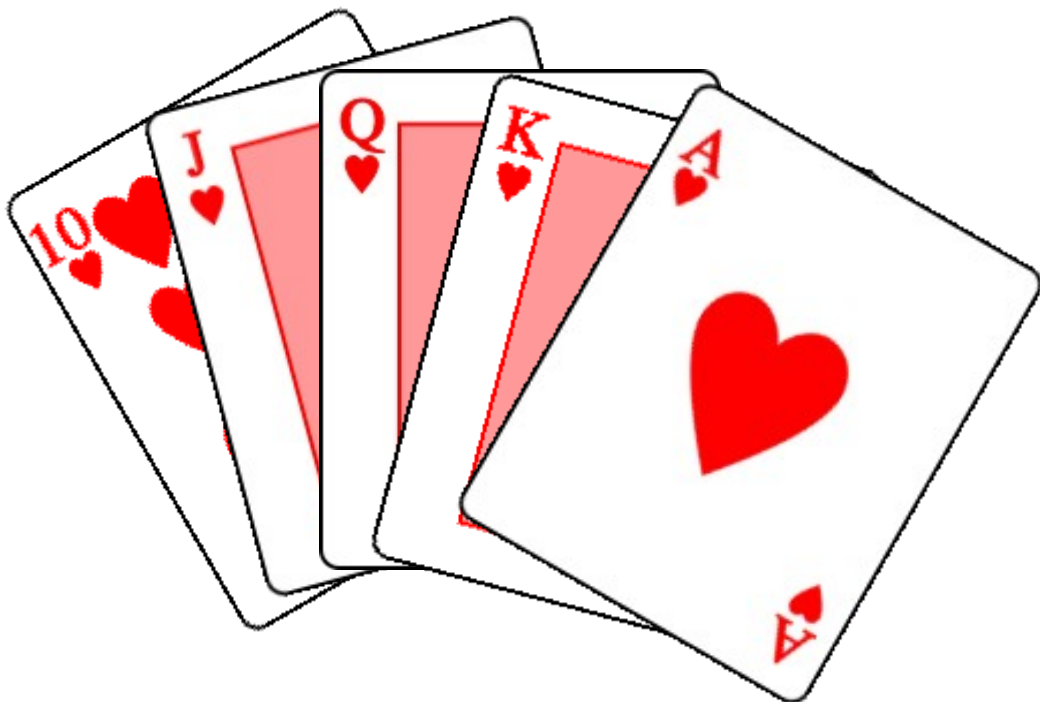


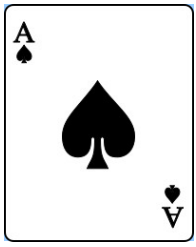
An Introduction to the Current Approaches in

Computer Poker

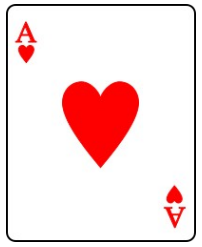
Richard Gibson
December 4, 2009



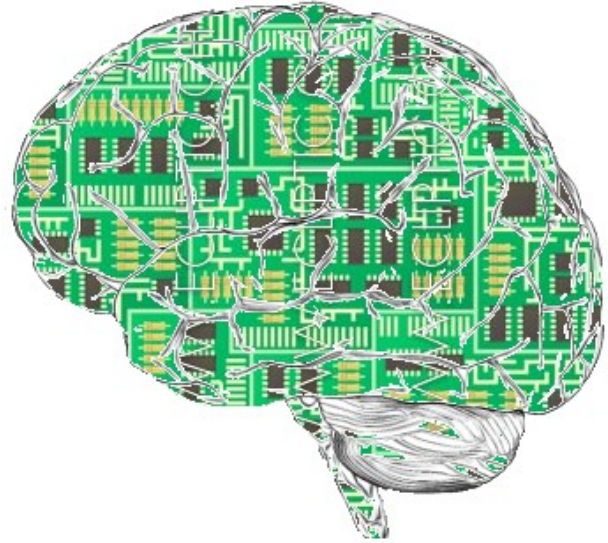
Source (all card images) http://en.wikipedia.org/wiki/Playing_card



Motivation

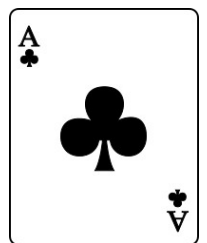
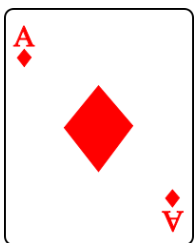


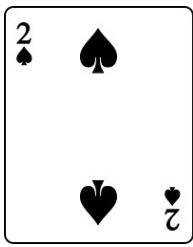
Source: <http://www.flickr.com/photos/andresrueda/3453821052/>



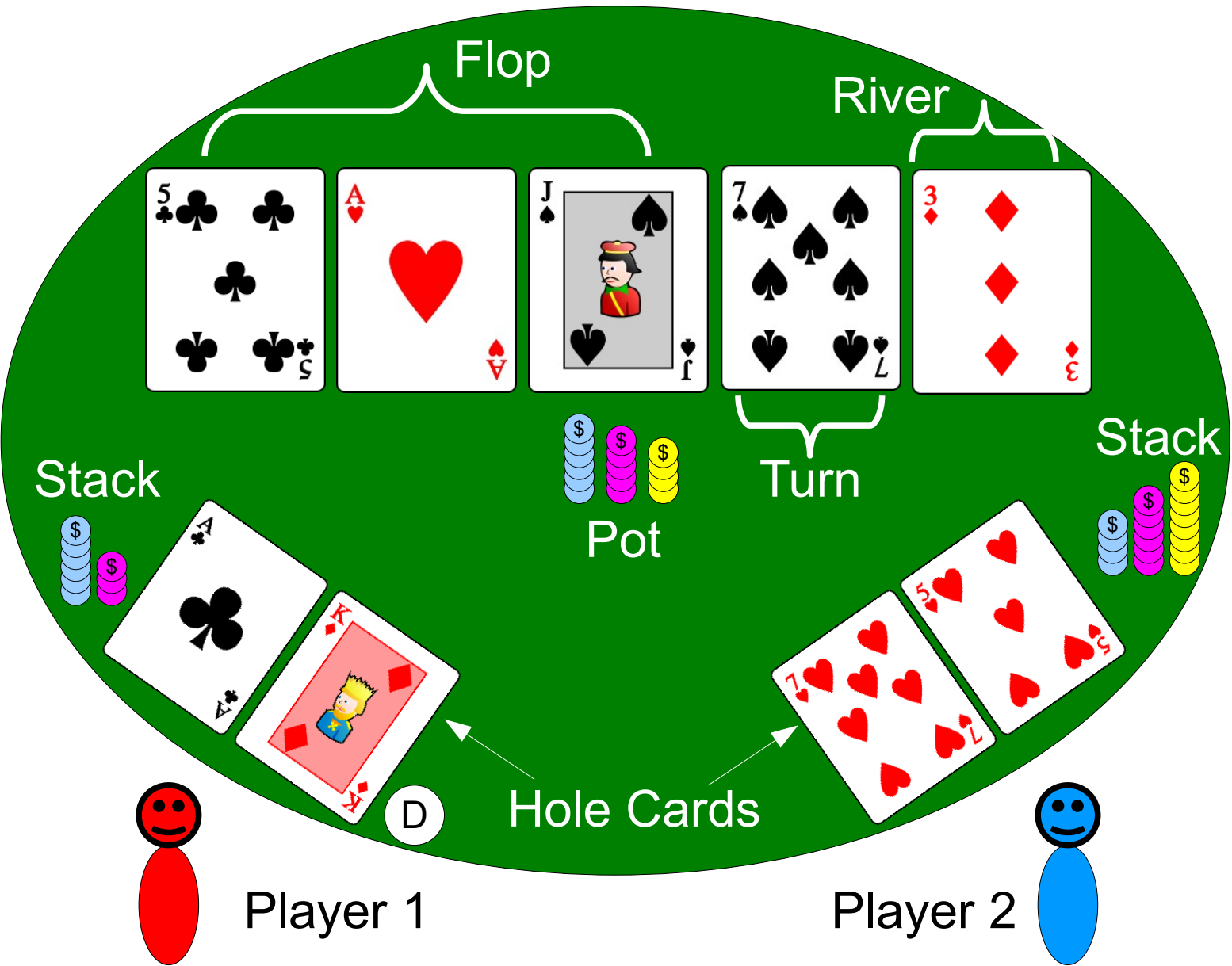
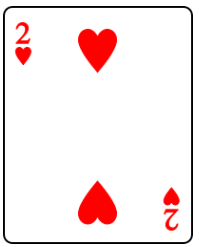
Source: <http://en.wikipedia.org/wiki/File:ArtificialFictionBrain.png>

- Fully autonomous intelligent computers
- We are far from completely autonomous behaviour
- Use games as a stepping stone for artificial intelligence research

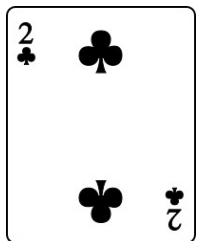
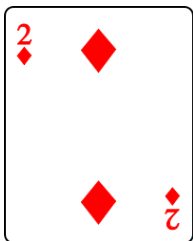


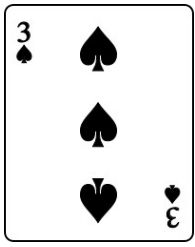


Texas Hold'em

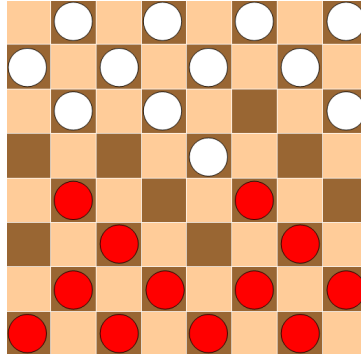
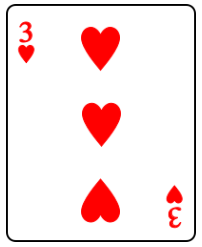


- Example: Player 2 wins the pot in a showdown

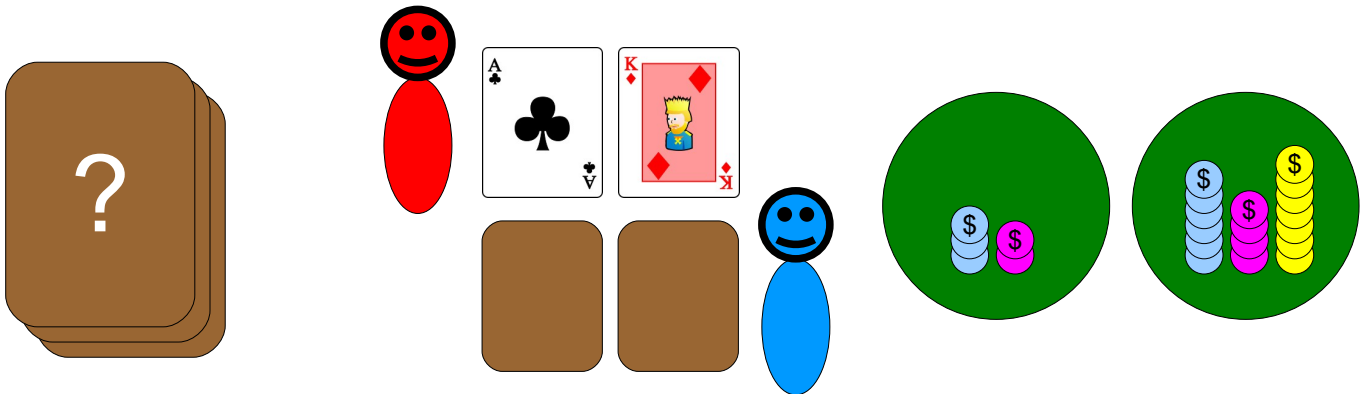




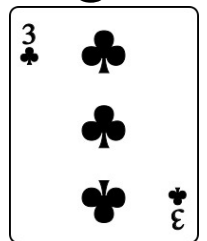
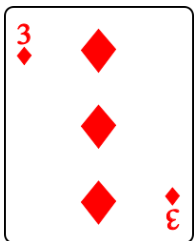
Challenges

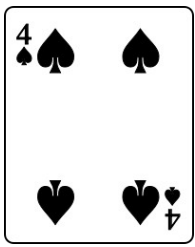


- Other studied games, like Checkers, are:
 - Deterministic
 - Full information
 - Win, lose, or draw

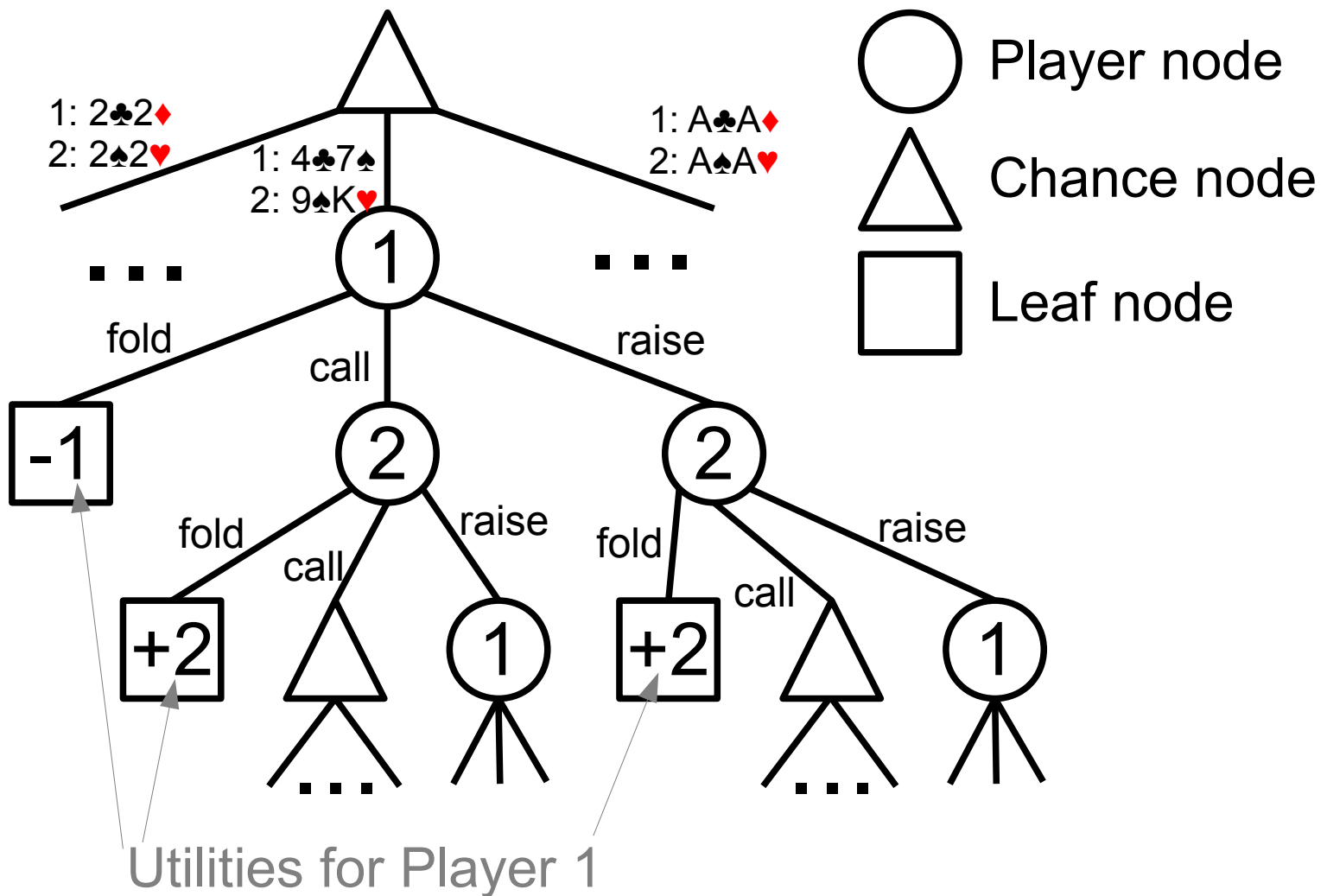
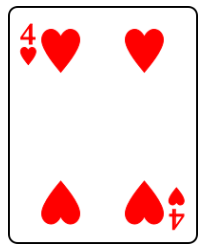


- In Texas Hold'em:
 - Card deals are random
 - Hole cards are private
 - Variable degrees of winning and losing

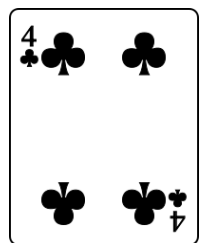
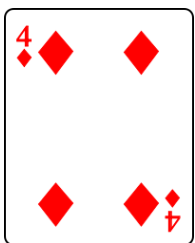


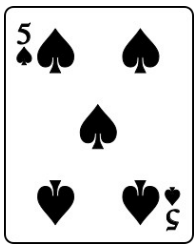


Extensive Form Games

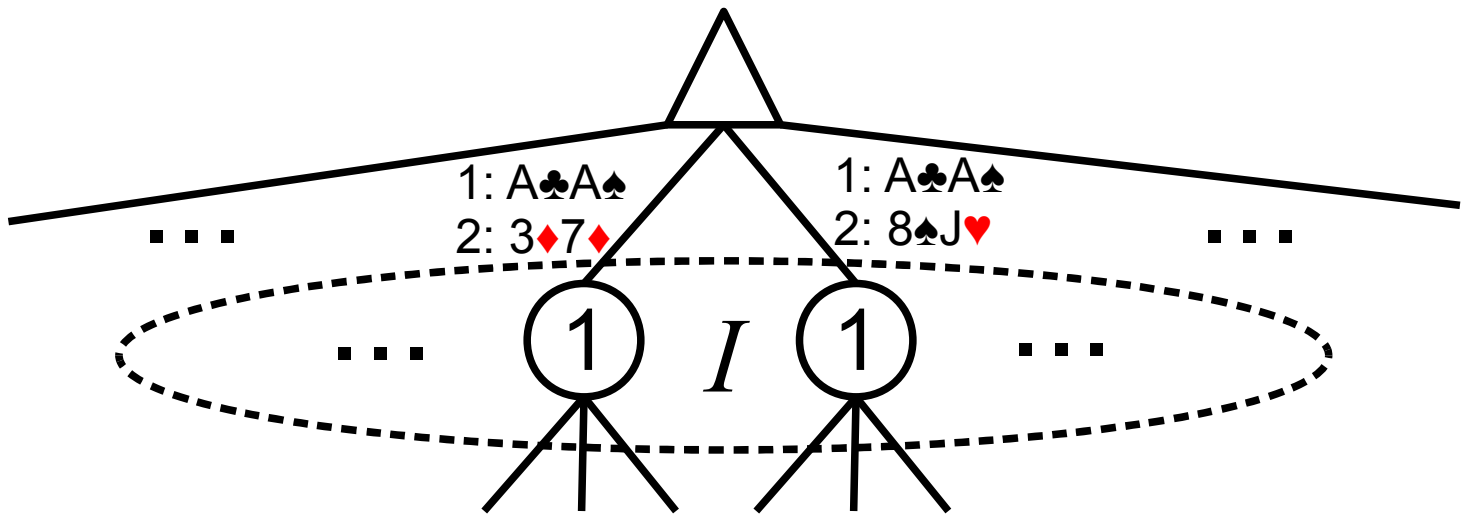
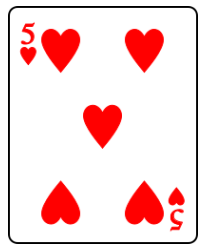


- Upper part of the extensive form game tree [Osborne & Rubenstein 1994] for Heads-Up Limit Texas Hold'em





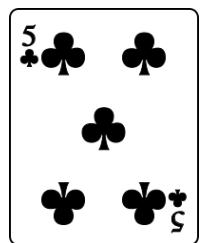
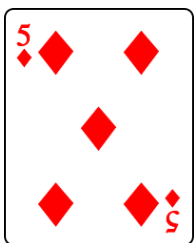
Extensive Form Games

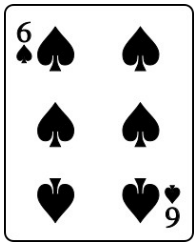


- Two states in the same information set for Player 1

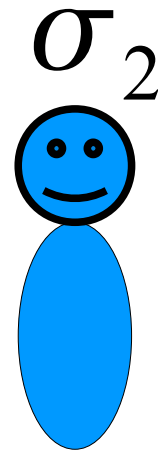
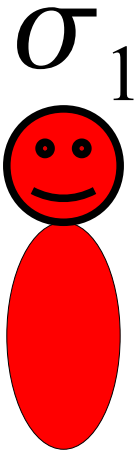
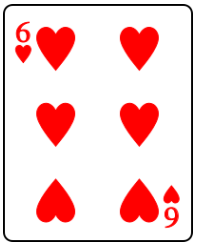
$$\underset{\substack{\uparrow \\ \text{Strategy}}}{\sigma_1(I)} = \underbrace{\{p_{fold}, p_{call}, p_{raise}\}}_{\text{Action Probabilities}}$$

Information Set





Nash Equilibrium

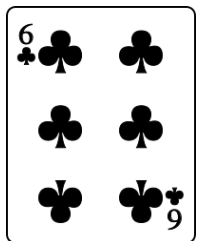
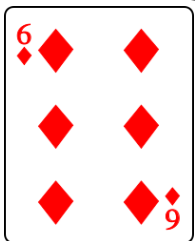


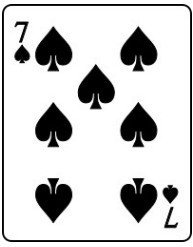
For all σ'_1 ,

For all σ'_2 ,

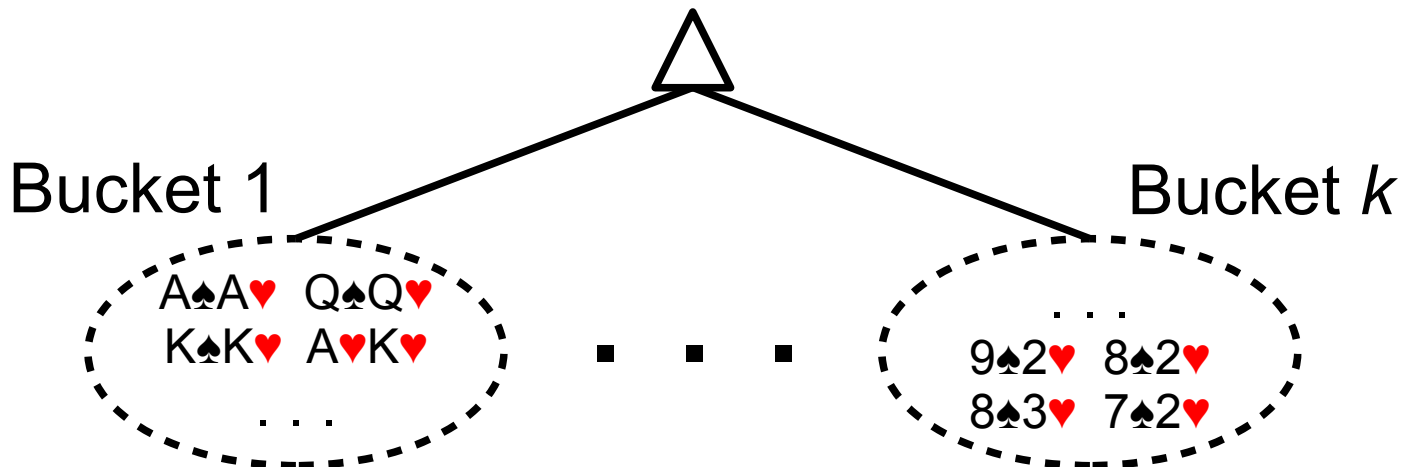
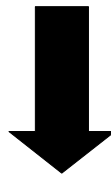
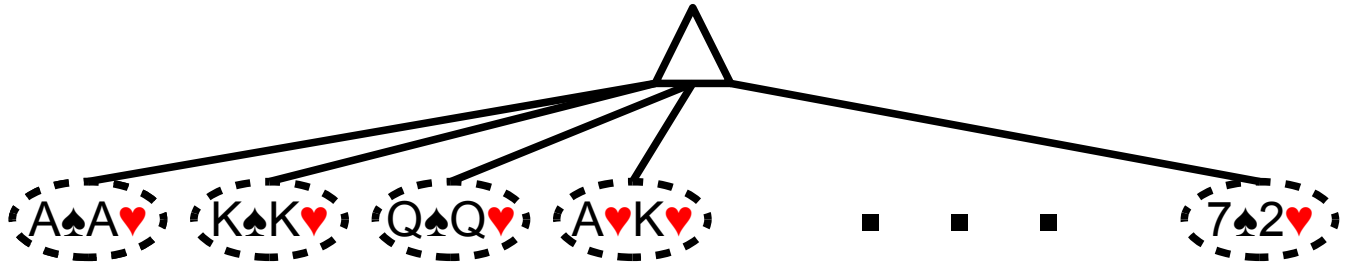
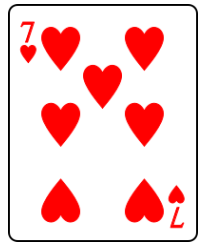
$$\mathbf{u}_1(\sigma_1, \sigma_2) \geq \mathbf{u}_1(\sigma'_1, \sigma_2) \quad \mathbf{u}_2(\sigma_1, \sigma_2) \geq \mathbf{u}_2(\sigma_1, \sigma'_2)$$

- (σ_1, σ_2) is a Nash equilibrium [Nash 1951]
- Provides a guarantee on expected winnings in Heads-Up games ($\mathbf{u}_2 = -\mathbf{u}_1$)
- Can theoretically approximate via linear programming [Koller et al. 1994]

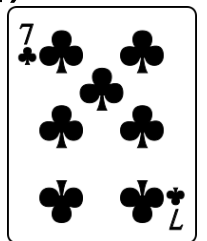
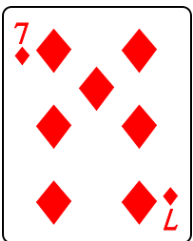


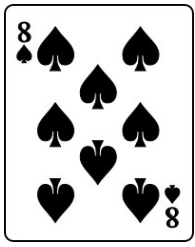


Abstraction

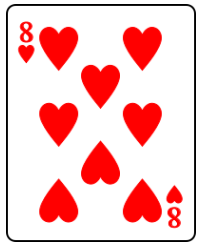


- Heads-Up Limit Texas Hold'em too large; instead, analyze an abstract game
- Group hands according to *expected hand strength* = probability of winning against a uniformly random hand (as found in [Johanson 2007]).





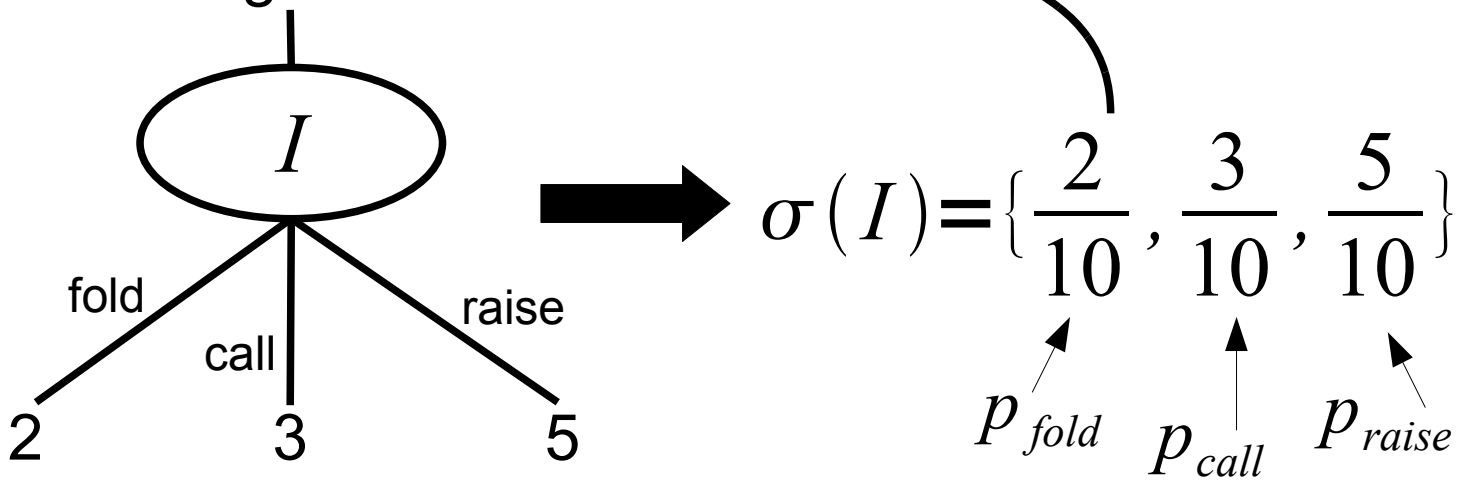
CFR



Counter-factual Regret Minimization
algorithm [Zinkevich et al. 2008]:

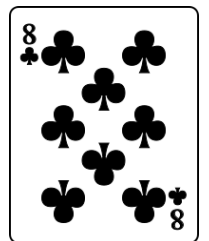
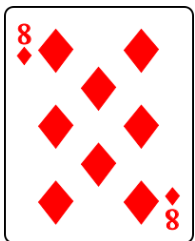
Input: Extensive form game tree, number of iterations T

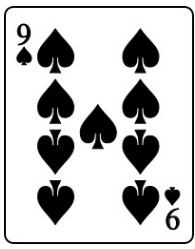
How much do I *regret*
not taking each action?



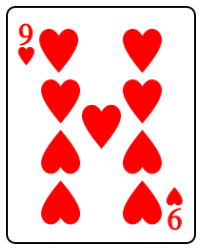
Output: $(\bar{\sigma}_1, \bar{\sigma}_2)$

- Finds an approximate Nash equilibrium
- Can analyze larger abstractions than linear programming





Polaris



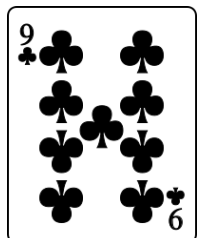
Man-Machine Poker Championships
2007 and 2008 [man-machine]

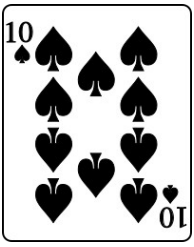
Source: <http://www.lasvegasvegas.com/viewer/v/W SOP2004-2006/W SOP2006+2006+World+Series+of+Poker+-+Rio+Las+Vegas/3619-Ig.jpg.html>



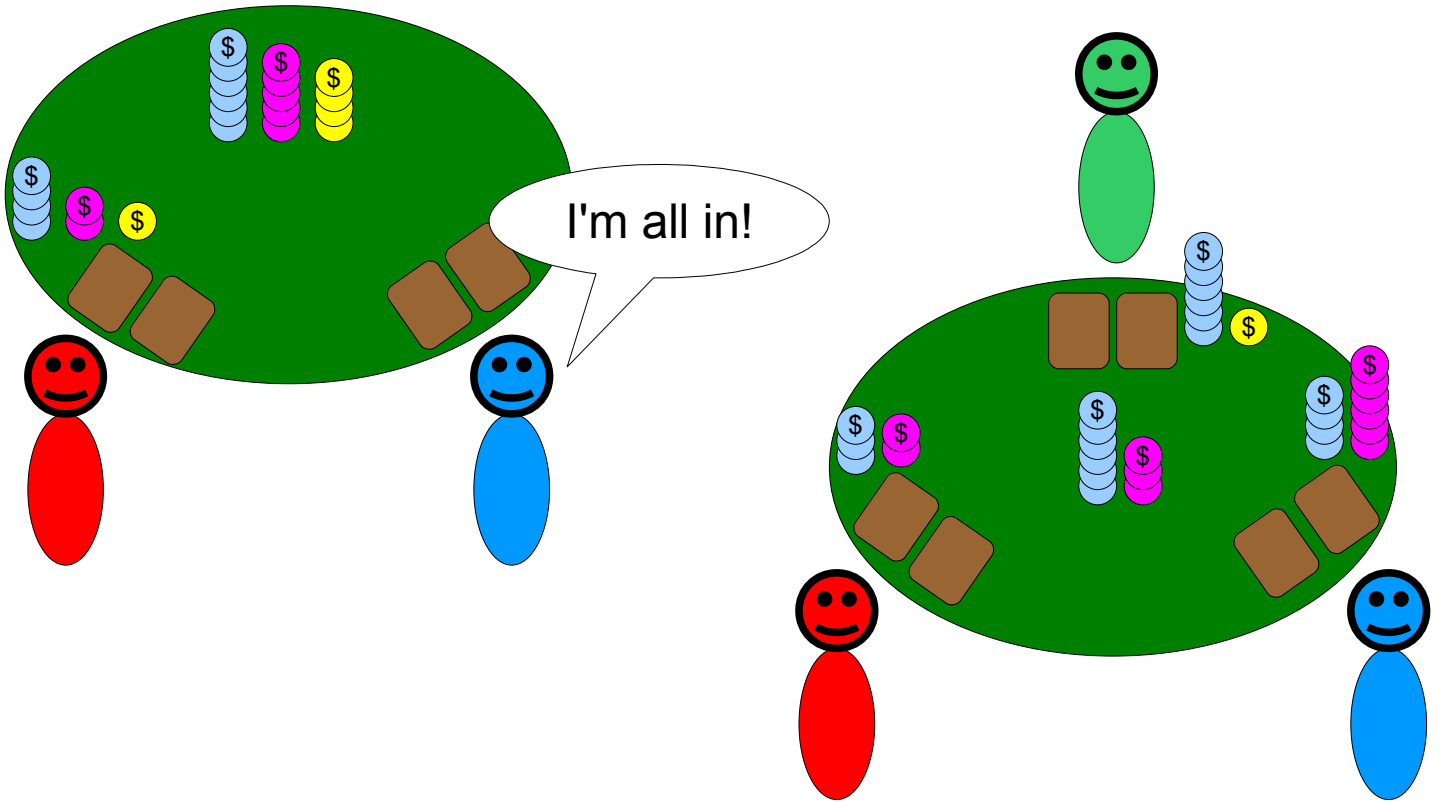
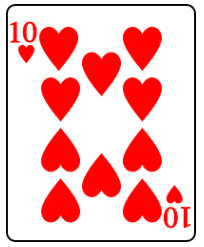
vs *Polaris*

- Heads-Up Limit Texas Hold'em only
- Polaris used strategy based on CFR
- 2007: Polaris loses to Phil Laak and Ali Eslami
- 2008: Polaris defeats a team of professionals including Matt Hawrilenko and IJay Palansky

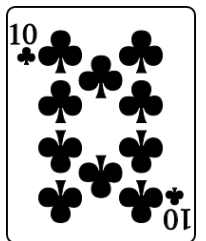
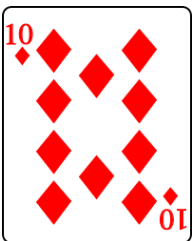


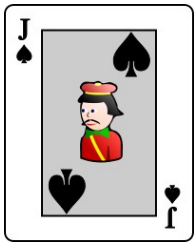


Future Work

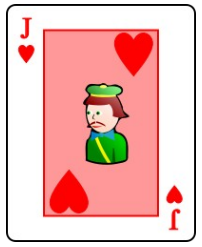


- No Limit Hold'em
 - Must also abstract actions. But how?
- Ring (Multi-Player) Limit Hold'em
 - Will CFR find a “useful” strategy?
 - Do we even want to play in equilibrium?





References



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<http://poker.cs.ualberta.ca/man-machine>, 2008.
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