Distributional Semantic Models

Part 2: The parameters of a DSM

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http://wordspace.collocations.de/doku.php/course:start

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DSM parameters A taxonomy of DSM parameters

Outline

DSM parameters

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Outline

DSM parameters

A taxonomy of DSM parameters Examples

Scaling up

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Overview of DSM parameters

Term-context vs. term-term matrix

Definition of terms & linguistic pre-processing

Size & type of context

Geometric vs. probabilistic interpretation

Feature scaling

Normalisation of rows and/or columns

Similarity / distance measure



Dimensionality reduction

Term-context matrix

Term-context matrix records frequency of term in each individual context (e.g. sentence, document, Web page, encyclopaedia article)

$$\mathbf{F} = egin{bmatrix} \cdots & \mathbf{f}_1 & \cdots \\ \cdots & \mathbf{f}_2 & \cdots \\ & dots \\ & dots \\ \cdots & \mathbf{f}_k & \cdots \end{bmatrix}$$

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cat	10	10	/	_	_		_
dog	_	10	4	11	_	_	_
animal	2	15	10	2	_	_	_
time	1	_	_	_	2	1	_
reason	_	1	-	_	1	4	1
cause	_	_	-	2	1	2	6
effect	_	_	-	1	_	1	_

24

Term-context matrix

Some footnotes:

- ▶ Features are usually context tokens, i.e. individual instances
- ► Can also be generalised to context types, e.g.
 - bag of content words
 - specific pattern of POS tags
 - n-gram of words (or POS tags) around target
 - subcategorisation pattern of target verb
- ► Term-context matrix is often very **sparse**

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Term-term matrix

Term-term matrix records co-occurrence frequencies with feature terms for each target term

$$\mathbf{M} = \begin{bmatrix} \cdots & \mathbf{m}_1 & \cdots \\ \cdots & \mathbf{m}_2 & \cdots \\ & \vdots & \\ \vdots & \vdots & \\ \cdots & \mathbf{m}_k & \cdots \end{bmatrix}$$

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	4	taji	, seed	kill	.[4]	* 4×	1/1/20
cat	83	17	7	37	_	1	_
dog	561	13	30	60	1	2	4
nimal	42	10	109	134	13	5	5
time	19	9	29	117	81	34	109
eason	1	_	2	14	68	140	47
cause	_	1	_	4	55	34	55
effect	_	-	1	6	60	35	17

we will usually assume a term-term matrix in this tutorial

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Term-term matrix

Some footnotes:

- \triangleright Often target terms \neq feature terms
 - e.g. nouns described by co-occurrences with verbs as features
 - ▶ identical sets of target & feature terms → symmetric matrix
- ▶ Different types of contexts (Evert 2008)
 - surface context (word or character window)
 - textual context (non-overlapping segments)
 - syntactic contxt (specific syntagmatic relation)
- ► Can be seen as smoothing of term-context matrix
 - average over similar contexts (with same context terms)
 - data sparseness reduced, except for small windows
 - we will take a closer look at the relation between term-context and term-term models later in this tutorial

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Overview of DSM parameters

Term-context vs. term-term matrix Definition of terms & linguistic pre-processing Size & type of context Geometric vs. probabilistic interpretation Feature scaling Normalisation of rows and/or columns Similarity / distance measure Dimensionality reduction

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Corpus pre-processing

- ▶ Minimally, corpus must be tokenised → identify terms
- Linguistic annotation
 - part-of-speech tagging
 - lemmatisation / stemming
 - word sense disambiguation (rare)
 - shallow syntactic patterns
 - dependency parsing
- ► Generalisation of terms
 - often lemmatised to reduce data sparseness: go, goes, went, gone, going → go
 - ► POS disambiguation (light/N vs. light/A vs. light/V)
 - ▶ word sense disambiguation (bank_{river} vs. bank_{finance})
- ▶ Trade-off between deeper linguistic analysis and
 - need for language-specific resources
 - possible errors introduced at each stage of the analysis

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Effects of pre-processing

Nearest neighbours of walk (BNC)

word forms

- stroll
- walking
- walked
- ▶ go
- path
- drive
- ▶ ride
- wander
- sprinted
- sauntered

lemmatised corpus

- hurry
- stroll
- stride
- trudge
- amble
- wander walk-nn
- walking
- retrace
- scuttle

raggiunge arrivasse arriverà

Effects of pre-processing

Nearest neighbours of arrivare (Repubblica)

word forms

- giungere
- raggiungere
- arrivi
- raggiungimento
- raggiunto
- trovare
- concludere

lemmatised corpus

- giungere
- aspettare
- attendere
- arrivo-nn
- ricevere
- accontentare
- approdare
- pervenire
- venire
- piombare

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Effects of pre-processing

1. Colours seem to indicate inflected forms belonging to the same lemma.

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Surface context

Context term occurs within a window of k words around target.

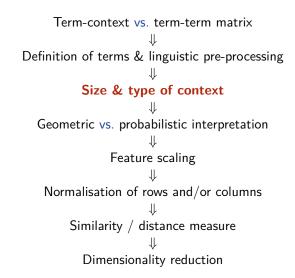
The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

- window size (in words or characters)
- symmetric vs. one-sided window
- uniform or "triangular" (distance-based) weighting
- window clamped to sentences or other textual units?

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Effect of different window sizes

Nearest neighbours of dog (BNC)

2-word window

- ▶ cat
- horse ► fox
- pet rabbit
- pig
- animal
- mongrel
- sheep
- pigeon

30-word window

- kennel
- puppy
- pet
- bitch
- rottweiler
- canine
- to bark
- Alsatian

A taxonomy of DSM parameters

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Textual context

Context term is in the same linguistic unit as target.

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

- type of linguistic unit
 - sentence
 - paragraph
 - ▶ turn in a conversation
 - Web page

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"Knowledge pattern" context

Context term is linked to target by a lexico-syntactic pattern (text mining, cf. Hearst 1992, Pantel & Pennacchiotti 2008, etc.).

In Provence, Van Gogh painted with bright colors such as red and yellow. These colors produce incredible effects on anybody looking at his paintings.

Parameters:

- inventory of lexical patterns
 - ▶ lots of research to identify semantically interesting patterns (cf. Almuhareb & Poesio 2004, Veale & Hao 2008, etc.)
- fixed vs. flexible patterns
 - patterns are mined from large corpora and automatically generalised (optional elements, POS tags or semantic classes)

Syntactic context

Context term is linked to target by a syntactic dependency (e.g. subject, modifier, ...).

The silhouette of the sun beyond a wide-open bay on the lake; the sun still glitters although evening has arrived in Kuhmo. It's midsummer; the living room has its instruments and other objects in each of its corners.

Parameters:

- types of syntactic dependency (Padó and Lapata 2007)
- ▶ direct vs. indirect dependency paths
 - direct dependencies
 - direct + indirect dependencies
- homogeneous data (e.g. only verb-object) vs. heterogeneous data (e.g. all children and parents of the verb)
- maximal length of dependency path

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Structured vs. unstructured context

- ▶ In unstructered models, context specification acts as a filter
 - determines whether context token counts as co-occurrence
 - e.g. linked by specific syntactic relation such as verb-object
- ▶ In structured models, context words are subtyped
 - depending on their position in the context
 - e.g. left vs. right context, type of syntactic relation, etc.

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Structured vs. unstructured surface context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

A dog bites a man. The man's dog bites a dog. A dog bites a man.

structured	bite-l	bite-ı
dog	3	1
man	1	2

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Structured vs. unstructured dependency context

A dog bites a man. The man's dog bites a dog. A dog bites a man.

A dog bites a man. The man's dog bites a dog. A dog bites a man.

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Comparison

- Unstructured context
 - ▶ data less sparse (e.g. man kills and kills man both map to the *kill* dimension of the vector \mathbf{x}_{man})
- Structured context
 - more sensitive to semantic distinctions (kill-subj and kill-obj are rather different things!)
 - dependency relations provide a form of syntactic "typing" of the DSM dimensions (the "subject" dimensions, the "recipient" dimensions, etc.)
 - ▶ important to account for word-order and compositionality

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Geometric vs. probabilistic interpretation

- Geometric interpretation
 - row vectors as points or arrows in *n*-dim. space
 - very intuitive, good for visualisation
 - use techniques from geometry and linear algebra
- Probabilistic interpretation
 - co-occurrence matrix as observed sample statistic
 - "explained" by generative probabilistic model
 - recent work focuses on hierarchical Bayesian models
 - probabilistic LSA (Hoffmann 1999), Latent Semantic Clustering (Rooth et al. 1999), Latent Dirichlet Allocation (Blei et al. 2003), etc.
 - explicitly accounts for random variation of frequency counts
 - ▶ intuitive and plausible as topic model

focus on geometric interpretation in this tutorial

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Feature scaling

Feature scaling is used to "discount" less important features:

- ▶ Logarithmic scaling: $x' = \log(x + 1)$ (cf. Weber-Fechner law for human perception)
- ► Relevance weighting, e.g. tf.idf (information retrieval)
- ► Statistical association measures (Evert 2004, 2008) take frequency of target word and context feature into account
 - ▶ the less frequent the target word and (more importantly) the context feature are, the higher the weight given to their observed co-occurrence count should be (because their expected chance co-occurrence frequency is low)
 - ▶ different measures e.g., mutual information, log-likelihood ratio – differ in how they balance observed and expected co-occurrence frequencies

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Association measures: Mutual Information (MI)

$word_1$	$word_2$	$f_{\sf obs}$	f_1	f_2
dog	small	855	33,338	490,580
dog	domesticated	29	33,338	918

Expected co-occurrence frequency:

$$f_{\text{exp}} = \frac{f_1 \cdot f_2}{N}$$

Mutual Information compares observed vs. expected frequency:

$$\mathsf{MI}(w_1, w_2) = \log_2 \frac{f_{\mathsf{obs}}}{f_{\mathsf{exp}}} = \log_2 \frac{N \cdot f_{\mathsf{obs}}}{f_1 \cdot f_2}$$

Disadvantage: MI overrates combinations of rare terms.

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Other association measures

$word_1$	$word_2$	$f_{\sf obs}$	$f_{\sf exp}$	MI	local-MI	t-score
dog	small	855	134.34	2.67	2282.88	24.64
dog	domesticated	29	0.25	6.85	198.76	5.34
dog	sgjkj	1	0.00027	11.85	11.85	1.00

The log-likelihood ratio (Dunning 1993) has more complex form, but its "core" is known as local MI (Evert 2004).

$$local-MI(w_1, w_2) = f_{obs} \cdot MI(w_1, w_2)$$

The t-score measure (Church and Hanks 1990) is popular in lexicography:

t-score
$$(w_1, w_2) = \frac{f_{\text{obs}} - f_{\text{exp}}}{\sqrt{f_{\text{obs}}}}$$

Details & many more measures: http://www.collocations.de/

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Normalisation of row vectors

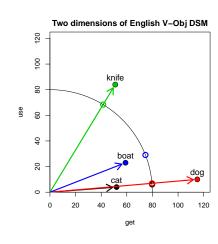
- geometric distances only make sense if vectors are normalised to unit length
- divide vector by its length:

$$\mathbf{x}/\|\mathbf{x}\|$$

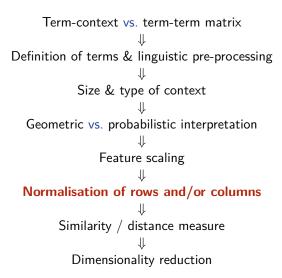
- normalisation depends on distance measure!
- special case: scale to relative frequencies with

$$\|\mathbf{x}\|_1 = |x_1| + \cdots + |x_n|$$

→ probabilistic interpretation



Overview of DSM parameters



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Scaling of column vectors

▶ In statistical analysis and machine learning, features are usually centred and scaled so that

mean
$$\mu=0$$
 variance $\sigma^2=1$

- ▶ In DSM research, this step is less common for columns of M
 - centring is a prerequisite for certain dimensionality reduction and data analysis techniques (esp. PCA)
 - scaling may give too much weight to rare features
 - co-occurrence matrix no longer sparse after centring!
- ▶ M cannot be row-normalised and column-scaled at the same time (result depends on ordering of the two steps)

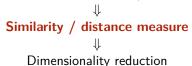
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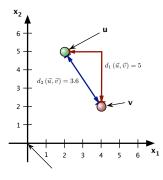
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Geometric distance

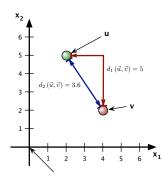
- ▶ Distance between vectors $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \rightarrow (dis)$ similarity
 - $\mathbf{v} = (u_1, \ldots, u_n)$
 - $\mathbf{v} = (v_1, \dots, v_n)$
- **Euclidean** distance $d_2(\mathbf{u}, \mathbf{v})$
- "City block" Manhattan distance $d_1(\mathbf{u}, \mathbf{v})$
- \triangleright Extension of p-distance $d_p(\mathbf{u}, \mathbf{v})$ (for $0 \le p \le 1$)



$$d_p(\mathbf{u}, \mathbf{v}) := |u_1 - v_1|^p + \dots + |u_n - v_n|^p$$
$$d_0(\mathbf{u}, \mathbf{v}) = \#\{i \mid u_i \neq v_i\}$$

Geometric distance

- ► **Distance** between vectors $\mathbf{u}, \mathbf{v} \in \mathbb{R}^n \rightarrow (dis)$ similarity
 - $\mathbf{u} = (u_1, \dots, u_n)$
 - $\mathbf{v} = (v_1, \dots, v_n)$
- **Euclidean** distance $d_2(\mathbf{u}, \mathbf{v})$
- ► "City block" Manhattan distance $d_1(\mathbf{u}, \mathbf{v})$
- ▶ Both are special cases of the Minkowski p-distance $d_p(\mathbf{u}, \mathbf{v})$ (for $p \in [1, \infty]$)



$$d_p(\mathbf{u}, \mathbf{v}) := (|u_1 - v_1|^p + \dots + |u_n - v_n|^p)^{1/p}$$

$$d_{\infty}(\mathbf{u}, \mathbf{v}) = \max\{|u_1 - v_1|, \dots, |u_n - v_n|\}$$

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Metric: a measure of distance

- \blacktriangleright A metric is a general measure of the distance $d(\mathbf{u}, \mathbf{v})$ between points **u** and **v**, which satisfies the following axioms:
 - $d(\mathbf{u},\mathbf{v}) = d(\mathbf{v},\mathbf{u})$
 - $d(\mathbf{u},\mathbf{v}) > 0$ for $\mathbf{u} \neq \mathbf{v}$
 - $d(\mathbf{u}, \mathbf{u}) = 0$
 - $d(\mathbf{u}, \mathbf{w}) < d(\mathbf{u}, \mathbf{v}) + d(\mathbf{v}, \mathbf{w})$ (triangle inequality)
- ▶ Metrics form a very broad class of distance measures, some of which do not fit in well with our geometric intuitions
- ► E.g., metric need not be translation-invariant

$$d(\mathbf{u} + \mathbf{x}, \mathbf{v} + \mathbf{x}) \neq d(\mathbf{u}, \mathbf{v})$$

► Another unintuitive example is the discrete metric

$$d(\mathbf{u}, \mathbf{v}) = \begin{cases} 0 & \mathbf{u} = \mathbf{v} \\ 1 & \mathbf{u} \neq \mathbf{v} \end{cases}$$

Distance vs. norm

- ► Intuitively, **distance** $d(\mathbf{u}, \mathbf{v})$ should correspond to **length** $\|\mathbf{u} - \mathbf{v}\|$ of displacement vector $\mathbf{u} - \mathbf{v}$
 - \rightarrow $d(\mathbf{u}, \mathbf{v})$ is a metric
 - ▶ $\|\mathbf{u} \mathbf{v}\|$ is a **norm**
 - ||u|| = d(u, 0)
- ► Such a metric is always translation-invariant



- $d_{p}(\mathbf{u},\mathbf{v}) = \|\mathbf{v} \mathbf{u}\|_{p}$
- ▶ Minkowski *p*-norm for $p \in [1, \infty]$ (not p < 1):

$$\|\mathbf{u}\|_{p} := (|u_{1}|^{p} + \cdots + |u_{n}|^{p})^{1/p}$$

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Other distance measures

Information theory: Kullback-Leibler (KL) divergence for probability vectors (non-negative, $\|\mathbf{x}\|_1 = 1$)

$$D(\mathbf{u}||\mathbf{v}) = \sum_{i=1}^n u_i \cdot \log_2 \frac{u_i}{v_i}$$

- Properties of KL divergence
 - most appropriate in a probabilistic interpretation of M
 - > zeroes in v without corresponding zeroes in u are problematic
 - ▶ not symmetric, unlike geometric distance measures
 - ▶ alternatives: skew divergence, Jensen-Shannon divergence
- A symmetric distance measure (Endres and Schindelin 2003)

$$D_{\mathbf{u}\mathbf{v}} = D(\mathbf{u}\|\mathbf{z}) + D(\mathbf{v}\|\mathbf{z})$$
 with $\mathbf{z} = \frac{\mathbf{u} + \mathbf{v}}{2}$

Norm: a measure of length

- ▶ A general **norm** ||**u**|| for the length of a vector **u** must satisfy the following axioms:
 - ▶ ||u|| > 0 for $u \neq 0$
 - ▶ $\|\lambda \mathbf{u}\| = |\lambda| \cdot \|\mathbf{u}\|$ (homogeneity, not req'd for metric)
 - ▶ $\|\mathbf{u} + \mathbf{v}\| \le \|\mathbf{u}\| + \|\mathbf{v}\|$ (triangle inequality)
- every norm defines a translation-invariant metric

$$d(\mathbf{u},\mathbf{v}) := \|\mathbf{u} - \mathbf{v}\|$$

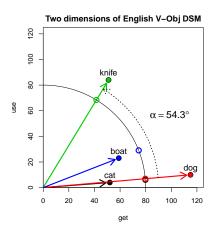
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Similarity measures

ightharpoonup angle α between two vectors \mathbf{u}, \mathbf{v} is given by

$$\cos \alpha = \frac{\sum_{i=1}^{n} u_i \cdot v_i}{\sqrt{\sum_i u_i^2} \cdot \sqrt{\sum_i v_i^2}}$$
$$= \frac{\langle \mathbf{u}, \mathbf{v} \rangle}{\|\mathbf{u}\|_2 \cdot \|\mathbf{v}\|_2}$$

- **cosine** measure of similarity: $\cos \alpha$
 - $ightharpoonup \cos \alpha = 1 \rightarrow \text{collinear}$
 - ightharpoonup cos $\alpha = 0 \Rightarrow$ orthogonal
- \blacktriangleright distance metric: α



Euclidean distance or cosine similarity?

- ▶ Which is better, Euclidean distance or cosine similarity?
- ▶ They are equivalent: if vectors are normalised ($\|\mathbf{u}\|_2 = 1$), both lead to the same neighbour ranking

$$d_{2}(\mathbf{u}, \mathbf{v}) = \sqrt{\|\mathbf{u} - \mathbf{v}\|_{2}} = \sqrt{\langle \mathbf{u} - \mathbf{v}, \mathbf{u} - \mathbf{v} \rangle}$$

$$= \sqrt{\langle \mathbf{u}, \mathbf{u} \rangle + \langle \mathbf{v}, \mathbf{v} \rangle - 2 \langle \mathbf{u}, \mathbf{v} \rangle}$$

$$= \sqrt{\|\mathbf{u}\|_{2} + \|\mathbf{v}\|_{2} - 2 \langle \mathbf{u}, \mathbf{v} \rangle}$$

$$= \sqrt{2 - 2\cos\phi}$$

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Dimensionality reduction = model compression

- ► Co-occurrence matrix **M** is often unmanageably large and can be extremely sparse
 - ▶ Google Web1T5: 1M × 1M matrix with one trillion cells, of which less than 0.05% contain nonzero counts (Evert 2010)
- Compress matrix by reducing dimensionality (= rows)
- ► Feature selection: columns with high frequency & variance
 - measured by entropy, chi-squared test, ...
 - ▶ may select correlated (→ uninformative) dimensions
 - joint selection of multiple features is useful but expensive
- Projection into (linear) subspace
 - principal component analysis (PCA)
 - independent component analysis (ICA)
 - random indexing (RI)
 - intuition: preserve distances between data points

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Dimensionality reduction & latent dimensions

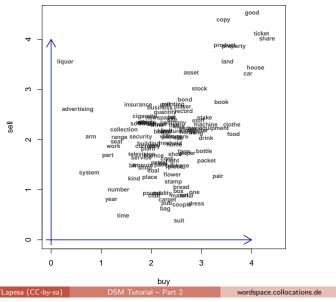
Landauer and Dumais (1997) claim that LSA dimensionality reduction (and related PCA technique) uncovers latent dimensions by exploiting correlations between features.

- Example: term-term matrix
- ▶ V-Obj cooc's extracted from BNC
 - ► targets = noun lemmas
 - ► features = verb lemmas
- ▶ feature scaling: association scores (modified log Dice coefficient)
- k = 111 nouns with f > 20(must have non-zero row vectors)
- ightharpoonup n = 2 dimensions: buy and sell

noun	buy	seli
bond	0.28	0.77
cigarette	-0.52	0.44
dress	0.51	-1.30
freehold	-0.01	-0.08
land	1.13	1.54
number	-1.05	-1.02
per	-0.35	-0.16
pub	-0.08	-1.30
share	1.92	1.99
system	-1.63	-0.70

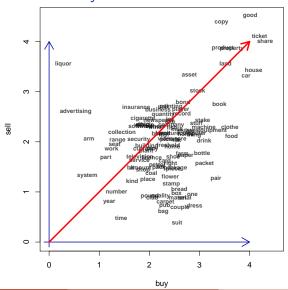
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Dimensionality reduction & latent dimensions



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The latent "commodity" dimension



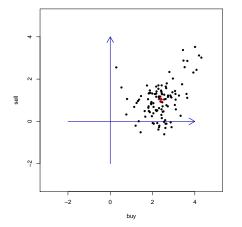
Motivating latent dimensions & subspace projection

- ▶ The **latent property** of being a commodity is "expressed" through associations with several verbs: sell, buy, acquire, . . .
- ► Consequence: these DSM dimensions will be correlated
- ▶ Identify latent dimension by looking for strong correlations (or weaker correlations between large sets of features)
- ▶ Projection into subspace V of k < n latent dimensions as a "noise reduction" technique → LSA
- ► Assumptions of this approach:
 - ▶ "latent" distances in *V* are semantically meaningful
 - ▶ other "residual" dimensions represent chance co-occurrence patterns, often particular to the corpus underlying the DSM

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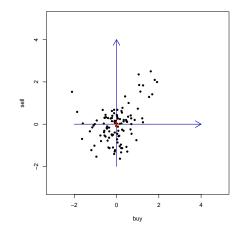
Centering the data set

- Uncentered data set
- Centered data set
- Variance of centered data



Centering the data set

- Uncentered data set
- Centered data set
- Variance of centered data

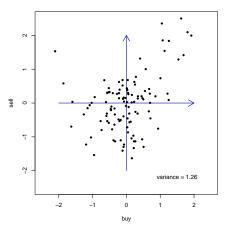


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Centering the data set

- Uncentered data set
- Centered data set
- ► Variance of centered data

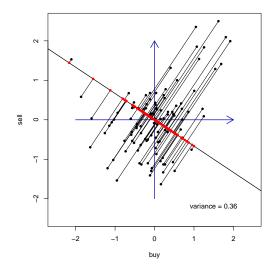
$$\sigma^2 = \frac{1}{k-1} \sum_{i=1}^k \|\mathbf{x}^{(i)}\|^2$$



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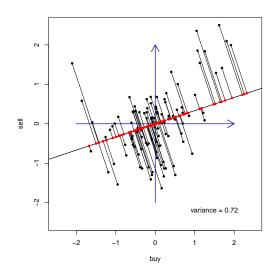
DSM parameters A taxonomy of DSM parameters

Projection and preserved variance: examples

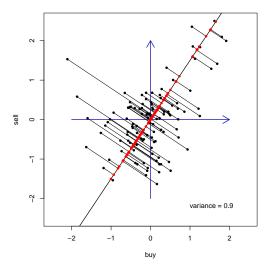


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Projection and preserved variance: examples



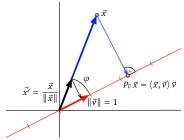
Projection and preserved variance: examples



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The mathematics of projections

- ► Line through origin given by unit vector $\|\mathbf{v}\| = 1$
- ► For a point **x** and the corresponding unit vector $\mathbf{x}' = \mathbf{x}/\|\mathbf{x}\|$, we have $\cos \varphi = \langle \mathbf{x}', \mathbf{v} \rangle$



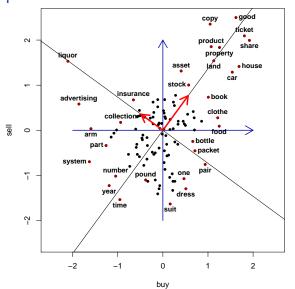
- ▶ Trigonometry: position of projected point on the line is $\|\mathbf{x}\| \cdot \cos \varphi = \|\mathbf{x}\| \cdot \langle \mathbf{x}', \mathbf{v} \rangle = \langle \mathbf{x}, \mathbf{v} \rangle$
- ▶ Preserved variance = one-dimensional variance on the line (note that data set is still centered after projection)

$$\sigma_{\mathbf{v}}^2 = \frac{1}{k-1} \sum_{i=1}^k \langle \mathbf{x}_i, \mathbf{v} \rangle^2$$

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PCA example



DSM parameters Examples

Outline

DSM parameters

A taxonomy of DSM parameters

Examples

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Some well-known DSM examples

Some well-known DSM examples

Latent Semantic Analysis (Landauer and Dumais 1997)

- term-context matrix with document context
- weighting: log term frequency and term entropy
- distance measure: cosine
- ▶ dimensionality reduction: SVD

Hyperspace Analogue to Language (Lund and Burgess 1996)

- term-term matrix with surface context.
- structured (left/right) and distance-weighted frequency counts
- distance measure: Minkowski metric (1
- dimensionality reduction: feature selection (high variance)

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Infomap NLP (Widdows 2004)

- term-term matrix with unstructured surface context
- weighting: none
- distance measure: cosine
- ▶ dimensionality reduction: SVD

Random Indexing (Karlgren and Sahlgren 2001)

- term-term matrix with unstructured surface context
- weighting: various methods
- distance measure: various methods
- dimensionality reduction: random indexing (RI)

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DSM parameters Examples

Some well-known DSM examples

Dependency Vectors (Padó and Lapata 2007)

- term-term matrix with unstructured dependency context
- weighting: log-likelihood ratio
- distance measure: information-theoretic (Lin 1998)
- dimensionality reduction: none

Distributional Memory (Baroni and Lenci 2010)

- term-term matrix with structured and unstructered dependencies + knowledge patterns
- weighting: local-MI on type frequencies of link patterns
- distance measure: cosine
- dimensionality reduction: none

Outline

DSM parameters Scaling up

DSM parameters

Scaling up

Scaling up to the real world

- ▶ So far, we have worked on small toy models
 - ▶ DSM matrix restricted to 2.000 5.000 rows and columns
 - ▶ small corpora (or dependency sets) can be processed within R
- ▶ Now we need to scale up to real world data sets
 - for most statistical models, more data are better data!
 - cf. success of Google-based NLP techniques (even if simplistic)
- ► Example 1: window-based DSM on BNC content words
 - ▶ 83,926 lemma types with f > 10
 - \blacktriangleright term-term matrix with 83.926 \cdot 83.926 = 7 billion entries
 - standard representation requires 56 GB of RAM (8-byte floats)
 - ▶ only 22.1 million non-zero entries (= 0.32%)
- ► Example 2: Google Web 1T 5-grams (1 trillion words)
 - more than 1 million word types with f > 2500
 - ▶ term-term matrix with 1 trillion entries requires 8 TB RAM
 - only 400 million non-zero entries (= 0.04%)

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DSM parameters Scaling up

Sparse matrix representation

► Invented example of a sparsely populated DSM matrix

eat	get	hear	kill	see	use
	59			39	23
		•	26	58	
	98	•	•	•	
33	•	42	•	83	
					84
9		•	27	•	•
	33	. 59 . 98 33 .	. 59	59	39

▶ Store only non-zero entries in compact sparse matrix format

row	col	value	row	col	value
1	2	59	4	1	33
1	5	39	4	3	42
1	6	23	4	5	83
2	4	26	5	6	84
2	5	58	6	1	9
3	2	98	6	4	27

Handling large data sets: three approaches

- 1. Sparse matrix representation
 - full DSM matrix does not fit into memory
 - but much smaller number of non-zero entries can be handled
- 2. Feature selection
 - ▶ reduce DSM matrix to subset of columns (usu. 2,000 10,000)
 - select most frequent, salient, discriminative, . . . features
- 3. Dimensionality reduction
 - ▶ also reduces number of columns, but maps vectors to subspace
 - singular value decomposition (usu. ca. 300 dimensions)
 - random indexing (2,000 or more dimensions)
 - ▶ performed with external tools → R can handle reduced matrix

DSM parameters Scaling up

Working with sparse matrices

- ► Compressed format: each row index (or column index) stored only once, followed by non-zero entries in this row (or column)
 - convention: column-major matrix (data stored by columns)
- Specialised algorithms for sparse matrix algebra
 - especially matrix multiplication, solving linear systems, etc.
 - take care to avoid operations that create a dense matrix!
- ▶ **R** implementation: Matrix package (from CRAN)
 - ▶ can build sparse matrix from (row, column, value) table
 - unfortunately, no implementation of sparse SVD so far
- Other software packages: Matlab, Octave (recent versions)

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