



# Chronological Backtracking

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**Abstract.** Non-Chronological Backtracking (NCB) has been implemented in every modern CDCL SAT solver since the original CDCL solver GRASP. NCB's importance has never been questioned. This paper argues that NCB is not always helpful. We show how one can implement the alternative to NCB—Chronological Backtracking (CB)—in a modern SAT solver. We demonstrate that CB improves the performance of the winner of the latest SAT Competition, `Maple_LCM_Dist`, and the winner of the latest MaxSAT Evaluation `Open-WB0`.

## 1 Introduction

Conflict-Driven Clause Learning (CDCL) SAT solving has been extremely useful ever since its the original implementation in the GRASP solver over 20 years ago [13], as it enabled solving real-world instances of intractable problems [2]. The algorithmic components of the original GRASP algorithms have been meticulously studied and modified over the years with the one notable exception of Non-Chronological Backtracking (NCB). NCB has always been perceived as an unquestionably beneficial technique whose impact is difficult to isolate, since it is entangled with other CDCL algorithms. NCB's contribution went unstudied even in [6]—a paper which aimed at isolating and studying the performance of fundamental CDCL algorithms. In this paper, we show how to implement the alternative to NCB—Chronological Backtracking (CB)—in a modern SAT solver.

Recall the CDCL algorithm. Whenever Boolean Constraint Propagation (BCP) discovers a falsified *conflicting clause*  $\beta$ , the solver learns a new *conflict clause*  $\sigma$ . Let the *conflict decision level*  $cl$  be the highest decision level in the conflicting clause  $\beta$ .<sup>1</sup> The new clause  $\sigma$  must contain one variable  $v$  assigned at  $cl$  (the UIP variable). Let the *second highest decision level*  $s$  be the highest decision level of  $\sigma$ 's literals lower than  $cl$  ( $s = 0$  for a unit clause). Let the *backtrack level*  $bl$  be the level the solver backtracks to just after recording  $\sigma$  and before flipping  $v$ .

*Non-Chronological Backtracking (NCB)* always backtracks to the second highest decision level (that is, in NCB,  $bl = s$ ). The idea behind NCB is to improve the solver's locality by removing variables irrelevant for conflict analysis

<sup>1</sup> In the standard algorithm,  $cl$  is always equal to the current decision level, but, as we shall see, that is not the case for CB.

from the assignment trail. NCB’s predecessor is conflict-directed backjumping, proposed in the context of the Constraint Satisfaction Problem (CSP) [11].

Let *Chronological Backtracking (CB)* be a backtracking algorithm which always backtracks to the decision level immediately preceding the conflict decision level  $cl$  (that is, in CB,  $bl = cl - 1$ ). In our proposed implementation, after CB is carried out,  $v$  is flipped and propagated (exactly as in the NCB case), and then the solver goes on to the next decision or continues the conflict analysis loop.

Implementing CB is a non-trivial task as it changes some of the indisputable invariants of modern SAT solving algorithms. In particular, the decision level of the variables in the assignment trail is no longer monotonously increasing. Moreover, the solver may learn a conflict clause whose highest decision level is higher than the current decision level. Yet, as we shall see, implementing CB requires only few short modifications to the solver.

To understand why CB can be useful consider the following example. Let  $F = S \wedge T$  be a propositional formula in Conjunctive Normal Form (CNF), where  $S$  is a long satisfiable CNF formula (for example, assume that  $S$  has  $10^7$  variables),  $T \equiv (c \vee \neg b) \wedge (c \vee b)$ , and  $V(S) \cap V(T) = \emptyset$ , where  $V(H)$  comprises the set of  $H$ ’s variables. Consider Minisat’s [3] execution, given  $F$ . The solver is likely to start by assigning the variables in  $V(S)$  (since  $S$ ’s variables are likely to have higher scores), satisfying  $S$ , and then getting to satisfying  $T$ . Assume that the solver has satisfied  $S$  and is about to take the next decision. Minisat will pick the literal  $\neg c$  as the next decision, since the variable  $c$  has a higher index than  $b$  and 0 is always preferred as the first polarity. The solver will then learn a new *unit* conflict clause  $(c)$  and backtrack to decision level 0 as part of the NCB algorithm. After backtracking, the solver will satisfy  $S$  again from the very beginning and then discover that the formula is satisfied. Note that the solver is not expected to encounter any conflicts while satisfying  $S$  for the second time because of the phase saving heuristic [4, 10, 14] which re-assigns the same polarity to every assigned variable. Yet, it will have to re-assign all the  $10^7$  variables in  $V(S)$  and propagate after each assignment. In contrast, a CB-based solver will satisfy  $F$  immediately after satisfying  $S$  without needing to backtrack and satisfy  $S$  once again.

Our example may look artificial, yet in real-word cases applying NCB might indeed result in useless backtracking (not necessarily to decision level 0) and reassignment of almost the same literals. In addition, NCB is too aggressive: it might remove good decisions from the trail only because they did not contribute to the *latest* conflict resolution. Guided by these two insights, our backtracking algorithm applies CB when the difference between the CB backtrack level and the NCB backtrack level is higher than a user-given threshold  $T$ , but only after a user-given number of conflicts  $C$  passed since the beginning of solving.

We have integrated CB into the SAT Competition 2017 [5] winner, `Maple_LCM_Dist` [7], and MaxSAT Evaluation 2017 [1] winner `Open-WBO` [9] (code available in [8]). As a result, `Maple_LCM_Dist` solves 3 more SAT Competition benchmarks; the improvement on unsatisfiable instances is consistent. `Open-WBO`

solves 5 more MaxSAT Evaluation benchmarks and becomes much faster on 10 families.

In the text that follows, Sect. 2 provides CB's implementation details, Sect. 3 presents the experimental results, and Sect. 4 concludes our work.

## 2 Chronological Backtracking

We show how CB can be integrated into a modern CDCL solver [12] starting with an example. Consider the input formula, comprising 9 clauses  $c_1 \dots c_9$ , shown on the left-hand side in Fig. 1. We will walk through a potential execution of a CDCL solver using CB, while highlighting the differences between CB and NCB.

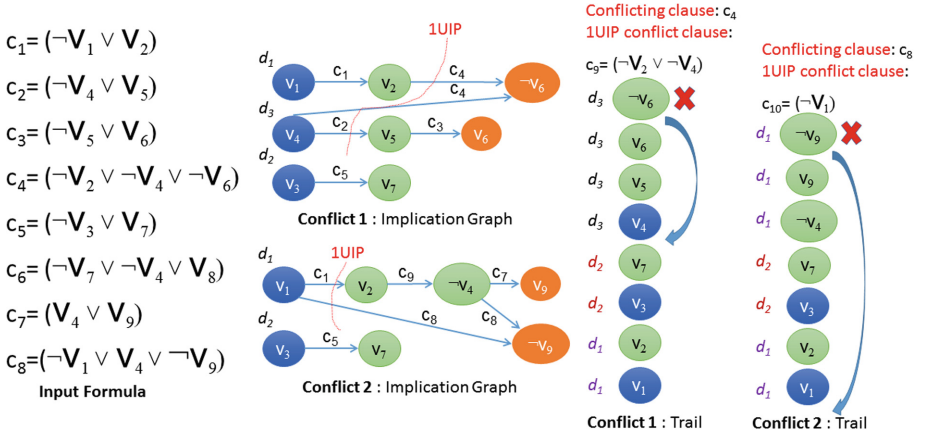


Fig. 1. CB example

Assume the first decision at decision level  $d_1$  is  $v_1$ , followed by the implication  $v_2$  in clause  $c_1$  (at the same level  $d_1$ ). Then, a new decision  $v_3$  implying  $v_7$  in  $c_5$  is carried out at decision level  $d_2$ . The next decision (at level  $d_3$ ) is  $v_4$ . It implies  $v_5$  in  $c_2$  and  $v_6$  in  $c_3$ , followed by a conflict, as all literals of  $c_4$  are falsified under the current partial assignment. The implication graph and the trail at the time of conflict 1 are shown in Fig. 1. The conflict analysis will then learn a new 1UIP clause  $c_9 = (\neg v_2 \vee \neg v_4)$  (resolution between clauses  $c_2, c_3, c_4$ ).

At this point, a difference between NCB and CB is manifested. NCB would backtrack to the end of level  $d_1$ , skipping the irrelevant decision level  $d_2$ . We apply CB, which backtracks to the end of the previous decision level  $d_2$ . Backtracking to the end of  $d_2$  undoes the assignments of  $v_6, v_5, v_4$ . Then, the algorithm asserts the unassigned 1UIP literal  $\neg v_4$  and pushes it to the trail.

Our CB implementation marks  $\neg v_4$ 's decision level as  $d_1$ , since  $d_1$  is the second highest level in the newly learned clause; however,  $\neg v_4$  is placed into the trail after literals assigned at a higher decision level  $d_2$ . Hence, unlike in the NCB

case, the decision levels of literals in the trail are not necessary monotonically increasing. It still holds, though, that each literal  $l$  implied at clause  $\alpha$  is placed in the trail after all the other literals of  $\alpha$ .

Let us proceed with our example. The assignment of  $\neg v_4$  implies  $v_9$  in  $c_7$ . Our algorithm marks the decision level of  $v_9$  as  $d_1$ , since it is the highest level in the clause  $c_7$  where  $v_9$  is implied. Then, BCP finds a falsified clause  $c_8$ . Our algorithm identifies the decision level of the conflict as  $d_1$ , since all the literals in the conflicting clause  $c_8$  were assigned at that level. At that point, CB will backtrack to the end of  $d_1$  *before proceeding with conflict analysis*. Our backtrack algorithm will unassign the variables assigned at  $d_2$ , that is,  $v_3$  and  $v_7$ , while keeping the variables assigned at  $d_1$  ( $v_4$  and  $v_9$ ) in the same order. After the backtracking, conflict analysis is invoked. Conflict analysis will learn a new clause  $c_{10} = (\neg v_1)$  (resolution between clauses  $c_1, c_9, c_7, c_8$ ). The algorithm will then backtrack to the decision level  $d_0 = d_1 - 1$  (to emphasize: in CB the backtrack level is the previous decision level, determined independently of the newly learned conflict clause).

## 2.1 Algorithm

Now we show the implementation of the high-level algorithms CDCL (Algorithm 1), BCP (Algorithm 2) and Backtrack (Algorithm 3) with CB. In fact, we show both the NCB and the CB versions of each function. For CDCL and BCP most of the code is identical, except for the lines marked with either *ncb* or *cb*.

Consider the high-level CDCL algorithm in Algorithm 1. It operates in a loop that finishes after either all the variables are assigned (SAT) or when an empty clause is derived (UNSAT). Inside the loop, BCP is invoked. BCP returns a falsified conflicting clause if there is a conflict. If there is no conflict, a new decision is taken and pushed to the trail.

The first difference between CB and NCB shows up right after a conflict detection. The code between lines 4 – 8 is applied only in the case of CB. If the conflicting clause contains one literal  $l$  from the maximal decision level, we let BCP propagating that literal at the second highest decision level in *conflicting\_cls*. Otherwise, the solver backtracks to the maximal decision level in the conflicting clause before applying conflict analysis. This is because, as we saw in the example, the conflicting clause may be implied at a decision level earlier than the current level. The conflict analysis function returns the 1UIP variable to be assigned and the conflict clause  $\sigma$ . If  $\sigma$  is empty, the solver returns UNSAT. Assume  $\sigma$  is not empty. The backtrack level  $bl$  is calculated differently for NCB and CB. As one might expect,  $bl$  comprises the second highest decision level in  $\sigma$  in the case of NCB case and the previous decision level in the case of CB (note that for CB the solver has already backtracked to the maximal decision level in the conflicting clause). Subsequently, the solver backtracks to  $bl$  and pushes the 1UIP variable to the trail before continuing to the next iteration of the loop.

Consider now the implementation of BCP in Algorithm 2. BCP operates in a loop as long as there exists at least one unvisited literal in the trail  $\nu$ . For the first unvisited literal  $l$ , BCP goes over all the clauses watched by  $l$ . Assume

**Algorithm 1.** CDCL $\nu$ : the trail, stack of decisions and implications $_{ncb}$ : marks the NCB code $_{cb}$ : marks the CB code**Input:** CNF formula**Output:** SAT or UNSAT

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1: while not all variables assigned do
2:    $conflicting\_cls := BCP()$ ;
3:   if  $conflicting\_cls \neq null$  then
4:     if  $conflicting\_cls$  contains one literal from the maximal level then
5:        $_{cb} \text{Backtrack}(\text{second highest decision level in } conflicting\_cls)$ 
6:        $_{cb}$  continue
7:     else
8:        $_{cb} \text{Backtrack}(\text{maximal level in } conflicting\_cls)$ 
9:        $(1uip, \sigma) := \text{ConflictAnalysis}(conflicting\_cls)$ 
10:      if  $\sigma$  is empty then
11:        return UNSAT
12:       $_{ncb} bl := \text{second highest decision level in } \sigma$  (0 for a unit clause)
13:       $_{cb} bl := \text{current decision level} - 1$ 
14:       $\text{Backtrack}(bl)$ 
15:      Push  $1uip$  to  $\nu$ 
16:    else
17:      Decide and push the decision to  $\nu$ 
18: return SAT

```

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a clause  $\beta$  is visited. If  $\beta$  is a unit clause, that is, all  $\beta$ 's literals are falsified except for one unassigned literal  $k$ , BCP pushes  $k$  to the trail. After storing  $k$ 's implication reason in  $reason(k)$ , BCP calculates and stores  $k$ 's implication level  $level(k)$ . The implication level calculation comprises the only difference between CB and NCB versions of BCP. The current decision level always serves as the implication level for NCB, while the maximal level in  $\beta$  is the implication level for CB. Note that in CB a literal may be implied *not* at the current decision level. As usual, BCP returns the falsified conflicting clause, if such is discovered.

Finally, consider the implementation of **Backtrack** in Algorithm 3. For the NCB case, given the target decision level  $bl$ , **Backtrack** simply unassigns and pops all the literals from the trail  $\nu$ , whose decision level is greater than  $bl$ . The CB case is different, since literals assigned at different decision levels are interleaved on the trail. When backtracking to decision level  $bl$ , **Backtrack** removes all the literals assigned after  $bl$ , but it puts aside all the literals assigned before  $bl$  in a queue  $\mu$  maintaining their relative order. Afterwards,  $\mu$ 's literals are returned to the trail in the same order.

## 2.2 Combining CB and NCB

Our algorithm can easily be modified to heuristically choose whether to use CB or NCB for any given conflict. The decision can be made, for each conflict, in the

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**Algorithm 2.** BCP

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$dl$ : current decision level  
 $\nu$ : the trail, stack of decisions and implications  
 $_{ncb}$ : marks the NCB code  
 $_{cb}$ : marks the CB code  
 BCP()  
 1: **while**  $\nu$  contains at least one unvisited literal **do**  
 2:    $l :=$  first literal in  $\nu$ , unvisited by BCP  
 3:    $wcls :=$  clauses watched by  $l$   
 4:   **for**  $\beta \in wcls$  **do**  
 5:     **if**  $\beta$  is unit **then**  
 6:        $k :=$  the unassigned literal of  $\beta$   
 7:       Push  $k$  to the end of  $\nu$   
 8:        $reason(k) := \beta$   
 9:        $_{ncb} level(k) := dl$   
 10:        $_{cb} level(k) := \max$  level in  $\beta$   
 11:     **else**  
 12:       **if**  $\beta$  is falsified **then**  
 13:         **return**  $\beta$   
**return**  $null$

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**Algorithm 3.** Backtrack

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$dl$ : current decision level  
 $\nu$ : the trail, stack of decisions and implications  
 $level\_index(bl + 1)$ : the index in  $\nu$  of  $bl + 1$ 's decision literal  
 Backtrack( $bl$ ) : **NCB version**  
 Assume:  $bl < dl$

```

1: while  $\nu.size() \geq level\_index(bl + 1)$  do
2:   Unassign  $\nu.back()$ 
3:   Pop from  $\nu$ 

```

**Backtrack( $bl$ ) : CB Version**

Assume:  $bl < dl$

```

1: Create an empty queue  $\mu$ 
2: while  $\nu.size() \geq level\_index(bl + 1)$  do
3:   if  $level(\nu.back()) \leq bl$  then
4:     Enqueue  $\nu.back()$  to  $\mu$ 
5:   else
6:     Unassign  $\nu.back()$ 
7:   Pop from  $\nu$ 
8: while  $\mu$  is not empty do
9:   Push  $\mu.first()$  to the end of  $\nu$ 
10:  Dequeue from  $\mu$ 

```

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main function in Algorithm 1 by setting the backtrack level to either the second highest decision level in  $\sigma$  for NCB (line 12) or the previous decision level for CB (line 13).

In our implementation, NCB is always applied before  $\mathbf{C}$  conflicts are recorded since the beginning of the solving process, where  $\mathbf{C}$  is a user-given threshold. After  $\mathbf{C}$  conflicts, we apply CB whenever the difference between the CB backtrack level (that is, the previous decision level) and the NCB backtrack level (that is, the second highest decision level in  $\sigma$ ) is higher than a user-given threshold  $\mathbf{T}$ .

We introduced the option of delaying CB for  $\mathbf{C}$  first conflicts, since backtracking chronologically makes sense only after the solver had some time to aggregate variable scores, which are quite random in the beginning. When the scores are random or close to random, the solver is less likely to proceed with the same decisions after NCB.

### 3 Experimental Results

We have implemented CB in `Maple_LCM_Dist` [7], which won the main track of the SAT Competition 2017 [5], and in `Open-WBO`, which won the complete unweighted track of the MaxSAT Evaluation 2017 [1]. The updated code of both solvers is available in [8]. We study the impact of CB with different values of the two parameters,  $\mathbf{T}$  and  $\mathbf{C}$ , in `Maple_LCM_Dist` and `Open-WBO` on SAT Competition 2017 and MaxSAT Evaluation 2017 instances, respectively. For all the tests we used machines with 32 GB of memory running Intel® Xeon® processors with 3 GHz CPU frequency. The time-out was set to 1800 s. All the results refer only to benchmarks solved by at least one of the participating solvers.

#### 3.1 SAT Competition

In preliminary experiments, we found that  $\{\mathbf{T} = 100, \mathbf{C} = 4000\}$  is the best configuration for `Maple_LCM_Dist`. Table 1 shows the summary of run time and unsolved instances of the default `Maple_LCM_Dist` vs. the best configuration in CB mode,  $\{\mathbf{T} = 100, \mathbf{C} = 4000\}$ , as well as “neighbor” configurations  $\{\mathbf{T} = 100, \mathbf{C} = 3000\}$ ,  $\{\mathbf{T} = 100, \mathbf{C} = 5000\}$ ,  $\{\mathbf{T} = 90, \mathbf{C} = 4000\}$  and  $\{\mathbf{T} = 110, \mathbf{C} = 4000\}$ . Figure 2 and Fig. 3 compare the default `Maple_LCM_Dist` vs. the overall winner  $\{\mathbf{T} = 100, \mathbf{C} = 4000\}$  on satisfiable and unsatisfiable instances respectively. Several observations are in place.

First, Table 1 shows that  $\{\mathbf{T} = 100, \mathbf{C} = 4000\}$  outperforms the default `Maple_LCM_Dist` in terms of for both the number of solved instances and the run-time. It solves 3 more benchmarks and is faster by 4536 s.

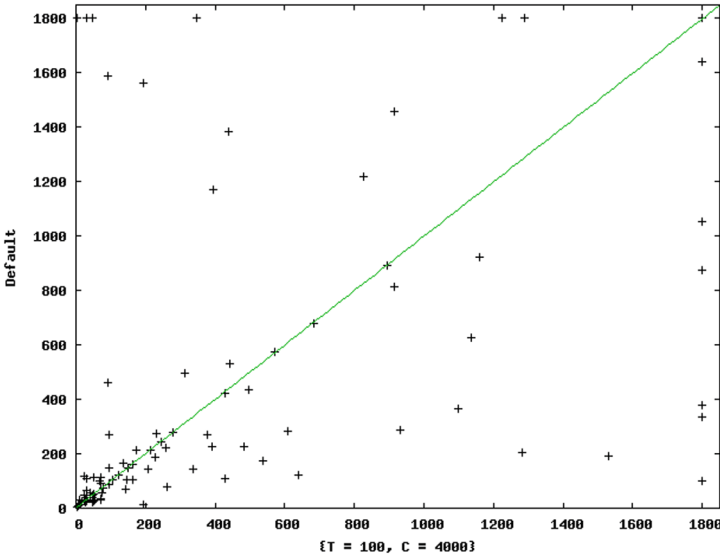
Second, CB is consistently more effective on unsatisfiable instances. Table 1 demonstrates that the best configuration for unsatisfiable instances  $\{\mathbf{T} = 100, \mathbf{C} = 5000\}$  solves 4 more instances than the default configuration and is faster by 5783 s. The overall winner  $\{\mathbf{T} = 100, \mathbf{C} = 4000\}$  solves 3 more unsatisfiable benchmarks than the default and is faster by 5113 s. Figure 3 shows that CB is beneficial on the vast majority of unsatisfiable instances. Interestingly, we found that there is one family on which CB consistently yields significantly better results: the 27 instances of the g2-T family. On that family, the run-time in CB mode is never worse than that in NCB mode. In addition, CB helps to

solve 4 more benchmarks than the default version and causes the solver to be faster by 1.5 times on average.

Finally, although the overall winner is slightly outperformed by the default configuration on satisfiable instances, CB can be tuned for satisfiable instances too.  $\{T = 100, C = 3000\}$  solves 2 additional satisfiable instances, while  $\{T = 110, C = 4000\}$  solves 1 additional instance faster than the default. We could not pinpoint a family, where CB shows a significant advantage on satisfiable instances.

**Table 1.** Results of `Maple_LCM_Dist` on SAT competition 2017 instances

		Base	T = 100			C = 4000	
SAT	Unsolved	13	11	13	16	20	12
	Time	50003	53362	50580	59167	59482	47748
UNSAT	Unsolved	6	5	3	2	4	6
	Time	58414	54034	53301	52631	52481	53991
ALL	Unsolved	19	16	16	18	24	18
	Time	108417	107396	103881	111798	111963	101739



**Fig. 2.** `Maple_LCM_Dist` on SAT

### 3.2 MaxSAT Evaluation

In preliminary experiments, we found that  $\{T = 75, C = 250\}$  is the best configuration for `Open-WBO` with CB. Consider the five left-most columns of Table 2.



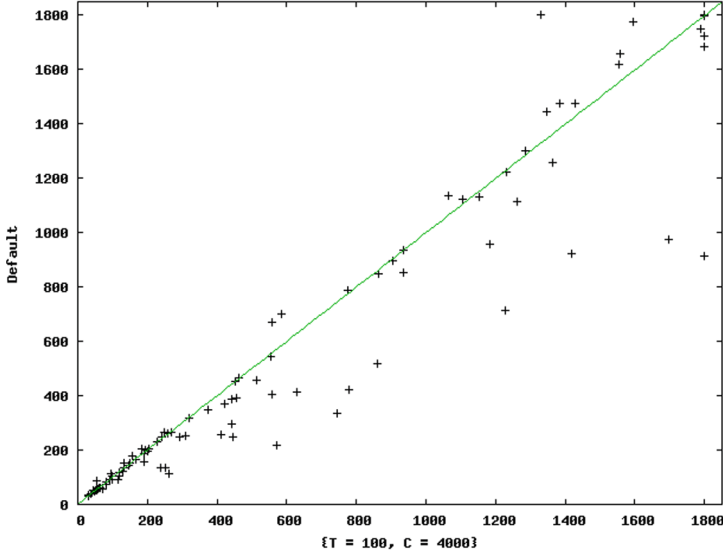


Fig. 3. Maple\_LCM\_Dist on UNSAT

Table 2. Results of **Open-WBO** on MaxSAT evaluation 2017 instances

Family	Default		{75, 250}		{75, 0}		{75, 500}		{50, 250}		{100, 250}	
	#S	Time	#S	Time	#S	Time	#S	Time	#S	Time	#S	Time
Grand Total	639	53048	644	50704	642	51370	640	52406	640	53582	643	51022
kbtrees	0	3600	2	2756	1	3332	2	2921	2	2771	2	2733
atcoss-sugar	11	2179	12	1812	12	1328	11	2013	11	2004	12	1889
close-solutions	32	2692	33	4235	32	2711	32	2597	33	2589	32	4382
extension-enforcement	7	1963	8	828	7	1975	7	1942	8	1093	8	1306
gen-hyper-tw	5	4348	6	3871	6	3219	5	4057	5	3901	7	3383
treewidth-computation	24	3407	25	2306	24	3661	25	2169	23	4527	24	3778
atcoss-mesat	11	1660	11	605	11	703	11	610	11	674	11	534
min-fill	4	1105	4	413	4	384	4	910	4	244	4	349
packup	35	697	35	253	35	172	35	460	35	252	35	253
scheduling	1	206	1	92	1	153	1	164	1	141	1	130
bcp-syn	21	2535	20	2643	21	2247	21	2642	20	3145	20	2733
mbd	35	1327	34	1982	34	1972	34	2006	35	1275	35	1222
hs-timetableing	1	48	1	317	1	276	1	968	1	396	1	453

They present the number of solved instances and the run-time of the default **Open-WBO** vs.  $\{T = 75, C = 250\}$  (abbreviated to  $\{75, 250\}$ ) over the MaxSAT Evaluation families (complete unweighted track). The second row shows the overall results. CB helps **Open-WBO** to solve 5 more instances in less time. The subsequent rows of Table 2 show the results for families, where either **Open-WBO** or  $\{T = 75, C = 250\}$  was significantly faster than the other solver, that is, it either solved more instances or was at least two times as fast. One can see that CB significantly improved the performance of **Open-WBO** on 10 families, while the performance was significantly deteriorated on 3 families only. The other columns of Table 2 present the results of 4 configurations neighbor to  $\{T = 75, C = 250\}$  for reference.

## 4 Conclusion

We have shown how to implement Chronological Backtracking (CB) in a modern SAT solver as an alternative to Non-Chronological Backtracking (NCB), which has been commonly used for over two decades. We have integrated CB into the winner of the SAT Competition 2017, **Maple\_LCM\_Dist**, and the winner of MaxSAT Evaluation 2017 **Open-WBO**. CB improves the overall performance of both solvers. In addition, **Maple\_LCM\_Dist** becomes consistently faster on unsatisfiable instances, while **Open-WBO** solves 10 families significantly faster.

## References

1. Ansotegui, C., Bacchus, F., Järvisalo, M., Martins, R. (eds.): MaxSAT evaluation 2017: solver and benchmark descriptions, Department of Computer Science Series of Publications B. University of Helsinki, vol. B-2017-2 (2017)
2. Biere, A., Heule, M., van Maaren, H., Walsh, T. (eds.): Handbook of Satisfiability, Volume 185 of Frontiers in Artificial Intelligence and Applications. IOS Press, Amsterdam (2009)
3. Eén, N., Sörensson, N.: An extensible SAT-solver. In: Giunchiglia, E., Tacchella, A. (eds.) SAT 2003. LNCS, vol. 2919, pp. 502–518. Springer, Heidelberg (2004). [https://doi.org/10.1007/978-3-540-24605-3\\_37](https://doi.org/10.1007/978-3-540-24605-3_37)
4. Frost, D., Dechter, R.: In search of the best constraint satisfaction search. In: AAAI, pp. 301–306 (1994)
5. Heule, M., Järvisalo, M., Balyo, T.: SAT competition (2017). <https://baldur.itikit.edu/sat-competition-2017/>
6. Katebi, H., Sakallah, K.A., Marques-Silva, J.P.: Empirical study of the anatomy of modern SAT solvers. In: Sakallah, K.A., Simon, L. (eds.) SAT 2011. LNCS, vol. 6695, pp. 343–356. Springer, Heidelberg (2011). [https://doi.org/10.1007/978-3-642-21581-0\\_27](https://doi.org/10.1007/978-3-642-21581-0_27)
7. Luo, M., Li, C.-M., Xiao, F., Manyà, F., Lü, Z.: An effective learnt clause minimization approach for CDCL SAT solvers. In: Sierra, C. (ed.), Proceedings of the Twenty-Sixth International Joint Conference on Artificial Intelligence IJCAI 2017, Melbourne, Australia, 19–25 August 2017, pp. 703–711 (2017). [ijcai.org](http://ijcai.org)
8. Nadel, A., Ryvchin, V.: Chronological backtracking: solvers. [goo.gl/ssukuu](http://goo.gl/ssukuu)
9. Neves, M., Martins, R., Janota, M., Lynce, I., Manquinho, V.: Exploiting resolution-based representations for MaxSAT solving. In: Heule, M., Weaver, S. (eds.) SAT 2015. LNCS, vol. 9340, pp. 272–286. Springer, Cham (2015). [https://doi.org/10.1007/978-3-319-24318-4\\_20](https://doi.org/10.1007/978-3-319-24318-4_20)
10. Pipatsrisawat, K., Darwiche, A.: A lightweight component caching scheme for satisfiability solvers. In: Marques-Silva, J., Sakallah, K.A. (eds.) SAT 2007. LNCS, vol. 4501, pp. 294–299. Springer, Heidelberg (2007). [https://doi.org/10.1007/978-3-540-72788-0\\_28](https://doi.org/10.1007/978-3-540-72788-0_28)
11. Prosser, P.: Hybrid algorithms for the constraint satisfaction problem. *Comput. Intell.* **9**(3), 268–299 (1993)
12. Marques Silva, J.P., Lynce, I., Malik, S.: Conflict-driven clause learning SAT solvers. In: Biere et al. 2, pp. 131–153

13. Marques Silva, J.P., Sakallah, K.A.: GRASP - a new search algorithm for satisfiability. In: ICCAD, pp. 220–227 (1996)
14. Shtrichman, O.: Tuning SAT checkers for bounded model checking. In: Emerson, E.A., Sistla, A.P. (eds.) CAV 2000. LNCS, vol. 1855, pp. 480–494. Springer, Heidelberg (2000). [https://doi.org/10.1007/10722167\\_36](https://doi.org/10.1007/10722167_36)