#### Distributional Semantic Models

Part 2: The parameters of a DSM

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http://wordspace.collocations.de/doku.php/course:start

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DSM parameters

#### General definition of DSMs

A distributional semantic model (DSM) is a scaled and/or transformed co-occurrence matrix  $\mathbf{M}$ , such that each row  $\mathbf{x}$  represents the distribution of a target term across contexts.

	get	see	use	hear	eat	kill
knife	0.027	-0.024	0.206	-0.022	-0.044	-0.042
cat	0.031	0.143	-0.243	-0.015	-0.009	0.131
dog	-0.026	0.021	-0.212	0.064	0.013	0.014
boat	-0.022	0.009	-0.044	-0.040	-0.074	-0.042
cup	-0.014	-0.173	-0.249	-0.099	-0.119	-0.042
pig	-0.069	0.094	-0.158	0.000	0.094	0.265
banana	0.047	-0.139	-0.104	-0.022	0.267	-0.042

Term = word, lemma, phrase, morpheme, word pair, . . .

# DSM parameters

Outline

A taxonomy of DSM parameters Examples

#### Building a DSM

Sparse matrices

Example: a verb-object DSM

#### General definition of DSMs

Mathematical notation:

- ▶  $k \times n$  co-occurrence matrix  $\mathbf{M} \in \mathbb{R}^{k \times n}$  (example:  $7 \times 6$ )
  - ► *k* rows = **target** terms
  - ► *n* columns = **features** or **dimensions**

$$\mathbf{M} = \begin{bmatrix} m_{11} & m_{12} & \cdots & m_{1n} \\ m_{21} & m_{22} & \cdots & m_{2n} \\ \vdots & \vdots & & \vdots \\ m_{k1} & m_{k2} & \cdots & m_{kn} \end{bmatrix}$$

- lacktriangle distribution vector  $\mathbf{m}_i = i$ -th row of  $\mathbf{M}$ , e.g.  $\mathbf{m}_3 = \mathbf{m}_{\mathrm{dog}} \in \mathbb{R}^n$
- **•** components  $\mathbf{m}_i = (m_{i1}, m_{i2}, \dots, m_{in}) = \text{features of } i\text{-th term:}$

$$\mathbf{m}_3 = (-0.026, 0.021, -0.212, 0.064, 0.013, 0.014)$$
  
=  $(m_{31}, m_{32}, m_{33}, m_{34}, m_{35}, m_{36})$ 

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### Outline

#### DSM parameters

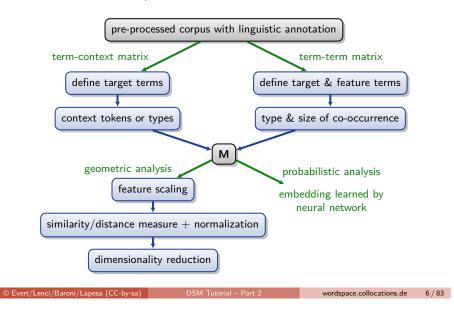
A taxonomy of DSM parameters

Example: a verb-object DSM

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#### Overview of DSM parameters



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# Term-context matrix

Term-context matrix records frequency of term in each individual context (e.g. sentence, document, Web page, encyclopaedia article)

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$$\mathbf{F} = egin{bmatrix} \cdots & \mathbf{f}_1 & \cdots \\ \cdots & \mathbf{f}_2 & \cdots \\ & dots \\ & dots \\ \cdots & \mathbf{f}_k & \cdots \end{bmatrix}$$

	6	υ				્ર <sup>ુ</sup>	
	Feliga 1000	ر وق	1/6/0	8/094	Phil	1 20 X	<i>8</i>
cat dog	10	10	7	_	_	_	_
dog	_	10	4	11	_	_	_
animal	2	15	10	2	-	_	_
time	1	_	_	_	2	1	_
reason	_	1	_	_	1	4	1
cause	_	_	_	2	1	2	6
effect	_	_	_	1	_	1	_

- > TC <- DSM\_TermContext
- > head(TC, Inf) # extract full co-oc matrix from DSM object

#### Term-term matrix

Term-term matrix records co-occurrence frequencies with feature terms for each target term

$$\mathbf{M} = \begin{bmatrix} \cdots & \mathbf{m_1} & \cdots \\ \cdots & \mathbf{m_2} & \cdots \\ & \vdots & \\ & \vdots & \\ \cdots & \mathbf{m_k} & \cdots \end{bmatrix}$$

	breed	. //e <sub>t</sub>	, 660	, kill	ing	explaint explains	likeh.
cat	83	17	7	37	_	1	_
dog	561	13	30	60	1	2	4
animal	42	10	109	134	13	5	5
time	19	9	29	117	81	34	109
reason	1	-	2	14	68	140	47
cause	_	1	_	4	55	34	55
effect	_	-	1	6	60	35	17

- > TT <- DSM TermTerm
- > head(TT, Inf)

#### Term-term matrix

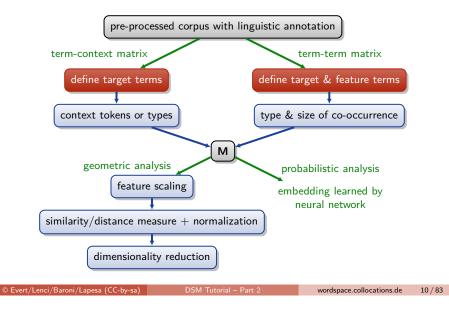
#### Some footnotes:

- $\triangleright$  Often target terms  $\neq$  feature terms
  - e.g. nouns described by co-occurrences with verbs as features
  - ▶ identical sets of target & feature terms → symmetric matrix
- ▶ Different types of co-occurrence (Evert 2008)
  - surface context (word or character window)
  - textual context (non-overlapping segments)
  - syntactic context (dependency relation)
- Can be seen as smoothing of term-context matrix
  - average over similar contexts (with same context terms)
  - data sparseness reduced, except for small windows
  - we will take a closer look at the relation between term-context and term-term models in part 5 of this tutorial

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## Overview of DSM parameters



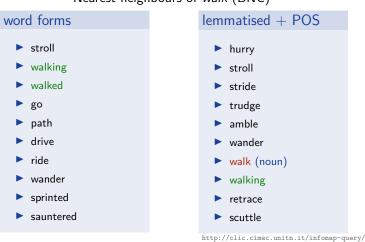
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# Definition of target and feature terms

- Choice of linguistic unit
  - words
  - bigrams, trigrams, . . .
  - multiword units, named entities, phrases, . . .
  - morphemes
  - word pairs (so analogy tasks)
- Linguistic annotation
  - word forms (minimally requires tokenisation)
  - often lemmatisation or stemming to reduce data sparseness: go, goes, went, gone, going → go
  - ▶ POS disambiguation (light/N vs. light/A vs. light/V)
  - word sense disambiguation (bank<sub>river</sub> vs. bank<sub>finance</sub>)
  - ▶ abstraction: POS tags (or bigrams) as feature terms
- ► Trade-off between deeper linguistic analysis and
  - need for language-specific resources
  - possible errors introduced at each stage of the analysis

# Effects of linguistic annotation

#### Nearest neighbours of walk (BNC)



# Effects of linguistic annotation

#### Nearest neighbours of arrivare (Repubblica)

# word forms giungere raggiungere arrivi raggiungimento raggiunto trovare raggiunge arrivasse arriverà concludere

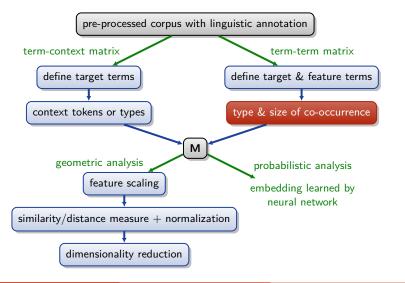
lemmatised + POS giungere aspettare attendere arrivo (noun) ricevere accontentare approdare pervenire venire piombare

http://clic.cimec.unitn.it/infomap-query/

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#### DSM parameters A taxonomy of DSM parameters

## Overview of DSM parameters



## Selection of target and feature terms

- ► Full-vocabulary models are often unmanageable
  - ▶ 762.424 distinct word forms in BNC. 605.910 lemmata
  - ▶ large Web corpora have > 10 million distinct word forms
  - low-frequency targets (and features) are not reliable ("noisy")
- ► Frequency-based selection
  - minimum corpus frequency:  $f > F_{min}$
  - or accept n<sub>w</sub> most frequent terms
  - sometimes also upper threshold:  $F_{min} < f < F_{max}$
- ► Relevance-based selection
  - criterion from IR: document frequency df
  - ▶ high df → uninformative / low df → too sparse to be useful
  - $\triangleright$  alternatives: entropy H or chi-squared statistic  $X^2$
- Other criteria

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- ▶ POS-based filter: no function words, only verbs, nouns, ...
- general dictionary, words required for particular task, ...

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#### Surface context

Context term occurs within a span of k words around target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners. [L3/R3 span, k = 6]

#### Parameters:

- span size (in words or characters)
- symmetric vs. one-sided span
- uniform or "triangular" (distance-based) weighting (don't!)
- spans clamped to sentences or other textual units?

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# Effect of span size

#### Nearest neighbours of dog (BNC)

# 2-word span cat horse ► fox rabbit pig animal mongrel sheep pigeon



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#### Textual context

Context term is in the same linguistic unit as target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

#### Parameters:

- type of linguistic unit
  - sentence
  - paragraph
  - turn in a conversation
  - Web page
  - tweet

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### Syntactic context

Context term is linked to target by a syntactic dependency (e.g. subject, modifier, ...).

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

#### Parameters:

- types of syntactic dependency (Padó and Lapata 2007)
- direct vs. indirect dependency paths
- homogeneous data (e.g. only verb-object) vs. heterogeneous data (e.g. all children and parents of the verb)
- maximal length of dependency path

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## "Knowledge pattern" context

Context term is linked to target by a lexico-syntactic pattern (text mining, cf. Hearst 1992, Pantel & Pennacchiotti 2008, etc.).

In Provence, Van Gogh painted with bright colors such as red and yellow. These colors produce incredible effects on anybody looking at his paintings.

#### Parameters:

- ▶ inventory of lexical patterns
  - ▶ lots of research to identify semantically interesting patterns (cf. Almuhareb & Poesio 2004, Veale & Hao 2008, etc.)
- ► fixed vs. flexible patterns
  - patterns are mined from large corpora and automatically generalised (optional elements, POS tags or semantic classes)

# Comparison of co-occurrence contexts

Contexts range from general/implict to specific/explicit:

	features are
textual / large span	from same general domain
small span	collocations
syntactic (single relation)	attributes (focus on aspect)
knowledge pattern	properties

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# Structured vs. unstructured context

- ▶ In unstructered models, context specification acts as a filter
  - determines whether context token counts as co-occurrence
  - e.g. muste be linked by any syntactic dependency relation
- ► In structured models, feature terms are subtyped
  - depending on their position in the context
  - e.g. left vs. right context, type of syntactic relation, etc.

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#### Structured vs. unstructured surface context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

A dog bites a man. The man's dog bites a dog. A dog bites a man.

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## Structured vs. unstructured dependency context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

A dog bites a man. The man's dog bites a dog. A dog bites a man.

structured	bite-subj	bite-obj
dog	3	1
man	0	2

# Comparison

#### Unstructured context

▶ data less sparse (e.g. man kills and kills man both map to the *kill* dimension of the vector  $\mathbf{x}_{man}$ )

#### Structured context

- more sensitive to semantic distinctions (kill-subj and kill-obj are rather different things!)
- dependency relations provide a form of syntactic "typing" of the DSM dimensions (the "subject" dimensions, the "recipient" dimensions, etc.)
- ▶ important to account for word-order and compositionality

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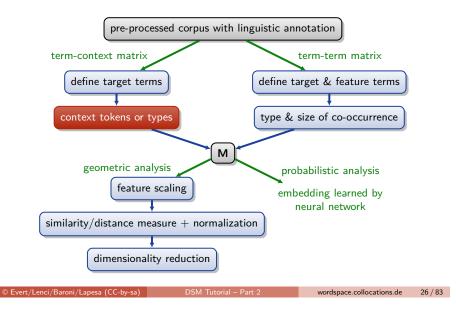
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### Context tokens vs. context types

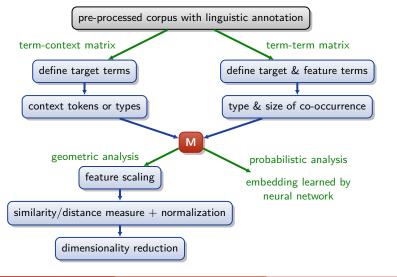
- Features are usually context **tokens**, i.e. individual instances
  - document, Wikipedia article, Web page, ...
  - paragraph, sentence, tweet, . . .
  - "co-occurrence" count = frequency of term in context token
- ► Can also be generalised to context **types**, e.g.
  - type = cluster of near-duplicate documents
  - type = syntactic structure of sentence (ignoring content)
  - ▶ type = tweets from same author
  - frequency counts from all instances of type are aggregated
- ► Context types may be anchored at individual tokens
  - n-gram of words (or POS tags) around target
  - subcategorisation pattern of target verb
  - overlaps with (generalisation of) syntactic co-occurrence

# Overview of DSM parameters



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## Overview of DSM parameters



# Marginal and expected frequencies

► Matrix of observed co-occurrence frequencies not sufficient

target	feature	0	R	С	Ε
dog	small	855	33,338	490,580	134.34
dog	domesticated	29	33,338	918	0.25

- Notation
  - ► *O* = observed co-occurrence frequency
  - ightharpoonup R = overall frequency of target term = row marginal frequency
  - ightharpoonup C = overall frequency of feature = column marginal frequency
  - ▶  $N = \text{sample size} \approx \text{size of corpus}$
- **Expected** co-occurrence **frequency**

$$E = \frac{R \cdot C}{N} \longleftrightarrow O$$

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## Obtaining marginal frequencies

- ► Surface co-occurrence
  - ▶ it is quite tricky to obtain fully consistent counts (Evert 2008)
  - $\blacktriangleright$  at least correct E for span size k (= number of tokens in span)

$$E = k \cdot \frac{R \cdot C}{N}$$

with R, C = individual corpus frequencies and N = corpus size

- can also be implemented by pre-multiplying  $R' = k \cdot R$
- alternatively, compute marginals and sample size by summing over full co-occurrence matrix ( $\rightarrow E$  as above, but inflated N)
- ▶ NB: shifted PPMI (Levy and Goldberg 2014) corresponds to a post-hoc application of the span size adjustment
  - performs worse than PPMI, but paper suggests they already approximate correct *E* by summing over co-occurrence matrix

# Obtaining marginal frequencies

- ► Term-document matrix
  - ightharpoonup R = frequency of target term in corpus
  - ► *C* = size of document (# tokens)
  - $\triangleright$  N =corpus size
- ► Syntactic co-occurrence
  - # of dependency instances in which target/feature participates
  - $\triangleright$  N = total number of dependency instances
  - can be computed from full co-occurrence matrix M
- ► Textual co-occurrence
  - R. C. O are "document" frequencies, i.e. number of context units in which target, feature or combination occurs
  - ► *N* = total # of context units

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# Marginal frequencies in wordspace

DSM objects in wordspace (class dsm) include marginal frequencies as well as counts of nonzero cells for rows and columns.

```
> TT$rows
    term
               f nnzero
           22007
     cat
           50807
     dog
  animal
           77053
         1156693
5 reason
           54739
  cause
7 effect 133102
> TT$cols
> TT$globals$N
[1] 199902178
> TT$M # the full co-occurrence matrix
```

pre-processed corpus with linguistic annotation

М

Overview of DSM parameters

define target terms

context tokens or types

term-context matrix

#### A taxonomy of DSM parameters

# Geometric vs. probabilistic interpretation

- ► Geometric interpretation
  - row vectors as points or arrows in *n*-dimensional space
  - very intuitive, good for visualisation
  - use techniques from geometry and matrix algebra
- Probabilistic interpretation
  - co-occurrence matrix as observed sample statistic that is "explained" by a generative probabilistic model
  - e.g. probabilistic LSA (Hoffmann 1999), Latent Semantic Clustering (Rooth et al. 1999), Latent Dirichlet Allocation (Blei et al. 2003), etc.
  - explicitly accounts for random variation of frequency counts
  - recent work: neural word embeddings
- focus on geometric interpretation in this tutorial

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term-term matrix

define target & feature terms

type & size of co-occurrence

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### Feature scaling

Feature scaling is used to "discount" less important features:

- ▶ Logarithmic scaling:  $O' = \log(O + 1)$ (cf. Weber-Fechner law for human perception)
- ► Relevance weighting, e.g. tf.idf (information retrieval)

$$tf.idf = tf \cdot log(D/df)$$

- ightharpoonup tf = co-occurrence frequency O
- ightharpoonup df = document frequency of feature (or nonzero count)
- $ightharpoonup D = \text{total number of documents (or row count of } \mathbf{M})$
- ► Statistical association measures (Evert 2004, 2008) take frequency of target term and feature into account
  - often based on comparison of observed and expected co-occurrence frequency
  - ▶ measures differ in how they balance O and E

#### geometric analysis probabilistic analysis feature scaling embedding learned by neural network similarity/distance measure + normalization

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### Simple association measures

pointwise Mutual Information (MI)

dimensionality reduction

$$\mathsf{MI} = \log_2 \frac{O}{F}$$

► local MI

$$local-MI = O \cdot MI = O \cdot log_2 \frac{O}{F}$$

t-score

$$t = \frac{O - E}{\sqrt{O}}$$

target	feature	0	Ε	MI	local-MI	t-score
dog	small	855	134.34	2.67	2282.88	24.64
dog	domesticated	29	0.25	6.85	198.76	5.34
dog	sgjkj	1	0.00027	11.85	11.85	1.00

#### Other association measures

▶ simple log-likelihood ( $\approx$  local-MI)

$$G^2 = \pm 2 \cdot \left(O \cdot \log_2 \frac{O}{E} - (O - E)\right)$$

with positive sign for O > E and negative sign for O < E

▶ Dice coefficient

$$\mathsf{Dice} = \frac{2O}{R + C}$$

- ► Many other simple association measures (AMs) available
- ► Further AMs computed from full contingency tables, see
  - Evert (2008)
  - ▶ http://www.collocations.de/
  - ▶ http://sigil.r-forge.r-project.org/

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## Sparse association measures

▶ Sparse association scores are cut off at zero, i.e.

$$f(x) = \begin{cases} x & x > 0 \\ 0 & x \le 0 \end{cases}$$

- ► Also known as "positive" scores
  - ▶ PPMI = positive pointwise MI (e.g. Bullinaria and Levy 2007)
  - ▶ wordspace computes sparse AMs by default → "MI" = PPMI
- $\triangleright$  Preserves sparseness if x < 0 for all empty cells (O = 0)
  - combine with signed AM (x > 0 for O > E, x < 0 for O < E)
  - $\triangleright$  sparseness may even increase: cells with x < 0 become empty
- ► Further thinning may be beneficial (Polajnar and Clark 2014)
  - apply shifted cutoff threshold  $x > \theta$  (Levy et al. 2015)
  - ▶ keep only *k* top-scoring features for each target

# Applying association scores in wordspace

> options(digits=3) # print fractional values with limited precision > dsm.score(TT, score="MI", sparse=FALSE, matrix=TRUE) tail feed kill important explain likely 6.21 4.568 3.129 2.801 -Inf 0.0182 -Inf 3.081 3.922 2.323 -3.774 -1.1888 -0.4958 3.50 2.132 4.747 2.832 -0.674 -0.4677 -0.0966 -1.65 -2.236 -0.729 -1.097 -1.728 -1.2382 0.6392 reason -2.30 -Inf -1.982 -0.388 1.472 4.0368 2.8860 -Inf -0.834 -Inf -2.177 1.900 2.8329 4.0691 effect -Inf -2.116 -2.468 -2.459 0.791 1.6312 0.9221

- sparseness of the matrix has been lost!
- $\bowtie$  cells with score  $x = -\infty$  are inconvenient
- distribution of scores may be even more skewed than co-occurrence frequencies themselves (esp. for local-MI)

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#### Score transformations

An additional scale transformation can be applied in order to de-skew association scores:

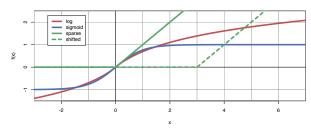
signed logarithmic transformation

$$f(x) = \pm \log(|x| + 1)$$

sigmoid transformation as soft binarization

$$f(x) = \tanh x$$

sparse AM as (shifted) cutoff transformation



# Association scores & transformations in wordspace

```
> dsm.score(TT, score="MI", matrix=TRUE) # PPMI
      breed tail feed kill important explain likely
       6.21 4.57 3.13 2.80
                              0.000 0.0182 0.000
dog
       7.78 3.08 3.92 2.32
                              0.000 0.0000 0.000
animal 3.50 2.13 4.75 2.83
                              0.000 0.0000 0.000
      0.00 0.00 0.00 0.00
                              0.000 0.0000 0.639
reason 0.00 0.00 0.00 0.00
                              1.472 4.0368 2.886
cause 0.00 0.00 0.00 0.00
                              1.900 2.8329 4.069
effect 0.00 0.00 0.00 0.00
                              0.791 1.6312 0.922
> dsm.score(TT, score="simple-ll", matrix=TRUE)
> dsm.score(TT, score="simple-ll", transf="log", matrix=T)
# logarithmic co-occurrence frequency
> dsm.score(TT, score="freq", transform="log", matrix=T)
# now try other parameter combinations
> ?dsm.score # read help page for available parameter settings
```

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#### Scaling of column vectors

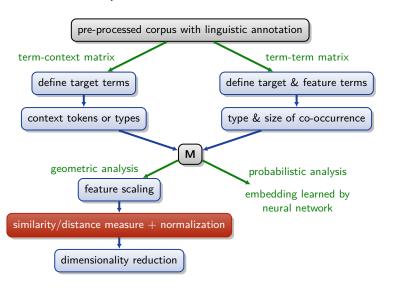
▶ In statistical analysis and machine learning, features are usually centered and scaled so that

mean 
$$\mu = 0$$
 variance  $\sigma^2 = 1$ 

- ▶ In DSM research, this step is less common for columns of M
  - centering is a prerequisite for certain dimensionality reduction and data analysis techniques (esp. PCA)
  - but co-occurrence matrix no longer sparse!
  - scaling may give too much weight to rare features
- ▶ M cannot be row-normalised and column-scaled at the same time (result depends on ordering of the two steps)

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### Overview of DSM parameters



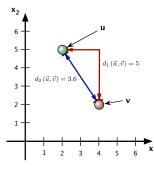
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#### Geometric distance = metric

- Distance between vectors  $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \rightarrow \text{(dis)similarity}$ 
  - $\mathbf{u} = (u_1, \dots, u_n)$   $\mathbf{v} = (v_1, \dots, v_n)$
- **Euclidean** distance  $d_2(\mathbf{u}, \mathbf{v})$
- "City block" Manhattan distance  $d_1(\mathbf{u}, \mathbf{v})$
- ▶ Both are special cases of the Minkowski p-distance  $d_p(\mathbf{u}, \mathbf{v})$ (for  $p \in [1, \infty]$ )



$$d_p(\mathbf{u},\mathbf{v}) := (|u_1 - v_1|^p + \cdots + |u_n - v_n|^p)^{1/p}$$

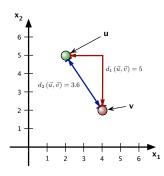
$$d_{\infty}(\mathbf{u},\mathbf{v}) = \max\{|u_1-v_1|,\ldots,|u_n-v_n|\}$$

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#### Geometric distance = metric

- Distance between vectors  $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \rightarrow (dis)$ similarity
  - $\mathbf{u} = (u_1, \ldots, u_n)$  $\mathbf{v} = (v_1, \dots, v_n)$
- **Euclidean** distance  $d_2(\mathbf{u}, \mathbf{v})$
- "City block" Manhattan distance  $d_1(\mathbf{u}, \mathbf{v})$
- $\triangleright$  Extension of p-distance  $d_p(\mathbf{u}, \mathbf{v})$ (for 0 )



$$d_p(\mathbf{u}, \mathbf{v}) := |u_1 - v_1|^p + \dots + |u_n - v_n|^p$$
$$d_0(\mathbf{u}, \mathbf{v}) = \#\{i \mid u_i \neq v_i\}$$

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 $d\left(\vec{u}, \vec{v}\right) = \|\vec{u} - \vec{v}\|$ 

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# Distance and vector length = norm

- ► Intuitively, distance  $d(\mathbf{u}, \mathbf{v})$  should correspond to length  $\|\mathbf{u} - \mathbf{v}\|$  of displacement vector  $\mathbf{u} - \mathbf{v}$ 
  - $\rightarrow$   $d(\mathbf{u}, \mathbf{v})$  is a metric
  - $\|\mathbf{u} \mathbf{v}\|$  is a **norm**
  - $\|\mathbf{u}\| = d(\mathbf{u}, \mathbf{0})$
- Anv norm-induced metric is translation-invariant
- $ightharpoonup d_p(\mathbf{u},\mathbf{v}) = \|\mathbf{u} \mathbf{v}\|_p$
- ▶ Minkowski *p*-norm for  $p \in [1, \infty]$  (not p < 1):

$$\|\mathbf{u}\|_{p} := (|u_{1}|^{p} + \cdots + |u_{n}|^{p})^{1/p}$$

# Computing distances

Preparation: store "scored" matrix in DSM object

> TT <- dsm.score(TT, score="freq", transform="log")

Compute distances between individual term pairs . . .

> pair.distances(c("cat", "cause"), c("animal", "effect"), TT. method="euclidean") cat/animal cause/effect 4.16 1.53

... or full distance matrix.

> dist.matrix(TT, method="euclidean") > dist.matrix(TT, method="minkowski", p=4)

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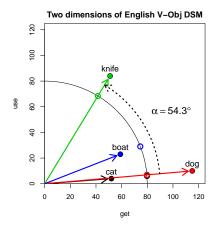
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#### Normalisation of row vectors

- ► Geometric distances only meaningful for vectors of the same length  $\|\mathbf{x}\|$
- Normalize by scalar division:  $\mathbf{x}' = \mathbf{x}/\|\mathbf{x}\| = \left(\frac{x_1}{\|\mathbf{x}\|}, \frac{x_2}{\|\mathbf{x}\|}, \ldots\right)$ with  $\|\mathbf{x}'\| = 1$
- ► Norm must be compatible with distance measure!
- ► Special case: scale to relative frequencies with

$$\|\mathbf{x}\|_1 = |x_1| + \cdots + |x_n|$$

→ probabilistic interpretation



#### Norms and normalization

```
> rowNorms(TT$S, method="euclidean")
         dog animal time reason cause effect
                                  6.86
```

```
> TT <- dsm.score(TT, score="freq", transform="log",
                  normalize=TRUE, method="euclidean")
> rowNorms(TT$S, method="euclidean") # all = 1 now
> dist.matrix(TT, method="euclidean")
        cat dog animal time reason cause effect
      0.000 0.224 0.473 0.782 1.121 1.239 1.161
      0.224 0.000 0.398 0.698 1.065 1.179 1.113
animal 0.473 0.398 0.000 0.426 0.841 0.971 0.860
time 0.782 0.698 0.426 0.000 0.475 0.585 0.502
reason 1.121 1.065 0.841 0.475 0.000 0.277 0.198
cause 1.239 1.179 0.971 0.585 0.277 0.000 0.224
effect 1.161 1.113 0.860 0.502 0.198 0.224 0.000
```

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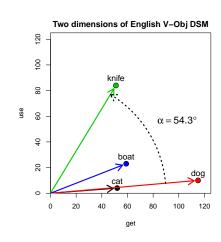
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## Similarity measures

ightharpoonup Angle  $\alpha$  between vectors  $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n$  is given by

$$\cos \alpha = \frac{\sum_{i=1}^{n} u_i \cdot v_i}{\sqrt{\sum_i u_i^2} \cdot \sqrt{\sum_i v_i^2}}$$
$$= \frac{\mathbf{u}^T \mathbf{v}}{\|\mathbf{u}\|_2 \cdot \|\mathbf{v}\|_2}$$

- **cosine** measure of similarity:  $\cos \alpha$ 
  - $ightharpoonup \cos \alpha = 1 \Rightarrow \text{collinear}$
  - $ightharpoonup \cos \alpha = 0 \Rightarrow \text{ orthogonal}$
- Corresponding metric: angular distance  $\alpha$



## Distance measures for non-negative vectors

► Information theory: Kullback-Leibler (KL) divergence for probability vectors ( $\mathbf{x}$  non-negative,  $\|\mathbf{x}\|_1 = 1$ )

$$D(\mathbf{u}||\mathbf{v}) = \sum_{i=1}^{n} u_i \cdot \log_2 \frac{u_i}{v_i}$$

- Properties of KL divergence
  - most appropriate in a probabilistic interpretation of M
  - > zeroes in v without corresponding zeroes in u are problematic
  - not symmetric, unlike geometric distance measures
  - ▶ alternatives: skew divergence, Jensen-Shannon divergence
- ► A symmetric distance metric (Endres and Schindelin 2003)

$$D_{uv} = D(u||z) + D(v||z)$$
 with  $z = \frac{u + v}{2}$ 

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# Euclidean distance or cosine similarity?

$$d_{2}(\mathbf{u}, \mathbf{v}) = \|\mathbf{u} - \mathbf{v}\|_{2} = \sqrt{\sum_{i} (u_{i} - v_{i})^{2}}$$

$$= \sqrt{\sum_{i} u_{i}^{2} + \sum_{i} v_{i}^{2} - 2\sum_{i} u_{i}v_{i}}$$

$$= \sqrt{\|\mathbf{u}\|_{2}^{2} + \|\mathbf{v}\|_{2}^{2} - 2\mathbf{u}^{T}\mathbf{v}}$$

$$= \sqrt{2 - 2\cos\phi}$$

 $d_2(\mathbf{u},\mathbf{v})$  is a monotonically increasing function of  $\phi$ 

Euclidean distance and cosine similarity are equivalent: if vectors have been normalised ( $\|\mathbf{u}\|_2 = \|\mathbf{v}\|_2 = 1$ ), both lead to the same neighbour ranking.

#### Similarity measures for non-negative vectors

► Generalized **Jaccard coefficient** = shared features

$$J(\mathbf{u}, \mathbf{v}) = \frac{\sum_{i=1}^{n} \min\{u_i, v_i\}}{\sum_{i=1}^{n} \max\{u_i, v_i\}}$$

- $ightharpoonup 1 J(\mathbf{u}, \mathbf{v})$  is a distance **metric** (Kosub 2016)
- ► An asymmetric measure of feature overlap (Clarke 2009)

$$o(\mathbf{u},\mathbf{v}) = \frac{\sum_{i=1}^{n} \min\{u_i,v_i\}}{\sum_{i=1}^{n} u_i}$$

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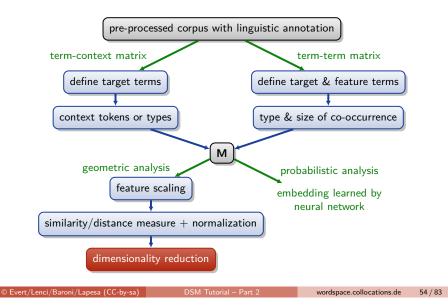
## Dimensionality reduction = model compression

- ► Co-occurrence matrix **M** is often unmanageably large and can be extremely sparse
  - ▶ Google Web1T5: 1M × 1M matrix with one trillion cells, of which less than 0.05% contain nonzero counts (Evert 2010)

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- Compress matrix by reducing dimensionality (= rows)
- **Feature selection**: columns with high frequency & variance
  - measured by entropy, chi-squared test, nonzero count, ...
  - may select similar dimensions and discard valuable information
- ► Projection into (linear) subspace
  - principal component analysis (PCA)
  - ▶ independent component analysis (ICA)
  - random indexing (RI)
  - intuition: preserve distances between data points

### Overview of DSM parameters



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# Dimensionality reduction & latent dimensions

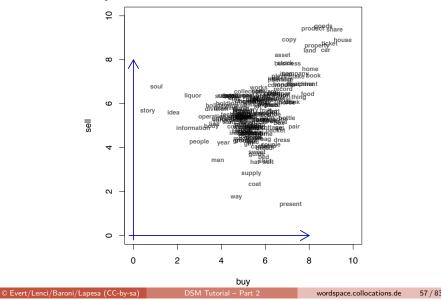
Landauer and Dumais (1997) claim that LSA dimensionality reduction (and related PCA technique) uncovers latent dimensions by exploiting correlations between features.

- Example: term-term matrix
- V-Obj co-oc. extracted from BNC
  - ▶ targets = noun lemmas
  - ▶ features = verb lemmas
- ► feature scaling: association scores (SketchEngine log Dice)
- k = 186 nouns with  $f_{buv} + f_{sell} \ge 25$
- $ightharpoonup n = 2 ext{ dimensions: } buy ext{ and } sell$

buy	sell
5.12	5.50
5.96	3.99
6.75	6.83
4.95	4.72
4.93	4.28
5.11	5.73
5.14	5.41
3.00	4.26
6.81	6.68
5.45	4.67
8.93	8.74
	5.12 5.96 6.75 4.95 4.93 5.11 5.14 3.00 6.81 5.45

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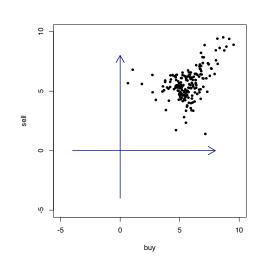
# Dimensionality reduction & latent dimensions



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# Step 1: Centering the data set

- Uncentered data set
- Centered data set
- Distance information = variance



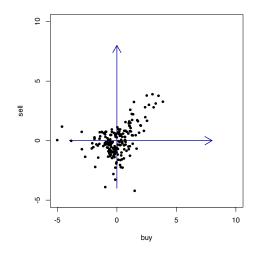
# Motivating latent dimensions & subspace projection

- ▶ The **latent property** of being a commodity is "expressed" through associations with several verbs: sell, buy, acquire, . . .
- ► Consequence: these DSM dimensions will be correlated
- ▶ Identify latent dimension by looking for strong correlations (or weaker correlations between large sets of features)
- ightharpoonup Projection into subspace V of k < n latent dimensions as a "noise reduction" technique → LSA
- ► Assumptions of this approach:
  - ▶ "latent" distances in V are semantically meaningful
  - other "residual" dimensions represent chance co-occurrence patterns, often particular to the corpus underlying the DSM

DSM parameters A taxonomy of DSM parameters

# Step 1: Centering the data set

- Uncentered data set
- Centered data set
- Distance information = variance

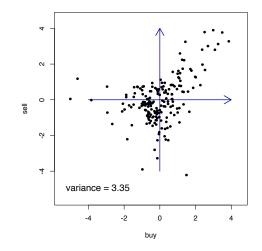


Step 2: Orthogonal projection into optimal subspace

# Step 1: Centering the data set

- Uncentered data set
- Centered data set
- Distance information = variance

$$\sigma^2 = \frac{1}{k-1} \sum_{i=1}^k ||\mathbf{x}^{(i)}||^2$$



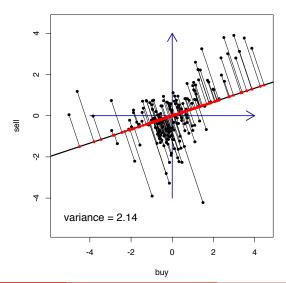
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α

variance = 0.98 buy

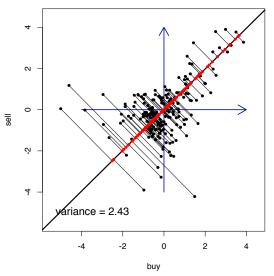
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# Step 2: Orthogonal projection into optimal subspace



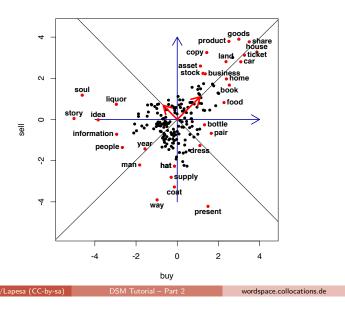
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Step 2: Orthogonal projection into optimal subspace



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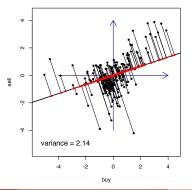
# Step 3: Further orthogonal dimensions



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## Dimensionality reduction by RI

- ► Random indexing (RI)
  - project into random subspace (Sahlgren and Karlgren 2005)
  - ▶ reasonably good if there are many subspace dimensions
  - ► can be performed online w/o collecting full co-oc. matrix



# Dimensionality reduction by PCA

- Principal component analysis (PCA)
  - orthogonal projection into orthogonal latent dimensions
  - finds optimal subspace of given dimensionality (such that orthogonal projection preserves distance information)
  - ▶ but requires centered features → no longer sparse
- Singular value decomposition (SVD)
  - the mathematical algorithm behind PCA
  - often applied without centering in distributional semantics
  - ▶ optimality of subspace not guaranteed (☞ part 5)
- ▶ NB: row vectors should be renormalised after PCA/SVD
  - unless cosine similarity / angular distance is used
  - also normalise vectors before dimensionality reduction

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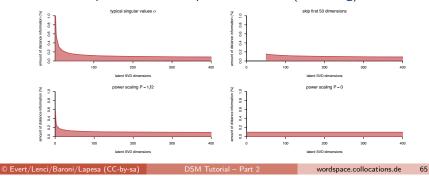
## Dimensionality reduction in practice

```
# it is customary to omit the centering: SVD dimensionality reduction
> TT2 <- dsm.projection(TT, n=2, method="svd")
> TT2
         svd1
                 svd2
       -0.733 - 0.6615
       -0.782 -0.6110
animal -0.914 -0.3606
       -0.993 0.0302
reason -0.889 0.4339
cause -0.817 0.5615
effect -0.871 0.4794
> x <- TT2[, 1] # first latent dimension
> y <- TT2[, 2] # second latent dimension
> plot(x, y, pch=20, col="red",
       xlim=extendrange(x), ylim=extendrange(y))
> text(x, y, rownames(TT2), pos=3)
```

#### A taxonomy of DSM parameters

# Scaling latent dimensions

- ► Capture different amounts of distance info (= variance)
- ▶ Indicated by singular values  $\sigma_i$  of PCA/SVD algorithm
- $\blacktriangleright$  Skip first k dimensions, e.g. k=50 (Bullinaria and Levy 2012)
- ▶ Power-scaling of dimensions:  $\sigma^P$  (Caron 2001)
  - ▶ Bullinaria and Levy (2012) report positive effect
  - ightharpoonup esp. with P=0 to equalize dimensions (whitening)



DSM parameters

#### Outline

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A taxonomy of DSM parameters

Examples

Example: a verb-object DSM

# Power-scaling in practice

```
> TT2 <- dsm.projection(TT, n=2, method="svd", power=0)
> TT2
         svd1
                 svd2
cat
       -0.322 -0.5110
       -0.343 -0.4721
animal -0.401 -0.2786
       -0.436 0.0233
reason -0.390 0.3353
cause -0.359 0.4338
effect -0.383 0.3704
# power-scaling can also be applied post-hoc
> sigma <- attr(TT2, "sigma")</pre>
                                        # singular values
> scaleMargins(TT2, cols=sigma^0.5) \# P = 1/2
> scaleMargins(TT2, cols=sigma)
                                       \# unscaled (P = 1)
```

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DSM parameters Examples

# Some well-known DSM examples

#### Latent Semantic Analysis (Landauer and Dumais 1997)

- term-context matrix with document context
- weighting: log term frequency and term entropy
- distance measure: cosine
- ▶ dimensionality reduction: SVD

#### Hyperspace Analogue to Language (Lund and Burgess 1996)

- term-term matrix with surface context
- ▶ structured (left/right) and distance-weighted frequency counts
- b distance measure: Minkowski metric  $(1 \le p \le 2)$
- ▶ dimensionality reduction: feature selection (high variance)

DSM parameters Examples

# Some well-known DSM examples

#### Infomap NLP (Widdows 2004)

term-term matrix with unstructured surface context

weighting: none

distance measure: cosine

dimensionality reduction: SVD

#### Random Indexing (Karlgren and Sahlgren 2001)

term-term matrix with unstructured surface context

weighting: various methods

distance measure: various methods

▶ dimensionality reduction: random indexing (RI)

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Building a DSM Sparse matrices

#### Outline

A taxonomy of DSM parameters

#### Building a DSM

Sparse matrices

Example: a verb-object DSM

# Some well-known DSM examples

#### Dependency Vectors (Padó and Lapata 2007)

▶ term-term matrix with unstructured dependency context

▶ weighting: log-likelihood ratio

▶ distance measure: PPMI-weighted Dice (Lin 1998)

▶ dimensionality reduction: none

#### Distributional Memory (Baroni and Lenci 2010)

term-term matrix with structured and unstructered dependencies + knowledge patterns

weighting: local-MI on type frequencies of link patterns

distance measure: cosine

dimensionality reduction: none

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Sparse matrices

# Scaling up to the real world

- ► So far, we have worked on minuscule toy models
- We want to scale up to real world data sets now
- ► Example 1: window-based DSM on BNC content words
  - ▶ 83,926 lemma types with f > 10
  - $\blacktriangleright$  term-term matrix with 83.926  $\cdot$  83.926 = 7 billion entries
  - standard representation requires 56 GB of RAM (8-byte floats)
  - $\triangleright$  only 22.1 million non-zero entries (= 0.32%)
- ► Example 2: Google Web 1T 5-grams (1 trillion words)
  - ▶ more than 1 million word types with f > 2500
  - term-term matrix with 1 trillion entries requires 8 TB RAM
  - only 400 million non-zero entries (= 0.04%)

Building a DSM Sparse matrices

# Sparse matrix representation

► Invented example of a sparsely populated DSM matrix

	eat	get	hear	kill	see	use
boat		59	•		39	23
cat		•		26	58	
cup		98		•		
dog knife	33	•	42	•	83	
knife		•		•	•	84
pig	9		•	27	•	

► Store only non-zero entries in compact sparse matrix format

row	col	value	row	col	value
1	2	59	4	1	33
1	5	39	4	3	42
1	6	23	4	5	83
2	4	26	5	6	84
2	5	58	6	1	9
3	2	98	6	4	27

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Building a DSM Example: a verb-object DSM

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A taxonomy of DSM parameters

#### Building a DSM

Example: a verb-object DSM

# Working with sparse matrices

- Compressed format: each row index (or column index) stored only once, followed by non-zero entries in this row (or column)
  - convention: column-major matrix (data stored by columns)
- Specialised algorithms for sparse matrix algebra
  - especially matrix multiplication, solving linear systems, etc.
  - take care to avoid operations that create a dense matrix!
- ▶ R implementation: Matrix package
  - essential for real-life distributional semantics
  - wordspace provides additional support for sparse matrices (vector distances, sparse SVD, ...)
- ▶ Other software: Matlab, Octave, Python + SciPy

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Building a DSM Example: a verb-object DSM

## Triplet tables

- ► A sparse DSM matrix can be represented as a table of triplets (target, feature, co-occurrence frequency)
  - ▶ for syntactic co-occurrence and term-document matrices, marginals can be computed from a complete triplet table
  - ▶ for surface and textual co-occurrence, marginals have to be provided in separate files (see ?read.dsm.triplet)

noun	rel	verb	f	mode
dog	subj	bite	3	spoken
dog	subj	bite	12	written
dog	obj	bite	4	written
dog	obj	stroke	3	written

- ▶ DSM\_VerbNounTriples\_BNC contains additional information
  - syntactic relation between noun and verb
  - written or spoken part of the British National Corpus

Building a DSM Example: a verb-object DSM

#### Example: a verb-object DSM

# Constructing a DSM from a triplet table

▶ Additional information can be used for filtering (verb-object relation), or aggregate frequencies (spoken + written BNC)

```
> tri <- subset(DSM VerbNounTriples BNC, rel == "obj")</pre>
```

- Construct DSM object from triplet input
  - ► raw.freg=TRUE indicates raw co-occurrence frequencies (rather than a pre-weighted DSM)
  - constructor aggregates counts from duplicate entries
  - marginal frequencies are automatically computed

```
> VObj <- dsm(target=tri$noun, feature=tri$verb,
              score=tri$f, raw.freq=TRUE)
```

> VObj # inspect marginal frequencies (e.g. head(VObj\$rows, 20))

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Building a DSM

Example: a verb-object DSM

## **Practice**

- ► How many different models can you build from DSM VerbNounTriples BNC?
- ► Apply different filters, scores, transformations and metrics explore nearest neighbours of selected words
- Code examples for this part show additional options
- Download practice session (part2\_input\_formats.R)
  - → different ways of loading your own co-occurrence data
- ▶ Build real-life DSMs from pre-compiled co-occurrence data
  - http://wordspace.collocations.de/doku.php/course:material
  - ▶ also download R script with instructions (part2 exercise.R)

# Exploring the DSM

```
> VObj <- dsm.score(VObj, score="MI", normalize=TRUE)
> nearest.neighbours(VObj, "dog") # angular distance
   horse
             cat
                   animal
                            rabbit
                                       fish
                                                guy
   73.9
            75.9
                     76.2
                              77.0
                                       77.2
                                               78.5
 cichlid
             kid
                      bee creature
   78.6
            79.0
                     79.1
                              79.5
> nearest.neighbours(VObj, "dog", method="manhattan")
# NB: we used an incompatible Euclidean normalization!
> VObj50 <- dsm.projection(VObj, n=50, method="svd")
> nearest.neighbours(VObj50, "dog")
```

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Example: a verb-object DSM

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Example: a verb-object DSM

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