Distributional Semantic Models

Part 3: Evaluation of distributional similarity

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What is semantic similarity? Semantic similarity and relatedness

Outline

What is semantic similarity?

Semantic similarity and relatedness

Attributional similarity & quantitative evaluation

An example (Bullinaria & Levy 2007, 2012)

Methodology for DSM Evaluation

Outline

What is semantic similarity?

Semantic similarity and relatedness Attributional similarity & quantitative evaluation

Parameter evaluation

Evaluation strategies An example (Bullinaria & Levy 2007, 2012)

A large scale evaluation study

Tasks & parameters Methodology for DSM Evaluation **Evaluation on Standard Tasks** Summary & conclusion

What is semantic similarity? Semantic similarity and relatedness

Distributional similarity as semantic similarity

- ▶ DSMs interpret semantic similarity as a quantitative notion
 - ▶ if **a** is closer to **b** than to **c** in the distributional vector space, then a is more semantically similar to b than to c

rhino	fall	rock
woodpecker	rise	lava
rhinoceros	increase	sand
swan	fluctuation	boulder
whale	drop	ice
ivory	decrease	jazz
plover	reduction	slab
elephant	logarithm	cliff
bear	decline	pop
satin	cut	basalt
sweatshirt	hike	crevice

What is semantic similarity? Semantic similarity and relatedness

What is semantic similarity? Semantic similarity and relatedness

Types of semantic relations in DSMs

Nearest DSM neighbors have different types of semantic relations.

car (BNC, L2/R2 span)

- ▶ van co-hyponym
- vehicle hyperonym
- ► truck co-hyponym
- motorcycle co-hyponym
- driver related entity
- motor part
- ► lorry co-hyponym
- motorist related entity
- cavalier hyponym
- bike co-hyponym

car (BNC, L30/R30 span)

- drive function
- park typical action
- bonnet part
- windscreen part
- hatchback part
- headlight part
- ▶ jaguar hyponym
- garage location
- cavalier hyponym
- tyre part

http://clic.cimec.unitn.it/infomap-query/

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Manual analysis of semantic relations

for 44 concrete English nouns (Baroni and Lenci 2008)

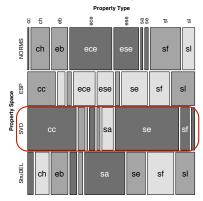


Figure 1: Distribution of property types across property spaces.

Taxonomic category:

- cc (co-)hyponym
- ch hypernym

Properties of entity:

- eb typical behaviour
- ece external component
- ese surface property

Situationally associated:

- sa action
- se other entity
- sf function

Attributional similarity & quantitative evaluation

sl location

Distribution of semantic relations among DSM neighbours (SVD), pattern collocations (StruDEL) and human-generated properties (NORMS).

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What is semantic similarity? Semantic similarity and relatedness

Semantic similarity and relatedness

- ► Attributional similarity two words sharing a large number of salient features (attributes)
 - synonymy (car/automobile)
 - hyperonymy (car/vehicle)
 - co-hyponymy (car/van/truck)
- Semantic relatedness (Budanitsky and Hirst 2006) two words semantically associated without necessarily being similar
 - ► function (*car/drive*)
 - meronymy (car/tyre)
 - ▶ location (*car/road*)
 - ► attribute (car/fast)
- ► Relational similarity (Turney 2006) similar relation between pairs of words (analogy)

policeman: gun :: teacher: book mason: stone :: carpenter: wood traffic: street :: water: riverbed

Outline

What is semantic similarity?

Attributional similarity & quantitative evaluation

Methodology for DSM Evaluation

What is semantic similarity? Attributional similarity & quantitative evaluation

What is semantic similarity? Attributional similarity & quantitative evaluation

DSMs and semantic similarity

- ▶ DSMs are thought to represent paradigmatic similarity
 - words that tend to occur in the same contexts
- ▶ Words that share many contexts will correspond to concepts that share many attributes (attributional similarity), i.e. concepts that are taxonomically/ontologically similar
 - synonyms (rhino/rhinoceros)
 - ▶ antonyms and values on a scale (good/bad)
 - co-hyponyms (rock/jazz)
 - hyper- and hyponyms (rock/basalt)
- ► Taxonomic similarity is seen as the fundamental semantic relation organising the vocabulary of a language, allowing categorization, generalization and inheritance

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What is semantic similarity? Attributional similarity & quantitative evaluation

Give it a try ...

- ► The wordspace package contains pre-compiled DSM vectors
 - based on a large Web corpus (9 billion words)
 - ▶ L4/R4 surface span, log-transformed G^2 , SVD dim. red.
 - ▶ targets = lemma + POS code (e.g. white J)
 - compatible with evaluation tasks included in package

```
library(wordspace)
```

```
M <- DSM Vectors
nearest.neighbours(M, "walk_V")
    amble V
               stroll V
                          traipse_V
                                       potter V
                                                    tramp_V
       19.4
                               21.8
                                                       22.9
                           trudge_V leisurely_R
  saunter_V
               wander_V
                                                  saunter_N
                               23.8
                   23.7
                                           26.2
                                                       26.4
# you can also try white, apple and kindness
```

Evaluation of attributional similarity

- ► Synonym identification
 - ► TOEFL test
- ► Modeling semantic similarity judgments
 - ► Rubenstein/Goodenough norms
 - ▶ WordSim-353
- ► Noun categorization
 - ► ESSLLI 2008 dataset
 - Almuhareb & Poesio dataset (AP)
 - **.** . . .
- Semantic priming
 - ► Hodgson dataset
 - Semantic Priming Project

Attributional similarity & quantitative evaluation

The TOEFL synonym task

- ▶ The TOEFL dataset (80 items)
 - ► Target: levied
 - Candidates: believed, correlated, imposed, requested
 - ► Target *fashion*

Candidates: craze, fathom, manner, ration

- DSMs and TOEFL
 - 1. take vectors of the target (t) and of the candidates ($\mathbf{c}_1 \dots \mathbf{c}_n$)
 - 2. measure the distance between **t** and \mathbf{c}_i , with $1 \le i \le n$
 - 3. select \mathbf{c}_i with the shortest distance in space from \mathbf{t}

ask your course instructor for non-public data package

- > library(wordspaceEval)
- > head(TOEFL80)

Attributional similarity & quantitative evaluation

Attributional similarity & quantitative evaluation

Humans vs. machines on the TOEFL task

► Average foreign test taker: 64.5%

► Macquarie University staff (Rapp 2004):

► Average of 5 non-natives: 86.75%

Average of 5 natives: 97.75%

Distributional semantics

Classic LSA (Landauer and Dumais 1997): 64.4%

▶ Padó and Lapata's (2007) dependency-based model: 73.0%

▶ Distributional memory (Baroni and Lenci 2010): 76.9%

▶ Rapp's (2004) SVD-based model, lemmatized BNC: 92.5%

▶ Bullinaria and Levy (2012) carry out aggressive parameter optimization: 100.0%

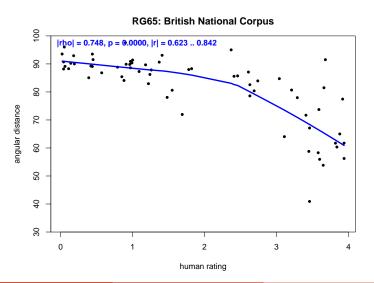
And you?

> eval.multiple.choice(TOEFL80, M)

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Attributional similarity & quantitative evaluation

Semantic similarity judgments: example



Semantic similarity judgments

▶ Rubenstein and Goodenough (1965) collected similarity ratings for 65 noun pairs from 51 subjects on a 0-4 scale

w_1	<i>W</i> ₂	avg. rating
car	automobile	3.9
food	fruit	2.7
cord	smile	0.0

- ▶ DSMs vs. Rubenstein & Goodenough
 - 1. for each test pair (w_1, w_2) , take vectors \mathbf{w}_1 and \mathbf{w}_2
 - 2. measure the distance (e.g. cosine) between \mathbf{w}_1 and \mathbf{w}_2
 - 3. measure (Pearson) correlation between vector distances and R&G average judgments (Padó and Lapata 2007)

```
> RG65[seq(0,65,5),]
```

> head(WordSim353) # extension of Rubenstein-Goodenough

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What is semantic similarity? Attributional similarity & quantitative evaluation

Semantic similarity judgments: results

Results on RG65 task:

- ▶ Padó and Lapata's (2007) dependency-based model: 0.62
- ▶ Dependency-based on Web corpus (Herdağdelen et al. 2009)
 - without SVD reduction: 0.69
 - ▶ with SVD reduction: 0.80
- ▶ Distributional memory (Baroni and Lenci 2010): 0.82
- ▶ Salient Semantic Analysis (Hassan and Mihalcea 2011): 0.86

And you?

```
> eval.similarity.correlation(RG65, M, convert=FALSE)
      rho p.value missing
                           r r.lower r.upper
                      RG65 0.687 2.61e-10
> plot(eval.similarity.correlation( # cosine similarity
      RG65, M, convert=FALSE, details=TRUE))
```

Noun categorization

- ▶ In categorization tasks, subjects are typically asked to assign experimental items - objects, images, words - to a given category or group items belonging to the same category
 - categorization requires an understanding of the relationship between the items in a category
- Categorization is a basic cognitive operation presupposed by further semantic tasks
 - ▶ inference
 - ★ if X is a CAR then X is a VEHICLE
 - compositionality
 - * $\lambda y : \mathsf{FOOD} \ \lambda x : \mathsf{ANIMATE} \ [\mathsf{eat}(x,y)]$
- ▶ "Chicken-and-egg" problem for relationship of categorization and similarity (cf. Goodman 1972, Medin et al. 1993)

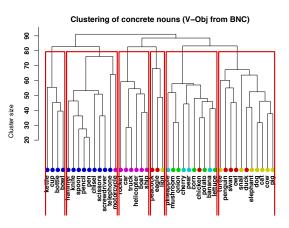
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What is semantic similarity? Attributional similarity & quantitative evaluation

Noun categorization: example



- ▶ majority labels: tools, tools, vehicles, birds, greens, animals
- correct: 4/4, 9/10, 6/6, 2/3, 5/10, 7/11
- ightharpoonup purity = 33 correct out of 44 = 75.0%

Noun categorization: the ESSLLI 2008 dataset

Dataset of 44 concrete nouns (ESSLLI 2008 Shared Task)

- ▶ 24 natural entities
 - ▶ 15 animals: 7 birds (eagle), 8 ground animals (lion)
 - ▶ 9 plants: 4 fruits (banana), 5 greens (onion)
- ▶ 20 artifacts
 - ▶ 13 tools (hammer), 7 vehicles (car)
- ▶ DSMs operationalize categorization as a clustering task
 - 1. for each noun w_i in the dataset, take its vector \mathbf{w}_i
 - 2. use a clustering method to group similar vectors \mathbf{w}_i
 - 3. evaluate whether clusters correspond to gold-standard semantic classes (purity, entropy, ...)

> ESSLLIO8_Nouns[seq(1,40,5),]

Attributional similarity & quantitative evaluation

ESSLLI 2008 shared task

- Clustering experiments with CLUTO (Karypis 2003)
 - repeated bisection algorithm
 - ▶ 6-way (birds, ground animals, fruits, greens, tools and vehicles), 3-way (animals, plants and artifacts) and 2-way (natural and artificial entities) clusterings
- ► Quantitative evaluation
 - entropy whether words from different classes are represented in the same cluster (best = 0)
 - purity degree to which a cluster contains words from one class only (best = 1)
 - global score across the three clustering experiments

$$\sum_{i=1}^{3} \mathsf{Purity}_{i} - \sum_{i=1}^{3} \mathsf{Entropy}_{i}$$

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Attributional similarity & quantitative evaluation

ESSLLI 2008 shared task

model	6-way		3-way		2-way		global
	Р	E	Р	Ε	P	E	
Katrenko	89	13	100	0	80	59	197
Peirsman+	82	23	84	34	86	55	140
dep-typed (DM)	77	24	79	38	59	97	56
dep-filtered (DM)	80	28	75	51	61	95	42
window (DM)	75	27	68	51	68	89	44
Peirsman-	73	28	71	54	61	96	27
Shaoul	41	77	52	84	55	93	-106

Katrenko, Peirsman+/-, Shaoul: ESSLLI 2008 Shared Task DM: Baroni & Lenci (2009)

And you?

> eval.clustering(ESSLLI08_Nouns, M) # uses PAM clustering

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Attributional similarity & quantitative evaluation

Simulating semantic priming

McDonald and Brew (2004); Padó and Lapata (2007)

- DSMs and semantic priming
 - 1. for each related prime-target pair, measure cosine-based similarity between items (e.g., to dread / to fear)
 - 2. to estimate unrelated primes, take average of cosine-based similarity of target with other primes from same semantic relation (e.g., to value / to fear)
 - 3. similarity between related items should be significantly higher than average similarity between unrelated items
- ▶ Significant effects (p < .01) for all semantic relations
 - strongest effects for synonyms, antonyms & coordinates
- ► Alternative: classification task
 - ▶ given target and two primes, identify related prime (→ multiple choice like TOEFL)

Semantic priming

- ▶ Hearing/reading a "related" prime facilitates access to a target in various psycholing, tasks (naming, lexical decision, reading)
 - ▶ the word *pear* is recognized faster if heard/read after *apple*
- ▶ Hodgson (1991) single word lexical decision task, 136 prime-target pairs (cf. Padó and Lapata 2007)
 - similar amounts of priming found for different semantic relations between primes and targets (≈ 23 pairs per relation)
 - ★ synonyms (synonym): to dread/to fear
 - ★ antonyms (antonym): short/tall
 - ★ coordinates (coord): train/truck
 - ★ super- and subordinate pairs (supersub): container/bottle
 - ★ free association pairs (freeass): dove/peace
 - ★ phrasal associates (phrasacc): vacant/building

Parameter evaluation

Evaluation strategies

Outline

Parameter evaluation

Evaluation strategies

Methodology for DSM Evaluation

An example (Bullinaria & Levy 2007, 2012)

DSM evaluation in published studies

- ▶ One model, many tasks (Padó and Lapata 2007; Baroni and Lenci 2010; Pennington et al. 2014)
 - ► A novel DSM is proposed, with specific features & parameters
 - ▶ This DSM is tested on a range of different tasks (e.g. TOEFL, priming, semantic clustering)
- ▶ Incremental tuning of parameters (Bullinaria and Levy 2007, 2012; Kiela and Clark 2014; Polajnar and Clark 2014)
 - ▶ Several parameters (e.g., scoring measure, distance metric, dimensionality reduction)
 - Many tasks (e.g. TOEFL, semantic & syntactic clustering)
 - Varying granularity of parameter settings
 - One parameter (sometimes two) varied at a time, with all other parameters set to fixed values or optimized for each setting
 - Optimal parameter values are determined sequentially

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Parameter evaluation An example (Bullinaria & Levy 2007, 2012)

Bullinaria & Levy (2007, 2012)

- ▶ One of the first systematic evaluation studies
- ► Test influence of many standard parameter settings
 - ▶ frequency weighting + distance measure
 - co-occurrence window, structured vs. unstructured
 - ▶ corpus type & size, number of feature dimensions
 - dimensionality reduction (SVD), number of latent dimension
- ▶ In four different evaluation tasks
 - ► TOEFL
 - ▶ distance comparison: related word vs. 10 random words
 - semantic categorization: nearest-centroid classifier
 - syntactic categorization (2007)
 - semantic clustering of nouns (2012)
- Novel parameters
 - skipping of first latent dimensions (with highest variance)
 - ► Caron's (2001) *P*: power-scaling of singular values

Outline

Parameter evaluation

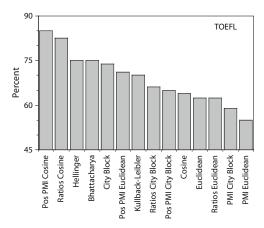
An example (Bullinaria & Levy 2007, 2012)

Methodology for DSM Evaluation

An example (Bullinaria & Levy 2007, 2012)

TOEFL results: feature weighting & distance measure

(Bullinaria and Levy 2007, p. 516, Fig. 1)



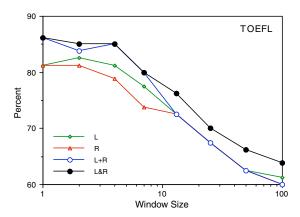
British National Corpus (BNC). Vectors not L2-normalized (frequency is L1-normalized). All other parameters optimized for each setting.

Parameter evaluation An example (Bullinaria & Levy 2007, 2012)

An example (Bullinaria & Levy 2007, 2012)

TOEFL results: size & type of co-occurrence window

(Bullinaria and Levy 2012, p. 893, Fig. 1)



ukWaC Web corpus. Positive PMI + cosine (Bullinaria and Levy 2007). Number of feature dimensions optimized for each window size & task. No dimensionality reduction. L&R = structured surface context (left/right).

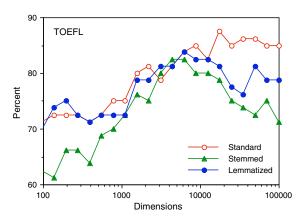
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Parameter evaluation An example (Bullinaria & Levy 2007, 2012)

TOEFL results: feature dimensions & pre-processing

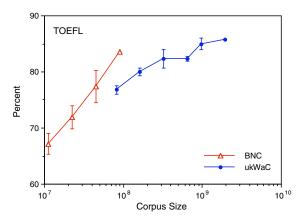
(Bullinaria and Levy 2012, p. 895, Fig. 4)



ukWaC corpus. L+R context of size 1. Other parameters presumably as above.

TOEFL results: corpus type & size

(Bullinaria and Levy 2012, p. 894, Fig. 2)

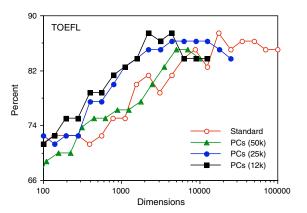


L+R context of size 1. Average + standard error over equally-sized corpus slices. Other parameter settings unclear.

Parameter evaluation An example (Bullinaria & Levy 2007, 2012)

TOEFL results: dimensionality reduction

(Bullinaria and Levy 2012, p. 898, Fig. 5)



ukWaC corpus. Positive PMI + cosine. Standard = no dimensionality reduction. Other: number of latent dimensions for 12k, 25k and 50k original feature dimensions.

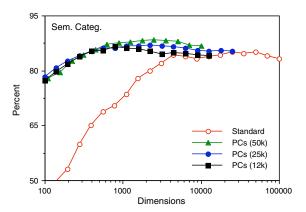
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Parameter evaluation An example (Bullinaria & Levy 2007, 2012)

Semantic categorization: dimensionality reduction

(Bullinaria and Levy 2012, p. 898, Fig. 5)



ukWaC corpus. Positive PMI + cosine. Standard = no dimensionality reduction. Other: number of latent dimensions for 12k, 25k and 50k original feature dimensions.

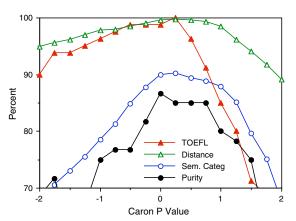
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Parameter evaluation An example (Bullinaria & Levy 2007, 2012)

TOEFL results: power scaling (Caron's P)

(Bullinaria and Levy 2012, p. 900, Fig. 7)

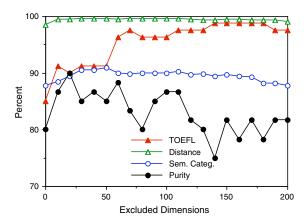


ukWaC corpus with standard settings. 50k feature dimensions reduced to 5000 latent dimensions. Neutral value is P = 1.

Parameter evaluation An example (Bullinaria & Levy 2007, 2012)

Combined results: skipping first latent dimensions

(Bullinaria and Levy 2012, p. 900, Fig. 7)



ukWaC corpus with standard settings. 50k feature dimensions reduced to 5000 latent dimensions.

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A (very) large-scale evaluation study

(Lapesa and Evert 2014)

Outline

An example (Bullinaria & Levy 2007, 2012)

A large scale evaluation study

Tasks & parameters

Methodology for DSM Evaluation

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A large scale evaluation study Tasks & parameters

Distributional models: general features

- ► Term-term distributional semantic models (bag-of-words)
- Target terms (rows)
 - vocabulary from Distributional Memory (Baroni and Lenci 2010) + terms from evaluation datasets
 - ▶ 27522 lemma types
- Feature terms (columns)
 - filtered by part-of-speech (nouns, verbs, adjectives, adverbs)
 - further context selection determined by two model parameters

Distributional models were compiled and evaluated using the IMS Corpus Workbench¹, the UCS toolkit² and the wordspace package for R.

Tasks

1. Classification

► TOEFL80: multiple-choice classification task (Landauer and Dumais 1997)

2. Correlation to Similarity Ratings

- ▶ RG65: 65 noun pairs (Rubenstein and Goodenough 1965)
- ▶ WordSim353: 351 noun pairs (Finkelstein *et al.* 2002)

3. Semantic Clustering

- ▶ Battig82: 82 nouns, 10 classes (Van Overschelde et al. 2004)
- ► AP402: 402 nouns, 21 classes (Almuhareb 2006)
- ► ESSLLI08 Nouns: 44 nouns, 6 classes
- ▶ Mitchell: 60 nouns, 12 classes (Mitchell et al. 2008)

A large scale evaluation study Tasks & parameters

Evaluated parameters

Building the co-occurrence matrix

1. Source corpus: BNC, Wackypedia, UkWac

Our source corpora – standard choices in distributional semantics – differ in both size and quality. Is there a quantity/quality trade-off?

- 2. Window (= surface span)
 - ▶ **Direction**: directed (= structured), undirected
 - ► Size: 1, 2, 4, 8, 16 words

We expect those parameters to be crucial as they determine the granularity (direction) and amount (size) of shared context involved in the computation of similarity.

¹http://cwb.sf.net/

Tasks & parameters

Tasks & parameters

Evaluated parameters

Selecting dimensions from the co-occurrence matrix

3. Feature selection:

- ► Criterion: frequency, number of non-zero entries
- ▶ **Threshold**: top *n* dimensions (n = 5000, 10000, 20000,50000, 100000)

How many context dimensions (words) are needed for DSMs to perform well in specific tasks? Are too many context dimensions detrimental? What is the best selection criterion?

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Evaluated parameters

Weighting and scaling co-occurrence counts

4. **Feature scoring**: frequency, simple-II, MI, Dice, t-score, z-score, tf.idf

Association measures represent an interpretation of co-occurrence frequency, and they emphasize different types of collocations (Evert 2008). Does this have an effect on DSM performance?

5. Transformation: none, logarithmic, square root, sigmoid

Transformations reduce the skewness of feature scores.

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A large scale evaluation study

Tasks & parameters

Evaluated parameters

Dimensionality reduction

- 6. **Dimensionality reduction** with randomized SVD:
 - number of reduced dimensions: 100, 300, 500, 700, 900
 - ▶ number of skipped dimensions: 0, 50, 100

Dimensionality reduction is expected to improve semantic representation and make computations more efficient. How does SVD interact with the other parameters? Bullinaria and Levy (2012) report improvements in some tasks (e.g. TOEFL) when the first latent dimensions (with highest variance) are discarded. Does this result generalize to our tasks/datasets?

Tasks & parameters

Evaluated parameters

Computation and usage of distances

7. **Distance metric**: cosine (angular distance), manhattan

Both are symmetric, while cognitive processes are often asymmetric

- 8. Index of distributional relatedness
 - distance: dist(a, b)
 - neighbor rank, calculated differently for different tasks:
 - ★ TOEFL: backward rank, i.e. rank(b, a)
 - * Ratings and Clustering: average of logarithmic forward and backward rank, i.e. $(\log rank(a, b) + \log rank(b, a))/2$

This parameter allows us to account for asymmetries: rank(b, a) is different from rank(a, b). While cognitively plausible, neighbor rank is computationally expensive: does it improve the performance of DSMs?

Methodology for DSM Evaluation

A large scale evaluation study Methodology for DSM Evaluation

Outline

An example (Bullinaria & Levy 2007, 2012)

A large scale evaluation study

Methodology for DSM Evaluation

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How many models did we end up with?

... and how do we make sense of all those results?

- ▶ We tested all the possible parameter combinations (we will see later that this is crucial for our evaluation methodology)
- ▶ 537600 model runs (33600 in the unreduced setting, 504000 in the reduced setting)
- ▶ The models were generated and evaluated on a large HPC cluster at FAU Erlangen-Nürnberg as well as servers at the University of Stuttgart, within approximately 5 weeks

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A large scale evaluation study Methodology for DSM Evaluation

Evaluation methodology: linear regression

Our proposal for a robust evaluation of DSM parameters

- ▶ Attempts to predict the values of a "dependent" variable from one or more "independent" variables and their combinations
- ▶ Is used to understand which independent variables are closely related to the dependent variable, and to explore the forms of these relationships

Example

Dependent variable: income

Independent variables: gender, age, ethnicity, education level, first letter of the surname (hopefully not significant)

A large scale evaluation study Methodology for DSM Evaluation

Evaluation methodology: linear regression

Our proposal for a robust evaluation of DSM parameters

We use linear models to analyze the influence of different DSM parameters and their combinations on DSM performance

- dependent variable = performance (accuracy, correlation coefficient, purity)
- ▶ independent variables = model parameters (e.g., source corpus, window size, window direction)

We want to understand which of the parameters are related to the dependent variable, i.e., we want to find the parameters whose manipulation has the strongest effect on DSM performance.

A large scale evaluation study Methodology for DSM Evaluation

A large scale evaluation study Methodology for DSM Evaluation

DSM evaluation and linear regression

Toy example: a $2 \times 2 \times 2$ design

Corpus	Window size	Window direction	Accuracy
ukWaC	1	directed	88
ukWaC	16	undirected	92
ukWaC	1	directed	91
ukWaC	16	undirected	93
BNC	1	undirected	80
BNC	16	undirected	53
BNC	1	directed	72
BNC	16	directed	71

$$\begin{split} \textit{Accuracy} &= \beta_0 + \beta_1(\mathsf{corpus}) + \beta_2(\mathsf{window\ size}) + \beta_3(\mathsf{window\ direction}) \\ &+ \beta_4(\mathsf{corpus}:\ \mathsf{window\ size}) + \beta_5(\mathsf{corpus}:\ \mathsf{window\ direction}) + \\ &+ \beta_6(\mathsf{window\ size}:\ \mathsf{window\ direction}) + \epsilon \end{split}$$

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A large scale evaluation study Methodology for DSM Evaluation

DSM evaluation and linear regression

Analysis of variance: feature ablation

Feature ablation

Proportion of variance explained by a parameter together with all its interactions, corresponding to the reduction in R^2 of the linear model fit if this parameter is left out.

In our toy model with 3 parameters and all two-way interactions:

- Ablation(corpus) = R^2 (corpus) + R^2 (corpus: window size) + R^2 (corpus: window direction)
- Ablation(window size) = R^2 (window size) + R^2 (corpus: window size) + R^2 (window size: window direction)
- ▶ Ablation(window direction) = R^2 (window direction) + R^2 (corpus: window direction) + R^2 (window size: window direction)

DSM evaluation and linear regression

Analysis of variance

Goal: quantify the impact of a specific parameter (or interaction) on DSM performance, in terms of the proportion of variance explained by the parameter

Key notions:

- $ightharpoonup R^2$ (R squared)
 - proportion of explained variance, i.e.

$$1 - \frac{\text{residual variance of } \epsilon}{\text{variance of dependent variable}}$$

- ► calculated (i) for the full model (→ how well the model exlains the experimental results) as well as (ii) for specific parameters and interactions (quantifying how much they contribute to predictions)
- ► Feature ablation

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Evaluation on Standard Tasks

Outline

A large scale evaluation study

Methodology for DSM Evaluation

Evaluation on Standard Tasks

^{*}we're aware that this regression model is almost saturated ...

TOEFL multiple-choice classification task

Introducing the task

A collection of 80 multiple-choice questions from a synonym task in the Test Of English as a Foreign Language (TOEFL)

TOFFI dataset

Target: consume - Choices: breed, catch, eat, supply

Target: constant - Choices: accidental, continuing, instant, rapid Target: concise - Choices: free, positive, powerful, succinct

- ► A classification task
- ▶ If DSMs capture synonymy relations, we expect that the distance between the target and the correct choice will be smaller than to the wrong choices
- ► Performance: % accuracy

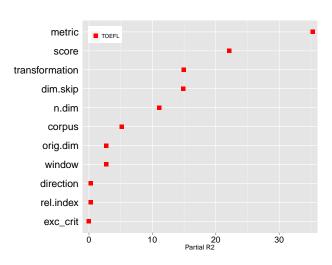
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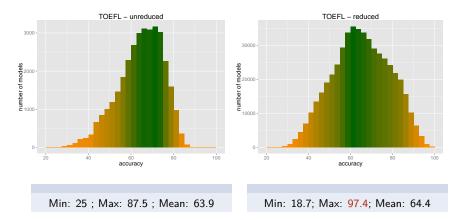
TOEFL task: parameters and explained variance

Reduced setting: feature Ablation (model R^2 : 89%)



TOEFL task: performance

Unreduced versus Reduced Experiments



Evaluation on Standard Tasks

TOEFL task: interactions

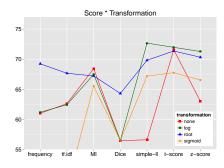
Reduced setting ($R^2 > 0.5$)

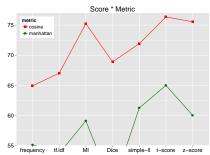
Interaction	Df	R^2
score:transformation	18	7.42
metric:dim.skip	2	4.44
score:metric	6	1.77
metric:orig.dim	4	0.98
window:transformation	12	0.91
corpus:score	12	0.84
score:orig.dim	24	0.64
metric:n.dim	4	0.63

TOEFL task: interactions, R^2

TOEFL task: Metric, Score, Transformation

Partial effect displays (Fox 2003)

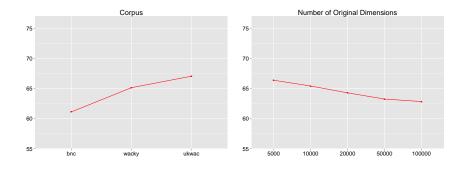




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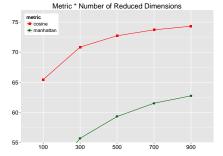
TOEFL task: Corpus and Number of Feature Dimensions

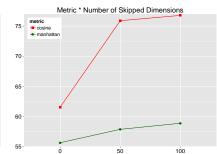
Partial effect displays (Fox 2003)



TOEFL task: Dimensionality Reduction

Partial effect displays (Fox 2003)

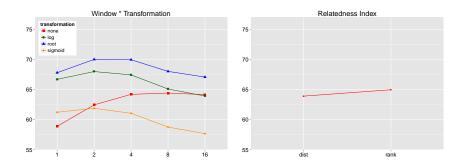




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TOEFL task: Window and Relatedness Index

Partial effect displays (Fox 2003)



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Evaluation on Standard Tasks

Evaluation on Standard Tasks

TOEFL task: summary

TOEFL: best setting

► Corpus: ukWac

▶ Window: undirected, 2 words

► Feature selection: top 5000/10000 dimensions, based on frequency

► Score * Transformation: simple-II * log

▶ Dimensionality Reduction: 900 latent dimensions, skipping the first 100

► Distance Metric: cosine

► Index of Distributional Relatedness: neighbor rank

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DSMs and similarity ratings

Introducing the task

RG65

65 pairs, rated from 0 to 4

gem - jewel: 3.94 grin - smile: 3.46 fruit - furnace: 0.05

WordSim353

353 pairs, rated from 1 to 10

announcement - news: 7.56 weapon – secret: 6.06 travel - activity: 5.00

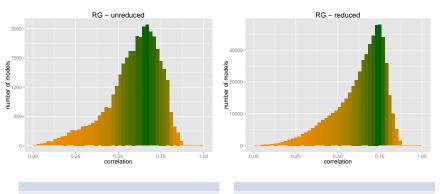
► A **prediction** task

▶ If distributional representation are close to speakers' conceptual representations, we expect to find some correlation between distance in the semantic space and speaker's judgments concerning semantic similarity

▶ Performance: **Pearson correlation** *r*

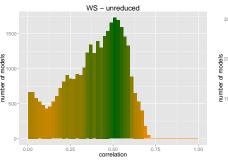
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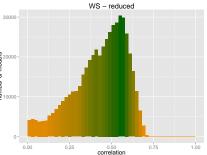
Similarity ratings: performance on RG65



Min: 0.00; Max: 0.89; Mean: 0.63 reduced

Similarity ratings: performance on WordSim353





Min: 0.00; Max: 0.73; Mean: 0.39

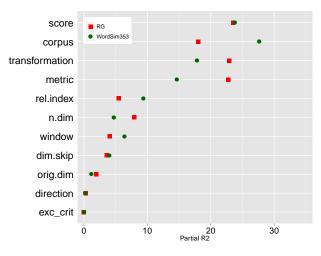
Min: 0.00; Max: 0.73; Mean: 0.43 reduced

unreduced

Min: 0.01; Max: 0.88; Mean 0.59 unreduced

Similarity ratings: parameters and explained variance

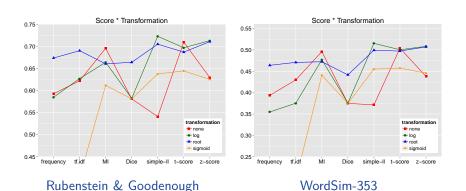
Reduced setting: feature ablation (full model R²: RG65 86%; WS353 90%)



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Similarity ratings: Score, Transformation

Partial effect displays (Fox 2003)



Similarity ratings: interactions

Reduced setting ($R^2 > 0.5$)

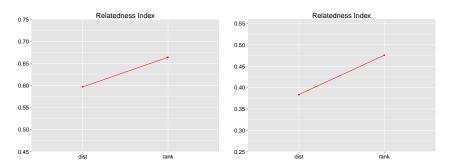
Interaction	Df	RG65	WordSim353
score:transf	18	10.28	8.66
metric:n.dim	4	2.18	1.42
window:transf	12	1.43	1.01
corpus:metric	2	1.83	0.51
score:metric	6	1.91	0.59
metric:orig.dim	4	1.08	0.62
corpus:score	12	0.77	0.82
window:score	24	0.77	0.69
score:dim.skip	12	0.58	0.85

Similarity ratings: interactions, R^2

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Similarity ratings: Relatedness Index

Partial effect displays (Fox 2003)



Rubenstein & Goodenough

WordSim-353

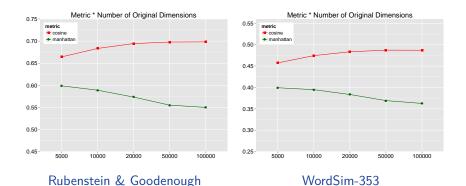
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Similarity ratings: Metric, Number of Feature Dimensions

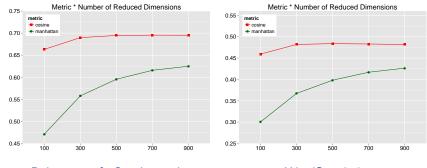
Partial effect displays (Fox 2003)



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Similarity ratings: Number of Latent Dimensions

Partial effect displays (Fox 2003)



Rubenstein & Goodenough

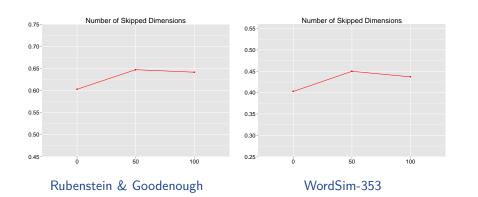
WordSim-353

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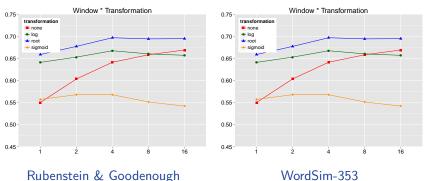
Similarity ratings: Number of Skipped Dimensions

Partial effect displays (Fox 2003)



Similarity ratings: Window Size, Transformation

Partial effect displays (Fox 2003)



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A large scale evaluation study

Evaluation on Standard Tasks

Summing up: Ratings

Ratings: best setting

Corpus: wacky

Window: undirected, 4 words

► Feature selection: top 20000/50000 dimensions, based on frequency

► Score * Transformation: simple-II * log

▶ Dimensionality Reduction: 300 latent dimensions, skipping the first 50

► Distance Metric: cosine

► Index of Distributional Relatedness: neighbor rank

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DSMs and semantic clustering

Introducing the task

- A categorization task
- ▶ If distributional representations approximate human conceptual representations, we expect word categorization based on distributional features to produce concept clusters similar to those in the gold standard datasets
- Performance: cluster purity
 - classification accuracy for optimal cluster labelling
 - percentage of nouns that belong to the majority category within their cluster
- ▶ Partitioning around medoids (Kaufman and Rousseeuw 1990)
 - implemented as pam() in R standard library
 - ▶ direct comparison → equal to or even better than CLUTO
 - works with arbitrary dissimilarity matrix

DSMs and semantic clustering

Introducing the task

Almuhareb & Poesio

402 nouns, 21 classes

 $day \Longrightarrow TIME$

 $kiwi \Longrightarrow FRUIT$

 $kitten \Longrightarrow ANIMAL$

 $volleyball \implies GAME$

ESSLLI categorization task

44 nouns, 6 classes

 $potato \Longrightarrow GREEN$

 $hammer \Longrightarrow TOOL$

 $car \Longrightarrow VEHICLE$

 $peacock \implies BIRD$

BATTIG set

82 nouns, 10 classes

 $chicken \Longrightarrow BIRD$

 $bear \Longrightarrow LAND_MAMMAL$

pot ⇒ KITCHENWARE

 $oak \Longrightarrow TREE$

MITCHELL set

60 nouns, 12 classes

ant \Longrightarrow INSECT

 $carrot \Longrightarrow VEGETABLE$

 $train \Longrightarrow VEHICLE$

 $cat \Longrightarrow ANIMAL$

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Semantic clustering: performance

Overview: unreduced versus reduced experiments

Dataset	l	Inreduc	ed	Reduced			
Dataset	Min	Max	Mean	Min	Max	Mean	
AP	0.15	0.73	0.56	0.13	0.76	0.54	
BATTIG	0.28	0.99	0.77	0.23	0.99	0.78	
ESSLLI	0.32	0.93	0.72	0.32	0.98	0.72	
MITCHELL	0.26	0.97	0.68	0.27	0.97	0.69	

Semantic clustering: summary of performance (purity)

Df

18

12

12

24

AΡ

7.10

2.22

3.29

2.25

2.00

2.36

0.56

0.74

2 1.42

Semantic clustering: interactions

Reduced setting ($R^2 > 0.5$)

Interaction

window:metric

metric:dim.skip

corpus:metric

corpus:window

score:dim.skip

window:score

metric:n.dim

score:transformation

window:transformation

BATTIG

7.95

1.26

3.16

1.54

2.95

2.91

1.18

1.15

0.77

ESSLLI

7.56

2.97

2.03

2.77

0.88

2.79

1.49

0.99

0.54

MITCHELL

11.42

2.72

0.58

0.86

2.66

1.11

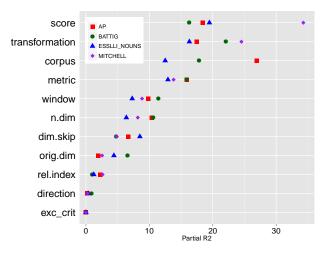
1.23

1.39

0.65

Semantic clustering: parameters and explained variance

Feature ablation (model R^2 – AP: 82%; BATTIG: 77%; ESSLLI 58%; MITCHELL 73%)



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Clustering datasets: interactions, R^2

A large scale evaluation study

Evaluation on Standard Tasks

Semantic clustering: Score, Transformation

Partial effect displays (Fox 2003)



Almuhareb & Poesio

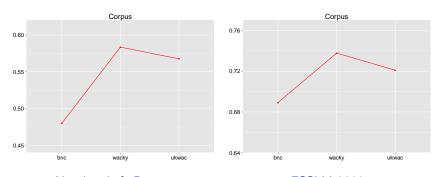


ESSLLI 2008

Evaluation on Standard Tasks

Semantic clustering: Corpus

Partial effect displays (Fox 2003)



Almuhareb & Poesio

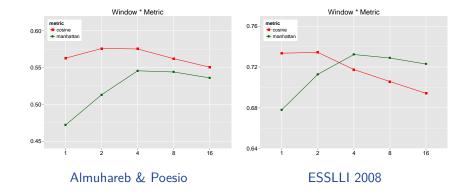
ESSLLI 2008

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Semantic clustering: Window Size, Metric

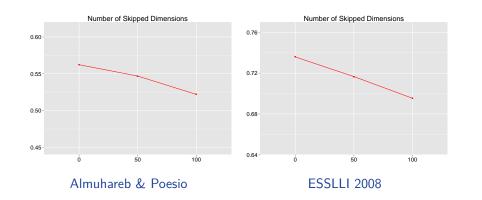
Partial effect displays (Fox 2003)



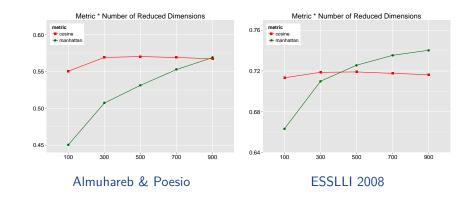
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Semantic clustering: Number of Skipped Dimensions

Partial effect displays (Fox 2003)



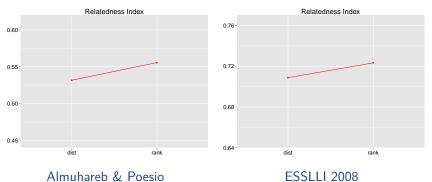
Semantic clustering: Metric, Number of Latent Dimensions Partial effect displays (Fox 2003)



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Semantic clustering: Relatedness Index

Partial effect displays (Fox 2003)



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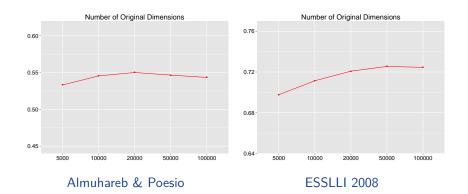
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Evaluation on Standard Tasks

Semantic clustering: Number of Feature Dimensions

Partial effect displays (Fox 2003)



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A large scale evaluation study

Summary & conclusion

Outline

Attributional similarity & quantitative evaluation

An example (Bullinaria & Levy 2007, 2012)

A large scale evaluation study

Methodology for DSM Evaluation

Summary & conclusion

Summing up: Semantic Clustering

Clustering: best setting

- ► Corpus: wacky
- ▶ Window: undirected, 4 words
- ► Feature selection: top 50000 dimensions, based on frequency
- ► Score * Transformation: simple-II * log (or t-score * log)
- ▶ Dimensionality Reduction: 300/500 latent dimensions, no skipping necessary
- ► Distance Metric: cosine
- ► Index of Distributional Relatedness: neighbor rank

A large scale evaluation study Summary & conclusion

Does our evaluation methodology work?

- 1. What are the most explanatory parameters?
- 2. By inspecting the effect plots, we identified best settings for every dataset: what is the performance of such best settings? Are they close to the best runs in the experiment?
- 3. Is it possible to identify a general best setting that performs reasonably well across all tasks?

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How about the index of distributional relatedness?

Summary: parameters

- ▶ Parameters with strong effect on DSM performance and homogeneous behavior across tasks and datasets
 - score
 - transformation
 - distance metric
- ▶ Parameters with strong effect on DSM performance, but differences across tasks
 - dimensionality reduction parameters
 - window
 - corpus (to a lesser extent)
- ▶ A less crucial parameter with homogeneous behavior
 - number of context dimensions
- ▶ Parameters that have no or little effect on DSM performance
 - criterion for context selection
 - direction of the context window

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60

A large scale evaluation study Summary & conclusion

BATTIG MITCHELL ESSLLI

A large scale evaluation study Summary & conclusion

Best settings and their performance

dataset	corpus	w	o.dim	SC	tr	m	rel.ind	n.dim	d.sk	best.s	best.m
TOEFL	ukwac	2	5k	s-II	log	cos	rank	900	100	92.5	98.75
WS	wacky	4	50k	s-II	log	cos	rank	300	50	0.67	0.73
RG	wacky	4	50k	s-II	log	cos	rank	300	50	0.86	0.89
AP	wacky	4	20k	s-II	log	cos	rank	300	0	0.69	0.76
BATTIG	wacky	8	50k	s-II	log	cos	rank	500	0	0.98	0.99
ESSLLI	wacky	2	20k	t-sc	log	cos	rank	300	0	0.77	0.98
MITCHELL	wacky	4	50k	s-II	log	cos	rank	500	0	0.88	0.97

Best settings for each dataset

w = window size, o.dim = number of feature dimensions, sc = scoring function, tr = transformation, m = metric, d.sk = number of skipped dimensions, best.s = performance of best setting for this dataset, best.m = performance of best run for this dataset

General settings

rel.index

TOEFL

task	corpus	w	o.dim	sc	tr.	m	rel.ind	n.dim	d.sk
TOEFL	ukwac	2	5k	s-II	log	cos	rank	900	100
Rating	wacky	4	50k	s-II	log	cos	rank	300	50
Clustering	wacky	4	50k	s-II	log	cos	rank	500	0
General	wacky	4	50k	s-II	log	cos	rank	500	50

General best settings

Task	TOEFL	RATINGS	CLUSTERING	GENERAL	SoA
TOEFL	92.5	85.0	75.0	90.0	100.0
RG	0.85	0.86	0.84	0.87	0.86
WS	0.60	0.67	0.64	0.68	0.81
AP402	0.60	0.66	0.67	0.67	0.79
BATTIG	0.85	0.91	0.98	0.90	0.96
ESSLLI	0.70	0.77	0.80	0.77	0.91
MITCHELL	0.73	0.83	0.88	0.83	0.94

General best settings - Performance

A large scale evaluation study

Summary & conclusion

A large scale evaluation study

Summary & conclusion

Conclusion

- ▶ Our results show that it is possible to find a single DSM configuration that performs relatively well on every task
- ► The most explanatory parameters show similar behavior across all tasks and datasets
 - ► Simple-II * Logarithmic Transformation
 - Cosine Distance
- Parameters that show variation determine the amount and nature of the shared context
 - ► Context window: 4 is a good compromise solution
 - ▶ Dimensionality reduction: skipping the first dimensions (but not too many) generally helps
 - Number of Feature Terms (to a lesser extent)

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Conclusion

- ▶ Among the source corpora, WaCkypedia appears to be a better option than UkWaC for all tasks but TOEFL
 - ► A good trade-off between quantity and quality?
- ▶ As an index of distributional relatedness, neighbor rank is always better than distance, even if its contribution to model performance varies across tasks
 - Perhaps some tasks/datasets are less asymmetric than others?
 - may need to exploit directionality in a more granular way

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Summary & conclusion

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07 / 09

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Summary & conclusion

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98 / 98