

# Distributional Semantic Models

## Part 2: The parameters of a DSM

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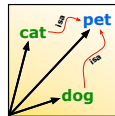
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<http://wordspace.collocations.de/doku.php/course:start>

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## Outline

### DSM parameters

A taxonomy of DSM parameters

Examples

### Building a DSM

Sparse matrices

Example: a verb-object DSM

## General definition of DSMs

A **distributional semantic model** (DSM) is a scaled and/or transformed co-occurrence matrix  $\mathbf{M}$ , such that each row  $\mathbf{x}$  represents the distribution of a target term across contexts.

|        | get    | see    | use    | hear   | eat    | kill   |
|--------|--------|--------|--------|--------|--------|--------|
| knife  | 0.027  | -0.024 | 0.206  | -0.022 | -0.044 | -0.042 |
| cat    | 0.031  | 0.143  | -0.243 | -0.015 | -0.009 | 0.131  |
| dog    | -0.026 | 0.021  | -0.212 | 0.064  | 0.013  | 0.014  |
| boat   | -0.022 | 0.009  | -0.044 | -0.040 | -0.074 | -0.042 |
| cup    | -0.014 | -0.173 | -0.249 | -0.099 | -0.119 | -0.042 |
| pig    | -0.069 | 0.094  | -0.158 | 0.000  | 0.094  | 0.265  |
| banana | 0.047  | -0.139 | -0.104 | -0.022 | 0.267  | -0.042 |

**Term** = word, lemma, phrase, morpheme, word pair, ...

## General definition of DSMs

Mathematical notation:

- ▶  $k \times n$  co-occurrence matrix  $\mathbf{M} \in \mathbb{R}^{k \times n}$  (example:  $7 \times 6$ )
  - ▶  $k$  rows = **target** terms
  - ▶  $n$  columns = **features** or **dimensions**

$$\mathbf{M} = \begin{bmatrix} m_{11} & m_{12} & \cdots & m_{1n} \\ m_{21} & m_{22} & \cdots & m_{2n} \\ \vdots & \vdots & & \vdots \\ m_{k1} & m_{k2} & \cdots & m_{kn} \end{bmatrix}$$

- ▶ distribution vector  $\mathbf{m}_i = i$ -th row of  $\mathbf{M}$ , e.g.  $\mathbf{m}_3 = \mathbf{m}_{\text{dog}} \in \mathbb{R}^n$
- ▶ components  $\mathbf{m}_i = (m_{i1}, m_{i2}, \dots, m_{in})$  = features of  $i$ -th term:

$$\begin{aligned} \mathbf{m}_3 &= (-0.026, 0.021, -0.212, 0.064, 0.013, 0.014) \\ &= (m_{31}, m_{32}, m_{33}, m_{34}, m_{35}, m_{36}) \end{aligned}$$

## Outline

### DSM parameters

A taxonomy of DSM parameters

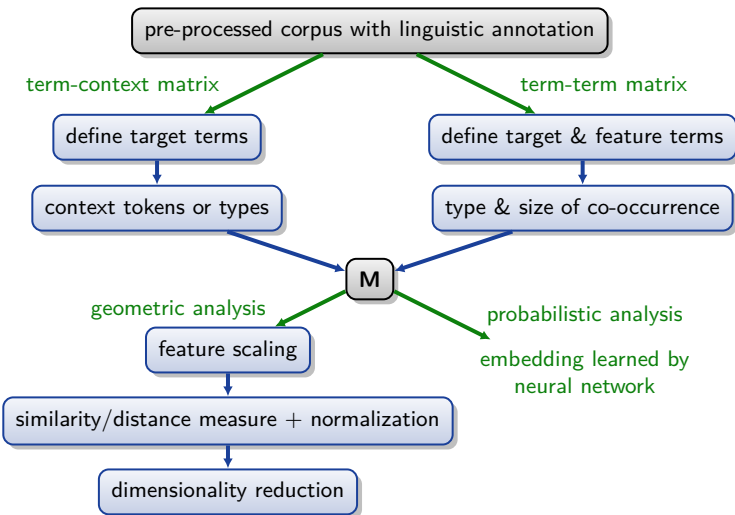
Examples

### Building a DSM

Sparse matrices

Example: a verb-object DSM

## Overview of DSM parameters



## Term-context matrix

**Term-context matrix** records frequency of term in each individual context (e.g. sentence, document, Web page, encyclopaedia article)

$$\mathbf{F} = \begin{bmatrix} \dots & \mathbf{f}_1 & \dots \\ \dots & \mathbf{f}_2 & \dots \\ & \vdots & \\ & \vdots & \\ \dots & \mathbf{f}_k & \dots \end{bmatrix}$$

|        | Felidae | Pet | Feral | Bloat | Philosophy | Kant | Back pain |
|--------|---------|-----|-------|-------|------------|------|-----------|
| cat    | 10      | 10  | 7     | –     | –          | –    | –         |
| dog    | –       | 10  | 4     | 11    | –          | –    | –         |
| animal | 2       | 15  | 10    | 2     | –          | –    | –         |
| time   | 1       | –   | –     | –     | 2          | 1    | –         |
| reason | –       | 1   | –     | –     | 1          | 4    | 1         |
| cause  | –       | –   | –     | 2     | 1          | 2    | 6         |
| effect | –       | –   | –     | 1     | –          | 1    | –         |

```
> TC <- DSM_TermContext
> head(TC, Inf) # extract full co-oc matrix from DSM object
```

## Term-term matrix

**Term-term matrix** records co-occurrence frequencies with feature terms for each target term

$$\mathbf{M} = \begin{bmatrix} \dots & \mathbf{m}_1 & \dots \\ \dots & \mathbf{m}_2 & \dots \\ & \vdots & \\ & \vdots & \\ \dots & \mathbf{m}_k & \dots \end{bmatrix}$$

|        | breed | tail | feed | kill | important | explain | likely |
|--------|-------|------|------|------|-----------|---------|--------|
| cat    | 83    | 17   | 7    | 37   | –         | 1       | –      |
| dog    | 561   | 13   | 30   | 60   | 1         | 2       | 4      |
| animal | 42    | 10   | 109  | 134  | 13        | 5       | 5      |
| time   | 19    | 9    | 29   | 117  | 81        | 34      | 109    |
| reason | 1     | –    | 2    | 14   | 68        | 140     | 47     |
| cause  | –     | 1    | –    | 4    | 55        | 34      | 55     |
| effect | –     | –    | 1    | 6    | 60        | 35      | 17     |

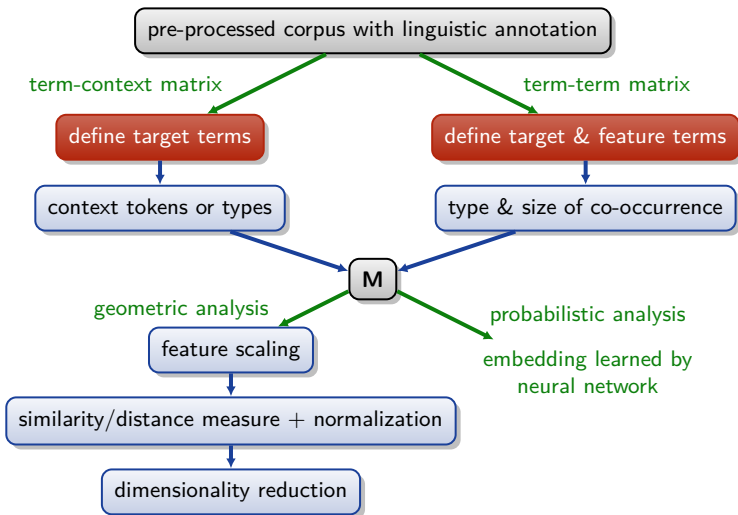
```
> TT <- DSM_TermTerm
> head(TT, Inf)
```

## Term-term matrix

Some footnotes:

- ▶ Often target terms  $\neq$  feature terms
  - ▶ e.g. nouns described by co-occurrences with verbs as features
  - ▶ identical sets of target & feature terms  $\rightarrow$  symmetric matrix
- ▶ Different types of co-occurrence (Evert 2008)
  - ▶ **surface context** (word or character window)
  - ▶ **textual context** (non-overlapping segments)
  - ▶ **syntactic context** (dependency relation)
- ▶ Can be seen as smoothing of term-context matrix
  - ▶ average over similar contexts (with same context terms)
  - ▶ data sparseness reduced, except for small windows
  - ▶ we will take a closer look at the relation between term-context and term-term models in part 5 of this tutorial

## Overview of DSM parameters



## Definition of target and feature terms

- ▶ Choice of linguistic unit
  - ▶ words
  - ▶ bigrams, trigrams, ...
  - ▶ multiword units, named entities, phrases, ...
  - ▶ morphemes
  - ▶ word pairs (e.g. analogy tasks)
- ▶ Linguistic annotation
  - ▶ word forms (minimally requires tokenisation)
  - ▶ often lemmatisation or stemming to reduce data sparseness: *go, goes, went, gone, going*  $\rightarrow$  *go*
  - ▶ POS disambiguation (*light*/N vs. *light*/A vs. *light*/V)
  - ▶ word sense disambiguation (*bank*<sub>river</sub> vs. *bank*<sub>finance</sub>)
  - ▶ abstraction: POS tags (or bigrams) as feature terms
- ▶ Trade-off between deeper linguistic analysis and
  - ▶ need for language-specific resources
  - ▶ possible errors introduced at each stage of the analysis

## Effects of linguistic annotation

Nearest neighbours of *walk* (BNC)

### word forms

- ▶ stroll
- ▶ walking
- ▶ walked
- ▶ go
- ▶ path
- ▶ drive
- ▶ ride
- ▶ wander
- ▶ sprinted
- ▶ sauntered

### lemmatised + POS

- ▶ hurry
- ▶ stroll
- ▶ stride
- ▶ trudge
- ▶ amble
- ▶ wander
- ▶ walk (noun)
- ▶ walking
- ▶ retrace
- ▶ scuttle

<http://clic.cimec.unitn.it/infomap-query/>

1. All models built with Infomap NLP: 2-word window, 20k targets, 2k features, 300 latent dims
2. Lemmatised model uses BNC lemma annotation (with POS category)



## Effects of linguistic annotation

Nearest neighbours of *arrivare* (Repubblica)

| word forms       | lemmatised + POS |
|------------------|------------------|
| ▶ giungere       | ▶ giungere       |
| ▶ raggiungere    | ▶ aspettare      |
| ▶ arrivi         | ▶ attendere      |
| ▶ raggiungimento | ▶ arrivo (noun)  |
| ▶ raggiunto      | ▶ ricevere       |
| ▶ trovare        | ▶ accontentare   |
| ▶ raggiunge      | ▶ approdare      |
| ▶ arrivasse      | ▶ pervenire      |
| ▶ arriverà       | ▶ venire         |
| ▶ concludere     | ▶ piombare       |

<http://clic.cimec.unitn.it/infomap-query/>

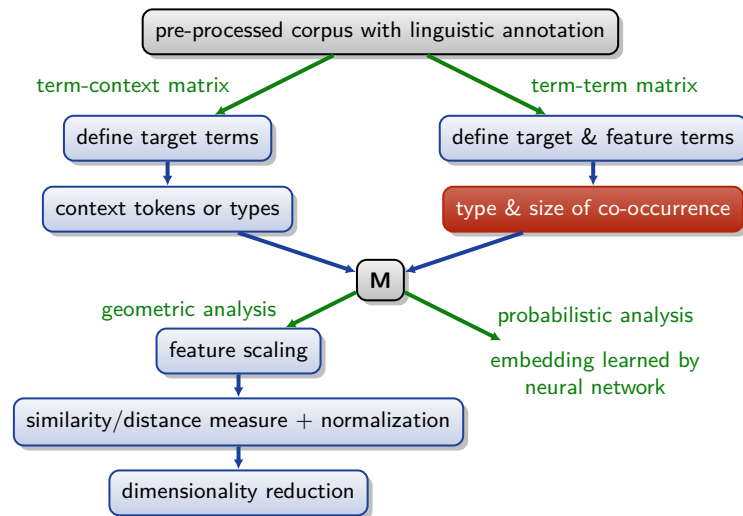
1. Colours seem to indicate inflected forms belonging to the same lemma.
2. Based on La Repubblica SSLMiT corpus
3. Lemmatised model includes two-letter POS codes



## Selection of target and feature terms

- ▶ Full-vocabulary models are often unmanageable
  - ▶ 762,424 distinct word forms in BNC, 605,910 lemmata
  - ▶ large Web corpora have > 10 million distinct word forms
  - ▶ low-frequency targets (and features) are not reliable (“noisy”)
- ▶ Frequency-based selection
  - ▶ minimum corpus frequency:  $f \geq F_{\min}$
  - ▶ or accept  $n_w$  most frequent terms
  - ▶ sometimes also upper threshold:  $F_{\min} \leq f \leq F_{\max}$
- ▶ Relevance-based selection
  - ▶ criterion from IR: document frequency  $df$
  - ▶ high  $df \rightarrow$  uninformative / low  $df \rightarrow$  too sparse to be useful
  - ▶ alternatives: entropy  $H$  or chi-squared statistic  $\chi^2$
- ▶ Other criteria
  - ▶ POS-based filter: no function words, only verbs, nouns, ...
  - ▶ general dictionary, words required for particular task, ...

## Overview of DSM parameters



## Surface context

Context term occurs **within a span of  $k$  words** around target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners. [L3/R3 span,  $k = 6$ ]

Parameters:

- ▶ span size (in words or characters)
- ▶ symmetric *vs.* one-sided span
- ▶ uniform or “triangular” (distance-based) weighting (don't!)
- ▶ spans clamped to sentences or other textual units?

## Effect of span size

Nearest neighbours of *dog* (BNC)

| 2-word span | 30-word span |
|-------------|--------------|
| ▶ cat       | ▶ kennel     |
| ▶ horse     | ▶ puppy      |
| ▶ fox       | ▶ pet        |
| ▶ pet       | ▶ bitch      |
| ▶ rabbit    | ▶ terrier    |
| ▶ pig       | ▶ rottweiler |
| ▶ animal    | ▶ canine     |
| ▶ mongrel   | ▶ cat        |
| ▶ sheep     | ▶ to bark    |
| ▶ pigeon    | ▶ Alsatian   |

<http://clie.cimec.unitn.it/infomap-query/>

## Textual context

Context term is in the **same linguistic unit** as target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

- ▶ type of linguistic unit
  - ▶ sentence
  - ▶ paragraph
  - ▶ turn in a conversation
  - ▶ Web page
  - ▶ tweet

## Syntactic context

Context term is linked to target by a **syntactic dependency** (e.g. subject, modifier, ...).

The **silhouette** of the **sun** beyond a wide-open **bay** on the lake; the **sun** still **glitters** although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

- ▶ types of syntactic dependency (Padó and Lapata 2007)
- ▶ direct *vs.* indirect dependency paths
- ▶ homogeneous data (e.g. only verb-object) *vs.* heterogeneous data (e.g. all children and parents of the verb)
- ▶ maximal length of dependency path

## Comparison of co-occurrence contexts

Contexts range from general/**implicit** to specific/**explicit**:

|                                | features are                    |
|--------------------------------|---------------------------------|
| textual / large span           | from same general domain        |
| small span                     | collocations                    |
| syntactic<br>(single relation) | attributes<br>(focus on aspect) |
| knowledge pattern              | properties                      |

## “Knowledge pattern” context

Context term is linked to target by a **lexico-syntactic pattern** (text mining, cf. Hearst 1992, Pantel & Pennacchiotti 2008, etc.).

In Provence, Van Gogh painted with bright **colors** such as **red** and **yellow**. These **colors** produce incredible **effects** on anybody looking at his paintings.

Parameters:

- ▶ inventory of lexical patterns
  - ▶ lots of research to identify semantically interesting patterns (cf. Almuhareb & Poesio 2004, Veale & Hao 2008, etc.)
- ▶ fixed *vs.* flexible patterns
  - ▶ patterns are mined from large corpora and automatically generalised (optional elements, POS tags or semantic classes)

## Structured vs. unstructured context

- ▶ In **unstructured** models, context specification acts as a **filter**
  - ▶ determines whether context token counts as co-occurrence
  - ▶ e.g. must be linked by any syntactic dependency relation
- ▶ In **structured** models, feature terms are **subtyped**
  - ▶ depending on their position in the context
  - ▶ e.g. left *vs.* right context, type of syntactic relation, etc.

## Structured vs. unstructured surface context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

| unstructured | bite |
|--------------|------|
| dog          | 4    |
| man          | 3    |

A dog bites a man. The man's dog bites a dog. A dog bites a man.

| structured | bite-l | bite-r |
|------------|--------|--------|
| dog        | 3      | 1      |
| man        | 1      | 2      |

## Structured vs. unstructured dependency context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

| unstructured | bite |
|--------------|------|
| dog          | 4    |
| man          | 2    |

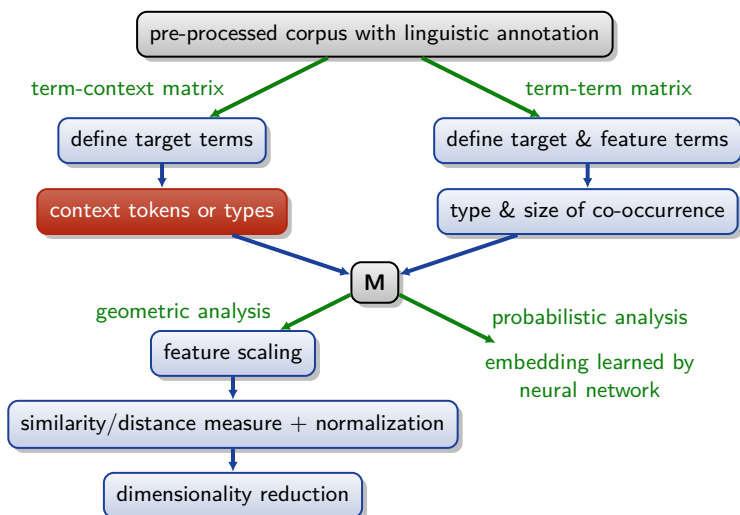
A dog bites a man. The man's dog bites a dog. A dog bites a man.

| structured | bite-subj | bite-obj |
|------------|-----------|----------|
| dog        | 3         | 1        |
| man        | 0         | 2        |

## Comparison

- ▶ Unstructured context
  - ▶ data less sparse (e.g. *man kills* and *kills man* both map to the *kill* dimension of the vector  $\mathbf{x}_{\text{man}}$ )
- ▶ Structured context
  - ▶ more sensitive to semantic distinctions (*kill-subj* and *kill-obj* are rather different things!)
  - ▶ dependency relations provide a form of syntactic “typing” of the DSM dimensions (the “subject” dimensions, the “recipient” dimensions, etc.)
  - ▶ important to account for word-order and compositionality

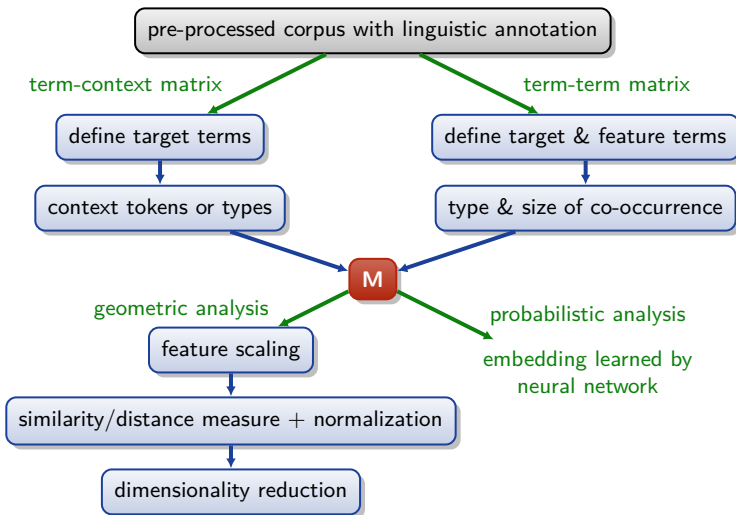
## Overview of DSM parameters



## Context tokens vs. context types

- ▶ Features are usually context **tokens**, i.e. individual instances
  - ▶ document, Wikipedia article, Web page, ...
  - ▶ paragraph, sentence, tweet, ...
  - ▶ “co-occurrence” count = frequency of term in context token
- ▶ Can also be generalised to context **types**, e.g.
  - ▶ type = cluster of near-duplicate documents
  - ▶ type = syntactic structure of sentence (ignoring content)
  - ▶ type = tweets from same author
  - ▶ frequency counts from all instances of type are aggregated
- ▶ Context types may be anchored at individual tokens
  - ▶ n-gram of words (or POS tags) around target
  - ▶ subcategorisation pattern of target verb
  - ▶ overlaps with (generalisation of) syntactic co-occurrence

## Overview of DSM parameters



## Marginal and expected frequencies

- ▶ Matrix of **observed** co-occurrence frequencies not sufficient

| target     | feature             | <i>O</i> | <i>R</i> | <i>C</i> | <i>E</i> |
|------------|---------------------|----------|----------|----------|----------|
| <i>dog</i> | <i>small</i>        | 855      | 33,338   | 490,580  | 134.34   |
| <i>dog</i> | <i>domesticated</i> | 29       | 33,338   | 918      | 0.25     |

- ▶ Notation
  - ▶ *O* = observed co-occurrence frequency
  - ▶ *R* = overall frequency of target term = row marginal frequency
  - ▶ *C* = overall frequency of feature = column marginal frequency
  - ▶ *N* = sample size  $\approx$  size of corpus
- ▶ **Expected** co-occurrence **frequency**

$$E = \frac{R \cdot C}{N} \longleftrightarrow O$$

## Obtaining marginal frequencies

- ▶ Term-document matrix
  - ▶ *R* = frequency of target term in corpus
  - ▶ *C* = size of document (# tokens)
  - ▶ *N* = corpus size
- ▶ Syntactic co-occurrence
  - ▶ # of dependency instances in which target/feature participates
  - ▶ *N* = total number of dependency instances
  - ▶ can be computed from full co-occurrence matrix **M**
- ▶ Textual co-occurrence
  - ▶ *R*, *C*, *O* are “document” frequencies, i.e. number of context units in which target, feature or combination occurs
  - ▶ *N* = total # of context units



## Obtaining marginal frequencies

- ▶ Surface co-occurrence
  - ▶ it is quite tricky to obtain fully consistent counts (Evert 2008)
  - ▶ at least correct  $E$  for span size  $k$  (= number of tokens in span)

$$E = k \cdot \frac{R \cdot C}{N}$$

with  $R, C$  = individual corpus frequencies and  $N$  = corpus size

- ▶ can also be implemented by pre-multiplying  $R' = k \cdot R$
- ▶ alternatively, compute marginals and sample size by summing over full co-occurrence matrix (→  $E$  as above, but inflated  $N$ )

- ▶ NB: shifted PPMI (Levy and Goldberg 2014) corresponds to a post-hoc application of the span size adjustment
  - ▶ performs worse than PPMI, but paper suggests they already approximate correct  $E$  by summing over co-occurrence matrix

## Marginal frequencies in wordspace

DSM objects in wordspace (class `dsm`) include marginal frequencies as well as counts of nonzero cells for rows and columns.

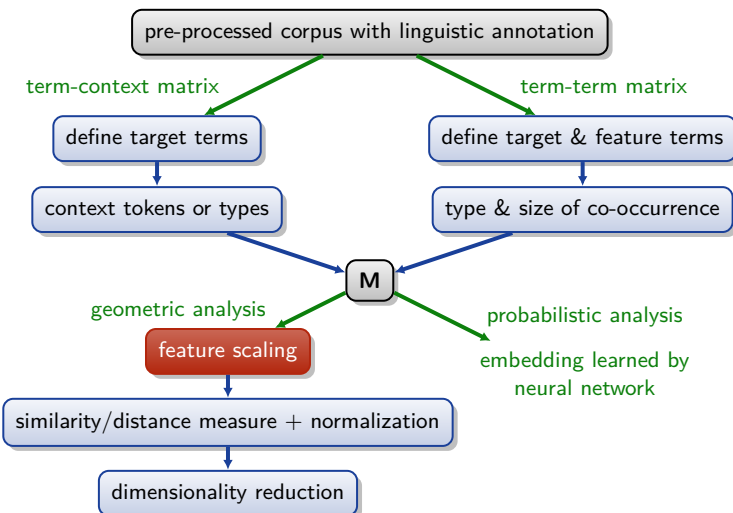
```
> TT$rows
  term      f nnzero
1  cat  22007      5
2  dog  50807      7
3 animal 77053      7
4  time 1156693     7
5 reason 95047      6
6  cause 54739      5
7 effect 133102     6
> TT$cols
...
> TT$globals$N
[1] 199902178
> TT$M # the full co-occurrence matrix
```

## Geometric vs. probabilistic interpretation

- ▶ Geometric interpretation
  - ▶ row vectors as points or arrows in  $n$ -dimensional space
  - ▶ very intuitive, good for visualisation
  - ▶ use techniques from geometry and matrix algebra
- ▶ Probabilistic interpretation
  - ▶ co-occurrence matrix as observed sample statistic that is “explained” by a generative probabilistic model
  - ▶ e.g. probabilistic LSA (Hoffmann 1999), Latent Semantic Clustering (Rooth *et al.* 1999), Latent Dirichlet Allocation (Blei *et al.* 2003), etc.
  - ▶ explicitly accounts for random variation of frequency counts
  - ▶ recent work: **neural word embeddings**

▶ focus on geometric interpretation in this tutorial

## Overview of DSM parameters



## Feature scaling

Feature scaling is used to “discount” less important features:

- ▶ Logarithmic scaling:  $O' = \log(O + 1)$   
(cf. Weber-Fechner law for human perception)
- ▶ Relevance weighting, e.g. **tf.idf** (information retrieval)

$$tf.idf = tf \cdot \log(D/df)$$

- ▶  $tf$  = co-occurrence frequency  $O$
- ▶  $df$  = document frequency of feature (or nonzero count)
- ▶  $D$  = total number of documents (or row count of **M**)
- ▶ Statistical **association measures** (Evert 2004, 2008) take frequency of target term and feature into account
  - ▶ often based on comparison of observed and expected co-occurrence frequency
  - ▶ measures differ in how they balance  $O$  and  $E$

## Simple association measures

- ▶ pointwise **Mutual Information** (MI)

$$MI = \log_2 \frac{O}{E}$$

- ▶ local MI

$$\text{local-MI} = O \cdot MI = O \cdot \log_2 \frac{O}{E}$$

- ▶ **t-score**

$$t = \frac{O - E}{\sqrt{O}}$$

| target | feature      | $O$ | $E$     | MI    | local-MI | t-score |
|--------|--------------|-----|---------|-------|----------|---------|
| dog    | small        | 855 | 134.34  | 2.67  | 2282.88  | 24.64   |
| dog    | domesticated | 29  | 0.25    | 6.85  | 198.76   | 5.34    |
| dog    | sgjkj        | 1   | 0.00027 | 11.85 | 11.85    | 1.00    |

## Other association measures

- ▶ simple **log-likelihood** ( $\approx$  local-MI)

$$G^2 = \pm 2 \cdot \left( O \cdot \log_2 \frac{O}{E} - (O - E) \right)$$

with positive sign for  $O > E$  and negative sign for  $O < E$

- ▶ **Dice** coefficient

$$\text{Dice} = \frac{2O}{R + C}$$

- ▶ Many other simple association measures (AMs) available
- ▶ Further AMs computed from full contingency tables, see
  - ▶ Evert (2008)
  - ▶ <http://www.collocations.de/>
  - ▶ <http://sigil.r-forge.r-project.org/>

## Applying association scores in wordspace

```
> options(digits=3) # print fractional values with limited precision
> dsm.score(TT, score="MI", sparse=FALSE, matrix=TRUE)
      breed  tail  feed  kill important explain likely
cat    6.21  4.568  3.129  2.801      -Inf  0.0182  -Inf
dog    7.78  3.081  3.922  2.323     -3.774 -1.1888 -0.4958
animal 3.50  2.132  4.747  2.832     -0.674 -0.4677 -0.0966
time  -1.65 -2.236 -0.729 -1.097     -1.728 -1.2382  0.6392
reason -2.30  -Inf -1.982 -0.388      1.472  4.0368  2.8860
cause  -Inf -0.834  -Inf -2.177      1.900  2.8329  4.0691
effect -Inf -2.116 -2.468 -2.459      0.791  1.6312  0.9221
```

- ⚠ sparseness of the matrix has been lost!
- ⚠ cells with score  $x = -\infty$  are inconvenient
- ⚠ distribution of scores may be even more skewed than co-occurrence frequencies themselves (esp. for local-MI)

## Sparse association measures

- Sparse association scores are cut off at zero, i.e.

$$f(x) = \begin{cases} x & x > 0 \\ 0 & x \leq 0 \end{cases}$$

- Also known as “positive” scores
  - PPMI = positive pointwise MI (e.g. Bullinaria and Levy 2007)
  - wordspace computes sparse AMs by default → “MI” = PPMI
- Preserves sparseness if  $x \leq 0$  for all empty cells ( $O = 0$ )
  - combine with signed AM ( $x > 0$  for  $O > E$ ,  $x < 0$  for  $O < E$ )
  - sparseness may even increase: cells with  $x < 0$  become empty
- Further thinning may be beneficial (Polajnar and Clark 2014)
  - apply shifted cutoff threshold  $x > \theta$  (Levy *et al.* 2015)
  - keep only  $k$  top-scoring features for each target

## Score transformations

An additional scale transformation can be applied in order to de-skew association scores:

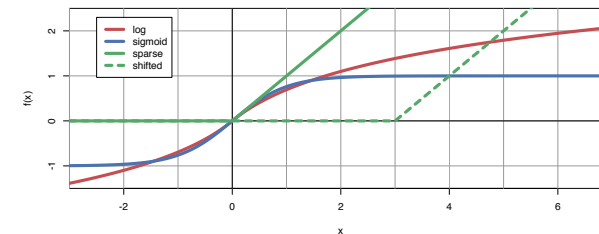
- signed **logarithmic** transformation

$$f(x) = \pm \log(|x| + 1)$$

- **sigmoid** transformation as soft binarization

$$f(x) = \tanh x$$

- **sparse** AM as (**shifted**) cutoff transformation



## Association scores & transformations in wordspace

```
> dsm.score(TT, score="MI", matrix=TRUE) # PPMI
      breed tail feed kill important explain likely
cat      6.21 4.57 3.13 2.80      0.000 0.0182 0.000
dog      7.78 3.08 3.92 2.32      0.000 0.0000 0.000
animal   3.50 2.13 4.75 2.83      0.000 0.0000 0.000
time      0.00 0.00 0.00 0.00      0.000 0.0000 0.639
reason    0.00 0.00 0.00 0.00      1.472 4.0368 2.886
cause     0.00 0.00 0.00 0.00      1.900 2.8329 4.069
effect    0.00 0.00 0.00 0.00      0.791 1.6312 0.922
> dsm.score(TT, score="simple-ll", matrix=TRUE)
> dsm.score(TT, score="simple-ll", trans="log", matrix=T)
# logarithmic co-occurrence frequency
> dsm.score(TT, score="freq", transform="log", matrix=T)

# now try other parameter combinations
> ?dsm.score # read help page for available parameter settings
```

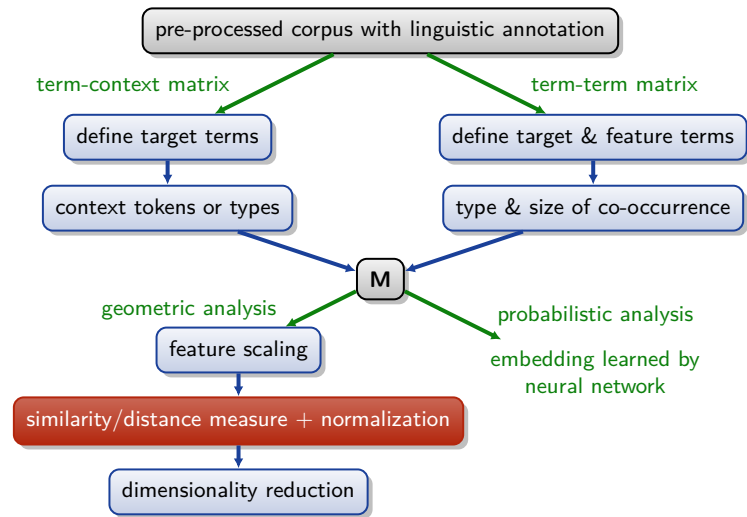
## Scaling of column vectors

- In statistical analysis and machine learning, features are usually **centered** and **scaled** so that

$$\begin{aligned} \text{mean} \quad \mu &= 0 \\ \text{variance} \quad \sigma^2 &= 1 \end{aligned}$$

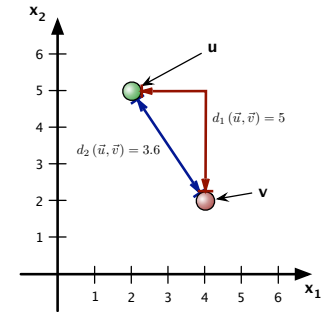
- In DSM research, this step is less common for columns of **M**
  - centering is a prerequisite for certain dimensionality reduction and data analysis techniques (esp. PCA)
  - but co-occurrence matrix no longer sparse!
  - scaling may give too much weight to rare features
- **M** cannot be row-normalised and column-scaled at the same time (result depends on ordering of the two steps)

## Overview of DSM parameters



## Geometric distance = metric

- **Distance** between vectors  $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \rightarrow$  (dis)similarity
  - $\mathbf{u} = (u_1, \dots, u_n)$
  - $\mathbf{v} = (v_1, \dots, v_n)$
- **Euclidean** distance  $d_2(\mathbf{u}, \mathbf{v})$
- “City block” **Manhattan** distance  $d_1(\mathbf{u}, \mathbf{v})$
- Both are special cases of the **Minkowski**  $p$ -distance  $d_p(\mathbf{u}, \mathbf{v})$  (for  $p \in [1, \infty]$ )

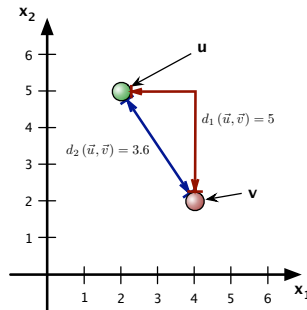


$$d_p(\mathbf{u}, \mathbf{v}) := (|u_1 - v_1|^p + \dots + |u_n - v_n|^p)^{1/p}$$

$$d_\infty(\mathbf{u}, \mathbf{v}) = \max\{|u_1 - v_1|, \dots, |u_n - v_n|\}$$

## Geometric distance = metric

- **Distance** between vectors  $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \rightarrow$  (dis)similarity
  - $\mathbf{u} = (u_1, \dots, u_n)$
  - $\mathbf{v} = (v_1, \dots, v_n)$
- **Euclidean** distance  $d_2(\mathbf{u}, \mathbf{v})$
- “City block” **Manhattan** distance  $d_1(\mathbf{u}, \mathbf{v})$
- Extension of  $p$ -distance  $d_p(\mathbf{u}, \mathbf{v})$  (for  $0 \leq p \leq 1$ )



$$d_p(\mathbf{u}, \mathbf{v}) := |u_1 - v_1|^p + \dots + |u_n - v_n|^p$$

$$d_0(\mathbf{u}, \mathbf{v}) = \#\{i \mid u_i \neq v_i\}$$

## Computing distances

Preparation: store “scored” matrix in DSM object

```
> TT <- dsm.score(TT, score="freq", transform="log")
```

Compute distances between individual term pairs ...

```
> pair.distances(c("cat", "cause"), c("animal", "effect"),
  TT, method="euclidean")
cat/animal cause/effect
4.16      1.53
```

... or full distance matrix.

```
> dist.matrix(TT, method="euclidean")
> dist.matrix(TT, method="minkowski", p=4)
```

## Distance and vector length = norm

- Intuitively, distance  $d(\mathbf{u}, \mathbf{v})$  should correspond to length  $\|\mathbf{u} - \mathbf{v}\|$  of displacement vector  $\mathbf{u} - \mathbf{v}$

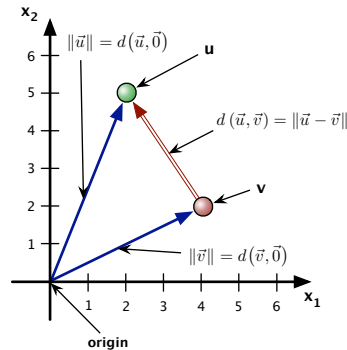
- $d(\mathbf{u}, \mathbf{v})$  is a **metric**
- $\|\mathbf{u} - \mathbf{v}\|$  is a **norm**
- $\|\mathbf{u}\| = d(\mathbf{u}, \mathbf{0})$

- Any norm-induced metric is **translation-invariant**

- $d_p(\mathbf{u}, \mathbf{v}) = \|\mathbf{u} - \mathbf{v}\|_p$

- Minkowski  $p$ -norm** for  $p \in [1, \infty]$  (not  $p < 1$ ):

$$\|\mathbf{u}\|_p := (|u_1|^p + \dots + |u_n|^p)^{1/p}$$



## Normalisation of row vectors

- Geometric distances only meaningful for vectors of the same length  $\|\mathbf{x}\|$

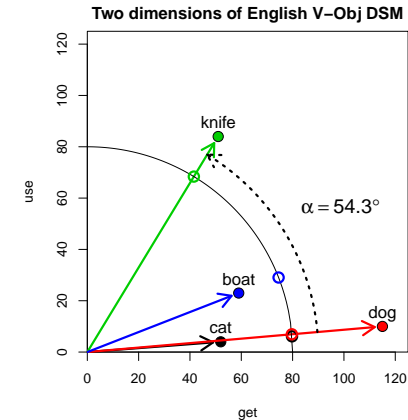
- Normalize by scalar division:  
 $\mathbf{x}' = \mathbf{x} / \|\mathbf{x}\| = (\frac{x_1}{\|\mathbf{x}\|}, \frac{x_2}{\|\mathbf{x}\|}, \dots)$   
 with  $\|\mathbf{x}'\| = 1$

- Norm must be compatible with distance measure!

- Special case: scale to relative frequencies with

$$\|\mathbf{x}\|_1 = |x_1| + \dots + |x_n|$$

- probabilistic interpretation



## Norms and normalization

```
> rowNorms(TT$S, method="euclidean")
  cat  dog animal  time reason  cause effect
6.90  8.96  8.82 10.29  8.13  6.86  6.52
```

```
> TT <- dsm.score(TT, score="freq", transform="log",
  normalize=TRUE, method="euclidean")
> rowNorms(TT$S, method="euclidean") # all = 1 now
> dist.matrix(TT, method="euclidean")
      cat  dog animal  time reason  cause effect
cat    0.000 0.224  0.473 0.782  1.121 1.239  1.161
dog    0.224 0.000  0.398 0.698  1.065 1.179  1.113
animal 0.473 0.398  0.000 0.426  0.841 0.971  0.860
time   0.782 0.698  0.426 0.000  0.475 0.585  0.502
reason 1.121 1.065  0.841 0.475  0.000 0.277  0.198
cause  1.239 1.179  0.971 0.585  0.277 0.000  0.224
effect 1.161 1.113  0.860 0.502  0.198 0.224  0.000
```

## Distance measures for non-negative vectors

- Information theory: **Kullback-Leibler (KL) divergence** for probability vectors (non-negative,  $\|\mathbf{x}\|_1 = 1$ )

$$D(\mathbf{u} \parallel \mathbf{v}) = \sum_{i=1}^n u_i \cdot \log_2 \frac{u_i}{v_i}$$

- Properties of KL divergence

- most appropriate in a probabilistic interpretation of  $\mathbf{M}$
- zeroes in  $\mathbf{v}$  without corresponding zeroes in  $\mathbf{u}$  are problematic
- not symmetric, unlike geometric distance measures
- alternatives: skew divergence, Jensen-Shannon divergence

- A symmetric distance metric (Endres and Schindelin 2003)

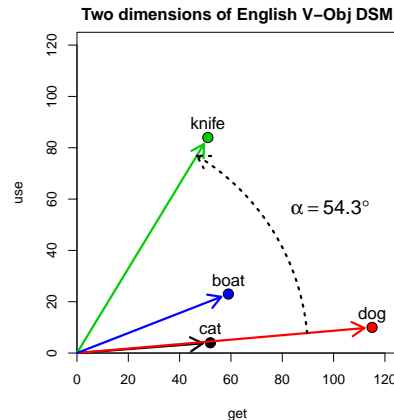
$$D_{uv} = D(\mathbf{u} \parallel \mathbf{z}) + D(\mathbf{v} \parallel \mathbf{z}) \quad \text{with} \quad \mathbf{z} = \frac{\mathbf{u} + \mathbf{v}}{2}$$

## Similarity measures

- Angle  $\alpha$  between vectors  $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n$  is given by

$$\cos \alpha = \frac{\sum_{i=1}^n u_i \cdot v_i}{\sqrt{\sum_i u_i^2} \cdot \sqrt{\sum_i v_i^2}} = \frac{\mathbf{u}^T \mathbf{v}}{\|\mathbf{u}\|_2 \cdot \|\mathbf{v}\|_2}$$

- cosine** measure of similarity:  $\cos \alpha$ 
  - $\cos \alpha = 1 \rightarrow$  collinear
  - $\cos \alpha = 0 \rightarrow$  orthogonal
- Corresponding metric: **angular distance**  $\alpha$



## Euclidean distance or cosine similarity?

$$\begin{aligned} d_2(\mathbf{u}, \mathbf{v}) &= \|\mathbf{u} - \mathbf{v}\|_2 = \sqrt{\sum_i (u_i - v_i)^2} \\ &= \sqrt{\sum_i u_i^2 + \sum_i v_i^2 - 2 \sum_i u_i v_i} \\ &= \sqrt{\|\mathbf{u}\|_2^2 + \|\mathbf{v}\|_2^2 - 2 \mathbf{u}^T \mathbf{v}} \\ &= \sqrt{2 - 2 \cos \phi} \end{aligned}$$

$d_2(\mathbf{u}, \mathbf{v})$  is a monotonically increasing function of  $\phi$

Euclidean distance and cosine similarity are equivalent: if vectors have been normalised ( $\|\mathbf{u}\|_2 = \|\mathbf{v}\|_2 = 1$ ), both lead to the same neighbour ranking.

## Similarity measures for non-negative vectors

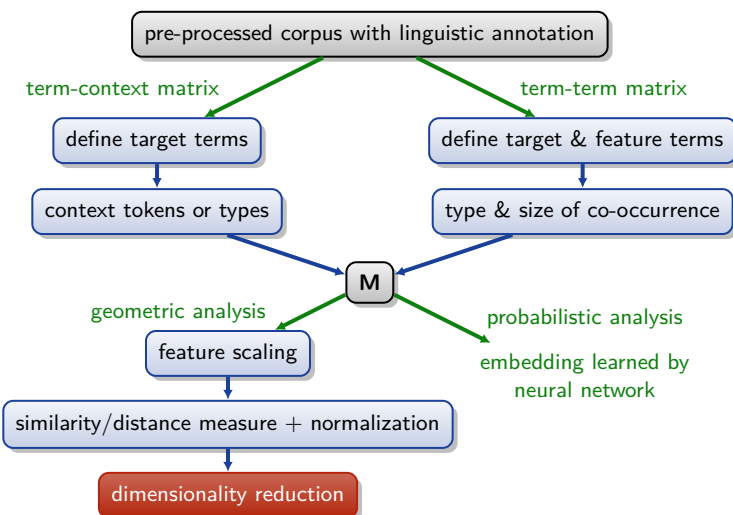
- Generalized **Jaccard coefficient** = shared features

$$J(\mathbf{u}, \mathbf{v}) = \frac{\sum_{i=1}^n \min\{u_i, v_i\}}{\sum_{i=1}^n \max\{u_i, v_i\}}$$

- $1 - J(\mathbf{u}, \mathbf{v})$  is a distance **metric** (Kosub 2016)
- An asymmetric measure of feature **overlap** (Clarke 2009)

$$o(\mathbf{u}, \mathbf{v}) = \frac{\sum_{i=1}^n \min\{u_i, v_i\}}{\sum_{i=1}^n u_i}$$

## Overview of DSM parameters



## Dimensionality reduction = model compression

- ▶ Co-occurrence matrix **M** is often unmanageably large and can be extremely sparse
  - ▶ Google Web1T5:  $1M \times 1M$  matrix with one trillion cells, of which less than 0.05% contain nonzero counts (Evert 2010)
- ➔ Compress matrix by reducing dimensionality (= rows)
- ▶ **Feature selection**: columns with high frequency & variance
  - ▶ measured by entropy, chi-squared test, nonzero count, ...
  - ▶ may select similar dimensions and discard valuable information
- ▶ **Projection** into (linear) subspace
  - ▶ principal component analysis (PCA)
  - ▶ independent component analysis (ICA)
  - ▶ random indexing (RI)
  - ▶ intuition: preserve distances between data points

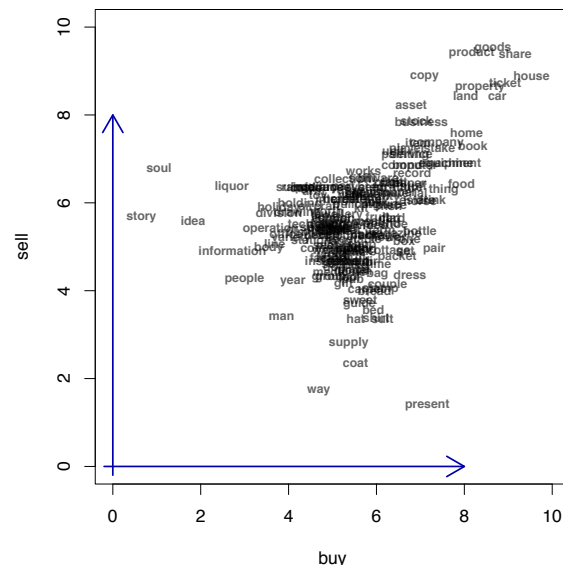
## Dimensionality reduction & latent dimensions

Landauer and Dumais (1997) claim that LSA dimensionality reduction (and related PCA technique) uncovers **latent dimensions** by exploiting correlations between features.

- ▶ Example: term-term matrix
- ▶ V-Obj co-oc. extracted from BNC
  - ▶ targets = noun lemmas
  - ▶ features = verb lemmas
- ▶ feature scaling: association scores (SketchEngine log Dice)
- ▶  $k = 186$  nouns with  $f_{\text{buy}} + f_{\text{sell}} \geq 25$
- ▶  $n = 2$  dimensions: *buy* and *sell*

| noun             | buy  | sell |
|------------------|------|------|
| <i>antique</i>   | 5.12 | 5.50 |
| <i>bread</i>     | 5.96 | 3.99 |
| <i>computer</i>  | 6.75 | 6.83 |
| <i>factory</i>   | 4.95 | 4.72 |
| <i>group</i>     | 4.93 | 4.28 |
| <i>jewellery</i> | 5.11 | 5.73 |
| <i>mill</i>      | 5.14 | 5.41 |
| <i>people</i>    | 3.00 | 4.26 |
| <i>record</i>    | 6.81 | 6.68 |
| <i>souvenir</i>  | 5.45 | 4.67 |
| <i>ticket</i>    | 8.93 | 8.74 |

## Dimensionality reduction & latent dimensions

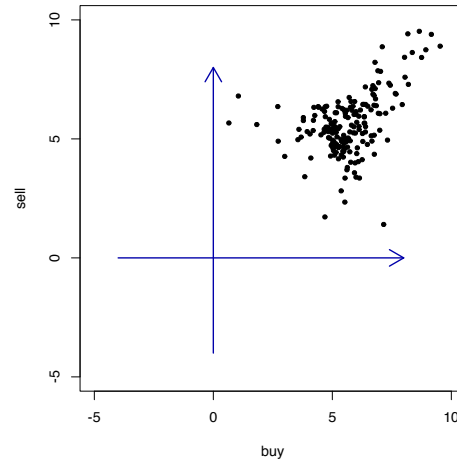


## Motivating latent dimensions & subspace projection

- ▶ The **latent property** of being a commodity is “expressed” through associations with several verbs: *sell*, *buy*, *acquire*, ...
- ▶ Consequence: these DSM dimensions will be **correlated**
- ▶ Identify **latent dimension** by looking for strong correlations (or weaker correlations between large sets of features)
- ▶ Projection into subspace  $V$  of  $k < n$  latent dimensions as a “**noise reduction**” technique → **LSA**
- ▶ Assumptions of this approach:
  - ▶ “latent” distances in  $V$  are semantically meaningful
  - ▶ other “residual” dimensions represent chance co-occurrence patterns, often particular to the corpus underlying the DSM

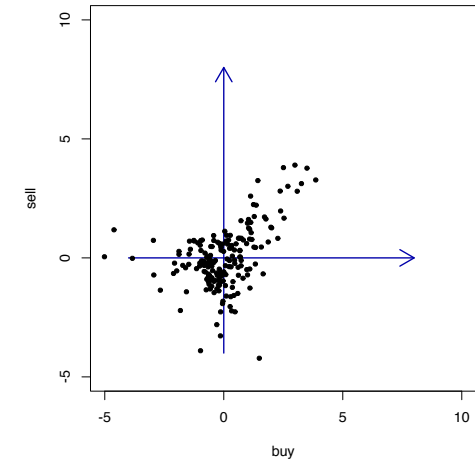
## Step 1: Centering the data set

- **Uncentered data set**
- Centered data set
- Distance information = variance



## Step 1: Centering the data set

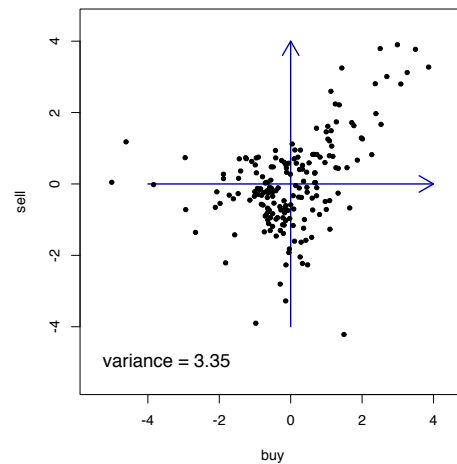
- Uncentered data set
- **Centered data set**
- Distance information = variance



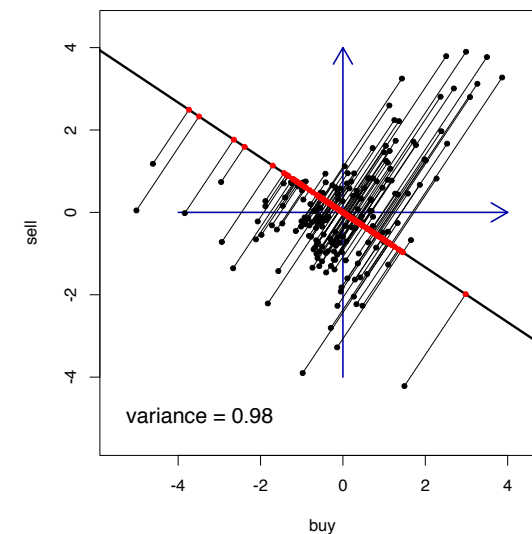
## Step 1: Centering the data set

- Uncentered data set
- Centered data set
- Distance information = **variance**

$$\sigma^2 = \frac{1}{k-1} \sum_{i=1}^k \|\mathbf{x}^{(i)}\|^2$$

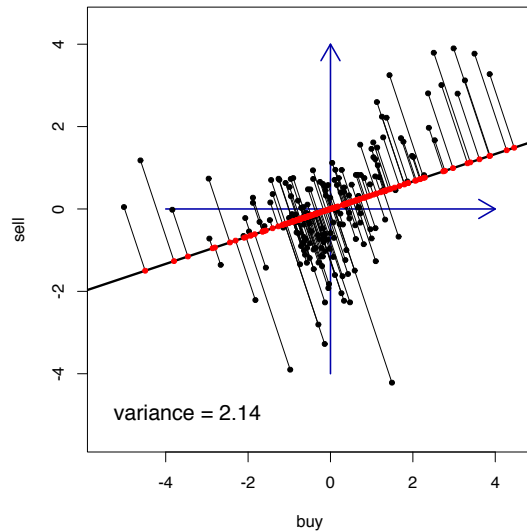


## Step 2: Orthogonal projection into optimal subspace

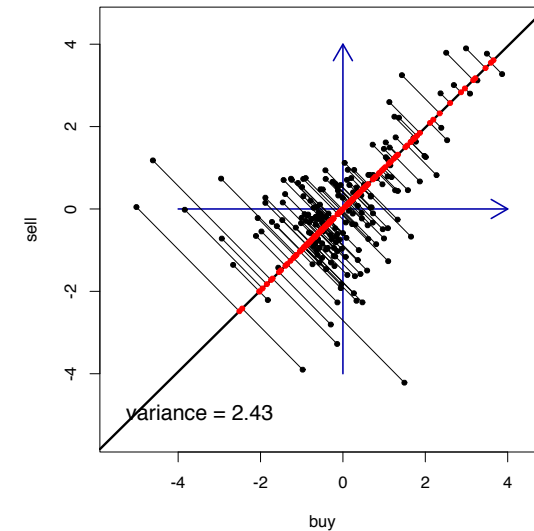




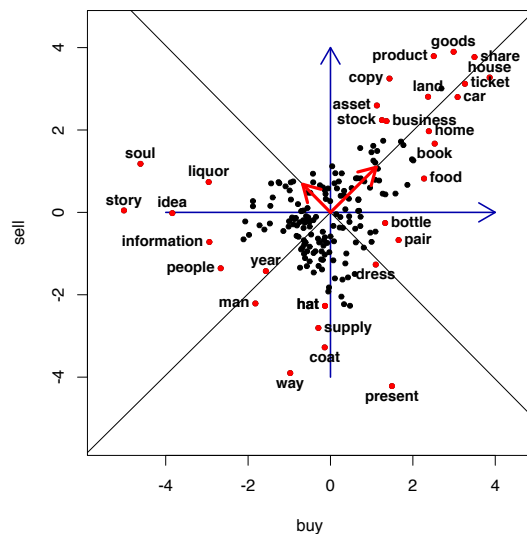
## Step 2: Orthogonal projection into optimal subspace



## Step 2: Orthogonal projection into optimal subspace



## Step 3: Further orthogonal dimensions

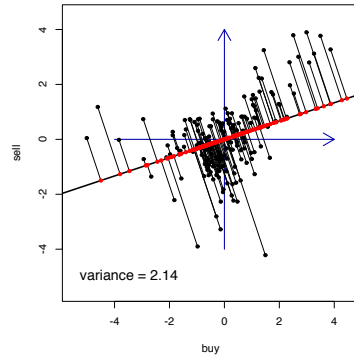


## Dimensionality reduction by PCA

- ▶ Principal component analysis (**PCA**)
  - ▶ orthogonal projection into orthogonal latent dimensions
  - ▶ finds optimal subspace of given dimensionality (such that orthogonal projection preserves distance information)
  - ▶ but requires centered features → no longer sparse
- ▶ Singular value decomposition (**SVD**)
  - ▶ the mathematical algorithm behind PCA
  - ▶ often applied without centering in distributional semantics
  - ▶ optimality of subspace not guaranteed (see part 5)
- ▶ NB: row vectors should be renormalised after PCA/SVD
  - ▶ unless cosine similarity / angular distance is used
  - ▶ also normalise vectors **before** dimensionality reduction

## Dimensionality reduction by RI

- Random indexing (**RI**)
  - project into random subspace (Sahlgren and Karlgren 2005)
  - reasonably good if there are many subspace dimensions
  - can be performed online w/o collecting full co-oc. matrix



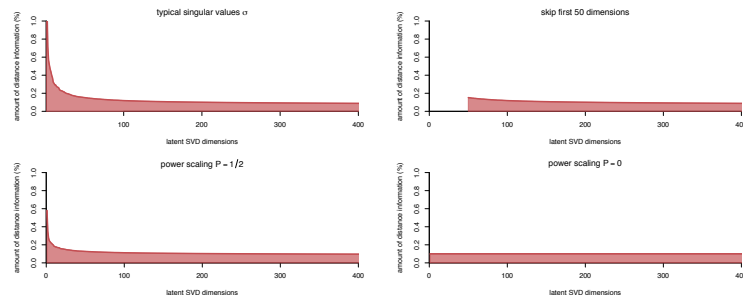
## Dimensionality reduction in practice

```
# it is customary to omit the centering: SVD dimensionality reduction
> TT2 <- dsm.projection(TT, n=2, method="svd")
> TT2
      svd1    svd2
cat   -0.733 -0.6615
dog   -0.782 -0.6110
animal -0.914 -0.3606
time  -0.993  0.0302
reason -0.889  0.4339
cause  -0.817  0.5615
effect -0.871  0.4794

> x <- TT2[, 1] # first latent dimension
> y <- TT2[, 2] # second latent dimension
> plot(x, y, pch=20, col="red",
      xlim=extendrange(x), ylim=extendrange(y))
> text(x, y, rownames(TT2), pos=3)
```

## Scaling latent dimensions

- Capture different amounts of distance info (= variance)
- Indicated by **singular values**  $\sigma_i$  of PCA/SVD algorithm
- Skip first  $k$  dimensions, e.g.  $k = 50$  (Bullinaria and Levy 2012)
- Power-scaling of dimensions:  $\sigma^P$  (Caron 2001)
  - Bullinaria and Levy (2012) report positive effect
  - esp. with  $P = 0$  to equalize dimensions (**whitening**)



## Power-scaling in practice

```
> TT2 <- dsm.projection(TT, n=2, method="svd", power=0)
> TT2
      svd1    svd2
cat   -0.322 -0.5110
dog   -0.343 -0.4721
animal -0.401 -0.2786
time  -0.436  0.0233
reason -0.390  0.3353
cause  -0.359  0.4338
effect -0.383  0.3704

# power-scaling can also be applied post-hoc
> sigma <- attr(TT2, "sigma") # singular values
> scaleMargins(TT2, cols=sigma^0.5) # P = 1/2
> scaleMargins(TT2, cols=sigma) # unscaled (P = 1)
```

## Outline

### DSM parameters

A taxonomy of DSM parameters

Examples

### Building a DSM

Sparse matrices

Example: a verb-object DSM

## Some well-known DSM examples

### Latent Semantic Analysis (Landauer and Dumais 1997)

- ▶ term-context matrix with document context
- ▶ weighting: log term frequency and term entropy
- ▶ distance measure: cosine
- ▶ dimensionality reduction: SVD

### Hyperspace Analogue to Language (Lund and Burgess 1996)

- ▶ term-term matrix with surface context
- ▶ structured (left/right) and distance-weighted frequency counts
- ▶ distance measure: Minkowski metric ( $1 \leq p \leq 2$ )
- ▶ dimensionality reduction: feature selection (high variance)

## Some well-known DSM examples

### Infomap NLP (Widdows 2004)

- ▶ term-term matrix with unstructured surface context
- ▶ weighting: none
- ▶ distance measure: cosine
- ▶ dimensionality reduction: SVD

### Random Indexing (Karlgrén and Sahlgrén 2001)

- ▶ term-term matrix with unstructured surface context
- ▶ weighting: various methods
- ▶ distance measure: various methods
- ▶ dimensionality reduction: random indexing (RI)

## Some well-known DSM examples

### Dependency Vectors (Padó and Lapata 2007)

- ▶ term-term matrix with unstructured dependency context
- ▶ weighting: log-likelihood ratio
- ▶ distance measure: PPMI-weighted Dice (Lin 1998)
- ▶ dimensionality reduction: none

### Distributional Memory (Baroni and Lenci 2010)

- ▶ term-term matrix with structured and unstructured dependencies + knowledge patterns
- ▶ weighting: local-MI on type frequencies of link patterns
- ▶ distance measure: cosine
- ▶ dimensionality reduction: none

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Example: a verb-object DSM

## Sparse matrix representation

- ▶ Invented example of a **sparsely populated** DSM matrix

|       | eat | get | hear | kill | see | use |
|-------|-----|-----|------|------|-----|-----|
| boat  | .   | 59  | .    | .    | 39  | 23  |
| cat   | .   | .   | .    | 26   | 58  | .   |
| cup   | .   | 98  | .    | .    | .   | .   |
| dog   | 33  | .   | 42   | .    | 83  | .   |
| knife | .   | .   | .    | .    | .   | 84  |
| pig   | 9   | .   | .    | 27   | .   | .   |

- ▶ Store only non-zero entries in compact **sparse matrix format**

| row | col | value | row | col | value |
|-----|-----|-------|-----|-----|-------|
| 1   | 2   | 59    | 4   | 1   | 33    |
| 1   | 5   | 39    | 4   | 3   | 42    |
| 1   | 6   | 23    | 4   | 5   | 83    |
| 2   | 4   | 26    | 5   | 6   | 84    |
| 2   | 5   | 58    | 6   | 1   | 9     |
| 3   | 2   | 98    | 6   | 4   | 27    |

## Scaling up to the real world

- ▶ So far, we have worked on minuscule **toy models**

📡 We want to scale up to **real world** data sets now

- ▶ Example 1: window-based DSM on BNC content words

- ▶ 83,926 lemma types with  $f \geq 10$
- ▶ term-term matrix with  $83,926 \cdot 83,926 = 7$  billion entries
- ▶ standard representation requires 56 GB of RAM (8-byte floats)
- ▶ only 22.1 million non-zero entries (= 0.32%)

- ▶ Example 2: Google Web 1T 5-grams (1 trillion words)

- ▶ more than 1 million word types with  $f \geq 2500$
- ▶ term-term matrix with 1 trillion entries requires 8 TB RAM
- ▶ only 400 million non-zero entries (= 0.04%)

## Working with sparse matrices

- ▶ Compressed format: each row index (or column index) stored only once, followed by non-zero entries in this row (or column)
  - ▶ convention: **column-major** matrix (data stored by columns)

- ▶ Specialised algorithms for sparse matrix algebra
  - ▶ especially matrix multiplication, solving linear systems, etc.
  - ▶ take care to avoid operations that create a dense matrix!

- ▶ R implementation: **Matrix** package

- ▶ essential for real-life distributional semantics
- ▶ wordspace provides additional support for sparse matrices (vector distances, sparse SVD, ...)

- ▶ Other software: Matlab, Octave, Python + SciPy

## Outline

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Example: a verb-object DSM

## Constructing a DSM from a triplet table

- ▶ Additional information can be used for filtering (verb-object relation), or aggregate frequencies (spoken + written BNC)

```
> tri <- subset(DSM_VerbNounTriples_BNC, rel == "obj")
```

- ▶ Construct DSM object from triplet input
  - ▶ `raw.freq=TRUE` indicates raw co-occurrence frequencies (rather than a pre-weighted DSM)
  - ▶ constructor aggregates counts from duplicate entries
  - ▶ marginal frequencies are automatically computed

```
> VObj <- dsm(target=tri$noun, feature=tri$verb,
              score=tri$f, raw.freq=TRUE)
> VObj # inspect marginal frequencies (e.g. head(VObj$rows, 20))
```

## Triplet tables

- ▶ A sparse DSM matrix can be represented as a table of triplets (target, feature, co-occurrence frequency)
  - ▶ for syntactic co-occurrence and term-document matrices, marginals can be computed from a complete triplet table
  - ▶ for surface and textual co-occurrence, marginals have to be provided in separate files (see `?read.dsm.triplet`)

| noun | rel  | verb   | f   | mode    |
|------|------|--------|-----|---------|
| dog  | subj | bite   | 3   | spoken  |
| dog  | subj | bite   | 12  | written |
| dog  | obj  | bite   | 4   | written |
| dog  | obj  | stroke | 3   | written |
| ...  | ...  | ...    | ... | ...     |

- ▶ `DSM_VerbNounTriples_BNC` contains additional information
  - ▶ syntactic relation between noun and verb
  - ▶ written or spoken part of the British National Corpus

## Exploring the DSM

```
> VObj <- dsm.score(VObj, score="MI", normalize=TRUE)
```

```
> nearest.neighbours(VObj, "dog") # angular distance
  horse   cat  animal  rabbit   fish   guy
  73.9   75.9   76.2   77.0   77.2   78.5
  cichlid  kid    bee creature
  78.6   79.0   79.1   79.5
```

```
> nearest.neighbours(VObj, "dog", method="manhattan")
# NB: we used an incompatible Euclidean normalization!
```

```
> VObj50 <- dsm.projection(VObj, n=50, method="svd")
> nearest.neighbours(VObj50, "dog")
```

## Practice

- ▶ How many different models can you build from `DSM_VerbNounTriples_BNC?`
- ▶ Apply different filters, scores, transformations and metrics
  - 🔍 explore nearest neighbours of selected words
- ▶ Code examples for this part show additional options
- ▶ Download practical exercise (`part2_input_formats.R`)
  - ➔ different ways of loading your own co-occurrence data

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