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- 3. Try to capture important properties of p with simple $\mathcal Q$
 - Begins with understanding how things go wrong (this paper!)
 - Hope to have our cake and eat it too (e.g. marginals and easy computation)
 - Much harder! But important, with big potential benefits

I would love to see more work like this!

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Two very common approaches to $\ensuremath{\mathsf{VI}}$ are:

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Why is n the right scaling? Why do we care about the numerical entropy gap anyway?

It's clear why variance matters. Less so the entropy gap, epsecially as n changes.