# COS-D419 Factor Analysis and Structural Equation Models 2023, Assignment 2

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# 1 Exercise 2.1

Specify and test the hypothesis given on the page 1 of the lecture material.

Draw conclusions based on the  $\chi^2$  statistic and the CFI, TLI, RMSEA, and SRMR indices.

What can you say about the parameter estimates?

Visualize the model.

# 1.1 Read in the data set

Start by downloading the data file from Moodle to Project folder.

```
library(tidyverse)#data wrangling
library(readr)# read data into r
orig_data <- read_csv("ASC7INDM.CSV", show_col_types = FALSE)</pre>
```

# 1.2 Write functions

# 1.3 Subset the data set

Subset the variables for analysis and name it as sc (Self-concept).

```
# Select the variables for use
sc <- orig_data %>% dplyr::select(starts_with("SDQ2N")) # namming logic: sc = self-concept
```

# 1.4 Inspect the data

Have a quick overview of the data.

#### glimpse(sc)

```
## Rows: 265
## Columns: 16
## $ SDQ2N01 <dbl> 6, 6, 4, 5, 6, 5, 1, 2, 5, 4, 2, 5, 6, 4, 4, 6, 6, 6, 5, 6, 6, 6, 6
## $ SDQ2N13 <dbl> 5, 6, 6, 5, 5, 5, 6, 1, 5, 6, 6, 5, 6, 3, 5, 6, 6, 6, 4, 5, 5,~
## $ SDQ2N25 <dbl> 4, 6, 6, 5, 5, 5, 1, 6, 6, 3, 6, 6, 6, 5, 5, 6, 6, 6, 6, 5, 4,~
## $ SDQ2N37 <dbl> 6, 6, 2, 6, 4, 3, 6, 4, 6, 6, 6, 5, 5, 5, 4, 5, 6, 4, 4, 6, 6,~
## $ SDQ2N04 <dbl> 3, 6, 6, 5, 3, 3, 4, 4, 6, 6, 5, 6, 5, 4, 4, 4, 4, 6, 5, 5, 3,~
## $ SDQ2N16 <dbl> 4, 6, 4, 6, 4, 2, 6, 4, 6, 5, 6, 6, 5, 5, 5, 5, 6, 5, 4, 6, 6,~
## $ SDQ2N28 <dbl> 4, 6, 6, 5, 4, 4, 6, 6, 6, 6, 6, 6, 5, 5, 5, 5, 6, 4, 2, 4, 4,~
## $ SDQ2N40 <dbl> 6, 6, 3, 6, 4, 4, 6, 6, 6, 6, 6, 6, 6, 5, 4, 4, 6, 6, 5, 5, 5, ~
## $ SDQ2N10 <dbl> 2, 5, 6, 5, 4, 4, 1, 6, 5, 4, 2, 6, 5, 5, 5, 3, 4, 6, 5, 4, 6,~
## $ SDQ2N22 <dbl> 6, 6, 5, 6, 6, 4, 6, 6, 6, 6, 6, 6, 6, 5, 6, 6, 6, 6, 6, 3, 6,~
## $ SDQ2N34 <dbl> 1, 6, 4, 3, 5, 5, 1, 1, 5, 4, 5, 6, 5, 2, 5, 2, 3, 2, 1, 3, 3,~
## $ SDQ2N07 <dbl> 6, 6, 6, 6, 3, 4, 5, 3, 6, 5, 6, 6, 6, 6, 4, 4, 6, 6, 6, 6, 3,~
## $ SDQ2N31 <dbl> 6, 6, 3, 6, 4, 4, 6, 4, 6, 6, 6, 6, 6, 6, 5, 5, 6, 6, 5, 5, 5, ~
## $ SDQ2N43 <dbl> 6, 6, 1, 5, 5, 4, 5, 6, 6, 6, 6, 6, 6, 6, 5, 6, 6, 6, 5, 6, 5, ~
```

The data set includes 16 variables from 265 observations. All the variables are numeric. Next, I examined the unique values of each variables.

# unique.levels(sc)

```
## [1] "Variable SDQ2N01 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N13 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N25 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N37 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N04 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N16 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N28 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N40 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N10 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N22 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N34 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N46 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N07 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N19 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N31 has values of 1,2,3,4,5,6"
## [1] "Variable SDQ2N43 has values of 1,2,3,4,5,6"
```

For each variable, the values distribute from 1 to 6.

# 2 Explore the data

# 2.1 Descriptive statistics

Table 1: Descriptive dtatistics of selected variables

|         | centralize | dispersion tendency |                     |       |      |     |
|---------|------------|---------------------|---------------------|-------|------|-----|
|         | mean       | median              | $\operatorname{sd}$ | range | se   | IQR |
| SDQ2N01 | 4.41       | 5                   | 1.35                | 5     | 0.08 | 1   |
| SDQ2N13 | 5.00       | 6                   | 1.36                | 5     | 0.08 | 2   |
| SDQ2N25 | 5.10       | 6                   | 1.23                | 5     | 0.08 | 1   |
| SDQ2N37 | 4.83       | 5                   | 1.14                | 5     | 0.07 | 2   |
| SDQ2N04 | 4.52       | 5                   | 1.40                | 5     | 0.09 | 2   |
| SDQ2N16 | 4.65       | 5                   | 1.24                | 5     | 0.08 | 2   |
| SDQ2N28 | 4.69       | 5                   | 1.33                | 5     | 0.08 | 2   |
| SDQ2N40 | 4.98       | 5                   | 1.36                | 5     | 0.08 | 1   |
| SDQ2N10 | 4.62       | 5                   | 1.15                | 5     | 0.07 | 1   |
| SDQ2N22 | 5.38       | 6                   | 1.09                | 5     | 0.07 | 1   |
| SDQ2N34 | 3.89       | 4                   | 1.70                | 5     | 0.10 | 3   |
| SDQ2N46 | 5.27       | 6                   | 1.30                | 5     | 0.08 | 1   |
| SDQ2N07 | 4.32       | 5                   | 1.78                | 5     | 0.11 | 3   |
| SDQ2N19 | 4.54       | 5                   | 1.69                | 5     | 0.10 | 2   |
| SDQ2N31 | 4.74       | 5                   | 1.57                | 5     | 0.10 | 2   |
| SDQ2N43 | 4.98       | 5                   | 1.40                | 5     | 0.09 | 1   |

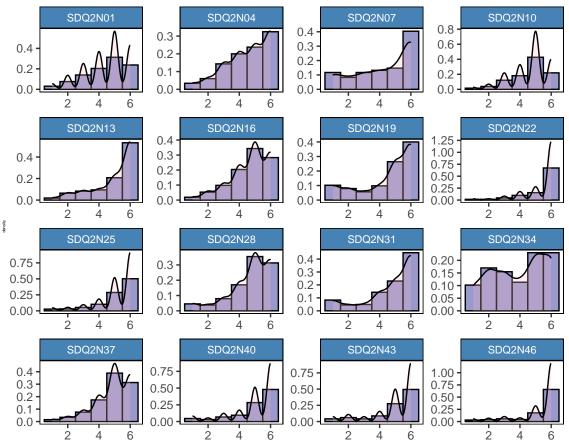
```
#sc.ds %>%
# tab_df(digits = 2,
# alternate.rows = T,
# title = "Table 1. Descriptive dtatistics of selected variables",
# CSS = list(css.centralign='text-align: right;'))
```

# 2.2 Visualization

#### 2.2.1 Histogram

```
sc %>%
 pivot_longer(everything()) %>% #longer format
  ggplot(aes(x = value)) + #x axis used variable "value" (a default of pivot)
  geom_histogram(binwidth = 1, aes(y = ..density..), #match ys of density and histogram plots
                 color = "black", fill = "#9999CC")+ # adjust aesthetics for hist
  geom_density(fill = "pink", alpha = 0.25)+ #adjust aesthetics for density plot
  facet_wrap(~name, scales = "free") + #wrap by name variable
  theme(panel.grid.major = element_blank(), #get rid of the grids
        panel.grid.minor = element_blank(),
        panel.background = element_rect(fill = "white", #adjust the background
                                        color = "black"),
       strip.background = element_rect(color = "black", #adjust the strips aes
                                        fill = "steelblue"),
       strip.text = element_text(size =8, color = "white"), #adjust strip text
       axis.title.x = element_text(size = 3), #adjust the x text
       axis.title.y = element_text(size = 3), # adjust the y text
       plot.title = element_text(size = 12, face = "bold"))+ #adjust the title
  labs(title = "Fig. 2.1.2.1 Distribution of variables") #title it
```

Fig. 2.1.2.1 Distribution of variables



library(GGally)