

MrPaw

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Are US non-voters becoming more Republican?

Blue Rose research says yes:

“Politically disengaged voters have become much more Republican, And because less-engaged voters swung away from [Democrats], an expanded electorate meant a more Republican electorate.”

[Blue Rose Research, 2024] (On Ezra Klein show, major professional pollsters)

On Data and Democracy says no:

“Claims of a decisive pro-Republican shift among the overall non-voting population are not supported by the most reliable, large-scale post-election data currently available.”

[Bonica et al., 2025] (Berkeley professor co-author, major professional researchers)

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- The problem is very hard (it's difficult to accurately poll non-voters)
 - Different data sources
 - **Very different statistical methods:** ★
 - Blue Rose uses Bayesian hierarchical modeling (MrP)
 - The CES uses weighted averages (calibration weighting)

Our contribution

We provide a calibration weighting interpretation of MrP analyses that:

- Is easily computable from MCMC draws and standard software, and
- Defines MrP versions of key diagnostics that motivate calibration weighting.

We provide apples-to-apples comparisons between MrP and calibration weighting.

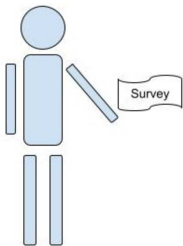
- Introduce the statistical problem and two methods (calibration weighting and MrP)
- Describe one of the classical calibration weighting diagnostics (covariate balance)
- Define MrPaw & state a key theorem
- Real-world results
- Future directions

The basic problem

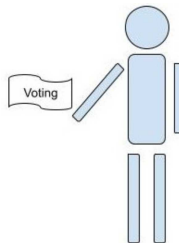
We have a survey population, for whom we observe:

- Covariates \mathbf{x} (e.g. race, gender, zip code, age, education level)
- Responses y (e.g. A binary response to “do you support policy such-and-such”)

We want the average response in a target population, in which we observe only covariates.



Observe (\mathbf{x}_s, y_s) for $s = 1, \dots, S$



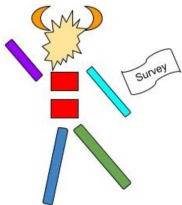
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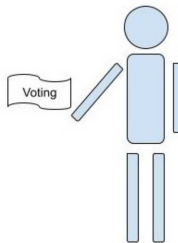
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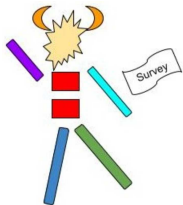
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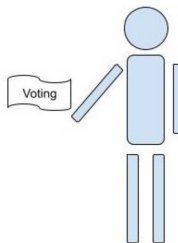
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The problem is that the populations are very different.

Our survey results may be biased.

How can we use the covariates to say something about the target responses?

Two approaches

We want $\mu := \frac{1}{T} \sum_{t=1}^T y_t$, but don't observe target population y_t .

- Assume $p(y|\mathbf{x})$ is the same in both populations,
- But the distribution of \mathbf{x} may be different in the survey and target.

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- Choose “calibration weights” w_s
(e.g. raking weights)

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- Partial pooling
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← (We open this box, providing analogues
of all these diagnostics)

What are we weighting for?¹

We want:

$$\text{Target average response} = \frac{1}{T} \sum_{t=1}^T y_p \approx \frac{1}{S} \sum_{s=1}^S w_s y_s = \text{Weighted survey average response}$$

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Even more, covariate balance is the criterion for a popular class of calibration weight estimators:

Raking calibration weights

“Raking” selects weights that

- Are as “close as possible” to some reference weights
- Under the constraint that they balance some selected regressors.

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We want to balance $f(\mathbf{x})$ because we think $\mathbb{E}[y|\mathbf{x}]$ might plausibly vary $\propto f(\mathbf{x})$, and want to check whether our estimator can capture this variability.

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Generalized covariate balance check (informal)

Pick a small δ , and define a *new response variable* \tilde{y} such that

$$\mathbb{E}[\tilde{y}|\mathbf{x}] = \mathbb{E}[y|\mathbf{x}] + \delta f(\mathbf{x}).$$

We know the change this is supposed to induce in the target population.

Covariate balance checks whether our estimators produce the same change.

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We know the expected change this perturbation produces in the target distribution:

$$\mathbb{E}[\mu(\tilde{y}) - \mu(y)|\mathbf{x}] = \frac{1}{T} \sum_{t=1}^T (\mathbb{E}[\tilde{y}|\mathbf{x}_p] - \mathbb{E}[y|\mathbf{x}_p]) = \delta \frac{1}{T} \sum_{t=1}^T f(\mathbf{x}_p)$$

Then, check whether your estimator $\hat{\mu}(\cdot)$ produces the same change:

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When $\hat{\mu}(\cdot) = \hat{\mu}_{\text{CAL}}(\cdot)$, this recovers the standard covariate balance check.

When $\hat{\mu}(y)$ is a calibration estimator, this is the same as covariate balance in expectation:

$$\mathbb{E} [\hat{\mu}(\tilde{y}) - \hat{\mu}(y) | \mathbf{x}] = \delta \frac{1}{S} \sum_{s=1}^S w_s f(\mathbf{x}_p) \stackrel{\text{check}}{=} \delta \frac{1}{T} \sum_{t=1}^T f(\mathbf{x}_p).$$

But now all we need to do is compare $\hat{\mu}(\tilde{y}) - \hat{\mu}(y)$ for “nearby” \tilde{y} and y .

We need to approximate $\hat{\mu}_{\text{MRP}}(\tilde{y}) - \hat{\mu}_{\text{MRP}}(y)$.

Step one: Define weights.

Noting that $w_s = \frac{d}{dy_s} \hat{\mu}_{\text{CAL}}$, we can define

$$w_s^{\text{MRP}} := \frac{d}{dy_s} \hat{\mu}_{\text{MRP}}.$$

It happens that the needed derivatives are given by simple a posteriori covariances involving only the inverse link function $m(\mathbf{x}; \theta)$ and log likelihood [Giordano et al., 2018]:

$$\frac{d\hat{y}_p}{dy_s} = \text{COV}_{\mathcal{P}(\theta | \text{Survey data})} \left(m(\mathbf{x}_p; \theta), \frac{\partial}{\partial y} \log p(y | \theta, \mathbf{x}_s) \right)$$

These can be computed using standard MCMC software [Bürkner, 2017].

No other weight definition will do — in some cases, MrP is exactly a calibration estimator (e.g. linear regression with flat priors), and we want the definitions to coincide in that case.

How to form a notion of covariate balance for estimators that are not weighted averages?

Calibration weights

$$\hat{\mu}_{\text{CAL}} = \frac{1}{S} \sum_{s=1}^S w_s y_s$$

MrP

Take $\hat{y}_p = \mathbb{E}_{\mathcal{P}(\theta|\text{Survey data})} [y|\mathbf{x}_p]$ and

$$\hat{\mu}_{\text{MRP}} = \frac{1}{T} \sum_{t=1}^T \hat{y}_p$$

Step two: Specify a Taylor series.

Suppose we wanted to re-compute MrP with new survey responses y_s^{new} .

$$\hat{\mu}_{\text{MRP}}(y_1^{\text{new}}, \dots, y_S^{\text{new}}) = \sum_{s=1}^S w_s^{\text{MRP}} (y_s^{\text{new}} - y_s) + \text{Residual}$$

In general, MrP is truly nonlinear. The residual is only small when $y_s^{\text{new}} \approx y_s$!

Step three: Define a data perturbation that captures regression balance.

Recall that our y is binary. How can we produce a \tilde{y} such that $\mathbb{E} [\tilde{y}|\mathbf{x}] = \mathbb{E} [y|\mathbf{x}] + \delta f(\mathbf{x})$?

- Use an estimate of $\mathbb{E} [y|\mathbf{x}]$ to draw new binary data, or
- Allow \tilde{y} to take values other than $\{0, 1\}$ and set $\tilde{y} = y + \delta f(\mathbf{x})$.

Focus on the second (we have examples of the first).

Theorem

- Let $\tilde{y} = y + \delta f(\mathbf{x})$,
- $\hat{\mu}_{\text{MRP}}$ be a hierarchical logistic regression posterior expectation, and
- \mathcal{F} be a class of uniformly bounded functions on \mathbf{x} .

Then, with probability approaching one, as $N \rightarrow \infty$,

$$\sup_{f \in \mathcal{F}} \left(\hat{\mu}_{\text{MRP}}(\tilde{y}) - \left(\hat{\mu}_{\text{MRP}}(y) + \sum_{s=1}^S w_s^{\text{MRP}} \delta f(\mathbf{x}_s) \right) \right) = O(\delta^2) \quad \text{as } \delta \rightarrow 0$$

The supremum over \mathcal{F} is the primary technical contribution! It means we are justified in searching over regressors to find imbalance.

Draws on our prior work on uniform and finite-sample error bounds for Bernstein–von Mises theorem–like results [Giordano and Broderick, 2024, Kasprzak et al., 2025].

In practice, compute

$$\text{Imbalance}(f) := \sum_{s=1}^S w_s^{\text{MRP}} f(\mathbf{x}_s) - \frac{1}{T} \sum_{t=1}^T f(\mathbf{x}_p)$$

for any $f(\cdot)$ you think might capture variability in y .

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