# The Statistical Sleuth in R: Chapter 5

Kate Aloisio Ruobing Zhang Nicholas J. Horton\*

September 16, 2012

#### Contents

T	Inti	coduction	J
2	Die	t and lifespan	2
	2.1	Summary statistics and graphical display	2
	2.2	One-way ANOVA	4
	2.3	Pairwise comparisons	١
	2.4	Other analyses	(
	2.5	Residual analysis and diagnostics	7
3	Spo	ock Conspiracy Trial	8
	3.1	Summary statistics and graphical display	$\epsilon$
	3.2	One-way ANOVA	1(
	3.3	Additional analyses	12
		3.3.1 Kruskal-Wallis Nonparametric Analysis of Variance	

### 1 Introduction

This document is intended to help describe how to undertake analyses introduced as examples in the Second Edition of the *Statistical Sleuth* (2002) by Fred Ramsey and Dan Schafer. More information about the book can be found at http://www.proaxis.com/~panorama/home.htm. This file as well as the associated knitr reproducible analysis source file can be found at http://www.math.smith.edu/~nhorton/sleuth.

This work leverages initiatives undertaken by Project MOSAIC (http://www.mosaic-web.org), an NSF-funded effort to improve the teaching of statistics, calculus, science and computing in the undergraduate curriculum. In particular, we utilize the mosaic package, which was written to simplify the use of R for introductory statistics courses. A short summary of the R needed to teach introductory statistics can be found in the mosaic package vignette (http://cran.r-project.org/web/packages/mosaic/vignettes/MinimalR.pdf).

<sup>\*</sup>Department of Mathematics and Statistics, Smith College, nhorton@smith.edu

To use a package within R, it must be installed (one time), and loaded (each session). The package can be installed using the following command:

```
> install.packages("mosaic") # note the quotation marks
```

Once this is installed, it can be loaded by running the command:

```
> require(mosaic)
```

This needs to be done once per session.

In addition the data files for the *Sleuth* case studies can be accessed by installing the **Sleuth2** package.

```
> install.packages("Sleuth2")  # note the quotation marks
```

```
> require(Sleuth2)
```

We also set some options to improve legibility of graphs and output.

```
> trellis.par.set(theme = col.mosaic()) # get a better color scheme
> options(digits = 3)
>
```

The specific goal of this document is to demonstrate how to calculate the quantities described in Chapter 5: Comparisons Among Several Samples using R.

# 2 Diet and lifespan

Does restricting the diet of female mice lead to increased lifespan? This is the question addressed in case study 5.1 in the *Sleuth*.

#### 2.1 Summary statistics and graphical display

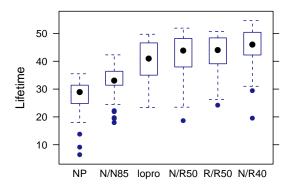
We begin by reading the data and summarizing the variables.

```
> summary(case0501)
    Lifetime
                   Diet
 Min. : 6.4
                NP
                     :49
 1st Qu.:31.8
                N/N85:57
Median:39.5
                lopro:56
 Mean
        :38.8
                N/R50:71
3rd Qu.:46.9
                R/R50:56
 Max. :54.6
                N/R40:60
```

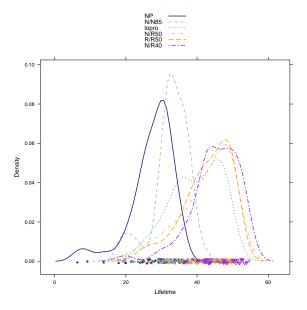
```
> favstats(Lifetime ~ Diet, data = case0501)
      min
              Q1 median
                           Q3 max
                                   mean
                                            sd
                                                n missing
       6.4 24.80
                  28.90 31.40 35.5 27.40 6.134 49
NP
N/N85 17.9 31.40 33.10 36.40 42.3 32.69 5.125 57
                                                        0
lopro 23.4 35.00 41.05 46.45 49.7 39.69 6.992 56
                                                        0
N/R50 18.6 37.95 43.90 48.20 51.9 42.30 7.768 71
                                                        0
R/R50 24.2 39.15 43.95 48.35 50.7 42.89 6.683 56
                                                        0
N/R40 19.6 42.27 46.05 50.35 54.6 45.12 6.703 60
```

There were a total of 349 female mice. These mice were randomly assigned to one of 6 diets. Their lifetimes were then recorded, as shown in Display 5.2 (page 115 of the *Sleuth*).

```
> bwplot(Lifetime ~ Diet, data = case0501) # Display 5.1
```







Statistical Sleuth in R: Chapter 5

#### 2.2 One-way ANOVA

First we fit the one way analysis of variance (ANOVA) model, using all of the groups.

There is a strong statistically significant difference between the diets.

By default, the use of the linear model (regression) function displays the pairwise differences between the first group and each of the other groups. Note that the overall test of the model is the same.

```
> summary(lm(Lifetime ~ Diet, data = case0501))
Call:
lm(formula = Lifetime ~ Diet, data = case0501)
Residuals:
   Min
            10 Median
                            3Q
                                  Max
-25.517 -3.386 0.814 5.183 10.014
Coefficients:
           Estimate Std. Error t value Pr(>|t|)
             27.402
                       0.954 28.72 < 2e-16 ***
(Intercept)
                       1.301
                                 4.07 5.9e-05 ***
DietN/N85
             5.289
Dietlopro
             12.284
                       1.306
                               9.40 < 2e-16 ***
DietN/R50
            14.895
                       1.240 12.01 < 2e-16 ***
DietR/R50
             15.484
                        1.306 11.85 < 2e-16 ***
DietN/R40
             17.715
                         1.286
                               13.78 < 2e-16 ***
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 6.68 on 343 degrees of freedom
Multiple R-squared: 0.454, Adjusted R-squared: 0.446
F-statistic: 57.1 on 5 and 343 DF, p-value: <2e-16
```

The reference group is NP, followed by N/N85, lopro, N/R50, R/R50, N/R40.

#### 2.3 Pairwise comparisons

Next we used contrasts for the results on page 121, Display 5.7, and part (a) on page 115:

The results for (b) on page 115-116:

The results for (c) on page 116:

```
> # N/R40 vs N/R50 (c)
> fit.contrast(lm(Lifetime ~ Diet, data = case0501), "Diet", c(0, 0, 0, -1, 0,
     1), conf.int = 0.95)
                       Estimate Std. Error t value Pr(>|t|) lower CI
Diet c=( 0 0 0 -1 0 1 )
                          2.819
                                    1.171 2.408 0.01659 0.516
                       upper CI
Diet c=( 0 0 0 -1 0 1 )
                          5.123
> # N/N85 vs N/R40
> fit.contrast(lm(Lifetime ~ Diet, data = case0501), "Diet", c(0, -1, 0, 0, 0,
    1), conf.int = 0.95)
                       Estimate Std. Error t value Pr(>|t|) lower CI
Diet c=( 0 -1 0 0 0 1 )
                          12.43
                                     1.235 10.06 4.964e-21
                                                                9.996
                       upper CI
Diet c=( 0 -1 0 0 0 1 ) 14.85
```

The results for (d) on page 116:

The results for (e) on page 116:

Another way of viewing these results is through a model table, which displays the differences between the grand mean and the group means.

Another way of calculating the above results is done with the following code:

```
> mean(Lifetime ~ Diet, data = case0501) - mean(~Lifetime, data = case0501)

NP N/N85 lopro N/R50 R/R50 N/R40
-11.3951 -6.1059 0.8886 3.5000 4.0886 6.3195
```

#### 2.4 Other analyses

We will next demonstrate how to calculate the quantities on page 120 (Display 5.6).

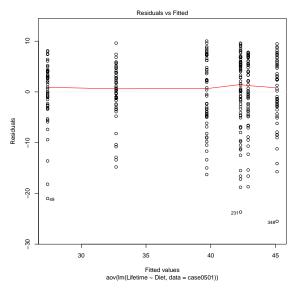
```
> df = length(case0501$Diet) - length(unique(case0501$Diet))
> df
[1] 343
> sdvals = with(case0501, tapply(Lifetime, Diet, sd))
> sdvals
   NP N/N85 lopro N/R50 R/R50 N/R40
6.134 5.125 6.992 7.768 6.683 6.703
> nvals = with(case0501, tapply(Lifetime, Diet, length))
> nvals
   NP N/N85 lopro N/R50 R/R50 N/R40
   49
         57
               56
                   71
                           56
                                 60
> pooledsd = sum(sdvals * nvals)/sum(nvals)
> pooledsd
[1] 6.625
```

Note that the pooled standard deviation reported in chapter 5 is not the same as the root MSE from the ANOVA. For the rest of this document we will use the ANOVA estimate of the root mean squared error.

#### 2.5 Residual analysis and diagnostics

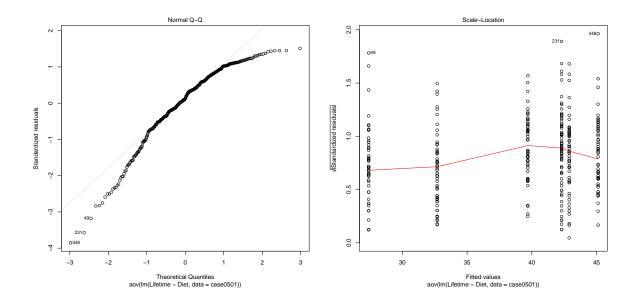
The residuals versus fitted graph does not demonstrate dramatic lack of fit (though some of the mice had very small residuals). The following figure is akin to Display 5.14 (page 132).

```
> aov1 = aov(lm(Lifetime ~ Diet, data = case0501))
> plot(aov1, which = 1)
```



The quantile plot of the residuals indicates that the normality assumption may be violated.

```
> plot(aov1, which = 2)
> plot(aov1, which = 3)
```



## 3 Spock Conspiracy Trial

Did Dr. Benjamin Spock have a fair trial? More specifically, were women underrepresented on his jury pool? This is the question considered in case study 5.2 in the *Sleuth*.

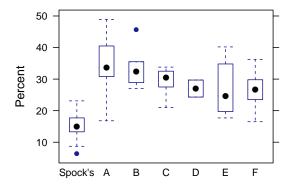
#### 3.1 Summary statistics and graphical display

We begin by reading the data and summarizing the variables.

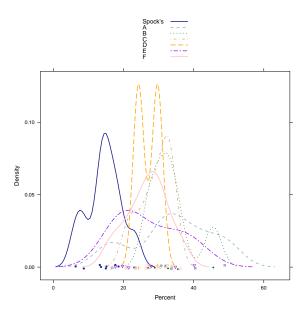
```
> summary(case0502)
    Percent
                     Judge
        : 6.4
                Spock's:9
 Min.
 1st Qu.:19.9
                        :5
 Median:27.5
                        :6
Mean
        :26.6
                C
                        :9
 3rd Qu.:32.4
                        :2
                D
Max.
        :48.9
                Ε
                        :6
                F
                        :9
> case0502$Judge = with(case0502, as.factor(Judge))
> favstats(Percent ~ Judge, data = case0502)
         min
                Q1 median
                              Q3 max mean
Spock's
        6.4 13.30
                    15.00 17.70 23.1 14.62
                                             5.039 9
Α
        16.8 30.80
                    33.60 40.50 48.9 34.12 11.942 5
                                                            0
В
        27.0 29.67
                    32.35 34.80 45.6 33.62
                                                            0
                                              6.582 6
C
        21.0 27.50
                    30.50 32.50 33.8 29.10
                                              4.593 9
                                                            0
D
        24.3 25.65
                    27.00 28.35 29.7 27.00
                                                            0
                                              3.818 2
Ε
        17.7 20.15
                    24.70 33.07 40.2 26.97
                                                            0
                                              9.010 6
        16.5 23.50
                    26.70 29.80 36.2 26.80
                                                            0
                                             5.969 9
```

There were a total of 46 venires. They compared Spock's judge with 6 other judges. The precent of women within each venire was recorded as shown in Display 5.4 (page 117 of the *Sleuth*).

```
> bwplot(Percent ~ Judge, data = case0502) # Display 5.5 (page 118)
```







### 3.2 One-way ANOVA

First we fit the one way analysis of variance (ANOVA) model, with all of the groups. These results are summarized on page 118 and shown in Display 5.10 (page 127).

By default, the use of the linear model (regression) function displays the pairwise differences between the first group and each of the other groups. Note that the overall test of the model is the same.

```
> summary(lm(Percent ~ Judge, data = case0502))

Call:
lm(formula = Percent ~ Judge, data = case0502)
```

```
Residuals:
  Min 1Q Median 3Q
                               Max
-17.32 -4.37 -0.25 3.32 14.78
Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 14.62 2.30 6.34 1.7e-07 ***
                        3.86 5.06 1.1e-05 ***
3.64 5.21 6.4e-06 ***
3.26 4.44 7.2e-05 ***
JudgeA
             19.50
             18.99
14.48
JudgeB
JudgeC
                         5.41 2.29 0.0275 *
JudgeD
             12.38
             12.34 3.64 3.39 0.0016 **
12.18 3.26 3.74 0.0006 ***
JudgeE
JudgeF
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 6.91 on 39 degrees of freedom
Multiple R-squared: 0.508, Adjusted R-squared: 0.433
F-statistic: 6.72 on 6 and 39 DF, p-value: 6.1e-05
```

Then we can fit the one way analysis of variance F-test of whether the mean percentage is the same for judges A-F (page 118).

#### 3.3 Additional analyses

Now we will demonstrate how to fit the reduced model comparing Spock's judge to a combination of the other judges. First we create a 2 level version of the grouping variable.

```
> case0502$twoJudge = as.character(case0502$Judge)
> case0502$twoJudge[case0502$Judge != "Spock's"] = "notspock"
> tally(twoJudge ~ Judge, format = "count", data = case0502)

Judge
twoJudge Spock's A B C D E F
Spock's 9 0 0 0 0 0 0
notspock 0 5 6 9 2 6 9
Total 9 5 6 9 2 6 9
```

Recall that the book calculates the extra sum of squares as (2,190.90 - 1864.45)/(44-39)) / (1864.45 / 39) = 1.37, with df 5 and 39. P(F > 1.366) = 0.26 (page 130). Below are the calculations for the results found on page 128.

```
> numdf1 = aov1["Residuals", "Df"]
> numdf1 # Within
Γ17 39
> ss1 = aov1["Residuals", "Sum Sq"]
> ss1 # Within
[1] 1864
> aov2 = anova(lm(Percent ~ as.factor(twoJudge), data = case0502))
> aov2
Analysis of Variance Table
Response: Percent
                    Df Sum Sq Mean Sq F value Pr(>F)
                                         32.1 1e-06 ***
as.factor(twoJudge) 1
                         1601
                                 1601
Residuals
                    44
                         2191
                                   50
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
> df2 = aov2["Residuals", "Df"]
> df2 # Spock and others
[1] 44
> ss2 = aov2["Residuals", "Sum Sq"]
> ss2 # Spock and others
```

```
[1] 2191
> Fstat = ((ss2 - ss1)/(df2 - numdf1))/(ss1/numdf1)
> Fstat
[1] 1.366
> 1 - pf(Fstat, length(levels(case0502$Judge)) - 2, numdf1)
[1] 0.2582
```

We can also compare the two models using ANOVA (Display 5.12, page 130).

There are some other ways to compare whether the other judges differ from Dr. Spock's judge in their female composition using contrasts.

```
> # test all of the other judges vs. Spock's judge using a contrast page 118
> fit.contrast(lm(Percent ~ Judge, data = case0502), "Judge", c(-6, 1, 1, 1, 1,
    1, 1), conf.int = 0.95)
                          Estimate Std. Error t value Pr(>|t|) lower CI
                                     15.85 5.67 1.489e-06 57.81
Judge c=( -6 1 1 1 1 1 1 )
                            89.87
                          upper CI
Judge c=( -6 1 1 1 1 1 1 )
                             121.9
> # calculate the 95% confidence interval for Dr. Spock's jury female
> # composition page 118
> estimable(lm(Percent ~ Judge, data = case0502), c(1, 0, 0, 0, 0, 0, 0), conf.int = 0.95)
               Estimate Std. Error t value DF Pr(>|t|) Lower.CI Upper.CI
(1 \ 0 \ 0 \ 0 \ 0 \ 0) 14.62
                             2.305 6.344 39 1.722e-07 9.96 19.28
```

#### 3.3.1 Kruskal-Wallis Nonparametric Analysis of Variance

For the results of the Kruskal-Wallis test on page 136 we can use the following code:

```
> kruskal.test(Percent ~ Judge, data = case0502)

Kruskal-Wallis rank sum test

data: Percent by Judge
Kruskal-Wallis chi-squared = 21.96, df = 6, p-value = 0.001229
```