zoo: An **\$3** Class and Methods for Indexed Totally Ordered Observations

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Abstract

zoo is an R package providing an S3 class with methods for indexed totally ordered observations, such as irregular time series. Its key design goals are independence of a particular index/time/date class and consistency with base R and the "ts" class for regular time series. This paper describes how these are achieved within zoo and provides several illustrations of the available methods for "zoo" objects which include plotting, merging and binding, several mathematical operations, extracting and replacing value and index, coercion and NA handling.

Keywords: totally ordered observations, irregular time series, S3, R.

1. Introduction

The R system for statistical computing (R Development Core Team 2004, http://www.R-project. org/) ships with a a class for regularly spaced time series, "ts" in package stats, but has no native class for irregularly spaced time series. With the increased interest in computational finance with R over the last years several implementations of classes for irregular time series emerged which are aimed particularly at finance applications. These include the \$3 classes "timeSeries" in package fBasics from the Rmetrics bundle (Wuertz 2004) and "irts" in package tseries (Trapletti 2004) and the \$4 class "its" in package its (Heywood 2004). With these packages available, why would anybody want yet another package providing infrastructure for irregular time series? The above mentioned implementations have in common that they are restricted to a particular class for the time scale: the former implementation comes with its own time class "timeDate" built on top of the "POSIXt" classes available in base R whereas the latter two use "POSIXct" directly. And this was the starting point for the zoo project: the first author of the present paper needed more general support for ordered observations, independent of a particular index class, for the package strucchange (Zeileis, Leisch, Hornik, and Kleiber 2002). Hence the package was called zoo which stands for Z's ordered observations. Since the first release, a major part of the additions to zoo were provided by the second author of this paper, so that the name of the package does not really reflect the authorship anymore. Nevertheless, independence of a particular index class remained one the most important design goal. While the package evolved to its current status, a second key design goal became more and more clear: to provide methods to standard generic functions for the "zoo" class that are similar to those for the "ts" class (and base R in general) such that the usage of **zoo** is rather intuitive because only few additional commands have to be learned.

This paper describes how these design goals are implemented in **zoo**. Section 2 explains how "zoo" objects are created and illustrates how the corresponding methods for plotting, merging and binding, several mathematical operations, extracting and replacing value and index, coercion and NA handling can be used. Section 3 outlines how other packages can build on this basic infrastructure before Section 4 gives a few summarizing remarks.

2. The class "zoo" and its methods

2.1. Creation of "zoo" objects

The simple idea for the creation of "zoo" objects is to have some vector or matrix of observations \mathbf{x} which are totally ordered by some index vector. In time series applications this index is measure of time but every other numeric, character or even more abstract vector that provides a total ordering of the observations is also suitable. Objects of class "zoo" are created by the function

```
zoo(x, order.by)
```

where x is the vector or matrix of observations and order.by is the index by which the observations should be ordered. It has to be of the same length as NROW(x), i.e., either the same length as x for vectors or the same number of rows for matrices. The "zoo" object created is essentially the vector/matrix as before but has an additional "index" attribute in which the index is stored. Both the value x and the index can, in principle, be of arbitrary classes. However, most of the following methods (plotting, aggregating, mathematical operations) for "zoo" objects are typically only useful for numeric values x. In contrast, special effort in the design was put into independence from a particular class for the index vector. In zoo it is assumed that combination c(), querying the length(), value matching match(), subsetting [,, and, of course, ordering order() work when applied to the index. This is the case, e.g., for standard numeric and character vectors and for vectors of classes "Date", "POSIXct" or "times" from package chron, but not for the class "dateTime" in fBasics. In the latter case, the solution is to provide methods for the above mentioned functions so that indexing "zoo" objects with "dateTime" vectors works. To achieve this independence of the index class the non-generic functions order and match are made S3 generics in zoo with their base definition as the default method.

To illustrate the usage of zoo, we first load the package and set the random seed to make the examples in this paper exactly reproducible.

```
> library(zoo)
> set.seed(1071)
Then, we create two vectors z1 and z2 with "POSIXct" indexes, one with random values
> z1.index <- ISOdatetime(2004, rep(1:2, 5), sample(28, 10), 0,
      0, 0)
> z1.value <- rnorm(10)
> z1 <- zoo(z1.value, z1.index)
and one with a sinus wave
> z2.index <- as.POSIXct(paste("2004-", rep(1:2, 5), "-", sample(1:28,
      10), sep = ""))
> z2.value <- sin(2 * 1:10/pi)
> z2 <- zoo(z2.value, z2.index)
Furthermore, we create a matrix Z with random values and a "Date" index
> Z.index <- structure(sample(12450:12500, 10), class = "Date")
> Z.value <- matrix(rnorm(30), ncol = 3)</pre>
> colnames(Z.value) <- c("Aa", "Bb", "Cc")
> Z <- zoo(Z.value, Z.index)
```

Note, that in the above examples the creation of indexes might seem a bit awkward at first sight, but this is only an artefact of the need for random generation of random dates for this illustration.

In "real world" applications, the indexes are typically part of the raw data set read into R. See Section 3 for such examples.

Methods to several standard generic functions are available for "zoo" objects, such as print, summary, str, head, tail and [(subsetting), a few of which are illustrated in the following.

There are three printing code styles for "zoo" objects: vectors are default printed in "horizontal" style

> z1

> z1[3:7]

```
2004-01-19 2004-01-25 2004-01-27 2004-02-07 2004-02-12 -0.2982353 0.6862577 1.9407885 1.2738445 0.2217044
```

and matrices in "vertical" style

> Z

```
AaBbCc2004-02-021.255433900.68157316-0.632920492004-02-08-1.494583261.32341223-1.494422692004-02-09-1.87462247-0.873292890.627339712004-02-21-0.145386080.45234903-0.145974012004-02-220.225424180.538389380.231361332004-02-291.206955180.31814222-0.011292022004-03-05-1.208610251.42379785-0.816144832004-03-10-0.110395631.347742540.955224682004-03-140.84202385-2.738420190.231506952004-03-20-0.190191040.12308872-1.51862157
```

> Z[1:3, 2:3]

```
Bb Cc
2004-02-02 0.6815732 -0.6329205
2004-02-08 1.3234122 -1.4944227
2004-02-09 -0.8732929 0.6273397
```

Additionally, there is a "plain" style which simply first prints the value and then the index. Summaries and most other methods for "zoo" objects are carried out column wise, reflecting the rectangular structure indexed by rows. In addition, a summary of the index is provided.

> summary(z1)

```
Index
                                    z1
Min.
      :2004-01-05 00:00:00
                              Min.
                                     :-2.07608
1st Qu.:2004-01-20 12:00:00
                              1st Qu.:-0.27251
Median :2004-02-01 12:00:00
                              Median: 0.12139
Mean
       :2004-02-01 09:36:00
                              Mean
                                     : 0.05364
3rd Qu.:2004-02-15 00:00:00
                              3rd Qu.: 0.73163
       :2004-02-24 00:00:00
                              Max.
                                      : 1.94079
```

> summary(Z)

```
Index
                                               Bb
                                                                   Cc
                            Aa
                              :-1.8746
                                                 :-2.7384
                                                                    :-1.51862
Min.
       :2004-02-02
                      Min.
                                         Min.
                                                            Min.
1st Qu.:2004-02-12
                      1st Qu.:-0.9540
                                         1st Qu.: 0.1719
                                                            1st Qu.:-0.77034
Median: 2004-02-25
                      Median :-0.1279
                                         Median: 0.4954
                                                            Median :-0.07863
                             :-0.1494
Mean
       :2004-02-25
                      Mean
                                         Mean
                                                 : 0.2597
                                                            Mean
                                                                    :-0.25739
3rd Qu.:2004-03-08
                      3rd Qu.: 0.6879
                                         3rd Qu.: 1.1630
                                                            3rd Qu.: 0.23147
       :2004-03-20
                      Max.
                              : 1.2554
                                         Max.
                                                 : 1.4238
                                                            Max.
                                                                    : 0.95522
```

2.2. Plotting

The plot method for "zoo" objects, in particular for multivariate "zoo" series, is based on the corresponding method for (multivariate) regular time series. It relies on plot and lines methods being available for the index class which can plot the index against the observations.

By default the plot method creates a panel for each series

```
> plot(Z)
```

but can also display all series in a single panel

```
> plot(Z, plot.type = "single", col = 2:4)
```

where in both cases additional graphical parameters like color col, plotting character pch and line type lty can be expanded to the number of series. But the plot method for "zoo" objects offers some more flexibility in specification of graphical parameters as in

```
> plot(Z, type = "b", lty = 1:3, pch = list(Aa = 1:5, Bb = 2, Cc = 4),
+ col = list(Bb = 2, 4))
```

The argument 1ty behaves as before and sets every series in another line type. The pch argument is a named list that assigns to each series a different vector of plotting characters each of which is expanded to the number of observations. Such a list does not necessarily have to include the names of all series, but can also specify a subset. For the remaining series the default parameter is then used which can again be changed: e.g., in the above example series "Bb" is plotted in red and all remaining series in blue. The results of the multiple panel plots are depicted in Figure 2 and the single panel plot in 1.

2.3. Merging and binding

As for many rectangular data formats in R, there are both methods for combining the rows and columns of "zoo" objects respectively. For the rbind method the number of columns of the combined objects has to be identical and the indexes may not overlap.

```
> rbind(z1[5:10], z1[2:3])

2004-01-14 2004-01-19 2004-01-27 2004-02-07 2004-02-12 2004-02-16 0.02107873 -0.29823529 1.94078850 1.27384445 0.22170438 -2.07607585 2004-02-20 2004-02-24 -1.78439244 -0.19533304
```

The cbind method by default combines the columns by the union of the indexes and fills the created gaps by NAs.

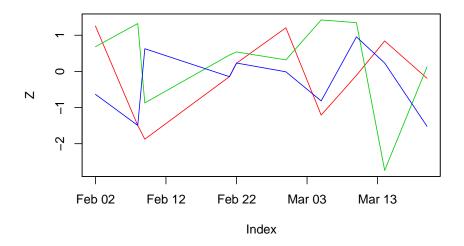


Figure 1: Example of a single panel plot

> cbind(z1, z2)

| | 1 | 2 |
|------------|-------------|-------------|
| 2004-01-03 | NA | 0.94306673 |
| 2004-01-05 | 0.74675994 | -0.04149429 |
| 2004-01-14 | 0.02107873 | NA |
| 2004-01-17 | NA | 0.59448077 |
| 2004-01-19 | -0.29823529 | -0.52575918 |
| 2004-01-24 | NA | -0.96739776 |
| 2004-01-25 | 0.68625772 | NA |
| 2004-01-27 | 1.94078850 | NA |
| 2004-02-07 | 1.27384445 | NA |
| 2004-02-08 | NA | 0.95605566 |
| 2004-02-12 | 0.22170438 | -0.62733473 |
| 2004-02-13 | NA | -0.92845336 |
| 2004-02-16 | -2.07607585 | NA |
| 2004-02-20 | -1.78439244 | NA |
| 2004-02-24 | -0.19533304 | NA |
| 2004-02-25 | NA | 0.56060280 |
| 2004-02-26 | NA | 0.08291711 |

In fact, the cbind method is synonymous to the merge method which also allows for combining the columns by the intersection of the indexes using the argument all = FALSE.

> merge(z1, z2, all = FALSE)

```
z1 z2
2004-01-05 0.74675994 -0.04149429
2004-01-19 -0.29823529 -0.52575918
2004-02-12 0.22170438 -0.62733473
```





Figure 2: Examples of multiple panel plots

Additionally, the filling pattern can be changed and the naming of the columns can be modified. In the case of merging of objects with different index classes, R gives a warning and tries to coerce the indexes, but this is generally rather difficult

Another function which performs operations along a subset of indexes is aggregate, which is therefore discussed in this section although it does not combine several objects. Using the aggregate method, "zoo" objects are split into subsets along a coarser index grid, summary statistics are computed for each and then the reduced object is returned. In the following example, first a function is set up which returns for a given "Date" value the corresponding first of the month. This function is then used to compute the coarser grid for the aggregate call: in the first example the mean of the observations in the month is returned, in the second example the last observation.

2.4. Mathematical operations

To allow for standard mathematical operations among "zoo" objects, zoo extends group generic functions Ops. These perform the operations only for the intersection of the indexes of the objects. Hence, the summation of z1 and z2 yields

```
> z1 + z2
2004-01-05 2004-01-19 2004-02-12
0.7052657 -0.8239945 -0.4056304
```

Additionally, methods for transposing t of "zoo" objects—which coerces to a matrix before, see below—and computing cumulative quantities such as cumsum, cumprod, cummin, cummax which are all applied column wise.

> cumsum(Z)

```
Bb
                                 Cc
          Aa
2004-02-02 1.2554339 0.6815732 -0.6329205
2004-02-08 -0.2391494 2.0049854 -2.1273432
2004-02-09 -2.1137718 1.1316925 -1.5000035
2004-02-21 -2.2591579
                      1.5840415 -1.6459775
2004-02-22 -2.0337337
                      2.1224309 -1.4146162
2004-02-29 -0.8267785
                      2.4405731 -1.4259082
2004-03-05 -2.0353888
                      3.8643710 -2.2420530
2004-03-10 -2.1457844
                      5.2121135 -1.2868283
2004-03-14 -1.3037606
                      2.4736933 -1.0553214
2004-03-20 -1.4939516 2.5967820 -2.5739429
```

2.5. Extracting and replacing the value and the index

zoo provides several generic functions and methods to work on the value (or data) contained in a "zoo" object, the index (or time) attribute associated to it, and on both data and index.

The value stored in "zoo" objects can be extracted by value which strips off all "zoo"-specific attributes and it can be replaced using value<-. Both are new generic functions with methods for "zoo" objects as illustrated in the following example.

The index associated with a "zoo" object can be extracted by index and modified by index<-. As the interpretation of the index as "time" in time series applications is more natural, there are also synonymous methods time and time<-. Hence, the following two commands return equivalent results

```
> index(z2)
```

```
[1] "2004-01-03 CET" "2004-01-05 CET" "2004-01-17 CET" "2004-01-19 CET" [5] "2004-01-24 CET" "2004-02-08 CET" "2004-02-12 CET" "2004-02-13 CET" [9] "2004-02-25 CET" "2004-02-26 CET"
```

> time(z2)

```
[1] "2004-01-03 CET" "2004-01-05 CET" "2004-01-17 CET" "2004-01-19 CET" [5] "2004-01-24 CET" "2004-02-08 CET" "2004-02-12 CET" "2004-02-13 CET" [9] "2004-02-25 CET" "2004-02-26 CET"
```

The index scale of z2 can be change to that of z1 by

```
> z2

2004-01-05 2004-01-14 2004-01-19 2004-01-25 2004-01-27 2004-02-07
0.94306673 -0.04149429 0.59448077 -0.52575918 -0.96739776 0.95605566
2004-02-12 2004-02-16 2004-02-20 2004-02-24
-0.62733473 -0.92845336 0.56060280 0.08291711
```

The start and the end of the index/time vector can be queried by start and end:

```
> start(z1)
[1] "2004-01-05 CET"
```

> index(z2) <- index(z1)

> end(z1)

[1] "2004-02-24 CET"

To work on both value and index/time, **zoo** provides method a method to window and also adds a new generic window<- with a method for "zoo" objects. In both cases the window is specified by

```
window(x, index, start, end)
```

where x is the "zoo" object, index is a set of indexes to be selected (by default the full index of x) and start and end can be used to restrict the index set. Thus, the first command in the following example selects all observations starting from 2004–03–01 whereas the second selects only from the observations with the 5th to 8th index those up to 2004–03–01.

> window(Z, start = as.Date("2004-03-01"))

```
Aa Bb Cc

2004-03-05 -1.2086102 1.4237978 -0.8161448

2004-03-10 -0.1103956 1.3477425 0.9552247

2004-03-14 0.8420238 -2.7384202 0.2315069

2004-03-20 -0.1901910 0.1230887 -1.5186216

> window(Z, index = index(Z)[5:8], end = as.Date("2004-03-01"))

Aa Bb Cc

2004-02-22 0.22542418 0.53838938 0.23136133

2004-02-29 1.20695518 0.31814222 -0.01129202
```

The same syntax can be used for the corresponding replacement function.

> window(z1, end = as.POSIXct("2004-02-01")) <- 9:5

Two methods to generic functions that are standard in time series applications are lag and diff which are available with the same arguments as the "ts" methods—with the only exception that diff not only allows for arithmetic but also geometric differences.

>
$$lag(z1, k = -1)$$
 $2004-01-14$ $2004-01-19$ $2004-01-25$ $2004-01-27$ $2004-02-07$ $2004-02-12$ $2004-02-16$

9 8 7 6 5 6 7

 $2004-02-20$ $2004-02-24$

8 9

> $diff(z1)$
 $2004-01-14$ $2004-01-19$ $2004-01-25$ $2004-01-27$ $2004-02-07$ $2004-02-12$ $2004-02-16$

-1 -1 -1 -1 1 1 1

 $2004-02-20$ $2004-02-24$

1 1

2.6. Coercion to and from "zoo"

Coercion to and from "zoo" objects is available for objects of various classes, in particular "ts", "irts" and "its" objects can be coerced to "zoo" using the respective as.zoo method. The reverse coercion is available for "its" and for "irts" (the latter in package tseries). Furthermore, "zoo" objects can be coerced to vectors, matrices and data frames (dropping the index/time attribute). A simple example is

```
> as.data.frame(Z)
```

```
Bb
                                 Сс
           Aa
    1.2554339
              0.6815732 -0.63292049
1
2
  -1.4945833 1.3234122 -1.49442269
3
  -1.8746225 -0.8732929 0.62733971
4
  -0.1453861 0.4523490 -0.14597401
   0.2254242 0.5383894 0.23136133
5
6
   1.2069552 0.3181422 -0.01129202
7
   -1.2086102
              1.4237978 -0.81614483
  -0.1103956 1.3477425
                         0.95522468
8
   0.8420238 -2.7384202 0.23150695
10 -0.1901910 0.1230887 -1.51862157
```

2.7. NA handling

Three methods for dealing with NAs (missing observations) in the value are applicable to "zoo" objects: na.omit, na.contiguous, na.locf. na.omit—or its default method to be more precise—returns a "zoo" object with incomplete observations removed. na.contiguous extracts the longest consecutive stretch of non-missing values. This function is made generic in zoo with a default method (also applicable to "zoo" objects) and the stats function being the "ts" method. Furthermore, a new generic function na.locf and corresponding default method is introduced in zoo which stands for last observation carried forward. It replaces missing observations by the most recent non-NA prior to it. Leading NAs, which cannot be replaced by precious observations, are removed by default.

```
> z1[sample(1:10, 3)] <- NA
> z1
2004-01-05 2004-01-14 2004-01-19 2004-01-25 2004-01-27 2004-02-07 2004-02-12
                                           6
                                                      5
                   NA
                               7
2004-02-16 2004-02-20 2004-02-24
         8
                    9
                              NΑ
> na.omit(z1)
2004-01-05 2004-01-19 2004-01-25 2004-01-27 2004-02-07 2004-02-16 2004-02-20
                    7
                               6
                                           5
                                                      6
> na.contiguous(z1)
2004-01-19 2004-01-25 2004-01-27 2004-02-07
         7
                    6
                                5
> na.locf(z1)
```

3. Combining zoo with other packages

The main purpose of the package **zoo** is to provide basic infrastructure for working with indexed totally ordered observations that can be either employed by useres directly or can be a basic ingredient on top of which other packages can build. The latter is illustrated with a few brief examples involving the packages **strucchange**, **tseries** and **fBasics** in this section.

3.1. strucchange: empirical fluctuation processes of class "zoo"

The package **structhange** provides a collection of methods for testing, monitoring and dating structural changes, in particular in linear regression models. Tests for structural change assess whether the parameters of a model remain constant over an ordering with respect to a specified variable, usually time. To adequatly store and visualize empirical fluctuation processes which capture instabilities over this ordering, a data type for indexed ordered observations is required. This was the motivation for starting the **zoo** project.

A simple example for the need of "zoo" objects in **strucchange** which could not (easily) be implemented by any of the other irregular time series classes available on CRAN is described in the following. We assess the constancy of the electrical resistance over the apparent juice content of kiwi fruits. The data set fruitohms is contained in the **DAAG** package (Maindonald and Braun 2004). The fitted ocus object contains the OLS-based CUSUM process for the mean of the electrical resistance (variable ohms) indexed by the juice content (variable juice).

```
> library(strucchange)
> library(DAAG)
> data(fruitohms)
> ocus <- gefp(ohms ~ 1, order.by = ~juice, data = fruitohms)</pre>
```

This OLS-based CUSUM process can be visualized using the plot method for "gefp" objects which builds on the "zoo" method and yields in this case the plot in Figure 3 showing the process which crosses its 5% critical value and thus signals a significant decrease in the mean electrical resistance over the juice content. for more information on the package strucchange and the function gefp see Zeileis et al. (2002) and Zeileis (2004).

3.2. tseries: historical financial data

A typical application for irregular time series which became increasingly important over the last years in computational statistics and finance is daily (or higher frequent) financial data. The package tseries provides the function get.hist.quote for obtaining historical financial data by querying Yahoo! Finance at http://finance.yahoo.com/, an online portal quoting data provided by Reuters. The following code queries the quotes of Lucent Technologies starting from 2001-01-01.

```
> library(tseries)
> LU <- get.hist.quote(instrument = "LU", start = "2001-01-01",
+ end = "2004-09-30", origin = "1970-01-01")
time series starts 2001-01-02</pre>
```

> plot(ocus)

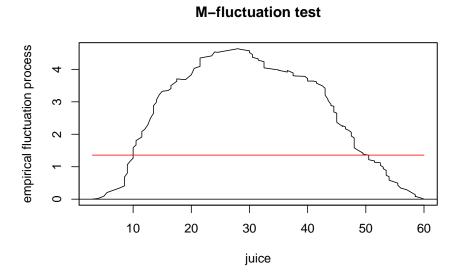


Figure 3: Empirical M-fluctuation process for fruitohms data

In the returned LU object the irregular data is stored by extending it to a regular grid and filling the gaps with NAs. The time is stored in days starting from an origin, in this case specified to be 1970-01-01. This series can be transformed easily into an irregula "zoo" series using a "Date" index. The log-difference returns for Lucent Technologies is depicted in Figure 4.

```
> LU <- zoo(value(LU), structure(time(LU), class = "Date"))
> LU <- na.omit(LU)</pre>
```

3.3. fBasics: indexes of class "timeDate"

Although the methods in **zoo** work out of the box for many index classes, it might be necessary for some index classes to provide c, length, order and match methods such that the methods in **zoo** work properly. An example for such an index class which requires a bit more attention is "timeDate" from the **fBasics** package.

But after the necessary methods have been defined

```
> length.timeDate <- function(x) prod(x@Dim)
> order.timeDate <- function(x, ...) order.default(as.POSIXct(x),
+ ...)
> match.timeDate <- function(x, y, ...) match.default(as.POSIXct(x),
+ as.POSIXct(y), ...)</pre>
```

the class "timeDate" can be used for indexing "zoo" objects. The following example illustrates how z2 can be transformed to use the "timeDate" class.

```
> library(fBasics)
```

No timezone information found, using default of GMT

> plot(diff(log(LU)))

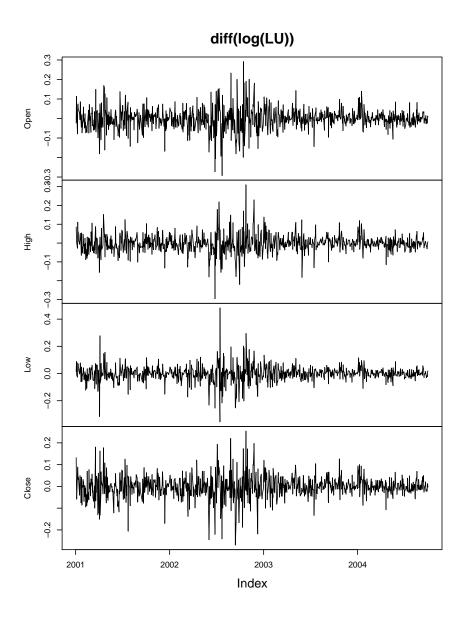


Figure 4: Log-difference returns for Lucent Technologies

```
Rmetrics, (C) 1999-2004, Diethelm Wuertz, GPL
fBasics: Markets, Basic Statistics, Date and Time
> z2td <- zoo(value(z2), timeDate(index(z2), FinCenter = "GMT"))
> z2td
2004-01-04 23:00:00 2004-01-13 23:00:00 2004-01-18 23:00:00 2004-01-24 23:00:00
         0.94306673
                           -0.04149429
                                                0.59448077
                                                                   -0.52575918
2004-01-26 23:00:00 2004-02-06 23:00:00 2004-02-11 23:00:00 2004-02-15 23:00:00
        -0.96739776
                            0.95605566
                                               -0.62733473
                                                                   -0.92845336
2004-02-19 23:00:00 2004-02-23 23:00:00
        0.56060280
                            0.08291711
```

4. Summary

The package **zoo** provides an S3 class and methods for indexed totally ordered observations, such as irregular time series. its key design goals are independence of a particular index class and compatibility with standard generics similar to the behaviour of the corresponding "ts" methods. This paper describes how these are implemented in **zoo** and illustrates the usage of the methods for plotting, merging and binding, several mathematical operations, extracting and replacing value and index, coercion and NA handling.

References

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