list of estimates for per unit area quantities associated with the "Stem" component of the object.
- userExtra: This can be anything else the user wants to associate with the object. Normally, it might be in the form of a list object, but can be anything. The user has complete control over this, it will not be used in any of the methods applied to the class, it is there for extra information storage as desired.

3 The "downLogIZ" Class

This is another small definitional step. It simply starts the bifurcation for subclasses that are related to "ArealSampling" classes for down logs. One slot is added in the process, that for a "downLog" object. Please note that this class is also *virtual*, and so just helps form the fact that its subclasses are "InclusionZone" classes for downed logs.

```
R> getClass('downLogIZ')
```

```
Virtual Class "downLogIZ" [package "sampSurf"]
```

Slots:

Name: downLog description units bbox spUnits Class: downLog character character matrix CRS

Name: puaBlowup puaEstimates userExtra Class: numeric list ANY

Extends: "InclusionZone"

Known Subclasses:

Class "standUpIZ", directly Class "chainSawIZ", directly Class "sausageIZ", directly

```
Class "pointRelascopeIZ", directly
Class "perpendicularDistanceIZ", directly
Class "distanceLimitedMCIZ", directly
Class "omnibusPDSIZ", by class "perpendicularDistanceIZ", distance 2
Class "distanceLimitedPDSIZ", by class "perpendicularDistanceIZ", distance 2
Class "omnibusDLPDSIZ", by class "distanceLimitedPDSIZ", distance 3
```

4 The "standUpIZ" Class

Gove and Van Deusen (2011) recognize three main protocols for sampling down logs with fixedarea plots. The so-called "standup" method is probably the most commonly used. Basically, the standup method includes the log if the center of the large-end of the log lands within the sample plot. Therefore, the inclusion zone can be envisioned as centered on that point of the log. The subclass is defined as...

```
R> getClass('standUpIZ')
Class "standUpIZ" [package "sampSurf"]
Slots:
Name:
       circularPlot
                          downLog
                                   description
                                                                      bbox
                                                       units
Class: circularPlot
                          downLog
                                     character
                                                   character
                                                                    matrix
Name:
            spUnits
                        puaBlowup puaEstimates
                                                   userExtra
Class:
                CRS
                          numeric
                                           list
                                                         ANY
Extends:
Class "downLogIZ", directly
Class "InclusionZone", by class "downLogIZ", distance 2
```

It is seen to be a direct extension of the "downLogIZ" class, having added a slot for the "circularPlot" object.

4.1 Object creation

The constructor for the subclass takes a "downLog" object and a fixed-plot radius, the "circularPlot" object is created from the latter using the same units as those in the "downLog" object...

```
R> dl = downLog(species='red maple', logLen=10, buttDiam=10,
             topDiam=2, center=c(x=3,y=2), logAngle=pi/4,
             units='English', vol2wgt=30.6, wgt2carbon=0.5)
R> su = standUpIZ(d1, 5)
R> summary(su)
Object of class: standUpIZ
______
inclusion zone for "standup" method
_____
InclusionZone...
 Units of measurement: English
 Per unit area blowup factor: 554.62315 per acre
 Object bounding box...
        min
                max
x -5.5330166 6.5944595
y -6.5349045 5.5944595
downLog component estimates...
 Spatial ID: log:xz7h9u56
 Number of logs: 554.62315 per acre
 Volume: 1531.5143 cubic feet per acre
 Surface area: 9878.5009 square feet per acre
 Coverage area: 3142.8645 square feet per acre
 Length: 5546.2315 feet per acre
 Biomass (woody): 46864.337 per acre
 Carbon content: 23432.169 per acre
standUpIZ...
 use "summary" on the circularPlot slot for details
R> summary(su@circularPlot)
Object of class: circularPlot
fixed area circular plot
ArealSampling...
```

```
units of measurement: English

circularPlot...
  radius = 5 feet
  area = 78.539816 square feet (0.001803 acres)
  spatial units: NA
  spatial ID: su:ob16z5s0
  location (plot center)...
    x coord: -0.53553391
    y coord: -1.5355339

Number of perimeter points: 101 (closed polygon)
```

In the above example, the summary shows the extents of the object. Note that summaries of the "downLog" and "circularPlot" slots can easily be generated as shown.

4.2 Plotting the object

The plot generic function has also been extended to be able to handle plotting of the objects of the "standUpIZ" class. The arguments are again detailed in the help page, but here is a simple example...

```
R> plot(su, axes=TRUE, showPlotCenter=TRUE, cex=2, showNeedle=TRUE)
```

A couple things are worth noting in Figure 2. The overall bounding box includes the two objects, the inclusion zone (fixed-area plot) and the log, as is also shown in the above summary. The center of the plot is correctly aligned with the center of the large-end of the log. In addition, everything is relative to the location of the exact center of the log as defined in the "downLog" class. The correct juxtaposition of the inclusion zone is shown with regard to the log's rotation angle (the logAngle slot in the object). Again this information is all self-contained within the object. For example, in this object, the log angle can be found simply as...

```
R> su@downLog@logAngle
[1] 0.78539816
R> identical(dl@logAngle, su@downLog@logAngle)
[1] TRUE
```

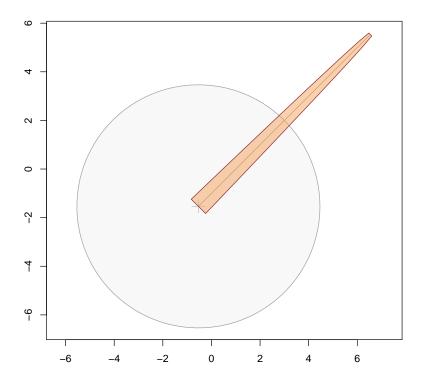


Figure 2: A "standupIZ" object.

5 The "chainSawIZ" Class

A second, but probably less commonly used protocol is what Gove and Van Deusen (2011) call the "chainsaw" method. With this method, the intersection of the plot with the log defines a 'sliver' of the log which is measured for volume. They discuss three main sub-protocols for the implementation of this method. This class essentially allows implementation of all three, tough only the sausage-based protocol is currently implemented as it is the most useful. The class extends "downLog" directly...

R> getClass('chainSawIZ')

Class "chainSawIZ" [package "sampSurf"]

Slots:

Name:	circularPlot	sliver	bolt	downLog
Class:	circularPlot	SpatialPolygons	list	downLog
Name:	description	units	bbox	spUnits
Class:	character	character	matrix	CRS
Name:	puaBlowup	puaEstimates	userExtra	
Class:	numeric	list	ANY	

Extends:

```
Class "downLogIZ", directly Class "InclusionZone", by class "downLogIZ", distance 2
```

wherein the following slots have been added...

5.1 Class slots

- circularPlot: An object of that class.
- sliver: A "SpatialPolygons" object representing the intersection (sliver) between the circular plot and the log.
- bolt: A list defining the 'minimal bounding bolt' within the log that fully encompases the sliver. The slots in the list are defined as 1 cdots...
 - rotBolt: A matrix representation of the minimal bounding bolt.
 - bolt Vol: The bolt's volume.
 - sectVol: The volume of the sliver section.
 - area: A vector containing the proportion of the bolt that the sliver encompasses, the bolt polygon area, and the sliver polygon area.
 - boltLen: The length of the bolt at its longest point, which is also the sliver section length.
 - boltSA: The bolt's surface area.
 - sectSA: The sliver's surface area.
 - bolt CA: The bolt's coverage area.
 - sectCA: The sliver's coverage area.
 - boltBms: The bolt's biomass content (can be NA).
 - sectBms: The sliver's biomass content (can be NA).

¹See the chainsawSliver function for more details.

- boltCarbon: The bolt's carbon content (can be NA).
- sect Carbon: The sliver's carbon content (can be NA).
- spBolt: A "SpatialPolygons" object representing the minimal bounding bolt within the log.

5.2 Object creation

The constructor for the subclass takes a "downLog" object, a fixed-plot radius, and a center point for the fixed-radius plot...

```
R > cs = chainSawIZ(dl, 2, c(x=7.8, y=3.9), runQuiet=FALSE)
Percentage sliver is of bolt area = 18.075158
Bolt volume (not expanded) = 0.019930252
Section/sliver volume (not expanded) = 0.0036024245
R> summary(cs)
Object of class: chainSawIZ
_____
inclusion zone for "chainsaw" method
______
InclusionZone...
 Units of measurement: English
 Per unit area blowup factor: 3466.3947 per acre
 Object bounding box...
        min
x -0.83016173 9.8000000
y -1.83016173 5.8997483
downLog component estimates...
 Spatial ID: log:xz7h9u56
 Number of logs: 3466.3947 per acre
 Volume: 12.487425 cubic feet per acre
 Surface area: 427.35022 square feet per acre
```

Coverage area: 135.60665 square feet per acre

Length: 3051.8683 feet per acre Biomass (woody): 382.11521 per acre Carbon content: 191.05761 per acre

The above estimates are based on the expanded sliver portion.

The following are unexpanded...

Sliver area is 0.18075158 of bounding bolt Total log volume: 2.7613602 cubic feet

Bounding bolt volume: 0.019930252 cubic feet

Sliver volume: 0.0036024245 cubic feet

Total log surface area: 17.811195 square feet

Bounding bolt surface area: 0.68206196 square feet

Sliver surface area: 0.12328377 square feet Total log coverage area: 5.6666667 square feet

Bounding bolt coverage area: 0.21643170 square feet

Sliver coverage area: 0.039120371 square feet

Total log length: 10 feet

Bounding bolt length: 0.88041571 feet

Total log biomass: 84.497622

Bounding bolt biomass: 0.60986572

Sliver biomass: 0.11023419 Total log carbon: 42.248811

Bounding bolt carbon: 0.30493286

Sliver carbon: 0.055117095

chainSawIZ...

use "summary" on the circularPlot slot for sample plot details

The summary method shows a bit more information about the resulting object than with other protocols. Most importantly, it shows information about the sliver size and volume, etc., and the minimal bounding bolt's size with respect to the entire log. We can see from this example, that we truly must have just cut a little sliver off, since its volume is so small. However, in the next example, we take a good chunk of the log in the plot intersection...

R > cs2 = chainSawIZ(dl, plotRadius=3, c(x=2, y=2), runQuiet=FALSE)

Percentage sliver is of bolt area = 97.81168 Bolt volume (not expanded) = 1.5331178 Section/sliver volume (not expanded) = 1.4995682

The constructor was requested to print the necessary information for comparison, and it will be verified by the graphics below.

5.3 Plotting the object

The plot generic function has also been extended to be able to handle plotting of the objects of the "chainSawIZ" class. The arguments are again detailed in the help page, but here is a simple example...

```
R> plot(cs, axes=TRUE, showNeedle=TRUE, showPlotCenter=TRUE)
R> plot(cs2, add=TRUE, showPlotCenter=TRUE, showLog=FALSE, izColor=NA)
```

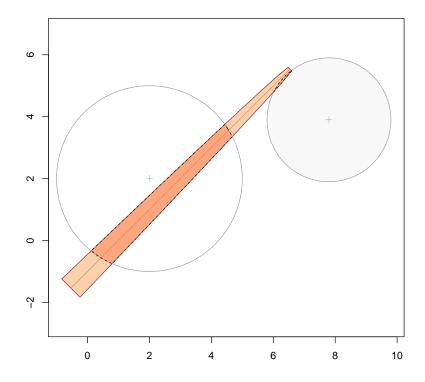


Figure 3: "chainsawIZ" objects comparison.

Figure 3 presents a comparison of the two "chainSawIZ" objects created above, using the same log for reference. As mentioned above, the second object takes a much larger slice of the log for an estimate of volume than the first. It is also worth noting that the first example shows an intersection where the log's 'needle' is not encountered. This would therefore not qualify as falling into the sausage-shaped inclusion zone for the overall log, unless it also intersected the end of the log (see Gove and Van Deusen (2011) for details). In the Figure, the minimal bounding bolts are

delineated by the dotted lines, and the slivers are clearly seen in the intersection, also shown as dashed.

6 The "sausageIZ" Class

Another method, which allows the log to be sampled if any part of it's "needle" falls inside the circular fixed-area plot is called the "sausage" method by Gove and Van Deusen (2011). It is a direct subclass of "downLogIZ"...

```
R> getClass('sausageIZ')
Class "sausageIZ" [package "sampSurf"]
Slots:
Name:
                                                                 perimeter
                sausage
                                  radius
                                                     area
Class:
                matrix
                                 numeric
                                                  numeric SpatialPolygons
                                              description
Name:
         pgSausageArea
                                 downLog
                                                                     units
Class:
                numeric
                                 downLog
                                                character
                                                                 character
Name:
                   bbox
                                 spUnits
                                                puaBlowup
                                                             puaEstimates
Class:
                 matrix
                                     CRS
                                                  numeric
                                                                      list
Name:
             userExtra
Class:
                    ANY
Extends:
Class "downLogIZ", directly
Class "InclusionZone", by class "downLogIZ", distance 2
```

wherein the following slots have been added...

6.1 Class slots

• sausage: A matrix representation of the sausage inclusion zone in homogeneous coordinates. This can be manipulated and plotted as desired for easy access to the inclusion zone where needed.

- radius: The radius for the fixed-area plot that determines the sausage inclusion zone area.
- area: The exact area of the inclusion zone.
- perimeter: This is the inclusion zone perimeter as a "SpatialPolygons" object.
- pgSausageArea: This is the area of the sausage inclusion zone as calculated from the polygon in the perimeter slot using the "SpatialPolygons" object. As such, it is an approximation of the true area of the inclusion zone, which is given in the area slot. This just enables us to see how close the graphic representation is to the real area.

6.2 Object creation

The constructor for the subclass takes a "downLog" object and a fixed-plot radius, much like the "standUpIZ" class. From this the inclusion zone is determined...

```
R > sa = sausageIZ(d1, 5)
R> summary(sa)
Object of class: sausageIZ
_____
inclusion zone for downed log "sausage" sampling method
_____
InclusionZone...
 Units of measurement: English
 Per unit area blowup factor: 243.97919 per acre
 Object bounding box...
       min
x -5.5348916 11.535534
y -6.5348916 10.535534
downLog component estimates...
 Spatial ID: log:xz7h9u56
 Number of logs: 243.97919 per acre
 Volume: 673.71443 cubic feet per acre
 Surface area: 4345.5609 square feet per acre
 Coverage area: 1382.5488 square feet per acre
 Length: 2439.7919 feet per acre
```

Biomass (woody): 20615.662 per acre

```
Carbon content: 10307.831 per acre

sausageIZ...

Spatial ID: saus:k5z7n94b

radius = 5 feet

area = 178.53982 square feet (0.004099 acres)

Number of perimeter points: 101 (closed polygon)

R> sa@pgSausageArea

[1] 178.48489
```

We note from the above that there is a little bias in the area of the inclusion zone when computed from the "SpatialPolygons" object. This is small, but shows the approximate nature of the inclusion zone perimeter. Using more points to define the half-circles on each end of the zone allows this area estimate to converge to the actual area. Using too few points obviously results in larger bias. This should be kept in mind when constructing grids for sampling surface simulations eventually with these objects, because the perimeter will determine what grid cell centers are within the inclusion zone, and hence get assigned a surface attribute value.

6.3 Plotting the object

The plot generic function has also been extended to be able to handle plotting of the objects of the "sausageIZ" class. The arguments are again detailed in the help page, but here is a simple example...

Figure 4 illustrates the sausage inclusion zones for two down logs. In the case of the longest log, the standup inclusion zone perimeter is shown for comparison.

One other thing to keep in mind under sausage sampling is that the log and inclusion zone centers coincide. Therefore, plotting the log center will identify them both using showLogCenter=TRUE;

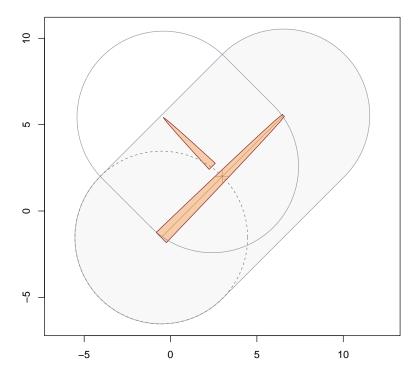


Figure 4: "sausageIZ" objects with "standUpIZ" perimeter for comparison.

using showPlotCenter=TRUE does nothing at present. If you really want to also display the plot center, it can always be accessed via the downLog slot in the object itself: the location slot in this object is an object of class "SpatialPoints" and therefore can be accessed as the inclusion zone plot center.

7 The "pointRelascopelZ" Class

This class combines the usual information from an individual "downLog" object along with a given "pointRealscope" areal sampling object to create an inclusion zone for the point relascope sampling method (Gove et al. 1999, Gove et al. 2001). Recall that the inclusion area is proportional to the squared-length, so both objects are required in the class. It is a direct subclass of "downLogIZ"...

R> getClass('pointRelascopeIZ')

Class "pointRelascopeIZ" [package "sampSurf"]

Slots:

Name:	prs	dualCircle	radius	area
Class:	pointRelascope	matrix	numeric	numeric
Name:	perimeter	pgDualArea	dualCenters	downLog
Class:	SpatialPolygons	numeric	matrix	downLog
Name:	description	units	bbox	spUnits
Class:	character	character	matrix	CRS
Name:	puaBlowup	puaEstimates	userExtra	
Class:	numeric	list	ANY	

Extends:

Class "downLogIZ", directly Class "InclusionZone", by class "downLogIZ", distance 2

7.1 Class slots

The following slots have been added to this subclass...

- prs: An object of class "pointRelascope" that furnishes the information about the point relascope method.
- dualCircle: A matrix representation of the inclusion zone in homogeneous coordinates. This can be manipulated and plotted as desired for easy access to the inclusion zone where needed.
- radius: The radius in the appropriate units of each of the dual circles comprising the inclusion zone.
- area: The exact area of the inclusion zone.
- perimeter: This is the inclusion zone perimeter as a "SpatialPolygons" object.
- pgDualArea: This is the area of the inclusion zone as calculated from the polygon in the perimeter slot using the "SpatialPolygons" object. As such, it is an approximation of the true area of the inclusion zone, which is given in the area slot. This just enables us to see how close the graphic representation is to the real area.
- dualCenters: The center points of the dual circles stored as a matrix (not in homogeneous form).

7.2 Object creation

The constructor for the subclass takes a "downLog" object and an object of class "pointRelascope". From this the inclusion zone is determined...

```
R> (rw.angle = .StemEnv$rad2Deg(2*atan(1/4)))
[1] 28.072487
R> prs4 = pointRelascope(rw.angle, units='English')
R> iz.prs = pointRelascopeIZ(d1, prs4)
R> iz.prs
Object of class: pointRelascopeIZ
inclusion zone for down log point relascope sampling method
______
InclusionZone...
 Units of measurement: English
 Per unit area blowup factor: 62.90802 per acre
 Object bounding box...
        min
x -14.253728 20.253728
y -15.253728 19.253728
downLog component estimates...
  Spatial ID: log:xz7h9u56
 Number of logs: 62.90802 per acre
 Volume: 173.71170 cubic feet per acre
  Surface area: 1120.4670 square feet per acre
 Coverage area: 356.47878 square feet per acre
 Length: 629.0802 feet per acre
 Biomass (woody): 5315.5781 per acre
 Carbon content: 2657.7890 per acre
pointRelascopeIZ...
  Spatial ID: prs:j026aho1
  dual circle radius = 10.625 feet
```

```
area = 692.43954 square feet (0.01590 acres)
Number of perimeter points: 201 (closed polygon)
```

R> iz.prs@pgDualArea

[1] 692.15325

Again, as in the sausage method, we have relatively good agreement in this example betweem the actual area of the inclusion zone and that calculated from the "SpatialPolygons" object. And again, the fact that the latter can be adjusted through the number of points in each dual circle should be kept in mind when running simulations (see <code>?pointRelascopeIZ</code>). This is a very small angle, and draws in logs from far away. Likewise, it will encompass a good number of grid cells in the final sampling surface simulation; therefore, it makes sense to have the polygon and true area agree well, so we are not excluding grid cells. If we try to cut the number of points in each circle down we see that the area does not agree as well. . .

```
R> iz.prs = pointRelascopeIZ(dl, prs4, nptsCircle=50)
R> c(iz.prs@area, iz.prs@pgDualArea)
```

[1] 692.43954 691.27141

This is something to be kept in mind, the smaller relascope angle, the more points are required on the perimeter, or some bias from the approximation to the inclusion zone polygon could show up in the simulations.

7.3 Plotting the object

The plot generic function has also been extended to be able to handle plotting of the objects of the "pointRelascopeIZ" class. The arguments are again detailed in the help page (methods?plot), a simple example follows...

```
R> plot(iz.prs, axes=TRUE, showDualCenters=TRUE, showLogCenter=TRUE,
+ cex=2, showNeedle=TRUE)
R> (rw.angle = .StemEnv$rad2Deg(2*atan(1/2)))
```

```
R> prs2 = pointRelascope(rw.angle, units='English')
R> iz.prs = pointRelascopeIZ(dl, prs2)
R> plot(perimeter(iz.prs), add=TRUE, lty='dashed', border=.StemEnv$izBorderColor)
```

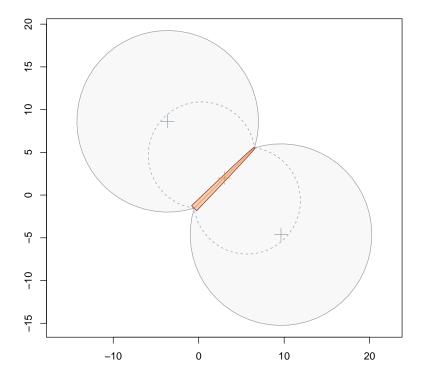


Figure 5: "pointRelascopeIZ" objects with different angles for comparison. Also shown are the dual circle centers for the smaller angle (larger inclusion zone).

8 The "perpendicular Distance IZ" Class

This class combines the usual information from an individual "downLog" object along with a given "perpendicularDistance" areal sampling object to create an inclusion zone for the perpendicular distance sampling method (Williams and Gove 2003, Williams et al. 2005, Ducey et al. 2008). Recall that the inclusion area is proportional to some function of diameter along the entire length, so both objects are required in the class. It is a direct subclass of "downLogIZ"...

R> getClass('perpendicularDistanceIZ')

Class "perpendicularDistanceIZ" [package "sampSurf"]

Slots:

Name:	pds	izPerim	area		
Class:	perpendicularDistance	matrix	numeric		
Name:	perimeter	pgArea	pdsType		
Class:	${ t SpatialPolygons}$	numeric	character		
Name:	${ t downLog}$	description	units		
Class:	downLog	character	character		
Name:	bbox	$ exttt{spUnits}$	puaBlowup		
Class:	matrix	CRS	numeric		
3.7		п.			
Name:	${\tt puaEstimates}$	userExtra			
Class:	list	ANY			
Extends:					
Class "downLogIZ", directly					

```
Class "downLogIZ", directly
Class "pdsIZNull", directly
Class "InclusionZone", by class "downLogIZ", distance 2
```

Known Subclasses:

Class "omnibusPDSIZ", directly

Class "distanceLimitedPDSIZ", directly

Class "omnibusDLPDSIZ", by class "distanceLimitedPDSIZ", distance 2

8.1 Class slots

The following slots have been added to this subclass...

- pds: An object of class "perpendicular Distance" that furnishes the information about the perpendicular distance method.
- izPerim: A matrix representation of the inclusion zone in homogeneous coordinates. This can be manipulated and plotted as desired for easy access to the inclusion zone where needed.
- area: The exact area of the inclusion zone.
- perimeter: This is the inclusion zone perimeter as a "SpatialPolygons" object.

- pgArea: This is the area of the inclusion zone as calculated from the polygon in the perimeter slot using the "SpatialPolygons" object. As such, it is an approximation of the true area of the inclusion zone, which is given in the area slot. This just enables us to see how close the graphic representation is to the real area.
- pdsType: Specifies the type of perpendicular distance sampling used: volume, surface or coverage area.

8.2 Object creation

As noted above, the pdsType slot stores the type of PDS sample we have used in the sense of sampling with probability proportional to either volume, surface area or coverage area. In what follows, we demonstrate only sampling with PP to volume, which is the default. However, if one would like to use either of the other two protocols, simply include the pdsType argument in the constructor, with one of the following as the specification to this argument...

```
R> .StemEnv$pdsTypes
```

```
[1] "volume" "surfaceArea" "coverageArea"
```

The constructor for the subclass takes a "downLog" object and an object of class "perpendicular Distance". From this the inclusion zone is determined...

```
R> pdsEng = perpendicularDistance(kpds=10, units='English')
R> iz.pdsv = perpendicularDistanceIZ(dl, pdsEng)
R> c(iz.pdsv@area, iz.pdsv@pgArea)

[1] 55.227204 55.212106
R> iz.pdsv
```

```
Object of class: perpendicularDistanceIZ
----inclusion zone for down log perpendicular distance sampling
```

InclusionZone...

```
Units of measurement: English
 Per unit area blowup factor: 788.74172 per acre
  Object bounding box...
         min
                   max
x -4.3922031 6.6898007
y -5.3922031 5.6898007
downLog component estimates...
  Spatial ID: log:xz7h9u56
 Number of logs: 788.74172 per acre
 Volume: 2178 cubic feet per acre
  Surface area: 14048.432 square feet per acre
  Coverage area: 4469.5364 square feet per acre
 Length: 7887.4172 feet per acre
  Biomass (woody): 66646.8 per acre
  Carbon content: 33323.4 per acre
perpendicularDistanceIZ...
  PDS type: volume
  Spatial ID: pds:5z18bkn2
  area = 55.227204 square feet (0.001268 acres)
  Number of perimeter points: 43 (closed polygon)
```

First, we create an "ArealSampling" object of class "perpendicularDistance", and subsequently create the inclusion zone object for the respective log. The area comparison between the theoretically correct area of the inclusion zone and that based on the polygon approximation is shown next. Surprisingly, the polygon approximation is quite good as it is based on the taper data in the "downLog" object. This is something to be kept in mind for simulations, if too few points are used to determine the taper, the inclusion zone can be poorly determined because it uses these taper points directly. So if a set of simulations produces some measureable bias, poor taper data restricting the underlying grid cells in the final sampling surface may be the cause under PDS. In the above example the taper slot in the log had 21 taper measurements, so the inclusion zone polygon has...

```
R> nrow(dl@taper)*2+1
```

[1] 43

perimeter points in the closed polygon (first and last point are repeated).

8.3 Plotting the object

The plot generic function has also been extended to be able to handle plotting of the objects of the "perpendicularDistanceIZ" class. The arguments are again detailed in the help page (methods?plot), a simple example follows...

```
R> plot(iz.pdsv, axes=TRUE, showLogCenter=TRUE, cex=2, showNeedle=TRUE)
R> pdsEng2 = perpendicularDistance(kpds=5, units='English')
R> iz.pdsv2 = perpendicularDistanceIZ(d1, pdsEng2)
R> plot(perimeter(iz.pdsv2), add=TRUE, lty='dashed', border=.StemEnv$izBorderColor)
```

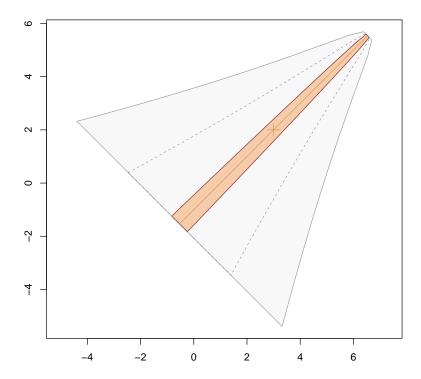


Figure 6: "perpendicular Distance IZ" objects with different K PDS values for comparison.

8.4 Omnibus PDS

Omnibus PDS is described by Ducey et al. (2008). It allows us to get estimates of attributes other than the one of the three primary selection attibutes of volume, surface area or coverage area. The "omnibus PDSIZ" class definition is *exactly* the same as the "perpendicular Distance IZ" class. In fact it is a subclass of the latter that adds no new slots, so we can refer directly to the information in the last section for the class definition.

8.5 Object creation

Length: NA feet per acre

Object creation is also the same for omnibus. This is because the inclusion zone is exactly the same. However, the eventual sampling surface inside the inclusion zone will be variable in height, so there is no one overall estimate of the quantities of interest that can be calculated. This is because the estimates for each point within the inclusion zone rely on some function of diameter at the perpendicular. More will be covered on this in "The InclusionZoneGrid Class" vignette.

```
R> iz.opdsv = omnibusPDSIZ(dl, pdsEng)
R> iz.opdsv
Object of class: omnibusPDSIZ
_____
inclusion zone for down log omnibus perpendicular distance sampling
InclusionZone...
 Units of measurement: English
 Per unit area blowup factor: 788.74172 per acre
 Object bounding box...
        min
                 max
x -4.3922031 6.6898007
y -5.3922031 5.6898007
downLog component estimates...
 Spatial ID: log:xz7h9u56
 Number of logs: NA per acre
 Volume: NA cubic feet per acre
 Surface area: NA square feet per acre
 Coverage area: NA square feet per acre
```

```
Biomass (woody): NA per acre
Carbon content: NA per acre
```

omnibusPDSIZ...

PDS type: volume

Spatial ID: opds:420drmw8

area = 55.227204 square feet (0.001268 acres)
Number of perimeter points: 43 (closed polygon)

Note particularly that the "downLog" component estimates are all NA reflecting the above point concerning the variable sampling surface within the inclusion zone.

A plot of this object would look *exactly* like the wide zone in Figure 6, so there is no need to repeat that here.

9 The "distanceLimitedMCIZ" Class

Distance limited Monte Carlo Sampling (DLMCS) has not been written up yet. Here we simply show how to create inclusion zones and what they look like. Basically, DLMCS is a PP to length sampling method that invokes a perpendicular distance limit, creating a rectangular inclusion zone that has the same length as the log. We introduce it here, because it plays a part in distance limited PDS, which will be discussed in the next section. Note that similar to omnibus PDS, the inclusion zone is variable in height for most attributes, the exception being log density (number of logs) and length.

```
R> getClass('distanceLimitedMCIZ')
```

Class "distanceLimitedMCIZ" [package "sampSurf"]

Slots:

Name:	dls	izPerim	area	perimeter
Class:	${\tt distanceLimited}$	matrix	numeric	SpatialPolygons
Name:	pgArea	downLog	description	units
Class:	numeric	downLog	character	character
Name:	bbox	${ t spUnits}$	puaBlowup	puaEstimates
Class:	matrix	CRS	numeric	list

```
Name: userExtra
Class: ANY

Extends:
Class "downLogIZ", directly
Class "dlmcIZNull", directly
Class "InclusionZone", by class "downLogIZ", distance 2
```

9.1 Class slots

The following slots have been added to this subclass...

- dls: An object of class "distanceLimited" that furnishes the information about the distance limited "ArealSampling" method.
- *izPerim*: A matrix representation of the inclusion zone in homogeneous coordinates. This can be manipulated and plotted as desired for easy access to the inclusion zone where needed.
- area: The exact area of the inclusion zone.
- perimeter: This is the inclusion zone perimeter as a "SpatialPolygons" object.
- pgArea: This is the area of the inclusion zone as calculated from the polygon in the perimeter slot using the "SpatialPolygons" object. As such, it is an approximation of the true area of the inclusion zone, which is given in the area slot. This just enables us to see how close the graphic representation is to the real area.

9.2 Object creation

Object creation is with its own constructor as usual...

```
InclusionZone...
  Units of measurement: English
 Per unit area blowup factor: 3630 per acre
  Object bounding box...
         min
x -4.7781746 10.7781746
y -5.7781746 9.7781746
downLog component estimates...
  Spatial ID: log:xz7h9u56
  Number of logs: 363 per acre
  Volume: NA cubic feet per acre
  Surface area: NA square feet per acre
  Coverage area: NA square feet per acre
  Length: 3630 feet per acre
  Biomass (woody): NA per acre
  Carbon content: NA per acre
  (Note: NAs signify location-dependent attributes.)
distanceLimitedMCIZ...
  Spatial ID: vpmc:uv20hn75
  distance limit = 6 feet
  area = 120 square feet (0.002755 acres)
  Number of perimeter points: 5 (closed polygon)
```

Note that we do not need to explicitly specify the units as 'English' in the costructor function because it takes the units from the "downLog" and "distanceLimited" objects passed. Also note that most of the estimates are NA, reflecting the variable surface height for these attributes.

9.3 Plotting the object

The plot generic function has also been extended to be able to handle plotting of the objects of the "distanceLimitedMCIZ" class. The arguments are again detailed in the help page (methods?plot), a simple example follows...

```
R> plot(iz.dlmcs, axes=TRUE, showLogCenter=TRUE, cex=2, showNeedle=TRUE)
R> dlsEng2 = distanceLimited(3, units='English')
R> iz.dlmcs2 = distanceLimitedMCIZ(dl, dls=dlsEng2)
R> plot(perimeter(iz.dlmcs2), add=TRUE, lty='dashed', border=.StemEnv$izBorderColor)
```

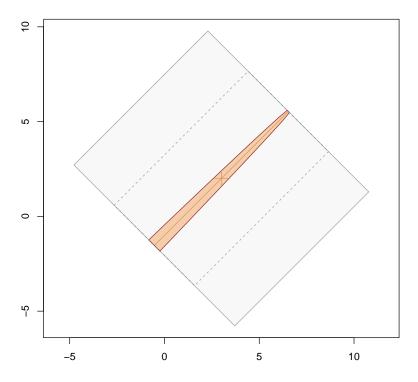


Figure 7: "distanceLimitedMCIZ" object.

Note that in Figure 7 we have plotted two inclusion zones of different widths for comparison.

10 The "distanceLimitedPDSIZ" Class

Distance limited PDS (DLPDS) was initially developed by Ducey et al. (2005). It established a distance limit, beyond which we truncate the PDS inclusion zone, effectively limiting the search distance for logs of any size. This class combines the usual information from an individual "downLog" object along with "perpendicular Distance" and "distance Limited" areal sampling objects, to create an inclusion zone. The inclusion zone thus may have both canonical PDS and DLMCS components to it. Notice we say it may have components of both forms included, but does not have to, there are three possibilities: (i) the inclusion zone is all PDS, (ii) the inclusion zone is all DLMCS, or (iii) it is a combination of the two. Which of the three are true for a given log depends on the distance limit chosen and the size of the log, which will determine whether there is any limiting diameter separating the two sampling types.

numeric

list

R> showClass('distanceLimitedPDSIZ')

Class "distanceLimitedPDSIZ" [package "sampSurf"]

Slots:

Name:	dls	dlsDiameter	pdsPart
Class:	distanceLimited	numeric	pdsIZNull
Name:	dlsPart	pdsFull	pds
Class:	dlmcIZNull	pdsIZNull	perpendicularDistance
Name:	izPerim	area	perimeter
Class:	matrix	numeric	SpatialPolygons
Name:	pgArea	pdsType	downLog
Class:	numeric	character	downLog
Name:	description	units	bbox
Class:	character	character	matrix
Name:	spUnits	puaBlowup	puaEstimates

Name: userExtra Class: ANY

Extends:

Class:

Class "perpendicularDistanceIZ", directly

CRS

Class "downLogIZ", by class "perpendicularDistanceIZ", distance 2

Class "pdsIZNull", by class "perpendicularDistanceIZ", distance 2

Class "InclusionZone", by class "perpendicularDistanceIZ", distance 3

Known Subclasses: "omnibusDLPDSIZ"

Note that this class is a direct subclass of "perpendicular Distance IZ".

10.1 Class slots

The following slots have been added to this subclass...

- dls: An object of class "distanceLimited" that furnishes the information about the distance limited "ArealSampling" method.
- *dlsDiameter*: The limiting diameter where the delineation (if any) occurs between PDS and DLMCS protocols within the log (see below for an example and calculation).
- pdsPart: Either a fully valid "perpendicularDistanceIZ" (or subclass, i.e., "omnibusPDSIZ" object) or NULL if no component of this class exists for the log.
- dlsPart: Either a fully valid "distanceLimitedMCIZ" or NULL if no component of this class exists for the log.
- pdsFull: This holds a fully valid "perpendicularDistanceIZ" (or subclass, i.e., "omnibusPDSIZ" object) delineating the full PDS zone as it would appear if the entire log were treated as a PDS sampling object. Note that it can be useful to compare this to the DLPDS object graphically.
- pds: An object of class "perpendicular Distance" that furnishes the information about the perpendicular distance method.
- *izPerim*: A matrix representation of the inclusion zone in homogeneous coordinates. This can be manipulated and plotted as desired for easy access to the inclusion zone where needed.
- area: The exact area of the inclusion zone.
- perimeter: This is the inclusion zone perimeter as a "SpatialPolygons" object.
- pgArea: This is the area of the inclusion zone as calculated from the polygon in the perimeter slot using the "SpatialPolygons" object. As such, it is an approximation of the true area of the inclusion zone, which is given in the area slot. This just enables us to see how close the graphic representation is to the real area.
- pdsType: Specifies the type of perpendicular distance sampling used: volume, surface or coverage area.

Now we can more fully look at the three component possibilities mentioned above with respect to the fields in the object...

- (i) In the case where the inclusion zone is just a regular PDS object, we will have: pdsPart and dlsPart both NULL, and pdsFull a redundant copy of the full PDS portion of the object itself.
- (ii) If the inclusion zone is all DLMCS, with no PDS component, then the overall object will 'act like' a "distanceLimitedMCIZ" object. The pdsPart slot will be NULL, while the dlsPart slot will carry a "distanceLimitedMCIZ" object (again redundant) and the pdsFull slot will again hold a full PDS inclusion zone class object.

(iii) Finally, if both components are involved in the log's inclusion zone, then the overall object contains the "hybrid" inclusion zone information. Both the pdsPart and dlsPart slots will contain the respective objects making up their components of the class, and the pdsFull slot will again hold a full PDS inclusion zone class object as if PDS were used on the entire log. In this case, for example, we could plot either the pdsPart or dlsPart objects to show the delineation between the two zones, and we could also plot the comparable PDS object for the whole log by plotting the object in the pdsFull slot.

It is important to realize in the above, that the slots containing the component parts (if they exist) are valid objects of the correct type in and of themselves. Thus, for example, they also contain the portion of the log that corresponds to the component part of the overall inclusion zone and piece together to form the whole.

10.2 Object creation

Object creation is with its own constructor as usual, though note that we need both types of "ArealSampling" objects to define the two regions...

Volume: NA cubic feet per acre

Surface area: NA square feet per acre Coverage area: NA square feet per acre

Length: NA feet per acre Biomass (woody): NA per acre Carbon content: NA per acre

perpendicularDistanceIZ...

PDS type: volume

Spatial ID: dlpds:08f94nsa

area = 25.755564 square feet (0.0005913 acres)

Number of perimeter points: 37 (closed polygon)

(The above summary is for the entire DLPDS region)

distanceLimitedPDSIZ...

distance limit = 2 feet

limiting diameter = 0.71364965 feet (8.564 in)

distance limited component available = TRUE

PDS component available = TRUE

Summaries of individual DLPDS components can be viewed seperately

The summary above shows the information for the overall object under the "perpendicular Distance IZ" section of the report. Following this, in the "distance Limited PDSIZ" section, is more specific information about the current class' extension. For example, the limiting diameter is listed along with information indicating whether or not the pdsPart and dlsPart slots are available within the object.

Note that the limiting diameter is determined differently under each of the different PDS PPS variables; viz., its formula in feet or meters for each is...

$$d_l^* = \sqrt{\frac{4*D_l}{\pi K_{\rm PDS}}}$$
 PP volume
$$d_l^* = \frac{D_l}{\pi K_{\rm PDS}}$$
 PP Surface Area
$$d_l^* = \frac{D_l}{K_{\rm PDS}}$$
 PP Coverage Area

where D_l is the distance limit in feet or meters. In the above example, the limiting diameter in inches is calculated as...

R> sqrt(4*dlsEng3@distanceLimit/(pi*pdsEng2@kpds))*12

which matches what was shown in the report above. Therefore, since this above diameter is between the butt (10 in) and top (2 in) diameters, both methods are present in the log. If we used a larger limiting distance then we would get a case where the entire log is sampled with PDS...

```
R> sqrt(4*dlsEng2@distanceLimit/(pi*pdsEng2@kpds))*12
```

```
[1] 10.488465
```

Likewise, the following shows the distance limit we would have to use in order for the entire log to be considered under only DLMCS...

```
R> iz.dlpds@downLog@topDiam^2 * pdsEng2@kpds*pi/4
```

[1] 0.10908308

10.3 Plotting the object

The plot generic function has also been extended to be able to handle plotting of the objects of the "distanceLimitedPDSIZ" class. The arguments are again detailed in the help page (methods?plot), a simple example follows...

10.4 The omnibus DLPDS

Omnibus DLPDS has not been written up yet. It allows us to get estimates of attributes other than the one of the three primary selection attributes of volume, surface area or coverage area within the PDS component (if present) of a DLPDS inclusion zone. The "omnibus DLPDSIZ" class definition is exactly the same as the "distance Limited PDSIZ" class. In fact it is a subclass of the latter that adds no new slots, so we can refer directly to the information in the last section for the class definition.

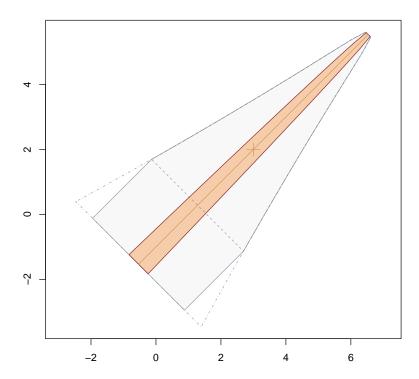


Figure 8: "distanceLimitedPDSIZ" object showing the PDS component delineation (dashed) and the full PDS inclusion zone (dot-dashed) for comparison.

10.5 Object creation

Object creation is also the same for omnibus. This is because the inclusion zone is exactly the same. However, the PDS component of the sampling surface inside the inclusion zone will be variable in height, so there is no one overall estimate of the quantities of interest that can be calculated—just as in "omnibusPDSIZ". This is because the estimates for each point within the inclusion zone rely on some function of diameter at the perpendicular. More will be covered on this in "The InclusionZoneGrid Class" vignette.

R> iz.odlpds = omnibusDLPDSIZ(d1, pds=pdsEng2, d1s=d1sEng3)
R> iz.odlpds

```
Object of class: omnibusDLPDSIZ
inclusion zone for down log omnibus distance limited PDS
_____
InclusionZone...
 Units of measurement: English
 Per unit area blowup factor: NA per acre
 Object bounding box...
        min
x -1.9497475 6.6126673
y -2.9497475 5.6126673
downLog component estimates...
  Spatial ID: log:xz7h9u56
 Number of logs: NA per acre
 Volume: NA cubic feet per acre
  Surface area: NA square feet per acre
  Coverage area: NA square feet per acre
 Length: NA feet per acre
  Biomass (woody): NA per acre
  Carbon content: NA per acre
omnibusPDSIZ...
 PDS type: volume
 Spatial ID: odlpds:94mjk5q0
  area = 25.755564 square feet (0.0005913 acres)
 Number of perimeter points: 37 (closed polygon)
  (The above summary is for the entire DLPDS region)
omnibusDLPDSIZ...
  distance limit = 2 feet
  limiting diameter = 0.71364965 feet (8.564 in)
  distance limited component available = TRUE
 PDS component available = TRUE
  Summaries of individual DLPDS components can be viewed seperately
```

Note particularly that the "downLog" component estimates are all NA reflecting the above point concerning the variable sampling surface within the inclusion zone.

A plot of this object would look *exactly* like that of Figure 8, so there is no need to repeat that here.

11 Container Classes

As we've mentioned in other vignettes, there needs to be a mechanism to have multiple versions of, e.g., "downLogIZ" objects or subclasses thereof stored in a population of sorts. This means there needs to be class and constructor methods, along with summary, plot, etc. One could just use a list structure, and this would work fine, but then there would be no ability to associate methods. So it is better to adopt an S4 class structure, albeit simple, that can encapsulate the behavior desired.

11.1 Class "downLogIZs"

This container holds a collection of "downlogIZ" objects along with some spatial information...

```
R> showClass('downLogIZs')
```

```
Class "downLogIZs" [package "sampSurf"]
```

Slots:

Name: iZones units bbox description Class: list character matrix character

Like the "downLogs" class, this is also a very simple class. At present, it holds a list of "downLogIZ" objects in the iZones slot, and the overall bounding box for the collection or population, along with a description and units for all objects. The bounding box is useful in plotting and will also be used in the sampling surface routines.

11.1.1 Class construction

In keeping with the previous naming conventions, the constructor function for this class is down-LogIZs. A collection can be created via the following steps, though there are alternatives in each case...

1. Measured population:

(a) Use the field measurements to make individual "downLog" objects, and then place them into a list container.

- (b) Create valid "downLogIZ" subclass objects for each log—they all must be of the same class.
- (c) Use the "downLogIZs" constructor on this list of logs, to create the collection.

2. Synthetic population:

- (a) Draw a sample of "downLog"s randomly within some sample area, using the "downLogs" constructor.
- (b) Then create a list of "downLogIZ" subclass objects.
- (c) Finally, group these into the container class with "downLogIZs".

The above are essentially the same in practice, as similar steps are followed whether a synthetic or real population of logs is used. At present, one must specify objects of exactly the same subclass in the list constructor. That is, you can not mix sampling methods as demonstrated below. Please see the "downLogs" constructor and "The Stem Class" vignette for more options in each of the first steps above.

In the first example, we will pretend that dl and dl2 are logs from a field sample, and we then have made sausage inclusion zones for these in the example above. Therefore, we follow the rest of the steps...

```
R> sal = list(sa,sa2)
R> sapply(sal, class)

[1] "sausageIZ" "sausageIZ"

R> izs = downLogIZs(sal, description = 'two inclusion zones...\nboth sausage')
R> sapply(izs@iZones, class)

[1] "sausageIZ" "sausageIZ"

R> summary(izs)

Object of class: downLogIZs
------two inclusion zones...
both sausage
```

```
Container class object...

There are 2 inclusion zones in the population Inclusion zones are of class: sausageIZ

Units of measurement: English

Encapulating bounding box...

min max

x -5.5348916 11.535534

y -6.5348916 10.535534
```

The above example is fine, because both of the member objects in the list used to construct the "downLogIZs" object were of class "sausageIZ". However, in the following example, we are mixing sampling methods, which is not allowed...

```
R> sal2 = list(su,sa)
R> iizs = tryCatch(downLogIZs(sal2), error = function(e) e)
R> if(is(iizs, 'simpleError')) cat(iizs[[1]],'\n')
```

invalid class "downLogIZs" object: You can not mix inclusion classes in the population!

```
R> sapply(sal2,class)
```

```
[1] "standUpIZ" "sausageIZ"
```

It is very simple to draw a simulated population of logs plus their inclusion zone. As shown below, this can be done for a log population of any size. Since the logs are stored within the objects as a list structure, we can apply the list-based object constructors via lapply to return a new list that can directly be converted to a container object...

```
R> dls = downLogs(6, units='English', buttDiam=c(6,20))
R> dls.su = lapply(dls@logs, 'standUpIZ', plotRadius=5)
R> izs.su = downLogIZs(dls.su)
R> dls.sa = lapply(dls@logs, 'sausageIZ', plotRadius=5)
R> izs.sa = downLogIZs(dls.sa)
```

In this case we have created two more container objects for a set of "downLog"s within a "downLogs" object, the first for the sausage method, and the second for the standup method.

11.2 Plotting the object

There is a plot method for "downLogIZs" objects that works as usual.

In the case of the first example, where the "downLogIZs" object was created using 'field data,' we have generate Figure 9...

R> plot(izs, axes=TRUE, showLogCenter=TRUE, cex=2, showNeedle=TRUE)

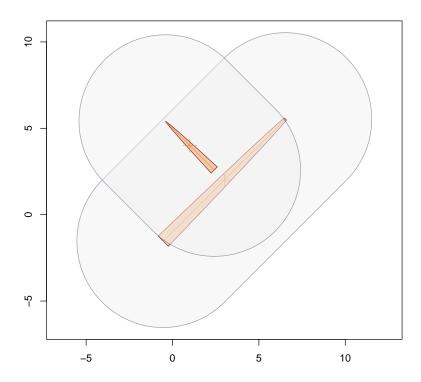


Figure 9: "downLogIZs" object with "sausageIZ" objects in the container.

In the second example, where we use synthetic logs, we generate Figure 10 showing the "standUpIZ" inclusion zones superimposed over the "sausageIZ" inclusion zones, purely for comparison...

```
R> plot(izs.sa, axes=TRUE, showLogCenter=TRUE, cex=2, showNeedle=TRUE)
R> plot(izs.su, add=TRUE, izColor=NA)
```

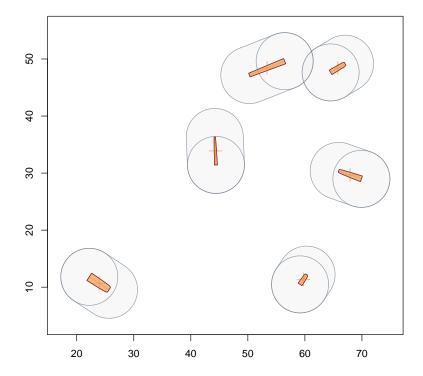


Figure 10: "downLogIZs" object of "sausageIZ" objects, with "standUpIZ" objects superimposed.

Note that in generating Figure 10, we have plotted the sausage collection before the standup collection, because the former has a larger overall bounding box that will contain all of the collected objects, regardless of their "InclusionZone" classes. Note again, however, the restriction that within a collection, all of the objects must share the same "InclusionZone" class.

References

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