An Automatic Finite-Sample Robustness Metric: Can Dropping a Little Data Make a Big Difference?

Ryan Giordano (rgiordan@mit.edu)¹ January 2022

¹With coauthors Rachael Meager (LSE) and Tamara Broderick (MIT)

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The conclusions of one's statistical analysis may depend on only a **small** fraction of the data, even for highly significant results in correctly specified models.

We provide a **generally applicable tool** to detect such sensitivity. Our methods are **efficiently and automatically computable**, and come with **finite-sample accuracy guarantees** and **clear intuition**.

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	Beta (SE)
Original result	-4.55 (5.88)

The original conclusion: No evidence that microcredit is effective...

⇒ Standard errors can be inadequate summaries of data sensitivity!

Cannot find influential subsets by brute force! $\binom{16,560}{15}\approx 1.5\cdot 10^{51}$

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The original conclusion: No evidence that microcredit is effective... ... can be reversed by dropping less than 0.1% of the data.

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Outline

- Why and when might you care about sensitivity to data dropping?
- How does our approximation work, and when is it accurate?
 - (A formalization of the problem and the class of estimators we study.)
- Examine real-life examples of analyses: some sensitive, some not. (The results may defy your intuition.)
- What kinds of analyses are sensitive to data dropping?
 - (Including comparison to standard errors and gross-error robustness.)

Dropping data: Motivation

Would you be concerned if you could **reverse your conclusion** by removing a **small proportion** of your data?

Not always! But sometimes, surely yes.

Thinking without random noise can be helpful.

Suppose you have a farm, and want to know whether your average yield is >170 bushels per acre. At harvest, you measure 200 bushels per acre.

- Scenario one: If your yield is greater than 170 bushels per acre, you
 make a profit.
 - Don't care about sensitivity to small subsets
- Scenario two: You want to recommend your farming methods to a friend across the valley.
 - Might care about sensitivity to small subsets

For example, often in economics:

- Policy population is different from analyzed population,
- Small fractions of data are missing not-at-random,
- We report a convenient summary (e.g. mean) of a complex effect.

Formalizing the question.

Ordinary least squares

A data point d_n has regressors x_n and response y_n : $d_n = (x_n, y_n)$.

The estimator $\hat{\theta} \in \mathbb{R}^p$ satisfies:

$$\hat{\theta} := \arg\min_{\boldsymbol{\theta}} \frac{1}{2} \sum_{n=1}^{N} \left(y_n - \boldsymbol{\theta}^{T} \boldsymbol{x}_n \right)^2$$

$$\Leftrightarrow \sum_{n=1}^{N} \left(y_n - \hat{\theta}^T x_n \right) x_n = 0.$$

Make a qualitative decision using:

- ullet A particular component: $heta_k$
- The end of a confidence interval: $\theta_k + \frac{1.96}{\sqrt{N}} \hat{\sigma}(\hat{\theta})$

Z-estimators

We observe N data points d_1, \ldots, d_N (in any domain).

The estimator $\hat{\theta} \in \mathbb{R}^p$ satisfies:

$$\sum_{n=1}^{N} G(\hat{\theta}, d_n) = 0_{P}.$$

 $G(\cdot, d_n)$ is "nice," \mathbb{R}^p -valued. E.g. OLS, MLE, VB, IV &c.

Make a qualitative decision using $\phi(\hat{\theta})$ for a smooth, real-valued ϕ .

(WLOG try to increase $\phi(\hat{\theta})$.)

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- \bullet There are ${N \choose \lfloor \alpha N \rfloor}$ sets to check. (Huge even for $\alpha \ll 1.)$
- ullet Evaluating $\hat{ heta}$ re-solving the estimating equation.
 - E.g., re-computing the OLS estimator.
 - Other examples are even harder (VB, machine learning)

Idea: Smoothly approximate the effect of leaving out points.

We have N data points d_1, \ldots, d_N , a quantity of interest $\phi(\cdot)$, and

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Original weights: $\vec{1} = (1, \dots, 1)$

Leave points out by setting their elements of \vec{w} to zero.



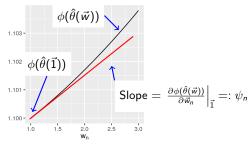
The map $\vec{w}\mapsto\phi(\hat{\theta}(\vec{w}))$ is well-defined even for continuous weights.

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The slopes ψ_n are the **empirical influence function** [Hampel, 1986]. We call them "influence scores."

We can use ψ_n to form a Taylor series approximation:

$$\phi(\hat{ heta}(\vec{w})) pprox \phi^{ ext{lin}}(\vec{w}) := \phi(\hat{ heta}(\vec{1})) + \sum_{n=1}^{N} \psi_n(\vec{w}_n - 1)$$

Taylor series approximation.

Problem: How much can you change $\phi(\hat{\theta}(\vec{w}))$ dropping $\lfloor \alpha N \rfloor$ points? Combinatorially hard by brute force!

Approximate Problem: How much can you change $\phi^{\text{lin}}(\hat{\theta}(\vec{w}))$ dropping $|\alpha N|$ points? **Easy!**

$$\phi^{\mathrm{lin}}(\vec{w}) := \phi(\hat{\theta}(\vec{1})) + \sum_{n=1}^{N} \psi_n(\vec{w}_n - 1)$$

Dropped points have $\vec{w}_n - 1 = -1$. Kept points have $\vec{w}_n - 1 = 0$ \Rightarrow The most influential points for $\phi^{\text{lin}}(\vec{w})$ have the most negative ψ_n .

Procedure: (see rgiordan/zaminfluence on github)

- **1** Compute your original estimator $\hat{\theta}(\vec{1})$.
- ② Compute and sort the influence scores $\psi_{(1)}, \ldots, \psi_{(N)}$.
- Worry if $-\sum_{n=1}^{\lfloor \alpha N \rfloor} \psi_{(n)}$ is large enough to change your conclusions.

How to compute the ψ_n 's? And how accurate is the approximation?

How to compute the influence scores?

How can we compute the influence scores $\psi_n = \frac{\partial \phi(\hat{\theta}(\vec{w}))}{\partial \vec{w}_n}\Big|_{\vec{1}}$?

By the **chain rule**,
$$\psi_n = \frac{\partial \phi(\theta)}{\partial \theta} \Big|_{\hat{\theta}(\vec{1})} \frac{\partial \hat{\theta}(\vec{w})}{\partial \vec{w}_n} \Big|_{\vec{1}}$$
.

Recall that $\sum_{n=1}^{N} \vec{w}_n G(\hat{\theta}(\vec{w}), d_n) = 0_P$ for all \vec{w} near $\vec{1}$.

- \Rightarrow By the **implicit function theorem**, we can write $\frac{\hat{\theta}(\vec{w})}{\partial \vec{w}_n}\Big|_{\vec{1}}$ as a linear system involving $G(\cdot, \cdot)$ and its derivatives.
- \Rightarrow The ψ_n are automatically computable from $\hat{\theta}(\vec{1})$ and software implementations of $G(\cdot,\cdot)$ and $\phi(\cdot)$ using **automatic differentiation**.

```
import jax
import jax.numpy as np
def phi(theta):
    ... computations using np and theta ...
    return value

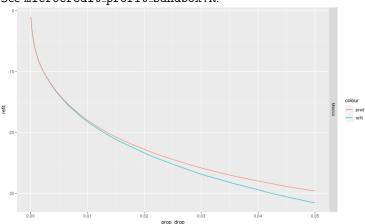
# Exact gradient of phi (1st term in the chain rule):
jax.grad(phi)(theta_opt)
```

See rgiordan/vittles on github.

How accurate is the approximation?

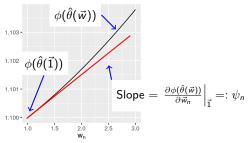
Mexico example:

See $microcredit_profit_sandbox.R.$



How accurate is the approximation?

By conrolling the curvature, we can control the error in the linear approximation.



We provide **finite-sample theory** [Giordano et al., 2019] showing that

$$\left|\phi(\hat{ heta}(\vec{w})) - \phi^{\mathrm{lin}}(\vec{w})
ight| = O\left(\left\|\frac{1}{N}(\vec{w} - \vec{1})\right\|_2^2\right) = O\left(lpha
ight) ext{ as } lpha o 0.$$

But you don't need to rely on the theory!

Our method returns which points to drop. **Re-running once** without those points provides an **exact lower bound** on the worst-case sensitivity.

Selected experimental results.

Original estimate (SE)	Refit estimate (SE)	Observations dropped
-4.549 (5.879)	7.030 (2.549)*	15 = 0.09%

Table: Microcredit Mexico results [Angelucci et al., 2015].

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Table: Microcredit Mexico results [Angelucci et al., 2015].

Study case	Original estimate (SE)	Target change	Refit estimate	Observations dropped
Poor, period 10	33.861 (4.468)*	Sign change Significance change Significant sign change	-2.559 (3.541) 4.806 (3.684) -9.416 (3.296)*	697 = 6.63% 435 = 4.14% 986 = 9.37%

Table: Cash transfers results. [Angelucci and De Giorgi, 2009]

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Health notpoor 12m	0.029 (0.005)*	Sign change Significance change Significant sign change	-0.001 (0.005) 0.008 (0.005) -0.009 (0.004)*	156 = 0.67% 101 = 0.43% 224 = 0.96%

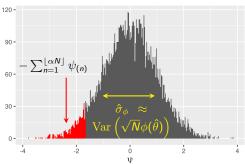
Table: Medicaid profit results [Finkelstein et al., 2012]

What makes an estimator non-robust? A tail sum.

We show that
$$\phi^{\text{lin}}(\vec{w}^*) - \phi(\hat{\theta}) = -\sum_{n=1}^{\lfloor \alpha N \rfloor} \psi_{(n)} =: \hat{\sigma}_{\phi} \hat{\mathcal{T}}_{\alpha}$$
 where

- ullet The "noise" $\hat{\sigma}_{\phi}^2
 ightarrow \mathrm{Var}(\sqrt{N}\phi)$
 - $\hat{\sigma}_{\phi}^2=$ is the robust "sandwich" variance estimator [Hampel, 1986]
- The "shape" $\hat{\mathscr{T}}_{\alpha} \leq \sqrt{\alpha(1-\alpha)}$ determined by ψ_n distribution

Influence score histogram (N = 10000, α = 0.05)



Example.

Report non-robustness if:

$$\phi^{\mathrm{lin}}(\vec{w}^*) - \phi(\hat{\theta}) = \hat{\sigma}_{\phi} \hat{\mathscr{T}}_{\alpha} \geq \Delta \qquad \Leftrightarrow \qquad \frac{\Delta}{\hat{\sigma}_{\phi}} \leq \hat{\mathscr{T}}_{\alpha}.$$

The **signal to noise ratio** $\frac{\Delta}{\hat{\sigma}_{\phi}}$ determines sensitivity to data dropping.

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Let's analyze with $\alpha = 0.01 = 1\%$.

$$\begin{array}{llll} \phi(\hat{\theta}) = & -0.029 & (\text{Increase QOI by defn}) & \Delta = & 0.029 \\ \hat{\sigma}_{\phi} = & 0.766 & (\text{Noise}) & \frac{1}{\sqrt{N}} \hat{\sigma}_{\phi} = & 0.005 & (\text{SE}) \\ & & & & \\ \hat{\mathcal{T}}_{\alpha} = & 0.046 & (\text{Shape}) & \frac{1.96}{\sqrt{N}} = & 0.0128 & \rightarrow 0 \text{ as } N \rightarrow \infty \\ & & & & \\ \hat{\mathcal{T}}_{\alpha} \hat{\sigma}_{\phi} = & 0.035 & (\text{Data dropping sensitivity}) & \frac{1.96}{\sqrt{N}} \hat{\sigma}_{\phi} = & 0.010 & (\text{SE sensitivity}) \end{array}$$

The noise is much larger than the signal \Rightarrow Sensitive to data dropping.

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Corollary: Leave- $\lfloor \alpha N \rfloor$ -out is different from standard errors. Standard errors reject when $\frac{\Delta}{\hat{\sigma}_{\alpha}} \leq \frac{1.96}{\sqrt{N}} \neq \hat{\mathcal{G}}_{\alpha}$.

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Corollary: Leave- $\lfloor \alpha N \rfloor$ -out robustness does not vanish as $N \to \infty$. Both $\hat{\mathscr{T}}_{\alpha}$ and $\hat{\sigma}_{\phi}$ typically converge to nonzero constants.

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Corollary: Non-robustness possible even with correct specification.

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Corollary: To robustify, reduce the noise or increase the signal.

Other forms of robustness

We proceeded as follows:

- Took presence of datapoints as a model input,
- Formed an automatically-computable differential approximation,
- Provided theory by analyzing higher-order derivatives,
- Studied its effectiveness in problems with open-access data.

Presence of datapoints is only one model input of many!

- Prior sensitivity in Bayesian nonparametrics [Giordano et al., 2021]
- Model sensitivity of MCMC output [Gustafson, 2000, Giordano et al., 2018]
- Cross-validation [Giordano et al., 2019, Wilson et al., 2020]
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- Frequentist variances of MCMC posteriors (in progress)

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- We can quickly and automatically find an approximate influential set which is accurate for small sets.
- Robustness to removing small sets is principally determined by the signal to noise ratio.
- In the present work, we studied data dropping. But we provide a framework for studying many other robustness questions, both to data and model perturbations.

Links and references

Tamara Broderick, Ryan Giordano, Rachael Meager (alphabetical authors) "An Automatic Finite-Sample Robustness Metric: Can Dropping a Little Data Change Conclusions?"

https://arxiv.org/abs/2011.14999

Open-source software:

R package zaminfluence https://github.com/rgiordan/zaminfluence Python package vittles https://github.com/rgiordan/vittles

Some related content can be found on my blog: https://rgiordan.github.io/

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