

Results

We used `pyunlocbox` as the implementation for the FISTA algorithm. To select the optimal amount of regularization, we tried λ values ranging from 10 to 10^{-5} and created an L-curve. In all three cases (i.e. 540, 270, and 90 views), we found that $\lambda = 10^{-3}$ gave the optimal reconstruction (Figure 1). The reconstruction from the full sinogram for all values of λ is shown in Supplemental Figure S1.

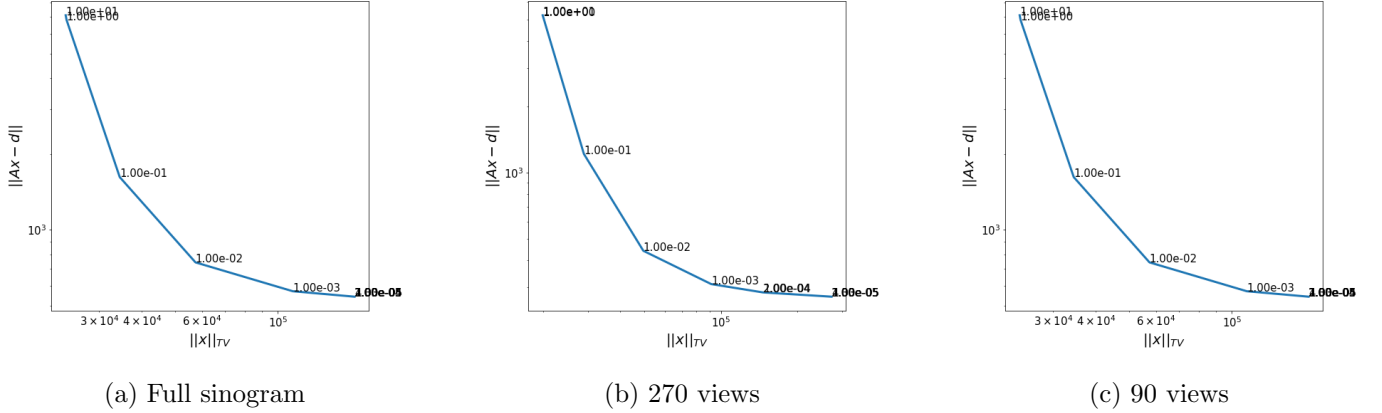


Figure 1: L-curves for FISTA reconstruction of image.

We compared the image reconstructed with FISTA to reconstructions with SART. We chose to implement SART as our stationary method because it is less prone to overfitting than ART and converges faster than SIRT. We assessed image quality using two metrics, the structural similarity (SSIM) index and the mean squared error (MSE). We computed these metrics on the full image and on a defined region of interest (ROI). We set our ROI to cover pixel rows 175-220 and pixel columns 100-140 because the image has complex shapes in this region. The reconstructed images for 540, 270, and 90 views are shown in Figures 2, 3, and 4, respectively. The SSIM metrics are shown in Table 1 and the MSE metrics are shown in Table 2. In virtually every case, FISTA outperforms SART. However, the reconstruction from 90 views over the ROI is better with SART than with FISTA.

Number of views	FISTA	FISTA ROI	SART	SART ROI
540	0.874	0.924	0.885	0.855
270	0.880	0.872	0.877	0.849
90	0.872	0.706	0.792	0.741

Table 1: SSIM of image reconstructions.

Number of views	FISTA	FISTA ROI	SART	SART ROI
540	35.24	115.76	40.91	244.75
270	39.18	207.21	43.62	251.27
90	62.37	471.45	80.66	397.23

Table 2: MSE of image reconstructions.

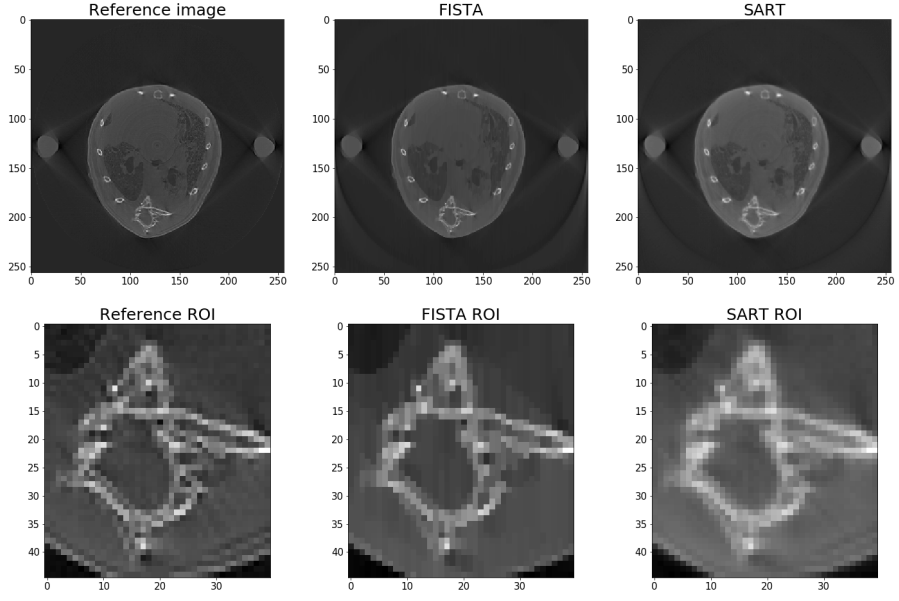


Figure 2: Reconstructed image using FISTA and SART from the full sinogram.

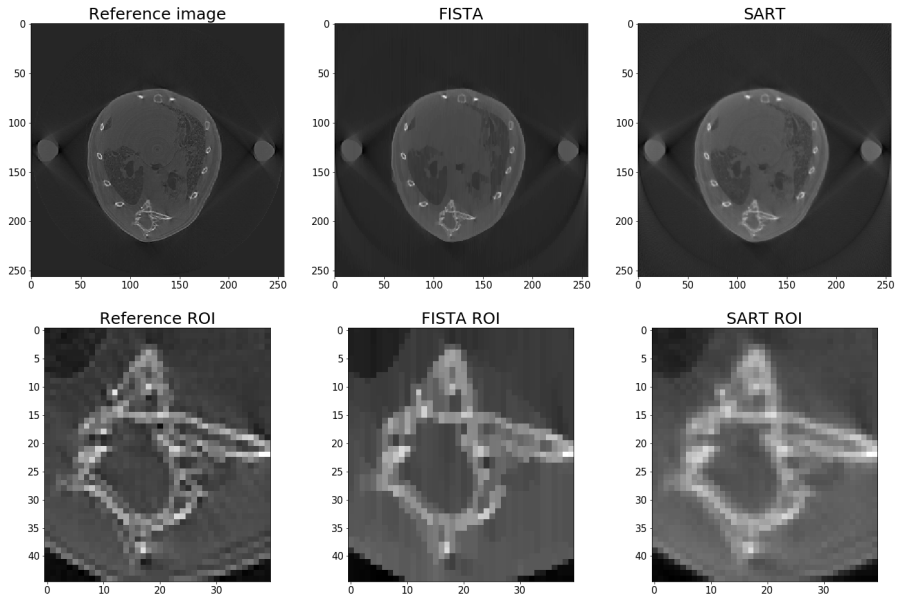


Figure 3: Reconstructed image using FISTA and SART from the 270 views.

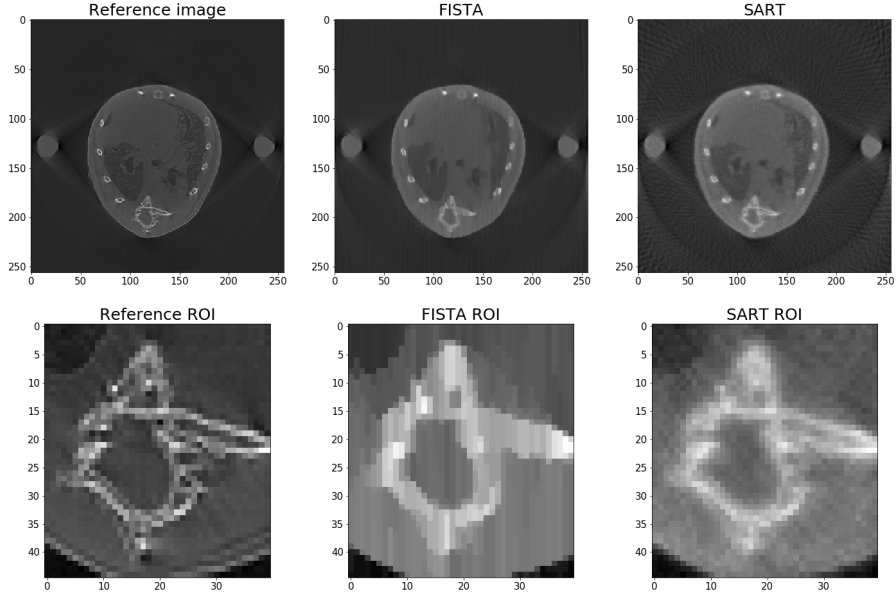


Figure 4: Reconstructed image using FISTA and SART from the full sinogram.

Discussion

In general, FISTA outperforms SART at reconstructing the image. By comparing reconstructions on the three different sinograms, we see that the SSIM and MSE is more stable with FISTA (Tables 1, 2). Therefore, FISTA creates more robust reconstructions with less data. The FISTA reconstruction also has sharper edges compared to the SART reconstruction. This is especially apparent as fewer views are used (Figure 3). The two methods also appear to handle noise differently. In the 90 view reconstruction, the SART reconstruction contains wavy patterns whereas the FISTA reconstruction contains vertical bands (Figure 4). This may explain why the FISTA reconstruction is worse over the ROI because the ROI contains many horizontal and diagonal segments that are blurred by the vertical bands in the reconstruction.

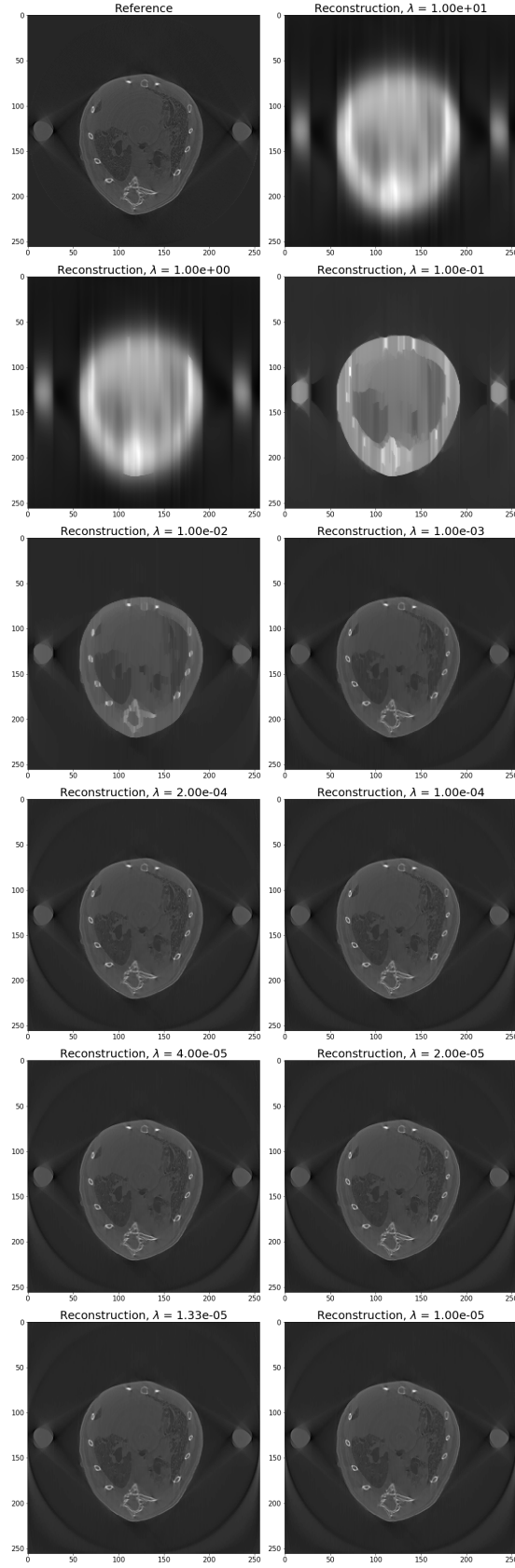


Figure S1: FISTA reconstruction from full sinogram with different values of λ .