

Statistical Analysis of Corpus Data with R

Hypothesis Testing for Corpus Frequency Data – The Library Metaphor

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<http://purl.org/stefan.evert/SIGIL>

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More interesting questions

- ◆ How often is *kick the bucket* really used?
- ◆ What are the characteristics of “translationese”?
- ◆ Do Americans use more split infinitives than Britons? What about British teenagers?
- ◆ What are the typical collocates of *cat*?
- ◆ Can the next word in a sentence be predicted?
- ◆ Do native speakers prefer constructions that are grammatical according to some linguistic theory?
- ➔ answers are based on the same frequency estimates

A simple question

How many passives are there in English?

- a simple, innocuous question at first sight, and not particularly interesting from a linguistic perspective
- but it will keep us busy for many hours ...
- slightly more interesting version:
Are there more passives in written English than in spoken English?

Back to our simple question

How many passives are there in English?

- ◆ American English style guide claims that
 - “In an average English text, no more than 15% of the sentences are in passive voice. So use the passive sparingly, prefer sentences in active voice.”
 - <http://www.ego4u.com/en/business-english/grammar/passive> actually states that only 10% of English sentences are passives (as of June 2006)!
- ◆ We have doubts and want to verify this claim

Problem #1

- ◆ Problem #1: **What is English?**
- ◆ Sensible definition: group of speakers
 - e.g. American English as language spoken by native speakers raised and living in the U.S.
 - may be restricted to certain communicative situation
- ◆ Also applies to definition of sublanguage
 - dialect (Bostonian, Cockney), social group (teenagers), genre (advertising), domain (statistics), ...

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Intensional vs. extensional

- ◆ We have given an **intensional** definition for the language of interest
 - characterised by speakers and circumstances
- ◆ But does this allow quantitative statements?
 - we need something we can *count*
- ◆ Need **extensional** definition of language
 - i.e. language = body of utterances

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The library metaphor

- ◆ Extensional definition of a language:
“All utterances made by speakers of the language under appropriate conditions, plus all utterances they *could* have made”
- ◆ Imagine a huge library with all the books written in a language, as well as all the hypothetical books that were never written
→ **library metaphor** (Evert 2006)

Problem #2

- ◆ Problem #2: **What is “frequency”?**
- ◆ Obviously, extensional definition of language must comprise an infinite body of utterances
 - So, how many passives *are* there in English?
 - ∞ ... infinitely many, of course!
- ◆ Only **relative** frequencies can be meaningful

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Relative frequency

- ◆ How many passives are there ...
 - ... per million words?
 - ... per thousand sentences?
 - ... per hour of recorded speech?
 - ... per book?
- ◆ Are these measurements meaningful?

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Problem #3

- ◆ Problem #3: **How can we possibly count passives in an infinite amount of text?**
- ◆ Statistics deals with similar problems:
 - goal: determine properties of **large population** (human populace, objects produced in factory, ...)
 - method: take (completely) **random sample** of objects, then extrapolate from sample to population
 - this works only because of **random** sampling!
- ◆ Many statistical methods are readily available

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Relative frequency

- ◆ How many passives could there be at most?
 - every VP can be in active or passive voice
 - frequency of passives is only interpretable by comparison with frequency of potential passives
- ◆ What proportion of VPs are in passive voice?
 - easier: proportion of sentences that contain a passive
- ◆ **Relative frequency = proportion π**

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Statistics & language

- ◆ Apply statistical procedure to linguistic problem
 - take random sample from (extensional) language
- ◆ What are the objects in our population?
 - words? sentences? texts? ...
- ◆ Objects = whatever proportions are based on
→ **unit of measurement**
- ◆ We want to take a random sample of these units

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The library metaphor

- ◆ Random sampling in the library metaphor
 - take sample of VPs (to be correct) or sentences (for convenience)
 - walk to a random shelf ...
 - ... pick a random book ...
 - ... open a random page ...
 - ... and choose a random VP from the page
 - this gives us 1 item for our sample
 - repeat ***n*** times for **sample size *n***

Types vs. tokens

- ◆ Important distinction between types & tokens
 - we might find many copies of the “same” VP in our sample, e.g. *click this button* (software manual) or *includes dinner, bed and breakfast*
 - sample consists of occurrences of VPs, called **tokens**
 - each *token* in the language is selected at most once
 - distinct VPs are referred to as **types**
 - a sample might contain many instances of the same *type*
- ◆ Definition of types based on research question

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Types vs. tokens

- ◆ Example: word frequencies
 - word type = dictionary entry (distinct word)
 - word token = instance of a word in library texts
- ◆ Example: passives
 - relevant VP types = **active** or **passive** (→ abstraction)
 - VP token = instance of VP in library texts

Types, tokens and proportions

- ◆ Proportions in terms of types & tokens
- ◆ Relative frequency of type ***v***
= proportion of tokens ***t_i*** that belong to this type

$$p = \frac{f(v)}{n}$$

frequency of type $f(v)$

sample size n

Inference from a sample

- ◆ Principle of inferential statistics
 - if a sample is picked at random, proportions should be roughly the same in the sample and in the population
- ◆ Take a sample of, say, 100 VPs
 - observe 19 passives → $p = 19\% = .19$
 - style guide → population proportion $\pi = 15\%$
 - $p > \pi$ → reject claim of style guide?
- ◆ Take another sample, just to be sure
 - observe 13 passives → $p = 13\% = .13$
 - $p < \pi$ → claim of style guide confirmed?

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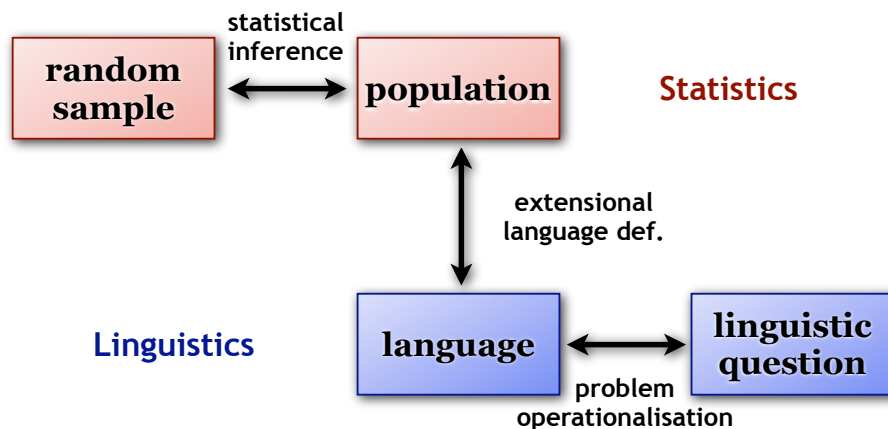
Problem #4

◆ Problem #4: **Sampling variation**

- random choice of sample ensures proportions are the same on average in sample and in population
- but it also means that for every sample we will get a different value because of chance effects
→ **sampling variation**
- ◆ The main purpose of statistical methods is to estimate & correct for sampling variation
 - that's all there is to statistics, really 😊

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The role of statistics



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Estimating sampling variation

- ◆ Assume that the style guide's claim is correct
 - the **null hypothesis** H_0 , which we aim to refute

$$H_0 : \pi = .15$$

- we also refer to $\pi_0 = .15$ as the **null proportion**
- ◆ Many corpus linguists set out to test H_0
 - each one draws a random sample of size $n = 100$
 - how many of the samples have the expected $k = 15$ passives, how many have $k = 19$, etc.?

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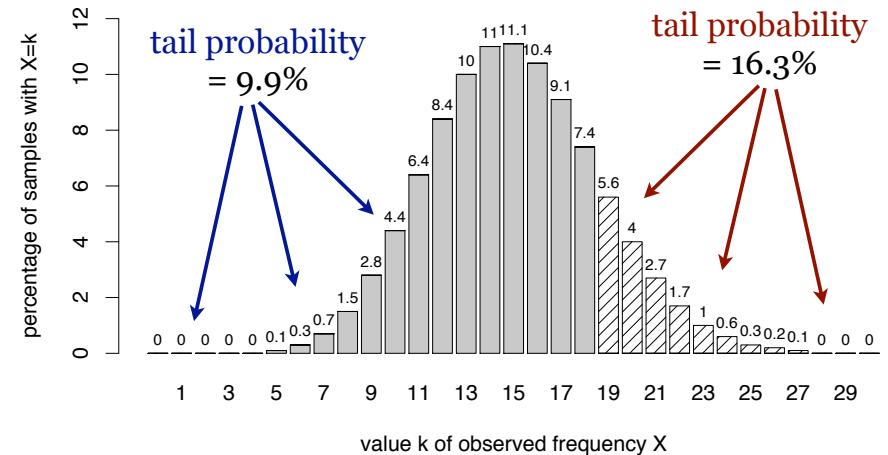
Estimating sampling variation

- ◆ We don't need an infinite number of monkeys (or corpus linguists) to answer these questions
 - randomly picking VPs from our metaphorical library is like drawing balls from an infinite urn
 - red ball = passive VP / white ball = active VP
 - H_0 : assume proportion of red balls in urn is 15%
- ◆ This leads to a **binomial distribution**

$$\Pr(X = k) = \binom{n}{k} (\pi_0)^k (1 - \pi_0)^{n-k}$$

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Binomial sampling distribution



Statistical hypothesis testing

- ◆ Statistical **hypothesis tests**
 - define a **rejection criterion** for refuting H_0
 - control the risk of false rejection (**type I error**) to a “socially acceptable level” (**significance level**)
 - **p-value** = risk of false rejection for observation
 - p-value interpreted as amount of evidence against H_0
- ◆ Two-sided vs. one-sided tests
 - in general, two-sided tests should be preferred
 - one-sided test is plausible in our example

Hypothesis tests in practice

SIGIL: Corpus Frequency Test Wizard

This site provides some online utilities for the project **Statistical Inference: A Gentle Introduction for Linguists (SIGIL)** by Marco Baroni and Stefan Evert. The main SIGIL homepage can be found at purl.org/stefan.evert/SIGIL.

One sample: frequency estimate (confidence interval)

Frequency count	Sample size
<input type="text" value="19"/>	<input type="text" value="100"/>

95% confidence interval
 in automatic format
☐ extrapolate to items with 4 significant digits

Two samples: frequency comparison

	Frequency count	Sample size
Sample 1	<input type="text" value="19"/>	<input type="text" value="100"/>
Sample 2	<input type="text" value="25"/>	<input type="text" value="200"/>

95% confidence interval
 in automatic format
 with 4 significant digits

<http://sigil.collocations.de/wizard.html>

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Hypothesis tests in practice

- ◆ Easy: use online wizard
 - <http://sigil.collocations.de/wizard.html>
 - <http://faculty.vassar.edu/lowry/VassarStats.html>
- ◆ More options: statistical computing software
 - commercial solutions like SPSS, S-Plus, ...
 - open-source software <http://www.r-project.org/>
 - we recommend R, of course, for the usual reasons



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Binomial hypothesis test in R

- ◆ Relevant R function: `binom.test()`
- ◆ We need to specify
 - **observed data**: 19 passives out of 100 sentences
 - **null hypothesis**: $H_0: \pi = 15\%$
- ◆ Using the `binom.test()` function:
 - > `binom.test(19, 100, p=.15)` # two-sided
 - > `binom.test(19, 100, p=.15, alternative="greater")` # one-sided

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Binomial hypothesis test in R

```
> binom.test(19, 100, p=.15)
Exact binomial test
data: 19 and 100
number of successes = 19, number of
trials = 100, p-value = 0.2623
alternative hypothesis: true probability of
success is not equal to 0.15
95 percent confidence interval:
 0.1184432 0.2806980
sample estimates:
probability of success
      0.19
```

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Binomial hypothesis test in R

```
> binom.test(19, 100, p=.15)$p.value
[1] 0.2622728

> binom.test(23, 100, p=.15)$p.value
[1] 0.03430725

> binom.test(190, 1000, p=.15)$p.value
[1] 0.0006356804
```

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Power

- ◆ Type II error = failure to reject incorrect H_0
 - the larger the discrepancy between H_0 and the true situation, the more likely it will be rejected
 - e.g. if the true proportion of passives is $\pi = .25$, then most samples provide enough evidence to reject; but true $\pi = .16$ makes rejection very difficult
 - a **powerful** test has a low type II error
- ◆ Basic insight: larger sample = more power
 - relative sampling variation becomes smaller
 - might become powerful enough to reject for $\pi = 15.1\%$

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Parametric vs. non-parametric

- ◆ People often speak about parametric and non-parametric tests, but no precise definition
- ◆ Parametric tests make stronger assumptions
 - not just those assuming a normal distribution
 - binomial test: strong random sampling assumption → might be considered a parametric test in this sense!
- ◆ Parametric tests are usually more powerful
 - strong assumptions allow less conservative estimate of sampling variation → less evidence needed against H_0

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Trade-offs in statistics

- ◆ Inferential statistics is a trade-off between type I errors and type II errors
 - i.e. between **significance** and **power**
- ◆ Significance level
 - determines trade-off point
 - low significance level (p-value) → low power
- ◆ Conservative tests
 - put more weight on avoiding type I errors → weaker
 - most non-parametric methods are conservative

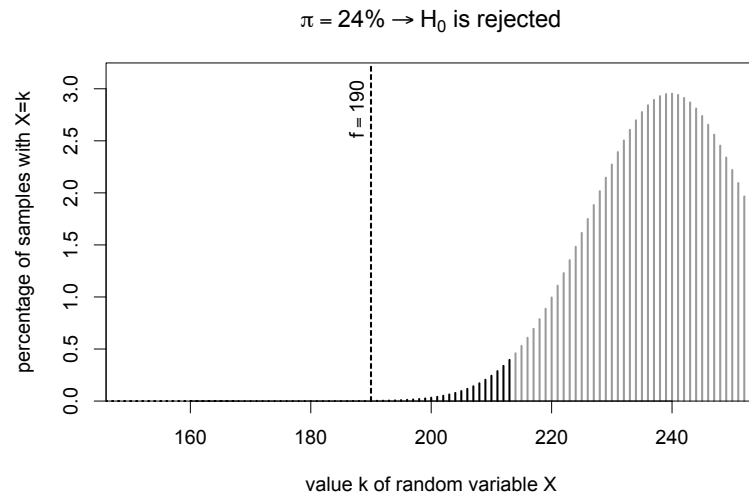
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Confidence interval

- ◆ We now know how to test a null hypothesis H_0 , rejecting it only if there is sufficient evidence
- ◆ But what if we do not have an obvious null hypothesis to start with?
 - this is typically the case in (computational) linguistics
- ◆ We can estimate the true population proportion from the sample data (relative frequency)
 - sampling variation → range of plausible values
 - such a **confidence interval** can be constructed by inverting hypothesis tests (e.g. binomial test)

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Confidence interval



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Confidence intervals

- ◆ Confidence interval = range of plausible values for true population proportion
- ◆ Size of confidence interval depends on sample size and the significance level of the test

	$n = 100$ $k = 19$	$n = 1,000$ $k = 190$	$n = 10,000$ $k = 1,900$
$\alpha = .05$	11.8%...28.1%	16.6%...21.6%	18.2%...19.8%
$\alpha = .01$	10.1%...31.0%	15.9%...22.4%	18.0%...20.0%
$\alpha = .001$	8.3%...34.5%	15.1%...23.4%	17.7%...20.3%

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Confidence intervals in R

- ◆ Most hypothesis tests in R also compute a confidence interval (including `binom.test()`)
 - omit H_0 if only interested in confidence interval
- ◆ Significance level of underlying hypothesis test is controlled by `conf.level` parameter
 - expressed as confidence, e.g. `conf.level=.95` for significance level $\alpha = .05$, i.e. 95% confidence
- ◆ Can also compute one-sided confidence interval
 - controlled by `alternative` parameter
 - two-sided confidence intervals strongly recommended

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Confidence intervals in R

```
> binom.test(190, 1000, conf.level=.99)
Exact binomial test

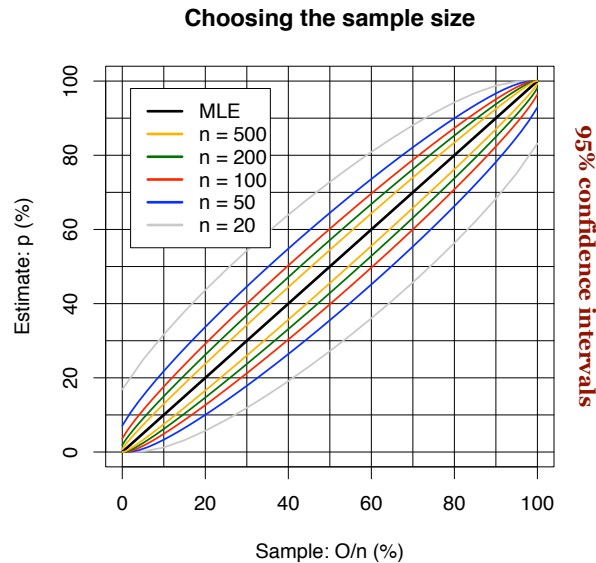
data: 190 and 1000
number of successes = 190, number of trials = 1000, p-value < 2.2e-16

alternative hypothesis: true probability of success is not equal to 0.5
99 percent confidence interval:
 0.1590920 0.2239133

sample estimates:
probability of success
               0.19
```

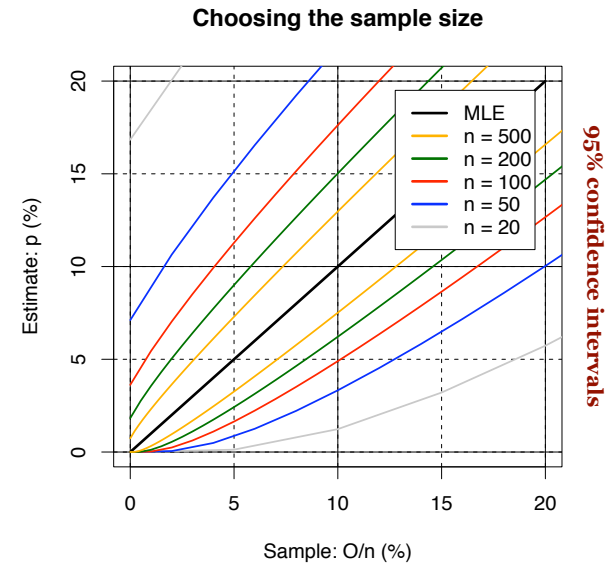
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Choosing sample size



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Choosing sample size



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Using R to choose sample size

- ◆ Call `binom.test()` with hypothetical values
- ◆ Plots on previous slides also created with R
 - requires calculation of large number of hypothetical confidence intervals
 - `binom.test()` is both inconvenient and inefficient
- ◆ The `corpora` package has a vectorized function
 - > `library(corpora)` # install from CRAN
 - > `prop.cint(190, 1000, conf.level=.99)`
 - > `?prop.cint` # “conf. intervals for proportions”

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Frequency comparison

- ◆ Many linguistic research questions can be operationalised as a frequency comparison
 - Are split infinitives more frequent in AmE than BrE?
 - Are there more definite articles in texts written by Chinese learners of English than native speakers?
 - Does *meow* occur more often in the vicinity of *cat* than elsewhere in the text?
 - Do speakers prefer *I couldn't agree more* over alternative compositional realisations?
- ◆ Compare observed frequencies in two samples

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Frequency comparison

k_1	k_2
$n_1 - k_1$	$n_2 - k_2$

19	25
81	175

- ◆ Contingency table for frequency comparison
 - e.g. samples of sizes $n_1 = 100$ and $n_2 = 200$, containing 19 and 25 passives
 - H_0 : same proportion in both underlying populations
- ◆ Chi-squared X^2 , likelihood ratio G^2 , Fisher's test
 - based on same principles as binomial test

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Frequency comparison

- ◆ Chi-squared, log-likelihood and Fisher are appropriate for different (numerical) situations
- ◆ Estimates of effect size (confidence intervals)
 - e.g. difference or ratio of true proportions
 - exact confidence intervals are difficult to obtain
- ◆ Frequency comparison in practice
 - all relevant tests can be performed in R
 - easier (for non-techies) with **online wizards**



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Frequency comparison in R

- ◆ Frequency comparison with `prop.test()`
 - easy to use: specify counts k_i and sample sizes n_i
 - uses chi-squared test “behind the scenes”
 - also computes confidence interval for difference of population proportions
- ◆ E.g. for 19 passives out of 100 vs. 25 out of 200
 - `prop.test(c(19,25), c(100,200))`
 - parameters `conf.level` and `alternative` can be used in the familiar way

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Frequency comparison in R

```
> prop.test(c(19,25), c(100,200))
      2-sample test for equality of proportions with
      continuity correction
data:  c(19, 25) out of c(100, 200)
X-squared = 1.7611, df = 1, p-value = 0.1845
alternative hypothesis: two.sided
95 percent confidence interval:
 -0.03201426  0.16201426
sample estimates:
prop 1 prop 2
 0.190  0.125
```

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Frequency comparison in R

- ◆ Can also carry out chi-squared (`chisq.test`) and Fisher's exact test (`fisher.test`)
 - requires full contingency table as 2×2 matrix
 - NB: likelihood ratio test not in standard library

- ◆ Table for 19 out of 100 vs. 25 out of 200

```
> ct <- cbind(c(19,81),  
              c(25,175))  
> chisq.test(ct)  
> fisher.test(ct)
```

19	25
81	175

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Some fine print

- ◆ Convenient `cont.table` function for building contingency tables in `corpora` package

```
> library(corpora)  
> ct <- cont.table(19, 100, 25, 200)
```
- ◆ Difference of proportions no always suitable as **measure of effect size**
 - especially if proportions can have different magnitudes (e.g. for lexical frequency data)
 - more intuitive: ratio of proportions (**relative risk**)
 - Conf. int. for similar **odds ratio** from Fisher's test

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A case study: passives

- ◆ As a case study, we will compare the frequency of passives in Brown (AmE) and LOB (BrE)
 - pooled data
 - separately for each genre category
- ◆ Data files provided in CSV format
 - **passives.brown.csv** & **passives.lob.csv**
 - `cat` = genre category, `passive` = number of passives, `n_w` = number of word, `n_s` = number of sentences, `name` = description of genre category

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Preparing the data

```
> Brown <- read.csv("passives.brown.csv")  
> LOB <- read.csv("passives.lob.csv")  
  
> Brown      # take a first look at the data tables  
> LOB
```

```
# pooled data for entire corpus = column sums (col. 2 ... 4)  
> Brown.all <- colSums(Brown[, 2:4])  
> LOB.all <- colSums(LOB[, 2:4])
```

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Frequency tests for pooled data

```
> ct <- cbind(c(10123, 49576-10123), # Brown
              c(10934, 49742-10934)) # LOB
> ct          # contingency table for chi-squared / Fisher
> fisher.test(ct)

# proportions test provides more interpretable effect size
> prop.test(c(10123, 10934), c(49576, 49742))

# we could in principle do the same for all 15 genres ...
```

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A nicer user function

```
# extract relevant information directly from data frames
> do.test(Brown$passive[15], Brown$n_s[15],
          LOB$passive[15], LOB$n_s[15])

# nicer version of user function with genre category labels
> do.test <- function (k1, n1, k2, n2, cat="") {
  res <- prop.test(c(k1, k2), c(n1, n2))
  fmt <- data.frame(p=res$p.value,
                    lower=res$conf.int[1], upper=res$conf.int[2])
  rownames(fmt) <- cat # add genre as row label
  fmt
}

> do.test(Brown$passive[15], Brown$n_s[15],
          LOB$passive[15], LOB$n_s[15],
          cat=Brown$cat[15])
```

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Automation: user functions

```
# user function do.test() executes proportions test for samples
#  $k_1/n_1$  and  $k_2/n_2$ , and summarizes relevant results in compact form
> do.test <- function (k1, n1, k2, n2) {
  # res contains results of proportions test (list = data structure)
  res <- prop.test(c(k1, k2), c(n1, n2))
  # data frames are a nice way to display summary tables
  fmt <- data.frame(p=res$p.value,
                    lower=res$conf.int[1], upper=res$conf.int[2])
  fmt # return value of function = last expression
}

> do.test(10123, 49576, 10934, 49742) # pooled data
> do.test(146, 975, 134, 947)         # humour genre
```

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Automation: the for loop

```
# our code relies on same ordering of genre categories!
> all(Brown$cat == LOB$cat)

# carry out tests for all genres with a simple for loop
> for (i in 1:15) {
  res <- do.test(Brown$passive[i], Brown$n_s[i],
                 LOB$passive[i], LOB$n_s[i],
                 cat=Brown$cat[i])
  print(res)
}

# it would be nice to collect all these results in a single overview
# table; for this, we need a little bit of R wizardry ...
```

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Collecting rows

```
# lapply collects results from iteration steps in a list
> result.list <- lapply(1:15, function (i) {
  do.test(Brown$passive[i], Brown$n_s[i],
          LOB$passive[i], LOB$n_s[i],
          cat=Brown$name[i])
})
> result <- do.call(rbind, result.list)
# think of this as an idiom that you just have to remember ...
> round(result, 5) # easier to read after rounding
```

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It's your turn now ...

◆ Questions:

- Which differences are significant?
- Are the effect sizes linguistically relevant?

◆ Homework:

- Extend `do.test()` such that the two sample proportions are included in the summary table.
- Do you need to modify any of the other code as well?

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Further reading

- ◆ Baroni, Marco and Evert, Stefan (2008, in press). **Statistical methods for corpus exploitation**. In A. Lüdeling and M. Kytö (eds.), *Corpus Linguistics. An International Handbook*, chapter 38. Mouton de Gruyter, Berlin.
 - [an extended and more detailed version of this talk](#)
- ◆ Evert, Stefan (2006). **How random is a corpus?** The library metaphor. *Zeitschrift für Anglistik und Amerikanistik*, **54**(2), 177–190.
 - [introduces library metaphor for statistical tests on corpus data](#)
- ◆ Agresti, Alan (2002). *Categorical Data Analysis*. John Wiley & Sons, Hoboken, 2nd edition.
 - [mathematical details on frequency tests and frequency comparison](#)

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