

A design-oriented numerical investigation on seismic soil-structure interaction

Master of Science Thesis

Raluca-Fulguta Toma

A thesis presented for the degree of
Master of Science

Faculty of Civil Engineering and Geosciences
Delft University of Technology
Crux Engineering BV Netherlands



Committee board is composed by

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ISBN 000-00-0000-000-0

An electronic version of this dissertation is available at
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Contents

1	Introduction	4
1.1	Current situation - an overview	4
1.2	Solutions	6
1.2.1	Conventional design	6
1.2.2	New design philosophy	7
1.3	Research objectives	10
1.4	Research outline	11
2	Literature survey	13
2.1	A new design philosophy	13
2.2	Newmark sliding block analogue	13
2.3	Non-linear soil response - Effects	16
2.4	Geometrical non-linearity: Uplifting	17
2.5	Material non-linearity: Soil yielding	18
2.6	Soil condition	20
2.6.1	Problem statement	20
2.6.2	Constitutive model	20
2.7	Numerical analyses	22
2.7.1	General features	22
2.7.2	Conventional versus new design philosophy	23
2.7.3	Relevant studies	26
2.7.4	Embedded foundations	28
2.8	Numerical tools	28
2.9	Expected results	29
3	Material calibration using one element mesh	33
3.1	General	33
3.2	Normalized stiffness degradation and material damping curves	34
3.2.1	G/G_{max} curves	36
3.2.2	Darendeli results	36
3.3	Modelling	38
3.3.1	Steps	38
3.4	Material description	42
3.4.1	Input parameters	42
3.4.2	Non-linear parameters (kinematic hardening model with Von Mises failure criterion)	48
3.5	Results	49
3.5.1	General	49

3.5.2	Parameters that influence the soil response	51
3.5.3	Validation - Comparison with Darendeli curves	52
3.6	Conclusions	54
4	Site Response Analysis	55
4.1	Introduction	55
4.2	Model description	55
4.2.1	Steps of analysis	56
4.2.2	Input parameters	58
4.2.3	Rayleigh coefficients	58
4.2.4	Integration scheme	60
4.2.5	FEM stability	60
4.2.6	Mesh	60
4.3	NERA - Non-linear Earthquake Site Response	61
4.4	Results	62
4.5	Comparison Abaqus vs NERA	66
4.5.1	Remarks	67
4.5.2	Additional investigation	69
4.6	Conclusions	70
5	Soil Structure Interaction analysis	73
5.1	New design philosophy	73
5.2	Problem definition	73
5.3	Model description	74
5.4	Method of analysis	75
5.4.1	Analysis procedure - Steps	75
5.4.2	Contact definition	76
5.4.3	Boundary conditions	78
5.5	Implementation of ABC	81
5.6	Results	84
5.6.1	Effects of applied boundary conditions	84
5.6.2	Effects of loads	84
5.6.3	FBC vs TSI	84
5.6.4	Stresses	87
5.6.5	Acceleration response	88
5.7	Limitations and recommendations	90
5.8	Conclusions	90
	Appendix	91
I	Appendix	91
A	Cone penetration test results	92
B	Constitutive model: Nonlinear kinematic hardening model with a Von Mises failure criterion	94
B.1	Von Mises failure criterion. A definition	94
B.2	Constitutive model according to Lemaitre and Chaboche: Nonlinear kinematic hardening rules	95

C Description of Darendeli hyperbolic model	98
D Input parameter - Stresses calculation	100
E Determination of undrained shear strength value	102
F Abaqus Input parameters - Empirical and Measurements	105
G Flow chart - Abaqus subroutines	107
H User subroutine implemented in analysis	109
I Newmark integration schemes	111
J FEM stability in dynamic calculations	113
K NERA - Iwan Mroz material model description	115
L NERA - Input example	120
Bibliography	122

Chapter 1

Introduction

1.1 Current situation - an overview

In the past few decades, Northern area of Netherlands is facing ground tremors induced by the gas extraction, the greatest event being registered on 16th of August 2012, at Huizinge [1], with a depth of 10km and a magnitude of $M_w=3.6$. Even though the majority of these earthquakes are shallow and small, the larger events can eventually produce damage concerning the citizens and mining companies. The level of uncertainties rises and the phenomena starts to be problematic when combined with other detrimental factors. For instance, the foundation shape and design, the uncertainties related to the soil homogeneity and nonlinear response or the need of updating the design codes accordingly. Currently, numerous organizations and companies investigate the phenomenon - performing hazard studies and aiming to provide reliable design methods that best suit the condition.

The first particularity of the state of affairs is represented by the characteristic of the earthquake itself. Europe mainly encounters tectonic seism in south and south-eastern parts, while the the Groningen site condition reveals a triggered seismic activity - which is more difficult to assess source-wise. Induced seismicity relates to human activities that alter the stress-strain development within the crust and usually associates with low magnitudes. It follows that the relationship between “anthropogenic” stress disturbances and the resulting earthquake magnitude will always be somewhat unpredictable, insofar as it is partly associated with “background” event probabilities. Nevertheless, the factors that could influence the maximum size of induced earthquakes are of great interest.

Secondly, guidelines for the selection of appropriate suites of acceleration time-series for this purpose are lacking and seismic design codes are particularly poor in this respect. Additionally, accelerograms and borehole sensors data are insufficient to develop a reliable ground prediction model. (Accelerograms represent recordings of the ground acceleration during an earthquake). Obviously, real records are an ever more attractive option for defining the input to dynamic analyses in geotechnical and structural engineering - however, few relevant events took place so far.

During the event from August 2012, the devices recorded the ground motion and transcribed the signals into plots containing the ground acceleration against time. The available accelerogram data allows a better understanding of the entire phenomena whilst several aspects arise after a close investigation. Firstly, the seismicity shows similar patterns compared to the triggered type of earthquake - which, based on empirical data, is considered to have an upper limit of $M_w = 5.0$. Studying the event, considering a large

time scale, reveals that the Groningen field is mainly dominated by rather frequent small events than scarce large ones. Meanwhile, both statistical and physical modelling are performed for estimating the maximum moment magnitude M_{max} values.

Furthermore, the seismic source is usually described through principal (P) waves, secondary or shear (S) waves and surface waves that are all affected by the orientation of the fault plane. In addition, waveform data allows detection of focal mechanisms of the small earthquake in inhomogeneous subsoil. A correct evaluation of the waves further provides reliable parameters such as the seismic moment, amplitude correction along with the focal mechanism. The current seismic survey, found in the figure below, shows this dissimilarity in data recorded in close locations (red representing Middelstum event in 2009 and blue the Huizinge event, respectively) highlighting the difference in the polarity pattern of the P waves [as it can be seen in the vertical accelerograms]. This translates into a difficulty in understanding the characteristics of the earthquake and its mechanical behaviour. Moreover, the double S pulse, evident in the Huizinge earthquake, extends the duration of the ground shaking. These multiple S-phases might be generated by the salt layer which varies in thickness along the area. Salt deposit is a high velocity layer - hence multiple reflections can be the culprit for this particular wave propagation pattern.

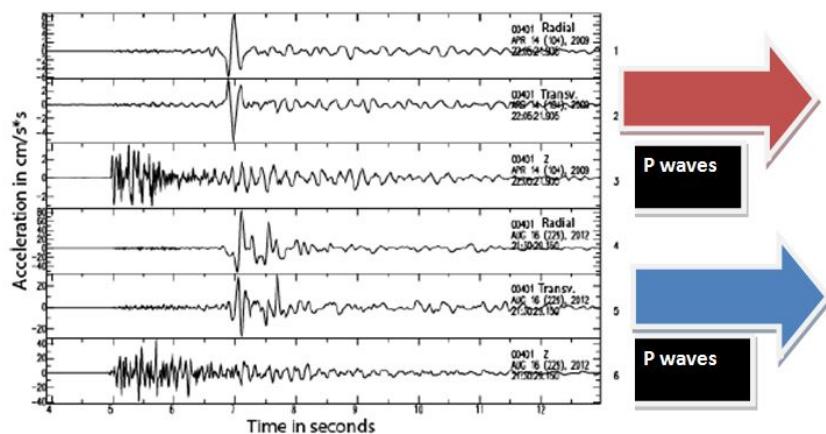


Figure 1.1: Accelerograms from Middelstum 1st April 2009 (red arrow) and Huizinge 16th of August 2012 (1 - Radial, 2 - Transverse, 3 - Vertical)

Another aspect important to mention refers to previous times where the Dutch standard did not include seismic design which further reflected into inadequately reinforced concrete structures as well as the lack of reinforcement within masonry buildings. Existing constructions are not seismically prepared - as the only lateral force taken into consideration, while designing, was the wind load (5 - 15 times lower than a seismic load). Ductility demand is not fulfilled henceforth, cracks appear after earthquake and structures start to account irreversible damage. The foundations of most buildings are footing strips, 10cm to 30cm high and 20cm wide unable to withstand the stresses produced during an ground shaking. The floor does not provide the rigid diaphragm property, allowing the vertical elements (walls and columns) to displace independently. The overall stiffness cannot avoid damage and so foundation strengthening methods *supply the solution*.

One major factor influencing the structural nonlinear response is the subsoil on which the buildings are founded on. The typical soil for Netherlands consists in layers of sand in all states, peat, clay which all denote weak strength, potential of swelling, creep and pore pressure build-up as well as low seismic velocities. Softer soils amplify more the

seismic waves, increasing the effect. This, in association with the multiple S-phase, leads to an augmented energy pulse throughout a longer duration. In fact, due to its prolonged duration, it is considered to exceed the limits imposed by the simplified response spectrum given within the Eurocode 8 guidelines.

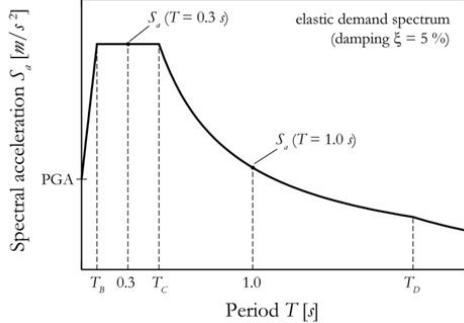


Figure 1.2: Simplified response spectra according to Eurocode 8

Reflecting on all these aspects, the situation calls for extensive investigation to determine the nature of the seismic action, its consequences and mitigation forms - or seismic design computation methods.

1.2 Solutions

1.2.1 Conventional design

Earthquake effects on buildings have been studied for over a century. Since the civil engineering community realized that guaranteeing great bearing capacity to the structures does not necessarily translate into enhanced safety, it adopted a *fail-safe* design concept. The aim included a better control over the load path and energy dissipation throughout the structure, reliable solutions in case of unforeseen collapse of an element. A number of requirements arise from the concept such as: (i) structural elements are able to withstand exceeding dynamic loads avoiding collapse - acknowledged as *ductility design*; (ii) the building encloses specific elements that are designed to fail in order to maintain overall integrity; and (iii) bending type of failure is preferable instead of shear failure - *capacity design* (Park and Pauley, 1975 [2]).

Conventional or capacity seismic design implies that highly inelastic response cannot be always avoided, thus an optimal energy dissipation mechanism is preferred that would engage several bearing elements to experience full strength mobilization. One of the most successful concepts of energy dissipation suggests that columns should remain strong while beams can display plastic articulation at the extremities; additionally, the pier encounters plasticity at their base level. The concept is also known as *strong columns, weak beams* and it can be seen in Figure 1.3. The plastic articulation (or hinge) means a type of energy damping device allowing rotation of an otherwise rigid element; it develops when plastic bending takes place within the element. This also comes in conformity with the capacity design rule: *bending failure* rather than *brittle shear failure*.

On the other hand, EC8 (Part 2, section 5.8) [3] states that the foundation seismic design should avoid the mobilization of strength in the foundation at any costs: "...foundations shall not be used as sources of hysteretic energy dissipation, and therefore shall

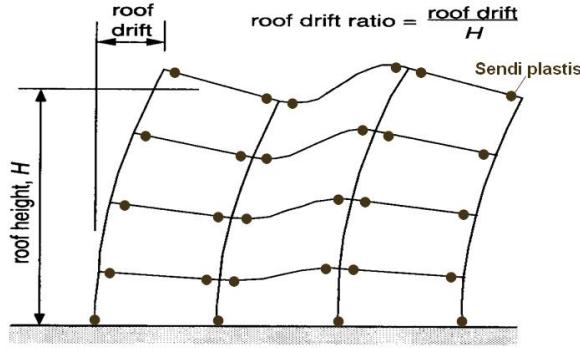


Figure 1.3: Strong columns, weak beam concept

be designed to remain elastic under the design seismic action.” Numerically, this means that the safety factor for static loads used in foundation design are large ($FS = 2 - 3$). Structurally, it hints that no plastic hinges should develop within the underlying soil. And from geotechnical point of view, the foundation should not reach any state that might imply failure.

To outline the main features of the conventional foundation design:

1. No plastic hinging formation in pile-caps, foundation beams, rafts, so on.
2. Prevention of bearing capacity type of failure mechanism under uplifting shallow foundations.
3. No sliding at the soil-footing interface or excessive uplifting of a shallow foundation is allowed.
4. No passive failure adjacent to the edges of an embedded foundation.
5. No combination of any of the previous “failure” modes.

1.2.2 New design philosophy

Recent researches focused on the behaviour of shallow foundations subjected to strong seismic loading and proved that the bearing capacity of the underlying soil is a reliable element that helps the structure to withstand such excitation and, further, the nonlinear foundation response acts rather beneficial in case of strong ground shakes. The concept of “rocking isolation” has thereby emerged as an alternative to the conservative – yet not safer – design of foundations against strong seismic shaking (Pecker, 1998, 2003 [4]; Martin & Lam, 2000; Faccioli et al., 2001 [5]; Kutter et al., 2003; Gazetas et al., 2004 [6]; Gajan et al., 2005 [7]; Anastasopoulos et al., 2010 [8], 2012 [9]; Kourkoulis et al 2012 [10]; Gazetas 2013 [11]). The reasons behind this new approach can relate to the following:

- The last 25 years showed increasing ground acceleration values; this implies a higher capacity demand for the foundation in order to remain elastic and a larger ductility demand for the superstructure if the soil fails in limiting the transmitted accelerations.
- There is a considerable amount of historical monuments surviving earthquake actions showing that sliding and uplifting played a beneficial role during the ground shaking. Two opposite examples can be visualized in Figures 1.5 and 1.6.

- The earthquake can be regarded as a combination of fast-cyclic and kinematic effects – it is common practice to take advantage of such features when designing slopes or retaining walls and allow sliding to occur.

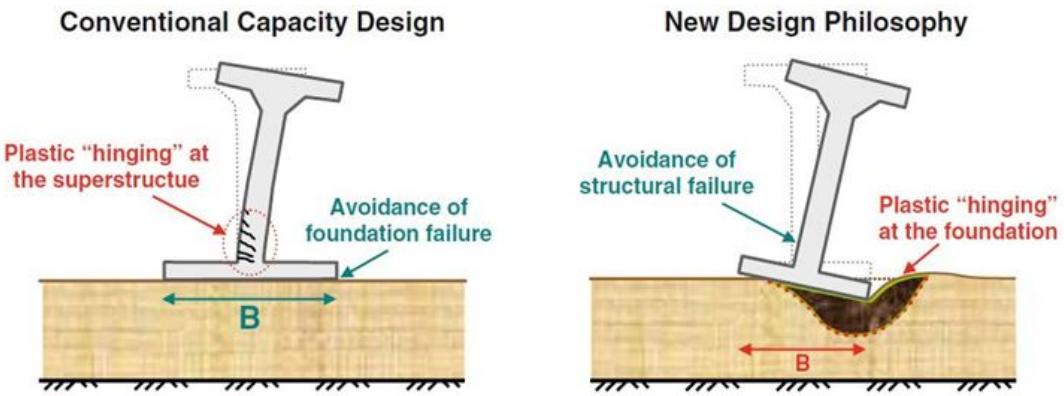


Figure 1.4: Comparison between conventional capacity design and the new design philosophy



Figure 1.5: Plastic hinging at the base of the superstructure associated with collapse - Kobe, Japan 1995



Figure 1.6: Unintentional plastic hinging development within the soft soil; large rotations leading eventually to collapse - Adapazari, Turkey 1999

The new design philosophy proposes to “contradict” aspects of the conventional design with emphasis on development of plastic articulations within the soil. Strong seismic

motion induces large structural inertia forces which, in the case of slender buildings, means larger overturning moments compared to vertical forces. As a result, the footing experiences uplifting at one edge and, possibly, high normal stresses under the opposite edge; if this concentration of stresses is sufficiently large then bearing capacity failure mechanism materializes. Even though, in static conditions this phenomena would act detrimental causing failure, in dynamic circumstances the cyclic and kinematic effects of the earthquake actually improve the structural performance because:

1. The inertial forces change the loading direction rapidly; in the end, it is a cyclic motion so the forces reverse and distress the soil; hence an under-designed foundation ($FS < 1$) will experience large displacements during a limited period of time (tenths of a second) but they are reversed before the critical point is reached.
2. The developing inertial forces should be regarded as an vibratory displacement at the base and not as an external load on the superstructure. Excessive settlements and rotation can be generated as a function of the foundation capacity, however, failure is almost improbable. Thus, the loads transmitted to the superstructure are also restricted to the actual capacity of base or the interface separating the foundation-structure system.

Thus, the main objectives of the new design philosophy focus on foundation response when subjected to seismic motion – a response that opposes the current codes requirements and typically is associated with failure. Thus, the fundamental features of the new method are:

1. Soil uplift and sliding at soil-structure interface is allowed and actually triggered;
2. Mobilization of bearing capacity failure mechanism due to large over-turning moments;
3. Plastification of soil near the edges of the footing described by large vertical stresses;
4. Combination of any of the above.

The current study works with a collection of peculiar characteristics. First of all, the earthquake is defined as a triggered type, unlike the usual European tectonic one. Moreover, Netherlands national code does not incorporate chapters regarding suitable seismic design simply because it was not the case so far – organizations and companies are currently busy elaborating a proper formulation for this matter. Secondly, the soil is very soft, bedrock lacks at any meaningful depth; the multi-shear waves might amplify the acceleration response at surface, thus the whole assembly describes a unique situation. Thirdly, it would improve the economical aspect, since a reduction in the superstructure ductility demand means a cost reduction regarding the necessary reinforcement required by a conventional capacity design.

Having all these mentioned, the challenge of this thesis is to apply and examine the new design philosophy effects upon this particular set of aspects. The method proved to be efficient in cases of soft soil responding to the largest earthquake motions of all time; furthermore, it addressed shallow foundations in many tests– which is also the case in this investigation. Instead of taking the standard steps to analyse the dynamic response of the shallow footing, why not adopt this new design philosophy? Why not take advantage of the soft soil prone to accumulate large stresses and use it to limit the ductility demand within the superstructure?

At the end of the research, it should be concluded whether this new method is a trustworthy approach for Groningen seismic conditions. In case of success, perhaps it will attract more attention and it will stimulate future research towards this trend.

1.3 Research objectives

Given the complexity of the current application, several limitations are required to be imposed such as:

- water is considered at surface level to match the undrained conditions assumption. No pore pressure is accounted for – only total stress analysis conditions are evaluated.
- the soil parameters correspond to a homogeneous clay material with linearly increasing properties along the depth which are determined empirically.
- no complicated structure is analysed: the foundation-structure system is implemented in Abaqus using a simple geometry: rectangular footing with a lumped mass on top of the slender pier. The emphasis is on the inelastic soil response and not on the superstructure.
- only a qualitative comparison with results from scientific literature associated with 2D plane strain conditions is performed, since no real data is available.

In order to prepare the final analysis, several previous steps need to be taken:

1. Calibration of the material model to match the normalized curves proposed by Darendeli, 2011 [12].
2. Examination of one-dimensional site response analysis incorporating the calibrated material model. Validation of results through a comparison between two software: Abaqus and NERA.
3. Evaluation of inelastic soil responses at surface level when subjected to various values of PGA.
4. Investigation of the influence of the model boundary conditions on soil response.

Finally, the main scope of the research is to verify whether the new design philosophy is suitable for the ground and seismic conditions specific to Groningen area. This will materialize in an investigation carried out on a soil layer supporting a simple elastic foundation and the main emphasis is on:

1. Soil inelastic response: uplift and sliding at soil-structure interface - large settlements and rotation at foundation centre of mass.
2. Bearing-capacity failure mechanism: large overturning moments at foundation level.
3. Soil plastification: large vertical stresses beneath the footing edges.

The effects of such analysis will be compared to the results the researchers group obtained when dealing with similar situations. In case the outcome show a fair match, it can be speculated that the new design philosophy is successful for this particular set of conditions.

1.4 Research outline

A schematic outline regarding the processes conducted during the thesis project are presented below.

The study starts with an overview of the new design philosophy to be used in the analyses - a new method that promotes the idea of seismic response going beyond certain thresholds that are commonly associated with system failure. Additionally, it gains knowledge regarding the specific conditions the Northern area of Netherlands reveals, including the particular type of earthquake.

A first step towards the main goal is made through the calibration of the material model and it is described in Chapter 3. A strain-controlled shear test is simulated through one element mesh; by applying several strain levels to the shear box it is possible to obtain the non-linear soil response and represent it using normalized stiffness degradation together with material damping curves. The validation consists in comparing the achieved results with the ones existing in the scientific literature.

Chapter 4 extends the previous analysis to a one dimensional soil column subjected to both uniform harmonic as well as real acceleration time history. A site response analysis is performed with emphasis on the inelastic soil outcome in frequency domain together with the site amplification factor. A comparison is performed between Abaqus software output and NERA (Non-Linear Earthquake Site Response Analysis) software - in order to validate the model which will assist the future investigation. Despite various differences that can emerge from distinctions in calculation algorithms, the results display a quite satisfactory match. In addition, two acceleration time history records are examined characterised by a higher PGA value and a lower, respectively. Thus, the results can sustain a comparison with the general response assigned for Groningen area expressed in soil amplification hence the validation relates to the context.

In Chapter 5, a finite-element model describes the soil-structure interaction capturing the new design philosophy features (a) soil uplift and (b) mobilization of bearing capacity type of failure. One of the most important aspects of such analysis relates to the boundary conditions associated with wave propagation phenomena. Since the need of reducing the computational expense of the numerical investigation, solutions must offer a good balance between model dimensions and accurate outcome - hence, various boundary condition options were explored and their effect on the overall inelastic soil outcome. Moreover, the nonlinear ground response is highlighted through interaction curves produced under static conditions and compared to the existing literature. Considering the geometrical nonlinearity associated with the out-rival of the soil-footing interface tensile strength and thus with the uplifting, parametric studies focus on the influence of structural mass dividing the analysis between (a) *lightly-loaded* and (b) *heavily-loaded footings*. In addition, to accentuate the differences between the conventional and the new design philosophy together with the uplifting effect, two other distinctions in terms of soil-footing contact are formulated as (a) Fully Bonded Contact *FBC* and (b) Tensionless Sliding Interface *TSI*.

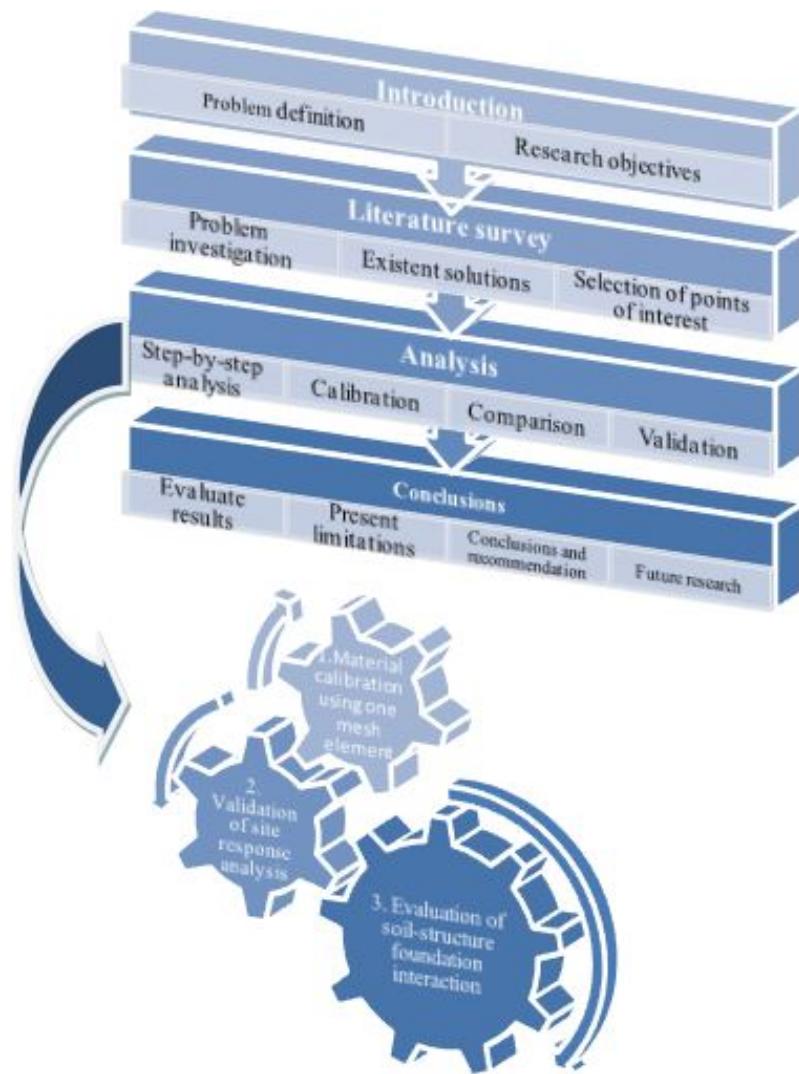


Figure 1.7: Overview of thesis outline

Chapter 2

Literature survey

2.1 A new design philosophy

The current chapter presents the particularities of the new approach together with a summary of results and conclusions yielding from numerical models compared to experimental tests (centrifuge tests). The design seems appealing mainly because of current soil conditions Groningen area displays - mostly silty clay layers carrying strip foundations - if the method proves to be successful, it might mark the beginning of a new trend in seismic design research.

It becomes important to understand the effects, benefits and disadvantages of the new method before carrying any analysis. The priority is to examine the inelastic soil response consequences on overall structural assembly, to follow recent research outcome and means of obtaining it. Moreover, a comparison between the two methods help defining advantages, recognize limitations and improvements one method might bring against the other. Let us begin by acknowledging the starting points of the new design philosophy.

2.2 Newmark sliding block analogue

Newmark, 1965 [13] proposed a simplified model to examine the dynamic behaviour of earth dams and embankments in terms of permanent deformations, both rotation and settlement. The subject of the study is the analogue of a rigid block positioned on an inclined surface; the focus is on the deformations caused when the inertia forces acting on the sliding mass exceed the frictional resistance of the failure surface. A key parameter is represented by the critical, or yield, acceleration A_c which plays different roles depending on the application. On one example, it depicts the pseudo-static base acceleration A_c generating inertia forces that enhance the **sliding failure** ($FS = 1$) whereas on the other example, it describes the constant base acceleration A_c leading to large over-turning moments, thus to a **bearing-capacity failure** ($FS = 1$). The author showed that when the peak amplitude excitation A exceeds the critical acceleration of the system A_c , the underlying medium will only encounter permanent (inelastic) deformations; however, the displacement is not sufficient to provoke failure. A schematization of Newmark model is available in Figures 2.1 and 2.2. Important to mention that these models work in pseudo-static conditions.

The main lesson learned from Newmark's application is that using an engineering safety factor F_E less than 1 does not necessarily act detrimental on the structure, but it rather leads to a fair performance.

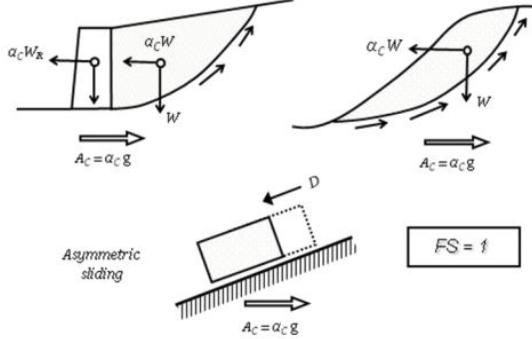


Figure 2.1: First example of Newmark model on inclined plane: critical acceleration depicting the sliding failure at the soil-block interface

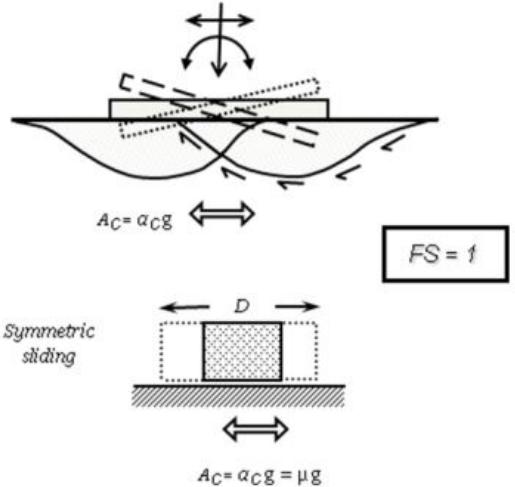


Figure 2.2: A second example of Newmark application on horizontal plane: critical acceleration leading to bearing capacity failure

Learning from this concept, Gazetas, 2013 [14] creates two numerical examples that include a safety factor F_E less than unity, focusing on both sliding and bearing-capacity failure. Firstly, the author investigates the rocking motion of a rigid block highlighting the toppling effect. The object of the study is a rectangular block situated on rigid base with a tensionless interface; details can be seen in Figure 2.3. The excitation comes in the form of Ricker pulse (a representative signal with three main amplitudes) with a peak value exceeding the critical value A_c , thus leading to a safety factor:

$$F_E = \frac{A_c}{A} \longrightarrow F_E = 1/4 \longrightarrow F_E < 1 \quad (2.1)$$

Moreover, the effect of the wavelet frequency gains attention as three various frequencies are introduced ranging from 0.5Hz to 4Hz (representative for the typical ground accelerograms). Results show that the lower frequency produces the maximum angle of rotation θ with a value close to the "overturning" (or critical) angle θ_c :

$$\theta_c = \arctan(b/h) \quad (2.2)$$

The conclusion states that high frequencies induce less rotation compared to lower frequencies; also, the higher frequency input "barely uplifts the block" hence, assuming an engineering safety factor F_E of less than unity does not imply failure by overturning the slender rigid structures.

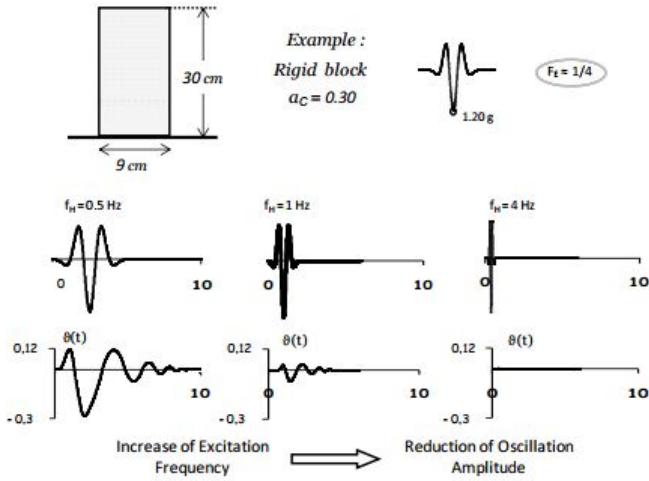
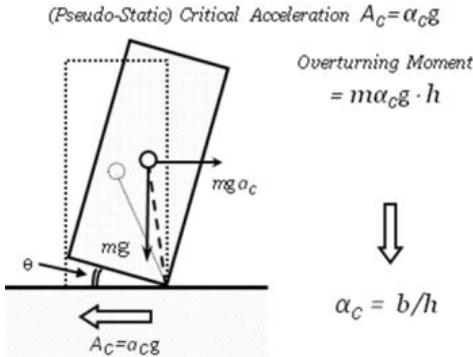


Figure 2.3: Representation of rock-ing rigid block together with a pseudo-static critical acceleration

Figure 2.4: Representation of Ricker pulse. Input frequencies (0.5Hz - 4Hz) and the outcome in terms of angle of rotation θ

Furthermore, Gazetas analysed a simple one-bay building frame subjected to low frequency acceleration record corresponding to Kocaeli earthquake (Turkey, 1999) - the choice of a low frequency motion corresponds to a large angle of rotation as it was discussed in the previous example. The aim of the study is to highlight the mobilisation of soil failure. The author incorporated the pseudo-static critical acceleration A_c that Newmark proposed and calculated the safety factor in terms of accelerations:

$$F_E = \frac{A_c}{A} \longrightarrow F_E = 1/3 \longrightarrow F_E < 1 \quad (2.3)$$

where A_c is the critical acceleration leading to large overturning moments M and shear forces Q on the foundation which, in combination with the vertical force N , lead to the bearing capacity failure. And A is the peak ground acceleration of the input record, here $A = 0.36g$. Figure 2.5 shows the configuration of the model.

The results of the analysis can be seen in Figure 2.6. It can be concluded that, indeed, failure mechanisms develop within the underlying soil; however, due to the cyclic nature of the seismic motion, the "failure" does not take long and is cancelled by the trend in opposite direction. The third snapshot (at $t=17\text{s}$) represents the end of the earthquake and it shows that the final outcome is a combination of settlements and permanent rotation. This might be acceptable in many cases; still, it is the responsibility of the structural engineer to decide the critical deformations.

Nevertheless, the entire phenomenon requires more attention to the details - the chapter continues with a description of non-linear aspects emerging from such dynamic application.

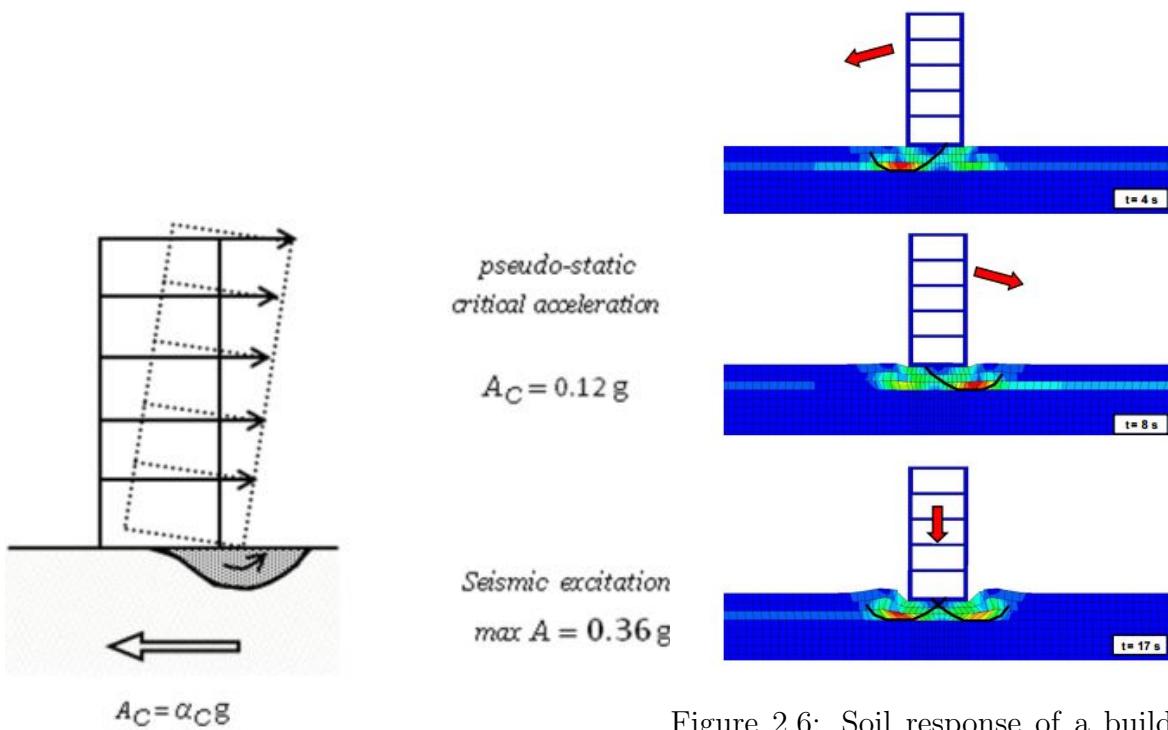


Figure 2.5: Representation of bearing-capacity failure of a one-bay building frame associated with a $F_E < 1$

Figure 2.6: Soil response of a building frame subjected to acceleration record with $A=0.36g$. The shear stress contours indicate the failure zones at different times

2.3 Non-linear soil response - Effects

During seismic loading, the soil responds in a non-linear fashion; studies (Gazetas, 2004 [15], Apostolou, 2012[16]) highlight three mechanisms that might occur in case of ground shaking as the figure below shows. Moreover, one can recognize two types of nonlinearities that govern the response - **geometrical** and **material**.

Geometrical nonlinearity can be described as the separation at supporting soil-strip footing interface that it usually addressed as *uplifting*. The material nonlinearity refers to the type of failure mechanisms governed by the bearing capacity mobilization induced by large cyclic overturning moments - also known as *soil failure*.

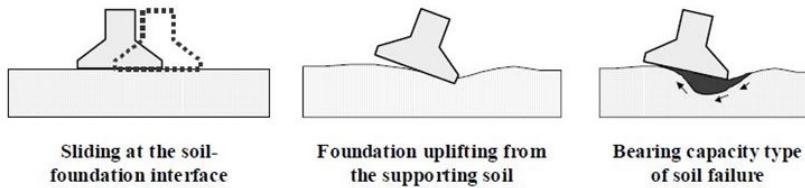


Figure 2.7: Types of nonlinearity

Scientific literature (Chopra, 1985 [17], Pecker, 2001 [18], Gazetas, 2013 [14]) describes several types of possibilities of nonlinear soil-foundation response in terms of both geometric nonlinearity (uplifting and sliding) and material inelasticity (soil yielding) and it can be studied using the following methods:

- Winkler method - comprises the settlement-rotation at the base of the foundation which is described as a series of dashpots and springs. The structure was described by a beam on an elastic medium;
- advanced macro-element modelling - the whole soil-structure system is described by an unique element which simulates the generalized force-displacement behaviour of the foundation. It is worth noting that in the elastic range, and without uplifting, the macroelement reduces to the familiar dynamic spring and dashpot(impedance) matrix;
- direct methods (finite element or finite difference methods) that successfully simulate both the soil and the foundation and the contact surface between them. This method is currently used as it proves itself efficient and accurate.

2.4 Geometrical non-linearity: Uplifting

New philosophy not only allows one of the nonlinearity behaviour to develop within the soil but also encourages that design should apply a safety factor against uplifting and soil failure lower than unity. This way, the structure ductility demand will decrease considerably, optimizing the energy dissipation path throughout the building. Various studies focused on the rocking response simulating the soil in different manners; for example, the first models described the rigid soil via tensionless spring-dashpot elements (Chopra & Yim 1985 [17], Koh et al, 1986 [19]) followed by a single macro-element which includes a constitutive law that accounts for the uplift mechanism in a soil-foundation system. Ultimately, the dynamic analysis is performed in finite-element based software (Hibbit et al, 2001 [20], Gazetas et al, 2010 [8]) - the model combines a rigid foundation footing, elasto-plastic soil and an advanced contact algorithm that inserts the potential sliding and uplifting.

The geometrical non-linearity is generated when large overturning moments (associated with uplift) or lateral forces (inducing sliding) act on the footing. Uplifting occurs due to the incapability of the soil to withstand tensile stresses and it materializes through loss of contact at soil-foundation interface. Additionally, it dictates the moment-rotation relationship towards a softening behaviour even under elastic conditions.

Early studies (Meek, 1975 [21], Chopra & Yim,1985, [17]) considered a simplified rigid soil model and highlighted two states of response: (1) full-contact stage and (2) uplifting stage. A transition between the two phases relates to the bending capacity the structure displays. For a rectangular shallow foundation under static conditions, the moment capacity of the structure right before the initialization of the uplift is:

$$M_{ult} = \frac{NB}{2} \quad (2.4)$$

where N is the permanent axial force on the footing, B is the width of the foundation. The load is assumed to be applied with an eccentricity equal to the half-span of the footing ($B/2$).

Further, the maximum overturning moment induced by inertial forces is:

$$M_{max} = N \frac{a}{g} \frac{H}{2} \quad (2.5)$$

where a is the PGA value, g is the gravitational acceleration ($g = 9.81m/s^2$), H is the height of the superstructure.

Now, the criterion for uplifting is expressed as a function of these two moments; particularly, if the maximum overturning moment goes beyond the capacity ($M_{max} > M_{ult}$), then toppling of the structure occurs. This statement is true for static conditions while in dynamic conditions the uplifting acts beneficial. This is because the foundation can withstand higher values of bending moments compared to the ultimate capacity, M_{ult} . The key in this rocking behaviour is the relatively short time period in which the stresses surpass the limiting values. The ground acceleration displays a rapid change in trend which makes the foundation block to decelerate, stop and rock in the opposite direction. Researchers (Gazetas, 2013 [14]) showed the correlation between the natural period of the foundation footing and rocking potential: high frequency seismic motion leads to a somehow "safer" rocking response preventing collapse or toppling of the superstructure as section 2.2 also justifies.

Scientific literature (Gazetas et al, 2013 [11], Apostolou, 2011 [16], Faccioli et al, 2001 [5], Anastasopoulos et al [8] etc.) confirms that the nature of the seismic excitations along with the fundamental period of the structure dictate the response of the soil-foundation system via a more complicated material model that allows for soil yielding.

One important aspect to keep in mind is that uplifting systems experience larger rotations and occasional overturning whilst the sliding system resists the strong seismic motions with large permanent displacements.

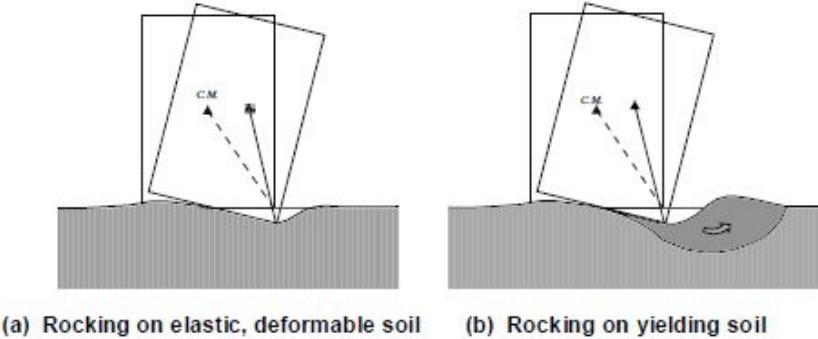


Figure 2.8: The geometrically non-linear nature of the problem is evident even under the assumption of an elastic soil. The image confirms the conclusions from both earlier and more recent models

2.5 Material non-linearity: Soil yielding

In dynamic conditions, the soil response is generally inelastic, hysteretic and irreversible. Pecker and Pender, 2000 [22] proposed a model in which the underlying medium was divided into two main areas: *near field* and *far field* - Figure 2.9 shows a configuration of their model. The authors described how the sub-domains display slightly different soil non-linear response:

- *near field* - represents the soil in the proximity of the foundation where it encounters both the seismic signal and the stress concentrations caused by the vibrations of the structure.

- *far field* - represents the soil located far enough from the structural system such that it experiences only seismic waves propagation.

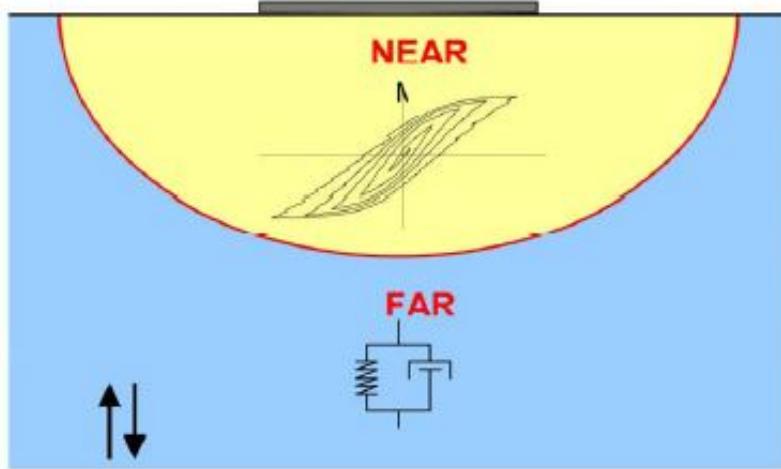


Figure 2.9: Schematization of Pecker&Pender model, 2000

The near-field domain is governed by the material non-linearities. Seed and Idriss, 1986 [23] first introduced the concept of equivalent linear analysis focusing on the non-linear soil response. Using a linear, wave propagation analysis, it updates the visco-elastic soil properties (shear stiffness and damping ratio) in an iterative fashion. The method is valuable for determining the stress state in far-field domain; however, it is not suitable for the near-field as it fails to estimate the plastic strains caused by the footing oscillations. The level of these strains can reach a considerable amount if the foundation experiences large overturning moments.

Thus, the need of a more advanced material model able to incorporate such effects. Starting from late '60s, numerous constitutive models have been proposed describing the non-linear characteristics. First models focused on a elasto-(visco)-plastic material model which further included features such as isotropic plastic hardening rules; these models are adequate if only loading occurs with moderately unloading - which is not necessarily the case. Hence, the situation calls for an constitutive model upgrade integrating hysteresis effects while combining the isotropic and kinematic plastic hardening rules. One of the remarkable material models was proposed by Mroz and Iwan, 1967 [24] - it represents the continuous yielding via multiple yield surfaces in stress space. The constitutive model offers a powerful and flexible calculation tool when combined with kinematic and isotropic hardening/softening plastic rules.

Lemaitre and Chaboche, 1994 [25] gather the conceptual work of the last decades, providing an inventory of constitutive models for continuum mechanics and thermodynamics. Among many others, the book investigates aspects of plasticity, out of which a *non-linear kinematic hardening rule* drew the attention of the current thesis.

The following section will present in more detail the adopted constitutive model which successfully integrates hysteretic features as well as kinematic hardening rules.

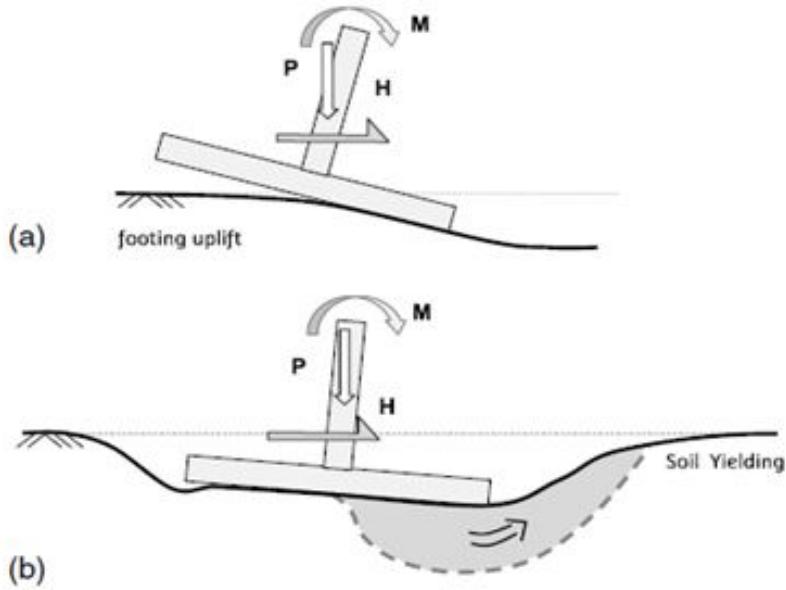


Figure 2.10: Mobilization of ultimate bearing capacity; uplifting(a) and soil yielding (b)

2.6 Soil condition

2.6.1 Problem statement

The current situation deals with a relatively weak clay layer, typical to northern area of Netherlands - the rock layer lacks in most of the cases, being replaced by dense sand deposits. The clay is characterised by little friction angle, cohesive properties as well as low Young's modulus values and, implicitly, low shear wave velocity - amplification of the seismic motion can be expected when dealing with such soil properties.

Appendix A shows a sample of CPT taken in the area of interest - which confirms the assumption of predominantly clayey soil with pockets of silty sand of medium strength. Such soil conditions associated with this type of induced earthquake define a new unique situation that requires its own seismic design approach.

2.6.2 Constitutive model

General A first step in deciding the implementation of the material model is understanding the application to be investigated - what phenomena happens, what are the effects, what mitigations does it require. Having in mind the dynamic nature of the problem, the material model should enclose features that are able to describe mechanically the non-linear phenomena.

As the former section explained, the near-field sub-domain is governed by both the inelastic soil response caused by seismic waves propagation and stress concentrations developed underneath the footing. The situation calls for an advanced constitutive model able to accurately integrate the hysteretic effects, the isotropic and kinematic hardening rules.

Lemaitre and Chaboche, 1994 [25] developed such material model discussing the be-

haviour of both sand and undrained clay soils. Nowadays, research trend (Gazetas et al. [15], [11], [8]) comprises the nonlinear kinematic hardening model characterized by a von Mises failure criterion along with an associated flow rule. The description of the model is rather accessible as it requires only Young's modulus E , soil yield stress σ_y and strength σ . The research group performs multiple analyses using the software ABAQUS; the FEM program incorporates the non-linear kinematic hardening rule in the material section and it yields satisfying results. One of the material model limitations stand in its incapacity of acquiring pore pressure build-up nor dissipation effects. Yet, it proves safe to assume an undrained behaviour given the short duration of seismic loading applied on the system.

Plastic models Materials experience irreversible deformations when elastic limit is reached but loading persists. Theory of the elasticity explains the occurrence of slip surfaces caused by instabilities via the time-independent irreversible deformations. Moreover, it determines the permanent deformations that lead to collapse preventing them while investigating the stability of the system. In order to create a plasticity model, there is the need of few features such as:

- a yield criterion
- a strain hardening rule
- a plastic flow rule

Simplifications of this constitutive models tend to responsibly neglect anisotropy and temperature independence aspects. Important to mention that the term *kinematic* refers to criteria evolution while textitisotropic relates to flow and hardening criteria. Linear kinematic hardening rules provide the translation of the loading surface making use of the hardening variable which indicates the position of the loading surface. However, its limitations call for a more advanced model able to capture the nonlinearity caused by the kinematic hardening. For instance, the linear hardening rule fails to assess the relaxation effects induced by average stresses or the ratcheting effect. In addition, stabilization occurs accordingly to a perfectly plastic cycle when subjected to prescribed strains which does not happen in reality.

Henceforth, the evolution of stress in nonlinear conditions includes two components:

- isotropic hardening component which based on the plastic deformation defines the size of the yield surface giving information related to the change in the equivalent stress;
- nonlinear kinematic hardening component which contains a purely kinematic term and a relaxation one describing the translation of the yield surface.

Considering all above, von Mises failure criterion can be briefly described using three main equations:

$$\sigma_y = \sqrt{3}S_u \quad (2.6)$$

$$\sigma_y = \frac{C}{K} + \sigma_0 \quad (2.7)$$

$$K = \frac{C}{\sqrt{3}S_u - \sigma_0} \quad (2.8)$$

where C is the initial kinematic hardening parameter, K is the parameter characterizing the rate of reduction of the kinematic hardening with increasing plastic deformation, σ_y is the maximum yield stress, σ_0 represents the yield stress at zero plastic strain and S_u is the undrained shear strength.

A more detailed description of the constitutive model can be found in Appendix B in terms of stress state, failure criterion development and mathematical formulas.

2.7 Numerical analyses

2.7.1 General features

Researchers (Anastasopoulos, [26], Ntritsos et al, 2015 [27], Panagiotidou, 2012 [28]) developed various models that highlight the new design particularities - both two-dimensional and three-dimensional elements were used in order to elaborate the soil-foundation system behaviour in static, cyclic and dynamic load combinations.

All the FE analyses performed to research this approach were formulated using the software *Abaqus* [29]. Both the soil and the foundation are modelled as eight-noded hexahedral brick-type element, the soil being considered a non-linear element while the latter elastic. Additionally, centrifuge tests and experiments are compared with the numerical outcome for validation purposes.

A number of simulations included a saturated clay type of material characterised by an undrained shear strength S_u and a maximum shear modulus G_{max} . It proves appropriate to consider undrained soil behaviour due to the rapid loading that corresponds to the seismic excitation - in addition, it allows a total stress analysis which can be described using a von Mises failure criterion along with an associative flow rule. The inelastic soil response was described through an evolution law based on both nonlinear kinematic hardening and isotropic hardening components that account for the changes the yield surface experiences within the stress state.

The two main components of the structural system were separated through an interface that permits sliding and uplifting - a special contact algorithm dictates the detachment in the specific areas where the angle of rotation exceeds the foundation characteristic critical rotation θ_c . The boundaries, both lateral and vertical, depend on the loading type the structure experiences - static conditions do not impose special requirements regarding the position of the boundaries. However, dynamic conditions introduce the wave propagation effect that might distort the final results due to reflections. Two boundary options are proposed - the first one assumes the bounds at a considerable distance from the foundation such that the reflected waves do not influence the results. The second one places the bounds in a position consistent with the static conditions - the trick is to add "lateral infinite elements" that absorb the propagated waves and have similar effect with the first option. The location of the later borders accounts for the pressure-bulbs generated by the dissipation of vertical stresses induced by the moment loading on the foundation strips. Figures 2.11 and 2.12 show examples of FEM models incorporating all the features formerly described.

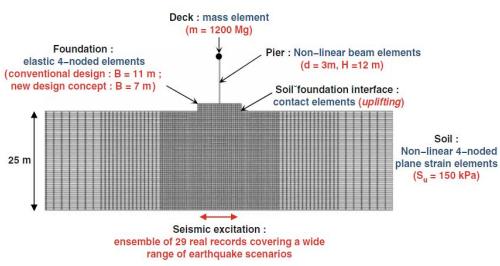


Figure 2.11: Overview of the finite element modeling: plane-strain conditions are assumed, taking account of material (soil and superstructure) inelasticity and geometric

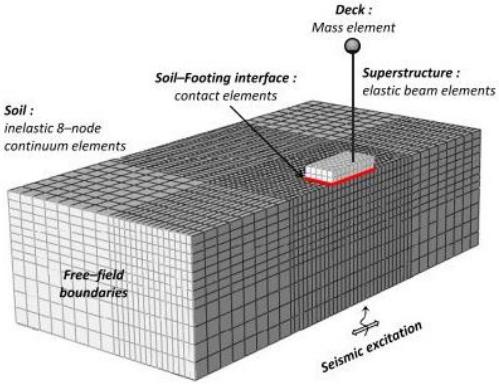


Figure 2.12: Rigorous 3D FEM model comprising the soil-footing-structure system accounting for material and geometric nonlinearities

2.7.2 Conventional versus new design philosophy

The whole design research started with a comparison between the conventional and new design philosophy when subjected to various acceleration time histories. Figure 2.13 shows the results for a situation with moderate seismic input corresponding to Kalamata earthquake, 1986 whereas Figure 2.14 shows the distinction between the two alternatives when considering a stronger earthquake (Kobe, 1995). All the assumptions aforementioned are valid for these analyses. The conventional design premises correspond to the ones described in section 1.2.1 whilst the later method characteristics are depicted in section 1.2.2. Moreover, the capacity design includes an overstrength factor of safety for seismic loading $\gamma_{Rd} = 1.4$ dictating the position of the plastic hinge at the pier base. On the other hand, the under-designed foundation, corresponding to the new design, is assigned with an understrength factor of safety $1/\gamma_{Rd} = 0.7 < 1$.

Medium earthquake motion Few remarks can be formulated based on the observed results. The first set of plots highlight the elastic response of the footing when conventional design is considered whereas the new design shows highly inelastic response. The non-linear response comes at the cost of large settlements under the foundation as the second plot shows; on the contrary, the elastic foundation and pier yielding prevent such consequences. Furthermore, the conventionally designed pier experiences inelasticity, however in tolerable limits while in the new design scheme, the pier remains mainly elastic thanks to soil yielding. Finally, the deck drift, or horizontal displacement at mass, is on one hand caused by the flexural pier distortion (here, Δc) while on the other hand is due to foundation rotation (Δr).

Strong earthquake motion The investigation is further extended to included a stronger earthquake motion which is exceeding the design limits (the Takatori accelerogram recorded at Kobe, 1995). This acceleration time history is relevant as it represents one of the most disastrous earthquakes of the recent times (PGA=0.7g, PGV=169cm/s); the simplified structural system corresponds to a section of Hanshin Expressway which partly collapsed during the earthquake. The results of the two alternatives can be visualized in Figure 2.14.

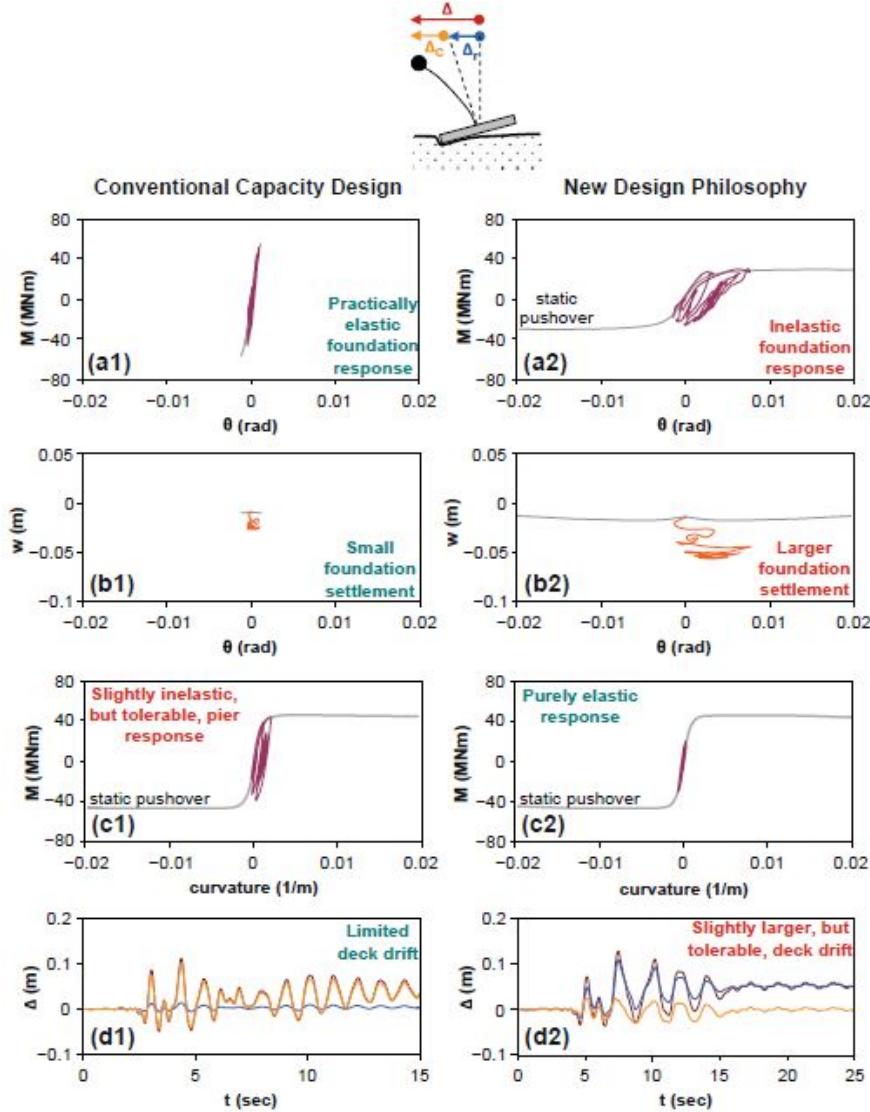


Figure 2.13: Distinction between capacity design and new design philosophy when subjected to a medium earthquake signal (Kalamata, 1985); (a) moment-rotation relationship at foundation level; (b) settlement-rotation response of the footings; (c) bending-moment curvature response at the pier base; (d) time history of deck drift Δ

Similar conclusions can be drawn from this comparison; the deformed mesh examples makes the position of the "plastic hinging" quite evident: the capacity designed system experiences large curvature at the base of the pier and little inelastic deformation at the soil level whereas the other alternative shows opposite effects. The accumulation of stresses beneath the foundation (the extended red areas) hint the bearing capacity type of failure expected from the under-designed footing. The curvature recorded at pier level clearly indicate collapse for the conventional case and inelastic response for the other. These effects are linked with the deck drift Δ : large horizontal displacement at the top of the pier are observed in contrast with limited deck drift for the second alternative. Additionally, the moment-rotation at foundation level corresponds to the soil response: on one hand, elastic foundation response as the pier failure limits the transmitted stresses towards the soil and, on the other hand, inelastic response associated with bearing capacity failure mechanism. As consequences, the conventional designed foundation experiences

small settlements at soil level (approx. 7cm) when the other method triggers increased foundation settlements (24cm). As Anastasopoulos, 2010 [8] acknowledged "...although such settlement is certainly not negligible, it can be considered as a small price to pay to avoid collapse under such a tremendous ground shaking".

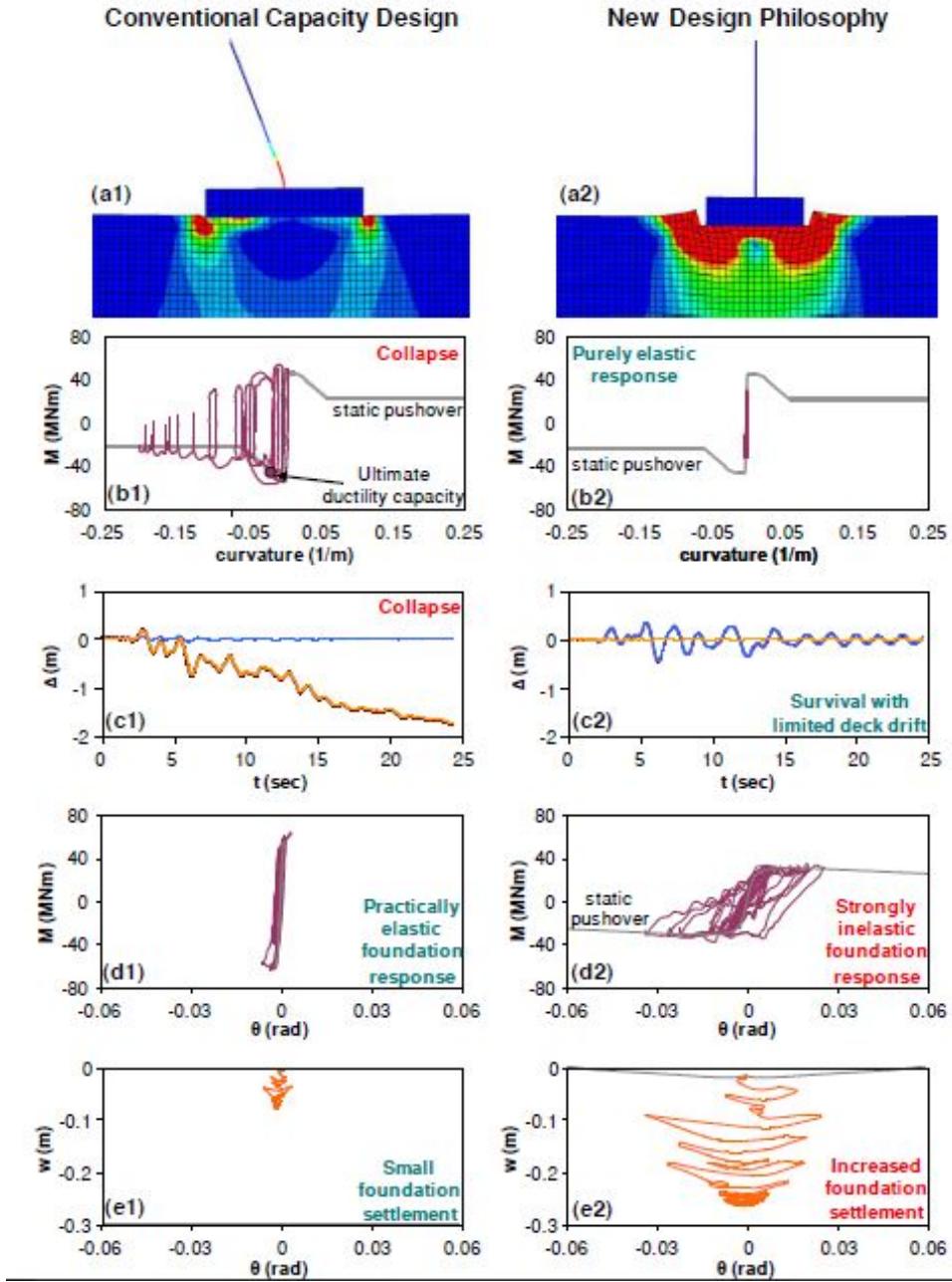


Figure 2.14: Comparison between the two design alternatives for strong seismic signal; (a) deformed mesh indicating the location of plastic hinging zones; (b) bending moment-curvature response at pier base level; (c) time history of deck drift ; (d) overturning moment-rotation relationship at foundation level; (e) foundation settlement-rotation response.

2.7.3 Relevant studies

Now, that the main differences in response were evaluated, it is important to select relevant cases from the vast collection of studies performed to support the new design philosophy. Various methods of simulating dynamic response were investigated for systems considering slender structures simplified as rigid oscillators standing on inelastic soil. The system response was further processed in order to obtain an approximation of the rocking behaviour - moment-rotation response together with settlement-rotation are of main interest. In addition, emphasis on the nonlinearities effects were made with respect to the fundamental period of the oscillator.

Monotonic response The monotonic tests represent a simplified method to estimate the dynamic response; it comes in the form of a "push-over analysis" and it gained popularity for being able to accurately estimate the seismic deformation demands and ultimate capacity. The concept consists in applying a monotonically increasing lateral displacement loading at superstructure level until failure by overturning is reached.

Cyclic response The cyclic tests act in accordance with the previous concept; in fact, it is known as "cyclic push-over test". A rather rotation-controlled loading is applied on the same location in superstructure to simulate the cyclic effects: the rotation is applied through a lateral displacement associated with a constant cyclic amplitude.

Dynamic response Finally, the seismic response is generated via a series of ground-shaking accelerograms - both medium and strong earthquakes recorded all around the world (Kalamata, 1986; Kobe, 1995; Lefkada, 2003, etc). The dynamic input was introduced at bedrock level whilst the response was extracted at the base of the structure.

Furthermore, all simulations examined the difference in response between lightly and heavily loaded foundation expressed as safety factor. The former situation translates into a high vertical safety factor $FS_v = 5$ whereas the later assumes a low value $FS_v = 2$. *The vertical safety factor FS_v is defined as the ratio between the ultimate bearing capacity under pure vertical static load N_u and the currently applied axial force N - $FS_v = \frac{N_u}{N}$.

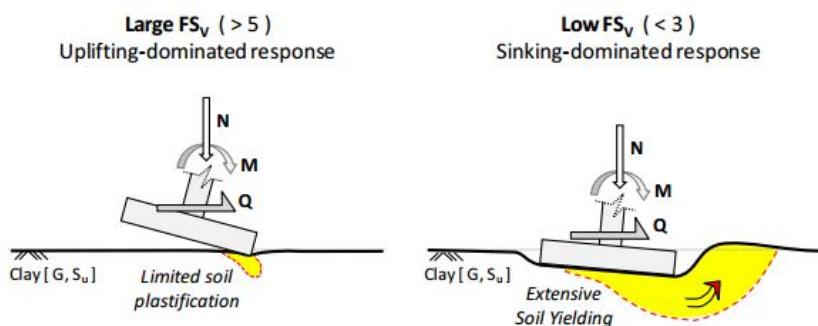


Figure 2.15: Distinction between lightly and heavily loaded foundation highlighting the effects on the soil response

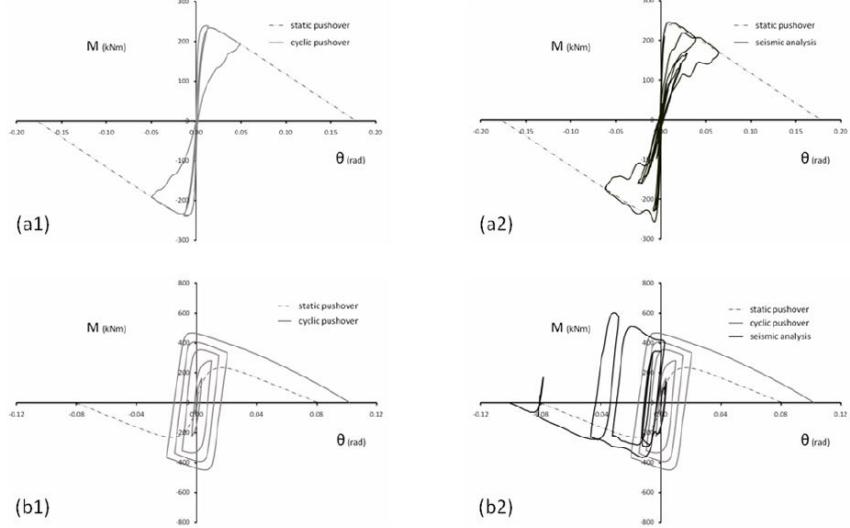


Figure 2.16: Comparison between the soil response when subjected to monotonic/cyclic/seismic loading; moment-rotation response for (a) $FS_v=5$ and (b) $FS_v=2$

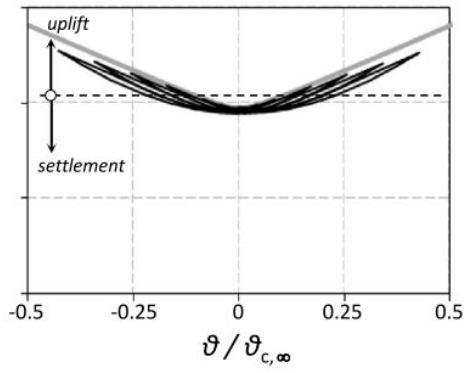


Figure 2.17: Settlement-rotation relationship for $FS_v=5$ (lightly loaded foundation) (gray line corresponds to monotonic backbone curve)

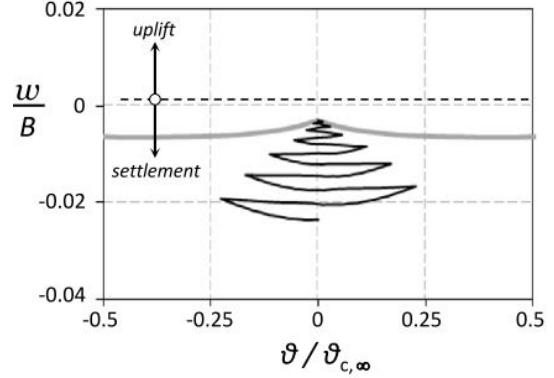


Figure 2.18: Settlement-rotation relationship for $FS_v=2$ (heavily loaded foundation) (gray line corresponds to monotonic backbone curve)

Figures 2.15, 2.16, 2.17 and 2.18 show a collection of responses highlighting the inelastic response; several remarks can be made regarding the difference in response and the correlation with the vertical safety factor, as it follows:

- the lightly loaded foundation displays an uplifting-dominated response compared to the sinking-dominated response associated with the heavily loaded foundation (see fig 2.15);
- for the former situation, the cyclic moment-rotation envelope is well comprised within the static push-over one (see fig 2.16 (a1)) - it relates to the low dissipated energy. The cyclic loading causes small deformations - as a consequence, the area underneath the footing edges show progressive recession (small downward settlements and considerable degradation of rotational stiffness), see fig 2.17.
- in contrast, the highly loaded foundations experience a different trend: the moment-rotation envelope does not follow the static conditions anymore. As the safety factor

increases, the soil encounters an accumulation of downward settlements; furthermore, bearing capacity failure mechanism is evident since excessive shear deformation occur;

- the deformation of the lightly loaded footings is roughly elastic whereas the heavily loaded exhibit a strongly inelastic response - this means gradual accumulation of plastic deformation leading to higher residual rotations.
- the results of the cyclic push-over analysis match the seismic analysis outcome. The soil high compliance leads to large deformations and, thus, the bearing capacity failure mechanism becomes apparent.

Anastasopoulos et al., 2011 [9] investigate the response of a shallow foundation subjected to cyclic loading using results from centrifuge and large-scale tests to validate the numerical simulation performed in ABAQUS.

2.7.4 Embedded foundations

Overall, numerical analyses provide satisfactory results compared to experimental tests. One of the conclusions that can be drawn from the comparison refers to the influence of the rotation amplitude - an increase in the amplitude leads to a decrease in rotational stiffness and does not affect the moment capacity as the number of cycles increase; moreover, the soil settles less each rotational cycle as the number of cycles adds up contributing to vertical stiffness build-up, phenomena known as soil densification. Although the effect cannot be described accurately within the numerical model, the systemic events govern the behaviour hence more attention should be paid in that area.

As discussed before, the static vertical safety factor strongly influences the rocking effectiveness and it relates to soil properties. One of the greatest challenges remains the soil parameterization, especially strength wise, due to consequences of an overestimation - large rotations at foundation level along with intolerable settlements. Varying the value of the safety factor in order to capture the differences between actual and overestimated soil characteristics, several conclusions can be drawn.

Secondly, even the studies successfully describe the response of 1 dof oscillator using the new philosophy design, complex structures introduce deformation compatibility requirements which prove to be vital. After Hucklebridge, 1977 [30] followed by Midorikawa et al., 2006 [31] established the beneficial effects of introducing a rocking-column capacity into structural design, Roh and Reinhorn, 2010 [32] stress on the disadvantages of this method - one element relaxations induces overstress in another leading to unbearable deformations within the superstructure. Extensive uplifting induced by asymmetric loading distribution leads to increased rotation demand of the structural elements and further in residual irreversible deformations. Yet, the system performs in a satisfactory style for strong seismic loadings, here Takatori earthquake recorded in Kobe, 1995. In addition, the presence of beams connecting the columns might limit the drift at top level dictating, more or less, the same displacement.

2.8 Numerical tools

Abaqus [20] offers a wide range of elements and features that help achieving a nonlinear analysis regardless the domain or simulation expertise - it's attractiveness stands in the

possibility of customization, making the software extremely flexible, yet meticulous. It serves well the geotechnical engineering goals as it provides soil and structural elements, total and effective stress analysis, consolidation, static and dynamic analysis and many more. Several types of analysis are available - the main interest relates to Abaqus/Standard.

Abaqus/Standard represents a model database appropriate for both linear and nonlinear static, linear and/or low-speed nonlinear dynamic situations in which stress solutions have a great significance. The current information determines the unknown values at the current time requiring convergence and iteration - it becomes computationally expensive when it does not reach the equilibrium. Two types of behaviour are selected from the available list of analysis techniques - Static, General and Dynamic, Implicit. The first method is a static stress procedure which neglects the inertia forces and time-dependent material effects such as creep or viscoelasticity and can be both linear and nonlinear. It does account for small-displacements performing a geometrically linear analysis during that specific step while ignoring the large-displacements (represented by geometric nonlinearity).

General nonlinear dynamic analysis in Abaqus/Standard uses implicit time integration to calculate the transient dynamic or quasi-static response of a system. Quasi-static applications are primarily interested in determining a final static response. These problems typically show monotonic behaviour, and inertia effects are introduced primarily to regularize unstable behaviour. For example, the statically unstable behaviour may be due to temporarily unconstrained rigid body modes or “snap-through” phenomena. Large time increments are taken when possible to obtain the final solution at minimal computational cost. Considerable numerical dissipation may be required to obtain convergence during certain stages of the loading history.

The following sections describe the current input accordingly to the step sequence required in Abaqus/Standard model database. Theories and equations, software description and images are introduced in order to justify the selected options that led to the current simulation and results.

2.9 Expected results

The nonlinearity observed in the soil response mainly depends on the shear strains which develop within the material when the foundation experiences large angles of rotation. An important parameter arises when the foundation is subjected to large rotations - vertical safety factor FS_v defined as the ratio between the ultimate bearing capacity under pure vertical static load N_u and the currently applied axial force N - $FS_v = \frac{N_u}{N}$. Furthermore, the rotational capacity expressed in terms of ultimate moment resistance of the footing relates to both the axial force N , and the shear force Q acting on the foundation. Recent research emphasize on elaborating ultimate limit states defined by combinations of N , Q and M loads - the graphical representation is known as failure envelope. Another of the new concept goals stands in defining this failure locus - based on load combinations and their position regarding this envelope, one can state whether the foundation acts stable or not. Many experiments based on model-scale shallow footing support this theory along with theoretical and numerical failure equations (Murff, 1994, Bransby and Randolph, 1998 [33], Butterfield and Gottardi, 1994 [34]). Experiments (Gajan et al, 2005 [7]) highlight the influence of two parameters governing the load displacement and energy dissipation aspects of the soil-foundation interface during cyclic loading: static factor of safety re-

garding vertical force exclusively (FSv) and moment-to-shear ratio - together describing the load path. Henceforth, a challenge in assessing seismic loading impact represents the correct evaluation of loading combination (shear force Q and overturning moment M) that will lead to failure for a given vertical force, N , acting on the superstructure.

Having inclusively formulated both the problem and the means for achieving the scope, close investigations can face various directions regarding the outcome each of them being equally relevant. The current study should decide on few aspects to emphasize on, as the time does not suffice for an extensive examination. However, for the little features subjected to investigation, parametric studies are required to be able to make statements, express limitations and recommendations.

The current dissertation narrows on few aspects from the vast possibilities that come along with the new approach as Nitros et al, 2015 [27] describe. One feature relates to the types of interface available for the analysis and two conditions are taken into consideration as it follows:

1. Fully bonded contact [FBC] - the foundation remains in perfect contact throughout the entire analysis; this condition prevents sliding and separation of the foundation from the surrounding soil because of the infinite tensional and shear capacities of the interface.
2. Tensionless sliding interface [TSI] - allows sliding at the contact surface as well as separation of the foundation; the interface follows Coulomb's friction law in total stress depending on the adhesion coefficient α .

Furthermore, several studies focused on the importance of the combined NQM loading and the effect of every of the three forces susceptible to act on the foundation at certain points. Yun & Brandy, 2007 and Gouverneur (2008) [35] formerly examined the undrained bearing capacity of rigid embedded strip foundations under combined NQM loading using a fully bonded contact, followed by Ntritsos et al (2015) who extended the studies to three-dimensional problem of squared foundations adding the option of a tensionless sliding interface.

Nevertheless, the two maximum values - horizontal load Q_{max} and overturning moment M_{max} do not solely represent the failure mechanism; infinite combinations of Q and M are comprised within a failure envelope plotted against normalized values. Additionally, the effect of the vertical load which influences the QM interaction was set to $N = 0$. The figure beneath displays the four main points on the envelope that represent different loading conditions together with significant output at carefully selected points. Both the fully bonded contact (FBC) and tensionless sliding interface (TSI) conditions were investigated and presented for comparison. Important to mention is that the authors preferred to normalize the Q and M values in accordance to the foundation width B , area A and undrained shear strength S_u - the plot contains on the x direction Q/AS_u whilst for the y direction it has M/BAS_u . The main points have specific characteristics as it follows:

- **Point A** *pure moment loading M_{ult}* ; in this point, shear force $Q = 0$. A scoop-type of mechanism is noticeable along with the plastic shear strains shadow contours. Negative rotation can be observed from both the embedded plot as well from the graph.
- **Point B** *pure rotation M_{max}* ; the tangent line to this point is parallel to the horizontal axis which acts accordingly to the associated flow rule which dictates preservation

of normality. Given the dependence of moment loading, the mechanism is characterized by the scoop shape as well. The foundation response is mainly rotational with negative horizontal translation.

- **Point C** *pure horizontal translation* Q_{max} ; also, the preservation of normality can be noticed in the form of the tangent line which is parallel to the vertical axis. The failure mechanism is characterized by the sliding of the whole system; both active and passive sides exhibit failure as presented above - including the side walls effects.
- **Point D** *pure horizontal load* Q_{ult} ; reversed scoop mechanism is observed with the centre of rotation close to the soil surface - the failure mechanism equally depends on both the horizontal translation and counter-clockwise rotation.

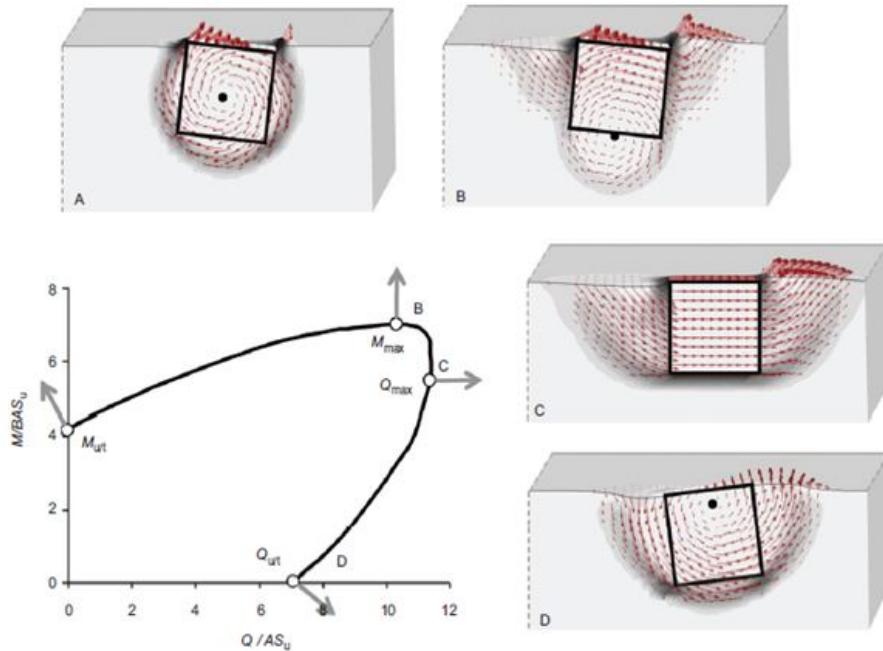


Figure 2.19: Failure envelope include four points of main interest

The herewith figure corresponds to the second type of interface - tensionless sliding interface. There are certain dissimilarities between the two contact surfaces effects - few are exposed as it follows:

- First, the failure mechanisms partly coincide with the ones earlier described in terms of the four limit points (A-D). The sliding faces only constrain the extent of the failure surface leading to no foundation-soil contact which lead to a prevention of wedge development.
- Moreover, the response associated with point B - pure rotation - is different compared to FBC which displays a scoop mechanism; a rather wedge type of failure is evident. Besides, the mechanism at lateral sides, corresponding to the sidewalls, and below the foundation strip seem half of the previous contact situation (FBC).

- Consequently, the sliding and separation of the foundation from the soil is permitted. This leads to a reduction in displacement - just about 1/2 compared to fully bonded contact. Additionally, the ratio D/B which describes the footing geometry and depth (D - height, B - width), varied within the analyses allowing the researchers to observe the influence of embedment on the Q-M failure envelopes.

Furthermore, a comparison between a FBC and a tensionless sliding interface (TSI) type of foundation was made in terms of normalised bending moment M and shear force Q - again using the failure envelopes as reference. This study introduces the influence of the axial force N and, more important, it relates the ultimate capacity of the foundation subjected to cyclic loadings under undrained conditions to the vertical safety factor ($FS_v = N/N_{ult}$). The footing non-linear response is captured throughout models that vary this safety factor, making the distinction between lightly-loaded and heavily-loaded foundations.

Chapter 3

Material calibration using one element mesh

This chapter presents the analysis corresponding to the simulation of a simple shear test in the interest of validating the available soil parameters, its inelastic behaviour and, in the same time, calibrating the FEM model for future and more complicated analysis. The procedure works on a one-mesh element - this way, the material properties can be easily calibrated reducing the computational expenses.

3.1 General

The new design philosophy will be studied numerically upon a model which consists in a homogeneous clay stratum and an elastic foundation. A chimney structure located in the north of Netherlands serves as example, being represented by a rigid strip footing type of foundation connected to a lumped mass element through a rigid beam element. It is desirable to declare these structural elements as both rigid behaving elastically since the main interest channels on soil inelastic response. The underlying strata is associated with a saturated, homogeneous clay responding in an undrained manner, with linearly increasing undrained shear strength S_u along its depth. The figure below briefly presents the structure introduced within the software ABAQUS.

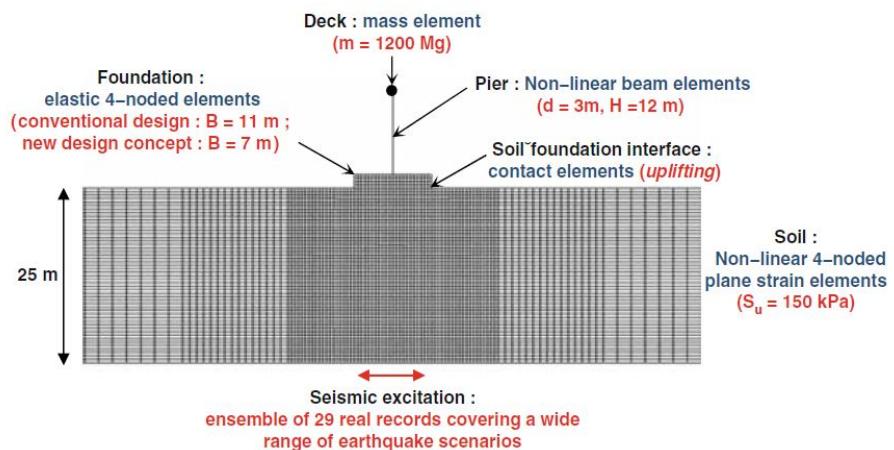


Figure 3.1: Schematization of finite element modeling in 2D space

This chapter represents the first step in achieving the final scope, because it is important to establish reliable features to the main element. The calibration becomes valid once the obtained output coincides with the data published in scientific papers that are analogous to the soil in terms of stiffness, shear modulus and damping parameters. In addition, it is possible to transfer model information from a simulation to a new Abaqus/- Standard analysis, where additional model definitions can be specified. One might first study the local behaviour of a particular component during an assembly process and then study the behaviour of the assembled product. Hence the simple shear test represents the local behaviour mechanism to be studied which will aid the material model validation.

The test helps obtaining results that further lead to the formulation of the normalized stiffness degradation curves together with the material damping ones - an important stepping stone in predicting the material inelastic behaviour when subjected the earthquake ground motions. The test assumes the application of a force on top of the sample such that shear strains are induced within the material. Stiffness degradation is observed and investigated; to better capture the features of the problem in discussion, the cyclic shear test seems more appropriate - the harmonic signal will also highlight the material damping - such a relevant factor when studying nonlinearity. Figure 3.2 shows the schematization of such simple shear test - further aspects will be discussed in more detail later on.

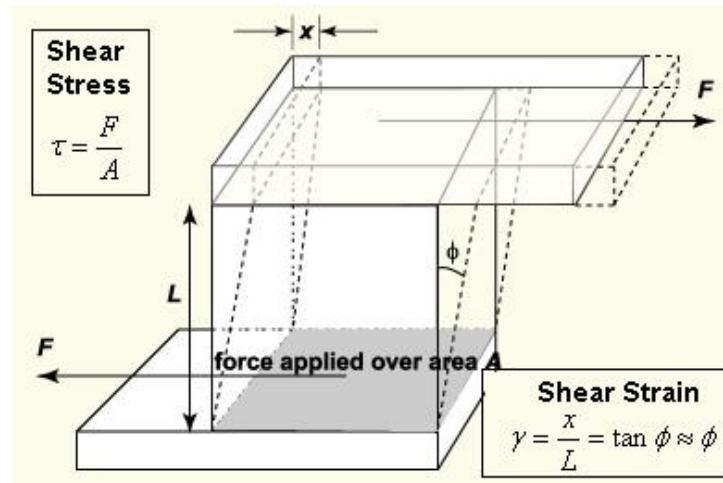


Figure 3.2: Schematization of shear test

3.2 Normalized stiffness degradation and material damping curves

The current sub-chapter presents the concept of stiffness degradation together with material damping. As the soil experiences increase in yield stress, phenomena also known as hardening, the elastic domain undergoes a certain evolution. This evolution can be related to the elastic modulus and shear modulus implicitly - most commonly illustrated with these standard curves (G/G_{max} and damping). The site parametrization plays an important role as it also influences the ground motion parameters (such as Fourier spectra or response spectra) - it becomes essential to evaluate and assign the soil reliable characteristics that capture the non-linear behaviour. Figure 3.3 shows a schematization of the problem that confirms the relevance of the two parameters: G/G_{max} and D_{min} .

The estimation and measurement of the soil modulus reduction with respect to the shear strain has been long studied in geotechnical engineering, as it allows the prediction of the strain level which might lead to crucial modulus reduction together with the prediction of damping and the seismic response overall.

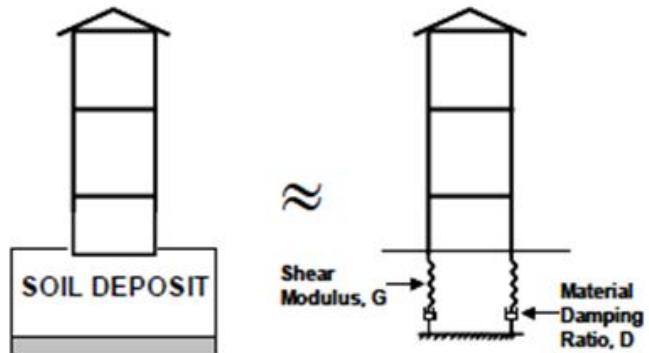


Figure 3.3: Transformation of soil deposit into two parameters - schematization

3.2.1 G/G_{max} curves

Nonlinear response can be achieved through several types of tests, monotonic and cyclic, static and dynamic, each displaying stiffness modulus degradation proportionally influenced by strain development. Generally, the shear stiffness of the soil is represented by the shear modulus, G - physically, it represents the slope of the shear stress and strain when plotting them one against the other. On these specific plots it can be noticed that when a soil is subjected to symmetric cyclic loading, hysteresis loops develop depending on the strain level. The loops support the secant shear modulus calculation which can be considered as the average shear stiffness of the soil. Features such as inclination or breadth of the hysteresis loops strongly depend on both soil stiffness and damping. Given that the cyclic behaviour of the soil is nonlinear as well as hysteretic, it becomes clear that stiffness together with the damping are strain dependent. Therefore, a series of cyclic tests should be performed with varying strain levels such that the collection of results, in terms of stiffness, lead to the normalized modulus reduction curves.

One key parameter is the shear modulus at small strains, also known as *small-strain shear modulus*, G_{max} because it plays a significant role in the elaboration of the normalized modulus reduction curves. As the name itself describes it, G_{max} serves the normalization of the cyclic tests stiffness outcome as being the maximum value the material can experience.

One other key parameter, damping ratio represents a material property related to the friction between soil grains, strain rate effects and inelastic stress-strain response. Each hysteresis loop describes the dissipation of energy during a loading cycle; the post-processing of data leads to the damping ratio as it depends both on the energy dissipated during a complete loading cycle at a given strain amplitude and maximum retained strain energy. Moreover, the decrease in shear strain translates into decrease in dissipated energy, thus the area of the loop will suffer a reduction as well.

Similarly, the damping ratio curves are defined collecting different nonlinear soil responses based on increasing strain amplitude. However, the trend is opposite, as in the nonlinearity of the soil results in an amplification of dissipated energy, thus in the damping ratio, with increasing strain magnitude.

In small-strains domain, the soil behaves elastically leading to a constant shear modulus, equal to G_{max} , as well as a constant damping ratio, equal to D_{min} .

Figure 3.4 shows a typical set of curves which can be divided in three main areas with different behaviour properties defined by the following values:

1. **nonlinearity threshold** γ_e^t or elastic threshold; represents the strain magnitude for which the shear modulus ratio $G/G_{max} > 98\%$. The soil behaves elastically above the strain amplitude, deformations are producing but they are reversible during unloading process. The damping curve shows a correspondence with D_{min} .
2. **cyclic threshold** γ_e^t or plastic threshold; deformations become irreversible, shear modulus ratio G/G_{max} decreases to approximately 80% while damping ratio becomes 3% higher than D_{min} . Beyond this point, the soil can experience volume change.

3.2.2 Darendeli results

Many authors treated this subject of the degradation curves, the most acknowledged being Hardin & Drnevich, 1972, Vucetic & Dobry, 1991[36], Ishibashi & Zhang, 1993 [37]

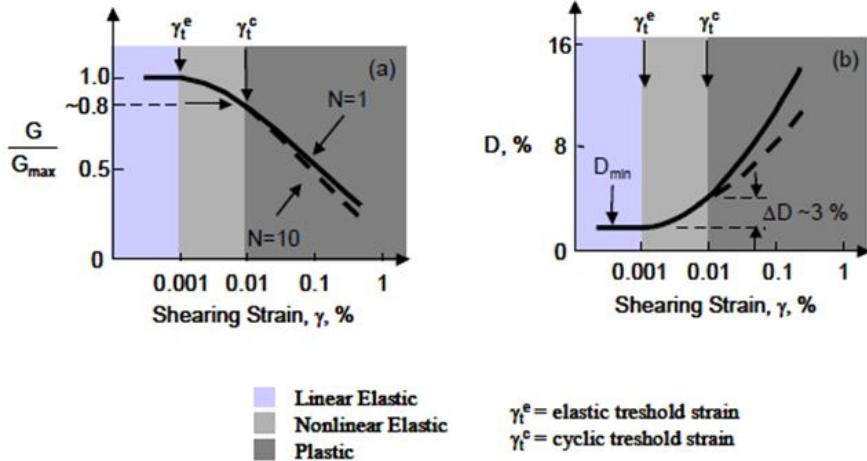


Figure 3.4: Normalized stiffness degradation curve (left) and material damping curve (right)

and Darendeli, 2001[12]. The current thesis opts for the latter given its topicality, also because it combines all the results obtained from previously mentioned authors working on their limitations. Additionally, it offers results associated with a granular material comparable with the Dutch soil used within the present model. M.Darendeli proposes a new empirical framework able to generate normalized modulus reduction and material damping curves. The author investigates the influence of several parameters (for instance soil plasticity or confining pressure) on the dynamic soil response using pre-existent data from University of Texas which has been collected over the past decades. The work of Darendeli is regarded as valuable because the results of the probabilistic seismic hazard analysis include the uncertainty in inelastic soil response.

As other many authors, Darendeli was inspired by the work of Hardin and Drnevich, 1972[38] that represented a step forward in evaluating the dynamic soil behaviour. His study focuses initially on finding strengths and weaknesses in other studies in order to counteract them in his following experiments. The first observation highlights a feature common to all the previous generic curves: the confining pressure takes a relatively "fixed" value of approximately 1 atm and the curves do not incorporate the effect of the confining pressure on the inelastic soil behaviour. Ishibashi and Zhang, 1993 [37] consider soil plasticity and confining pressure but lead to unrealistic values at pressure higher than 10 atm. Darendeli proposes a four-parameter soil model which will account for the effects of the soil type, confining pressure, loading frequency and number of cycles in generating the normalized stiffness degradation and material damping curves. In addition, Table 3.1 presents in detail other factors that might influence the inelastic soil behaviour according to Darendeli study.

Hence, the four-parameter soil model Darendeli proposes can be summarized using two main equations as it follows:

$$\frac{G}{G_{max}} = \frac{1}{1 + \frac{\gamma}{\gamma_{ref}}^a} \quad (3.1)$$

The reference strain γ_{ref} describes the strain level at which the shear modulus G decreases to half of the maximum value G_{max} . Studies show that increasing confining pressures and

Parameter	Impact on G/Gmax curves	Impact on D curves
Strain amplitude	***	***
Mean effective confinement	***	***
Soil type and plasticity	***	***
Number of loading cycles	*+	***++
Frequency of loading	*	**
Overconsolidation ratio	*	*
Void ratio	*	*

*** Very important ** Important * Less important ++ Soil dependent

Table 3.1: Parameters that control nonlinear soil behaviour and their relative importance on the curves according to Darendeli, 2001 [12]

soil plasticity lead to higher strain levels in the normalized modulus reduction curves. The equation of the material damping curve is then expressed as a function of two main parameters (b and D_{min}):

$$D = b \left(\frac{G}{G_{max}} \right)^{0.1} * D_{masing} + D_{min} \quad (3.2)$$

A more detail description of Darendeli's material model can be found in Appendix C.

The current study works with the recommended reduction curves presented by Darendeli within his PhD thesis [12]. The collection of data used by the author for investigation display a good match with the parameters of the ongoing study. A selection of matching data was extracted from Darendeli's work - tables containing values for the normalized modulus reduction and damping curves; data corresponds to a soil with a plasticity index of PI=25% and a confining pressure of 1 atmosphere which also matches current conditions and can be seen in Appendix C.

3.3 Modelling

The analysis starts with the assumption of one element - for the ease of material calibration - homogeneous 3D solid. The model simulates a strain-controlled simple shear test, the parameters correspond to a sample taken within the homogeneous clay layer previously described located at 10m below surface. A single parameter set suffices given the dimensions of the sample: 1m each side; The bottom nodes are created such way to create a rigid base at all times during the analysis whilst the top nodes are connected through an MPC (multi-point connector) - a feature available within the software that enforces a master-slave formulation linking the top nodes to the master node assigned with a reference point. All load and boundary conditions are applied to the master node solely which transmits them further to the slave nodes guaranteeing equal displacements. The master node is assigned with its own system of coordinates which corresponds to the whole model system.

3.3.1 Steps

This sub-chapter presents the steps taken within this calculation including the boundary and the loads conditions as well as a short description of the testing procedure. The main

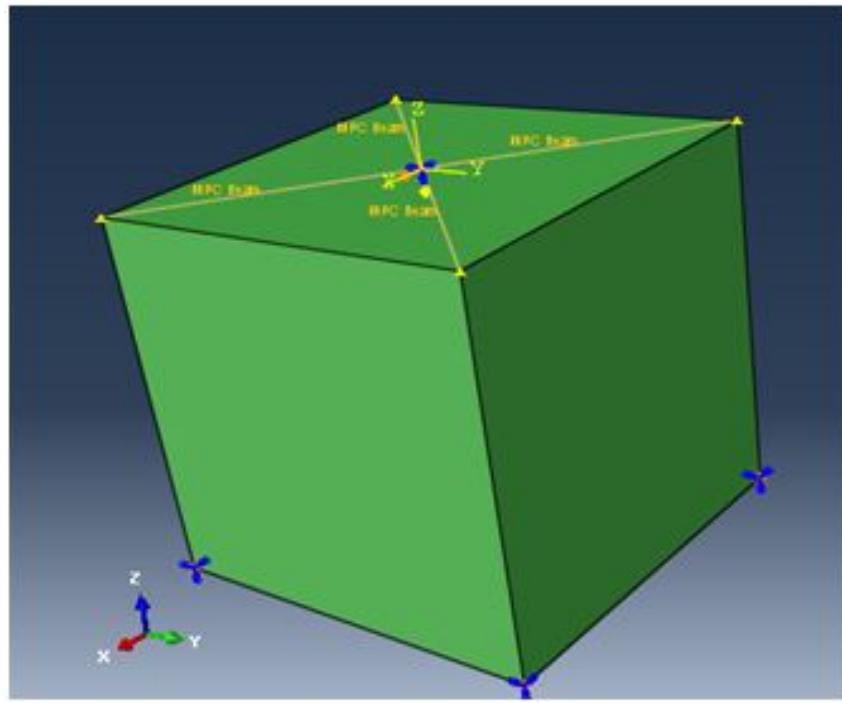


Figure 3.5: Schematization of one element mesh model

idea behind this analysis is first to confine the sample to mimic the natural conditions in terms of stress path. Secondly, the shearing stage consists in controlling and varying the applied strain in order to obtain the nonlinear response. More details about the process are presents below.

First step confinement - assumes the application of the confining pressure at the (top) reference point. The overburden stress is calculated as a function of the unit weight of the soil and the depth corresponding to the sample position. Given the total stress analysis, the pore water pressure is also accounted for within the value; so, for a sample located around 10m below the surface, it yields a confining pressure $F=100\text{kPa}$. As cause of total stress analysis, equilibrium is taken into account – no attention should be pointed at the development of excess pore pressure nor drainage. The illustration below corresponds to the boundary conditions applied at reference point; it turns out that only the vertical translation is permitted whilst all other displacements are restricted. Subsequently, the total overburden pressure is applied on the same vertical direction. In addition, the sample has all the bottom nodes restricted for both translation and rotation.

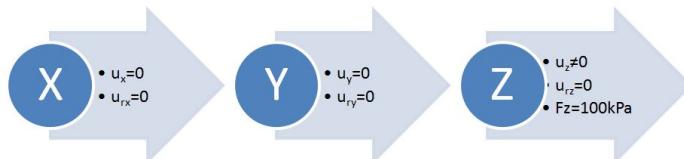


Figure 3.6: Boundary conditions applied at bottom nodes during confinement step

The step is defined as static, general - the analysis can account for both linear and non-linear response. It ignores the time-dependent material effects such as creep or swelling,

but accounts for rate-dependent plasticity or hysteretic behaviour. In a general static analysis the code is iteratively solving $[K_t]du = dF$, where $[K_t]$ is the tangent stiffness matrix, du is the vector of unknown nodal displacements, and dF is the incremental load vector. Each step starts with the end conditions of the previous one, with the state of the model evolving throughout the history of general analysis steps as it responds to the history of loading. The step is associated with a direct linear equation solver - a useful tool in both linear and nonlinear analysis - the solver finds the exact solution to the system of linear equations using a direct Gauss elimination method.

Second step – shearing – propagates most of the existing boundary conditions, deactivating the restriction of top master node translation on x direction. In addition, on the same direction, a new boundary condition is created specific for the strain-controlled shear test. The principle of the simple shear test is to induce direct shear within the sample and it represents a direct method of determining the shear modulus of the soil; hence the usefulness of the current application.

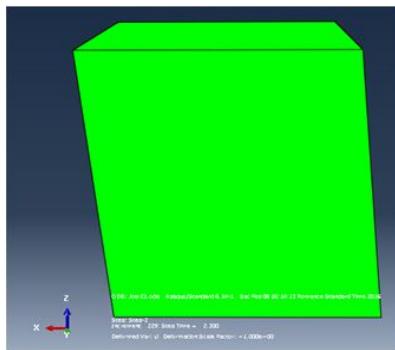


Figure 3.7: Deformed shape of the model after second step

The boundary condition permitting translation on X direction gets assigned with an amplitude feature. Strictly speaking, the cyclic tests should be performed with irregular amplitudes in order to accurately simulate the earthquake action; however, given the difficulties in performing such irregular tests, the simple shear test was always simplified to an uniform amplitude test.

Figure displays the uniform amplitude defined in current analysis - it can be regarded as a "template" for further analyses. Abaqus combines the amplitude history with the prescribed displacement, u_x , through a multiplication and so, the cyclic strain input is created. The magnitude of the cyclic strain varies capturing the transition between small strain and large strain domain as well ($1\% - 1E^{-4}\%$). Several analytical jobs are performed with different strain values until fully elastic behaviour is attained. Each job results in a different response where the main emphasis goes on the shear strain-stress plot that describes hysteretic loops. Based on these loops, the most important parameters for degradation of the stiffness curves are determined, as well as the damping ratio.

Abaqus offers several methods for performing dynamic analysis of problems in which inertia effects are considered. Direct integration of the system must be used when non-linear dynamic response is being studied. The step is defined as a dynamic one; general linear or nonlinear dynamic analysis in Abaqus/Standard uses implicit time integration to calculate the transient dynamic response of a system. Nonlinearities are usually more simply accounted for in dynamic situations than in static situations because the inertia terms provide mathematical stability to the system; thus, the method is successful in

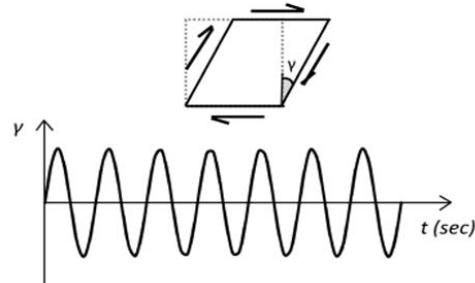
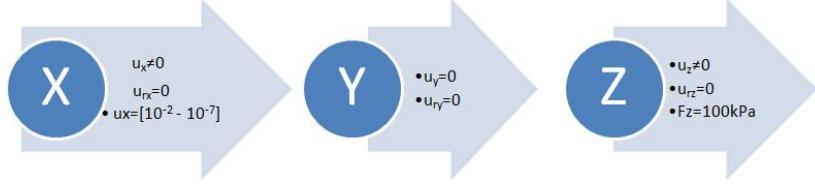


Figure 3.8: Boundary condition at bottom nodes during second step (top); schematization of strain-controlled test concept including uniform cyclic load (bottom)

all but the most extreme cases. An automatic incrementation scheme is provided for use with the general implicit dynamic integration method. The scheme uses a half-step residual control to ensure an accurate dynamic solution. The half-step residual is the equilibrium residual error (out-of-balance forces) halfway through a time increment; for a continuum solution the equilibrium residual should be moderately small compared to significant forces in the problem. Direct implicit algorithm shall be stipulated further on in the following chapters as well as in Appendix I and Appendix J.

3.4 Material description

For the current situation, Abaqus requires the definition of several behaviour components such as:

1. Density - the unit weight density of the model; it is assigned with one value $\rho = 1800 \text{ kg/m}^3$;
2. Elastic - for isotropic conditions, Young's modulus E and Poisson's ratio ν are sufficient for defining the elastic domain;
3. Plastic - non-linear kinematic hardening formulated with a von Mises failure criterion with associative flow; the initial stiffness modulus C , yield stress at zero plastic strain σ_0 and the hardening parameter K , all being defined in Appendix B.

Eventually, in a more advanced stage of the analysis, damping properties are added along with a customized subroutine which introduces the ultimate shear strength along the depth as a function of the elastic stiffness and the effective stresses (E and σ'_0).

3.4.1 Input parameters

As mentioned before, the analysis considers several parameters that are characteristic to the soil in Groningen area – a silty clay, weak to medium weak. In addition, a homogeneous clay layer of 20m is considered – for the ease of the calculation, the soil is converted in a one-layered soil column such that the strength and stiffness parameter distribution along the depth is linear. This chapter presents parameters derived from both measurements and empirical equations, the analysis of one element subjected to a strain-controlled shear test and the results in terms of stiffness degradation and damping. The more detailed equations and methods of obtaining the parameters can be found in Appendix F.

Stresses Total vertical stress represents the starting value for the evaluation of the stresses in each soil segment; assuming vertical equilibrium and neglecting the surcharge, the vertical stresses can be determined. Moreover, the shear stresses on the vertical planes are assumed zero hence, no stress transformation is needed.

Conform Terzaghi's principle, total stress comprises the *effective stress* - which acts on the contact surfaces between the soil grains - and the *pore pressure* - which is considered isotropic and it is in the form of water and air. Due to the isotropic character of the water, the shear stresses are transmitted to and through the skeleton grains exclusively. The case of pure shear suggests change in shape at constant volume and deformations of the granular material are determined by change in effective stresses. That is the reason why the initial parameters are expressed as functions of effective stresses. The equations leading to the definition of the stress state are described in Appendix D.

Now, considering a foundation slab subjected to permanent load, the pore pressure will initially develop decreasing the effective stresses and, since water drainage does not occur immediately, the soil underneath will behave in an undrained fashion. Subsequently, consolidation occurs with dissipation of the excess pore pressure - from this moment onward the foundation is gaining more stability as it passed the critical situation. Moreover, during earthquake, due to the dynamic loading, the undrained behaviour is displayed; these facts emphasize the choice of undrained conditions as being appropriate.

Given the supposition of no volume changes specific to the undrained conditions, the isotropic effective stresses remain constant which means that the mean effective stress remains constant as well:

$$\sigma'_0 = \frac{1}{3}(\sigma'_z + 2\sigma'_x) \quad (3.3)$$

Undrained shear strength The value of the undrained shear strength can be determined with the use of multiple parameters as well as methods. Appendix E shows a collection of techniques for obtaining the undrained shear strength of the soil based on both empirical and measurements data and the plot containing all the values can be seen in Figure 3.9. In order to summarize the features in the calculations, the undrained shear strength can be a function of plasticity index (PI), stress history within the soil (more importantly the effective vertical stress), pore pressure, mode of testing et cetera. One important method to mention is represented by the study of Den Haan, 2011 [39] as he treats the current situation (of Groningen soils) in his article "Ongedraaide sterkte van slappe Nederlandse grond" developing new equations for obtaining undrained shear strength of clayey soils. Crux Engineering develops a Plaxis model to validate the equation leading to a set of formulae as a function of the normalized stress given in Table 1.

For the current situation, considering the normalized shear stress to be 40kPa as characteristic, the undrained shear strength equation becomes:

$$S_u = 2.8 + 0.37 * \sigma'_v \quad (3.4)$$

Classification	Normalized undrained shear strength	Undrained shear strength
[-]	[kPa]	[kPa]
Organic clay (medium)	25	$c_{u,ref} = s_u = 2.8 + 0.22\sigma'_v$
Clay, slightly sandy(weak)	40	$c_{u,ref} = s_u = 2.8 + 0.37\sigma'_v$
Clay,slightly sandy (medium)	55	$c_{u,ref} = s_u = 2.8 + 0.52\sigma'_v$
Clay, slighlty sandy (dense)	80	$c_{u,ref} = s_u = 2.8 + 0.77\sigma'_v$

Table 3.2: Undrained shear strength equations according to Den Haan, 2011 [39]

The graph shows the agreement between all the methods aforementioned; the decision of continuing the calculations with Den Haan [39] formulae is due to its applicability for the soft Dutch soils - which is the current case - and the measurements consistency. Appendix F shows the table of values characteristic for the soil including the associated stiffness parameters. The analysis relies on this set of parameters representing the soil sub-layer located at a depth of 10m below surface.

Stiffness Stiffness plays an important role in dynamic analysis, hence the correct estimation becomes significant for evaluating the non-linear soil response. This sub-chapter presents two different methods of calculating the shear modulus - *empirical* and based on *measurements* - this way one can compare and validate the results.

Shear modulus determined empirically For the empirical determination of the stiffness G_{max} , a simple equation was used based on studies performed by Hardin and Black, 1968 [38]. The expression contains a void-ratio function together with a confining-stress function and it was developed mainly based on laboratory test results. The first

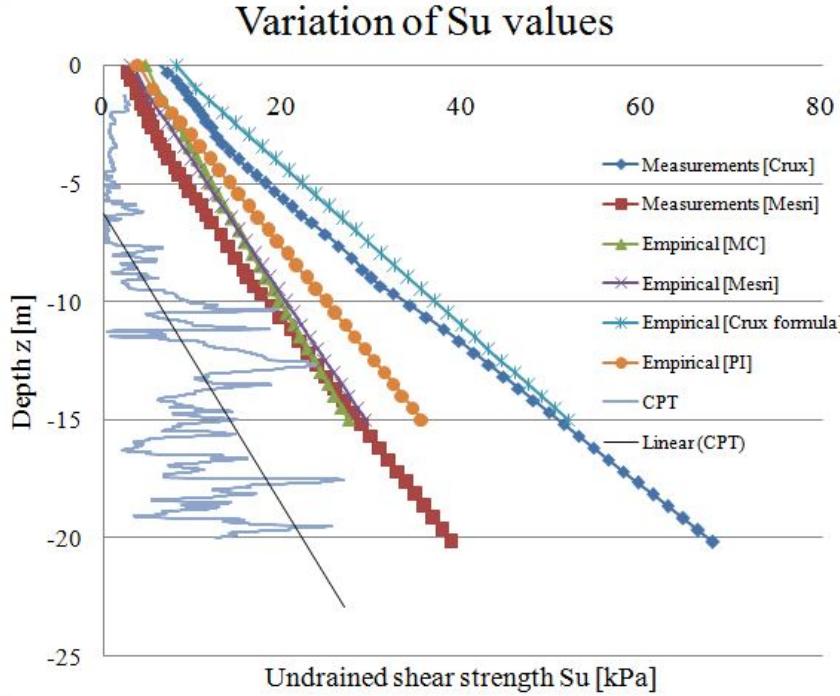


Figure 3.9: Various values of the undrained shear strength Su

function accounts for the plasticity index as well as the void ratio as an alternative to the overconsolidation ratio whilst the later considers the stresses developed within the soil. The equation described by the two authors can be written as:

$$G_{max} = C \frac{(2.973 - e)^2}{1 + e} OCR^K (p')^{0.5} \quad (3.5)$$

where e - void ratio; OCR - overconsolidation ratio p' - initial mean effective stress (kPa) K - coefficient which directly relates to the plasticity index Ip ; C - constant = 3.23 1/2

Thirty years later, after several refinements of the previous equation, Shibuya et al., 1997 [40] performed several tests in order to introduce a simplified void-ratio function using the specific volume. They avoided the sharp reduction of stiffness observed in Hardin & Black equation introducing a sounder physical parameter equivalent to the dry density; consequently, the formula becomes:

$$\frac{G_{max}}{p_r} = \frac{B}{(1 + e)^{2.4}} \left(\frac{p'}{p_r}\right)^{0.5} \quad (3.6)$$

where p_r - is the reference pressure, considered 1kPa; e - void ratio, p' - mean effective stress, factor B for soft clays ranged between [18000 - 30000] with an average of 24000, as it is proved in Shibuya et al, 1997 study.

Current soil investigation and laboratory tests aimed to determine several specific values, among them the void ratio; for a silty clay, medium weak, the results yield values between $e = 0.8 - 0.9$, while the plasticity index $Ip=25\%-30\%$. Given the fact that the reference pressure is 1kPa the ratio p'/p_r is equivalent to the value of the mean effective stress; this is determined based on the equations formerly described and varies along

the depth. Therefore, performing the calculation with the corresponding parameters, it results the equation for the G_{max} as it is shown:

$$G_{max} = [5400 - 5800](\sigma'_0)^{0.5} \quad (3.7)$$

Shear modulus determined based on available measurements On the other hand, the measurements give soil features in terms of shear wave velocity. In homogeneous and isotropic medium, there are two types of waves - pressure and shear waves. The shear wave velocity V_s is controlled by the shear modulus as it is shown:

$$V_s = \sqrt{\frac{G_0}{\rho}} \quad (3.8)$$

where G_o – shear modulus [kPa] ρ – the solid density [kg/m³]. $V_{s,30}$ is calculated as the time for a shear wave to travel from a depth of 30 m to the ground surface, and not as the arithmetic average of V_s to a depth of 30 m. There are various classification based on the soil type, one presented below corresponding to the normative Eurocode EN1998-1-1:cl3.1.2 including the ground types and the specific shear wave velocities:

Type of ground soil (EN1998-1-1,cl.3.1.2)				
Ground type	Description of stratigraphic profile	Parameters		
		$v_{s,30}$ (m/s)	N _{SPT} (blows/30cm)	c_u (kPa)
A	Rock or other rock-like geological formation, including at most 5 m of weaker material at the surface.	>800	-	-
B	Deposits of very dense sand, gravel, or very stiff clay, at least several tens of metres in thickness, characterised by a gradual increase of mechanical properties with depth.	360-800	>50	>250
C	Deep deposits of dense or medium dense sand, gravel or stiff clay with thickness from several tens to many hundreds of metres.	180-360	15-50	70-250
D	Deposits of loose-to-medium cohesion less soil (with or without some soft cohesive layers), or of predominantly soft-to-firm cohesive soil.	<180	<15	<70
E	A soil profile consisting of a surface alluvium layer with v_s values of type C or D and thickness varying between about 5 m and 20 m, underlain by stiffer material with $v_s > 800$ m/s.			
S ₁	Deposits consisting, or containing a layer at least 10 m thick, of soft clays/silts with a high plasticity index	<100 (indicative)	-	10-20
S ₂	Deposits of liquefiable soils, of sensitive clays, or any other soil profile not included in types A – E or S ₁			

Figure 3.10: Shear wave velocities according to the ground type [EN1998]

The current case deals with soft soil, henceforth the $V_{s,30}$ is assumed 180m/s –the real values determined from CPT tests and processed using Robertson's method seem to match the table previously presented. Appendix A shows an example of cone penetration test (CPT) results as well as a $V_{s,30}$ distribution along the soil layer measured at the specific site.

The G_0 is further derived from Vs as previously explained. The elastic moduli is related to the shear modulus through the Poisson ratio:

$$E' = 2G(1 + \nu') \quad (3.9)$$

The current analysis requires strength and stiffness parameters corresponding to undrained total stress analysis, therefore the formula described above will be converted accordingly:

$$E_u = \frac{3E'}{3 - (1 - 2\nu')} \quad (3.10)$$

$$\nu_u = \frac{3\nu' + (1 - 2\nu')B}{3\nu' + (1 - 2\nu')B} \quad (3.11)$$

The Poisson ratio for silty-clay in drained/effective analysis was considered $\nu' = 0.3$ whilst the undrained behaviour considers a value of 0.5 due to assumption of a fully saturated soil ($B=1$). For calculation purposes, this value will be altered to 0.48 to avoid a bulk density tending to infinity.

$$E = 2G(1 + \nu') \quad (3.12)$$

$$\nu_u = 0.5 \rightarrow G_u = 3E_u \quad (3.13)$$

$$\frac{E_u}{2(1 + \nu_u)} = \frac{E}{2(1 + \nu')}; E_u = \frac{3E'}{2(1 + \nu')} \quad (3.14)$$

Anastasopoulos et al, 2011 [9] use an empirical formulae (based on e.g., Hardin and Richart, 1963 [41]; Robertson and Campanella, 1983 [42]; Seed et al. 1986 [23]; Mayne and Rix 1993) for calculating the value of the small-strain Young's modulus as a function of the total overburden stress σ_y . $C = a\sigma_y$ with a ranging from 150 to 10.000 (for clays).

$$C = a\sigma_y \quad (3.15)$$

where C - initial hardening Young's modulus and σ_y corresponds to von Mises assumptions ($\sigma_y = \sqrt{3}S_u$) and a is a correlation factor with values between 150 and 1000 for clays, and 1000-10,000 for sands. So, the previous equations, if expressed in terms of Young's modulus at small strains and undrained shear strength, it will become:

$$E = a * S_u; a = [300 - 1800] \quad (3.16)$$

Appendix D presents both the tables containing the input parameters - from in-situ measurements and empirically determined. Nonetheless, differences appear due to several causes and assumptions but also because of the calculation methods. Few of the sources of dissimilarity are presented below:

1. measurements data presents a heterogeneous soil stratification consisting in silty clay at the upper part of the layer and potklei in the lower one whilst the empirical data accounts for a completely homogeneous layer.
2. he measurement related properties do not vary linearly along the depth in reality as it can be seen in figure 3.11 while empirical equations lead to a linearity between parameters; for instance, empirically determined stiffness G_0 is calculated combining the factor and the mean effective stress - which varies linearly with depth - thus the stiffness will result in a linearly distribution as well. Measurements do not display the same fashion given the Vs variation with depth.

3. empirical data works with factors determined for a specific type of soil - for the simplicity of the calculation, many assumptions lead to the selection of such factors that can over or underestimate reality.
4. the shear wave velocity V_s represents only an approximate of the entire region. Different results can be obtained in the vicinity of the actual measurements. However, its measurements offers a powerful tool for establishing the soil stiffness properties.

Such dissimilarities are clearly expected, the main interest in this situation pointing the correspondence between values; it was opted to continue the calculations using the empirical values for various reasons; one of them being represented by the future analysis, site response analysis, in combination with the software requirements - the model definition in Abaqus for a multi-layered material entails a subroutine that relates different parameters. For the current application, the connection between the parameters introduced within the subroutine refers to the correspondence between the Young's modulus and the undrained shear strength. This subject will be explained in more detail in the next chapter within the material definition part.

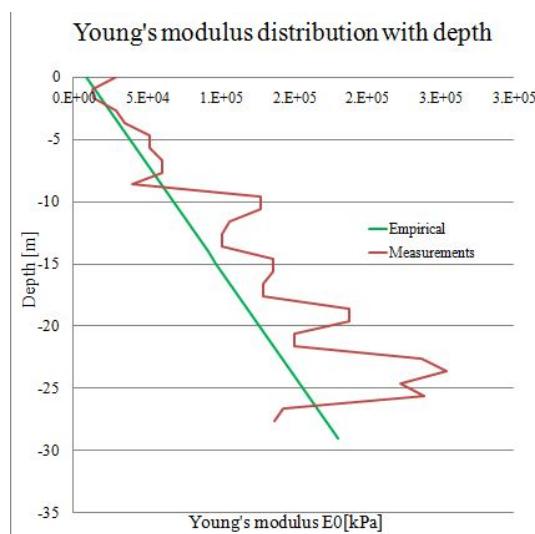


Figure 3.11: Young's modulus - Comparison between empirical and measurement data

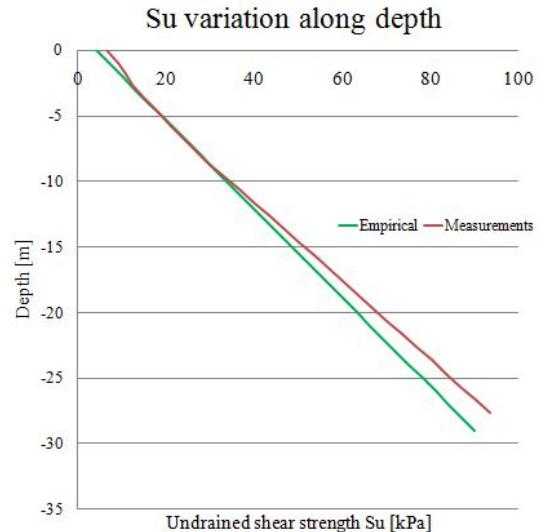


Figure 3.12: Undrained shear strength - Comparison between empirical and measurement data

3.4.2 Non-linear parameters (kinematic hardening model with Von Mises failure criterion)

The constitutive model marks down to several equations which describe the inelastic soil response. As a matter of fact, the software Abaqus only requires the selection of the appropriate material module which nominates the failure criterion and its corresponding parameters; the current case deals with only three parameters momentarily: the maximum stress at zero plastic strain - σ_0 , elastic Young's modulus $E = 2 * (1 + \nu)G_0$ and the ultimate strength σ_u or S_u . The evolution of kinematic hardening component of the yield stress is defined by:

$$\dot{\alpha} = C \frac{1}{\sigma_0} (\sigma - \alpha) \dot{\epsilon}^{pl} - \gamma \alpha \dot{\epsilon}^{pl} \quad (3.17)$$

where

- C - the initial kinematic hardening modulus represented by Young's modulus at small strains;
- K - parameter determining the rate of decrease of kinematic hardening with increasing plastic deformation;
- α - backstress;
- $\dot{\epsilon}^{pl}$ - plastic strain rate;

For clays, the following equation describes the maximum yield stress σ_y :

$$\sigma_y = \sqrt{3}S_u \quad (3.18)$$

$$K = \frac{C}{\sqrt{3}S_u - \sigma_0} \quad (3.19)$$

The yield stress at zero plastic strain σ_0 controls the initiation of inelastic behaviour and it is defined as it results:

$$\sigma_0 = \frac{G_{max}}{\gamma_{el}} \quad (3.20)$$

The shear modulus was derived previously from the Vs values measured by CPT, as well as all other stiffness parameters. The elastic limit strain represents the point in which the plasticity is triggered - here was taken into calculation as 10^{-4} . Hence all the kinematic parameters are further obtained based on this value and it can be seen in Appendix F.

3.5 Results

3.5.1 General

The connection between the stress-strain plot and modulus reduction curves is straightforward for two-way cyclic loading (complete stress cycle). The set-up of the normalized stiffness degradation curve allows the prediction of stress-strain path of the soil subjected to monotonic loading. The analysis starts by creating several jobs in which the strain amplitude varied its values between $\gamma = 0.1\% - 10^{-5}\%$. From each analysis the stress-strain paths are extracted and plotted leading to different curves also known as hysteresis loops. The secant shear modulus is further calculated as:

$$G = \frac{\tau}{\gamma} \quad (3.21)$$

All the shear modulus values are then collected within a table which will serve for the construction of the normalized modulus degradation curve. The small-strain shear modulus G_{max} can be determined based on elastic Young's modulus, E_0 , and it serves for the normalization of the obtain shear moduli.

$$G_{max} = G_0 = \frac{E_0}{2(1 + \nu)} \quad (3.22)$$

An example of the applied amplitude can be observed in Figure 3.13. The current model includes a maximum amplitude of $A_{max} = 1$, a period $T = 0.3s$ and a period shift of zero seconds. Each set of calculation will apply the shear strain value to this harmonic signal leading to the cyclic effect.

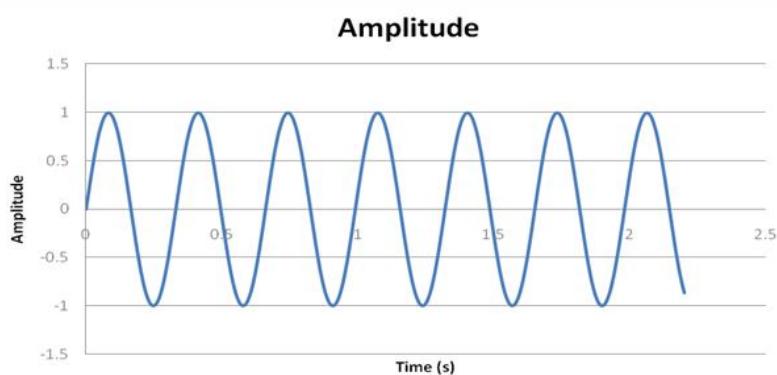


Figure 3.13: Input cyclic signal

Such inelastic response proves to be not that sensitive to the frequency of the signal but to the maximum recorded amplitude as Gazetas, 2004 [6] shows in his study of foundation rocking and uplifting. Indeed, models showed that the same cyclic response is obtained when varying the amplitude frequency. The degradation curve is then composed by the normalization of the secant stiffness displayed by each analysis, G , with the maximum shear stiffness value corresponding to the sample, G_{max} . Meanwhile, the damping ratio is expressed as the ratio between the dissipated energy and stored strain energy in one complete and stable cycle of motion. Based on Figure 3.14, the dissipated energy A_L

is described by the area inside the loop and it is calculated using the integral of the stress-strain curve as it follows:

$$A_L = \int \tau d\gamma \quad (3.23)$$

while the stored strain energy A_T is expressed as:

$$A_T = \frac{\tau\gamma}{2} \quad (3.24)$$

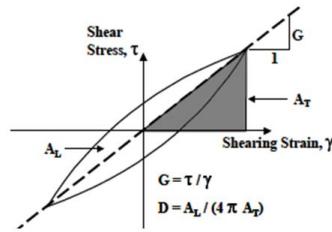


Figure 3.14: Calculation of damping ratio using a hysteresis loop

3.5.2 Parameters that influence the soil response

The influence of the sample location within the layer on the inelastic response was investigated. Each analysis consisted in a different set of input parameters yielding the elasto-plastic response for different positions. The table below shows the data used for calculation and the variation in parameters followed by a plot that helps visualizing the results.

Sample depth	Confinement stress	Young's modulus	Undrained shear strength	Stress at zero plastic strain	Hardening parameter
z[m]	F [kPa]	C=E [MPa]	S _u [kPa]	σ ₀ [kPa]	K [-]
1	20	12.5	8.61	0.61	1283
5	50	38.2	19.09	3.30	1283
13	100	85.5	42.76	7.41	1283
15	150	97.4	48.68	8.43	1283
20	230	126.9	63.5	11.0	1283

Table 3.3: Data for various sample location within the layer

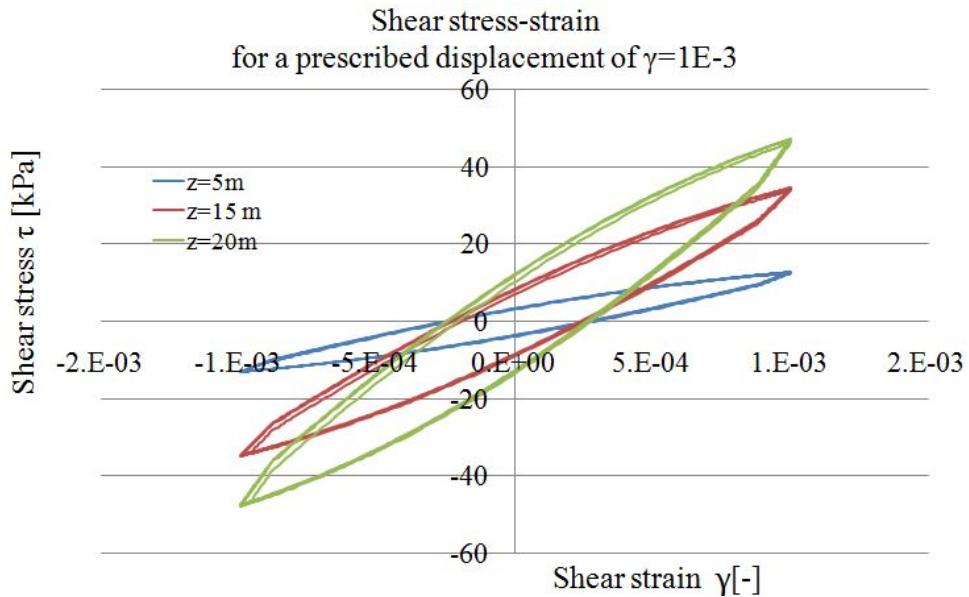


Figure 3.15: Various responses according to the depth

Figure 3.15 displays the difference in response for three locations of the sample; nonetheless, the stiffness plays an important part as well as the undrained shear strength. The three loops correspond to different stress levels, thus different amounts of dissipated energy. Important to mention that the maximum shear stress associated to each loop matches the undrained shear strength ($\tau_{max} = S_u$), validating the undrained conditions and the analysis itself. The breadth of the loops expands with the energy dissipated whilst the inclination tends towards the vertical axis as the level reaches the soil base because the shear strength increases as well.

The parametric study continued with the variation of the prescribed displacement or the shear strain at which the plastic response is triggered. Darendeli results display the plasticity being activated at a strain level of $10^{-5}\%$; the current analysis shows a better agreement when using a prescribed displacement of $10^{-4}\%$ than the lower one. This decides that the calculation should continue with the aforementioned value in order to get comparable results with Darendeli ones.

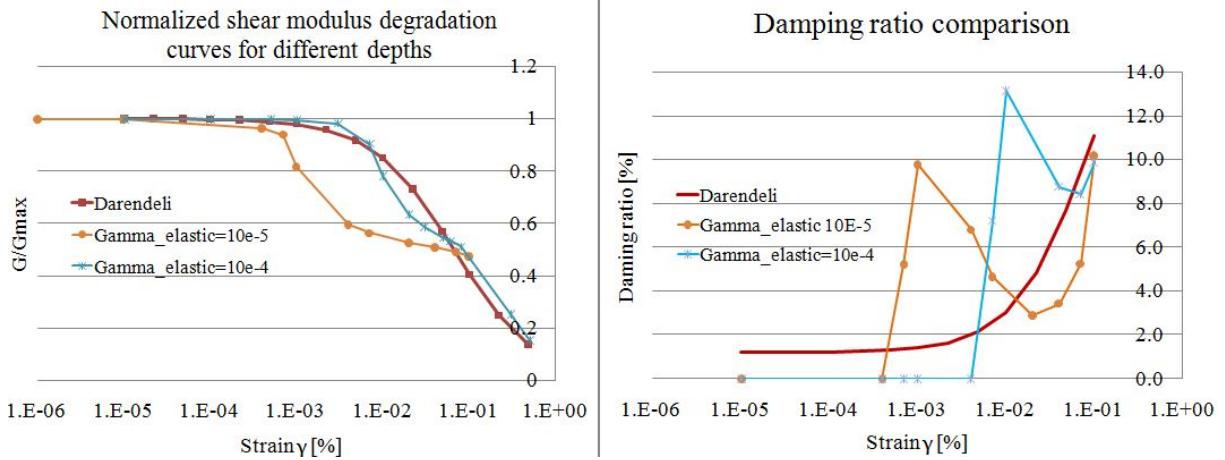


Figure 3.16: Normalized stiffness degradation curves for various plastic strains

3.5.3 Validation - Comparison with Darendeli curves

The comparison shows a relatively good agreement between the current results and Darendeli data. Few remarks can be stated regarding the obtained values. First, the increase in stiffness can be observed from the first plot with increasing depth. Plasticity is triggered earlier around surface level compared to deeper layers.

The damping ratio might seem not to follow the exact same shape as Darendeli; important to mention that the current case ignores several features which the author included within his calculation. First, there is no additional damping introduced in the analysis; Rayleigh damping parameters were not comprised but they will in the future calculation. This explains the zero damping values once the elastic domain is active - meanwhile Darendeli results still show damping at that strain level. Moreover, Darendeli assumes that damping for any given strain level is a function of the curvature coefficient - which is also neglected in the current analysis. Also, Darendeli scales the results with several coefficients (such as curvature coefficient, scaling coefficient) together with the D_{min} in order to get a better match between experimental data and empirically obtained results.

Additionally, studies (Pisanò et al, 2014 [43]) investigated a comparable simulation on a elastic-plastic model on two Drucker-Prager material models (including kinematic hardening) and obtained similar trends in the damping curves as it can be seen Figure 3.17. Which hints that the obtained output might not necessarily be incorrect, possible numerical errors or conditions have an impact and flaws can occur materialize.

Given these, it can be concluded that the current results match to a certain extent Darendeli's curves and that a good calibration of the one element shear test was obtained.

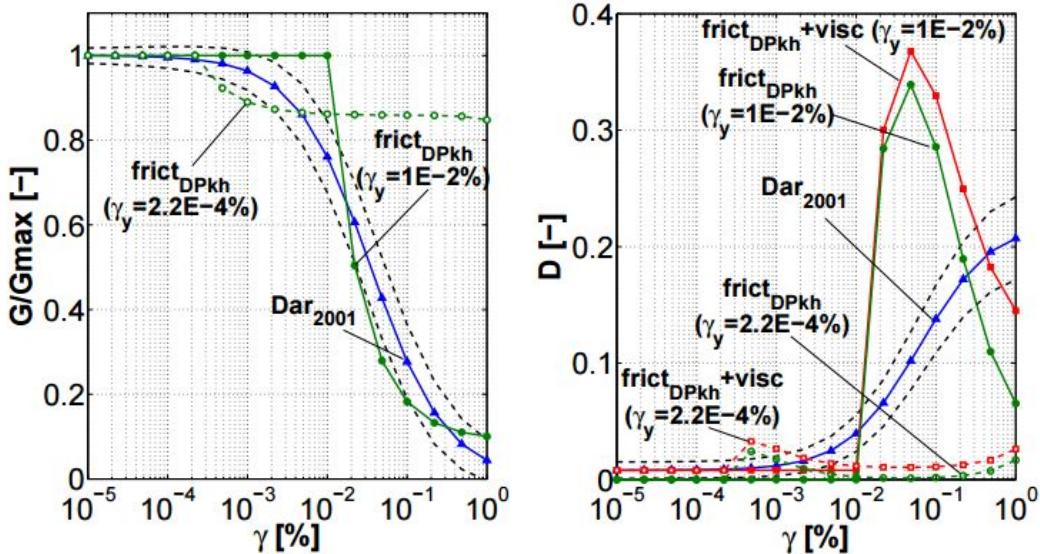


Figure 3.17: Comparison of a Drucker-Prager kinematic hardening bounding surface model (DPbs) with vanishing elastic region with Darendeli at $p_0 = 1\text{atm}$

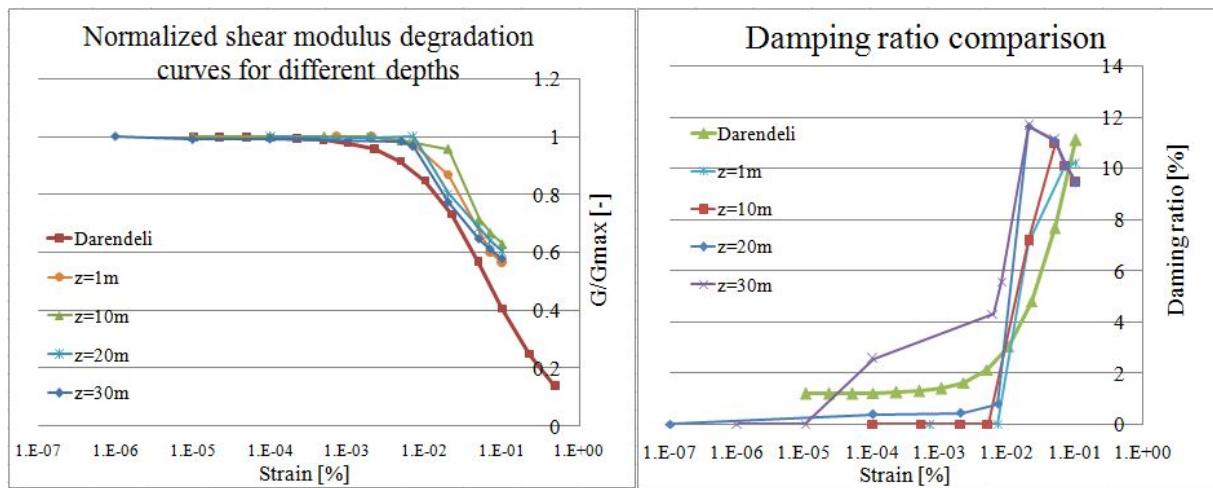


Figure 3.18: Normalized stiffness degradation (right) and material damping curves for various sample locations

3.6 Conclusions

A strain-controlled numerical test was performed on a simple element assigned with properties of different clay samples located across the depth of a homogeneous layer. The aim of the study strived to generate normalized stiffness degradation and material damping curves similar to the ones provided by Darendeli's, 2001 [12]. They represent a reference standard in this domain, based on a 4-parameters mathematical model that describes the behaviour of a soil specimen when subjected to shear cyclic loading. It is suitable for dynamic problems that assist shear wave propagation - which is also the current case.

Despite the lack of damping characteristics and coefficients that guarantee a smooth transition along the curvature, the model succeeds in generating normalized modulus reduction curves and material damping with a decent degree of accuracy when examining in contrast with Darendeli's set of curves.

It can be concluded that the proposed material model qualifies as reasonable for the future examination and, thus, the current paper continues the research towards a one-dimensional site response analysis.

Chapter 4

Site Response Analysis

4.1 Introduction

The seismic waves generated at the bedrock suffer variation until they reach the surface; both the characteristics of the ground shaking as well as the material parameters influence the ground response that can be expressed in terms of amplitude, duration and frequency content. The importance of the ground response analysis relates to the overall dynamic study of the superstructure; the seismic waves can experience amplification or de-amplification at surface level as a function of soil damping properties together with encountered frequencies. In the case of matching frequencies between the maximum amplification of ground motion and natural frequency of the structure, the two elements (soil and construction) resonate one with the other. This translates into high oscillating amplitudes and thus, considerable damage.

In conclusion, performing a site response analysis enables the engineers to predict the site frequency content, the spectral acceleration alongside to peak ground acceleration and thus to create a reliable seismic design. For the current study, the Site Response Analysis is performed in the interest of attaining results that support the next analysis step: the soil-structure interaction.

4.2 Model description

The model represents an extrapolation of the previous analysis step; the soil sample becomes a homogeneous layer with properties increasing linearly with depth and it is subjected to two steps: *the gravity* and *the seismic excitation*. Given the lack of bedrock in reality and for the simplicity of calculation, the bedrock is assumed to be located at 30m below surface. In order to simulate a one dimensional analysis, the problem is analysed in a 2D space plane strain ($\epsilon_{zz} = 0$) with the lateral width of the soil relatively small compared to the height; the presence of bedrock is numerically equivalent to a rigid base having translational constraints in both directions. Each pair of horizontal nodes are tied together such that will experience equal displacements. Figure shows the schematization of the problem, the blue numbers representing the nodes, the red numbers the elements, respectively. The 1D soil column serves as the typical model for a site response analysis as the shear wave propagation direction is assumed to be vertical - thus the main interest relates to the soil performance when experiencing vertically travelling seismic waves.

The validation of the model will consists of results comparison between the analysis performed in Abaqus and the ones in NERA together with the SRA performed by ARUP

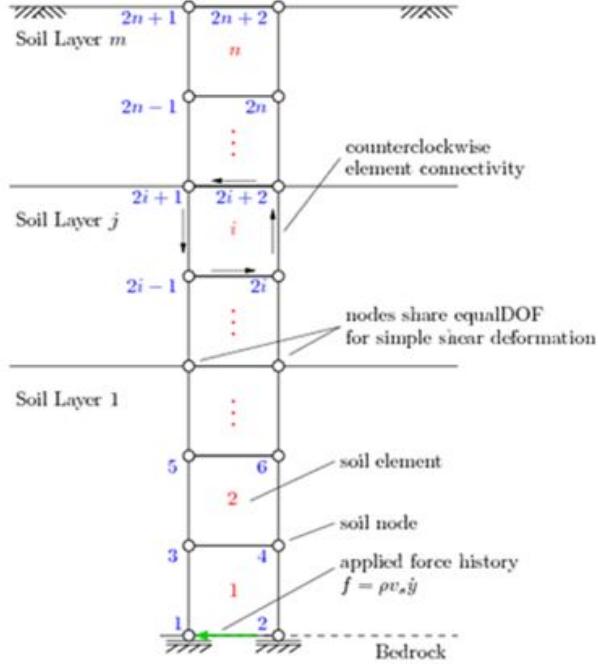


Figure 4.1: Schematization of soil column

for Groningen site - the latter only offers a rough guide. The differences between the means of analysis will be investigated, the outcome will be expressed in terms of acceleration response in frequency domain together with stiffness degradation.

4.2.1 Steps of analysis

Geostatic The first step of the analysis simulates the natural stress state within the soil using a gravity load spread all over the layer and it is declared as static, general. The self weight of the elements provide the loads, therefore no need of extra loading conditions. The definition of the gravity load involves the software in updating several parameters to account for the confining pressure. As the schematization shows, the model contains elements and nodes - the nodes will be assigned with boundary conditions reproducing the one dimensional vertical propagation of the shear waves. The base nodes are constrained in both directions in accordance with the assumption of the bedrock presence underneath the soil layer whilst each pair of nodes horizontally displayed are linked using a feature called multi-point constraint - this provides a pinned joint between the nodes making the global displacements be equal while leaving the rotations independent.

Dynamic The second step represents the soil medium subjected to the earthquake motion; it is defined as dynamic step using an implicit integration scheme which will be explained in more detail later on. During the step, the user propagates the boundary conditions aforementioned with the exception of the horizontal base constraint; it is replaced by an acceleration type of boundary condition that is assigned with an amplitude curve - this allows the user to define an arbitrary variation in time (or frequency) of any quantity or can be defined as a mathematical function (e.g. sinusoidal), series of values in time (acceleration history) and many more. For the current study, the amplitude curve contained the acceleration-time record for a period of 10 seconds as 4.2 shows; this pe-

riod is considered as the representative duration of Groningen acceleration measured time history and it starts right before the peak acceleration [44]. Although the acceleration record was implemented in the analysis as an amplitude and further assigned to an angular/acceleration boundary condition, Abaqus converts it into a relative force-time history acting on the model.

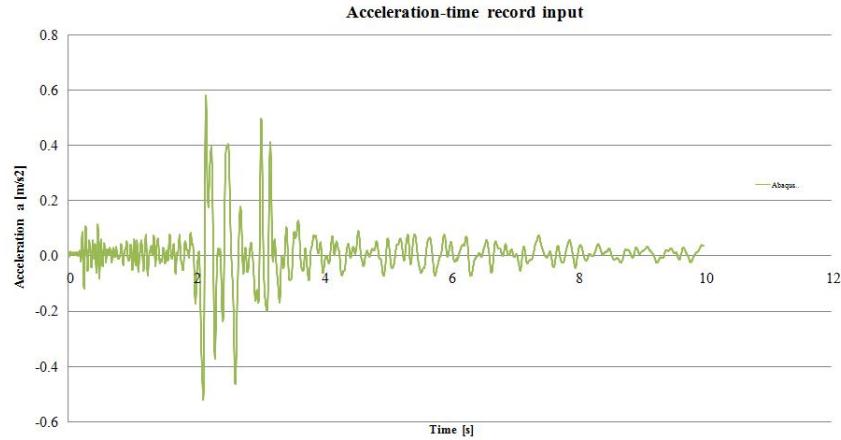


Figure 4.2: Acceleration input (induced earthquake, WSE station, Huizige, Groningen, 16 Aug 2012)

4.2.2 Input parameters

The material parameters, as presented in Chapter 3 and Appendix B, can be divided into several categories the software requires:

1. *Elastic* again, Young's modulus together with Poisson's ratio becomes sufficient for the definition of elastic domain.
2. *Plastic* the nonlinear isotropic/kinematic model applies von Mises failure criterion for which three parameters are required: yield stress at zero plastic strain σ_0 , small-strain Young's modulus C and hardening parameter K .
3. *Density* - the soil layer is considered to be homogeneous, thus one single material is defined. So density for a silty-clay medium was considered 1800kg/m³
4. *Damping* - the software offers many damping options [from numerical to material damping]; however, for this example the Rayleigh damping parameters α and β are sufficient for the scope of analysis. This matter will be discussed later on.

In addition, the model contains a subroutine which introduces the values of undrained shear strength as a function of the vertical effective stress as well as the correlation of this parameter with Young's modulus. The benefits of using a subroutine relate the expansion of the standard input parameter set by inserting field variables at material points as functions of time or of any material quantity. Moreover, it links the field variables with solution-dependent material properties, values being updated at the start of each increment through interpolation; an average value is used for linear elements; an approximate linear variation is used for quadratic elements. The routine allows the user to access quantities at material points and manipulate them according to the desired application.

Appendix G shows the flow chart of Abaqus user defined subroutine whilst Appendix H shows the routine created for these calculations. The input parameters are calculated as presented in the previous chapter (see Chapter 3 and Appendix F).

4.2.3 Rayleigh coefficients

The dissipative character of the elasto-plastic material can be better enhanced by introducing a viscous damping mechanism. The overall stress state of the soil skeleton can be separated into two parts:

- *frictional component*- relating to the elasto-plastic behaviour, being displacement proportional
- *viscous component* - relating to the Rayleigh damping coefficients, being velocity proportional.

The advantage of coupling these two terms refers to the smoothing of the shear stress-strain cycles as well as a higher material damping. The viscous component has a favourable effect on the damping curves for small-strain domain; whilst it leads to an overestimation for large-strains. As mentioned previously, the second step of the analysis, and the most important, is declared as dynamic, implicit. In non-linear analysis, the dynamic equation of motion is:

$$[M] \Delta \ddot{u} + [C] \Delta \dot{u} + [K] \Delta u = - [M] I \Delta \ddot{u}_g \quad (4.1)$$

where $[M]$ - mass matrix, $[C]$ - viscous damping matrix, $[K]$ - stiffness matrix, $\Delta\ddot{u}$, $\Delta\dot{u}$ and Δu - vectors of nodal relative acceleration, velocity and displacement, $\Delta\ddot{u}_g$ - acceleration at the base and I - unit vector. The matrices are compiled based on the incremental response recorded within the software analysis. The equation is solved at every incremental time step using the Newmark [45] method.

The viscous damping matrix follows Rayleigh and Lindsay, 1976 [46] equation that relates the small strain damping to both mass and stiffness matrices. Thus, the equation for the viscous damping is:

$$[C] = \alpha [M] + \beta [K] \quad (4.2)$$

where

$$\xi = \frac{1}{2}(\beta\omega + \frac{\alpha}{\omega}) \quad (4.3)$$

α and β are determined by choosing fractions of the critical damping ξ_{crit} . Assuming two different circular frequencies ω_1 and ω_2 with the corresponding damping ratios ξ_1 and ξ_2 , the two parameters become:

$$\alpha = \frac{2\omega_1\omega_2(\xi_1\omega_2 - \xi_2\omega_1)}{\omega_2^2 - \omega_1^2} \quad (4.4)$$

$$\beta = \frac{2(\xi_1\omega_2 - \xi_2\omega_1)}{\pi(\omega_2^2 - \omega_1^2)} \quad (4.5)$$

Small strain viscous damping effects are assumed proportional only to the stiffness of the soil layers because the soil medium is regarded as relatively short, thus the contribution of higher modes becomes negligible. Additionally, for cases with low frequencies, the ω_1 is the related to the first natural mode while the second relevant mode can be considered zero (and $\omega_2 = 0$). Thus, α parameter is set to zero, whilst β yields:

$$\beta = 2\frac{\xi}{\omega_1} \quad (4.6)$$

ξ is the damping ratio at small strain; for this application $\xi=1.2$ corresponding to Darendeli's results; while ω_1 is the natural circular frequency at first natural mode;

Despite that the experimental results prove that the damping matrix $[C]$ is frequency independent and it has a constant value, Park and Hashash, 2002 [47] show the correlation between the stiffness $[K]$ and the damping $[C]$. Since the stiffness depends on the strain level, then it can be concluded that the damping is also strain dependent, including the natural frequency. Thus, the viscous damping matrix $[C]$ is updated at each time increment as well as the stiffness. Kramer, 1996 [48] proposes an equation for the calculation of the period of vibration that corresponds to the fundamental frequency of the selected mode as it follows:

$$T_n = (2n - 1)\frac{\bar{V}_s}{4H} \longrightarrow T_n = \frac{V_s}{4H}. \quad (4.7)$$

where \bar{V}_s average shear wave velocity and H = layer height.

Further, the natural circular frequency is obtained through the following transformation:

$$\omega_n = \frac{2\pi}{T_n} \rightarrow \omega_1 = \pi \frac{V_s}{2H} \quad (4.8)$$

And finally, Rayleigh β damping parameter becomes:

$$\beta = \frac{2H\xi}{V_s\pi} \quad (4.9)$$

ξ	1.2	%	Darendeli damping ratio
T_n	$4H/V_s$	sec	Fundamental period
V_s	132	m/s	Average shear wave velocity
H	30	meters	Layer depth
ω	6.91	$Hz(sec^{-1})$	Fundamental frequency
β	0.001736	sec	Rayleigh β coefficient

Table 4.1: Calculation of Rayleigh β parameter

4.2.4 Integration scheme

It is important to understand the type of nonlinear analysis the software was opted to perform and its influence of the results. For this particular analysis, an implicit direct integration scheme was selected - this means that the set of nonlinear equations of motion solved at the time step Δt_{n+1} are employed to compute the transition from the state at t_n to t_{n+1} ; on the other hand, an explicit integration uses all information at the beginning of t_n to estimate the latter state at t_{n+1} .

Abaqus/Standard uses the Hilber-Hughes-Taylor time integration method [49] which is an extension of the Newmark β method, 1959 [45]. Basically it controls the numerical damping within the system which might rise due to the energy dissipation mechanisms associated with different operator types. More details related to Newmark integration method are presented in Appendix I.

4.2.5 FEM stability

According to Jeremić, [50], the accuracy of such nonlinear problem dealing with wave propagation is controlled by two factors - node spacing in the FE model Δh and the time step δt . The spacing is directly related to the wavelength whilst the time step depends on the fundamental period of the system.

$$\Delta h \leq \frac{\lambda_{min}}{10} = \frac{1}{10} \frac{v}{f_{max}} \quad (4.10)$$

$$\Delta t = \frac{T_n}{10} \quad (4.11)$$

More details regarding the calculation of the two stability criterion are presented within Appendix J

4.2.6 Mesh

For the meshing part, structured four-node continuum elements (*CPE4*) are used to model the soil using the plane strain formulation of the quad-element. The element connectivity uses a counterclockwise pattern for the previously-described node numbering scheme (see

??). The soil elements in each layer are assigned the material tag corresponding to that layer. A unit thickness is used in all examples for simulating the 1D condition. The self-weight of the soil is considered as a body force acting on each element. The body force is set as the unit weight of the soil in each layer, which is determined from the respective mass density input value.

4.3 NERA - Non-linear Earthquake Site Response

An additional analysis was performed using NERA (Nonlinear Earthquake site Response Analyses) [51] computer program in order to have a better grasp of the whole concept as well as a meaningful comparison. It derives from EERA that uses an equivalent linear model to investigate the same problem; the constitutive material model is proposed by Iwan and Mroz, 1967 [24] and it describes the nonlinear kinematic model as a series of n mechanical elements, each displaying different stiffness k_i and sliding resistance R_i as it is shown in Figure 4.3. More details concerning the calibration NERA performs are presented in Appendix K.

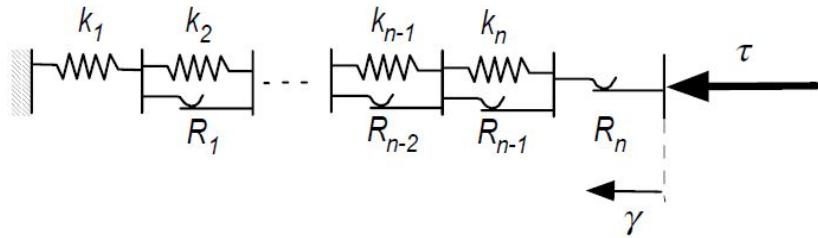


Figure 4.3: Plasticity description of Iwan and Mroz nonlinear model

NERA is composed by a FORTRAN 90 code together with a Excel plug-in that capture the nonlinear site response of a layered soil column subjected to an earthquake signal. As input, it requires the acceleration-time record, elastic material properties with emphasis on the stiffness parameters - normalized stiffness degradation and material damping curves.

The material properties introduced within the software require a general description of the soil medium as well as an individual material classification (in case the user is dealing with a multi-layered ground). The general input portrays the column with its sub-layers and unit weights, shear wave velocities and the ground water table followed by an automatic assessment of the maximum shear modulus, effective stresses and fundamental period. One example of input parameters can be seen in Appendix L.

The software allows for multiple layer definition together with the normalized shear modulus degradation curves and material damping curves. One example of output can be seen in Appendix... For this particular case, Darendeli's results presented previously were used in order to obtain a consequent comparison. In the end, the two numerical analyses (ABAQUS and NERA) aim towards the same goal; thus, the standard normalized set of curves proposed by Darendeli serves as benchmark for non-linear behaviour. However, the software does not account for data corresponding to damping curves as it is calculating its own set of values. This is because the nonlinear model proposed by Iwan and Mroz uses a different scheme for determining the damping characteristics.

NERA starts the analysis by processing the earthquake input signal and material properties followed by step-by-step determination of the relative velocity and displacement at a selected sub-layer. The integration scheme NERA uses is the central difference which, contrary to Abaqus analysis, it is conditionally stable (the time step size is limited). This calculation method is a particular type of Newmark method in which the predicted velocity is:

$$\tilde{v}_{i,n+1} = v_{i,n} + \frac{1}{2}a_{i,n}\Delta t \quad (4.12)$$

The stress and strains are calculated at each node from nodal displacements, next step calculates the velocity from the input acceleration history. Subsequently, the predicted values for velocities at time t_{n+1} yield from those determined at time t_n and finally the nodal displacements, velocities and accelerations are update at each node i. In addition, the output includes spectral response based on Fourier transform calculation for any selected sub-layer.

4.4 Results

This subchapter presents the results obtained from the site response analysis performed in Abaqus, followed by a comparison with NERA outcome; several plots are used as mean of verification and the main interest lies on the G/G_{max} and damping curves, acceleration response as well as the amplification ratio in frequency domain.

After performing a dynamic, implicit type of analysis to the assembly described previously, the output was investigated with an initial emphasis on the stiffness degradation. To check the validity of the overall model, an uniform cyclic signal served as acceleration amplitude; a circular frequency $f = 1Hz$ was applied at the bottom of the model for a period of 10 seconds in a sinusoidal fashion. Such uniform harmonic loading represents a simplification of the signal, and helps the user better understand the non-linear soil response. A real acceleration-time history consists in many irregularities and the results may be sometimes misinterpreted. That is why the investigation starts simple towards complicated.

The results can be visualized in figures 4.4, 4.5 and 4.6. The same remarks can be made as for the preceding analysis (see previous analysis in Chapter 3); however, this model includes an additional Rayleigh damping parameter together with the subroutine that updates the values of the Young's modulus as a function of the undrained shear strength and effective stresses, respectively. The acceleration response displays a de-amplification of the bottom signal together with damping effects visible in the irregularities of the curves; the de-amplification effect can be seen as the average wave speed decreases (blue line wave travels with 0.5m/s whilst the green line with almost half the speed). The values are obtained by dividing the maximum acceleration to the time period of a complete sinusoidal cycle. The shear stress-strain plots show plasticity occurring at different stress levels - the hysteresis loops shift towards origin which means that the soil achieves plasticity gradually together with residual plasticity. Additionally, the plots show a decrease in dissipated energy as the seismic waves travels from bottom to top - the area comprised within the hysteresis loops reduces as well, which comes in conformity with the conclusions of the previous chapter (see Chapter 3)

Once the validation of this simplistic model is achieved, the real acceleration-time history is applied to the boundary condition at the bottom nodes for the same period of

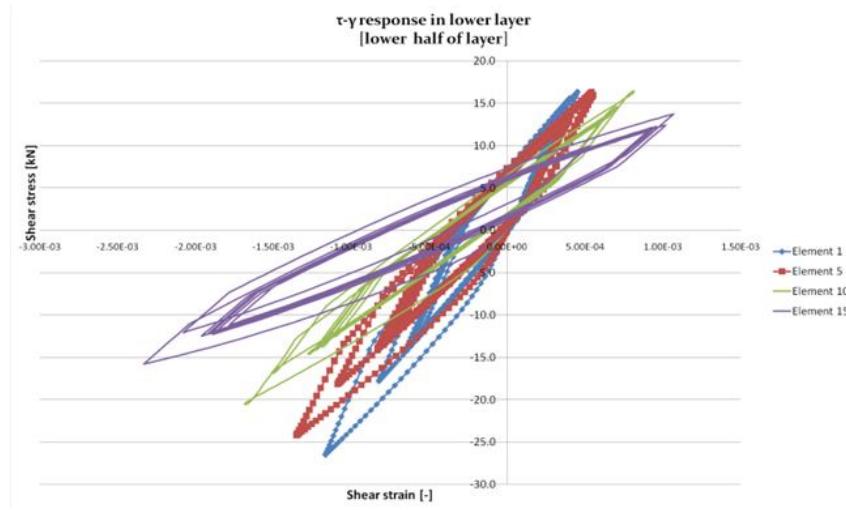


Figure 4.4: Hysteresis loops on the lower half of the soil layer (Element 1 - Base; Element 15 - Middle of the layer)

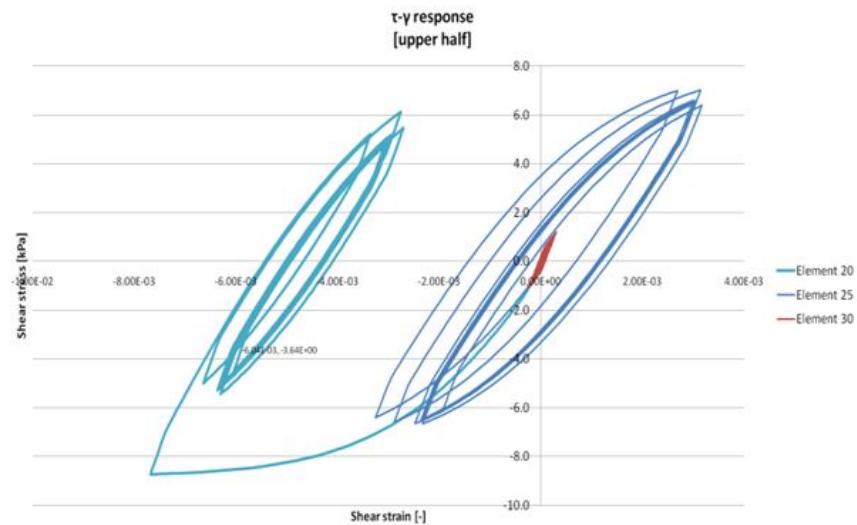


Figure 4.5: Hysteresis loops for lower half of the soil layer (Element 1 - Base; Element 31 - Surface)

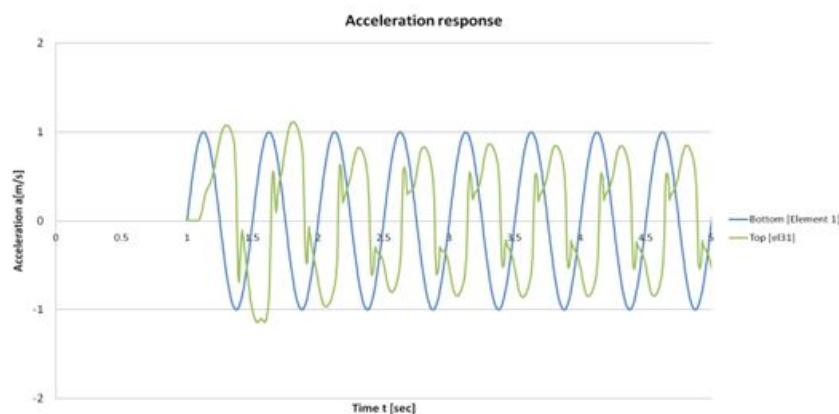


Figure 4.6: Acceleration response (surface and bottom)

10 seconds. The records correspond to the measurements from WSE station, Huizinge, Groningen [1]. Even though the earthquake signal lasts for 35 seconds, it was trimmed to incorporate the most unfavourable 10 seconds [with the highest acceleration peak] which, according to ARUP [52], are appointed as the representative duration of Groningen acceleration measured time history starting just before the peak acceleration. The obtained values in terms of shear stress and strain can be seen in Figure 4.7 whilst the top and bottom acceleration outcome is represented in Figure 4.8. Important to mention is that the boundary condition applied at the bottom of the model simulates the bedrock presence, therefore the waves are incident and not reflective - the discussion about the boundary conditions influence on the wave propagation shall be presented shortly after.

Note: As a sign convention, element 1 represents the bottom one whilst element 30 is the surface.

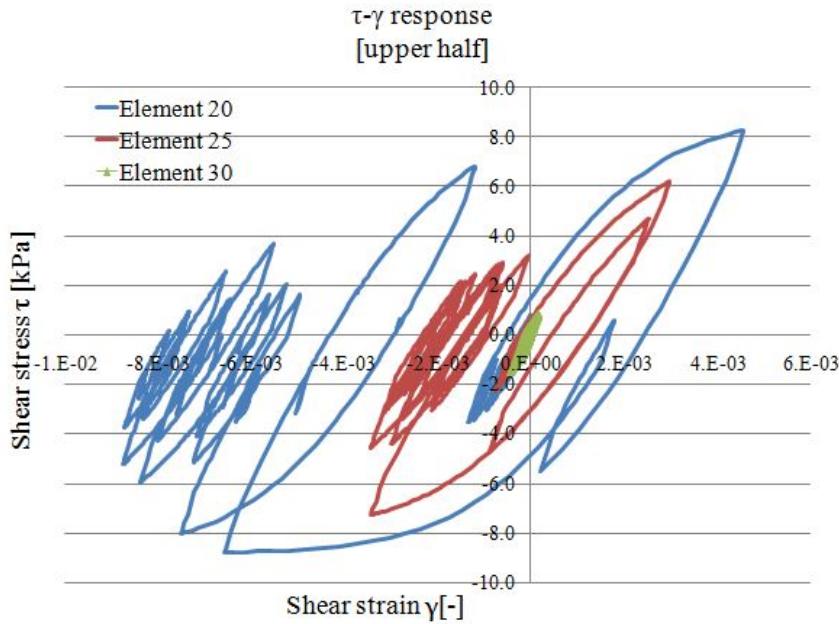


Figure 4.7: Hysteresis loops for upper half of the layer when real acceleration is applied

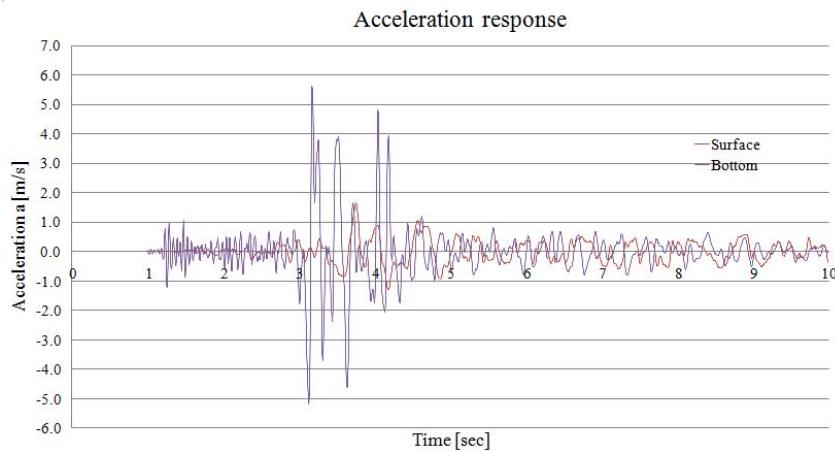


Figure 4.8: Acceleration response - surface and bottom

Once the bottom and top acceleration outcome is extracted from the software, a Fast

Fourier transform is applied with the scope of converting the current data from time domain to a representation in frequency domain. As Kristeková et al., 2006 [53] stated "the most complete and informative characterization of a signal can be obtained by its decomposition in the time-frequency plane". However, FFT is used as a digital signal processing tool that aids other operation, rather than providing a final result itself. For example, the transfer function or a site amplification factor allows the calculation of the motion of any layer i based on other motion (of any layer j). This transfer function relates the displacement at position i to that at position j as it follows:

$$F_{ij} = \frac{|u_i|}{|u_j|} \quad (4.13)$$

The Fourier spectrum represents the distribution of energy in the ground motion for a frequency interval $[0 \leq f \leq 1/2\Delta t]$. The amplification factor can also be written as:

$$A(f) = \frac{F_{a,site}(f)}{F_{a,bedrock}(f)} \quad (4.14)$$

where $A(f)$ - site amplification factor; $F_{a,site}(f)$ and $F_{a,bedrock}(f)$ - Fourier amplitudes of ground acceleration at surface and bedrock, respectively calculated as the vector sum of the two horizontal components. The importance of the site amplification factor relates to the structural damage pattern (rather than the PGA amplification) due to site effects. If the natural period of the structure matches the soil natural period, the structure will be more vulnerable to earthquakes.

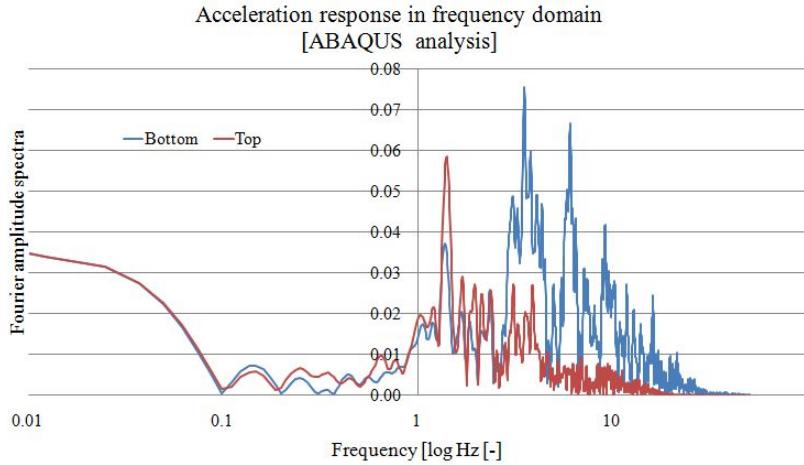


Figure 4.9: Fourier amplitude spectra - surface and bottom

It is important to discuss the boundary conditions and their influence on the wave transmission throughout the layer. The current model created in Abaqus includes tied boundaries, also described by Zienkiewicz et al. (1989) [54] and it assumes that all displacements on the left side of the column correspond to the ones at the right side, simulating a free field boundaries, whereas the bottom nodes do not absorb the oscillating waves. The software offers the baseline correction option for the acceleration input for time domain analysis; the practice is proposed by Newmark [45] and it introduces an additional correction to the acceleration such that the mean square velocity over the event time is minimized. The use of more correction intervals provides tighter control over any "drift"

in the displacement at the expense of more modification of the given acceleration trace. However, in acceleration history it does not show large difference between the responses.

Because the boundary will transmit the waves only upwards, an additional analysis was performed with a bottom acceleration record manually reduced by half. Physically, the waves within a soil have both downwards and upwards motion (incident and reflective). The decision of applying half of the signal also relates to NERA procedure as it assumes that the velocity at base is the sum of both incident and reflected waves and since at bedrock level shear force is zero it yields that the velocity becomes:

$$v_{base} = 2v_{incident} \quad (4.15)$$

4.5 Comparison Abaqus vs NERA

The comparison between the two analyses were formulated in terms of acceleration response, shear stress-strain response together with the spectral ratio and the plots can be visualized below.

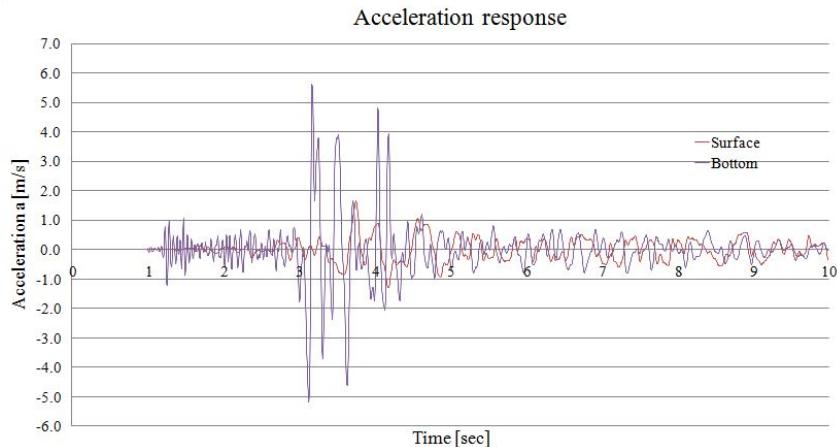


Figure 4.10: Acceleration comparison Abaqus vs. NERA

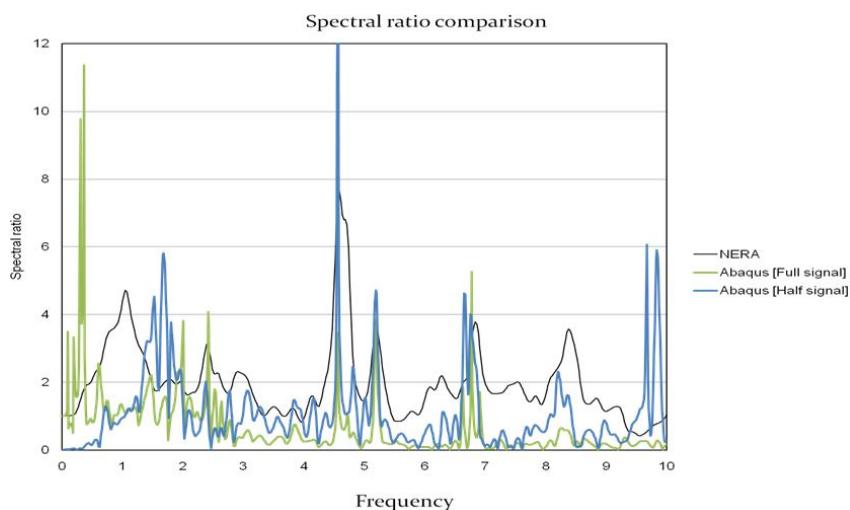


Figure 4.11: Fourier amplitude spectra comparison

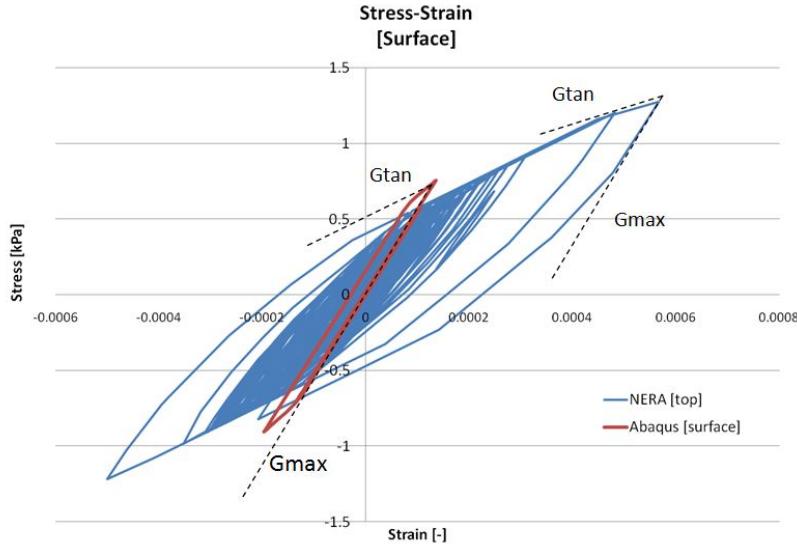


Figure 4.12: Hysteresis loops comparison for surface level

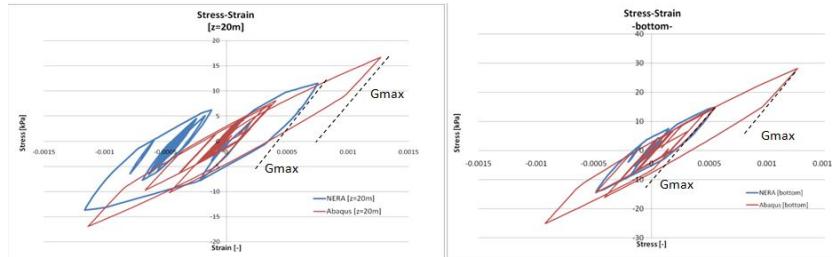


Figure 4.13: Hysteresis loops comparison for $z=20\text{m}$ (left) and bottom level(right)

4.5.1 Remarks

It is difficult to have a relevant comparison at surface level when the sample experiences low stresses; calibration of cyclic parameters was referred to rather high confining stresses. Moreover, it was noticed that Abaqus generates higher plastic strains; this might explain the signal attenuation expressed in frequency domain when comparing to NERA response.

Overall, the results show a quite satisfying match; nonetheless, differences appear due to several factors as it follows:

1. Abaqus works with a dynamic implicit integration scheme with an Euler backwards theory that is unconditionally stable whereas NERA solves the system of equation through a central-difference integration which is conditionally stable; thus on one software, user has the option of manually adjusting the time step while on the other he cannot. The equation of motion for the system in dynamic domain it is basically the same:

$$f = F - \rho \ddot{u} \quad (4.16)$$

where f - body force, F - external body force, ρ - soil unit weight and \ddot{u} - relative nodal acceleration. Thus, the difference is *numerical* and cannot be adjusted in detail.

2. Both the models are based on the concept of a yield surface which means that there is a surface defined in stress space within which no plastic deformation takes place.

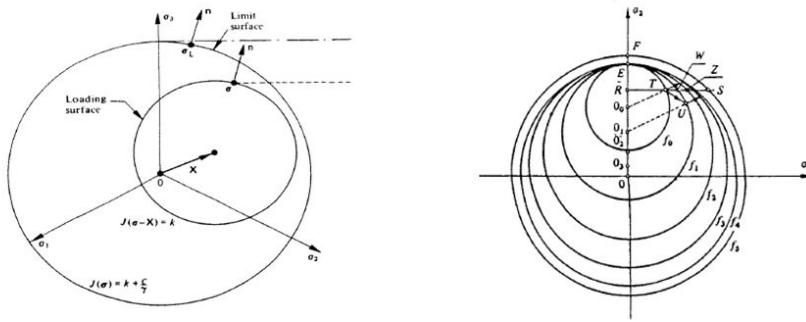


Figure 4.14: Non-linear kinematic hardening model according to Lemaitre,Chaboche [left] and Iwan,Mroz[right]

The nonlinear kinematic hardening model used in Abaqus is based on the Lemaitre and Chaboche [25] model that considers two yield surfaces and a varying hardening modulus whilst NERA works according to Iwan and Mroz [24] multi-linear kinematic hardening model that has a multiple surface plasticity. Both models include a 'fading memory' term but function differently. Thus, the difference is related to the plastic domain and how the model behaves when irreversible deformations are encountered.

3. NERA computes the shear stress and strain increments according to the sliding resistance and tangent modulus of each slider that are derived from the $G_i - \gamma_i$ points introduced as input. The tangential shear modulus is related to the secant shear modulus by $H_i = G_{max} \frac{G'_{i+1}\gamma_{i+1} - G'_i\gamma_i}{\gamma_{i+1} - \gamma_i}$ where $G_i = \frac{G_i}{G_{max}}$. The stiffness of each component of the system is related to the tangent modulus while the shear stress is associated with the sliding resistance. On the other hand, Abaqus does not work with the tangent modulus, but with maximum shear modulus G_{max} and the undrained shear strength. Also, in NERA there is no option for introducing the values corresponding to the undrained shear strength or its correlation with any other parameter. Figure 14 shows the distribution of the shear modulus with depth in both the software - these values are calculated from the input parameter - Abaqus extracts it based on the Young's modulus together with Poisson's ratio whilst NERA does it based on the soil unit weight and shear wave velocity. The values are exactly the same, it can be noticed also from the slope the hysteresis loops presented in the stress-strain plots; the width also resembles as well as the unloading-reloading areas. However, the tangent shear modulus differs from one software to the other.
4. Abaqus results are extracted in two different locations: the stresses and strains are obtained from Gauss integration points and the accelerations are obtained at nodal positions which are situated at the interface of each two element. NERA performs the analysis according to the middle of each sub-layer, so both the top and bottom outcome are actually 0.25m below the surface or above the bottom. However, not much difference should rise from this aspect.
5. Another difference relates to the viscous part of the model and it is more apparent in the acceleration response in time domain, especially in the initial period. Abaqus works with the viscous term defined exclusively as a function of Rayleigh

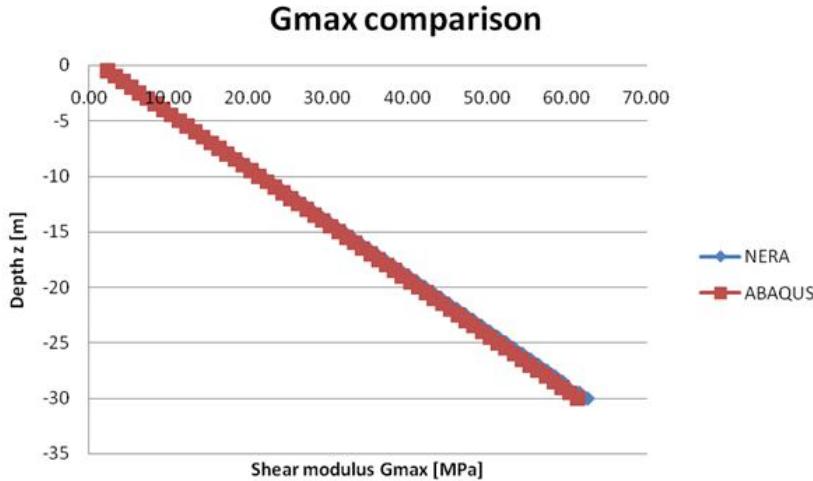


Figure 4.15: Shear modulus G_{max} comparison

damping parameter β meaning that the system damping depends on the stiffness, whilst NERA requires the critical damping ratio value, incorporating both α and β Rayleigh factors. Moreover, the energy dissipation mechanism accounts for both viscous damping and plasticity terms which, as described previously, differ from NERA to Abaqus. When working with a high PGA value, the contribution of the non-linear model and hysteretic damping becomes greater compared to the viscous damping component.

6. The aforementioned differences between the calculation programs derive mainly from numerical algorithms; however, a more important aspect seems to govern the outcome of each analysis - the dynamic nature of the problem itself. The two models are not identical, thus a difference in any given point might generate distinct response at unknown location and time because of the non-linear propagation fashion.
7. Noise can be experienced in both the signals of the different computer programs. This can distort the final results; filtering is possible, however it is time demanding and does not represent the main interest in this study.

4.5.2 Additional investigation

An additional investigation was performed in order to check the soil response when closer to elastic domain - as in, a lower PGA was applied at the bottom boundary. The first analysis contained a PGA value of approximately 0.5g whilst the second one scaled down the value to 0.1g. The results can be seen in the following figures.

The results confirm the expectation regarding the amplification effect of the soil combined with the PGA level, also they are in accordance with ARUP report regarding the site response analysis performed for the specific location in discussion. The acceleration responses at surface produced in both the computational software present the same maximum value, of course, with differences that were exposed previously, the elastic response seems to match together with the stiffness degradation effect.

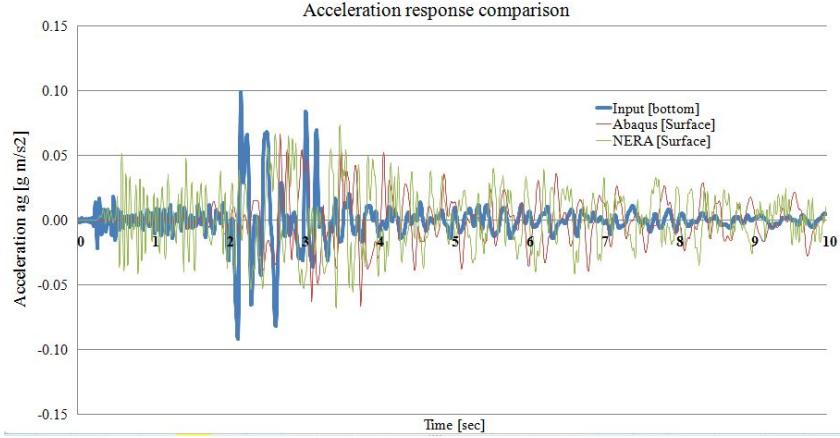


Figure 4.16: Acceleration response comparison for $\text{PGA}=0.1\text{g}$

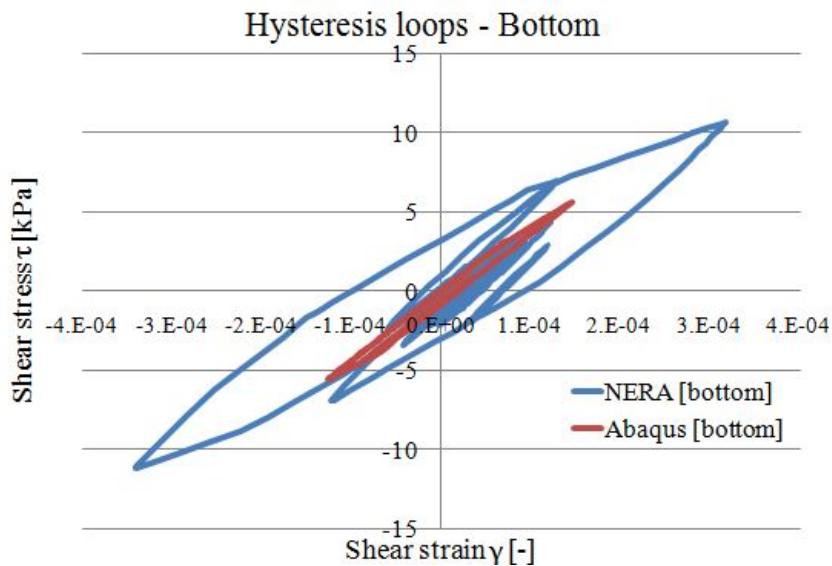


Figure 4.17: Hysteresis loops comparison for bottom level

4.6 Conclusions

The present study assembles the soft soil conditions and a recorded acceleration time history from the specific site, applies various numerical methods to achieve same output and proceeds with a comparison between the analyses. It acknowledges, in the same time, the differences and limitations occurring amid. Given the fact that the study deals with a non-linear kinematic hardening process, it becomes quite difficult to point exactly the main cause that leads to dissimilarity. The overall results show a fair match when comparing the two software, but also when accounting for external sources KNMI, [55], [44], [1] that carried out particular investigations.

It can be concluded that for the Groningen sites, low PGA input ($a_g = 0.1\text{g}$) the surface acceleration response amplified whereas when dealing with a high PGA input ($a_g > 0.15\text{g}$) the top PGA is de-amplified. Both the strength properties of the homogeneous medium and the earthquake motion characteristics influence the seismic wave propagation through the soil; for this particular case, the inelastic response depends on the limited capability of the soft layers to transmit seismic signals to the surface because of the low strength and on

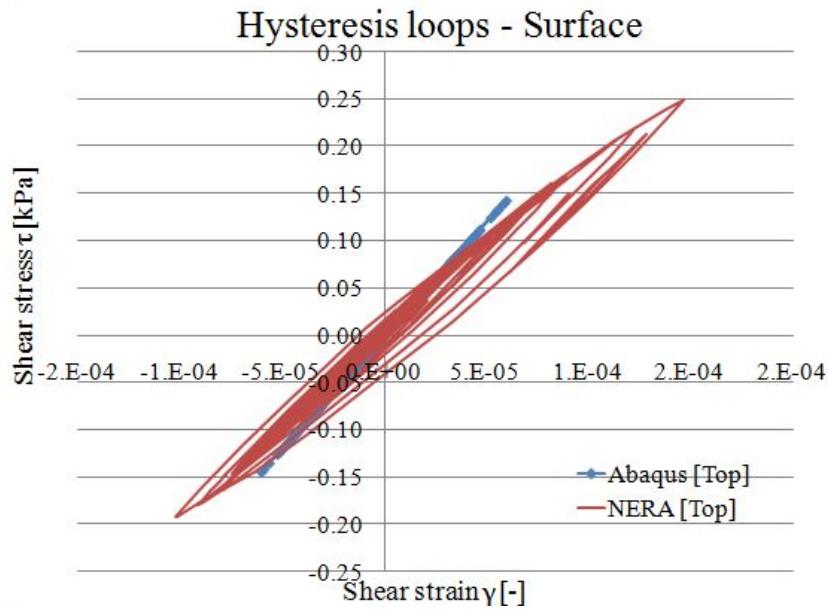


Figure 4.18: Hysteresis loops comparison for surface level

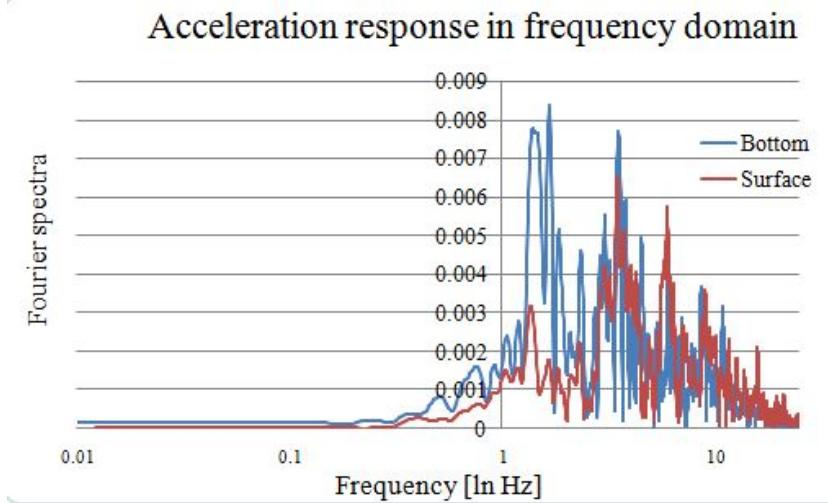


Figure 4.19: Fourier amplitude spectra for PGA=0.1 - logarithmic scale

the high hysteretic damping observed at large strains. At low PGA values, the soil displays elastic behaviour as it reaches the surface, the frequencies do not experience considerable damping whereas at high PGA levels, the soil shifts towards its natural frequency, damping the higher ones and non-linear constitutive model plays a more important role than the viscous damping effect.

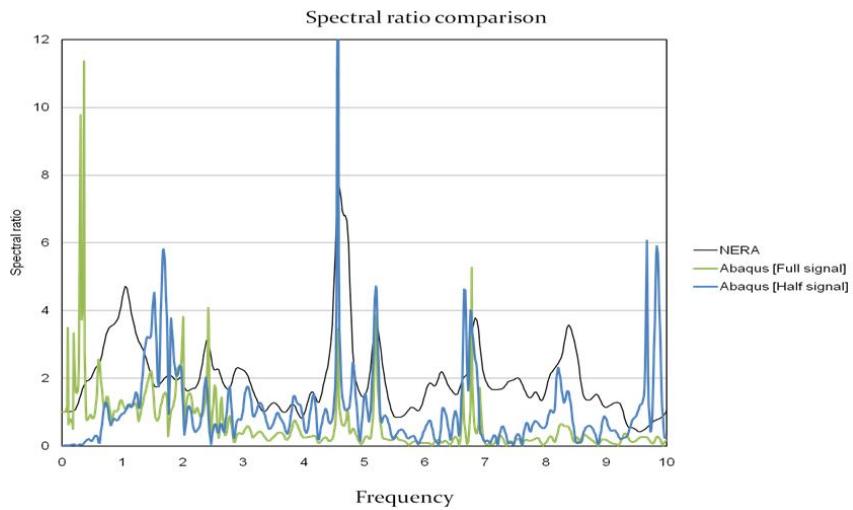


Figure 4.20: Site amplification factor comparison for PGA=0.1g

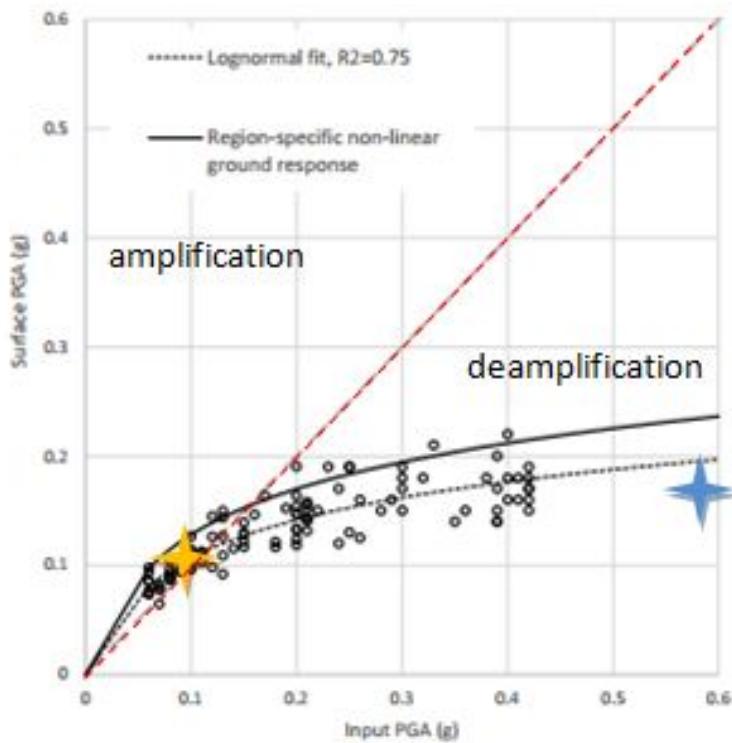


Figure 4.21: Groningen site non-linear ground response, input vs surface PGA according to ARUP report; the additional blue star corresponds to the present high PGA analysis (PGA=0.6g) and the yellow star to the low PGA case (PGA=0.1g). The red line marks the border between the two regions - amplification and de-amplification.

Chapter 5

Soil Structure Interaction analysis

The current chapter presents the analysis performed in 2D plane stress domain of the soil-footing(-structure) interaction considering a shallow foundation subjected to a recorded acceleration-time history. Various methods of seismic implementation are carried out to examine aspects such as load effects on soil response, effectiveness of energy dissipation mechanisms and soil uplift occurrence.

5.1 New design philosophy

As previously presented, the new design philosophy suggests a different perspective on the induced non-linearity over the soil-structure assembly. Researchers involved within this study (Anastasopoulos et al., 2010 [8], Gazetas et al, 2013 [11], Apostolou et al., 2011 [16], etc.) showed several effects associated with soil "failure" as acting beneficially in case of seismic ground motion. The interest in the present essay is to apply such approach on a different setting: soft soils, lack of bedrock, induced, and not tectonic, earthquakes together with shallow foundations. In order to summarize the goals, it is utmost important to define the characteristic non-linear effects:

- separation at soil-footing surface under rocking vibration originating from the soil layer also known as *uplifting* that occurs when negligible interface tensile capacity is considered.
- mobilisation of the bearing capacity type of failure surface mechanism arises when experiencing large cyclic overturning moments - *soil failure*.
- plastification of the underlying ground in the proximity of the edges of the foundation induced by large vertical stresses.

5.2 Problem definition

The former chapter gets extended towards a 2D plane stress problem involving a homogeneous soil layer supporting a shallow foundation and the entire structure is subjected to a seismic input motion. The study aims at inspecting the inelastic soil response, the proposed method accuracy and its limitations. The final goal is to be able to acknowledge the new design philosophy suitability for this specific earthquake in Groningen area.

5.3 Model description

As expected, the soil properties do not change drastically, for all the work that was previously conducted proves the parameters validity. The preceding model (1D soil column) is expanded into a larger soil layer supporting a shallow foundation. The resting building relates to a chimney located in Hoogezand village, Groningen, in the north of Netherlands and it was chosen for its relatively simple geometry together with available structural properties. The location and the chimney itself can be seen in Figures 5.1 and 5.2.



Figure 5.1: Map location of the chimney - Groningen area



Figure 5.2: Real structure objected to study

The chimney is represented by a rectangular footing with a lumped mass on top of a slender, infinitely rigid pier. Moreover, the footing is also considered to behave in a stiff fashion when seismically loaded. The main emphasis is on the soil response rather than on the structural one, thus the simplification.

5.4 Method of analysis

Inelastic soil response investigation is implemented numerically with a finite element method considering two-dimensional plane strain assumptions; both the soil medium and the footing are modelled as deformable solids using quadrilateral, continuum elements, the superstructure simplified to a pier is assigned with a beam element section whilst the lumped mass is represented by a mass element. A state-of-art contact algorithm defines the soil-structure interface incorporating uplifting and sliding features whereas purely elastic impact assumption is adopted. Every analysis starts with a static step - the geostatic step in which initial stress conditions are established.

The dynamic analyses operate through an implicit direct-integration algorithm - global equations of motion are integrated in time domain via implicit Hilber-Hughes-Taylor operator. Newton's method includes the α and β parameters with the values explained in the previous chapter (see section 4.2.4, chapter 3 and Appendix I). The numerical stability is achieved by calibrating both the mesh size and the time-step increment - such way elastic wave propagation laws are not violated - the calibration is also explained in Appendix J. A schematization of the FE model can be seen in Figure 5.9 followed by a detailed description of the model.

5.4.1 Analysis procedure - Steps

Every analysis begins with the calculation of the in-situ stresses to establish the geostatic conditions. Gravity load is applied all over the soil medium, simulating the real status when no foundation is resting on the ground.

Further, the footing presence is reproduced using a point load applied at its centre of the mass. This method relates to the mechanics of the software as well - as the foundation is declared as a rigid body, the program requires the definition of a reference point which will become the simplified representation of the section: every load or boundary condition imposed to the footing is prescribed to this very point only. Thus, the available structural uniform load distribution was converted into a point load and applied to the reference point in discussion. This way, the foundation self weight is reproduced together with the activation of the soil-footing interface.

Lastly, the seismic excitation must be integrated within the model. Many approaches are formulated in the scientific literature regarding the simulation of the earthquake action for obtaining an accurate results. Numerous methods relate to the implementation of boundary conditions as the problem becomes non-linear and it is subjected to wave propagation. Stability, computational expenses and model dimensions play an important role for the accuracy of the output and require most attention. Henceforth, different types of boundary conditions were imposed that mimic the acceleration time history in distinct manners. Important to keep in mind that some methods do not necessarily require dynamic algorithms, a quasi-static analysis is preferable for such cases - this aspects will be explained in detail later in this chapter.

Thus, there are three main steps conducted within all analyses:

1. **Geostatic** - for introducing the initial stress conditions of a free-field;
2. **Self weight application** - the perturbation on the stresses close to the surface due to the presence of the footing;
3. **Dynamic/ Quasi-static** - applying the seismic input in various manners to simulate the earthquake motion.

5.4.2 Contact definition

An important role in uplifting triggering is played by the contact definition - the user can create and customize the interface properties accordingly to the desired application. In finite element analysis, contact conditions describe a particular category of discontinuities, enabling forces to be transmitted from one part to another. The model must recognize and distinguish when the parts are in contact and when separation occurs in order to apply the constraints properly.

Abaqus offers the possibility of defining contact pairs or contact elements; the former is recommended and it is based on the master-slave approach. In addition, it allows the definition of these entities as surfaces or a collection of nodes - the differences refer to methods of discretization and calculation. In order to define a contact, its interaction properties have to be formulated - again, Abaqus allows the user to customize these features in correspondence with the model in use. For this particular case, only mechanical properties were created. An advanced contact algorithm is applied in order to permit uplifting and sliding and, additionally, to control their development during the seismic excitation.

As previously mentioned, the study investigates two types of soil-footing contact: *fully bonded* and *tensionless sliding interface*. The advanced algorithm refers to the sliding interface whilst the fully bonded contact is effortlessly depicted through a **Tie constraint** - using the same master-slave formulation, it provides a simple way of bounding the two surfaces permanently, preventing sliding/separation.

However, the tensionless sliding interface requires much more attention and research as it incorporates various features that will be detailed further on.

Mechanical properties The contact is described for both normal and tangential direction, more precisely a pressure-overclosure relationship illustrates the normal behaviour whereas a frictional interaction deals with the tangential behaviour.

For normal direction, Abaqus implements a "hard-contact" relationship by default which consists of:

- no penetration of master surface into the slave;
- no upper bound for the transmitted contact pressure;
- no stress transfer between surfaces when there is no contact detected.

Nonetheless, the current study indicates another type of normal contact, a softened one involving a pressure-overclosure relationship. According to Abaqus documentation, the softened contact can be introduced as linear or exponential, the latter being preferred. In an exponential (soft) contact pressure-overclosure relationship the surfaces begin to transmit contact pressure once the clearance between them, measured in the contact

(normal) direction, reduces to c_0 . The contact pressure transmitted between the surfaces then increases exponentially as the clearance continues to diminish. The schematization of the relationship can be visualized in Figure 5.3.

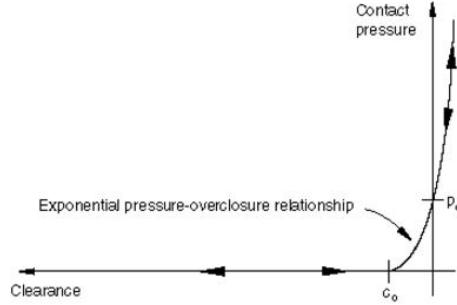


Figure 5.3: Exponential “softened” pressure-overclosure relationship in Abaqus/Standard

where p_0 is the contact pressure at zero distance, c_0 is the distance from the master surface at which the pressure is decreased to 1 % of p_0 . The behaviour in between is exponential. A large value of c_0 leads to soft contact, a small value to hard contact. It is difficult to know a priori which values are suitable, however literature studies suggest for $p_0 = 10kPa$ correlated with a clearance $c_0 = 10E^{-5}m$.

For the tangential behaviour, the software provides the following options:

- frictionless - default;
- rough - no slip is allowed;
- penalty friction which allows for:
 - Coulomb friction law $T = \mu N$;
 - constant shear limit at surface;
 - friction coefficient as a function of the slip rate and contact pressure;

Considering the cohesive character of the soil, the Coulomb friction law might not be the appropriate solution, thus the second option was chosen. Thus, the frictional behaviour is actually a cohesive one. This shear stress limit is typically introduced in cases when the contact pressure stress may become very large causing the Coulomb theory to provide a critical shear stress at the interface that exceeds the yield stress in the material beneath the contact surface. A reasonable upper bound estimate for τ_{max} is $\sigma_y/\sqrt{3}$, where σ_y is the Mises yield stress of the material adjacent to the surface. In some cases some incremental slip may occur even though the friction model determines that the current frictional state is “sticking.” In other words, the slope of the shear (frictional) stress versus total slip relationship may be finite while in the “sticking” state, as shown in Figure 5.4.

The relationship shown in this figure is analogous to elastic-plastic material behavior without hardening: K corresponds to Young’s modulus, and τ_{crit} corresponds to yield stress; sticking friction is associated with the elastic regime, and slipping friction to the plastic one. A typical average value recommended in the literature for the elastic slip is 0.1mm and it seems appropriate for this case as well.

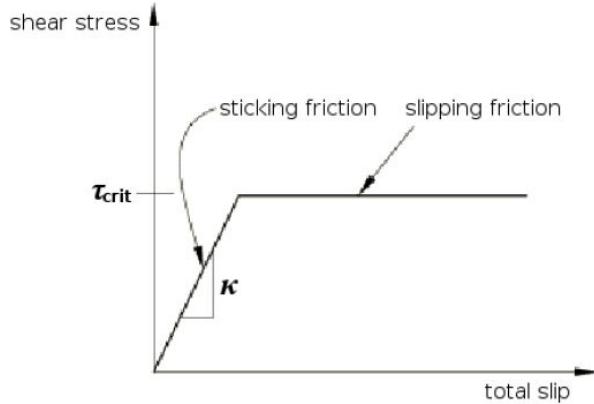


Figure 5.4: Elastic slip versus shear traction relationship for sticking and slipping friction

Contact interface discretization Having all interaction properties defined, the contact itself must be formulated; the most suitable interaction option Abaqus/Standard offers is *Surface-to-surface*; the contact discretization can be chosen node-to-surface (N-S) or surface-to-surface (S-S), the latter being preferable. Firstly, because the conditions will be enforced based on an average region instead of strictly node-wise. The averaging regions are approximately centered on slave nodes, so each contact constraint will predominantly consider one slave node but will also consider adjacent slave nodes. Secondly, this option does not include spikes in the pressure distribution along the surface, as it happens in the N-S case. Lastly, large and unintended penetration of master nodes into slave does not occur leading to a smoothing effect.

The sliding formulation require for the interaction implementation also has two options: finite sliding or small sliding. The second alternative is more convenient, as the footing will not slide considerable. Additionally, coupling of slave nodes with their projections on master surface is calculated at the beginning of the analysis and does not change throughout the analysis, whereas for finite sliding approach, this coupling is checked and recalculated throughout the analysis.

5.4.3 Boundary conditions

For this type of application, it becomes necessary to define two sets of boundary conditions: the *global* and the *local* ones. The first set assumes the top surface as being constraint-free, whilst rigid bottom is initially defined. The lateral boundaries are both vertically and horizontally constrained. Nevertheless, in dynamic analyses, a fixed boundary condition will lead to wave reflection at the outer limits of the model translated into energy trapped inside the model. This effect becomes detrimental, therefore solutions must mitigate reflective waves propagating throughout the model. One way is to create a large enough model to simulate an infinite medium - however, the calculation can become quite time and space consuming, thus the need of another concepts. Many researchers proposed methods of tackling the problem, here highlighting the work of Lysmer and Kuhlemeyer [54], Zienkiewicz et al (1989) [54], and many more.

Theory of wave propagation For the simplicity of the problem, vertically propagating waves were considered exclusively; it is also well known that both the body waves - P

waves and S waves - are independent of each other. According to Love(1944) [56], the wave equation for an isotropic elastic medium is:

$$c_p^2 \nabla (\nabla \cdot u) - c_s^2 \nabla \times \nabla \times u = \frac{\partial^2 u}{\partial t^2} \quad (5.1)$$

where, according to D'Alembert equation solution, c_p is the P-wave velocity ($c_p = \sqrt{\frac{\lambda+2\mu}{\rho}}$) and c_s is the S-wave velocity ($c_s = \sqrt{\frac{\mu}{\rho}}$) with λ and μ as Lamé constants and ρ the density of the medium.

It becomes clear that when working with seismically propagating waves, the real challenge lies in the a correct implementation of artificial boundaries construction rather than defining the propagating medium. Important to mention are the two conditions required by a surface of a wave front as Nielsen, 2006 [57] states in his research:

1. **kinematical** which can be written under the form:

$$\frac{1}{\cos(\theta)} \frac{\partial u}{\partial x} = \frac{1}{\sin(\theta)} \frac{\partial u}{\partial y} = -\frac{1}{c} \frac{\partial u}{\partial t} \quad (5.2)$$

$$\frac{1}{\cos(\theta)} \frac{\partial v}{\partial x} = \frac{1}{\sin(\theta)} \frac{\partial v}{\partial y} = -\frac{1}{c} \frac{\partial v}{\partial t} \quad (5.3)$$

where θ is the angle of incidence between the surface wave front and the incident waves and c is the wave velocity that depending on the direction can be either associated with compressive or shear waves.

2. **dynamical** are expressed in terms of traction forces coplanar with the wave front

$$\rho c \frac{\partial u}{\partial t} = -f_x \quad (5.4)$$

$$\rho c \frac{\partial v}{\partial t} = -f_y \quad (5.5)$$

In the following section 5.5 , several boundary condition concepts are presented highlighting the necessity of each. The section includes information describing the methods, differences between the studies, limitations and mathematical background. This represents one principal goal the current paper strives to achieve - an extended investigation to understand what various boundaries influence the performance of the FE model and thus decide which one is more suitable for this application.

There are a couple of methods that are well known in literature and are tested within the section and presented as it follows:

Tied lateral boundaries The traditional approach considers pairs of lateral nodes being tied together such way that the horizontal and vertical displacement are equal throughout the entire analysis. This feature can be easily achieved using Abaqus MPC (multi-point constraint) option specifically designed for this situation. The assumption is in conformity with Zienkiewicz's work stating that the presence of the structure on soil oscillation is negligible when the boundaries are sufficiently far.

Subsequently, the input motion is introduced at the vertically fixed base of the model that replicates the presence of the bedrock. As previously discussed, the acceleration signal obtained from the dataset for Groningen field was recorded at borehole depth,

not at bedrock, which means that the recordings can include both incident and reflected waves. In order to exclude an overestimation of the real input signal, the accelerogram was truncated in half to ensure that only upward travelling waves are considered.

Nevertheless, this method can be formulated in the FE product either through a dynamic or a quasi-static step depending whether the earthquake is expressed in terms of total displacements or total accelerations. However attractive this simple method might be, its shortcomings originate from both the lack of an actual bedrock or from the uncertainties rising when defining the model dimensions - there are no rule of thumbs for determining the truncation of the mathematical model.

Transmitting boundaries Given the flaws of the aforementioned concept, it becomes necessary to incorporate features as radiation boundaries that guarantee the outgoing waves are not reflected at the boundary surfaces.

Transmitting boundaries or absorbing boundaries (*ABC*) were first proposed by Lysmer and Kuhlemeyer (1969) [58], followed by Zienkiewicz (1989) [54]. As the name also hints, these types of boundaries are used in the form of viscous boundary tractions or dashpots in order to absorb the normal incident waves. They can be declared both globally or locally, the later proving more appealing from the numerical implementation point of view.

The reason why these types of boundaries are adopted for the FE model expresses the necessity of preventing the occurrence of reflected waves whilst capturing correctly the incoming waves at the boundaries. It can be regarded as a simulation of the "horizontal infinity" of a real soil layer. It proves well-suited when associated with an internal source of excitation, however it requires improvements when the input signal originates from external sources. The solution upgrade relates to the theory proposed by Zienkiewicz, also known as *free-field boundary conditions* which introduces the combination between viscous boundaries and a free-field soil column.

Having in mind that for a simple one dimensional, homogeneous, elastic, isotropic wave propagation problem, the free surface displacement wave equals the double of the incoming waves, it can be deducted that the input signal can be extracted from the recorded total signal on the undeformed surface. The free-field soil column allows the user to obtain sets of incoming waves parameters (displacement, velocity, acceleration) in time domain at a known position and correlate them with the viscous boundaries located at the sides of the model. As a consequence, outside the boundaries, the elastic and isotropic conditions pertain.

The theoretical background of the free-field boundary element was proposed in an efficient manner by Lysmer and Kuhlemeyer that associates the vertical free-field soil column with viscous boundary tractions. This way, the incoming wave takes the form of equivalent forces, rather than accelerations. The traction consists of two terms as it follows:

1. viscous dashpots absorb incoming waves;
2. free-field motion simulating the undisturbed soil layer;

Henceforth, the equations describing the tractions, both normal f_n and shear f_s are:

$$f_n = \rho c_p \left(\frac{\partial u}{\partial t} - \frac{\partial u}{\partial t} \right) + l_x \sigma_x' \quad (5.6)$$

$$f_s = \rho c_s \left(\frac{\partial v^*}{\partial t} - \frac{\partial v}{\partial t} \right) + l_x \tau_{xy}^* \quad (5.7)$$

where prime quantities relate to the free-field output values, $l_x = -1$ or $l_x = 1$ for outward normal points either negative or positive direction. First term of the equations represents the Lysmer and Kuhlemeyer traction due to the presence of dashpots whereas the second term represents the stress resulting from free-field wave propagation, including eventual static reaction forces.

Gathering all information, the modelling scheme should consist of two, perhaps three calculations as it can be seen in Figure 5.5 :

1. one model for each column generating the free-field soil response;
2. one main model representing the soil - footing interaction including viscous dampers at the lateral boundaries;

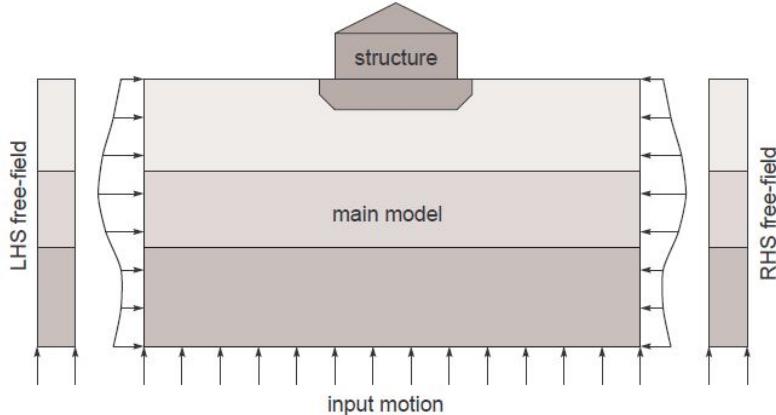


Figure 5.5: Real structure objected to study

5.5 Implementation of ABC

The aforementioned features of the free-field boundary conditions are detailed below, starting with the free-field soil column followed by the main model description together with various modelling techniques.

Free-field soil column The free-field soil column performs similar to a vertical soil medium located far enough from the actual foundation for the vibrations not to perturb its state stress. This can be simply implemented as the one-dimensional column subjected to seismic excitation, identical to the model created for the site response analysis. Its advantages involve the option of extracting the results at any desired node, converting them into input for further calculations. Moreover, these results aid reducing the size of the main model domain and this saves the procedure considerable time. Thus, the previous analysis becomes essential as it satisfies all the apparent requirements.

It is worth to acknowledge the constraints linking pairs of lateral nodes in order to maintain equal horizontal displacements along the seismic test. Then, it suffices extracting the outcome from one set of lateral nodes, left or right displaying equal results. The

output yields displacement, velocity and acceleration time histories for each lateral node
- allowing a further implementation into the main model.

A series of results are presented below:

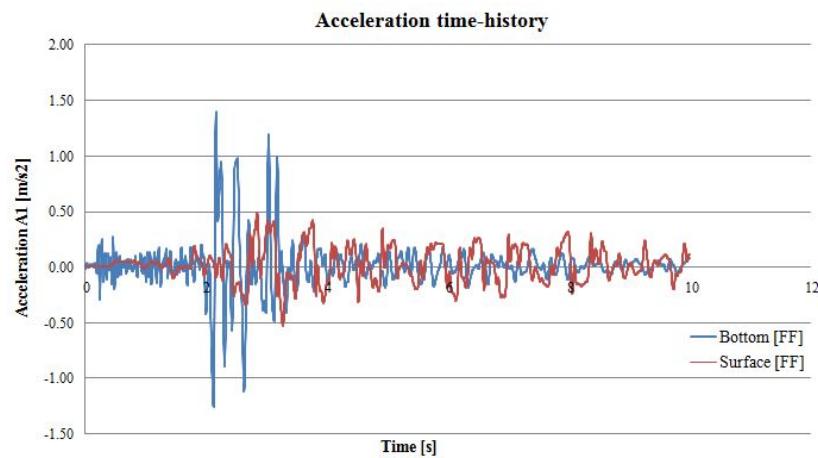


Figure 5.6: Acceleration time history output at base and surface level

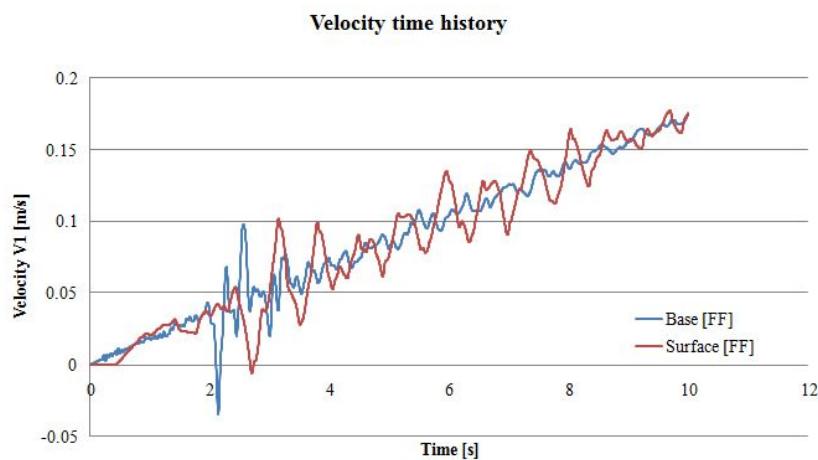


Figure 5.7: Velocity time history output from Free field soil column

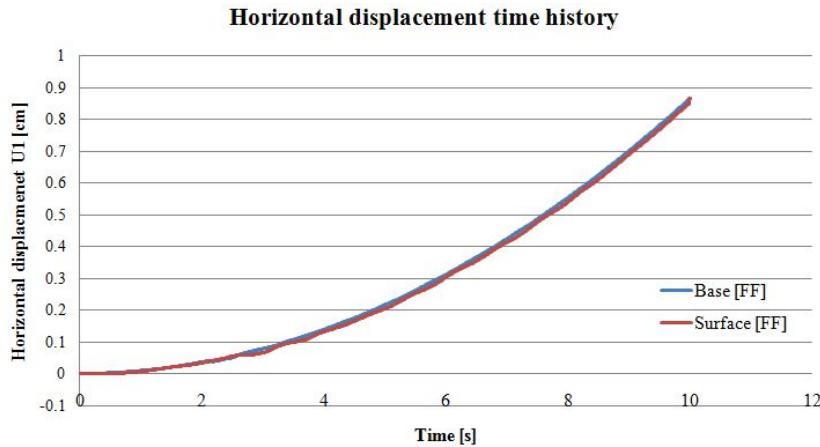


Figure 5.8: Horizontal displacement time history

Main model The main model, as it can be seen in Figure 5.9, consists in few features such as:

1. *soil medium* - a homogeneous clay layer, solid, deformable, displaying non-linear kinematic hardening. Same material and meshing properties as the free-field column.
2. *footing* - rectangular solid, deformable, meshed with continuum elements behaving elastically.
3. *mass* - concentrated mass represented by a point assigned with inertial mass. It is in conformity with the assumption of a SDOF system.
4. *pier* - beam element, infinitely rigid representing the chimney itself.
5. *contact interface* - special algorithm contact;

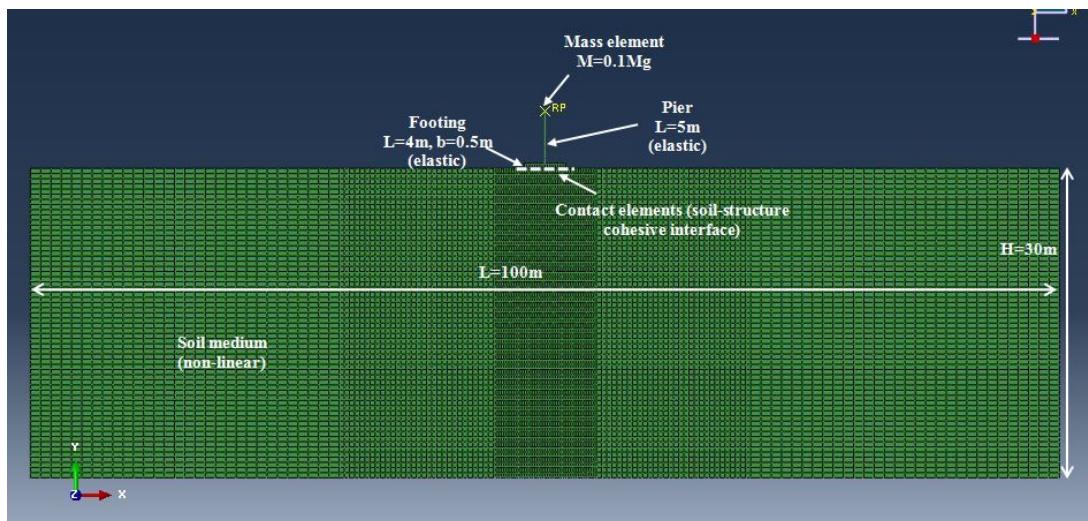


Figure 5.9: Schematization of the main FE model

The steps were presented before, the boundary conditions change accordingly to each method of implementation. The absorbing boundaries proposed by Lysmer and Kuhlemeyer - which can be efficiently implemented as viscous dampers or dashpots assigned

to lateral boundaries of the soil medium - are evaluated performance-wise in correlation with seismic loading procedures. These dampers indicate a local boundary that absorb the incoming wave - their accuracy increase proportionally with distance from the area of interest(footing) and if they are defined as frequency independent. Abaqus allows the user to specify dashpots connected to the ground - an option requiring the definition of the local DOF direction and the dashpot coefficient. In dynamic analysis the velocities are obtained as part of the integration operator; in quasi-static analysis in Abaqus/Standard the velocities are obtained by dividing the displacement increments by the time step. Additionally, it can model relative velocity-dependent force and provide a energy dissipation mechanism. The dashpot coefficient is calculated:

$$C_1 = \rho V_p A \quad (5.8)$$

$$C_2 = \rho V_s A \quad (5.9)$$

where V_s and V_p are the compressive and shear wave velocities of the soil, ρ is the soil density, A is the tributary area of the element assigned with dashpot and C_1, C_2 are the dashpots coefficients for normal and tangential direction.

It is worth mentioning few assumptions related to wave propagation which simplify the problem without suffering from loss of accuracy:

- only vertically propagating seismic waves were taken into account; firstly, because a distinctive feature of this specific induced earthquake are the dominant shear waves. Secondly, because the free-field soil was also subjected to S-waves exclusively. And thirdly, because the two body waves are independent of each other. Thus, the compressive waves do not influence the soil-structure behaviour for now.
- the body waves travel towards the lateral boundaries under an incidence angle of $\theta = 0$. Basically, there are no *evanescent waves* within the deformable body, waves that occur due to combinations of boundary conditions and, unlike the P and S-waves, are frequency dependent.

With these being said, the main model consists of:

NOTE: This analysis is currently in stand-by as I had troubles using these features in Abaqus.

Equivalent forces

5.6 Results

5.6.1 Effects of applied boundary conditions

5.6.2 Effects of loads

5.6.3 FBC vs TSI

Soil-Foundation interaction A simple rectangular footing with dimensions L=4m and b=0.5m is resting on the non-linear soil medium. As mentioned before, the analysis investigates the differences between two types of soil-footing contact: FBC and TSI. The fully bonded contact assumes the elements are permanently tied together during

the analysis whilst the sliding interface allows uplifting to occur. The advanced contact algorithm was described in previous sections and the output consists of responses extracted from both analyses. The footing acts like a rigid body; the boundaries are located at considerable distance from the footing in order to avoid its influence on the stress field. In fact, a test was performed to check the accuracy of the boundary position. Thus, the results from the site response analysis were compared to the ones at the boundaries until they were matching - because the one-dimensional soil column used in the SRA is representative for a far-field soil element, it shows how the ground itself behaves during an earthquake. As soon as this goal was achieved, it could be concluded on a correct width of the soil body - for this specific case, it proved that $L=100\text{m}$ is sufficient. A collection of figures can be seen as it follows:

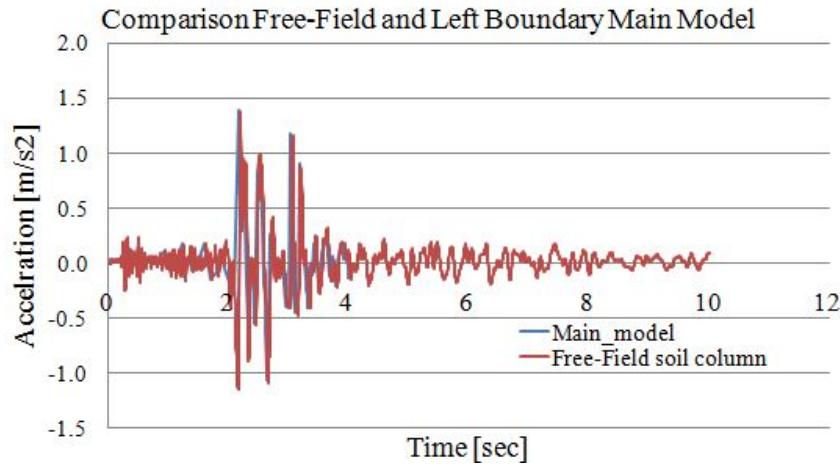


Figure 5.10: Validation for soil layer width

to be continued...

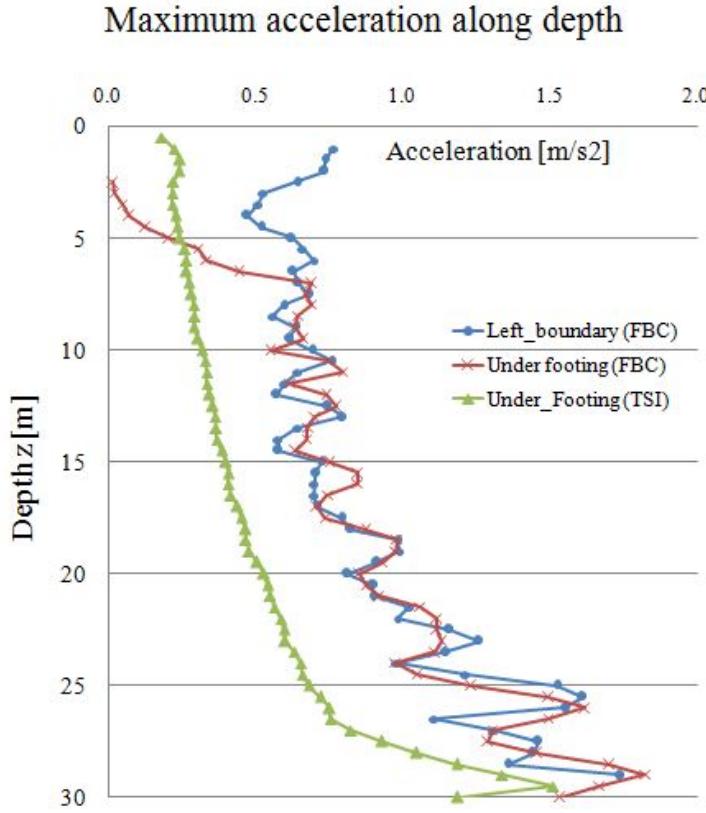


Figure 5.11: Maximum acceleration for FBC and TSI analyses recorded underneath the foundation

Soil-Foundation-Structure interaction Two additional elements are to be added for this section: the pier, acting infinitely rigid and the lumped mass on top of it. For the current situation, only the pier is present - (*NOTE: Abaqus proves to be difficult when defining the connection between these elements - I shall insist more on this part*); the outcome is presented by means of stresses and displacements under footing, acceleration response, amplification factor etcetera.

The results correspond to a more advanced analysis consisting in the non-linear soil supporting a rigid footing-pier assembly. The test starts with a geostatic step, followed by the appliance of self weight of the foundation-pier and seismic excitation at the base of the layer.

The self weight of the footing relates to the calculations performed by Arcadis and Crux Engineering BV, which state that an uniform pressure load acts on the footing with a value of $q = 65.5 \text{ kN/m}^2$. Converting this load into a concentrated force applied at the footing centre of the mass, yields $F = 260 \text{ kN}$.

As for the dynamic step, the acceleration time history was scaled to include a PGA of 0.28g as representative for this specific site. The signal is trimmed yet again, because it contains both upward and downward waves and because the base aims to simulate the presence of the bedrock. Thus, the wave should be travelling upwards exclusively. A sketch of the input can be seen in the figure below.

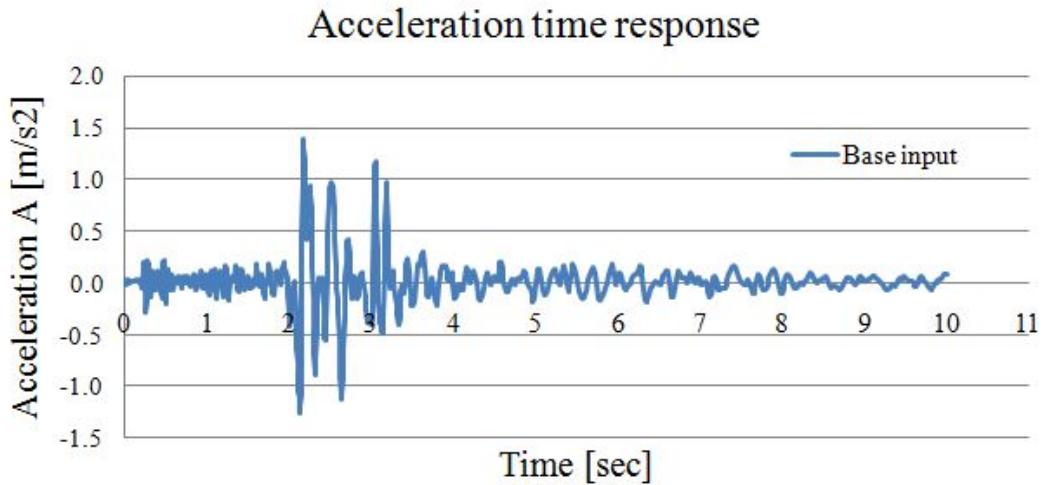


Figure 5.12: Acceleration input for PGA=0.28g trimmed to half

5.6.4 Stresses

The main emphasis is on the proximity of the footing; the stresses developing from both the self weight action as well as the seismic excitation were collected and presented in the following plots.

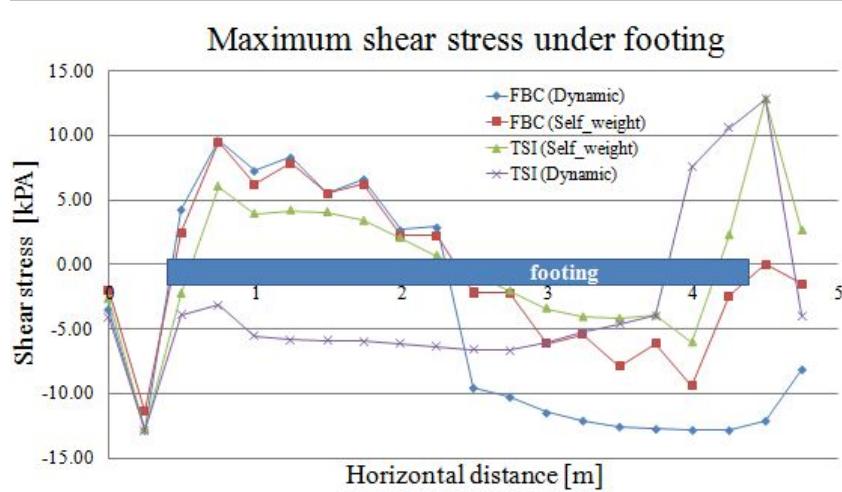


Figure 5.13: Maximum shear stress comparison

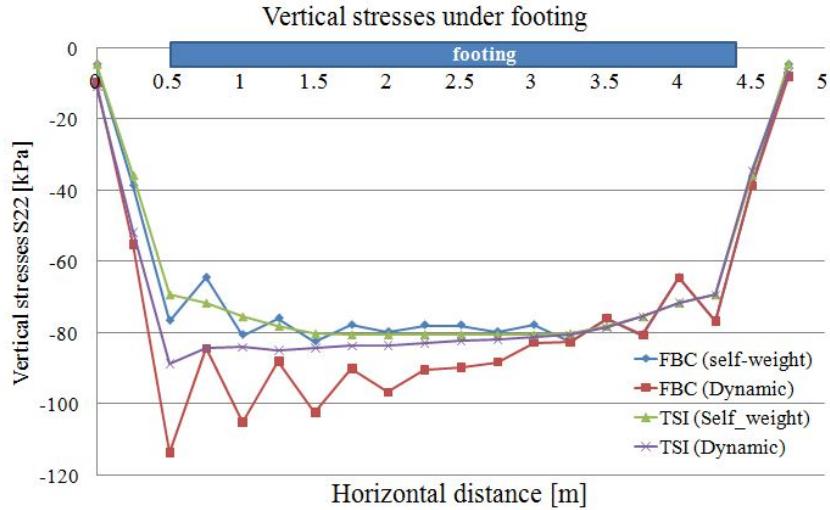


Figure 5.14: Maximum vertical stress under footing comparison

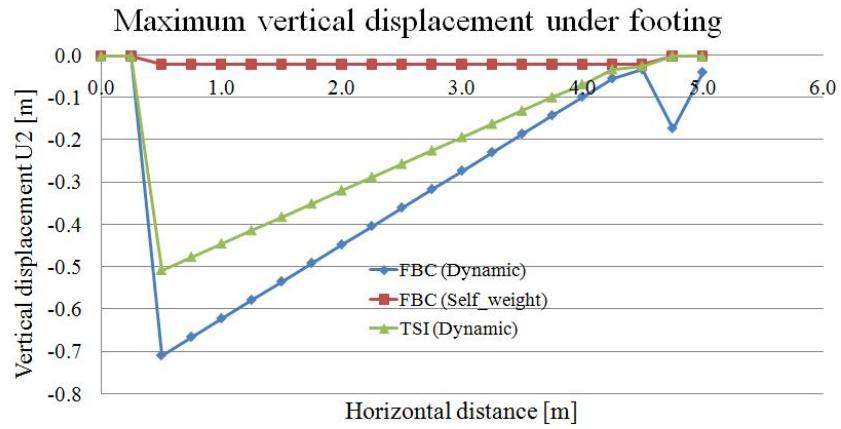


Figure 5.15: Maximum vertical displacement under footing

5.6.5 Acceleration response

The study extends to the investigation of the dynamic response at the mass location -which represents the top of the pier element. The acceleration is extracted for three main points: the base of the model, the surface point of the soil right beneath the footing and the lumped mass positioned on top of the structure. One goal is to observe whether the structure experiences amplification or de-amplification which can hint if the ductility demand decreased or not. Apart from comparing the acceleration response in various positions, the amplification factor is investigated in the same fashion previous chapter operates.

Acceleration outcome is transferred in frequency domain via a Fast Fourier computation for responses from soil surface and lumped mass; the transfer function is calculated:

$$A(f) = \frac{F_{a,mass}(f)}{F_{a,surface}(f)} \quad (5.10)$$

where $A(f)$ - site amplification factor; $F_{a,mass}(f)$ and $F_{a,surface}(f)$ - Fourier amplitudes of the lumped mass on top of the pier and of the ground acceleration at surface, respectively.

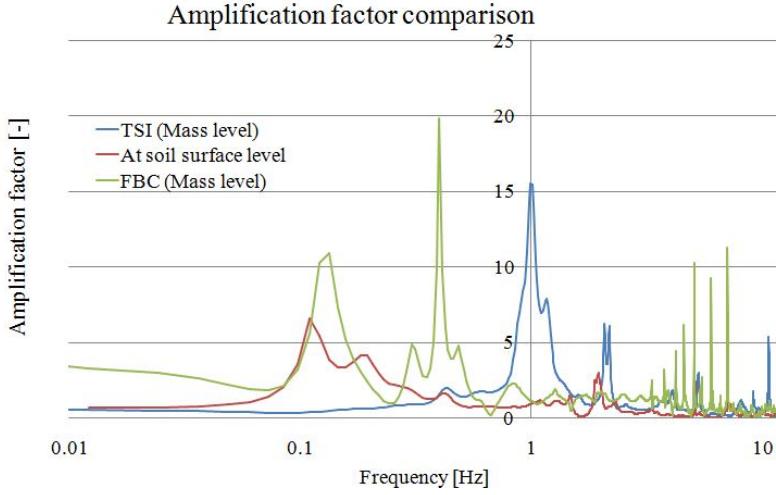


Figure 5.16: Amplification factor structure-soil surface

The output of the TSI case displays way fewer increment steps - it is speculated that this relates to the convergence; as it converges faster than FBC, the analysis does not require a smaller time step, thus it prints the values at larger increment intervals. *NOTE: The problem shall be investigated in more detailed with the interest of obtaining more point results.*

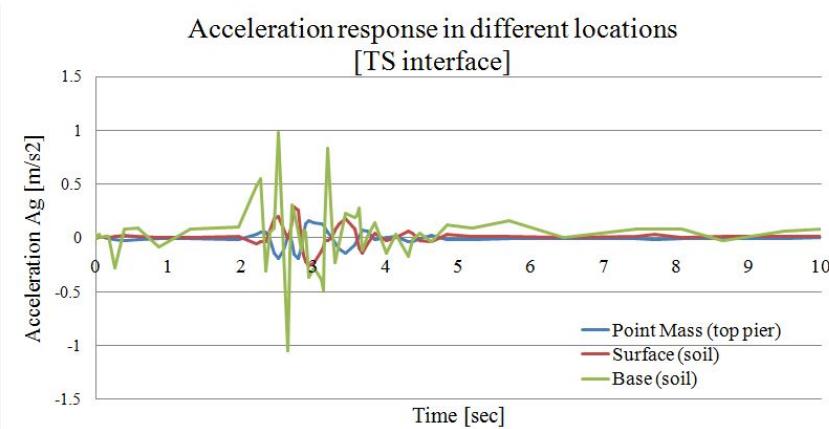


Figure 5.17: Acceleration response for TSI

The two analyses are originating from the same base model (same mesh, material input parameters, time incrementation elements), however, there are some numerical uncertainties that leads to an unsatisfactory collection of information points for the case with TS interface. Nonetheless, it is assumed, for the moment, that the peak acceleration was not omitted and that it can be depicted in the plot. Then, it seems that considering a tensionless sliding interface instead of a fully bonded contact reduces the acceleration at higher levels, thus the building experiences de-amplification. The output in frequency domain also indicates this phenomena as a larger amplification factor is observed when applying a permanent soil-footing tie. Additionally, the frequencies of soil surface and point mass are relatively close when working with a fully bonded footing; as previously said, if two elements oscillate with similar frequency, resonance can occur amplifying the damage.

Notes For the future investigation, I will:

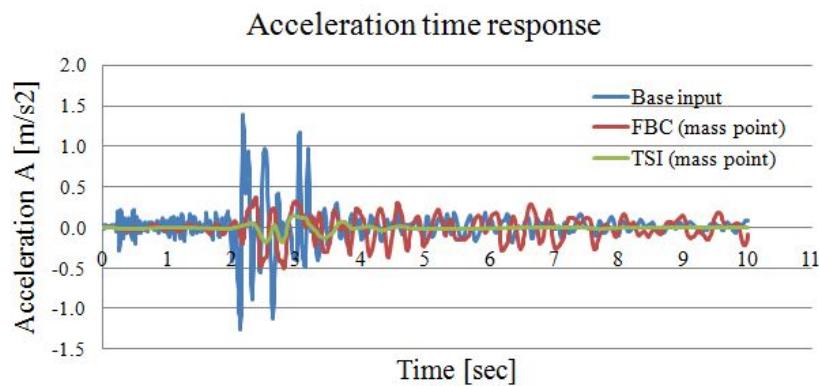


Figure 5.18: Acceleration response comparison at point mass level

1. add a lumped mass on top of the pier and repeat this analysis;
2. create the moment-shear envelope;
3. check rotations at the centre of the mass to validate the uplifting and bearing capacity type of failure mechanism (overturning moments);
4. investigate the absorbing conditions (if time allows).

5.7 Limitations and recommendations

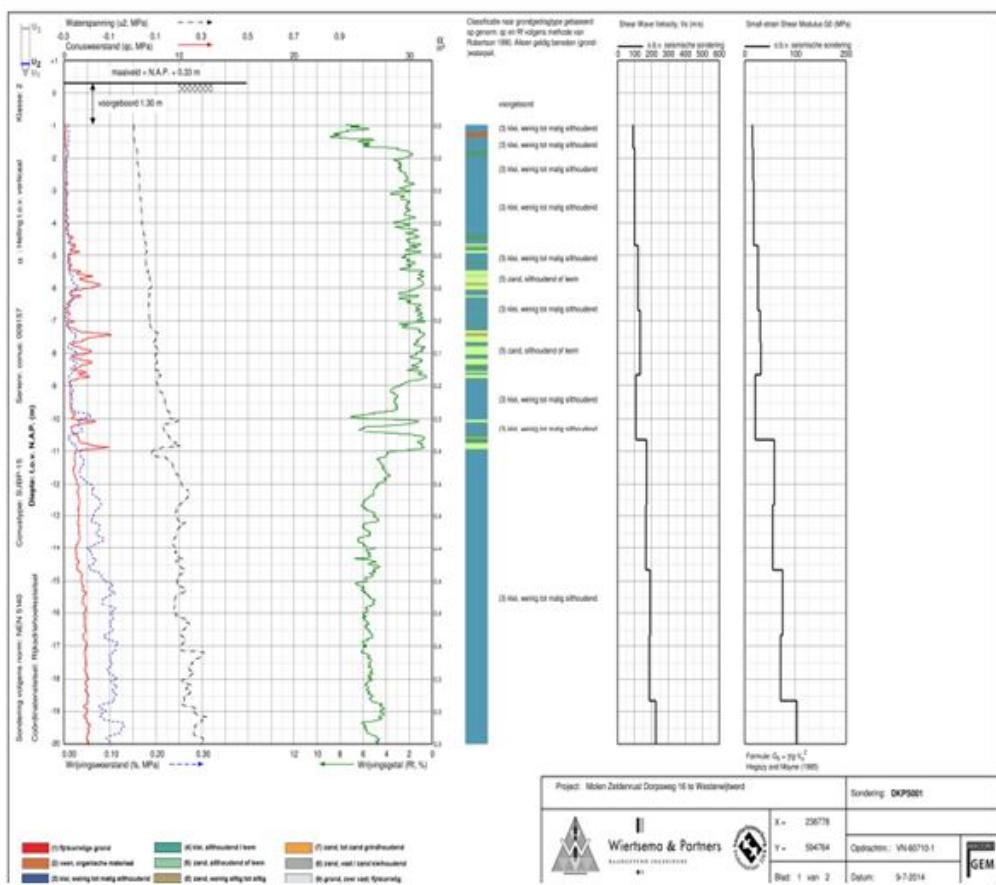
5.8 Conclusions

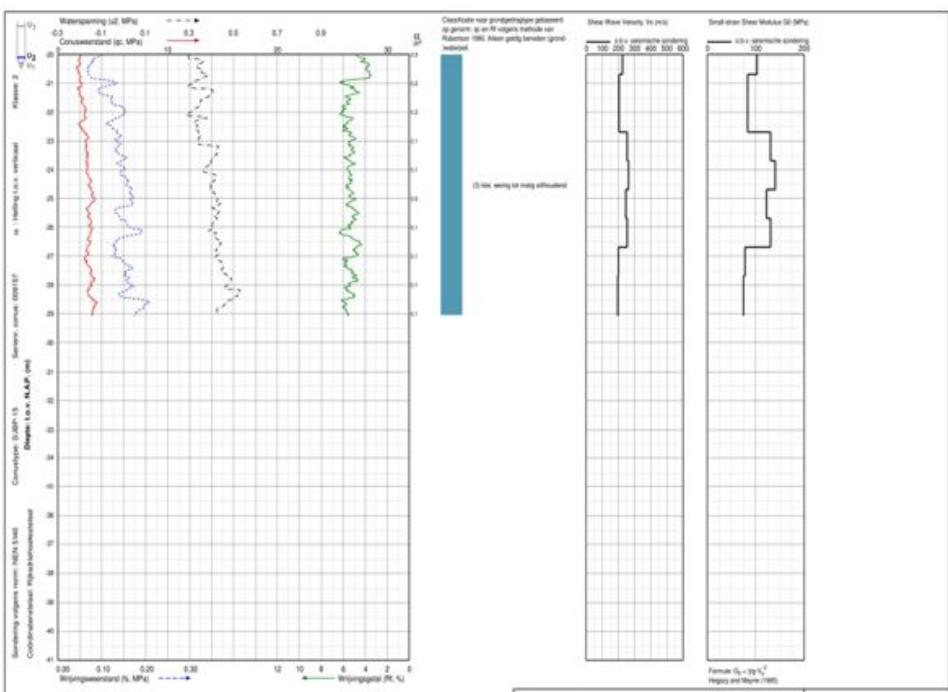
Part I

Appendix

Appendix A

Cone penetration test results





Appendix B

Constitutive model: Nonlinear kinematic hardening model with a Von Mises failure criterion

B.1 Von Mises failure criterion. A definition

The plasticity characteristics correspond to a Von Mises failure criterion - *a total stress analysis* is performed. The reason behind this option relates, on one hand, to the pore pressure dissipation - due to the load rate the volumetric strain is almost zero because the excess pore pressure does not have the chance to dissipate. The chosen criterion suits the goal as it is independent on the hydrostatic pressure and mean stress invariant s .

When considering a point P in stress space representing a vector describing the stress state, it can be projected on the hydrostatic axis with the use of two components: the parallel vector representing the hydrostatic component - which is function of the mean stress invariant I_1 and the perpendicular component, the deviatoric one as a function of the second deviatoric stress invariant J_2 .

introduce the drawing here

$$OP = \sqrt{\sigma_1^2 + \sigma_2^2 + \sigma_3^2} \quad (\text{B.1})$$

$$I_1 = \frac{\sigma_1 + \sigma_2 + \sigma_3}{3} \quad (\text{B.2})$$

$$J_2 = \frac{1}{6}[(\sigma_1^2 + \sigma_2^2) + (\sigma_1^2 + \sigma_3^2) + (\sigma_2^2 + \sigma_3^2)] \quad (\text{B.3})$$

where OP is the vector describing stress state, I_1 is the mean stress invariant and J_2 is the second stress invariant.

For simplification purpose, the stress state can be defined by three invariants - the mean stress invariant s , the second stress invariant T and Lode angle θ - each representing volumetric and deviatoric lengths in stress space.

$$s = \sqrt{3}\sigma_m \quad (\text{B.4})$$

$$t = \sqrt{2}J_2 \quad (\text{B.5})$$

The failure criterion is defined by a function of the aforementioned invariants - it describes a surface in the stress space which delimits safety from failure. Any point within

the stress space situated below the surface attains safety - the points cannot exceed the failure plane because collapse occurs; hence the equation for failure is $F = 0$, where F is the function in discussion.

Generally, a soil sample will reach failure when the total stress Mohr circle attains the strength envelope - which is described as $\tau = S_u$ and it is represented by a straight line dependent on the friction angle and cohesion c . For materials for which the cohesion can be set to $c = S_u$ whilst $\phi = 0$, the Mohr-Coulomb failure envelope turns into a Tresca failure criterion which is parallel to the normal stress axis:

$$\sigma_{max} - \sigma_{min} = 2S_u \quad (B.6)$$

$$F(s, T, \theta) = 0, \text{Mohr - Coulomb failure criterion} \quad (B.7)$$

$$F(s, T) = 0, \text{Drucker - Prager failure criterion} \quad (B.8)$$

$$F(s, \theta) = 0, \text{Tresca failure criterion} \quad (B.9)$$

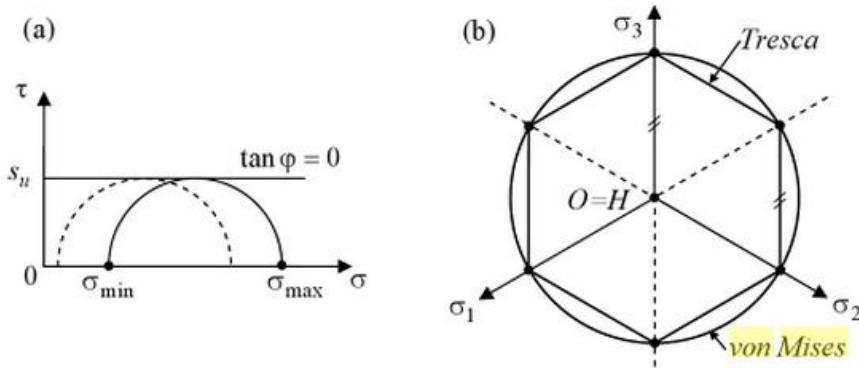


Figure B.1: Tresca and Von mises failure criterion in stress space

Consequently, Drucker-Prager failure criterion represents a smooth version of the Mohr-Coulomb criteria in the sense that it accounts for two of the stress invariants ($F(s, T) = 0$) neglecting Lode angle, θ . This leads to a cone shape of the failure surface.

Furthermore, Von Mises only considers the **second invariant being independent of hydrostatic pressure** and yielding a cylindrical failure shape in three-dimensional stress space. The physical meaning of the mean invariant, I_1 , can relate to the radius of the cross section of failure criterion - the larger the I_1 , the larger the radius and thus the evolution of the failure surface follows a conical profile. Given von Mises does not require this term, it becomes clear the cylindrical shape of the failure envelope obtained with a constant radius. Moreover, when mapping the deviatoric component - that associates with a normal plane on the failure surface - it stands out that there is no volume change. Thus, the undrained behaviour of the clay layer can be successfully expressed in terms of von Mises failure criterion.

B.2 Constitutive model according to Lemaitre and Chaboche: Nonlinear kinematic hardening rules

The formulation for plasticity criterion is always expressed in the following form and it is important to mention that the *plasticity function is linear* and depends exclusively on

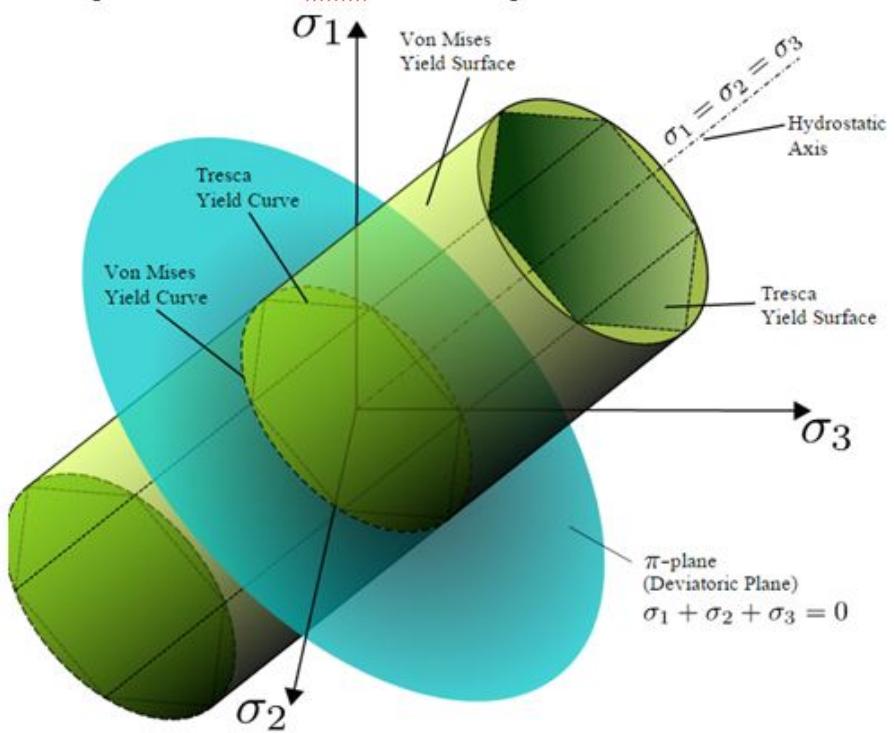


Figure B.2: Von mises failure criterion in 3D stress space

the second invariant J_2 as it follows:

$$f = J_2(\sigma - X)k \quad (\text{B.10})$$

where X represents the kinematic hardening and it is assumed zero in initial state, k hardening modulus and sigma introduces the stress tensor. The hypothesis of proportionality between the accumulative plastic strain increment $d\varepsilon_p$ and X is replaced by a term that introduces the fading memory effect present on the stress path:

$$dX = \frac{2}{3}Cd\varepsilon_p - \gamma X dp \quad (\text{B.11})$$

One can notice that the kinematic hardening depends on characteristic material coefficients such as C which represents the initial kinematic hardening modulus while γ introduces the inverse proportionality between the kinematic hardening and plastic deformation. Including normality hypothesis and the consistency condition $df = 0$ the equation for the incremental accumulative plastic strain becomes:

$$d\varepsilon_p = d\lambda \frac{\partial f}{\partial \sigma} = \frac{H(f)}{h} \left\langle \frac{\partial f}{\partial \sigma} \middle| d\sigma \right\rangle \frac{\partial f}{\partial \sigma} \quad (\text{B.12})$$

Following, the hardening modulus turns into kinematic stress dependent factor:

$$h = \frac{2}{3}C \frac{\partial f}{\partial \sigma} \left| \frac{\partial f}{\partial \sigma} - \gamma X \right| \left(\frac{\partial f}{\partial \sigma} \left(\frac{2}{3} \frac{\partial f}{\partial \sigma} \right) \left| \frac{\partial f}{\partial \sigma} \right| \right)^{1/2} \quad (\text{B.13})$$

Considering von Mises assumption where $d\lambda = dp$ and inserting in the above equation the hardening modulus becomes:

$$h = C - \frac{3}{2}\gamma X \left| \frac{\sigma' - X'}{k} \right| \quad (\text{B.14})$$

Clearly it can be stated that increase of the kinematic hardening X induces a decrease of hardening modulus k .

A generalized nonlinear kinematic hardening model would replace the associated plasticity with another flow potential which is different from loading surface. Additionally, other set of von Mises material assumptions yield:

$$d\varepsilon_p = \frac{\partial F}{\partial \sigma} d\lambda = \frac{3}{2} \frac{(\sigma' - X')}{J_2} dp \quad (\text{B.15})$$

$$d\varepsilon_p = \frac{\partial F}{\partial \sigma} d\lambda = d\varepsilon_p - \frac{3}{2} \frac{\gamma}{C} X dp \quad (\text{B.16})$$

However, when plastic flow is considered the function f becomes zero ($f = 0$), the dissipation potential can be calculated from the initial equation. Hence:

$$F = J_2(\sigma - X) + \frac{3}{4} \frac{\gamma}{C} X |X - k| = f + \frac{3}{4} \frac{\gamma}{C} X |X| \quad (\text{B.17})$$

becomes

$$F = \frac{3}{4} \frac{\gamma}{C} X |X| \quad (\text{B.18})$$

Assuming $dX = 0$ leads to maximum value of the second invariant J_2 then the shape boundaries of the function can be calculated:

$$J_2(X) = \left(\frac{3}{4} X' |X'| \right)^{1/2} \leq \frac{C}{\gamma} \quad (\text{B.19})$$

* $X' = X$ because of plastic incompressibility and initial condition $X(0) = 0$.

Therefore, the dissipation potential or backstress, as it is referred in other studies, should be limited within a cylinder with radius $\sqrt{\frac{2}{3}}C/\gamma$ whilst the boundaries of the yield stress describe a cylinder of radius $\sqrt{\frac{2}{3}}\sigma_y$ where γ_y represents the maximum stress. Applying on a clay soil characterized by an undrained shear strength, the maximum stress can be expressed as:

$$\sigma_y = \sqrt{3}S_u \quad (\text{B.20})$$

$$\sigma_y = \frac{C}{\gamma} + \sigma_o \quad (\text{B.21})$$

$$\gamma = \frac{C}{\sqrt{3}S_u - \gamma_o} \quad (\text{B.22})$$

The equations incorporate the term C which refers to Young's modulus for very small strains describing the elastic stiffness when low-amplitudes are encountered and it can be computed using Roberston method based on shear wave velocity or through empirical correlations (Roberston and Campanella, 1983, Seed et al, 1986).

** In order to avoid the confusion between the hardening parameter (here noted with γ) and the shear strain (also γ), the notation of the hardening parameter is changed to K .

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Appendix C

Description of Darendeli hyperbolic model

The study presents a modified hyperbolic model which describes the normalized modulus reduction curve; the model starts from the example created by **Hardin and Drnevich** being adjusted through a curvature coefficient, a . The role of the coefficient is given by its name as it influences the curvature of the outcome. The hyperbolic model is expressed using the following equation:

$$\frac{G}{G_{max}} = \frac{1}{1 + (\frac{\gamma}{\gamma_{ref}})^a} \quad (C.1)$$

The material damping curves consider *Masing behaviour* which proves that the stress-strain path associated to a cyclic loading can be related to the monotonic loading path, also known as the backbone curve. **Masing(1926)** states that the backbone curve serves to the creation of the hysteresis loop; the curve is scaled by a factor of two and flipped with respect to both horizontal and vertical axis to simulate the unloading path. The assumption is valid for an uniform cyclic loading, unlike the real earthquake signals; however it has its own limitations in modelling nonlinear soil behaviour. A schematization of Masing behaviour assumption can be seen in Figure C.1; the dashed line represents the monotonic loading response which coincides with the initial path of the cyclic loading.

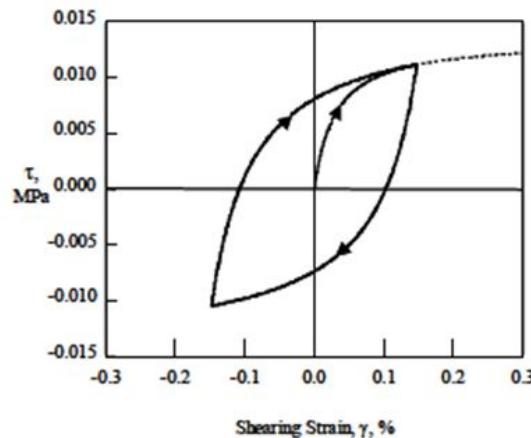


Figure C.1: Hysteresis loop estimated by modelling stress-strain reversals for two-way cyclic loading according to Mass behaviour

The material damping ratio is expressed as the ratio of the dissipated energy to stored

strain energy during a loading cycle; combining this concept together with Masing behaviour, the area inside the hysteresis loop (A_L) can be determined through the integration of the stress-strain curve described during one loading cycle.

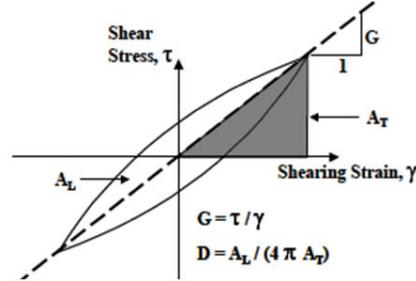


Figure C.2: Calculation of damping ratio using a hysteresis loop

$$A_L = 8 \left(\int \tau d\gamma \right) - \frac{1}{2} \tau \gamma \quad (\text{C.2})$$

$$A_T = \frac{1}{2} \tau \gamma \quad (\text{C.3})$$

$$D_{eq} = \frac{A_L}{4\pi A_T} \quad (\text{C.4})$$

Combining all the equations previously presented, Masing-behaviour damping ratio can be expressed:

$$D_{masing} = \frac{4}{\pi} \frac{\int \frac{\gamma}{1 + (\frac{\gamma}{\gamma_{ref}})^a} d\gamma - \frac{1}{2} \left(\frac{\gamma^2}{\gamma_{ref}} \right)^a}{1 + \left(\frac{\gamma}{\gamma_{ref}} \right)^a} \quad (\text{C.5})$$

For the final formulation of the material damping ratio, Darendeli uses fitting parameters and functions for a better matching with the experimental observations. The equation of the material damping curve is then expressed as a function of two main parameters (b and D_{min}):

$$D = b \left(\frac{G}{G_{max}} \right)^{0.1} * D_{masing} + D_{min} \quad (\text{C.6})$$

Parameter b represents a scaling factor whilst D_{min} comprises the impact on the damping curve caused by confining pressure, loading frequency and soil plasticity. The influence of D_{min} is most visible through the shift within small-strain damping ratio area; the curve does not touch the horizontal axis of the plot - this means that no matter how small the strain level is, the soil will experience damping.

In conclusion, the modified hyperbolic model described by Darendeli for the normalized modulus reduction curve and material damping curve relies on four parameters: a, b, γ_{ref} and D_{min} .

Appendix D

Input parameter - Stresses calculation

The total vertical stress is calculated both in terms of soil density (D.1), in [Mg/m^3] and soil unit weight (D.2), in [kN/m^2], at a depth z as it follows:

$$p(z) = p_0 + \int_0^z \rho(z) dz \quad (\text{D.1})$$

$$\sigma_v = \gamma_{soil} * z \quad (\text{D.2})$$

The water level is considered at 1 m below surface level, hence the pore pressure equation is:

$$u = \gamma_{water} * z_{water} \quad (\text{D.3})$$

The effective vertical stress can now be determined based on Terzaghi's principle:

$$\sigma'_v = \sigma_v - u \quad (\text{D.4})$$

The determination of the horizontal stress is a subject still uncertain, however empirical relations can be used to approximate the value; according to Jaky (1948) it yields that for normally consolidated clays:

$$K_o = 1 - \sin \phi' \quad (\text{D.5})$$

This coefficient is expressed in terms of effective stresses as well because it depends on the material and the geological history. The assumption of a typical Dutch clay soil leads to certain parameters such as:

- density: $\rho = 1750 kg/m^3$
- cohesion $c = 2 kPa$
- friction angle $\phi = 22.5 \text{ deg}$
- lateral pressure coefficient $K_o = 1 - \sin \phi' = 0.617$

Even though there are empirical relations which directly calculate the total coefficient of lateral pressure, it is preferable to use effective stresses since water is isotropic and it can be easily added to obtain the total horizontal stress; hence:

$$\sigma_h^* = K_0 * \sigma_v^* \quad (\text{D.6})$$

$$\sigma_h = \sigma_h^* + u \quad (\text{D.7})$$

Given the supposition of no volume changes specific to the undrained conditions, the isotropic effective stresses remain constant which means that the mean effective stress remains constant as well:

$$\sigma_o^* = \frac{1}{3}(\sigma_z^* + 2\sigma_x^*) \quad (\text{D.8})$$

Appendix E

Determination of undrained shear strength value

The calculations continue in terms of effective stresses and head to the estimation of the stiffness parameters, mainly Young's modulus and undrained shear strength. Mohr-Coulomb failure criterion will serve for the estimation of the strength parameters; the straight line represents the failure envelope within the plot of the shear strength against normal effective stress and it is described by the following equation:

$$\tau' = c + \sigma' \tan \phi' \quad (\text{E.1})$$

The undrained shear strength can be determined considering that drainage does not occur while loading the sample with a confining pressure. This way, the failure envelope for total stress becomes a straight horizontal line. For instance, in the figure below, circle P represents the stress conditions at failure for consolidated sample at pressure σ_3 then sheared to failure where:

$$\sigma'_1 = [\sigma_3 + (\Delta d)_f] - (\Delta u_d)_f = \sigma_1 - (\Delta u_d)_f \quad (\text{E.2})$$

$$\sigma'_3 = \sigma_3 - (\Delta u_d)_f \quad (\text{E.3})$$

where $(\Delta u_d)_f$ is the pore pressure of the specimen at failure.

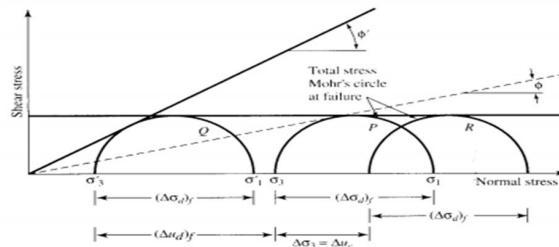


Figure E.1: Mohr's circles according to undrained conditions

Finally, the undrained shear strength is calculated as:

$$S_u = \frac{\sigma'_1 - \sigma'_3}{2} \quad (\text{E.4})$$

Scientific literature exposes several formulae used to determine the value of the undrained shear strength. In the order displayed on the graph the values were calculated as it follows:

1. *Measurements (CRUX)* - Den Haan (2011) treats the problem in his article - based on this article, Crux Engineering develops a Plaxis model to validate the equation for the shear strength leading to a set of formulae as a function of the normalized stress given in 3.2:

For the current situation, considering the normalized shear stress to be 40kPa as characteristic, the undrained shear strength equation becomes:

$$S_u = 2.8 + 0.37 * \sigma'_v \quad (\text{E.5})$$

Classification	Normalized undrained shear strength	Undrained shear strength
[]	[kPa]	[kPa]
Organic clay (medium)	25	$c_{u,\text{ref}} = s_u = 2.8 + 0.22\sigma'_v$
Clay, slightly sandy(weak)	40	$c_{u,\text{ref}} = s_u = 2.8 + 0.37\sigma'_v$
Clay,slightly sandy (medium)	55	$c_{u,\text{ref}} = s_u = 2.8 + 0.52\sigma'_v$
Clay, slightlty sandy (dense)	80	$c_{u,\text{ref}} = s_u = 2.8 + 0.77\sigma'_v$

Table E.1: Undrained shear strength equations according to Den Haan

2. *Measurements (Mesri)* - Many researchers focused on the determination of the undrained shear strength based on the CPT results. Numerous equations relate the strength to the plasticity index of the clays. However, Mesri (1975, 1989) found that the undrained shear strength of normally consolidated and lightly overconsolidated clays (overconsolidation ratio less than 2) could be expressed practically independent of plasticity by combining Bjerrum's (1973) proposed relationship between S_u/σ'_p and plasticity with Bjerrum's correction factor μ . This relationship led to the following equation:

$$S_u = 0.22 * \sigma'_v \quad (\text{E.6})$$

3. *Measurements (MC)* - Another way of determining the undrained shear strength value takes into account the Mohr-Coulomb failure criterion, as it was established previously:

$$S_u = \frac{\sigma'_v - \sigma'_h}{2} \quad (\text{E.7})$$

4. *Empirical Mesri* - the same formulae presented above, only applied to the parameters determined empirical.
5. *Empirical (Den Haan formula)* - same formulae used by Crux Engineering, again, applied to the empirical parameters.
6. *Empirical [PI]* - The CPT results represent important data to derive many soil parameters. Various equations were developed to better capture the link between the undrained shear strength and soil properties. A part of the equations express su as a function of the plasticity index. The typical Dutch clay soil is considered to have a plasticity index PI=25% - 30% leading to the following formulae:

$$S_u = (0.11 + 0.01 * PI) * \sigma'_v \quad (\text{E.8})$$

7. *CPT - Mayne(2014)* gathers many equations for the interpretation of seismic piezo-cone tests. It is common to relate the shear strength to characteristics such as: plasticity index, pore pressure, stress history, mode of testing and so on. The net cone resistance may be used to profile the peak undrained shear strength as well as the measured excess pore pressures; these two being the most frequent methods of determination also known as direct expressions.

$$S_u = \frac{q_t - u_2}{N_{kt}} \quad (\text{E.9})$$

$$S_u = \frac{u_2 - u_T}{N_{\Delta u}} \quad (\text{E.10})$$

where q_t - net cone resistance, u_2 - penetration pore water pressure, u_0 - water pressure behind the cone tip, N_{kt} - factor depending on the mode of testing (vane test, triaxial compression/extension, etc) with an usual value of $N_{kt} = 13.6 \pm 1.9$ for soft clays (Low et al, 2010), $N_{\Delta u}$ - factor depending on the pore pressures, approximated for soft clays as $N_{\Delta u} = 6.8 \pm 2.2$ (Low et al, 2010).

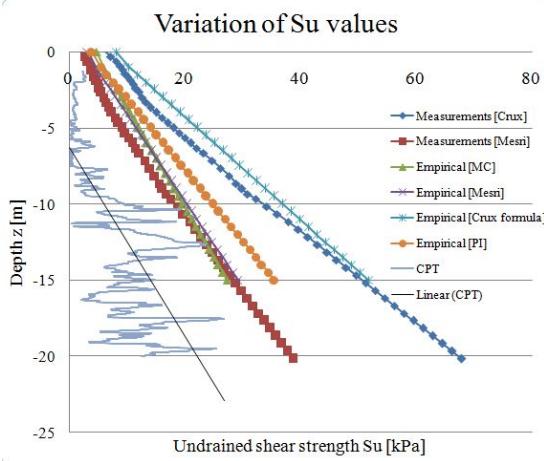


Figure E.2: Various values of the undrained shear strength S_u

Appendix F

Abaqus Input parameters - Empirical and Measurements

Depth z [m]	ELASTIC			PLASTIC PARAMETERS			Shear modulus G0 [kPa]	Shear wave velocity Vs [m/s]	Additional	
	Young's modulus E0 [kPa]	Poisson's ratio νu	Max yield stress σy [kPa]	Yield stress at zero plastic strain σ00 [kPa]	Young's modulus [SS] [kPa]	Hardening parameter K [-]				
0	8560	0.48	7.41	0.74	8560.00	1283.00	2891.9	40.08		
-1	14480		12.54	1.25	14480.00	1283.00	4891.9	52.13		
-2	20400		17.67	1.77	20400.00	1283.00	6891.9	61.88		
-3	26320		22.79	2.28	26320.00	1283.00	8891.9	70.28		
-4	32240		27.92	2.79	32240.00	1283.00	10891.9	77.79		
-5	38160		33.05	3.30	38160.00	1283.00	12891.9	84.63		
-6	44080		38.17	3.82	44080.00	1283.00	14891.9	90.96		
-7	50000		43.30	4.33	50000.00	1283.00	16891.9	96.87		
-8	55920		48.43	4.84	55920.00	1283.00	18891.9	102.45		
-9	61840		53.56	5.36	61840.00	1283.00	20891.9	107.73		
-10	67760		58.68	5.87	67760.00	1283.00	22891.9	112.77		
-11	73680		63.81	6.38	73680.00	1283.00	24891.9	117.60		
-12	79600		68.94	6.89	79600.00	1283.00	26891.9	122.23		
-13	85520		74.06	7.41	85520.00	1283.00	28891.9	126.69		
-14	91440		79.19	7.92	91440.00	1283.00	30891.9	131.00		
-15	97360		84.32	8.43	97360.00	1283.00	32891.9	135.18		
-16	103280		89.44	8.94	103280.00	1283.00	34891.9	139.23		
-17	109200		94.57	9.46	109200.00	1283.00	36891.9	143.16		
-18	115120		99.70	9.97	115120.00	1283.00	38891.9	146.99		
-19	121040		104.82	10.48	121040.00	1283.00	40891.9	150.72		
-20	126960		109.95	11.00	126960.00	1283.00	42891.9	154.37		
-21	132880		115.08	11.51	132880.00	1283.00	44891.9	157.92		
-22	138800		120.20	12.02	138800.00	1283.00	46891.9	161.40		
-23	144720		125.33	12.53	144720.00	1283.00	48891.9	164.81		
-24	150640		130.46	13.05	150640.00	1283.00	50891.9	168.15		
-25	156560		135.58	13.56	156560.00	1283.00	52891.9	171.42		
-26	162480		140.71	14.07	162480.00	1283.00	54891.9	174.63		
-27	168400		145.84	14.58	168400.00	1283.00	56891.9	177.78		
-28	174320		150.97	15.10	174320.00	1283.00	58891.9	180.88		
-29	180240		156.09	15.61	180240.00	1283.00	60891.9	183.93		
-30	186160		161.22	16.12	186160.00	1283.00	62891.9	186.92		

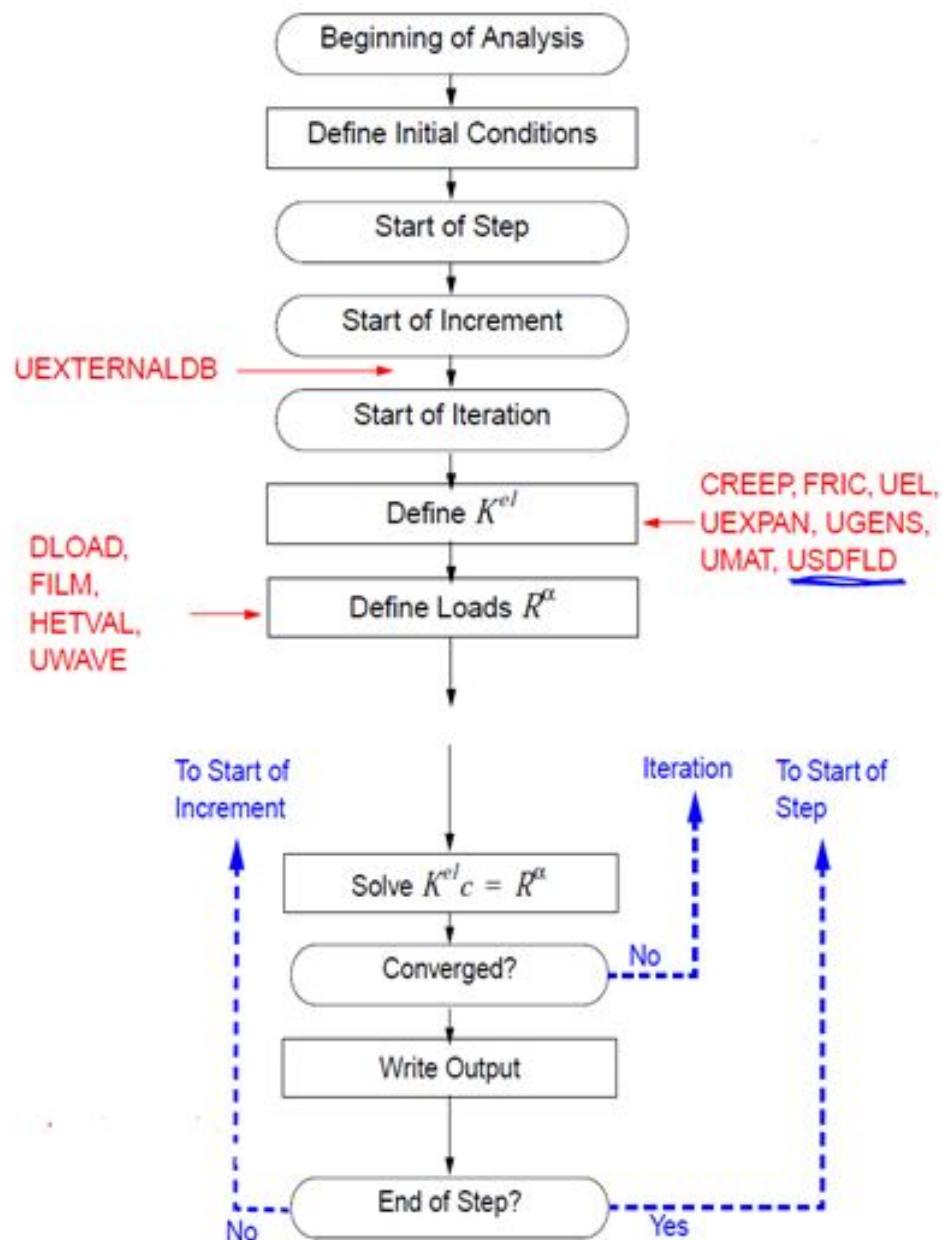
Figure F.1: Input parameters empirically determined

Depth z [m]	ELASTIC		PLASTIC PARAMETERS			Shear modulus G0 [kPa]	Additional	
	Young's modulus E0 [kPa]	Poisson's ratio vu [-]	Max yield stress σ_y [kPa]	Yield stress at zero plastic strain σ_0 [kPa]	Young's modulus [SS] [kPa]		Shear wave velocity Vs [m/s]	
0	29378.88		7.82	0.78	29378.88	3288.60	7817.1	65.90
-1	12844.86		7.82	0.78	12844.86	2016.46	7817.1	65.90
-2	13495.66		7.82	0.78	13495.66	1708.58	7817.1	65.90
-3	29413.80		7.82	0.78	29413.80	1491.33	7817.1	65.90
-4	35296.56		6.69	0.67	35296.56	1391.46	6690.0	66.78
-5	51683.94		6.69	0.67	51683.94	1322.88	6690.0	66.78
-6	51683.94		6.69	0.67	51683.94	1260.75	6690.0	66.78
-7	60281.23		7.03	0.70	60281.23	1265.75	7029.0	68.45
-8	60281.23		7.03	0.70	60281.23	1207.68	7029.0	68.45
-9	40143.00		7.03	0.70	40143.00	1154.71	7029.0	68.45
-10	128000.00		7.03	0.70	128000.00	1106.18	7029.0	68.45
-11	128000.00		15.32	1.53	128000.00	2397.65	15319.7	101.06
-12	106247.40		15.32	1.53	106247.40	2271.10	15319.7	101.06
-13	101800.00		15.32	1.53	101800.00	2157.24	15319.7	101.06
-14	101800.00	0.5	18.38	1.84	101800.00	2463.56	18383.6	101.06
-15	135870.27		18.38	1.84	135870.27	2288.83	18383.6	101.06
-16	135870.27		18.38	1.84	135870.27	2137.25	18383.6	101.06
-17	129305.52		26.92	2.69	129305.52	3029.11	26918.7	122.29
-18	129305.52		26.92	2.69	129305.52	2846.63	26918.7	122.29
-19	188110.31		26.92	2.69	188110.31	2684.90	26918.7	122.29
-20	188110.31		26.92	2.69	188110.31	2540.55	26918.7	122.29
-21	150827.01		26.92	2.69	150827.01	2410.93	26918.7	122.29
-22	150827.01		26.92	2.69	150827.01	2293.89	26918.7	122.29
-23	237602.06		31.40	3.14	237602.06	2553.03	31396.5	132.07
-24	254636.38		31.40	3.14	254636.38	2387.16	31396.5	132.07
-25	223498.92		31.40	3.14	223498.92	2241.53	31396.5	132.07
-26	238925.93		31.40	3.14	238925.93	2112.65	31396.5	132.07
-27	143016.19		20.91	2.09	143016.19	1313.07	20907.8	107.78
-28	137296.13		20.91	2.09	137296.13	1267.71	20907.8	107.78

Figure F.2: Input parameters determined from field measurements

Appendix G

Flow chart - Abaqus subroutines



Note: The squared-boxes represent an action taken during the analysis. The round-shaped boxes represent a decision in the code or at a specific state (i.e. beginning of the increment) during the analysis.

Appendix H

User subroutine implemented in analysis

The current Appendix presents the subroutine code written to introduce the undrained shear strength S_u as a function of vertical effective stress; additionally, the undrained shear strength contributes to the calculation of the Young's modulus E_0 .

```
subroutine usdfld(field,statev,pnewdt,direct,t,celent,tim
1 cmname,orname,nfield,nstatv,noel,npt,layer,kspt,kstep,k
2 ndi,nshr,coord,jmac,jmtyp,matlayo,laccflg)

include 'aba_param.inc'

character*80 cmname,orname
character*8 flgray(15)
dimension field(nfield),statev(nstatv),direct(3,3),t(3,3)
& coord(*),jmac(*),jmtyp(*)
dimension array(15),jarray(15)
! Call and read current stresses
call getvrm('SP',array,jarray,flgray,jrcd,
&jmac, jmtyp, matlayo, laccflg)
S22=ARRAY(2)
c
if (kstep.eq.1 .and. kinc.eq.1) then
!      read y coordinates at first increment
y = coord(2)
!      define depth.
h= 30.0 - y
! Define vertical effective stress
SV=S22 - 10 * h
! Update undrained shear strength value
Su=2.8+0.37*ABS(SV)
E = 2000*Su
!      a=2000
field(1)=E
field(2)=Su
else
```

```
!           assign initial values computed in the first incre
field(1) = statev(1)
field(2) = statev(2)
end if
!
statev(1)=field(1)
statev(2)=field(2)
!      If error, write comment to .DAT file:
if(JRCD.NE.0)then
write(6,*) 'REQUEST_ERROR_IN_USDFLD_FOR_ELEMENT_NUMBER',
& NOEL,'INTEGRATION_POINT_NUMBER',NPT
endif
!
return
end
```

Appendix I

Newmark integration schemes

For this particular analysis, an implicit direct integration scheme was selected - this means that the set of equations concerning the set of nonlinear equations of motion are solved at each time step Δt involving both the current and the later state of the system. On the other hand, an explicit analysis finds the solution for the later state of the system starting from the current one. The method is appropriate for this specific application as it successfully solves problems involving nonlinearity, both material and geometric, contact and moderate energy dissipation.

A significant aspect when performing such analyses relates to the stability of the calculation which translates into the size of the time increment. An implicit direct integration scheme is unconditionally stable; it means that there is no limitation in defining the time step size thus, the user can adjust the accuracy of the analysis according to the application. However, care must be paid when establishing the size of the time increment because it influences the energy dissipation as well as the transmission of high frequencies throughout the model.

Abaqus/Standard uses the Hilbert-Hughes-Taylor time integration method which is an extension of the Newmark β method [45]. It basically controls the numerical damping within the system which might rise due to the energy dissipation mechanisms associated with different operator types (for instance, backward Euler operator is more dissipative than second-order Hilbert-Hughes-Taylor). The general equation for the integration method is:

$$\beta = 0.25(1 - \alpha)^2 \quad (\text{I.1})$$

$$\gamma = 0.5 - \alpha \quad (\text{I.2})$$

where α is the time integrator parameter $[-0.5 < \alpha < 0]$, β and γ are Newmark's method parameters.

$\alpha = 0$	No artificial damping; energy preserving; Leads to trapezoidal rule/Newmark's method
$\alpha = -0.05$	Negative damping; it produces enough artificial damping to ensure the automatic time step procedure to work smoothly;

Table I.1: Time integrator parameter

This control parameter was set to zero to obtain the Newmark's- β method characteristics leading to the parameters $\beta \geq 1/4$ and $\gamma \geq 1/2$ and an unconditionally stable analysis

- thus the implicit integration scheme does not encounter any numerical damping. This way, the user can define the time step instead of opting for an automatic time increment associated with an artificial damping - the accuracy can be manipulated manually.

Appendix J

FEM stability in dynamic calculations

The accuracy of such nonlinear problem dealing with wave propagation is controlled by two factors - node spacing in the FE model Δh and the time step Δt . The spacing is directly related to the wavelength whilst the time step depends on the fundamental period of the system. The first condition can be expressed as:

$$\Delta h \leq \frac{\lambda_{min}}{10} = \frac{1}{10} \frac{v}{f_{max}} \quad (J.1)$$

where Δh - maximum spatial grid, λ_{min} - smallest wavelength; v - average shear wave velocity (usually of the softer soil); f_{max} - maximum appropriate frequency (which can be considered 10Hz for a seismic analysis). This equation assumes that 10 nodes/wavelength should suffice, otherwise high frequencies might be overlooked leading to numerical damping. Soils that might encounter stiffness degradation need a smaller element size in order to better capture the behaviour. Table J.1 shows the values used in calculation.

Parameter	Value	Unit
v	132	m/s
f	10	Hz
λ_{min}	13.2	m
Δh	1.32	m
Δh_{final}	1	m

Table J.1: Calculation of final mesh size

The second condition has its own two criterion as it follows: stability in terms of time integration and stability related to the FEM. Within an implicit time integration scheme, the time step size decreases as the analysis diverges or the convergence rate is slow. The first criterion suggests the introduction of an upper bound applied to the frequencies that relates to the smallest fundamental period of the system and it is written:

$$\Delta t = \frac{T_n}{10} \quad (J.2)$$

The second criteria is connected to the FE method that states that during an analysis the nodes are covered in a successive order. If the time step is too large, two nodes can be

reached concomitantly - this violates the fundamental wave propagation condition leading to instability. Thus:

$$\Delta t = \frac{\Delta h}{v} \quad (\text{J.3})$$

here v - highest shear wave velocity. The final time step size is 0.005 sec according to Table J.2:

Parameter	Value	Unit
V_s	132	m/s
H	30	m
T_n	0.91	s
Δt_1	0.091	sec
V_{max}	180	m/s
Δh	1	m
Δt_2	0.0056	s
Δt_{final}	0.005	s

Table J.2: Calculation of final time step

For the mesh elements, four-node quad elements (CPE4) are used to model the soil using the plane strain formulation of the quad-element. The element connectivity uses a counterclockwise pattern for the previously-described node numbering scheme (see Figure 4.1). The soil elements in each layer are assigned the material tag of the material object corresponding to that layer. A unit thickness is used in all examples for simulating the 1D condition. The self-weight of the soil is considered as a body force acting on each element. The body force is set as the unit weight of the soil in each layer, which is determined from the respective mass density input value.

Appendix K

NERA - Iwan Mroz material model description

The information is according to NERA manual [51].

2.3 Nonlinear and Hysteretic Model

As illustrated in Fig. 3, Iwan (1967) and Mroz (1967) proposed to model nonlinear stress-strain curves using a series of n mechanical elements, having different stiffness k_i and sliding resistance R_i . Hereafter, their model is referred to as the IM model. The sliders have increasing resistance (i.e., $R_1 < R_2 < \dots < R_n$). Initially the residual stresses in all sliders are equal to zero. During a monotonic loading, slider i yields when the shear stress τ reaches R_i . After having yielded, slider i retains a positive residual stress equal to R_i . As shown in Fig. 4, the stress-strain curve generated by the IM model for two sliders (i.e., $n = 2$) is piecewise linear, whereas the corresponding slope and tangential modulus H varies in steps. In the case of an IM model with n sliders, the stress increment $d\tau$ and strain increment $d\gamma$ are related through:

$$\frac{d\tau}{d\gamma} = H \quad (9)$$

where the tangential modulus H is:

$$H = \begin{cases} H_1 = k_1 & \text{if } 0 \leq \tau < R_1 \\ H_2 = (k_1^{-1} + k_2^{-1})^{-1} & \text{if } R_1 \leq \tau < R_2 \\ H_{n-1} = (k_1^{-1} + k_2^{-1} + \dots + k_{n-1}^{-1})^{-1} & \text{if } R_{n-2} \leq \tau < R_{n-1} \\ H_n = (k_1^{-1} + k_2^{-1} + \dots + k_{n-1}^{-1} + k_n^{-1})^{-1} & \text{if } R_{n-1} \leq \tau < R_n \\ 0 & \text{if } \tau = R_n \end{cases} \quad (10)$$

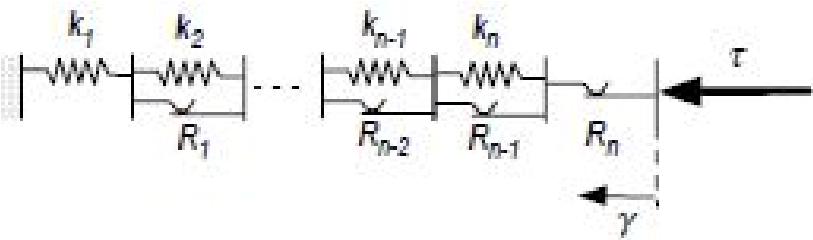


Figure 3. Schematic representation of stress-strain model used by Iwan (1967) and Mroz (1967).

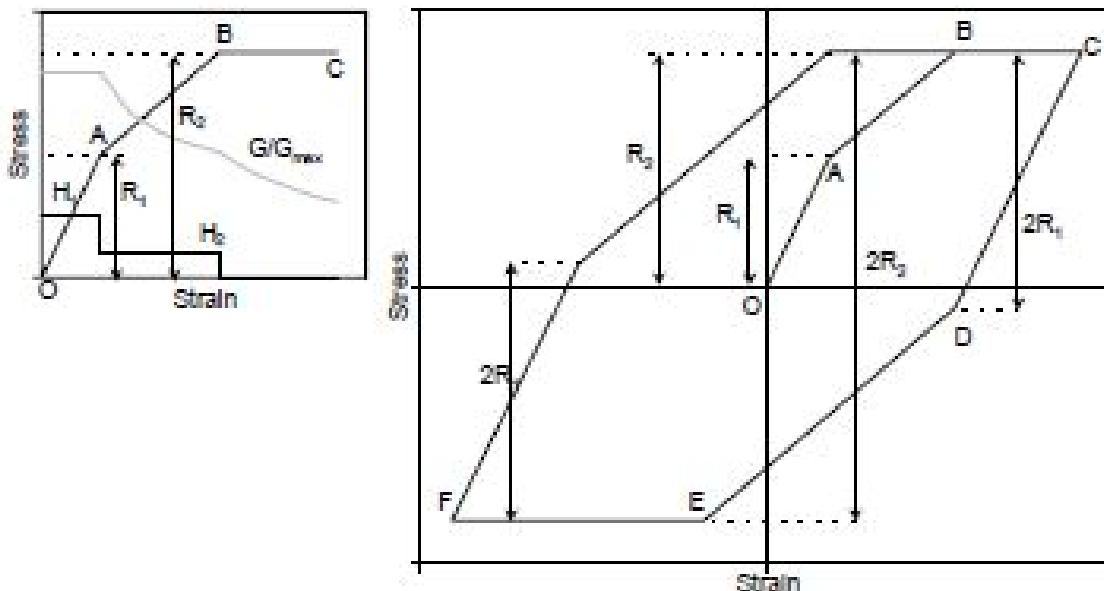


Figure 4. Backbone curve (left) during loading and hysteretic stress-strain loop (right) of IM model during loading-unloading cycle.

As shown in Fig. 4, the stress-strain curve during a loading is referred to a backbone curve. When the loading changes direction (i.e., unloading), the residual stress in slider j decreases; slider j yields in unloading when its residual stress reaches $-R_j$, i.e., after the stress τ decreases $-2R_j$. Instead of yield stress, it is convenient to introduce the back stress α_j ; slider j yields in loading and unloading when τ becomes equal to $\alpha_j + R_j$ and $\alpha_j - R_j$, respectively. The IM model assumes that parameters R_j are constant whereas the back stress α_j varies during loading processes. As shown in Fig. 4, the cyclic stress-strain curves is hysteretic, and follows Masing similitude rule (Masing, 1926). Curve CDEF is obtained from curve OABC by a similitude with a factor of 2.

The stress-strain curves of the IM model can be calculated using the algorithm of Table 1. this algorithm returns an exact value of stress τ independently of the strain increment amplitude $\Delta\gamma$. At first, the algorithm attempts to calculate the stress increment $\Delta\tau$ using the strain increment $\Delta\gamma$ and modulus H_j . If $\tau + \Delta\tau \leq \alpha_j + R_j$ (loading), then $\tau + \Delta\tau$ is accepted; the stress is smaller than the yield stress of slider 1. If $\tau + \Delta\tau > \alpha_j + R_j$, the strain increment $\Delta\gamma$ was too large, and the stress $\tau + \Delta\tau$ exceeded the yield stress of slider 1; the tangential modulus of the stress-strain response was H_j only for the stress increment $\Delta\tau = \alpha_j + R_j - \tau$ and strain increment $\Delta\gamma/H_j$. The algorithm is reapplied to slider 2. Instead of slider 1, using the remaining strain increment $\Delta\gamma - \Delta\gamma/H_j$. The algorithm is repeated for other sliders until $\tau + \Delta\tau$ becomes smaller than the yield stress of slider j . Each time, the remaining strain increment referred to as $\Delta\gamma$ in Table 1 becomes smaller. At this time,

backstresses of sliders 1 to $j-1$ are updated. The algorithm of Table 1 works for loading and unloading through the use of variable x , which is set to 1 for loading and -1 for unloading, respectively.

Table 1. Algorithm for stress calculation for given strain increment.

Given τ , $\Delta\gamma$, α_i , R_i , and H_i for $i = 1, \dots, n$	
$\Delta x = \Delta\gamma$	
If $\Delta\gamma > 0$ then $x = 1$ else $x = -1$	loading or unloading
For $i = 1$ to n	
$\Delta\tau = H_i \Delta x$	$\Delta\tau$ trial stress increment
If $ \tau + \Delta\tau - \alpha_i \leq R_i$ then	τ inside slider i
$\tau \leftarrow \tau + \Delta\tau$	
Go to "	
End If	
$\Delta\tau = \alpha_i + x R_i - \tau$	correct $\Delta\tau$
$\tau \leftarrow \tau + \Delta\tau$	update τ
$\Delta X \leftarrow \Delta X - \Delta\tau / H_i$	left over strain increment
Next i	
• If $i > n$ then $i = n$	avoid $n+1$
If $ \tau - \alpha < R_i$ or $i = n$ then $i = i-1$	τ strictly inside slider i
For $j = 1$ to i	
$\alpha_j = \tau - x R_j$	update α_j
Next j	

The nonlinear backbone curve of Fig. 4 can be described in terms a variation of secant shear modulus G with shear strain γ , especially by n data points, i.e., $G_i \gamma_i$, $i = 1, \dots, n$. In this case, the tangential shear modulus H_i is related to the secant modulus G_i as follows:

$$H_i = \frac{G_{i+1}Y_{i+1} - G_i Y_i}{Y_{i+1} - Y_i}, \quad i = 2, \dots, n-1 \quad \text{and} \quad H_1 = 0 \quad (11)$$

Assuming that the backstress α_i is initially equal to zero, R_i is:

$$R_i = G_i Y_i, \quad i = 1, \dots, n \quad (12)$$

Equations 11 and 12 imply that the maximum shear resistance is $R_o = G_n Y_n$, i.e., is specified by the last point of the G/γ -curve. When the $G/G_{max}, \gamma$ are specified, then Eqs. 11 and 12 become:

$$H_i = G_{max} \frac{G_{i+1}Y_{i+1} - G_i Y_i}{Y_{i+1} - Y_i}, \quad i = 2, \dots, n-1 \quad \text{and} \quad R_i = G_{max} G_i Y_i, \quad i = 1, \dots, n \quad (13)$$

where $G_i = G_i / G_{max}$.

2.3.1 Energy dissipated during strain cycles

As shown in Fig. 5, when the stress-strain curve follows Masing's amplitude rule (Masing, 1926), the areas I_i and J_i corresponding to an unloading from $+\gamma_i$ to $-\gamma_i$ and an reloading from $-\gamma_i$ to $+\gamma_i$, respectively, are four times greater than the area A_i under the stress-strain curve for a loading from 0 to γ_i . The areas A_i , I_i and J_i are defined as:

$$A_i = \int_0^{\gamma_i} \tau d\gamma, \quad I_i = \int_{-T_i}^{T_i} (\tau, -\tau) d\gamma = -4A_i, \quad \text{and} \quad J_i = \int_{-T_i}^{T_i} (\tau, +\tau) d\gamma = 4A_i \quad (14)$$

The dissipated energy W_{d_i} during a complete cycle of strain amplitude γ_i , which is the area of the hysteretic loop, is:

$$W_{d_i} = \oint \tau d\gamma = \int_{-\gamma_i}^{\gamma_i} \tau d\gamma + \int_{\gamma_i}^{-\gamma_i} \tau d\gamma = -I_i + J_i - 4\tau_i \gamma_i = 8A_i - 4\tau_i \gamma_i \quad i = 1, \dots, n \quad (15)$$

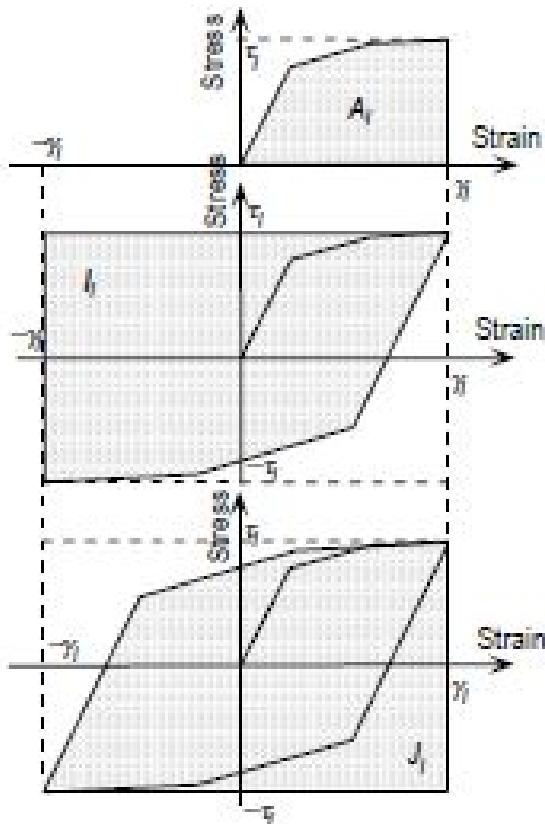


Figure 5. Areas A_i , I_i , and J_i used for calculation of hysteretic loop of IM model during loading-unloading cycle.

When the stress-strain curve is piecewise linear and generated by n discrete points $(\gamma_i, G(\gamma_i))$, A_i becomes:

$$A_i = 0 \text{ and } A_i = \frac{1}{2} \sum_{j=3}^i (G_j \gamma_j + G_{j-1} \gamma_{j-1})(\gamma_j - \gamma_{j-1}) \quad i = 2, \dots, n \quad (16)$$

and Eq. 15 becomes:

$$W_{d_i} = 8A_i - 4G_i \gamma_i^2 \quad i = 1, \dots, n \quad (17)$$

Since the maximum strain energy stored in the system is:

$$W_u = \frac{1}{2} G_i \gamma_i^2 \quad (18)$$

The critical damping ratio ξ at shear strain γ_i can be expressed:

$$\xi_1 = 0 \text{ and } \xi_i = \frac{W_{d_i}}{4\pi W_i} = \frac{2}{\pi} \left(\frac{2A_i}{G_i Y_i^3} - 1 \right) \quad i = 2, \dots, n \quad (19)$$

When the shear strain γ exceeds γ_c , the IM model assumes that the shear stress is equal to the shear strength R_s . In this case, the secant modulus G and critical damping ratio ξ becomes:

$$G = \frac{R_s}{Y} \text{ and } \xi = \frac{2}{\pi} \left(\frac{2(A_i + R_s(\gamma - \gamma_c))}{R_s Y} - 1 \right) \text{ for } \gamma > \gamma_c \quad (20)$$

For very large shear strain, the secant modulus tends toward zero and the damping ratio tends toward $2/\pi$, i.e.:

$$G \rightarrow 0 \text{ and } \xi \rightarrow \frac{2}{\pi} \text{ when } \gamma \rightarrow \infty \quad (21)$$

Equation 19 implies that ξ depends on the shape of the $G/G_{max}-\gamma$ curve, but is independent of G_{max} . The IM model assumes that the hysteretic stress-strain loop follows Masing similitude. Its material parameters (i.e., H_i and R_s , $i = 1, \dots, n$) are computed solely from the data points G_i/γ_i , $i = 1, \dots, n$, which characterizes the $G-\gamma$ -curves. The IM model can be assigned the same $G-\gamma$ -curves as the linear equivalent model. However the damping ratio curves of the IM model are calculated using Eq. 19. They can not be defined independently as in the case of the linear equivalent model. In summary, the IM model and the linear equivalent model can be assigned the same $G-\gamma$ curve but in general have different damping ratio curves. Figures 6 and 7 show examples of calculation of damping ratio from $G/G_{max}-\gamma$ -curves, and comparison to the damping ratio used by linear equivalent model in the case of clay and sand (Idriss, 1990).

Strain (%)	G/G_{max}	Strain (%)	Damping (%)	Calculated	
				Area A_i	Damping (%)
0.0001	1	0.0001	0.24	0.000000	0.00
0.0002	1	0.0002	0.42	0.000000	0.00
0.001	0.98	0.001	0.8	0.000000	0.00
0.002	0.99	0.002	1.4	0.000004	0.91
0.01	0.85	0.01	2.8	0.000044	3.53
0.02	0.84	0.02	5.1	0.000201	7.34
0.1	0.37	0.1	9.8	0.023388	15.08
0.3	0.18	0.3	15.5	0.010388	22.84
1	0.08	1	21	0.002388	29.11
3	0.05	3	25	0.000200	17.91
10	0.005	10	28	0.000200	10.49
100	0.0005		30	0.000200	5.34

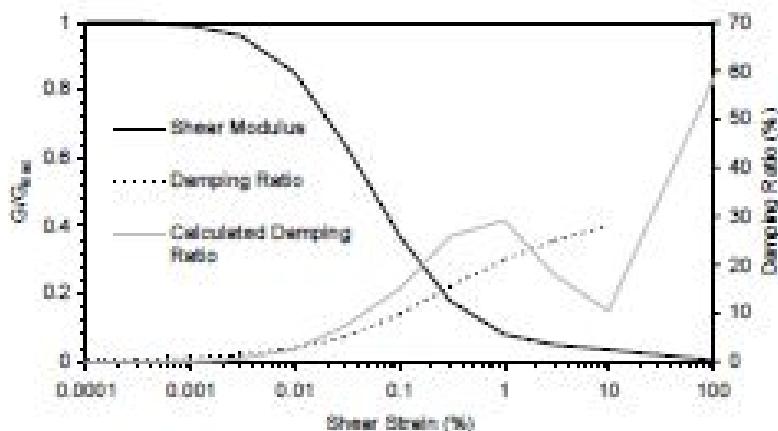


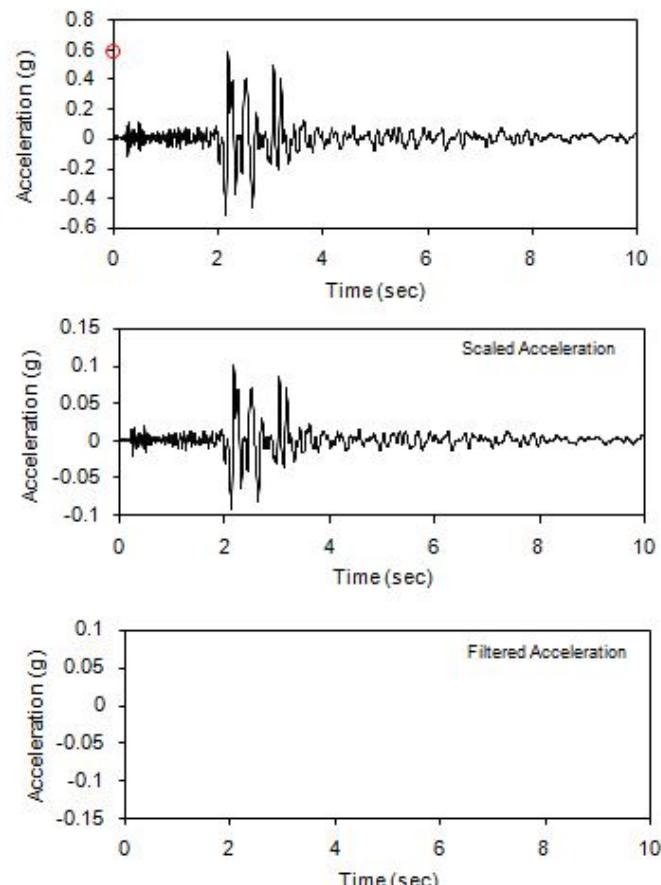
Figure 6. First example of calculation of damping ratio from a $G/G_{max}-\gamma$ -curve, and comparison to a damping ratio used by linear equivalent model.

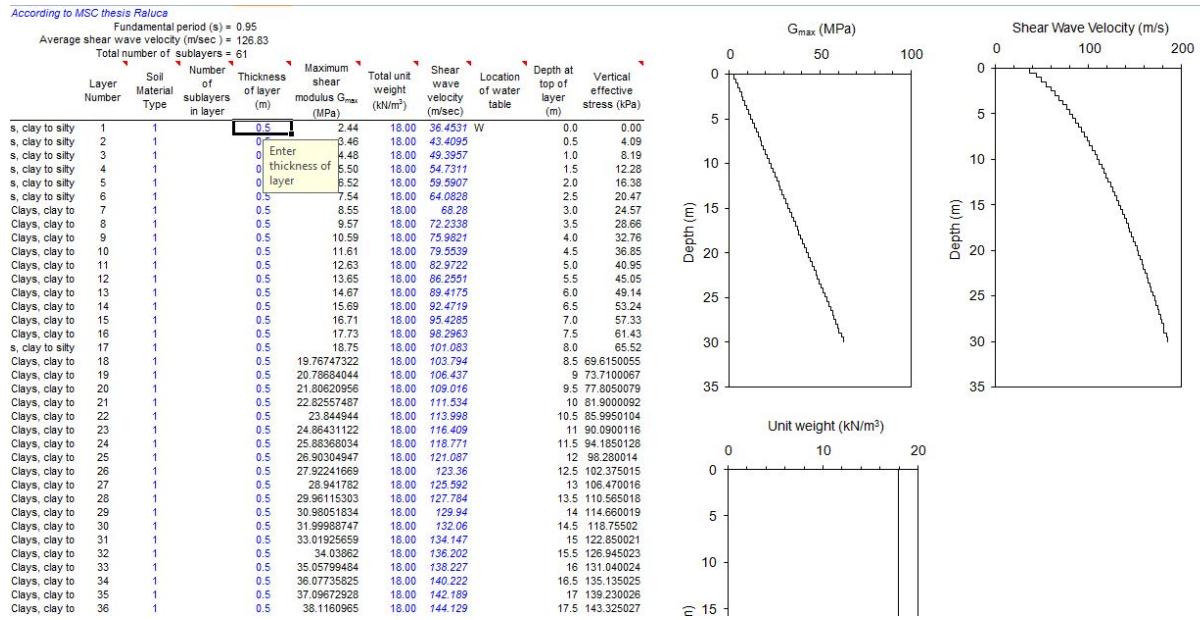
Appendix L

NERA - Input example

The appendix presents a set of input parameters corresponding to the low peak ground acceleration case.

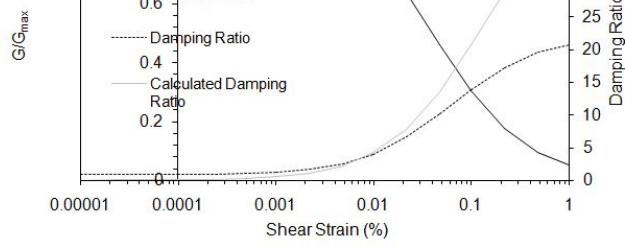
120816 NLSE hhe (Huizinge, 2012)			
	Time step ΔT (sec) =	0.005	
Desired maximum acceleration (g) =	0.1		
Maximum frequency cut-off (Hz) =	15		
Use filtered input in calculation ?	No		
Import input motion from external file ?	No		
Name of input file =	DIAM.ACC		
Total number of values read =	7541		
Peak Acceleration in input file (g) =	0.5800		
Time of peak acceleration (sec) =	0.000		
Mean Square Frequency (Hz) =	6.413		
Peak acceleration after filtering (g) =	0.095		
Input	Scaled	Filtered	
Time (sec)	Acceleration n (g)	Acceleration n (g)	Acceleration n (g)
0.000	0.0124	0.00	0.00
0.005	0.0092	0.00	0.00
0.010	0.0056	0.00	0.00
0.015	-0.0004	0.00	0.00
0.020	-0.0032	0.00	0.00
0.025	-0.0004	0.00	0.00
0.030	0.0048	0.00	0.00
0.035	0.0112	0.00	0.00
0.040	0.016	0.00	0.00
0.045	0.0168	0.00	0.00
0.050	0.014	0.00	0.00
0.055	0.01	0.00	0.00
0.060	0.0056	0.00	0.00
0.065	0.002	0.00	0.00
0.070	0.0004	0.00	0.00
0.075	0.0008	0.00	0.00
0.080	0.0036	0.00	0.00
0.085	0.0068	0.00	0.00
0.090	0.0104	0.00	0.00
0.095	0.012	0.00	0.00
0.100	0.0132	0.00	0.00
0.105	0.0124	0.00	0.00
0.110	0.0092	0.00	0.00
0.115	0.0064	0.00	0.00
0.120	0.0032	0.00	0.00
0.125	0.0028	0.00	0.00
0.130	0.0064	0.00	0.00
0.135	0.0108	0.00	0.00
0.140	0.0136	0.00	0.00
0.145	0.0136	0.00	0.00
0.150	0.012	0.00	0.00





Modulus for clay (Seed and Sun, 1989) upper range and damping for clay (Idriss 1990)

Calculated				
Strain (%)	G/G _{max}	Strain (%)	Damping (%)	Damping (%)
0.00001	1	0.00001	0.804	0.00
0.000022	0.999	0.000022	0.808	0.03
0.0000484	0.998	0.0000484	0.82	0.03
0.0001	0.996	0.0001	0.839	0.07
0.00022	0.992	0.00022	0.884	0.13
0.000484	0.983	0.000484	0.982	0.29
0.001	0.968	0.001	1.174	0.55
0.0022	0.936	0.0022	1.602	1.11
0.00484	0.876	0.00484	2.474	2.23
0.01	0.783	0.01	3.953	4.24
0.022	0.637	0.022	6.579	7.71
0.0484	0.459	0.0484	10.184	13.4326
0.1	0.303	0.1	13.788	20.6305
0.22	0.174	0.22	17.199	28.8761
0.484	0.093	0.484	19.565	36.3659
1	0.05	1	20.716	42.3439



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