Statistical Inference: a Gentle Introduction for Linguists and similar creatures (SIGIL) With practical examples in GNU R

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http://SIGIL.r-forge.r-project.org/

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Statistical inference and GNU R About this course

Getting Started With R

Installation tips

Basic functionalities

External files and data-frames

A simple case study: comparing Brown and LOB

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 - ▶ all linguistic data are samples (of language, speakers, ...)
 - observed effects may be coincidence of particular sample
 - inferential statistics

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 - statistical summaries, data analysis, visualisation
 - e.g. collocations as compact summary of word usage
 - descriptive statistics

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- Managing large data sets
 - statistical summaries, data analysis, visualisation
 - e.g. collocations as compact summary of word usage
 - descriptive statistics
- Discovering latent (hidden) properties
 - clustering, multivariate analysis, distributional semantics
 - advanced statistical modelling (e.g. mixed-effects models)
 - exploratory data analysis



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- ► Random variables & scales of measurement

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What you can do on your own:

Learn about specific statistical tests and procedures



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 - commercial: S-Plus (Insightful Corporation, since 1987)
- ▶ R is an open-source implementation of the S language
 - originally by Ross Ihaka and Robert Gentleman (Auckland)
 - open-source development since mid-1997



- binary packages available for Linux, Mac OS X and Windows
- ▶ 64-bit support for large data sets
- extensive documentation & tutorials
- thousands of add-on packages ready to install from CRAN

http://www.R-project.org/

Recommended cross-platform GUI: RStudio from http://www.rstudio.com/ide/

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More about R

- Advantages of R
 - ▶ free & open source
 - many add-on packages with state-of-the-art algorithms
 - large, enthusiastic and helpful user community
 - easy to automate and extend (every analysis is a program)
 - ▶ no point & click interface

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 - many add-on packages with state-of-the-art algorithms
 - large, enthusiastic and helpful user community
 - easy to automate and extend (every analysis is a program)
 - no point & click interface
- Disadvantages
 - learning curve sometimes rather steep
 - not very good at manipulating non-English text
 - no built-in data editor (spreadsheet)
 - ▶ no point & click interface

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Goals of the course

- Basic principles of statistical inference
- ► Elementary hypothesis tests, estimators & models
- Hands-on work with R on real-life data sets
- Data manipulation and basic R programming skills
- Get to know R implementations of statistical techniques, data analysis and visualisation methods that are useful in various areas of (computational) linguistics along the way

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What this course is **not** about:

- Deeper mathematical foundations of statistics
- Specific (advanced) statistical methods
- ► Cookbook recipes for particular analyses with R



Course units

- 1. R Basics: installation, data manipulation, input/output (h)
- 2. Corpus frequency data & statistical inference (h)
- 3. Descriptive and inferential statistics for continuous data (f)
- 4. Co-occurrence, contingency tables and collocations (f)
 + vectorised data processing, high-quality graphs
- 5. Word frequency distributions with the zipfR package (h)
- 6. Regression and linear models (f)
- 7. Exploratory data analysis: clustering, visualisation, ML (h)
- 8. The non-randomness of corpus data: a GLM approach (h)
- 9. Inter-annotator agreement (h)
- (h) = half-day session / (f) = full-day session (optimistic)



Introductions



Who are you?

Recommended textbooks: introductory level

- Baroni, Marco & Evert, Stefan (2008). Statistical methods for corpus exploitation. In A. Lüdeling & M. Kytö (eds.), Corpus Linguistics. An International Handbook, Mouton de Gruyter.
- ► Gries, Stefan Th. (2013). Statistics for Linguistics with R: A Practical Introduction, 2nd ed. Mouton de Gruyter. [€29]
 - German original from Vandenhoek & Ruprecht [€25]
- ▶ Johnson, Keith (2008). Quantitative Methods in Linguistics. Blackwell. [€38]
- Peter Dalgaard (2008). Introductory Statistics with R, 2nd ed. Springer. [€52]
- ► Teetor, Paul (2011). *R Cookbook*. O'Reilly Media. [€25]
- ► Kabacoff, Robert I. (2011). *R in Action: Data analysis and graphics with R.* Manning. [€40]



Recommended textbooks: advanced level

- ▶ R. Harald Baayen (2008). Analyzing Linguistic Data: A practical introduction to statistics. CUP. [€29]
 - http://www.sfs.uni-tuebingen.de/~hbaayen/publications/
- Morris H. DeGroot and Mark J. Schervish (2002). Probability and Statistics, 4th ed. Pearson Education Ltd. [€74]
- ▶ John M. Chambers (2008). *Software for Data Analysis: Programming with R.* Springer. [€85]
- ► Christopher Butler (1985), *Statistics in Linguistics*. Blackwell.
 - out of print and available online for free download from http://www.uwe.ac.uk/hlss/llas/statistics-in-linguistics/bkindex.shtml
- ▶ Burns, Patrick (2011). *The R inferno*. Online publication.
 - http://www.burns-stat.com/documents/books/the-r-inferno/



Course materials

Handouts, example scripts and data sets are available on our homepage for this course:

```
http://SIGIL.R-Forge.R-Project.org/
```

(includes additional material, software, links, etc.)

Another interesting online course:

- ► Shravan Vasishth (2006–2009). *The foundations of statistics:* A simulation-based approach.
 - http://www.ling.uni-potsdam.de/~vasishth/SFLS.html

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Installation guide for Linux & Mac OS X

Mac OS X

- ► Download binary installer from http://www.R-project.org/
- Start GUI application R (64-bit)
- Alternative: run from TextMate or various other text editors
- ▶ Shell commmand R available for command-line use

Linux (Ubuntu and other popular distributions)

- ► Install R with standard package manager (e.g. Synaptic)
- Add CRAN repository to obtain up-to-date version of R
 - e.g. http://cran.at.r-project.org/bin/linux/ubuntu precise/
 - ▶ pkgs: r-base-core r-base-html r-base-dev r-doc-html r-doc-pdf
- Various GUIs available, e.g. Rkward and R Commander
- ▶ Power users: Emacs + ESS or shell command R in terminal

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Installing add-on packages

Mac OS X

- ► Select Packages & Data | Package Installer from GUI menu
- Click Get List, then choose packages to be installed
 - you may need to check install dependencies, too
 - installing for all users is only possible on the command line

Linux (Ubuntu and other popular distributions)

- Use standard package manager with CRAN repository
 - offers choice of "difficult" binary packages named r-cran-*
 - make sure that you install the up-to-date CRAN versions!
- Other packages need to be installed from the command line

All Unix platforms

- ▶ Install packages from within R (system-wide with sudo R)
 - e.g. install.packages(c("languageR", "corpora"))
 - select CRAN mirror from pop-up list (recommended: Austria)



Installation on Windows (XP/Vista/7)

- Step 1: Download R for Windows installer from www.R-project.org
 - ► CRAN | choose mirror (Austria) | R for Windows | base
 - ▶ Download R . . . for Windows, then run the installer
 - ▶ if Windows complains, allow installer to run & make changes
 - select "full installation" and keep defaults for everything else
 - start R, adjust GUI preferences and save to default location (make sure to select SDI mode if you use Tinn-R GUI)

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Step 2: Install some important add-on packages

data(VSS); head(VSS, 20)

- ▶ Vista/Win 7: run R as administrator to install packages for all users (right-click program icon in Start menu)
- select Packages | Install package from GUI menu
- choose mirror (Austria), then pick the package(s) to install
- check successful installation with these R commands: library(corpora) help("VSS") # should pop up Web browser with help page

Recommended add-on packages for this course

```
SIGIL data sets and utilities for this course corpora some additional corpus-related functions

languageR data sets and functions from Baayen (2008)

exact2x2 exact inference for 2 × 2 contingency tables (relevant for corpus frequency comparisons)

zipfR word frequency distributions & Zipf's law
e1071 machine learning (SVM) and many other utilities

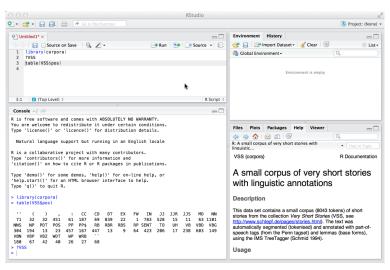
MASS lots of statistical functions (companion package to Modern Applied Statistics with S and S-Plus)
```

Some other useful packages:

```
rg1 animated 3D graphics with OpenGL (also: misc3d) vcd visualisation of categorical data (contingency tables) plyr, doBy, convenience functions for data manipulation
```

Recommended cross-platform GUI: RStudio

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R as an oversized calculator

```
> 1+1
[1] 2
> a <- 2
               # assignment does not print anything by default
> a * 2
[1] 4
> log(a)
               # natural, i.e. base-e logarithm
[1] 0.6931472
> log(a,2) # base-2 logarithm
[1] 1
```

Basic session management

Some of it is not necessary if you only use the GUI

```
# to start R on command line, simply type "R"
setwd("path/to/data") # or use GUI menus
ls()
                           # probably empty for now
าร
                           # notice difference with previous line
quit()
                           # or use GUI menus
quit(save="yes")
quit(save="no")
```

NB: at least some interfaces support history recall, TAB completion, etc.

Vectorial math

```
> a < c(1,2,3) # c (for combine) creates vectors
> a * 2 # operators are applied to each element of a vector
[1] 2 4 6
> log(a) # also works for most standard functions
[1] 0.0000000 0.6931472 1.0986123
> sum(a) # basic vector operations: sum, length, product, ...
[1] 6
> length(a)
Г1] 3
> sum(a)/length(a)
[1] 2
```

Initializing vectors

```
> a <- 1:100  # integer sequence
> a

> a <- 10^(1:100)

> a <- seq(from=0, to=10, by=0.1) # general sequence
> a <- rnorm(100)  # 100 random numbers
> a <- runif(100, 0, 5) # what you're used to from Java etc.</pre>
```

Summary statistics

More about these summary statistics in Unit 3

```
> length(a)
> summary(a) # statistical summary of numeric vector
  Min. 1st Qu. Median Mean 3rd Qu.
                                         Max.
0.02717 0.51770 1.05200 1.74300 2.32600 9.11100
> mean(a)
> median(a)
> sd(a)
                # standard deviation is not included in summary
> quantile(a)
   0%
         25%
                50% 75%
                           100%
0.0272 0.5177 1.0518 2.3261 9.1107
```

Basic plotting

```
> a <- 2^{(1:100)}
                           # don't forget the parentheses!
> plot(a)
> x <- 1:100
                           # most often: plot x against y
> y <- sqrt(x)
> plot(x, y)
> plot(x, a)
> plot(x, a, log="y") # various logarithmic plots
> plot(x, a, log="x")
> plot(x, a, log="xy")
> plot(log(x), log(a))
> hist(rnorm(100))
                           # histogram and density estimation
> hist(rnorm(1000))
> plot(density(rnorm(100000)))
```

(Slightly less) basic plotting

```
> a <- rbinom(10000,100,.5)
> hist(a)
> hist(a, probability=TRUE)
> lines(density(a))
> hist(a, probability=TRUE)
> lines(density(a), col="red", lwd=3)
> hist(a, probability=TRUE,
  main="Some Distribution", xlab="value",
  ylab="probability") # better to type command on a single line!
> lines(density(a), col="red", lwd=3)
```

Help!

- > help("hist") # R has excellent online documentation
- > ?hist # short, convenient form of the help command
- > help.search("histogram")
- > ?help.search
- > help.start() # searchable HTML documentation
- # or use GUI menus to access & search documentation

Your first R script

- Simply type R commands into a text file & save it
- Use built-in GUI functionality or external text editor
 - ▶ Microsoft Word is *not* a text editor!
 - nor is Apple's TextEdit application . . .
- Execute R script from GUI editor or by typing
 - > source("my_script.R") # more about files later
 - > source(file.choose()) # select with file dialog box
- ► Many GUI editors can execute scripts line by line
 - check your editor's documentation for keyboard shortcuts
- ▶ Just typing an expression will not automatically print the result in a script: use print(sd(a)) instead of sd(a)

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Input from an external file

▶ We like to keep our data in space- or TAB-delimited text files with a first row ("header") labeling the fields:

```
word frequency cat
dog 15 noun
bark 10 verb
```

- ► This is an easy format to import into R, and it is easy to convert to/from other tabular formats using standard tools
- We assume that external input is always in this format (or can easily be converted to it)
 - spreadsheet applications prefer CSV (comma-separated values), which R also reads and writes quite well
 - Microsoft Excel is a nice table editor, but beware of localised number formats

Reading a TAB-delimited file with header

```
> brown <- read.table("brown.stats.txt",</pre>
  header=TRUE)
# if file is not in working directory, you must specify the full path
# (or use setwd() function we introduced before)
# exact behaviour of file.choose() depends on operating system
> brown <- read.table(file.choose(), header=TRUE)</pre>
# more robust if you are sure file is in tab-delimited format
> brown <- read.delim("brown.stats.txt")</pre>
# this data set is also included in the SIGIL package
> library(SIGIL)
> brown <- BrownStats
```

Reading and writing CSV files

```
# R can also read and write files in CSV format
> write.csv(brown, "brown.stats.csv",
  row.names=FALSE)
# this is convenient for exchanging data with database and
# spreadsheet software (or using Excel as a data editor)
# NB: comma-separated values are not always separated by commas
# (e.g. in German; use write.csv2 if Excel doesn't recognise columns)
> write.csv2(brown, "brown.stats.csv",
  row.names=FALSE)
# TASK: load brown.stats.csv into Excel or OpenOffice.org
# check generated CSV file (use read.csv2 with write.csv2 above)
> brown.csv <- read.csv("brown.stats.csv")</pre>
> all.equal(brown.csv, brown)
```

Data frames

- ► The commands above create a data frame
- This is the basic data structure (object) used to represent statistical tables in R
 - rows = objects or "observations"
 - columns = variables, i.e. measured quantities
- Different types of variables
 - numerical variables (what we've used so far)
 - Boolean variables
 - factor variables (nominal or ordinal classification)
 - string variables
- ► Technically, data frames are collections of column vectors (of the same length), and we will think of them as such



Data frames

- > summary(brown)
- > colnames(brown)
- > dim(brown) # number of rows and columns
- > head(brown)
- > plot(brown)

Type/token counts and word lengths for Brown & LOB texts

Data files in TAB-delimited format:

- ▶ brown.stats.txt: information for Brown corpus (AmE)
- ▶ lob.stats.txt: information for LOB corpus (BrE)

Variables:

- to Token count
- ty Type count (distinct words)
- se Sentence count
- towl Average word length (averaged across tokens in document)
- tywl Average word length (averaged across distinct types in document)

Access vectors inside a data frame

```
> brown$to
> head(brown$to)
# TASK: compute summary statistics (length, mean, max, etc.)
# for vectors in the Brown data frame
# what does the following do?
> summary(brown$ty / brown$to)
> attach(brown)
                     # attach data frame for convenient access
> summary(ty/to)
> detach()
                     # detach from search path
> with(brown, summary(ty/to)) # a better approach
```

More data access

```
> brown$ty[1]  # vector indexing starts with 1
> brown[1,2]  # row, column

> brown$ty[1:10]  # use arbitrary vectors as indices
> brown[1:10,2]

> brown[1,]
> brown[,2]
```

Conditional selection

```
> brown[brown$to < 2200, ]</pre>
                                 # index with Boolean vector
> brown$ty[brown$to >= 2200]
> sum(brown$to >= 2200)
                                  # standard way to count matches
> subset(brown, to < 2200) # syntactic sugar (similar to with)
> lessdata <- subset(brown, to < 2200)</pre>
> a <- brown$ty[brown$to >= 2200]
\# equality: == (also works for strings)
# inequality: !=
# complex constraints: and &, or |, not !
# NB: always use single characters, not && or ||
```

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Procedure

The methods used here will be explained in Units 3 and 6

- Collect basic summary statistics for the two corpora
- ▶ Check if there is a significant difference in the token counts (since document length was controlled by corpus builders)
- ▶ If difference is significant (we will see that it is), then type counts are not directly comparable, and sentence counts should be normalized (divide by token count)
- Is word length correlated to document length? (corpus comparison would also not be appropriate in this case)

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- If difference is significant (we will see that it is), then type counts are not directly comparable, and sentence counts should be normalized (divide by token count)
- Is word length correlated to document length? (corpus comparison would also not be appropriate in this case)
- Please read the LOB data set into a data frame named lob now, and take a look at its basic statistics
 - ▶ file lob.stats.txt, or LOBStats in SIGIL package
- ► Also, plot the data frame for a first impression of correlations between the variables

Comparing token counts

```
> boxplot(brown$to,lob$to)
> boxplot(brown$to,lob$to,names=c("brown","lob"))
> boxplot(brown$to,lob$to,names=c("brown","lob"),
  ylim=c(1500,3000))
> ?boxplot
> t.test(brown$to. lob$to)
> wilcox.test(brown$to, lob$to)
> brown.to.center <-
  with(brown, to[to > 2200 & to < 2400])
> lob.to.center <-
  with(lob, to[to > 2200 \& to < 2400])
> t.test(brown.to.center, lob.to.center)
```

Is word length correlated with token count?

```
# average word length by tokens and types is almost the same:
> plot(brown$towl, brown$tywl)
> cor.test(brown$towl, brown$tywl)
> cor.test(brown$towl, brown$tywl, method="spearman")
# correlation with token count
> plot(brown$to, brown$towl)
> cor.test(brown$to, brown$towl)
```