

A design-oriented numerical investigation on seismic soil-structure interaction

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If I have seen further it is by standing on the shoulders of Giants.
Isaac Newton

Chapter 1

Introduction

1.1 Current situation - an overview

In the past few decades, Northern area of Netherlands is facing ground tremors induced by the gas extraction, the greatest event being registered on 16th of August 2012, at Huizinge, with a depth of 10km and a magnitude of $M_w=3.6$. Even though the majority of these earthquakes are shallow and small, the larger events can eventually produce damage concerning the citizens and mining companies. The level of uncertainties rises and the phenomena starts to be problematic when combined with other detrimental factors. For instance, the foundation shape and design, the uncertainties related to the soil homogeneity and nonlinear response or the need of updating the design codes accordingly. Currently, numerous organizations and companies investigate the phenomenon - performing hazard studies and aiming to provide reliable design methods that best suit the condition.

The first particularity of the state of affairs is represented by the characteristic of the earthquake itself. Europe mainly encounters tectonic seism in south and south-eastern parts, while the current condition reveals a triggered seismic activity - which is more difficult to assess source wise. Induced seismicity relates to human activities that alter the stress-strain development within the crust and usually reveals low magnitude. It follows that the relationship between “anthropogenic” stress disturbances and the resulting earthquake magnitude will always be somewhat unpredictable, insofar as it is partly associated with “background” event probabilities. Nevertheless, the factors that could influence the maximum size of induced earthquakes are of great interest.

Many devices have been installed in order to record the ground shaking events - accelerometers and borehole sensors serve to improve database. Accelerograms represent recordings of the ground acceleration during an earthquake. The other additional stations improve detection and monitoring through real-time continuous data transmission. The recordings, particularly those from analog instruments, invariably contain noise that can mask and distort the ground-motion signal at both high and low frequencies hence the need of correction equations eliminate the errors. Real records are an ever more attractive option for defining the input to dynamic analyses in geotechnical and structural engineering. Guidelines on procedures for the selection of appropriate suites of acceleration time-series for this purpose are lacking, and seismic design codes are particularly poor in this respect.

During the event from August 2012, the devices recorded the ground motion and transcribed the signals into plots containing the ground acceleration against time. The available accelerogram data allows a better understanding of the entire phenomena whilst several aspects arise after a close investigation. Firstly, the seismicity shows similar patterns compared to the triggered type of earthquake - which, based on empirical data, is considered to have an upper limit of $M_w=5.0$. Studying the event, considering a large time scale, reveals that the Groningen field is mainly dominated by rather frequent small events than scarce large ones. Meanwhile, both statistical and physical modelling are performed for estimating the Mmax values. The seismic source is usually described through P waves, S waves and surface waves that are all affected by the orientation of the fault plane. In addition, waveform data allows determination of focal mechanisms of the small earthquake in inhomogeneous subsoil. A correct evaluation of the waves further provides reliable parameters such as the seismic moment, amplitude correction along with the focal mechanism. The current seismic survey, found in the figure below, shows this dissimilarity in data

recorded in close locations (red representing Middelstum event in 2009 and blue the Huizinge event, respectively) highlighting the difference in the polarity pattern of the P waves [as it can be seen in the vertical accelerograms]. This translates into a difficulty in understanding the characteristics of the earthquake and its mechanical behaviour. In addition, the double S pulse, evident in the Huizinge earthquake, extends the duration of the strong shaking. These multiple S-phases might be generated by the salt layer which varies in thickness along the area. Salt deposit is a high velocity layer - hence multiple reflections can be the culprit for this particular wave propagation pattern.

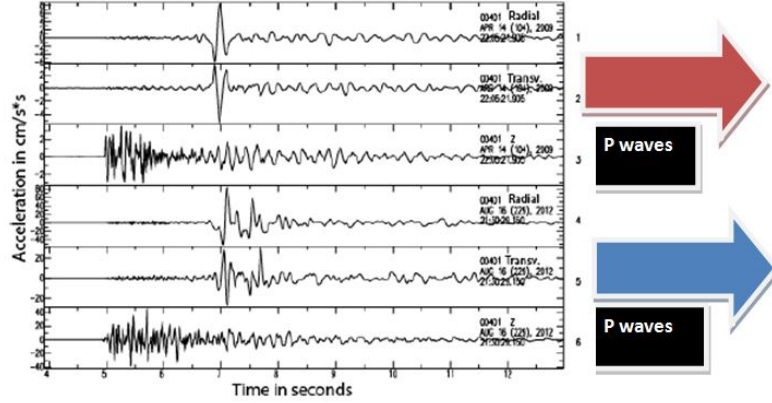


Figure 1.1: Accelerograms from Middelstum 1st April 2009 (red arrow) and Huizinge 16th of August 2012 (1 - Radial, 2 - Transverse, 3 - Vertical)

Another aspect important to mention refers to previous times where the Dutch standard did not include seismic design which further reflected into inadequately reinforced concrete structures as well as the lack of reinforcement within masonry buildings. Existing constructions are not seismically prepared - as the only lateral force taken into consideration, while designing, was the wind load (5 - 15 times lower than a seismic load). Ductility demand is not fulfilled henceforth, cracks appear after earthquake and structures start to account irreversible damage. The foundations of most buildings are footing strips, 10cm to 30cm high and 20cm wide unable to withstand the stresses produced during an ground shaking. The floor does not provide the rigid diaphragm property, allowing the vertical elements (walls and columns) to displace independently. The overall stiffness cannot avoid damage and so foundation strengthening methods *supply the solution*.

One major factor influencing the nonlinear response is the subsoil on which the structures are founded on. The typical soil for Netherlands consists in layers of sand in all states, peat, clay which all denote weak strength, potential of swelling, creep and pore pressure build-up as well as low seismic velocities. Softer soils amplify more the seismic waves, increasing the effect. This, in association with the multiple S-phase, leads to an augmented energy pulse throughout a longer duration. In fact, due to its prolonged duration, it is considered to exceed the limits imposed by the simplified response spectrum given within the Eurocode 8 guidelines.

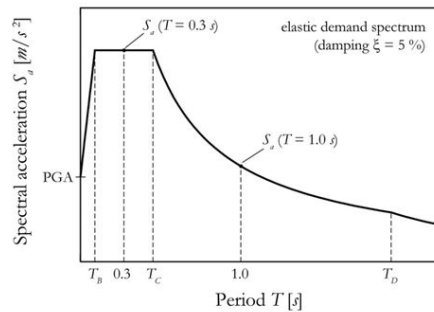


Figure 1.2: Simplified response spectra according to Eurocode 8

Reflecting on the previous aspects, the situation calls for extensive investigation to determine the nature of the seismic action, its consequences and mitigation forms - here, expressed in terms of seismic design computation methods.

1.2 Research objectives

Given the complexity of the current application, several limitations are required to be imposed

- Calibration of the material model to match the normalized curves proposed by Darendeli (2011)
- Validation of 1D site response analysis through a comparison between two software: Abaqus and NERA
- Evaluation of different soil responses when subjected to various values of PGA
- Investigation of the influence of the model boundary conditions on soil response
- Evaluation of the soil-foundation interaction as well as soil-foundation-structure interaction when subjected to a real earthquake signal
- continue

1.3 Research outline

Chapter 2

Literature survey

2.1 A new design philosophy

Earthquake effects on building have been studied for over a century. Since the civil engineering community realized that guaranteeing great bearing capacity to the structures does not necessarily translate into enhanced safety, it adopted a *fail-safe* design concept. The aim included a better control over the load path and energy dissipation throughout the structure, reliable solutions in case of unforeseen collapse of an element. A number of requirements arise from the concept such as: structural elements are able to withstand exceeding dynamic loads avoiding collapse - acknowledged as *ductility design*; the building encloses specific elements that are designed to fail in order to maintain overall integrity; and bending type of failure is preferable instead of shear failure - *capacity design* (Park and Pauley, 1975). All the requirements also include that the soil should avoid reaching a yielding state, behaving completely elastic. Moreover, the calculations relied on the hypothesis of a linear viscoelastic soil performance and a fully-bonded contact between the foundation block and underground. The adopted capacity design permits plastic deformation within structural elements but avoids reaching plastic state below the ground level. In other words, the foundation continues to behave elastically avoiding passive or shear failure along the sides or base, the ground shaking does not mobilizes the soil strength, and uplifting remains limited to 1/4 of the total area whilst sliding at the soil-structure contact surface is restricted. In addition, it seemed that using factors of safety larger than 1 imposes restrictions in exploiting the non-linearly energy dissipation mechanism that, in reality, would improve structural response. Also, several phenomena may become neglected for instance, sliding or uplifting.

Following the late records of several of the strongest earthquakes, it becomes clearly that uncertainties govern assessing the maximum credible seismic loading and the characteristic parameters (PGA, PGV, etc). Larger values are observed every earthquake, the structures behave differently within limited area whilst detailed seismic monitoring of large regions seems rather impracticable; for the earthquake in Kobe (1995) the accelerograms revealed a ground acceleration of 0.85g compared to the 0.30 g value used within the design. Evaluating the buildings after the earthquake in Bucharest (1977), records showed different PGA values for structures located approximately same distance from the fault which means that PGA does not govern exclusively but there are various other factors that dictate structural behaviour (frequency content, pulse). Henceforth, the necessity of a new design concept that permits the structure to bear larger earthquakes without collapsing or to avoid substantial deformation within the structural elements. This can be translated into a lesser structural ductility demand as the subsoil mobilizes its bearing capacity. Secondly, the economical aspect plays an important role in design as the current trend suggests stronger and larger structures equipped with reinforcement that withstand great earthquakes once or twice during operation stages. What if assuming the opposite of the actual situation - under-design the foundation while limiting the accelerations transmitted to the superstructure? In this way, the ductility demand decreases in the case of the structure due to the yielding capacity of the soil failure mechanism that ensures improved safety margins, as it shall be proved further.

Recent researches focused on the behaviour of shallow foundations subjected to strong seismic loading and proved that the bearing capacity of the underlying soil is a reliable element that helps the structure to withstand such excitation and, further, the nonlinear foundation response acts rather beneficial in case of strong ground shakes. The concept of “rocking isolation” has thereby

emerged as an alternative to the conservative – yet not safer – design of foundations against strong seismic shaking (Pecker, 1998, 2003; Martin & Lam, 2000; Faccioli et al., 2001; Kutter et al., 2003; Gazetas et al., 2004; Gajan et al., 2005; Kawashima et al., 2007; Paolucci et al., 2008; Gajan & Kutter, 2008; Anastasopoulos et al., 2010, 2012; Kourkoulis et al 2012; Gazetas 2014).

The current chapter presents the particularities of the new approach together with a summary of results and conclusions yielding from numerical models compared to experimental tests (centrifuge tests). The design seems appealing mainly because of current soil conditions Groningen area displays - mostly silty clay layers carrying strip foundations - if the method proves to be successful, it might mark the beginning of a new trend in seismic design research.

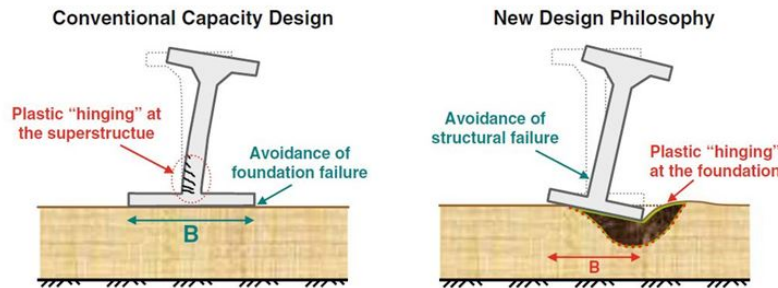


Figure 2.1: Comparison between conventional capacity design and the new design philosophy

2.2 Effects of nonlinearity

During seismic loading, the soil responds in a non-linear fashion; studies highlight three mechanisms that might occur in case of ground shaking as the figure below shows. Moreover, one can recognize two types of nonlinearities that govern the response - geometrical and material.

Geometrical nonlinearity can be described as the separation at supporting soil-strip footing interface that it usually addressed as *uplifting* whilst the material nonlinearity refers to the type of failure mechanisms governed by the bearing capacity mobilization induced by large cyclic over-turning moments - also known as *soil failure*.

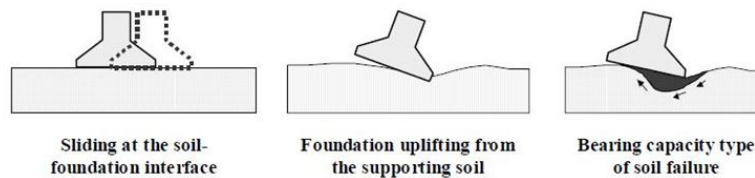


Figure 2.2: Types of nonlinearity

Scientific literature describes several types of possibilities of nonlinear soil-foundation response in terms of both geometric nonlinearity (uplifting and sliding) and material inelasticity (soil yielding) and it can be studied using the following methods:

- Winkler method - comprises the settlement-rotation at the base of the foundation which is described as a series of dashpots and springs. The model was described by a beam on an elastic medium;
- advanced macro-element modelling - the whole soil-structure system is described by an unique element which simulates the generalized force-displacement behaviour of the foundation. It is worth noting that in the elastic range, and without uplifting, the macroelement reduces to the familiar dynamic spring and dashpot(impedance) matrix;
- direct methods (finite element or finite difference methods) that successfully simulate both the soil and the foundation and the contact surface between them. This method is currently used as it proves itself efficient and accurate.

2.3 Uplifting

New philosophy not only allows one of the nonlinearity behaviour to develop within the soil but also encourages that design should apply a safety factor against uplifting and soil failure lower than unity. This way, the structure ductility demand will decrease considerably, optimizing the energy dissipation path throughout the building. Various studies focused on the rocking response simulating the soil in different manners; for example, the first models included tensionless spring-dashpot elements that described the soil (Chopra & Yim 1985, Koh et al, 1986) followed by a single macro-element which includes constitutive law that accounts for the uplift mechanism in a soil-foundation system. Ultimately, the dynamic analysis is performed in finite-element based software (Hibbit et al, 2001, Gazetas et al, 2010) - the model combines a rigid foundation footing, elasto-plastic soil and an advanced contact algorithm that inserts the potential sliding and uplifting.

The uplifting behaviour acts beneficial in dynamic conditions because the foundation can withstand higher values of bending moments compared to the ultimate capacity, Mult. The key in this rocking behaviour is the relatively short time period in which the stresses surpass the limiting values. The ground acceleration displays a rapid change in trend which makes the foundation block to decelerate, stop and rock in the opposite direction. Researchers showed the correlation between the natural period of the foundation footing and rocking potential - high frequency seismic motion lead to a somehow "safer" rocking response preventing collapse or toppling of the superstructure. Scientific literature confirms that the nature of the seismic excitations along with the fundamental period of the structure dictate the response of the soil-foundation system.

2.4 Soil yielding

The nonlinearity observed in the soil response mainly depends on the shear strains which develop within the material when the foundation experiences large angles of rotation. An important parameter arises when the foundation is subjected to large rotations - vertical safety factor FS_v defined as the ratio between the ultimate bearing capacity under pure vertical static load N_u and the currently applied axial force N - $FS_v = \frac{N_u}{N}$. Furthermore, the rotational capacity expressed in terms of ultimate moment resistance of the footing relates to both the axial force N , and the shear force Q acting on the foundation. Recent research emphasize on elaborating ultimate limit states defined by combinations of N , Q and M loads - the graphical representation is known as failure envelope.

Another of the new concept goals stands in defining this failure locus - based on load combinations and their position regarding this envelope, one can state whether the foundation acts stable or not. Many experiments based on model-scale shallow footing support this theory along with theoretical and numerical failure equations (Murff, 1994, Bransby and Randolph, 1998, Butterfield and Gottardi, 1994). Experiments (Gajan et al, 2005) highlight the influence of two parameters governing the load displacement and energy dissipation aspects of the soil-foundation interface during cyclic loading: static factor of safety regarding vertical force exclusively (FS_v) and moment-to-shear ratio - together describing the load path. Henceforth, a challenge in assessing seismic loading impact represents the correct evaluation of loading combination (shear force Q and overturning moment M) that will lead to failure for a given vertical force, N , acting on the superstructure.

2.5 Numerical analyses

Researchers developed several models that highlight the new design particularities - both 2D and three-dimensional elements were used in order to elaborate the soil-foundation system behaviour in static, cyclic and dynamic load combinations. All the FE analyses performed to research this approach used the software Abaqus. Both the soil and the foundation are modelled as eight-noded hexahedral brick-type element, the soil being considered a non-linear element while the latter elastic. Gauss points serve as reference points for extracting the results allowing a selective reduced integration - such method leads to accurate solutions including those for incompressible materials as it was confirmed in previous publications (Gazetas et al 2013).

The simulations included a saturated clay type of material characterised by an undrained shear strength S_u and a maximum shear modulus G_{max} . It proves appropriate to consider undrained

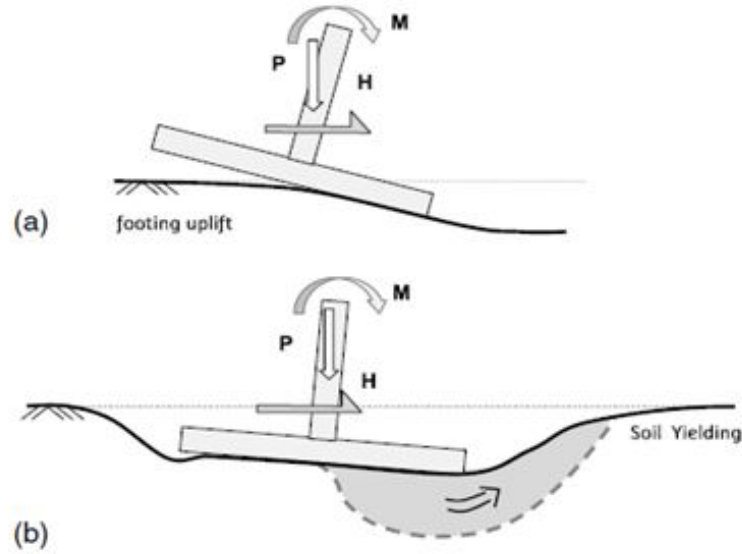


Figure 2.3: Mobilization of ultimate bearing capacity; uplifting(a) and soil yielding (b)

soil behaviour due to the rapid loading that corresponds to the seismic excitation - in addition, it allows a total stress analysis which can be described using a von Mises failure criterion along with an associative flow rule. The inelastic soil response was described through an evolution law based on both nonlinear kinematic hardening and isotropic hardening components that account for the changes the yield surface experience within the stress state.

The two main components of the structural system were separated through an interface that permits sliding and uplifting - a special contact algorithm was introduced such that the interface elements can detach in the specific areas where the angle of rotation exceeds the foundation characteristic critical rotation. The boundaries, both lateral and vertical, depend on the loading type the structure experiences - static conditions do not impose special requirements regarding the position of the boundaries. However, dynamic conditions introduce the wave propagation effect that might distort the final results due to reflections - hence the boundaries should be placed at a considerable distance from the foundation. The location of these borders account for the pressure-bulbs generated by the dissipation of vertical stresses induced by the moment loading on the foundation strips.

A series of ground-shaking accelerograms served as dynamic input for the analyses - generally strong earthquakes recorded all around the world. These data were introduced for a system that considered slender structures simplified as rigid oscillators standing on inelastic soil. The system response was further processed in order to obtain an approximation of the rocking behaviour. In addition, emphasis on the nonlinearities effects were made with respect to the fundamental period of the oscillator.

Anastasopoulos et al. [2011] investigates the response of a shallow foundation subjected to cyclic loading using results from centrifuge and large-scale tests to validate the numerical simulation performed in ABAQUS. The FE element model was subjected to several loading packets using prescribed displacements along with increasing cyclic amplitude. The output is described in terms of low strain stiffness along with the ultimate bearing capacity for both sand and clay material. In order to follow the new philosophy design assumptions, uplifting was allowed and expressed as a reduction in the effective width of the foundation combined with extensive soil plastification on the opposite side of the footing.

Overall, numerical analyses provides satisfactory results compared to experimental tests. One of the conclusions that can be drawn from the comparison refers to the influence of the rotation amplitude - an increase in the amplitude leads to a decrease in rotational stiffness and does not affect the moment capacity as the number of cycles increase; moreover, the soil settles less each rotational cycle as the number of cycles adds up contributing to vertical stiffness build-up, phe-

nomena known as soil densification. Although the effect cannot be described accurately within the numerical model, the systemic events govern the behaviour hence more attention should be paid in that area.

As discussed before, the static vertical safety factor strongly influences the rocking effectiveness and it relates to soil properties. One of the greatest challenges remains the soil parameterization, especially strength wise, due to consequences of an overestimation - large rotations at foundation level along with intolerable settlements. Varying the value of the safety factor in order to capture the differences between actual and overestimated soil characteristics, several conclusions can be drawn. Firstly, a lower FSv, translated into a lower soil strength, leads to an improved performance in contrast with the conventional design even though it records larger permanent displacements. Further, when the system is subjected to strong seismic loading, the expected response differs considerably from the actual one - uplifting governs the ideal case (FSv=5) whilst a rather sinking-dominated response yields from reality (FSv=3) leading to large accumulative settlements and foundation rotation. However, the system still reacts in an favourable manner; same situation was recorded for moderate seismic excitations -distinct responses for various FSv whose settlement level does not alter structural stability.

Secondly, even the studies successfully describe the response of 1 dof oscillator using the new philosophy design, complex structures introduce deformation compatibility requirements which prove to be vital. After Hucklebridge [1977] followed by Midorikawa et al.[2006] established the beneficial effects of introducing a rocking-column capacity into structural design, Roh and Reinhorn [2010] stress on the disadvantages of this method - one element relaxations induces overstress in another leading to unbearable deformations within the superstructure. Extensive uplifting induced by asymmetric loading distribution leads to increased rotation demand of the structural elements and further in residual irreversible deformations. Yet, the system performs in a satisfactory style for strong seismic loadings, here Takatori earthquake recorded in Kobe, 1995. In addition, the presence of beams connecting the columns might limit the drift at top level dictating, more or less, the same displacement.

2.6 Soil condition

2.6.1 Problem statement

Probably the most important aspect within the current problem it is represented by the underlying soil since it plays several roles simultaneously. It is expected to develop inelastic deformations before the superstructure as well as reliably sustain it. In addition, the soil is required to dissipate efficiently the amount of energy seismically induced avoiding, in the same time, reaching failure. The present study deals with a relatively weak clay layer, typical to northern area of Netherlands - the rock layer lacks in most of the cases, being replaced by dense sand deposits. The clay is characterised by little friction angle, cohesive properties as well as low Young's modulus values and, implicitly, low shear wave velocity - amplification of the seismic motion can be expected when dealing with such soil properties.

Appendix shows a sample CPT taken in the area of interest; following the displayed trends, it can be concluded that the soil in the area is predominantly clayey with pockets of silty sand of medium strength. Such soil conditions associated with the current type of induced earthquake define a new unique situation that requires its own seismic design approach.

2.6.2 Constitutive model

Given the problem statement and the proposed solution, the means of obtaining a reliable design method mainly relate to the underlying soil. The material will govern the overall behaviour - considering the nonlinear response that is required to be displayed in order to prove the theory. Care must be paid when choosing the material model used in the numerical analysis for it will largely dictate the outcome. A first step in deciding the implementation of the material model is understanding the application to be investigated - what phenomena happens, what are the effects, what mitigations does it require. This study in progress deals with earthquake motions, hence dynamic actions that induce a nonlinear response; therefore, the material model should enclose features that are able to describe mechanically the phenomena.

Several models were developed along the time which tried to best capture the soil inelastic response due to cyclic loadings - recent studies [Kremer and Pecker, 2002] include the uplifting effect as well as soil failure within an elastic or elasto-plastic material applied on a single macro-element. Nowadays, research trend relies on nonlinear kinematic hardening model characterized by a von Mises failure criterion along with an associated flow rule. The description of the model is rather accessible as it requires only Young's modulus E , soil yield stress σ_y and strength σ . Lemaitre and Chaboche (1990) developed the model discussing the behaviour of both sand and undrained clay soils. Dynamic analyses performed using the software ABAQUS incorporate the model and yield satisfying results. One of the model limitations stands in its incapacity of acquiring pore pressure build-up nor dissipation effects. Yet, it proves safe to assume an undrained behaviour given the short duration of seismic loading applied on the system.

Materials experience irreversible deformations when elastic limit is reached but loading persists. Theory of the elasticity explains the occurrence of slip surfaces caused by instabilities making use of the time-independent irreversible deformations. In addition, determines the permanent deformations that lead to collapse preventing them while investigating stability of the system. In order to create a plasticity model, there is the need of few features such as:

- a yield criterion
- a strain hardening rule
- a plastic flow rule

Simplifications of the constitutive models tend to responsibly neglect anisotropy and temperature independence aspects. Important to mention that the term kinematic refers to criteria evolution while isotropic relates to flow and hardening criteria. Linear kinematic hardening rules provide the translation of the loading surface making use of the hardening variable which indicates the position of the loading surface. However, its limitations call for a more advanced model able to capture the nonlinearity caused by the kinematic hardening. For instance, the linear hardening rule fails to assess the relaxation effects induced by average stresses or the ratcheting effect. In addition, stabilization occurs accordingly to a perfectly plastic cycle when subjected to prescribed strains which does not happen in reality.

Henceforth, the evolution of stress in nonlinear conditions includes two components:

- isotropic hardening component which based on the plastic deformation defines the size of the yield surface giving information related to the change in the equivalent stress;
- nonlinear kinematic hardening component which contains a purely kinematic term and a relaxation one describing the translation of the yield surface.

Considering all above, von Mises failure criterion can be briefly described using three main equations:

$$\sigma_y = \sqrt{3}S_u \quad (2.1)$$

$$\sigma_y = \frac{C}{K} + \sigma_0 \quad (2.2)$$

$$K = \frac{C}{\sqrt{3}S_u - \sigma_0} \quad (2.3)$$

where C is the initial kinematic hardening parameter, K is the parameter characterizing the rate of reduction of the kinematic hardening with increasing plastic deformation, σ_y is the maximum yield stress, σ_0 represents the yield stress at zero plastic strain and S_u is the undrained shear strength. A more detailed description of the constitutive model can be found in **Appendix** in terms of stress state, failure criterion development and mathematical formulas.

2.7 Numerical tools

Abaqus offers a wide range of elements and features that help achieving a nonlinear analysis regardless the domain or simulation expertise - it's attractiveness stands in the possibility of customization, making the software extremely flexible yet meticulous. It serves well the geotechnical engineering goals as it provides soil and structural elements, total and effective stress analysis,

consolidation, static and dynamic analysis and many more. Several types of analysis are available - the main interest relates to Abaqus/Standard. Abaqus/Standard represents a model database appropriate for both linear and nonlinear static, linear and/or low-speed nonlinear dynamic situations in which stress solutions have a great significance. The current information determines the unknown values at the current time requiring convergence and iteration - it becomes computationally expensive when it does not reach the equilibrium. Two types of behaviour are selected from the available list of analysis techniques - Static, General and Dynamic, Implicit. The first method is a static stress procedure which neglects the inertia forces and time-dependent material effects such as creep of viscoelasticity and can be both linear and nonlinear. It does account for small-displacements performing a geometrically linear analysis during that specific step while ignoring the large-displacements (represented by geometric nonlinearity).

General nonlinear dynamic analysis in Abaqus/Standard uses implicit time integration to calculate the transient dynamic or quasi-static response of a system. Quasi-static applications are primarily interested in determining a final static response. These problems typically show monotonic behavior, and inertia effects are introduced primarily to regularize unstable behavior. For example, the statically unstable behavior may be due to temporarily unconstrained rigid body modes or “snap-through” phenomena. Large time increments are taken when possible to obtain the final solution at minimal computational cost. Considerable numerical dissipation may be required to obtain convergence during certain stages of the loading history.

The following sections describe the current input accordingly to the step sequence required in Abaqus/Standard model database. Theories and equations, software description and images are introduced in order to justify the selected options that led to the current simulation and results.

2.8 Expected results

Having inclusively formulated both the problem and the means by achieving the scope, close investigations can face various directions regarding the outcome each of them being equally relevant. The current study should decide on few aspects to emphasize on, as the time does not suffice for an extensive examination. However, for the little features subjected to investigation, parametric studies are required to be able to make statements, express limitations and recommendations.

The current dissertation narrows on few aspects from the vast possibilities that come along with the new approach as Nitros et al, 2015 describe. One feature relates to the types of interface available for the analysis and two conditions are taken into consideration as it follows:

1. Fully bonded contact [FBC] - the foundation remains in perfect contact throughout the entire analysis; this condition prevents sliding and separation of the foundation from the surrounding soil because of the infinite tensional and shear capacities of the interface.
2. Tensionless sliding interface [TSI] - allows sliding at the contact surface as well as separation of the foundation; the interface follows Coulomb’s friction law in total stress depending on the adhesion coefficient α .

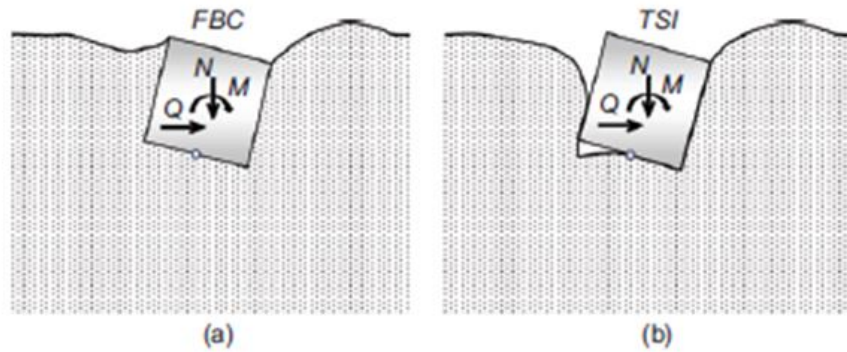


Figure 2.4: Types of boundary conditions; FBC (left) and TSI(right)

Furthermore, several studies focused on the importance of the combined NQM loading and the effect of every of the three forces susceptible to act on the foundation at certain points. Yun

& Brandy (2007) and Gouvernec (2008) formerly examined the undrained bearing capacity of rigid embedded strip foundations under combined NQM loading using a fully bonded contact, followed by Ntritsos et al (2015) who extended the studies to three-dimensional problem of squared foundations adding the option of a tensionless sliding interface.

Nevertheless, the two maximum values - horizontal load Q_{max} and overturning moment M_{max} do not solely represent the failure mechanism; infinite combinations of Q and M are comprised within a failure envelope plotted against normalized values. Additionally, the effect of the vertical load which influences the QM interaction was set to $N = 0$. The figure beneath displays the four main points on the envelope that represent different loading conditions together with significant output at carefully selected points. Both the fully bonded contact (FBC) and tensionless sliding interface (TSI) conditions were investigated and presented for comparison. Important to mention is that the authors preferred to normalize the Q and M values in accordance to the foundation width B , area A and undrained shear strength S_u - the plot contains on the x direction Q/AS_u whilst for the y direction it has M/BAS_u . The main points have specific characteristics as it follows:

- **Point A** *pure moment loading* M_{ult} ; in this point, shear force $Q = 0$. A scoop-type of mechanism is noticeable along with the plastic shear strains shadow contours. Negative rotation can be observed from both the embedded plot as well from the graph.
- **Point B** *pure rotation* M_{max} ; the tangent line to this point is parallel to the horizontal axis which acts accordingly to the associated flow rule which dictates preservation of normality. Given the dependence of moment loading, the mechanism is characterized by the scoop shape as well. The foundation response is mainly rotational with negative horizontal translation.
- **Point C** *pure horizontal translation* Q_{max} ; also, the preservation of normality can be noticed in the form of the tangent line which is parallel to the vertical axis. The failure mechanism is characterized by the sliding of the whole system; both active and passive sides exhibit failure as presented above - including the side walls effects.
- **Point D** *pure horizontal load* Q_{ult} ; reversed scoop mechanism is observed with the centre of rotation close to the soil surface - the failure mechanism equally depends on both the horizontal translation and counter-clockwise rotation.

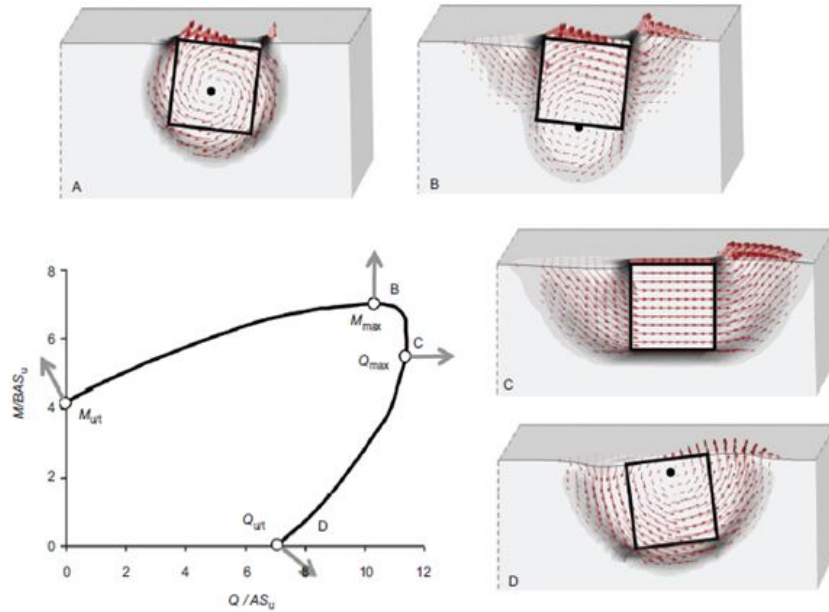


Figure 2.5: Failure envelope include four points of main interest

The herewith figure corresponds to the second type of interface - tensionless sliding interface. There are certain dissimilarities between the two contact surfaces effects - few are exposed as it follows:

- First, the failure mechanisms partly coincide with the ones earlier described in terms of the four limit points (A-D). The sliding faces only constrain the extent of the failure surface leading to no foundation-soil contact which lead to a prevention of wedge development.
- Moreover, the response associated with point B - pure rotation - is different compared to FBC which displays a scoop mechanism; a rather wedge type of failure is evident. Besides, the mechanism at lateral sides, corresponding to the sidewalls, and below the foundation strip seem half of the previous contact situation (FBC).
- Consequently, the sliding and separation of the foundation from the soil is permitted. This leads to a reduction in displacement - just about 1/2 compared to fully bonded contact. Additionally, the ratio D/B which describes the footing geometry and depth (D - height, B - width), varied within the analyses allowing the researchers to observe the influence of embedment on the Q-M failure envelopes.

Furthermore, a comparison between a FBC and a tensionless sliding interface (TSI) type of foundation was made in terms of normalised bending moment M and shear force Q - again using the failure envelopes as reference. This study introduces the influence of the axial force N and, more important, it relates the ultimate capacity of the foundation subjected to cyclic loadings under undrained conditions to the vertical safety factor ($FS_v = N/N_{ult}$). The footing non-linear response is captured throughout models that vary this safety factor, making the distinction between lightly-loaded and heavily-loaded foundations.

Chapter 3

Material calibration using one mesh element

This chapter presents the analysis corresponding to the simulation of a simple shear test in the interest of validating the available soil parameters, its inelastic behaviour and, in the same time, calibrating the FEM model for future and more complicated analysis. The procedure works on a one-mesh element - this way, the material properties can be easily calibrated reducing the computational expenses.

3.1 General

The new design philosophy will be studied numerically upon a model which consists in a homogeneous clay stratum and an elastic foundation. A typical Dutch house serves as example, being represented by a rigid strip footing type of foundation connected to a lumped mass element by a rigid beam elements. It is desirable to introduce these elements as both rigid and elastic since the main interest channels on soil inelastic response. The underlying strata is associated with a saturated, homogeneous clay responding in an undrained manner, with varying undrained shear strength S_u along its depth. The figure below briefly presents the structure introduced within the software ABAQUS - a finite element mesh based method that successfully offers complete solutions to sophisticated engineering problems regardless the application domain.

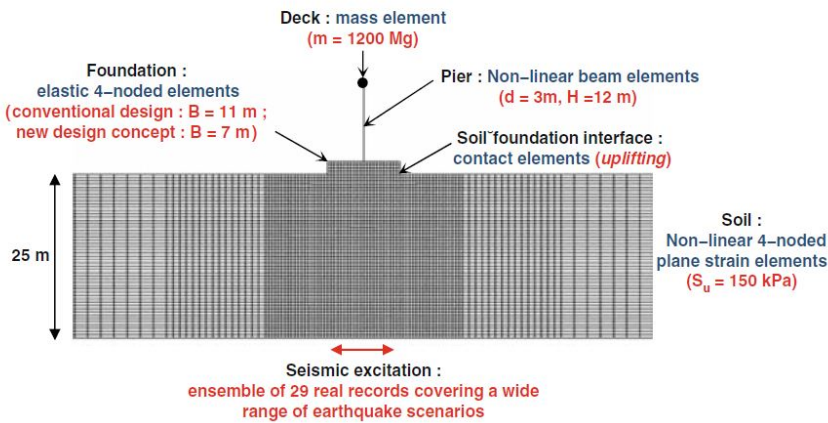


Figure 3.1: Schematization of finite element modeling in 2D space

This chapter represents the first step in achieving the final scope, because it is important to establish reliable features to the main element. The calibration becomes valid once the obtained output coincides with the data published in scientific papers that are analogous to the soil in terms of stiffness, shear modulus and damping parameters. In addition, it is possible to transfer model information from a simulation to a new Abaqus/Standard analysis, where additional model

definitions can be specified. One might first study the local behaviour of a particular component during an assembly process and then study the behaviour of the assembled product. Hence the simple shear test represents the local behaviour mechanism to be studied which will aid the material model validation.

The test helps obtaining results that further lead to the formulation of the normalized stiffness degradation curves together with the material damping ones - an important stepping stone in predicting the material inelastic behaviour when subjected the earthquake ground motions. The test assumes the application of a force on top of the sample such that shear strains are induced within the material. Stiffness degradation is observed and investigated; to better capture the features of the problem in discussion, the cyclic shear test seems more appropriate - the harmonic signal will also highlight the material damping - such a relevant factor when studying nonlinearity. Figure 3.2 shows the schematization of such simple shear test - further aspects will be discussed in more detail later on.

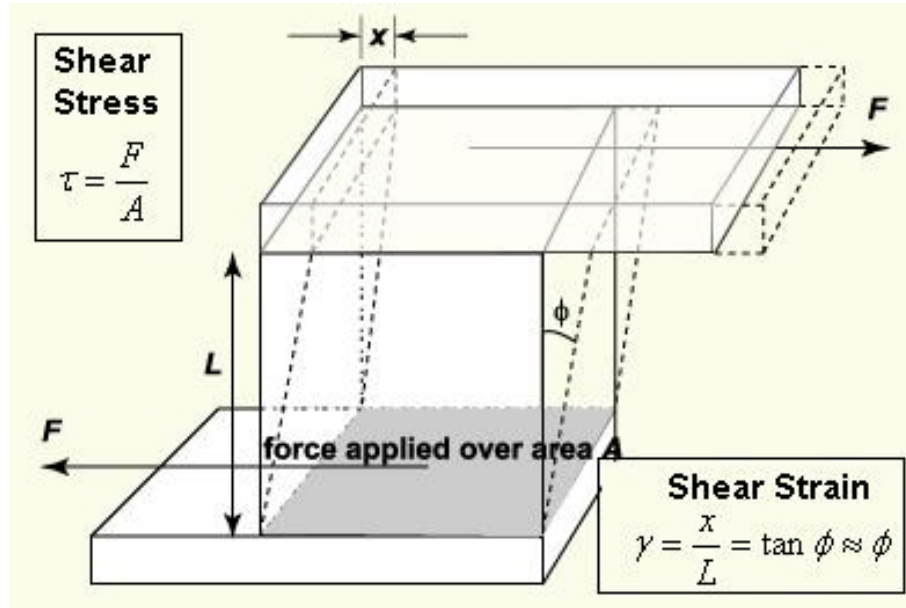


Figure 3.2: Schematization of shear test

3.2 Normalized stiffness degradation and material damping curves

The current sub-chapter presents the concept of stiffness degradation together with material damping. As the yield stress within the soil experiences increase, phenomena also known as hardening, the elastic domain undergoes a certain evolution. This evolution can be related to the elastic modulus and shear modulus implicitly - most commonly using these standard curves (G/G_{max} and damping). The site characterization plays an important role as it affects the ground motion parameters (such as Fourier spectra or response spectra). Figure 3.3 shows a schematization of the problem simplification: the soil requires the definition of two main characteristics for evaluating dynamic response. The estimation and measurement of the soil modulus reduction with respect to the shear strain has been long studied in geotechnical engineering, as it allows the prediction of the strain level which might lead to crucial modulus reduction together with the prediction of damping and the seismic response overall.

3.2.1 G/G_{max} curves

Nonlinear response can be achieved through several types of tests, monotonic and cyclic, static and dynamic, each displaying stiffness modulus degradation influenced proportional with strain development. Generally, the shear stiffness of the soil is represented by the shear modulus, G - physically it represents the slope of the shear stress and strain when plotting them one against the

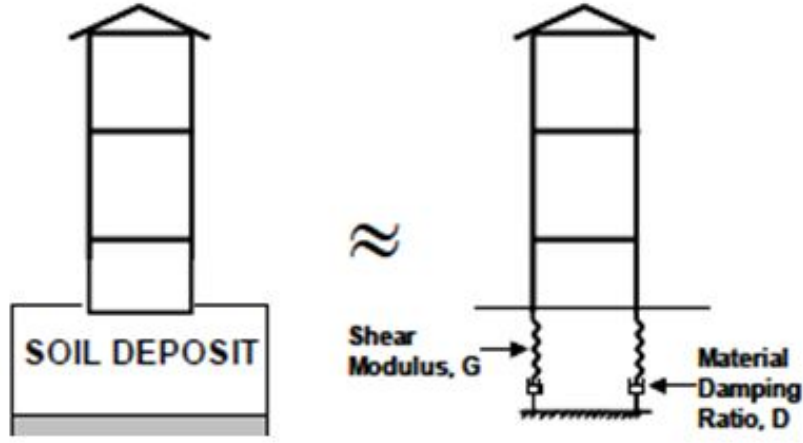


Figure 3.3: Transformation of soil deposit into two parameters - schematization

other. On these specific plots it can be noticed that when a soil is subjected to symmetric cyclic loading, hysteresis loops develop depending on the strain level. The loops support the secant shear modulus calculation which can be considered as the average shear stiffness of the soil. Features such as inclination or breadth of the hysteresis loops strongly depend on both soil stiffness and damping. Given that the cyclic behaviour of the soil is nonlinear as well as hysteretic, it becomes clear that stiffness together with the damping are strain dependent. Therefore, a series of cyclic tests should be performed with varying strain levels such that the collection of results, in terms of stiffness, lead to the normalized modulus reduction curves.

One key parameter is the shear modulus at small strains, also known as *small-strain shear modulus*, G_{max} because it plays a significant role in the elaboration of the normalized modulus reduction curves. As the name itself describes it, G_{max} serves the normalization of the cyclic tests stiffness outcome.

Damping ratio represents a material property related to the friction between soil grains, strain rate effects and inelastic stress-strain response. Each hysteresis loop describes the dissipation of energy during a loading cycle; the post-processing of data leads to the damping ratio as it depends both on the energy dissipated during a complete loading cycle at a given strain amplitude and maximum retained strain energy. The decrease in shear strain translates into decrease in dissipated energy, thus the area of the loop will suffer a reduction as well.

Similarly, the damping ratio curves are defined collecting different nonlinear soil responses based on increasing strain amplitude. However, the trend is opposite, as in the nonlinearity of the soil results in an amplification of dissipated energy, thus in the damping ratio, with increasing strain magnitude. In small-strains domain, the soil behaves elastically leading to a constant shear modulus, equal to G_{max} , as well as a constant damping ratio, equal to D_{min} .

The curves can be divided in three main areas with different behaviour properties defined by the following values:

1. **nonlinearity threshold** γ_e^t or elastic threshold; represents the strain magnitude for which the shear modulus ratio $G/G_{max} > 98\%$. The soil behaves elastically above the strain amplitude, deformations are producing but they are reversible during unloading process. The damping curve shows a correspondence with D_{min} .
2. **cyclic threshold** γ_e^t or plastic threshold; deformations become irreversible, shear modulus ratio G/G_{max} decreases to approximately 80% while damping ratio becomes 3% higher than D_{min} . Beyond this point, the soil can experience volume change.

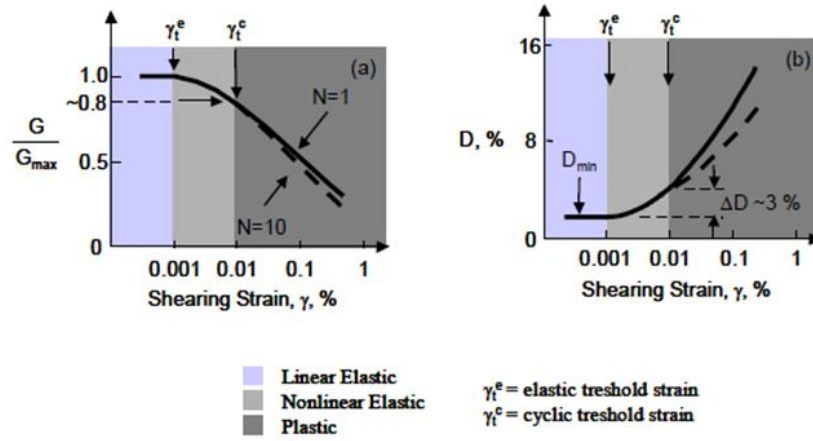


Figure 3.4: Normalized stiffness degradation curve (left) and material damping curve (right)

3.2.2 Darendeli results

Many authors treated this subject of the degradation curves, the most acknowledged being Hardin & Drnevich (1972), Vucetic & Dobry (1991), Ishibashi & Zhang (1993) and Darendeli (2001). The current thesis opts for the latter given its topicality, also for combining all the results obtained from previously mentioned authors and working on their limitations. In addition, it offers results associated with granular material which matches the Dutch soil used within the present model. M.Darendeli proposes a new empirical framework able to generate normalized modulus reduction and material damping curves. The author investigates the influence of several parameters (for instance soil plasticity or confining pressure) on the dynamic soil response using pre-existent data from University of Texas which has been collected over the past decades. The work of Darendeli is regarded as valuable because the results include the uncertainty in inelastic soil response within the probabilistic seismic hazard analysis.

As other many authors, Darendeli was inspired by the work of Hardin and Drnevich (1972) that represented a step forward in evaluating the dynamic soil behaviour. His study focuses initially on finding strengths and weaknesses in other studies in order to counteract them in his following experiments. The first observation highlights a feature common to all the previous generic curves: the confining pressure takes a relatively "fixed" value of approximately 1 atm and the curves do not incorporate the effect of the confining pressure on the inelastic soil behaviour. Ishibashi and Zhang (1993) consider soil plasticity and confining pressure but lead to unrealistic values at pressure higher than 10 atm. Darendeli proposes a four-parameter soil model which will account for the effects of the soil type, confining pressure, loading frequency and number of cycles in generating the normalized stiffness degradation and material damping curves. In addition, Table ?? presents in detail other factors that might influence the inelastic soil behaviour according to Darendeli study.

Parameter	Impact on G/G_{max} curves	Impact on D curves
Strain amplitude	***	***
Mean effective confinement	***	***
Soil type and plasticity	***	***
Number of loading cycles	*+	***++
Frequency of loading	*	**
Overconsolidation ratio	*	*
Void ratio	*	*

*** Very important ** Important * Less important ++ Soil dependent

Table 3.1: Parameters that control nonlinear soil behaviour and their relative importance on the curves according to Darendeli

Hence, the four-parameter soil model Darendeli proposes can be summarized using two main

equations as it follows:

$$\frac{G}{G_{max}} = \frac{1}{1 + \frac{\gamma}{\gamma_{ref}}^a} \quad (3.1)$$

The reference strain γ_{ref} describes the strain level at which the shear modulus G decreases to half of the maximum value G_{max} . Studies show that increasing confining pressures and soil plasticity lead to higher strain levels in the normalized modulus reduction curves. The equation of the material damping curve is then expressed as a function of two main parameters (b and D_{min}):

$$D = b\left(\frac{G}{G_{max}}\right)^{0.1} * D_{masing} + D_{min} \quad (3.2)$$

A more detail description of Darendeli's material model can be found in **Appendix**.

The current study works with the recommended reduction curves presented by Darendeli within his PhD thesis. The collection of data used by the author for investigation display a good match with the parameters of the ongoing study. A selection of matching data was extracted from Darendeli's work - tables containing values for the normalized modulus reduction and damping curves; data corresponds to a soil with a plasticity index of PI=25% and a confining pressure of 1 atmosphere which also matches current conditions. **Appendix 3** shows the values used for comparison and validation of the present analysis.

3.3 Modelling

The analysis starts with the assumption of one element - for the ease of material calibration - homogeneous 3D solid. The model simulates a strain-controlled simple shear test, the parameters correspond to a sample taken within the homogeneous clay layer previously described located at 10m below surface. A single parameter set suffices given the dimensions of the sample: 1m each side; The bottom nodes are behaving independently, being fixed at all times during the analysis whilst the top nodes are connected through an MPC (multi-point connector) - a feature available within the software that links the top nodes to a master node (centre point). All load and boundary conditions are applied to the master node solely which transmits them further to the slave nodes guaranteeing equal displacements. The master node is assigned with its own system of coordinates which corresponds to the whole model system.

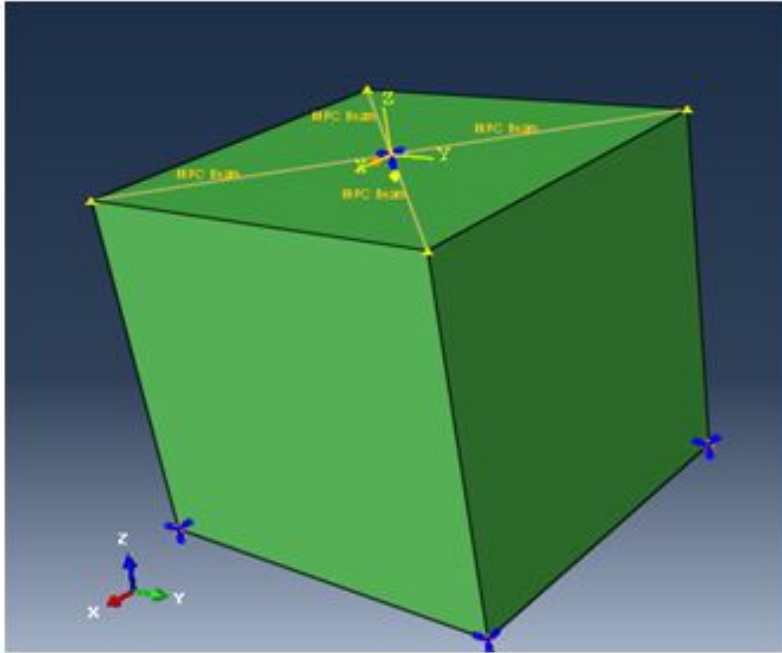


Figure 3.5: Schematization of one mesh element model

3.3.1 Steps

First step This sub-chapter presents the steps taken within this calculation including the boundary and the loads conditions as well as a short description of the testing procedure. The main idea behind this analysis is first to confine the sample to mimic the natural conditions in terms of stress path. Secondly, the shearing stage consists in controlling and varying the applied strain in order to obtain the nonlinear response. More details about the process are presents below.

The first step – **confinement** - assumes the application of the confining pressure at the (top) reference point. The overburden stress is calculated as a function of the unit weight of the soil and the depth at which the sample is considered to be. Considering the total stress analysis, the pore water pressure is also accounted for within the value. Considering the sample located 10m below the surface and performing the corresponding calculations, it yields a confining pressure $F=100\text{kPa}$. Equilibrium is taken into account since a total stress analysis is performed – no attention should be pointed at the development of excess pore pressure nor drainage. The illustration below represents the directions with the associated boundary conditions for the top master slave; it turns out that only the vertical translation is permitted whilst all other displacements are restricted. Subsequently, the overburden pressure is applied on the same vertical direction. In addition, the sample has all the bottom nodes restricted for both translation and rotation.

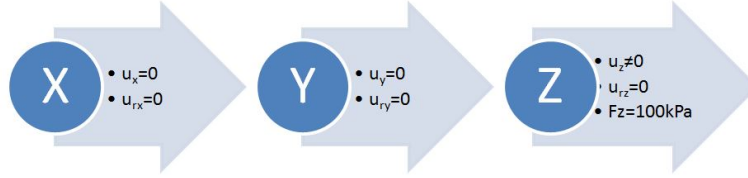


Figure 3.6: Boundary conditions applied at bottom nodes during confinement step

The step is defined as static, general - the analysis can account for both linear and nonlinear response. It ignores the time-dependent material effects such as creep or swelling, but accounts for rate-dependent plasticity or hysteretic behaviour. In a general static analysis the code is iteratively solving $[Kt]du = dF$, where $[Kt]$ is the tangent stiffness matrix, du is the vector of unknown nodal displacements, and dF is the incremental load vector. Each step starts with the end conditions of the previous one, with the state of the model evolving throughout the history of general analysis steps as it responds to the history of loading. The step is associated with a direct linear equation solver - a useful tool in both linear and nonlinear analysis - the solver finds the exact solution to the system of linear equations using a direct Gauss elimination method.

Second step The second step – shearing – propagates most of the existing boundary conditions, deactivating the restriction of top master node translation on x direction. In addition, on the same direction, a new boundary condition is created specific for the strain-controlled shear test. The principle of the simple shear test is to induce direct shear within the sample and it represents a direct method of determining the shear modulus of the soil; hence the usefulness of the current application.

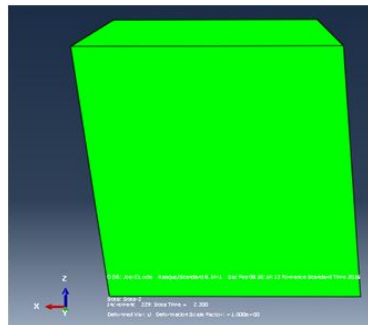


Figure 3.7: Deformed shape of the model after second step

The boundary condition which permits translation on x direction is assigned with an amplitude feature. Strictly speaking, the cyclic tests should be performed with irregular amplitudes in order to accurately simulate the earthquake action; however, given the difficulties in performing such irregular tests, the simple shear test was always simplified to an uniform amplitude test.

displays the uniform amplitude defined in current analysis - it can be regarded as a "template" for further analyses. The introduced plot is multiplied by each value assigned to the displacement boundary (u_x) leading to different soil responses. The value of the applied cyclic strain varies capturing the transition between small strain and large strain domain as well (1% - 1E-4%). Several jobs are performed with different strain values until fully elastic behaviour is attained. Each job results in a different response where the main emphasis goes on the shear strain-stress plot that describes hysteretic loops. Based on these loops, the most important parameters for degradation of the stiffness curves are determined, as well as the damping ratio.

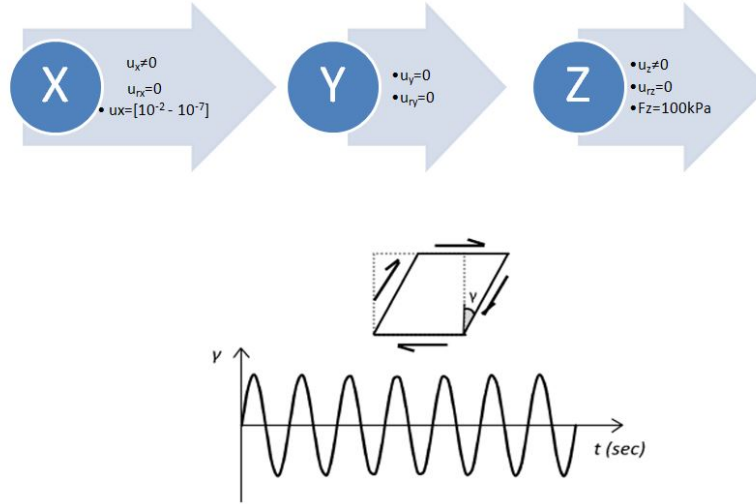


Figure 3.8: Boundary condition at bottom nodes during second step (top); schematization of strain-controlled test concept including uniform cyclic load (bottom)

Abaqus offers several methods for performing dynamic analysis of problems in which inertia effects are considered. Direct integration of the system must be used when nonlinear dynamic response is being studied. The step is defined as a dynamic one; general linear or nonlinear dynamic analysis in Abaqus/Standard uses implicit time integration to calculate the transient dynamic response of a system. Nonlinearities are usually more simply accounted for in dynamic situations than in static situations because the inertia terms provide mathematical stability to the system; thus, the method is successful in all but the most extreme cases. An automatic incrementation scheme is provided for use with the general implicit dynamic integration method. The scheme uses a half-step residual control to ensure an accurate dynamic solution. The half-step residual is the equilibrium residual error (out-of-balance forces) halfway through a time increment; for a continuum solution the equilibrium residual should be moderately small compared to significant forces in the problem.

3.4 Material description

For the current situation, Abaqus requires the definition of several behaviour components such as: density, elastic, plastic, damping and, eventually, a subroutine which introduces the distribution of the ultimate shear strength along the depth and the correlation between the stiffness and the strength parameters (E and S_u).

3.4.1 Input parameters

As mentioned before, the analysis considers several parameters that are characteristic to the soil in Groningen area – a silty clay, weak to medium weak. In addition, a homogeneous clay layer of 20m is considered – for the ease of the calculation, the soil is converted in a one-layered soil column

such that the strength and stiffness parameter distribution along the depth is linear. This chapter presents parameters derived from both measurements and empirical equations, the analysis of one element subjected to a strain-controlled shear test and the results in terms of stiffness degradation and damping. The more detailed equations and methods of obtaining the parameters can be found in **Appendix 5555**

Stresses Total vertical stress represents the starting value for the evaluation of the stresses in each soil segment; assuming vertical equilibrium and neglecting the surcharge, the vertical stresses can be determined. In addition, the shear stresses on the vertical planes are assumed zero hence, no stress transformation is needed.

Conform Terzaghi's principle, total stress comprises the *effective stress* - which acts on the contact surfaces between the soil grains - and the *pore pressure* - which is considered isotropic and it is in the form of water and air. Due to the isotropic character of the water, the shear stresses are transmitted to and through the skeleton grains exclusively. The case of pure shear suggests change in shape at constant volume and deformations of the granular material are determined by change in effective stresses. That is the reason why the initial parameters are expressed as functions of effective stresses. The equations leading to the definition of the stress state are described in **Appendix 2332**

The current analysis case deals with undrained conditions within a total stress analysis; for a foundation slab subjected to permanent load, pore pressure will initially develop decreasing the effective stresses and, since water drainage does not occur immediately, the soil underneath will behave in an undrained fashion. Subsequently, consolidation occurs with dissipation of the excess pore pressure - from this moment onward the foundation is gaining more stability as it passed the critical situation. Moreover, during earthquake, due to the dynamic loading, the undrained behaviour is displayed; hence, the calculation will take this assumption into consideration.

Given the supposition of no volume changes specific to the undrained conditions, the isotropic effective stresses remain constant which means that the mean effective stress remains constant as well:

$$\sigma'_0 = \frac{1}{3}(\sigma'_z + 2\sigma'_x) \quad (3.3)$$

Undrained shear strength The value of the undrained shear strength can be determined with the use of multiple parameters as well as methods. .5 shows a collection of methods applied for obtaining the undrained shear strength of the soil based on both empirical and measurements data and the plot containing all the values can be seen in Figure 22 One important method to mention is represented by the study of Den Haan (2011) as he treats the current situation (of Groningen soils) in his article "Ongedraineerde sterkte van slappe Nederlandse grond" developing new equations for obtaining undrained shear strength of clayey soils. Crux Engineering develops a Plaxis model to validate the equation leading to a set of formulae as a function of the normalized stress given in Table 1.

For the current situation, considering the normalized shear stress to be 40kPa as characteristic, the undrained shear strength equation becomes:

$$S_u = 2.8 + 0.37 * \sigma'_v \quad (3.4)$$

Classification	Normalized undrained shear strength	Undrained shear strength
[-]	[kPa]	[kPa]
Organic clay (medium)	25	$c_{u,ref} = s_u = 2.8 + 0.22\sigma'_v$
Clay, slightly sandy(weak)	40	$c_{u,ref} = s_u = 2.8 + 0.37\sigma'_v$
Clay, slightly sandy (medium)	55	$c_{u,ref} = s_u = 2.8 + 0.52\sigma'_v$
Clay, slightly sandy (dense)	80	$c_{u,ref} = s_u = 2.8 + 0.77\sigma'_v$

Table 3.2: Undrained shear strength equations according to Den Haan

The graph shows the agreement between all the methods aforementioned; the decision of continuing the calculations with Den Haan (1) formulae is due to its applicability for the soft Dutch soils - which is the current case - and the measurements consistency. **Appendix 1** shows the table of values characteristic for the soil including the associated stiffness parameters. The analysis

relies on this set of parameters representing the soil sub-layer located at a depth of 10m below surface.

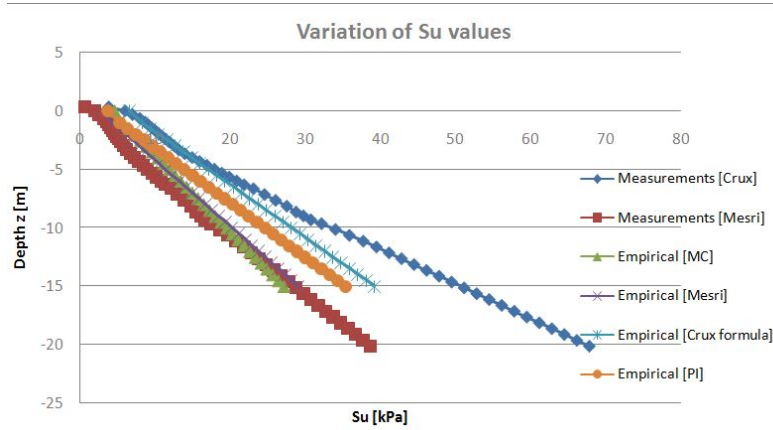


Figure 3.9: Various values of the undrained shear strength S_u

Stiffness Stiffness plays an important role in dynamic analysis hence the correct determination becomes significant for evaluating the non-linear soil response. This sub-chapter presents two different methods of calculating the shear modulus - empirical and based on measurements - this way one can compare and validate the results.

Shear modulus determined empirically For the empirical determination of the stiffness G_{max} , a simple equation was used based on studies performed by Hardin and Black (1968). The expression contains a void-ratio function together with a confining-stress function and it was developed mainly based on laboratory test results. The first function accounts for the plasticity index as well as the void ratio as an alternative to the overconsolidation ratio whilst the later considers the stresses developed within the soil. The equation described by the two authors can be written as:

$$G_{max} = C \frac{(2.973 - e)^2}{1 + e} OCR^K (p')^{0.5} \quad (3.5)$$

where e - void ratio; OCR - overconsolidation ratio p' - initial mean effective stress (kPa) K - coefficient which directly relates to the plasticity index I_p ; C - constant = 3.23 1/2

Thirty years later, after several refinements of the previous equation, Shibuya et al. (1997) performed several tests in order to introduce a simplified void-ratio function using the specific volume. They avoided the sharp reduction of stiffness observed in Hardin & Black equation introducing a sounder physical parameter equivalent to the dry density; consequently, the formula becomes:

$$\frac{G_{max}}{p_r} = \frac{B}{(1 + e)^{2.4}} \left(\frac{p'}{p_r} \right)^{0.5} \quad (3.6)$$

where p_r - is the reference pressure, considered 1kPa; e - void ratio, p' - mean effective stress, factor B for soft clays ranged between [18000 - 30000] with an average of 24000, as it is proved in Shibuya et al (1997) study. Current soil investigation and laboratory tests aimed to determine several specific values, among them the void ratio; for a silty clay, medium weak, the results yield values between $e = 0.8 - 0.9$, while the plasticity index was proved to have values $I_p = 25\% - 30\%$. Given the fact that the reference pressure is 1kPa the ratio p'/p_r turns into the value of the mean effective stress; this is calculated based on the equations described previously and varies along the depth. Therefore, performing the calculation with the corresponding parameters, it results the equation for the G_{max} as it is shown:

$$G_{max} = [5400 - 5800](\sigma'_0)^{0.5} \quad (3.7)$$

Shear modulus determined based on available measurements On the other hand, the measurements give soil features in terms of shear wave velocity. In homogeneous and isotropic medium, there are two types of waves - pressure and shear waves. The shear wave velocity V_s is controlled by the shear modulus as it is shown:

$$V_s = \sqrt{\frac{G_0}{\rho}} \quad (3.8)$$

where G_0 – shear modulus (calculated previously) [kPa] ρ – the solid density [kg/m³] $V_{s,30}$ is calculated as the time for a shear wave to travel from a depth of 30 m to the ground surface, not the arithmetic average of V_s to a depth of 30 m. There are various classification based on the soil type, one presented below corresponding to the normative Eurocode EN1998-1-1:cl.3.1.2 representing the ground types and the specific shear wave velocities:

Type of ground soil (EN1998-1-1,cl.3.1.2)				
Ground type	Description of stratigraphic profile	Parameters		
		$v_{s,30}$ (m/s)	N_{SPT} (blows/30cm)	c_u (kPa)
A	Rock or other rock-like geological formation, including at most 5 m of weaker material at the surface.	>800	-	-
B	Deposits of very dense sand, gravel, or very stiff clay, at least several tens of metres in thickness, characterised by a gradual increase of mechanical properties with depth.	360-800	>50	>250
C	Deep deposits of dense or medium dense sand, gravel or stiff clay with thickness from several tens to many hundreds of metres.	180-360	15-50	70-250
D	Deposits of loose-to-medium cohesion less soil (with or without some soft cohesive layers), or of predominantly soft-to-firm cohesive soil.	<180	<15	<70
E	A soil profile consisting of a surface alluvium layer with v_s values of type C or D and thickness varying between about 5 m and 20 m, underlain by stiffer material with $v_s > 800$ m/s.			
S_1	Deposits consisting, or containing a layer at least 10 m thick, of soft clays/silts with a high plasticity index	<100 (indicative)	-	10-20
S_2	Deposits of liquefiable soils, of sensitive clays, or any other soil profile not included in types A – E or S_1			

Figure 3.10: Shear wave velocities according to the ground type [EN1998]

The current case deals with soft soil, henceforth the $V_{s,30}$ is considered to be 180m/s –the real values determined from CPT tests and processed using Robertson’s method seem to match to table previously presented. **Appendix 2** shows the measurements in terms of CPT results as well as $V_{s,30}$. [add THE CPT].

The G_0 is further derived from V_s as previously explained. The elastic moduli is related to the shear modulus through the Poisson ratio:

$$E' = 2G(1 + \nu') \quad (3.9)$$

The current analysis requires strength and stiffness parameters with respect to undrained total stress analysis, therefore the formula described above will be transformed accordingly:

$$E_u = \frac{3E'}{3 - (1 - 2\nu')} \quad (3.10)$$

$$\nu_u = \frac{3\nu' + (1 - 2\nu')B}{3\nu' + (1 - 2\nu')B} \quad (3.11)$$

The Poisson ratio for silty-clay in drained/effective analysis was considered $\nu' = 0.3$ whilst the undrained behaviour considers a value of 0.5 due to assumption of a fully saturated soil ($B=1$). For calculation purposes, this value will be altered to 0.48 to avoid a bulk density tending to infinity.

$$E = 2G(1 + \nu') \quad (3.12)$$

$$\nu_u = 0.5 \longrightarrow G_u = 3E_u \quad (3.13)$$

$$\frac{E_u}{2(1 + \nu_u)} = \frac{E'}{2(1 + \nu')}; E_u = \frac{3E'}{2(1 + \nu')} \quad (3.14)$$

In addition, from empirical correlation (Hardin and Richart 1963; Robertson and Campanella 1983a,b; Seed et al 1986; Mayne and Rix, 1993) the elastic moduli can also be expressed as a function of the overburden stress σ_y .

$$C = a\sigma_y \quad (3.15)$$

where C - initial hardening Young's modulus and σ_y corresponds to von Mises assumptions ($\sigma_y = \sqrt{3}S_u$) and a is a correlation factor with values between 150 and 1000 for clays, and 1000-10,000 for sands. So, the previous equations, if expressed in terms of Young's modulus at small strains and undrained shear strength, it will become:

$$E = a * S_u; a = [300 - 1800] \quad (3.16)$$

Appendix 1 presents both the tables containing the input parameters - from in-situ measurements and empirically determined. Nonetheless, differences appear due to several causes and assumptions taken into account but also because of the calculation methods. Few of the sources of dissimilarity are presented below:

1. measurements data presents a heterogeneous soil stratification consisting in silty clay at the upper part of the layer and potklei in the lower one whilst the empirical data accounts for a completely homogeneous layer.
2. the measurement related properties do not vary linearly along the depth in reality as it can be seen in figure 3.11 while empirical equations lead to a linearity between parameters; for instance, empirically determined stiffness G_0 is calculated combining the factor and the mean effective stress - which varies linearly with depth - thus the stiffness will result in a linearly distribution as well. Measurements do not display the same fashion given the Vs variation with depth.
3. empirical data works with factors determined for a specific type of soil - for the simplicity of the calculation, many assumptions lead to the selection of such factors that can over or underestimate reality.
4. the shear wave velocity Vs represents only an approximate of the entire region. Different results can be obtained in the vicinity of the actual measurements. However, its measurements offers a powerful tool for establishing the soil stiffness properties.

Such dissimilarities are clearly expected, the main interest in this situation pointing the correspondence between values; it was opted to continue the calculations using the empirical values for various reasons; one of them being represented by the future analysis, site response analysis, in combination with the software requirements - the model definition in Abaqus for a multi-layered material entails a subroutine that relates different parameters. For the current application, the connection between the parameters introduced within the subroutine refers to the correspondence between the Young's modulus and the undrained shear strength. This subject will be explained in more detail in the next chapter within the material definition part.

3.4.2 Non-linear parameters (kinematic hardening model with Von Mises failure criterion)

The constitutive model marks down to several equations which describe the inelastic soil response. As a matter of fact, the software Abaqus only requires the selection of the appropriate material module which nominates the failure criterion and its corresponding parameters; the current case

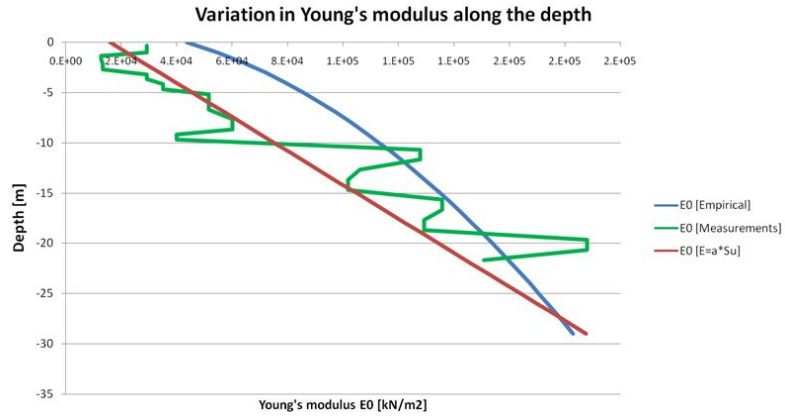


Figure 3.11: Young's modulus - Comparison between empirical and measurement data

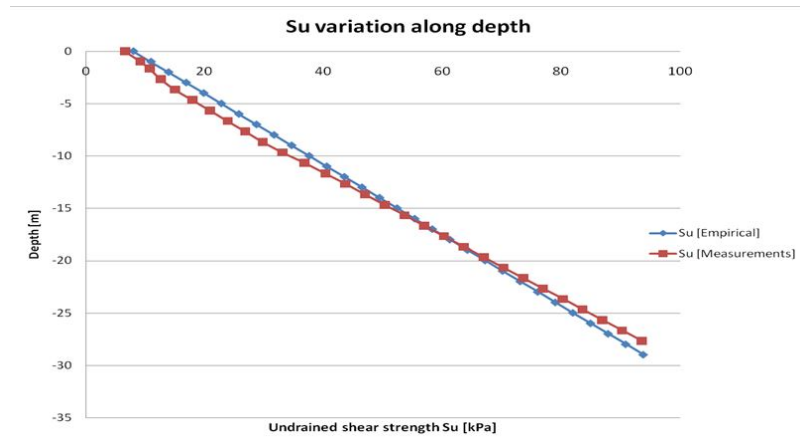


Figure 3.12: Undrained shear strength - Comparison between empirical and measurement data

deals with only three parameters momentarily: the maximum stress at zero plastic strain - σ_0 , elastic Young's modulus $E = 2 * (1 + \nu)G_0$ and the ultimate strength σ_u or S_u . The evolution of kinematic hardening component of the yield stress is defined by:

$$\dot{\alpha} = C \frac{1}{\sigma_0} (\sigma - \alpha) \dot{\epsilon}^{pl} - \gamma \alpha \dot{\epsilon}^{pl} \quad (3.17)$$

where

- C - the initial kinematic hardening modulus represented by Young's modulus at small strains;
- K - parameter determining the rate of decrease of kinematic hardening with increasing plastic deformation;
- α - backstress;
- $\dot{\epsilon}^{pl}$ - plastic strain rate;

For clays, the following equation describes the maximum yield stress σ_y :

$$\sigma_y = \sqrt{3} S_u \quad (3.18)$$

$$K = \frac{C}{\sqrt{3} S_u - \sigma_0} \quad (3.19)$$

The yield stress at zero plastic strain σ_0 controls the initiation of inelastic behaviour and it is defined as it results:

$$\sigma_0 = \frac{G_{max}}{\gamma_{el}} \quad (3.20)$$

The shear modulus was derived previously from the Vs values measured by CPT, as well as all other stiffness parameters. The elastic limit strain represents the point in which the plasticity is triggered - here was taken into calculation as 10-4. Hence all the kinematic parameters are further obtained based on this value and it can be seen in **Appendix 1**.

3.5 Results

3.5.1 General

The connection between the stress-strain plot and modulus reduction curves is straightforward for two-way cyclic loading (complete stress cycle). The set-up of the normalized stiffness degradation curve allows the prediction of stress-strain path of the soil subjected to monotonic loading. The analysis starts by creating several jobs in which the strain amplitude varied its values between $\gamma = 0.1\% - 10 - 5\%$. From each analysis the stress-strain paths are extracted and plotted leading to different curves also known as hysteresis loops. The secant shear modulus is further calculated as:

$$G = \frac{\tau}{\gamma} \quad (3.21)$$

All the shear modulus values are then collected within a table which will serve for the construction of the normalized modulus degradation curve. The small-strain shear modulus G_{max} can be determined based on elastic Young's modulus, E_0 , and it serves for the normalization of the obtain shear moduli.

$$G_0 = \frac{E_0}{2(1 + \nu)} \quad (3.22)$$

An example of the applied amplitude can be observed in Figure 3.13. The current model includes a maximum amplitude of $A_{max} = 1$, a period $T = 0.3s$ and a period shift of zero seconds. Each set of calculation will apply the shear strain value to this signal leading to the cyclic effect.

Such inelastic response proves to be not that sensitive to the frequency of the signal but to the maximum recorded amplitude as Gazetas, 2004 shows in his study of foundation rocking and uplifting. Indeed, models showed that the same cyclic response is obtained when varying the amplitude frequency. The degradation curve is then composed by the normalization of the secant stiffness displayed by each analysis, G , with the maximum shear stiffness value corresponding to the sample, G_{max} . Meanwhile, the damping ratio is expressed as the ratio between the dissipated

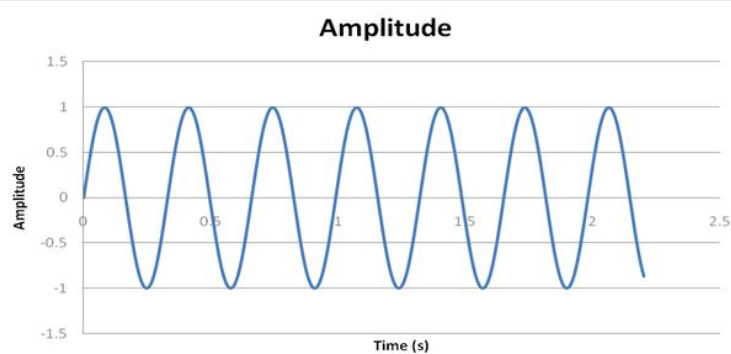


Figure 3.13: Input cyclic signal

energy and stored strain energy in one complete and stable cycle of motion. Based on Figure 3.14, the dissipated energy A_L is described by the area inside the loop and it is calculated using the integral of the stress-strain curve as it follows:

$$A_L = \int \tau d\gamma \quad (3.23)$$

while the stored strain energy A_T is expressed as:

$$A_T = \frac{\tau \gamma}{2} \quad (3.24)$$

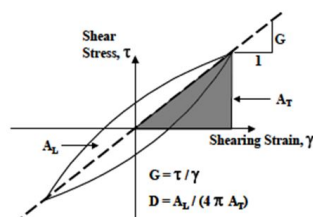


Figure 3.14: Calculation of damping ratio using a hysteresis loop

3.5.2 Parameters that influence the soil response

Another investigated aspect was the influence of the sample location within the layer on the inelastic response. Various analyses were performed with values correlated with different soil depth. The table below shows the data used for calculation and the variation in parameters followed by a plot that helps visualizing the results.

Sample depth	Confinement stress	Young's modulus	Undrained shear strength	Stress at zero plastic strain	Hardening parameter
z[m]	F [kPa]	C=E [MPa]	Su [kPa]	σ_0 [kPa]	K [-]
1	20	12.5	8.61	0.61	1283
5	50	38.2	19.09	3.30	1283
13	100	85.5	42.76	7.41	1283
15	150	97.4	48.68	8.43	1283
20	230	126.9	63.5	11.0	1283

Table 3.3: Data for various sample location within the layer

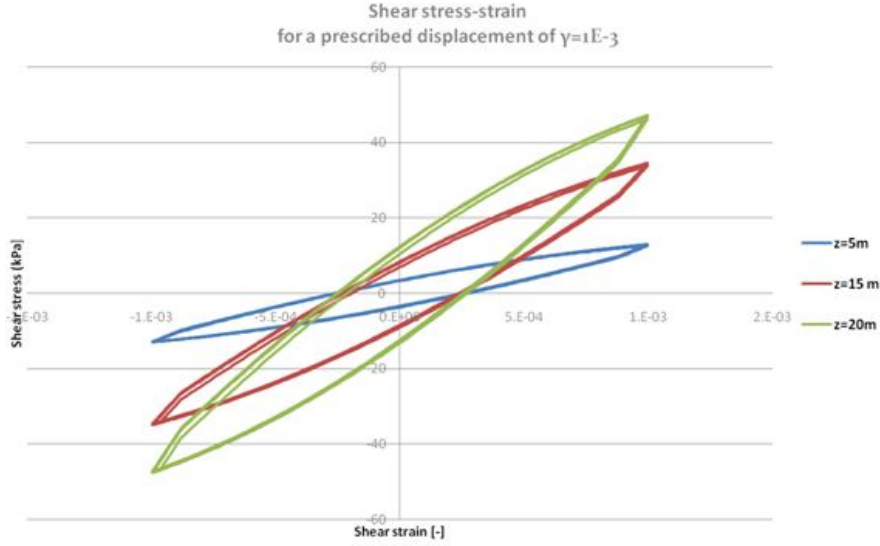


Figure 3.15: Various responses according to the depth

The figure displays the difference in response for three location of the sample; nonetheless, the stiffness plays an important part as well as the undrained shear strength. The three loops correspond to different stress levels, thus different amounts of dissipated energy. Important to mention that the maximum shear stress associated to each loop matches the undrained shear strength ($\tau_{max} = S_u$), this way validating the undrained conditions and the analysis itself.

The parametric study continued with the variation of the prescribed displacement or the shear strain at which the plastic response is triggered. Darendeli results display the plasticity being activated at a strain level of $10^{-5}\%$; the current analysis shows a better agreement when using a prescribed displacement of $10^{-4}\%$ than the lower one. This decides that the calculation should continue with the aforementioned value in order to get comparable results with Darendeli ones.

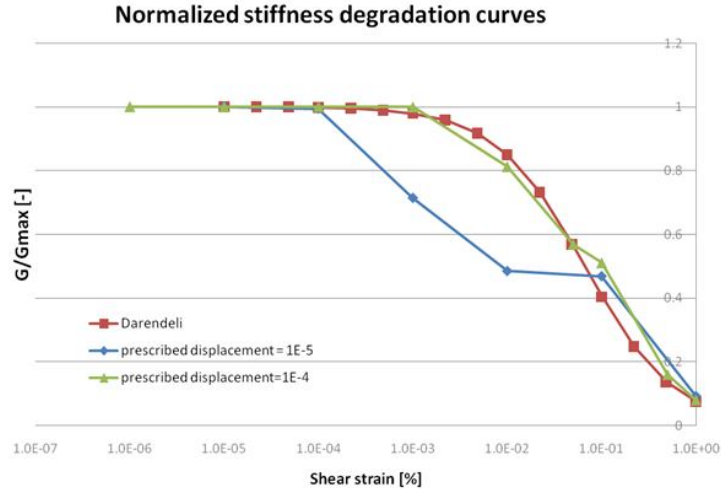


Figure 3.16: Normalized stiffness degradation curves for various plastic strains

3.5.3 Validation - Comparison with Darendeli curves

The comparison shows a relatively good agreement between the current results and Darendeli data. Few remarks can be stated regarding the obtained values. First, the increase in stiffness can be

observed from the first plot with increasing depth. Plasticity is triggered earlier around surface level compared to deeper layers.

The damping ratio might seem not to follow the exact same shape as Darendeli; important to mention that the current case ignores several features which the author included within his calculation. First, there is no additional damping introduced in the analysis; Rayleigh damping parameters were not comprised but they will in the future calculation. This explains the zero damping values once the elastic domain is active - meanwhile Darendeli results still show damping at that strain level. Moreover, Darendeli assumes that damping for any given strain level is a function of the curvature coefficient - which is also neglected in the current analysis. Also, Darendeli scales the results with several coefficients (such as curvature coefficient, scaling coefficient) together with the D_{min} in order to get a better match between experimental data and empirically obtained results.

Given these, it can be concluded that the current results match to a certain extent Darendeli curves and that a good calibration of the one element shear test was obtained.

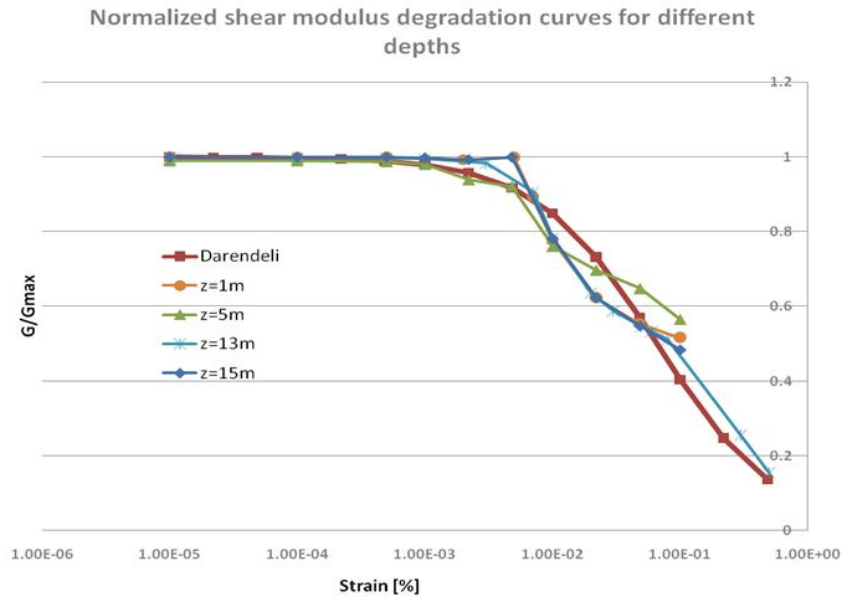


Figure 3.17: Normalized stiffness degradation curves comparison

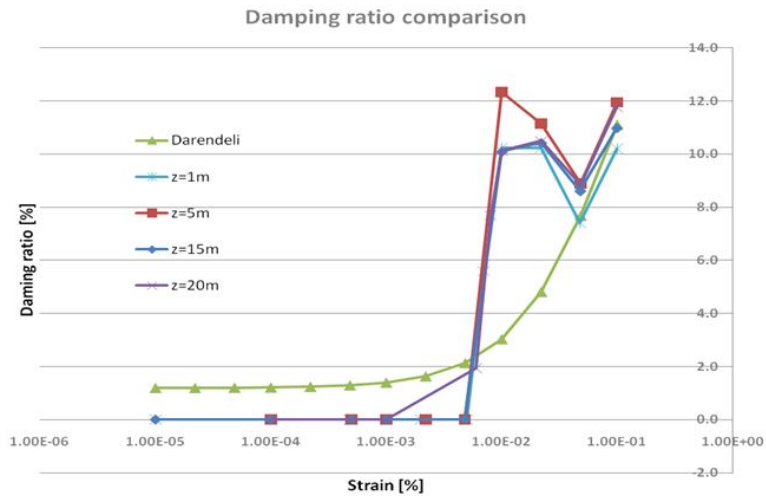


Figure 3.18: Damping ratio comparison

3.6 Conclusions

Chapter 4

Site Response Analysis

4.1 Introduction

The seismic waves generated at the bedrock suffer variation until they reach the surface; both the characteristics of the ground shaking as well as the material parameters influence the ground response that can be expressed in terms of amplitude, duration and frequency content. The importance of the ground response analysis relates to the overall dynamic study of the superstructure; the seismic waves can experience amplification or de-amplification at surface level as a function of soil damping properties together with encountered frequencies. In the case of matching frequencies between the maximum amplification of ground motion and natural frequency of the structure, the two elements (soil and construction) resonate one with the other. This translates into high oscillating amplitudes and thus considerable damage. In conclusion, performing a site response analysis enables the engineers to predict the site frequency content, the spectral acceleration alongside to peak ground acceleration and thus to create a reliable seismic design. presents the schematization of the entire site response analysis.

4.2 Model description

The model represents an extrapolation of the previous analysis step; the soil sample becomes a homogeneous layer with properties increasing linearly with depth and it is subjected to two steps: the gravity and the seismic excitation. The height of the layer is assumed 30 meters, this way it follows the prescriptions found in standards thus the possibility of a further meaningful results comparison. In order to simulate a one dimensional analysis, the problem is analyzed in a 2D space with the thickness of the soil relatively small compared to the height; shows the schematization of the problem, the blue numbers representing the nodes, the red numbers the elements, respectively. The 1D soil column represents the typical model for a site response analysis as the shear wave propagation direction is assumed to be vertical - thus the main interest stands in the interaction between the soil profile and the vertically travelling seismic wave.

The validation of the model will consists of a result comparison between the analysis performed in Abaqus and the ones obtained from NERA together with the Groningen SRA performed by ARUP - the latter only offers a rough guide. The differences between the means of analysis will be investigated, the results will be expressed in terms of acceleration response in frequency domain together with stiffness degradation.

4.2.1 Steps of analysis

The first step of the analysis simulates the natural stress state within the soil using a gravity load spread all over the layer and it is declared as static, general. The self weight of the elements provide the loads, therefore no need of extra loading conditions. The definition of the gravity load involves the software in updating several parameters to account for the confining pressure. As the schematization shows, the model contains elements and nodes - the nodes will be assigned with boundary conditions reproducing the one dimensional vertical propagation of the shear waves. The base nodes are constrained in both directions in accordance with the assumption of the bedrock presence underneath the soil layer whilst each pair of nodes horizontally displayed are linked using

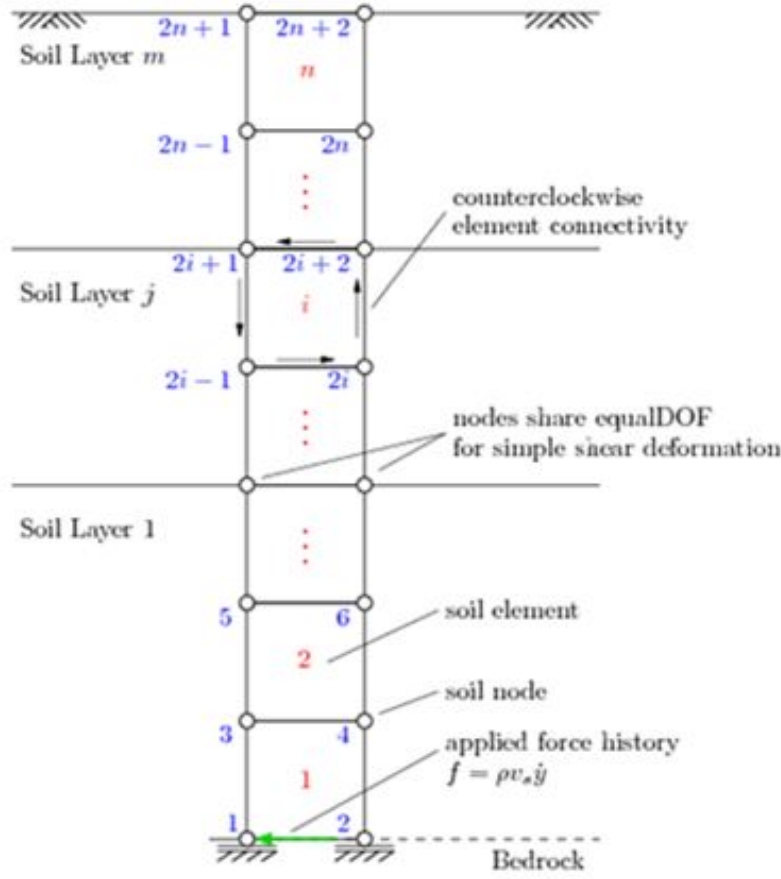


Figure 4.1: Schematization of soil column

a feature called multi-point constraint - this provides a pinned joint between the nodes making the global displacements be equal leaving the rotations independent.

The second step represents the soil layer subjected to the earthquake motion; it is defined as a dynamic step calculated using an implicit integration scheme. During the step, the user propagates the boundary conditions aforementioned with the exception of the horizontal base constraint; it is replaced by an acceleration type of boundary condition that is assigned with an amplitude curve - this allows the user to define an arbitrary variation in time (or frequency) of any quantity or can be defined as a mathematical function (e.g. sinusoidal), series of values in time (acceleration history) and many more. For the current study, the amplitude curve contained the acceleration-time record for a period of 10 seconds as 4.2 shows. By assigning the amplitude curve to the boundary condition on X direction together with a restraint in Y direction, the software applies this acceleration input to the base of the sample simulating the earthquake motion.

4.2.2 Input parameters

The material parameters can be divided into several categories the software requires:

1. *Elastic* - again, Young's modulus together with Poisson's ratio becomes sufficient for the definition of elastic domain.
2. *Plastic* - the nonlinear isotropic/kinematic model applies von Mises failure criterion for which three parameters are required: yield stress at zero plastic strain σ_0 , small-strain Young's modulus C and hardening parameter K .
3. *Density* - the soil layer is considered to be homogeneous, thus one single material is define. So density for a silty-clay medium weak was considered 1.8kg/m^3
4. *Damping* - the software offers many damping options [from numerical to material damping]; however, for this example the Rayleigh damping parameters α and β are sufficient for the

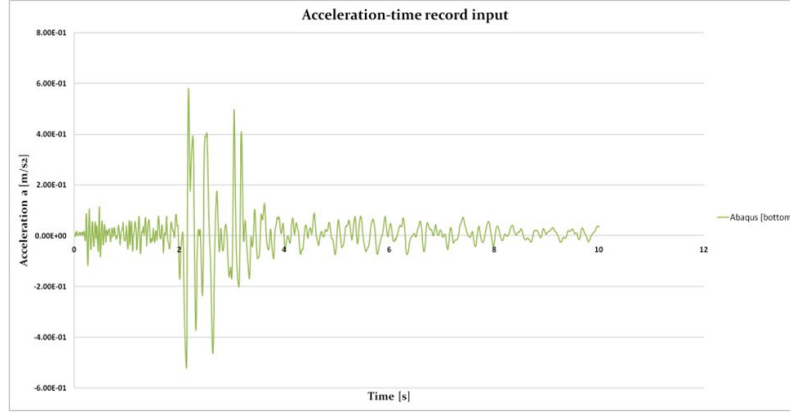


Figure 4.2: Acceleration input

scope of analysis. This matter will be discussed later on.

In addition, the model contains a subroutine which introduces the values of undrained shear strength as a function of the vertical effective stress as well as the correlation of this parameter with Young's modulus using field variables located at integration points of the elements. The field variable values can be functions of element variables such as stress or strain. *Appendix111* shows the flow chart of Abaqus user defined subroutine together with the subroutine introduced in the calculation.

The parameters are calculated as presented in the previous chapter (see 3.2.1.4. and *Appendix12123*). One important matter to mention is the change in the calculation of Young's modulus - for the ease of calculation, this value was determined as a function of the undrained shear strength value. Anastasopoulos et al (2011) use an empirical formulae (based on e.g., Hardin and Richart 1963; Robertson and Campanella1983; Seed et al. 1986; Mayne and Rix 1993) for calculating the value of the small-strain Young's modulus as a function of the overburden stress σ_y . $C = a\sigma_y$ with a ranging from 150 to 10.000 (for clays). Accounting for von Mises failure criterion and one of its defining equations $\sigma_y = a * S_u$ it finally yields:

$$E = a * S_u \quad (4.1)$$

For this application, the value of a was considered to be a=2000 and the correlation between the measurements and empirically determined Young's modulus can be visualized in 4.3

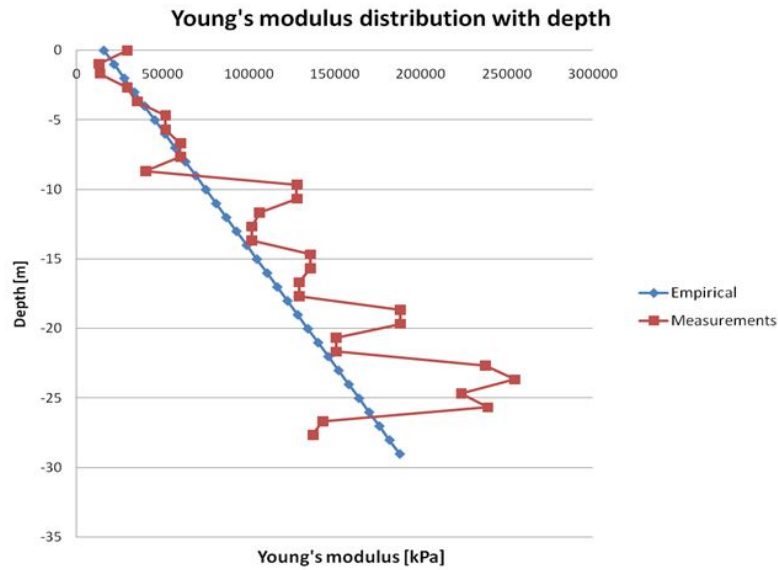


Figure 4.3: Young's modulus distribution along depth

4.2.3 Rayleigh coefficients

The dissipative character of the elasto-plastic material can be better enhanced by introducing a viscous damping mechanism. The overall stress state of the soil skeleton can be separated into two parts:

- *frictional component*- relating to the elasto-plastic behaviour, being displacement proportional
- *viscous component* - relating to the Rayleigh damping coefficients, being velocity proportional.

The advantage of coupling these two terms refers to the smoothing of the shear stress-strain cycles as well as a higher material damping. The viscous component has a favourable effect on the damping curves for small-strain domain; whilst it leads to an overestimation for large-strains. As mentioned previously, the second step of the analysis, and the most important, is declared as dynamic, implicit. In nonlinear analysis, the dynamic equation of motion is:

$$[M] \ddot{u} + [C] \dot{u} + [K] u = - [M] I \ddot{u}_g \quad (4.2)$$

where $[M]$ - mass matrix, $[C]$ - viscous damping matrix, $[K]$ - stiffness matrix, \ddot{u}, \dot{u} and u - vectors of nodal relative acceleration, velocity and displacement, \ddot{u}_g - acceleration at the base and I - unit vector. The matrices are compiled based on the incremental response recorded within the software analysis. The equation is solved at every incremental time step using the Newmark method.

The viscous damping matrix follows Rayleigh and Lindsay equation that relates the small strain damping to both mass and stiffness matrices. Thus, the equation for the viscous damping is:

$$[C] = \alpha [M] + \beta [K] \quad (4.3)$$

where

$$\beta = 2 \frac{\xi}{\omega_1} \quad (4.4)$$

ξ is the damping ratio at small strain; for this application $\xi=1.2$ corresponding to Darendeli's results; while ω_1 is the natural circular frequency at first natural mode;

The assumption of short layer leads to the simplification of the problem because the contribution of higher modes are relatively negligible. Despite that the experimental results prove that the damping matrix $[C]$ is frequency independent and it has a constant value, Park and Hashash show the correlation between the stiffness $[K]$ and the damping $[C]$. Since the stiffness depends on the strain level, then it can be concluded that the damping is also strain dependent, including the natural frequency. Thus, the viscous damping matrix $[C]$ is updated at each time increment as well as the stiffness. Kramer proposes an equation for the calculation of the period of vibration that corresponds to the fundamental frequency of the selected mode as it follows:

$$T_n = (2n - 1) \frac{\bar{V}_s}{4H} \longrightarrow T_n = \frac{V_s}{4H}. \quad (4.5)$$

where \bar{V}_s average shear wave velocity and H = layer height.

Further, the natural circular frequency is obtained through the following transformation:

$$\omega_n = \frac{2\pi}{T_n} \rightarrow \omega_1 = \pi \frac{V_s}{2H} \quad (4.6)$$

And finally, Rayleigh β damping parameter becomes:

$$\beta = \frac{2H\xi}{V_s\pi} \quad (4.7)$$

ξ	1.2	%	Darendeli damping ratio
T_n	$4H/V_s$	sec	Fundamental period
V_s	132	m/s	Average shear wave velocity
H	30	meters	Layer depth
ω	6.91	$Hz(sec^{-1})$	Fundamental frequency
β	0.001736	sec	Rayleigh β coefficient

Table 4.1: Calculation of Rayleigh β parameter

4.2.4 Integration scheme

It is important to understand the type of nonlinear analysis the software was opted to perform and its influence of the results. For this particular analysis, an implicit direct integration scheme was selected - this means that the set of equations concerning the set of nonlinear equations of motion are solved at each time step Δt involving both the current and the later state of the system.

Abaqus/Standard uses the Hilbert-Hughes-Taylor time integration method which is an extension of the Newmark β method. Basically it controls the numerical damping within the system which might rise due to the energy dissipation mechanisms associated with different operator types.

4.2.5 FEM stability

The accuracy of such nonlinear problem dealing with wave propagation is controlled by two factors - node spacing in the FE model δh and the time step δt . The spacing is directly related to the wavelength whilst the time step depends on the fundamental period of the system.

$$\Delta h \leq \frac{\lambda_{min}}{10} = \frac{1}{10} \frac{v}{f_{max}} \quad (4.8)$$

$$\Delta t = \frac{T_n}{10} \quad (4.9)$$

More details regarding the calculation of the two stability criterion are presented within *Appendix 23141*.

4.2.6 Mesh

For the mesh elements, four-node quad elements (*CPE4*) are used to model the soil using the plane strain formulation of the quad-element. The element connectivity uses a counterclockwise pattern for the previously-described node numbering scheme (see 4.1). The soil elements in each layer are assigned the material tag of the material object corresponding to that layer. A unit thickness is used in all examples for simulating the 1D condition. The self-weight of the soil is considered as a body force acting on each element. The body force is set as the unit weight of the soil in each layer, which is determined from the respective mass density input value.

4.3 NERA - Non-linear Earthquake Site Response

An additional analysis was performed using NERA (Nonlinear Earthquake site Response Analyses) computer program in order to have a better grasp of the whole concept as well as a meaningful comparison. It derives from EERA that uses an equivalent linear model to investigate the same problem; the constitutive material model is proposed by Iwan and Mroz (1967) and it describes the nonlinear kinematic model as a series of n mechanical elements, each displaying different stiffness k_i and sliding resistance R_i as it is shown in 4.4.

NERA is composed by a FORTRAN 90 code together with a Excel plug-in that capture the nonlinear site response of a layered soil column subjected to an earthquake signal. As input, it requires the acceleration-time record, material properties with emphasis on the stiffness parameters. The material properties introduced within the software require a general description of the soil column as well as an individual material classification (in case the user is dealing with a multi-layered ground). The general input portrays the column with its sub-layers and unit weights, shear wave velocities and the ground water table followed by an automatic assessment of the maximum shear modulus, effective stresses and fundamental period. The software allows for multiple layer

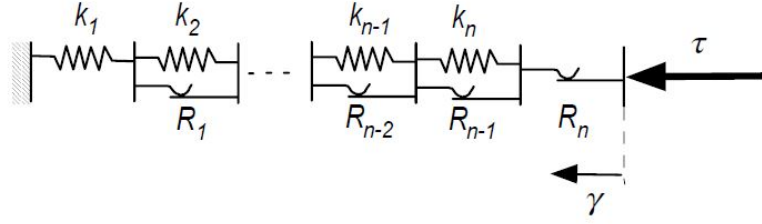


Figure 4.4: Plastic description of Iwan and Mroz nonlinear model

definition by introducing the normalized shear modulus degradation curves and material damping curves. For this particular case, Darendeli's results presented previously were used in order to obtain a consequent comparison. However, the software does not account for data corresponding to damping curves as it is calculating its own set of values. This is because the nonlinear model proposed by Iwan and Mroz uses a different scheme for determining the damping characteristics.

NERA starts the analysis by processing the earthquake input signal and material properties followed by step-by-step determination of the relative velocity and displacement at a selected sub-layer. The integration scheme NERA uses is the central difference which, contrary to Abaqus analysis, it is conditionally stable (the time step size is limited). This calculation method is a particular type of Newmark method in which the predicted velocity is:

$$\tilde{v}_{i,n+1} = v_{i,n} + \frac{1}{2}a_{i,n}\Delta t \quad (4.10)$$

The stress and strains are calculated at each node from nodal displacements, next step calculates the velocity from the input acceleration history. Subsequently, the predicted values for velocities at time t_{n+1} yield from those determined at time t_n and finally the nodal displacements, velocities and accelerations are update at each node i . In addition, the output includes spectral response based on Fourier transform calculation for any selected sub-layer.

4.4 Results

This subchapter presents the results obtained from the site response analysis performed in Abaqus, followed by a comparison with NERA outcome; several plots are used as mean of verification and the main interest lies on the G/G_{max} and damping curves, acceleration response as well as the amplification ratio in frequency domain. After performing a dynamic, implicit type of analysis to the assembly described previously, the output was investigated with an initial emphasis on the stiffness degradation. To check the validity of the overall model, an uniform cyclic signal served as acceleration amplitude; a circular frequency $f = 1\text{Hz}$ was applied at the bottom of the model for a period of 10 seconds in a sinusoidal fashion. The results can be visualized in 4.5, 4.6 and 4.7. The same remarks can be made as for the preceding analysis **see previous analysis One mesh element**; however, this model includes an additional Rayleigh damping parameter together with the subroutine that updates the values of the Young's modulus. The acceleration response highlights a de-amplification of the bottom signal together with damping effects visible in the irregularities of the curves.

Going forward with the results, the real acceleration-time history was applied to the boundary condition at the bottom nodes for the same period of 10 seconds. The records correspond to the measurements from WSE station, Huizinge, Groningen - even though the earthquake signal lasts for 35 seconds, it was trimmed to analyse the most unfavourable 10 seconds [with the highest acceleration peak]. The obtained values in terms of shear stress and strain can be seen in 4.8 whilst the top and bottom acceleration outcome is represented in 4.9. Important to mention is that the boundary condition applied at the bottom of the model represents the bedrock presence, therefore the waves are incident and not reflective - the discussion about the boundary conditions influence on the wave propagation shall be presented shortly after. [As a sign convention, element 1 represents the bottom one whilst element 30 is the surface].

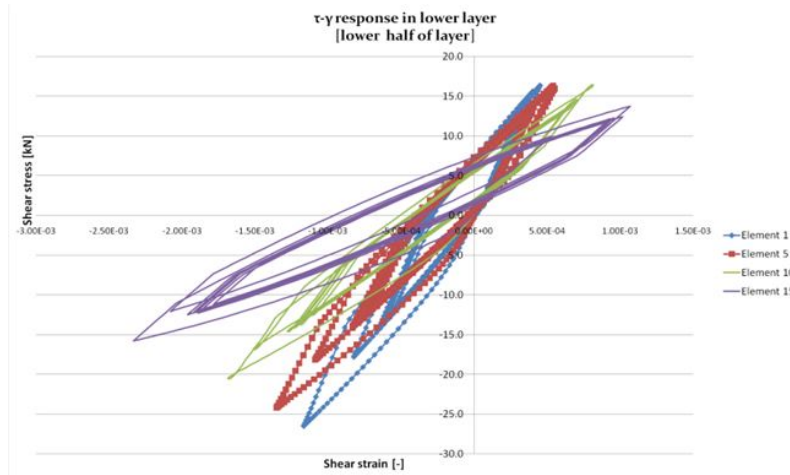


Figure 4.5: Hysteresis loops on the lower half of the soil layer

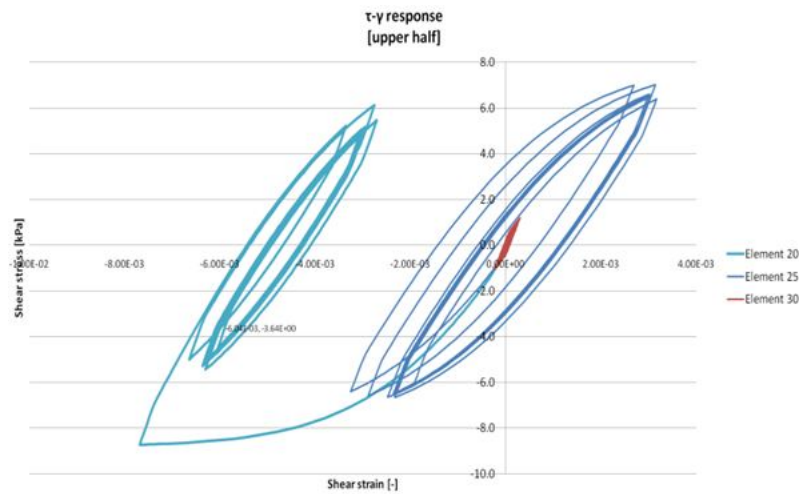


Figure 4.6: Hysteresis loops for lower half of the soil layer

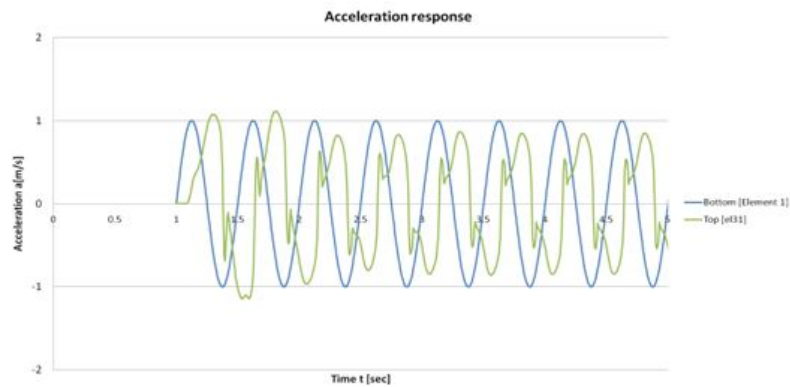


Figure 4.7: Acceleration response (surface and bottom)

Once the bottom and top acceleration outcome is extracted from the software, a Fast Fourier transform is applied with the scope of converting the current data from time domain to a representation in frequency domain. As Kristeková et al., 2006 stated "the most complete and informative characterization of a signal can be obtained by its decomposition in the time-frequency plane". However, FFT is used as a digital signal processing tool that aids other operation, rather than providing a final result itself. For example, the transfer function or a site amplification factor

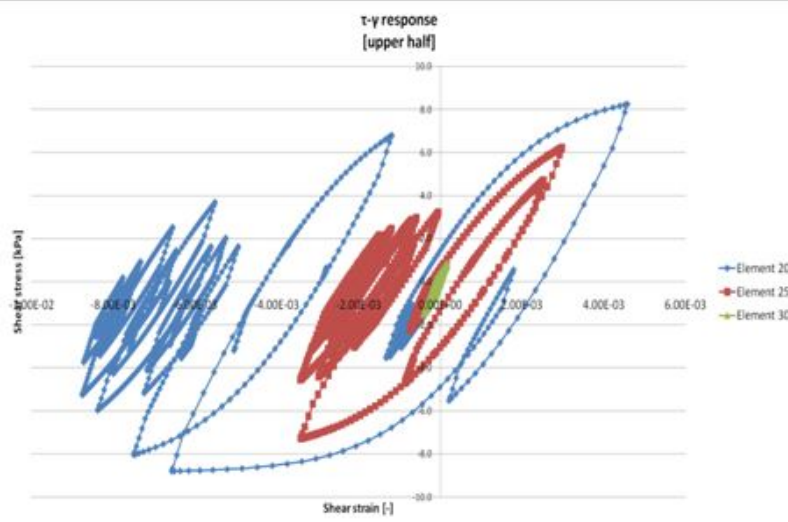


Figure 4.8: Hysteresis loops for upper half of the layer when real acceleration is applied

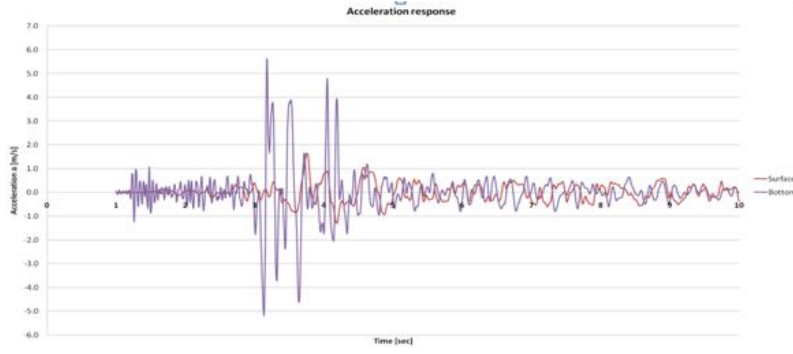


Figure 4.9: Acceleration response - surface and bottom

allows the calculation of the motion of any layer i based on other motion (of any layer j). This transfer function relates the displacement at position i to that at position j as it follows:

$$F_{ij} = \frac{|u_i|}{|u_j|} \quad (4.11)$$

The Fourier spectrum represents the distribution of energy in the ground motion for a frequency interval $[0 \leq f \leq 1/2\delta t]$. The amplification factor can also be written as:

$$A(f) = \frac{F_{a,site}(f)}{F_{a,bedrock}(f)} \quad (4.12)$$

where $A(f)$ - site amplification factor; $F_{a,site}(f)$ and $F_{a,bedrock}(f)$ - Fourier amplitudes of ground acceleration at surface and bedrock, respectively calculated as the vector sum of the two horizontal components. The importance of the site amplification factor relates to the structural damage pattern (rather than the PGA amplification) due to site effects. If the natural period of the structure matches the soil natural period, the structure will be more vulnerable to earthquakes. It is important to discuss the boundary conditions and their influence on the wave transmission throughout the layer. The current model created in Abaqus includes tied boundaries, also described by Zienkiewicz et al. (1989) and it assumes that all displacements on the left side of the column correspond to the ones at the right side, simulating a free field boundaries, whereas the bottom nodes do not absorb the oscillating waves. The software offers the baseline correction option for the acceleration input for time domain analysis; the practice is proposed by Newmark and it introduces an additional correction to the acceleration such that the mean square velocity over the event time is minimized. The use of more correction intervals provides tighter control over any “drift” in the displacement at the expense of more modification of the given acceleration trace. However, in

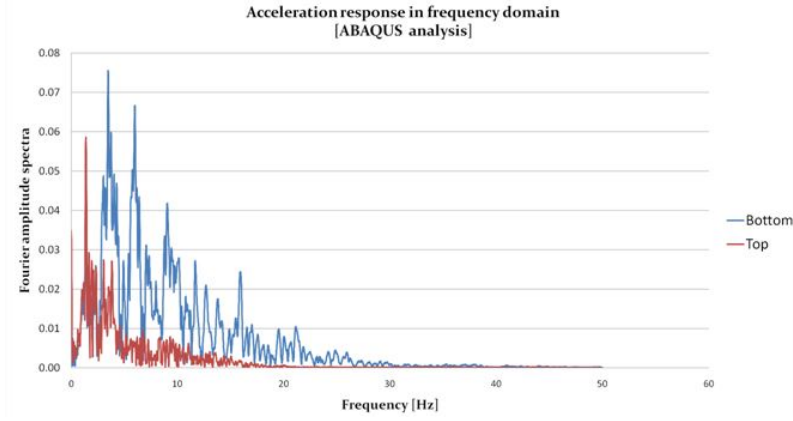


Figure 4.10: Fourier amplitude spectra - surface and bottom

acceleration history it does not show large difference between the responses. Because the boundary only transmits the waves upwards, an additional analysis was performed with a bottom acceleration record manually reduced by half. Physically, the waves within a soil have both downwards and upwards motion (incident and reflective). The decision of applying half of the signal also relates to NERA calculation in order to obtain a coherence between the two software; NERA assumes that the velocity at base is the sum of both incident and reflected waves and since at bedrock level shear force is zero it yields that the velocity becomes:

$$v_{base} = 2v_{incident} \quad (4.13)$$

4.5 Comparison Abaqus vs NERA

The comparison between the two analyses were formulated in terms of acceleration response, shear stress-strain response together with the spectral ratio and the plots can be visualized below.

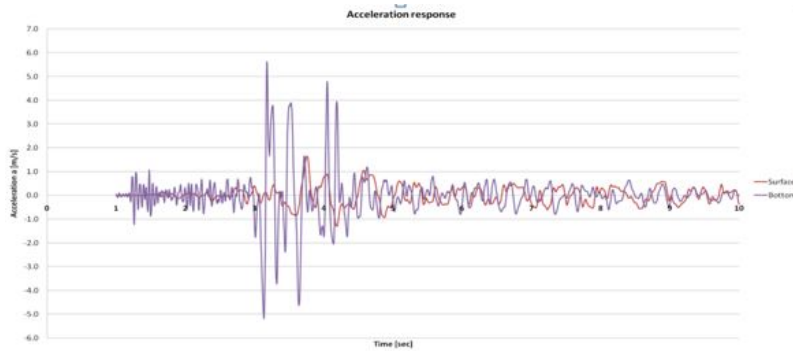


Figure 4.11: Acceleration comparison Abaqus vs. NERA

4.5.1 Remarks

Overall, the results show a quite satisfying math; nonetheless, differences appear due to several factors as it follows:

1. Abaqus works with a dynamic implicit integration scheme with an Euler backwards theory that is unconditionally stable whereas NERA solves the system of equation through a central-difference which is conditionally stable; thus on one software, user has the option of manually adjusting the time step while on the other he cannot. The equation of motion for the system in dynamic domain it is basically the same:

$$f = F - \rho \ddot{u} \quad (4.14)$$

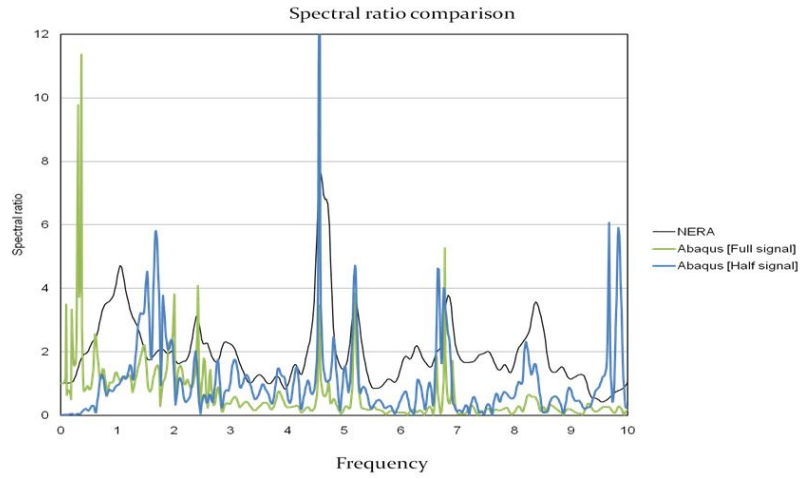


Figure 4.12: Fourier amplitude spectra comparison

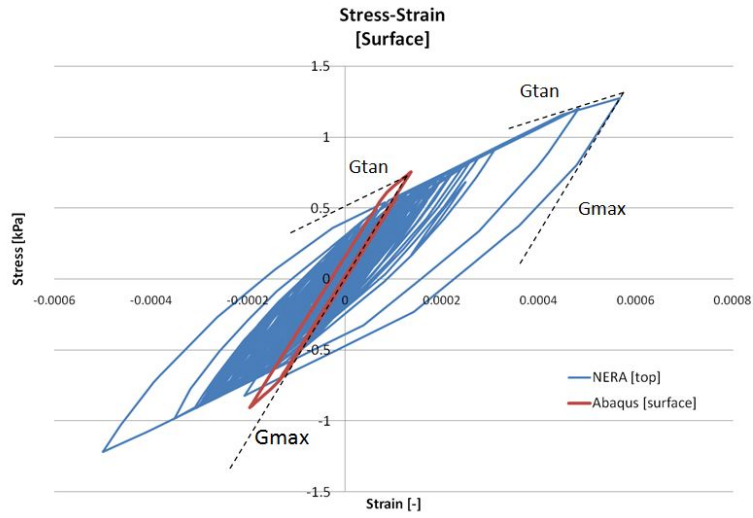


Figure 4.13: Hysteresis loops comparison for surface level

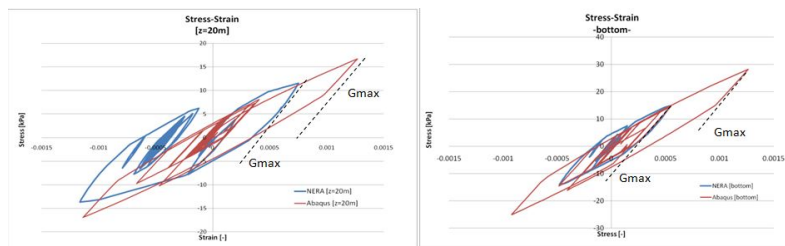


Figure 4.14: Hysteresis loops comparison for $z=20\text{m}$ (left) and bottom level(right)

where f - body force, F - external body force, ρ - soil unit weight and \ddot{u} - relative nodal acceleration. Thus, the difference is *numerical* and cannot be adjusted in detail.

- Both the models are based on the concept of a yield surface which means that there is a surface defined in stress space within which no plastic deformation takes place. The nonlinear kinematic hardening model used in Abaqus is based on the Lemaitre and Chaboche model that considers two yield surfaces and a varying hardening modulus whilst NERA works according to Iwan and Mroz multi-linear kinematic hardening model that has a multiple surface plasticity. First model includes a 'fading memory' term whereas the second model does not and preserves the memory width. Thus, the difference is related to the plastic

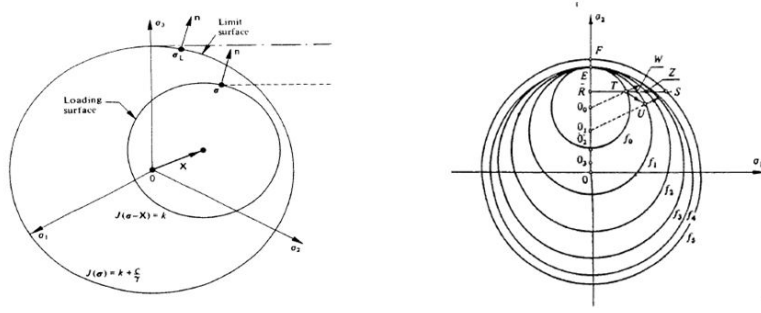


Figure 4.15: Non-linear kinematic hardening model according to Lemaitre,Chaboche [left] and Iwan,Mroz[right]

domain and how the model behaves when irreversible deformations are encountered.

3. NERA computes the shear stress and strain increments according to the sliding resistance and tangent modulus of each slider that are derived from the $G_i - \gamma_i$ points introduced as input. The tangential shear modulus is related to the secant shear modulus by $H_i = G_{max} \frac{G'_{i+1}\gamma_{i+1} - G'_i\gamma_i}{\gamma_{i+1} - \gamma_i}$ where $G_i = \frac{G_i}{G_{max}}$. The stiffness of each component of the system is related to the tangent modulus while the shear stress is associated with the sliding resistance. On the other hand, Abaqus does not work with the tangent modulus, but with maximum shear modulus G_{max} and the undrained shear strength. Also, in NERA there is no option for introducing the values corresponding to the undrained shear strength or its correlation with any other parameter. Figure 14 shows the distribution of the shear modulus with depth in both the software - these values are calculated from the input parameter - Abaqus extracts it based on the Young's modulus together with Poisson's ratio whilst NERA does it based on the soil unit weight and shear wave velocity. The values are exactly the same, it can be noticed also from the slope the hysteresis loops presented in the stress-strain plots; the width also resembles as well as the unloading-reloading areas. However, the tangent shear modulus differs from one software to the other.

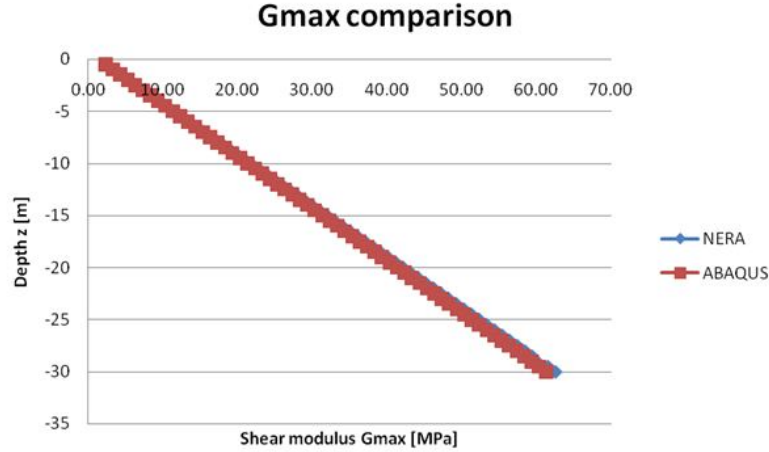


Figure 4.16: Shear modulus G_{max} comparison

4. Abaqus results are extracted in two different locations: the stresses and strains are obtained from Gauss integration points and the accelerations are obtained at nodal positions which are situated at the interface of each two element. NERA performs the analysis according to the middle of each sub-layer, so both the top and bottom outcome are actually 0.25m below the surface or above the bottom. However, not much difference should rise from this aspect.
5. Another difference relates to the viscous part of the model and it is more apparent in the acceleration response in time domain, especially in the initial period. Abaqus works with

the viscous term defined exclusively as a function of Rayleigh damping parameter β meaning that the system damping depends on the stiffness, whilst NERA requires the critical damping ratio value, incorporating both α and β Rayleigh factors. Moreover, the energy dissipation mechanism accounts for both viscous damping and plasticity terms which, as described previously, differ from NERA to Abaqus. When working with a high PGA value, the contribution of the non-linear model and hysteretic damping becomes greater compared to the viscous damping component.

6. Noise can be experienced in both the signals of the different computer programs. This can distort the final results; filtering is possible, however it is time demanding and does not represent the main interest in this study.

4.5.2 Additional investigation

An additional investigation was performed in order to check the soil response when closer to elastic domain - as in, a lower PGA was applied at the bottom boundary. The first analysis contained a PGA value of approximately 0.5g whilst the second one scaled down the value to 0.1g. The results can be seen in the following figures.

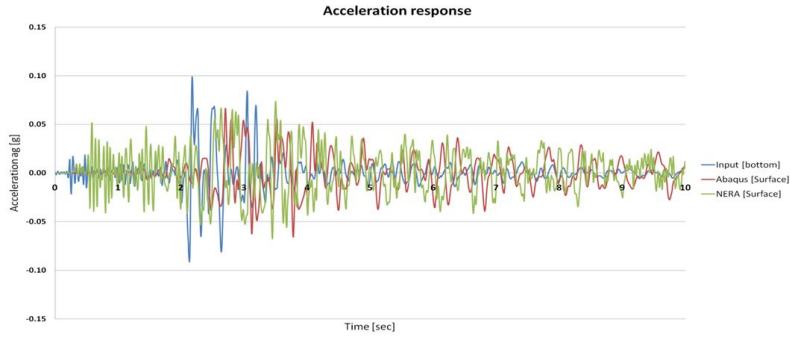


Figure 4.17: Acceleration response comparison for PGA=0.1g

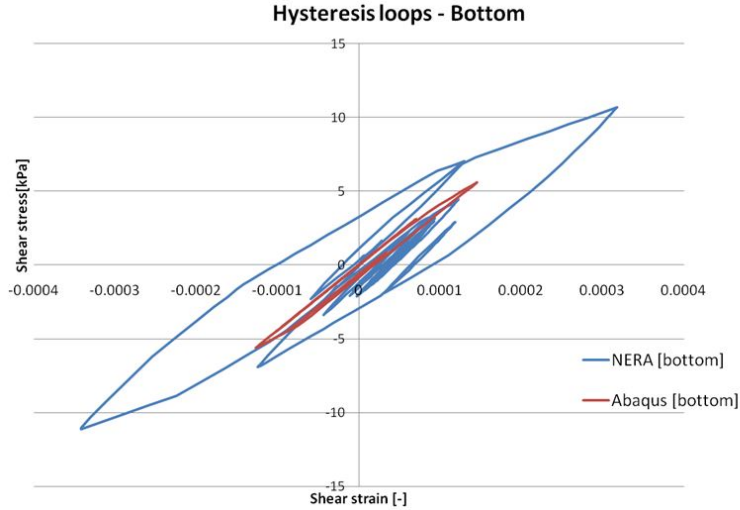


Figure 4.18: Hysteresis loops comparison for bottom level

The results confirm the expectation regarding the amplification effect of the soil combined with the PGA level, also they are in accordance with ARUP report regarding the site response analysis performed for the specific location in discussion. The acceleration responses at surface produced in both the computational software present the same maximum value, of course, with differences that were exposed previously, the elastic response seems to match together with the stiffness degradation effect.

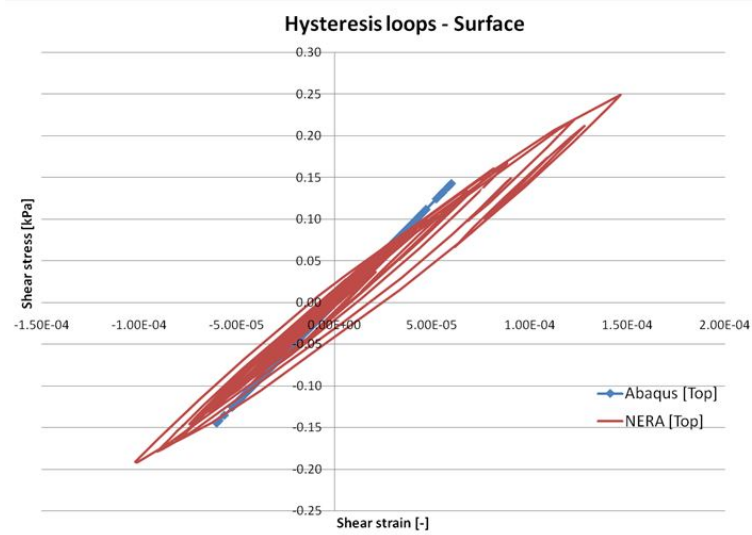


Figure 4.19: Hysteresis loops comparison for surface level

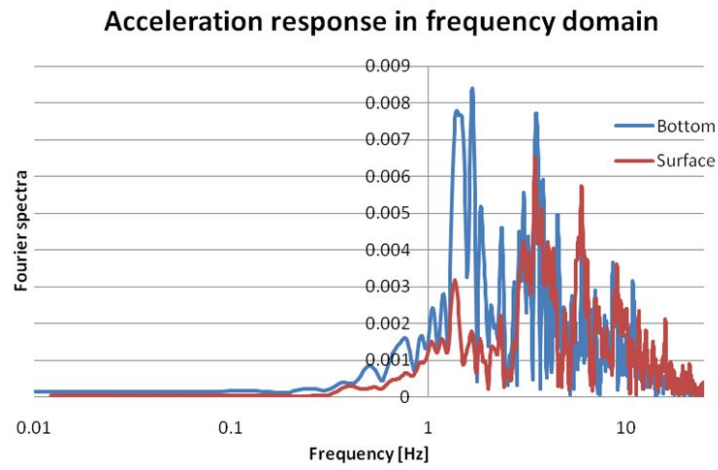


Figure 4.20: Fourier amplitude spectra for PGA=0.1 - logarithmic scale

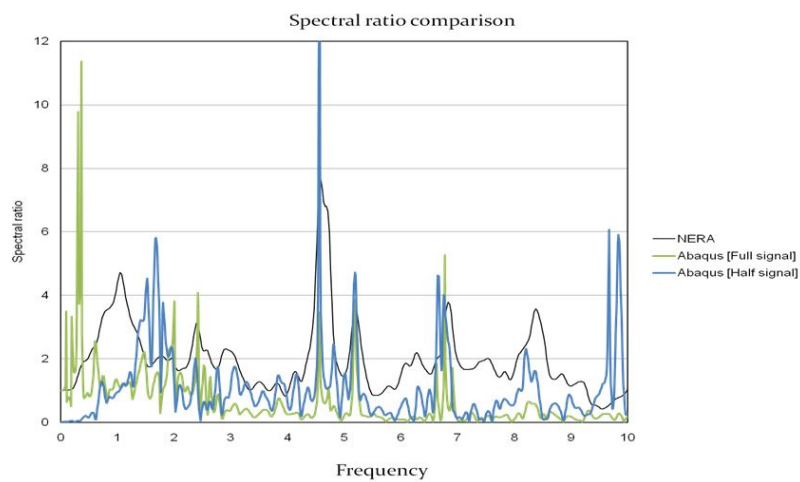


Figure 4.21: Site amplification factor comparison for PGA=0.1g

4.6 Conclusions

The differences between the software were investigated and speculated; given the fact that the study deals with a non-linear kinematic hardening process, it becomes quite difficult to point

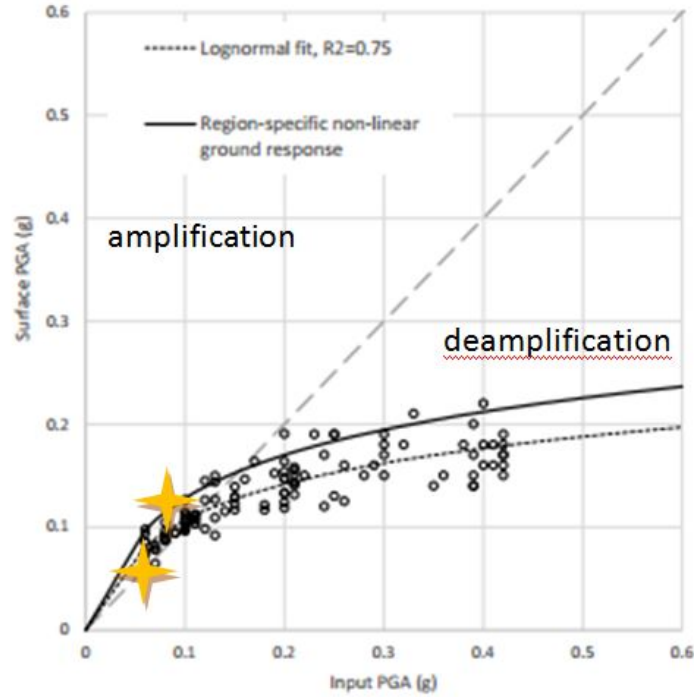
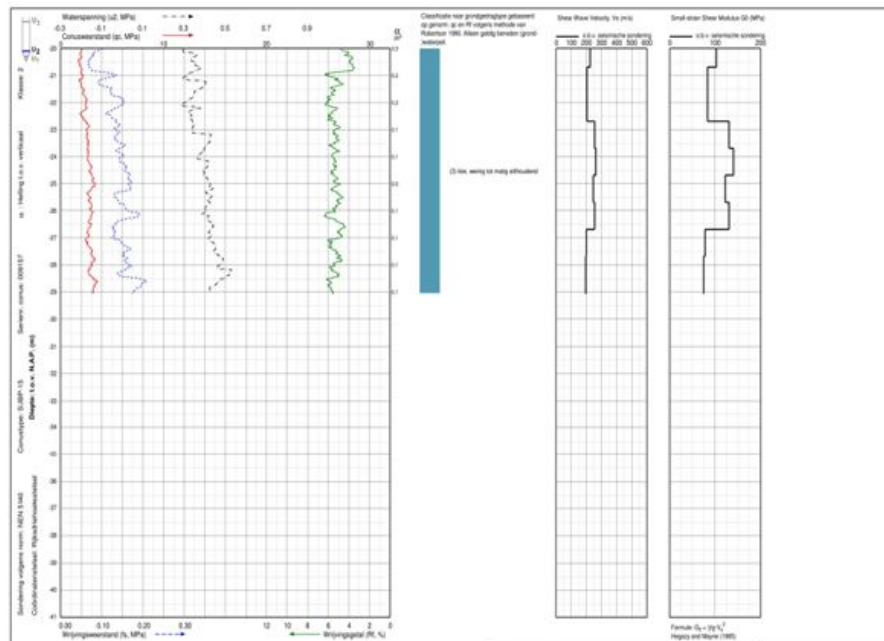
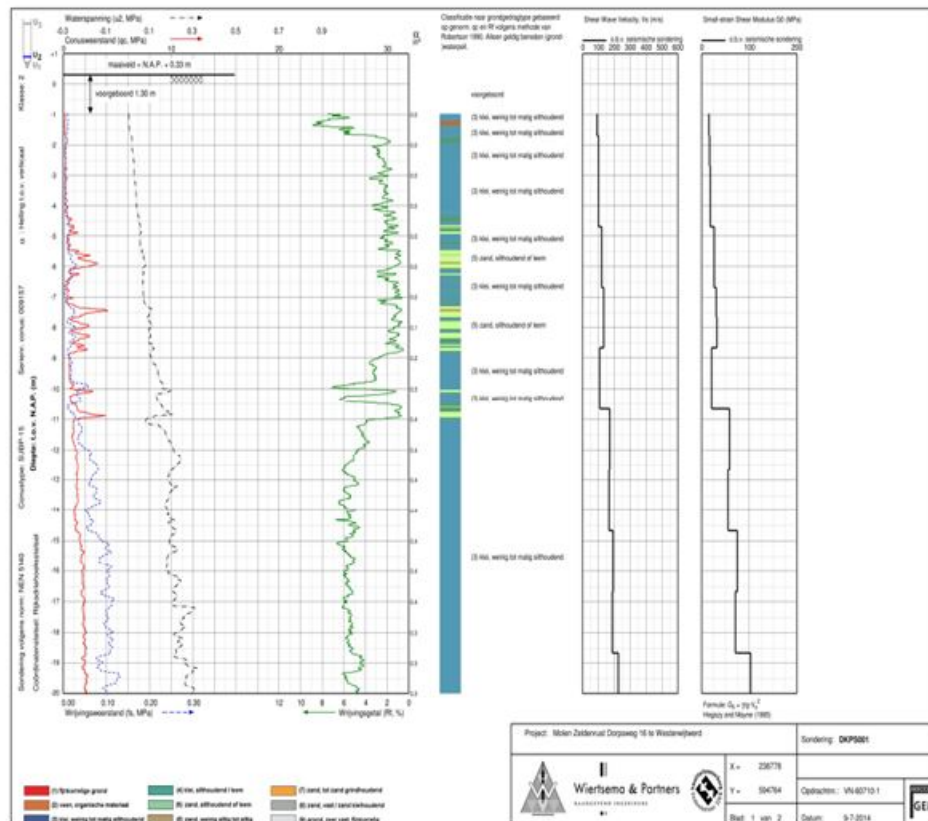


Figure 4.22: Groningen site non-linear ground response, input vs surface PGA according to ARUP report

exactly the main cause that leads to dissimilarity. However, reasons can be examined and despite the analyses run according to separate models and integration schemes, overall they display a reasonably agreement.

It can be concluded that for the Groningen sites, low PGA input ($a_g = 0.1g$) the surface acceleration response amplified whereas when dealing with a high PGA input ($a_g > 0.15g$) the top PGA is de-amplified. Both the strength properties of the homogeneous medium and the earthquake motion characteristics influence the seismic wave propagation through the soil; for this particular case, the inelastic response depends on the limited capability of the soft layers to transmit seismic signals to the surface because of the low strength and on the high hysteretic damping observed at large strains. At low PGA values, the soil displays elastic behaviour as it reaches the surface, the frequencies do not experience considerable damping whereas at high PGA levels, the soil shifts towards its natural frequency, damping the higher ones and non-linear constitutive model plays a more important role than the viscous damping effect.

Cone penetration test results



.2

Constitutive model: Nonlinear kinematic hardening model with a Von Mises failure criterion

.2.1 Von Mises failure criterion. A definition

The plasticity characteristics correspond to a Von Mises failure criterion - a *total stress analysis* is performed. The reason behind this option relates, on one hand, to the pore pressure dissipation - due to the load rate the volumetric strain is almost zero because the excess pore pressure does not have the chance to dissipate. The chosen criterion suits the goal as it is independent on the hydrostatic pressure and mean stress invariant s .

When considering a point P in stress space representing a vector describing the stress state, it can be projected on the hydrostatic axis with the use of two components: the parallel vector representing the hydrostatic component - which is function of the mean stress invariant I_1 and the perpendicular component, the deviatoric one as a function of the second deviatoric stress invariant J_2 .

introduce the drawing here

$$OP = \sqrt{\sigma_1^2 + \sigma_2^2 + \sigma_3^2} \quad (15)$$

$$I_1 = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3} \quad (16)$$

$$J_2 = \frac{1}{6}[(\sigma_1^2 + \sigma_2^2) + (\sigma_1^2 + \sigma_3^2) + (\sigma_2^2 + \sigma_3^2)] \quad (17)$$

where OP is the vector describing stress state, I_1 is the mean stress invariant and J_2 is the second stress invariant.

For simplification purpose, the stress state can be defined by three invariants - the mean stress invariant s , the second stress invariant T and Lode angle θ - each representing volumetric and deviatoric lengths in stress space.

$$s = \sqrt{3}\sigma_m \quad (18)$$

$$t = \sqrt{2}J_2 \quad (19)$$

The failure criterion is defined by a function of the aforementioned invariants - it describes a surface in the stress space which delimits safety from failure. Any point within the stress space situated below the surface attains safety - the points cannot exceed the failure plane because collapse occurs; hence the equation for failure is $F = 0$, where F is the function in discussion.

Generally, a soil sample will reach failure when the total stress Mohr circle attains the strength envelope - which is described as $\tau = S_u$ and it is represented by a straight line dependent on the friction angle and cohesion c . For materials for which the cohesion can be set to $c = S_u$ whilst $\phi = 0$, the Mohr-Coulomb failure envelope turns into a Tresca failure criterion which is parallel to the normal stress axis:

$$\sigma_{max} - \sigma_{min} = 2S_u \quad (20)$$

$$F(s, T, \theta) = 0, \text{Mohr} - \text{Coulomb failure criterion} \quad (21)$$

$$F(s, T) = 0, \text{Drucker} - \text{Prager failure criterion} \quad (22)$$

$$F(s, \theta) = 0, \text{Tresca failure criterion} \quad (23)$$

Consequently, Drucker-Prager failure criterion represents a smooth version of the Mohr-Coulomb criteria in the sense that it accounts for two of the stress invariants ($F(s, T) = 0$) neglecting Lode angle, θ . This leads to a cone shape of the failure surface.

Furthermore, Von Mises only considers the **second invariant being independent of hydrostatic pressure** and yielding a cylindrical failure shape in three-dimensional stress space. The physical meaning of the mean invariant, I_1 , can relate to the radius of the cross section of failure criterion - the larger the I_1 , the larger the radius and thus the evolution of the failure surface follows a conical profile. Given von Mises does not require this term, it becomes clear the cylindrical shape of the failure envelope obtained with a constant radius. Moreover, when mapping the deviatoric component - that associates with a normal plane on the failure surface - it stands out that there is no volume change. Thus, the undrained behaviour of the clay layer can be successfully expressed in terms of von Mises failure criterion.

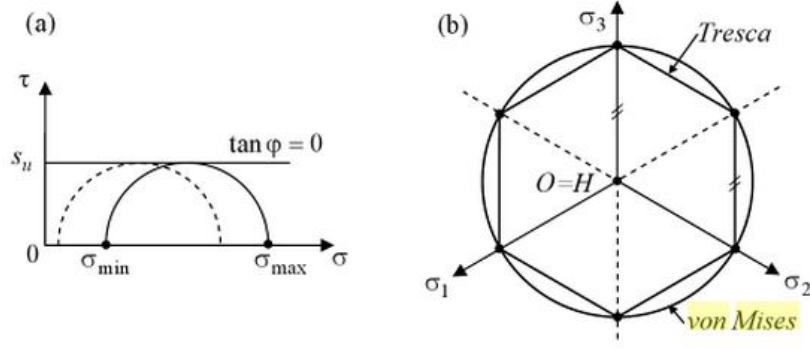


Figure 23: Tresca and Von mises failure criterion in stress space

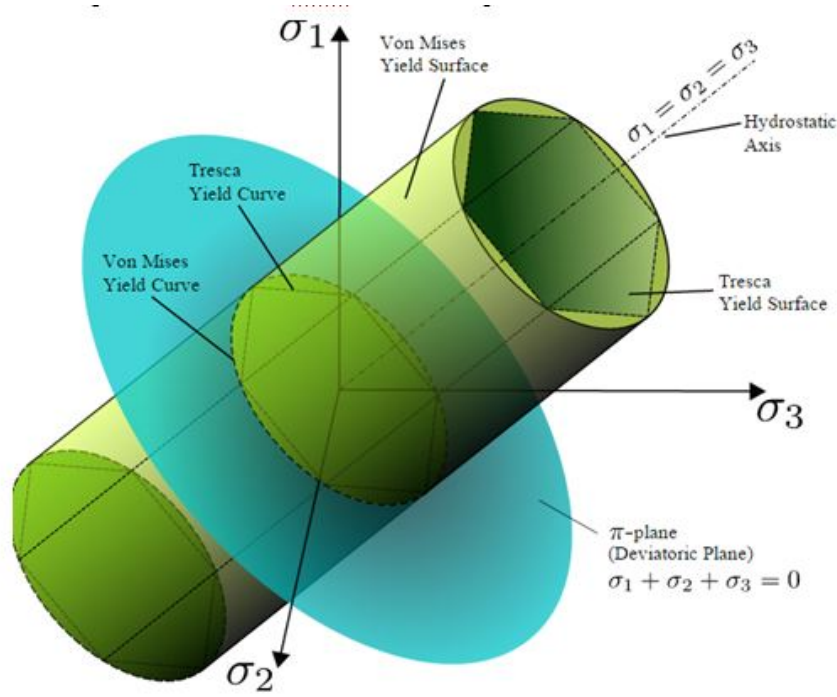


Figure 24: Von mises failure criterion in 3D stress space

.2.2 Constitutive model according to Lemaitre and Chaboche: Nonlinear kinematic hardening rules

The formulation for plasticity criterion is always expressed in the following form and it is important to mention that the *plasticity function is linear* and depends exclusively on the second invariant J_2 as it follows:

$$f = J_2(\sigma - X)k \quad (24)$$

where X represents the kinematic hardening and it is assumed zero in initial state, k hardening modulus and sigma introduces the stress tensor. The hypothesis of proportionality between the accumulative plastic strain increment $d\varepsilon_p$ and X is replaced by a term that introduces the fading memory effect present on the stress path:

$$dX = \frac{2}{3}C d\varepsilon_p - \gamma X dp \quad (25)$$

One can notice that the kinematic hardening depends on characteristic material coefficients such as C which represents the initial kinematic hardening modulus while γ introduces the inverse proportionality between the kinematic hardening and plastic deformation. Including normality hypothesis and the consistency condition $df = 0$ the equation for the incremental accumulative plastic strain becomes:

$$d\epsilon_p = d\lambda \frac{\partial f}{\partial \sigma} = \frac{H(f)}{h} \left\langle \frac{\partial f}{\partial \sigma} | d\sigma \right\rangle \frac{\partial f}{\partial \sigma} \quad (26)$$

Following, the hardening modulus turns into kinematic stress dependent factor:

$$h = \frac{2}{3} C \frac{\partial f}{\partial \sigma} \left| \frac{\partial f}{\partial \sigma} \right| - \gamma X \left| \left(\frac{\partial f}{\partial \sigma} \left(\frac{2}{3} \frac{\partial f}{\partial \sigma} \left| \frac{\partial f}{\partial \sigma} \right| \right) \right)^{1/2} \right| \quad (27)$$

Considering von Mises assumption where $d\lambda = dp$ and inserting in the above equation the hardening modulus becomes:

$$h = C - \frac{3}{2} \gamma X \left| \frac{\sigma' - X'}{k} \right| \quad (28)$$

Clearly it can be stated that increase of the kinematic hardening X induces a decrease of hardening modulus k .

A generalized nonlinear kinematic hardening model would replace the associated plasticity with another flow potential which is different from loading surface. Additionally, other set of von Mises material assumptions yield:

$$d\epsilon_p = \frac{\partial F}{\partial \sigma} d\lambda = \frac{3}{2} \frac{(\sigma' - X')}{J_2} dp \quad (29)$$

$$d\epsilon_p = \frac{\partial F}{\partial \sigma} d\lambda = d\epsilon_p - \frac{3}{2} \frac{\gamma}{C} X dp \quad (30)$$

However, when plastic flow is considered the function f becomes zero ($f = 0$), the dissipation potential can be calculated from the initial equation. Hence:

$$F = J_2(\sigma - X) + \frac{3}{4} \frac{\gamma}{C} X |X| - k = f + \frac{3}{4} \frac{\gamma}{C} X |X| \quad (31)$$

becomes

$$F = \frac{3}{4} \frac{\gamma}{C} X |X| \quad (32)$$

Assuming $dX = 0$ leads to maximum value of the second invariant J_2 then the shape boundaries of the function can be calculated:

$$J_2(X) = \left(\frac{3}{4} X' |X'| \right)^{1/2} \leq \frac{C}{\gamma} \quad (33)$$

* $X' = X$ because of plastic incompressibility and initial condition $X(0) = 0$.

Therefore, the dissipation potential or backstress, as it is referred in other studies, should be limited within a cylinder with radius $\sqrt{\frac{2}{3}} C / \gamma$ whilst the boundaries of the yield stress describe a cylinder of radius $\sqrt{\frac{2}{3}} \sigma_y$ where γ_y represents the maximum stress. Applying on a clay soil characterized by an undrained shear strength, the maximum stress can be expressed as:

$$\sigma_y = \sqrt{3} S_u \quad (34)$$

$$\sigma_y = \frac{C}{\gamma} + \sigma_o \quad (35)$$

$$\gamma = \frac{C}{\sqrt{3} S_u - \gamma_o} \quad (36)$$

The equations incorporate the term C which refers to Young's modulus for very small strains describing the elastic stiffness when low-amplitudes are encountered and it can be computed using Roberston method based on shear wave velocity or through empirical correlations (Roberston and Campanella, 1983, Seed et al, 1986).

** In order to avoid the confusion between the hardening parameter (here noted with γ) and the shear strain (also γ), the notation of the hardening parameter is changed to K .

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.3

Description of Darendeli hyperbolic model

The study presents a modified hyperbolic model which describes the normalized modulus reduction curve; the model starts from the example created by **Hardin and Drnevich** being adjusted through a curvature coefficient, a . The role of the coefficient is given by its name as it influences the curvature of the outcome. The hyperbolic model is expressed using the following equation:

$$\frac{G}{G_{max}} = \frac{1}{1 + (\frac{\gamma}{\gamma_{ref}})^a} \quad (37)$$

The material damping curves consider *Masing behaviour* which proves that the stress-strain path associated to a cyclic loading can be related to the monotonic loading path, also known as the backbone curve. **Masing(1926)** states that the backbone curve serves to the creation of the hysteresis loop; the curve is scaled by a factor of two and flipped with respect to both horizontal and vertical axis to simulate the unloading path. The assumption is valid for an uniform cyclic loading, unlike the real earthquake signals; however it has its own limitations in modelling nonlinear soil behaviour. A schematization of Masing behaviour assumption can be seen in Figure 25; the dashed line represents the monotonic loading response which coincides with the initial path of the cyclic loading.

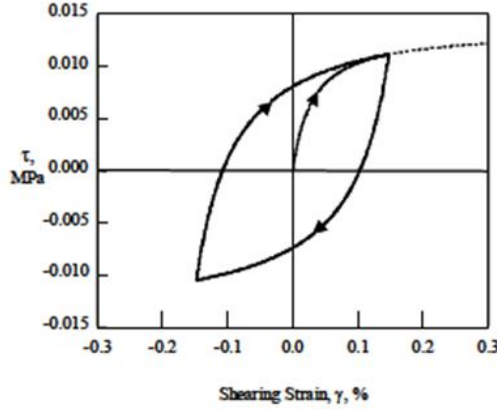


Figure 25: Hysteresis loop estimated by modelling stress-strain reversals for two-way cyclic loading according to Mass behaviour

The material damping ratio is expressed as the ratio of the dissipated energy to stored strain energy during a loading cycle; combining this concept together with Masing behaviour, the area inside the hysteresis loop (A_L) can be determined through the integration of the stress-strain curve described during one loading cycle.

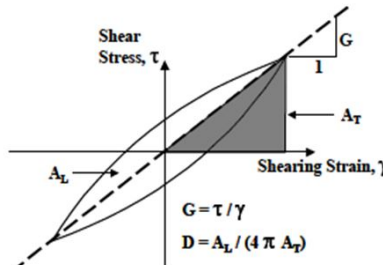


Figure 26: Calculation of damping ratio using a hysteresis loop

$$A_L = 8 \left(\int \tau d\gamma \right) - \frac{1}{2} \tau \gamma \quad (38)$$

$$A_T = \frac{1}{2} \tau \gamma) \quad (39)$$

$$D_e q = \frac{A_L}{4\pi A_T} \quad (40)$$

Combining all the equations previously presented, Masing-behaviour damping ratio can be expressed:

$$D_{masing} = \frac{4}{\pi} \frac{\int \frac{\gamma}{1+(\frac{\gamma}{\gamma_{ref}})^a} d\gamma - \frac{1}{2}(\frac{\gamma^2}{\gamma_{ref}})^a}{1 + (\frac{\gamma}{\gamma_{ref}})^a} \quad (41)$$

For the final formulation of the material damping ratio, Darendeli uses fitting parameters and functions for a better matching with the experimental observations. The equation of the material damping curve is then expressed as a function of two main parameters (b and D_{min}):

$$D = b(\frac{G}{G_{max}})^{0.1} * D_{masing} + D_{min} \quad (42)$$

Parameter b represents a scaling factor whilst D_{min} comprises the impact on the damping curve caused by confining pressure, loading frequency and soil plasticity. The influence of D_{min} is most visible through the shift within small-strain damping ratio area; the curve does not touch the horizontal axis of the plot - this means that no matter how small the strain level is, the soil will experience damping.

In conclusion, the modified hyperbolic model described by Darendeli for the normalized modulus reduction curve and material damping curve relies on four parameters: a , b , γ_{ref} and D_{min} .

.4

Input parameter - Stresses calculation

The total vertical stress is calculated both in terms of soil density (43), in $[Mg/m^3]$ and soil unit weight (44), in $[kN/m^2]$, at a depth z as it follows:

$$p(z) = p_0 + \int_0^z \rho(z) dz \quad (43)$$

$$\sigma_v = \gamma_{soil} * z \quad (44)$$

The water level is considered at 1 m below surface level, hence the pore pressure equation is:

$$u = \gamma_{water} * z_{water} \quad (45)$$

The effective vertical stress can now be determined based on Terzaghi's principle:

$$\sigma_v = \sigma'_v + u \quad (46)$$

The determination of the horizontal stress is a subject still uncertain, however empirical relations can be used to approximate the value; according to Jaky (1948) it yields that for normally consolidated clays:

$$K_o = 1 - \sin \phi' \quad (47)$$

This coefficient is expressed in terms of effective stresses as well because it depends on the material and the geological history. The assumption of a typical Dutch clay soil leads to certain parameters such as:

- density: $\rho = 1750 kg/m^3$
- cohesion $c = 2 kPa$
- friction angle $\phi = 22.5 \text{ deg}$
- lateral pressure coefficient $K_o = 1 - \sin \phi' = 0.617$

Even though there are empirical relations which directly calculate the total coefficient of lateral pressure, it is preferable to use effective stresses since water is isotropic and it can be easily added to obtain the total horizontal stress; hence:

$$\sigma'_h = K_o * \sigma'_v \quad (48)$$

$$\sigma_h = \sigma'_h + u \quad (49)$$

Given the supposition of no volume changes specific to the undrained conditions, the isotropic effective stresses remain constant which means that the mean effective stress remains constant as well:

$$\sigma'_o = \frac{1}{3}(\sigma'_z + 2\sigma'_x) \quad (50)$$

.5

Determination of undrained shear strength value

The calculations continue in terms of effective stresses and head to the estimation of the stiffness parameters, mainly Young's modulus and undrained shear strength. Mohr-Coulomb failure criterion will serve for the estimation of the strength parameters; the straight line represents the failure envelope within the plot of the shear strength against normal effective stress and it is described by the following equation:

$$\tau' = c + \sigma' \tan \phi \quad (51)$$

The undrained shear strength can be determined considering that drainage does not occur while loading the sample with a confining pressure. This way, the failure envelope for total stress becomes a straight horizontal line. For instance, in the figure below, circle P represents the stress conditions at failure for consolidated sample at pressure σ_3 then sheared to failure where:

$$\sigma_1' = [\sigma_3 + (\Delta d)_f] - (\Delta u_d)_f = \sigma_1 - (\Delta u_d)_f \quad (52)$$

$$\sigma_3' = \sigma_3 - (\Delta u_d)_f \quad (53)$$

where $(\Delta u_d)_f$ is the pore pressure of the specimen at failure.

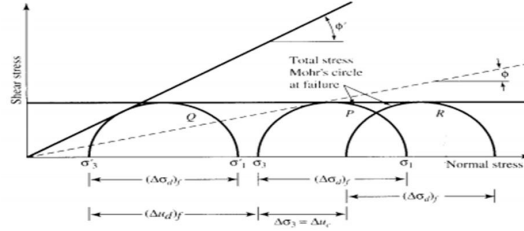


Figure 27: Mohr's circles according to undrained conditions

Finally, the undrained shear strength is calculated as:

$$S_u = \frac{\sigma_1' - \sigma_3'}{2} \quad (54)$$

Scientific literature exposes several formulae used to determine the value of the undrained shear strength. In the order displayed on the graph the values were calculated as it follows:

1. *Measurements (CRUX)* - Den Haan (2011) treats the problem in his article - based on this article, Crux Engineering develops a Plaxis model to validate the equation for the shear strength leading to a set of formulae as a function of the normalized stress given in 3.2:

For the current situation, considering the normalized shear stress to be 40kPa as characteristic, the undrained shear strength equation becomes:

$$S_u = 2.8 + 0.37 * \sigma_v' \quad (55)$$

Classification	Normalized undrained shear strength	Undrained shear strength
[-]	[kPa]	[kPa]
Organic clay (medium)	25	$c_{u,ref} = s_u = 2.8 + 0.22\sigma_v'$
Clay, slightly sandy(weak)	40	$c_{u,ref} = s_u = 2.8 + 0.37\sigma_v'$
Clay,slightly sandy (medium)	55	$c_{u,ref} = s_u = 2.8 + 0.52\sigma_v'$
Clay, slighlty sandy (dense)	80	$c_{u,ref} = s_u = 2.8 + 0.77\sigma_v'$

Table 2: Undrained shear strength equations according to Den Haan

2. *Measurements (Mesri)* - Many researchers focused on the determination of the undrained shear strength based on the CPT results. Numerous equations relate the strength to the plasticity index of the clays. However, Mesri (1975, 1989) found that the undrained shear strength of normally consolidated and lightly overconsolidated clays (overconsolidation ratio less than 2) could be expressed practically independent of plasticity by combining Bjerrum's (1973) proposed relationship between S_u/σ_p^i and plasticity with Bjerrum's correction factor μ . This relationship led to the following equation:

$$S_u = 0.22 * \sigma_v^i \quad (56)$$

3. *Measurements (MC)* - Another way of determining the undrained shear strength value takes into account the Mohr-Coulomb failure criterion, as it was established previously:

$$S_u = \frac{\sigma_v^i - \sigma_h^i}{2} \quad (57)$$

4. *Empirical Mesri* - the same formulae presented above, only applied to the parameters determined empirically.
5. *Empirical (Den Haan formula)* - same formulae used by Crux Engineering, again, applied to the empirical parameters.
6. *Empirical [PI]* - The CPT results represent important data to derive many soil parameters. Various equations were developed to better capture the link between the undrained shear strength and soil properties. A part of the equations express S_u as a function of the plasticity index. The typical Dutch clay soil is considered to have a plasticity index $PI=25\% - 30\%$ leading to the following formulae:

$$S_u = (0.11 + 0.01 * PI) * \sigma_v^i \quad (58)$$

7. *CPT - Mayne(2014)* gathers many equations for the interpretation of seismic piezocone tests. It is common to relate the shear strength to characteristics such as: plasticity index, pore pressure, stress history, mode of testing and so on. The net cone resistance may be used to profile the peak undrained shear strength as well as the measured excess pore pressures; these two being the most frequent methods of determination also known as direct expressions.

$$S_u = \frac{q_t - u_2}{N_{kt}} \quad (59)$$

$$S_u = \frac{u_2 - u_T}{N_{\Delta u}} \quad (60)$$

where q_t - net cone resistance, u_2 - penetration pore water pressure, u_0 - water pressure behind the cone tip, N_{kt} - factor depending on the mode of testing (vane test, triaxial compression/extension, etc) with an usual value of $N_{kt} = 13.6 \pm 1.9$ for soft clays (Low et al, 2010), $N_{\Delta u}$ - factor depending on the pore pressures, approximated for soft clays as $N_{\Delta u} = 6.8 \pm 2.2$ (Low et al, 2010).

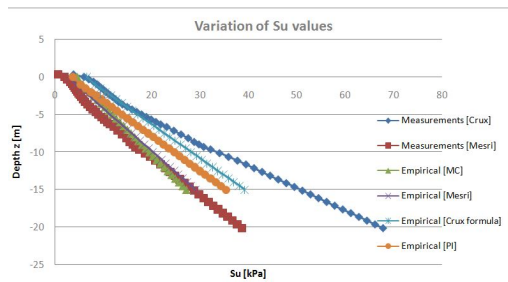


Figure 28: Various values of the undrained shear strength S_u

.6

Abaqus Input parameters - Empirical and Measurements


Depth z	ELASTIC		PLASTIC PARAMETERS					Additional	
	Young's modulus E0	Poisson's ratio ν	Max yield stress σ_y	Yield stress at zero plastic strain σ_0	Young's modulus [SS]	Hardening parameter K		Shear modulus G0	Shear wave velocity Vs
[m]	[kPa]	[-]	[kPa]	[kPa]	[kPa]	[-]		[Kpa]	[m/s]
0	8560	0.48	7.41	0.74	8560.00	1283.00		2891.9	40.08
-1	14480		12.54	1.25	14480.00	1283.00		4891.9	52.13
-2	20400		17.67	1.77	20400.00	1283.00		6891.9	61.88
-3	26320		22.79	2.28	26320.00	1283.00		8891.9	70.28
-4	32240		27.92	2.79	32240.00	1283.00		10891.9	77.79
-5	38160		33.05	3.30	38160.00	1283.00		12891.9	84.63
-6	44080		38.17	3.82	44080.00	1283.00		14891.9	90.96
-7	50000		43.30	4.33	50000.00	1283.00		16891.9	96.87
-8	55920		48.43	4.84	55920.00	1283.00		18891.9	102.45
-9	61840		53.56	5.36	61840.00	1283.00		20891.9	107.73
-10	67760		58.68	5.87	67760.00	1283.00		22891.9	112.77
-11	73680		63.81	6.38	73680.00	1283.00		24891.9	117.60
-12	79600		68.94	6.89	79600.00	1283.00		26891.9	122.23
-13	85520		74.06	7.41	85520.00	1283.00		28891.9	126.69
-14	91440		79.19	7.92	91440.00	1283.00		30891.9	131.00
-15	97360		84.32	8.43	97360.00	1283.00		32891.9	135.18
-16	103280		89.44	8.94	103280.00	1283.00		34891.9	139.23
-17	109200		94.57	9.46	109200.00	1283.00		36891.9	143.16
-18	115120		99.70	9.97	115120.00	1283.00		38891.9	146.99
-19	121040		104.82	10.48	121040.00	1283.00		40891.9	150.72
-20	126960		109.95	11.00	126960.00	1283.00		42891.9	154.37
-21	132880		115.08	11.51	132880.00	1283.00		44891.9	157.92
-22	138800		120.20	12.02	138800.00	1283.00		46891.9	161.40
-23	144720		125.33	12.53	144720.00	1283.00		48891.9	164.81
-24	150640		130.46	13.05	150640.00	1283.00		50891.9	168.15
-25	156560		135.58	13.56	156560.00	1283.00		52891.9	171.42
-26	162480		140.71	14.07	162480.00	1283.00		54891.9	174.63
-27	168400		145.84	14.58	168400.00	1283.00		56891.9	177.78
-28	174320		150.97	15.10	174320.00	1283.00		58891.9	180.88
-29	180240		156.09	15.61	180240.00	1283.00		60891.9	183.93
-30	186160		161.22	16.12	186160.00	1283.00		62891.9	186.92

Figure 29: Input parameters empirically determined


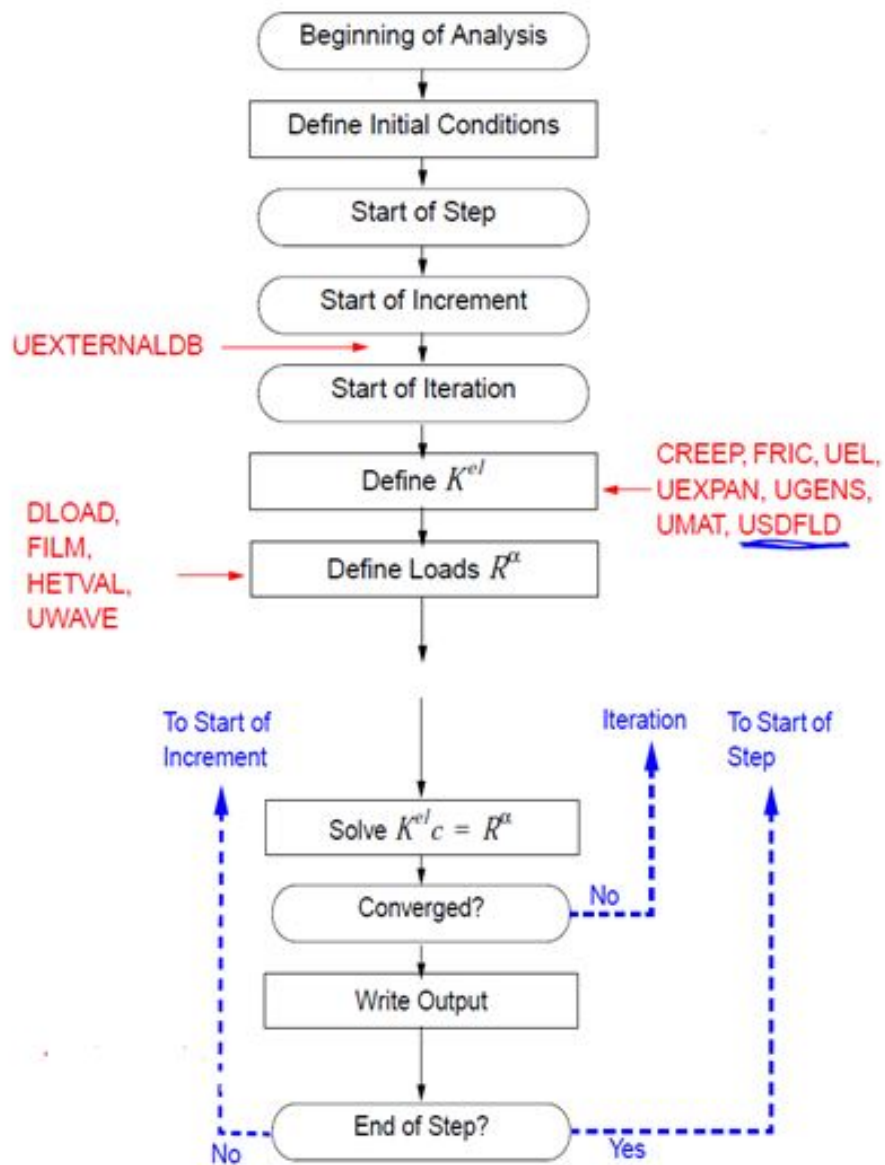
Depth z	ELASTIC		PLASTIC PARAMETERS					Additional	
	Young's modulus E0	Poisson's ratio ν	Max yield stress σ_y	Yield stress at zero plastic strain σ_0	Young's modulus [SS]	Hardening parameter K		Shear modulus G0	Shear wave velocity Vs
[m]	[kPa]	[-]	[kPa]	[kPa]	[kPa]	[-]		[Kpa]	[m/s]
0	29378.88	0.5	7.82	0.78	29378.88	3288.60		7817.1	65.90
-1	12844.86		7.82	0.78	12844.86	2016.46		7817.1	65.90
-2	13495.66		7.82	0.78	13495.66	1708.58		7817.1	65.90
-3	29413.80		7.82	0.78	29413.80	1491.33		7817.1	65.90
-4	35296.56		6.69	0.67	35296.56	1391.46		6690.0	66.78
-5	51683.94		6.69	0.67	51683.94	1322.88		6690.0	66.78
-6	51683.94		6.69	0.67	51683.94	1260.75		6690.0	66.78
-7	60281.23		7.03	0.70	60281.23	1265.75		7029.0	68.45
-8	60281.23		7.03	0.70	60281.23	1207.68		7029.0	68.45
-9	40143.00		7.03	0.70	40143.00	1154.71		7029.0	68.45
-10	128000.00		7.03	0.70	128000.00	1106.18		7029.0	68.45
-11	128000.00		15.32	1.53	128000.00	2397.65		15319.7	101.06
-12	106247.40		15.32	1.53	106247.40	2271.10		15319.7	101.06
-13	101800.00		15.32	1.53	101800.00	2157.24		15319.7	101.06
-14	101800.00		18.38	1.84	101800.00	2463.56		18383.6	101.06
-15	135870.27		18.38	1.84	135870.27	2288.83		18383.6	101.06
-16	135870.27		18.38	1.84	135870.27	2137.25		18383.6	101.06
-17	129305.52		26.92	2.69	129305.52	3029.11		26918.7	122.29
-18	129305.52		26.92	2.69	129305.52	2846.63		26918.7	122.29
-19	188110.31		26.92	2.69	188110.31	2684.90		26918.7	122.29
-20	188110.31		26.92	2.69	188110.31	2540.55		26918.7	122.29
-21	150827.01		26.92	2.69	150827.01	2410.93		26918.7	122.29
-22	150827.01		26.92	2.69	150827.01	2293.89		26918.7	122.29
-23	237602.06		31.40	3.14	237602.06	2553.03		31396.5	132.07
-24	254636.38		31.40	3.14	254636.38	2387.16		31396.5	132.07
-25	223498.92		31.40	3.14	223498.92	2241.53		31396.5	132.07
-26	238925.93		31.40	3.14	238925.93	2112.65		31396.5	132.07
-27	143016.19		20.91	2.09	143016.19	1313.07		20907.8	107.78
-28	137296.13		20.91	2.09	137296.13	1267.71		20907.8	107.78

Figure 30: Input parameters determined from field measurements

.7

Flow chart - Abaqus subroutines



Note: The squared-boxes represent an action taken during the analysis. The round-shaped boxes represent a decision in the code or at a specific state (i.e. beginning of the increment) during the analysis.

Newmark integration schemes

For this particular analysis, an implicit direct integration scheme was selected - this means that the set of equations concerning the set of nonlinear equations of motion are solved at each time step Δt involving both the current and the later state of the system. On the other hand, an explicit analysis finds the solution for the later state of the system starting from the current one. The method is appropriate for this specific application as it successfully solves problems involving nonlinearity, both material and geometric, contact and moderate energy dissipation.

A significant aspect when performing such analyses relates to the stability of the calculation which translates into the size of the time increment. An implicit direct integration scheme is unconditionally stable; it means that there is no limitation in defining the time step size thus, the user can adjust the accuracy of the analysis according to the application. However, care must be paid when establishing the size of the time increment because it influences the energy dissipation as well as the transmission of high frequencies throughout the model.

Abaqus/Standard uses the Hilbert-Hughes-Taylor time integration method which is an extension of the Newmark β method. It basically controls the numerical damping within the system which might rise due to the energy dissipation mechanisms associated with different operator types (for instance, backward Euler operator is more dissipative than second-order Hilbert-Hughes-Taylor). The general equation for the integration method is:

$$\beta = 0.25(1 - \alpha)^2 \quad (61)$$

$$\gamma = 0.5 - \alpha \quad (62)$$

where α is the time integrator parameter $[-0.5 < \alpha < 0]$, β and γ are Newmark's method parameters.

$\alpha = 0$	No artificial damping; energy preserving; Leads to trapezoidal rule/Newmark's method
$\alpha = -0.05$	Negative damping; it produces enough artificial damping to ensure the automatic time step procedure to work smoothly;

Table 3: Time integrator parameter

This control parameter was set to zero to obtain the Newmark's- β method characteristics leading to the parameters $\beta \geq 1/4$ and $\gamma \geq 1/2$ and an unconditionally stable analysis - thus the implicit integration scheme does not encounter any numerical damping. This way, the user can define the time step instead of opting for an automatic time increment associated with an artificial damping - the accuracy can be manipulated manually.

FEM stability in dynamic calculations

The accuracy of such nonlinear problem dealing with wave propagation is controlled by two factors - node spacing in the FE model Δh and the time step Δt . The spacing is directly related to the wavelength whilst the time step depends on the fundamental period of the system. The first condition can be expressed as:

$$\Delta h \leq \frac{\lambda_{min}}{10} = \frac{1}{10} \frac{v}{f_{max}} \quad (63)$$

where Δh - maximum spatial grid, λ_{min} - smallest wavelength; v - average shear wave velocity (usually of the softer soil); f_{max} - maximum appropriate frequency (which can be considered 10Hz for a seismic analysis). This equation assumes that 10 nodes/wavelength should suffice, otherwise high frequencies might be overlooked leading to numerical damping. Soils that might encounter stiffness degradation need a smaller element size in order to better capture the behaviour. Table 4 shows the values used in calculation.

Parameter	Value	Unit
v	132	m/s
f	10	Hz
λ_{min}	13.2	m
Δh	1.32	m
Δh_{final}	1	m

Table 4: Calculation of final mesh size

The second condition has its own two criterion as it follows: stability in terms of time integration and stability related to the FEM. Within an implicit time integration scheme, the time step size decreases as the analysis diverges or the convergence rate is slow. The first criterion suggests the introduction of an upper bound applied to the frequencies that relates to the smallest fundamental period of the system and it is written:

$$\Delta t = \frac{T_n}{10} \quad (64)$$

The second criteria is connected to the FE method that states that during an analysis the nodes are covered in a successive order. If the time step is too large, two nodes can be reached concomitantly - this violates the fundamental wave propagation condition leading to instability. Thus:

$$\Delta t = \frac{\Delta h}{v} \quad (65)$$

here v - highest shear wave velocity. The final time step size is 0.005 sec according to Table 5:

Parameter	Value	Unit
Vs	132	m/s
H	30	m
T_n	0.91	s
Δt_1	0.091	sec
V_{max}	180	m/s
Δh	1	m
Δt_2	0.0056	s
Δt_{final}	0.005	s

Table 5: Calculation of final time step

For the mesh elements, four-node quad elements (CPE4) are used to model the soil using the plane strain formulation of the quad-element. The element connectivity uses a counterclockwise pattern for the previously-described node numbering scheme (see Figure 4.1). The soil elements in each layer are assigned the material tag of the material object corresponding to that layer. A unit thickness is used in all examples for simulating the 1D condition. The self-weight of the soil is considered as a body force acting on each element. The body force is set as the unit weight of the soil in each layer, which is determined from the respective mass density input value.