Variational inference (VI) finds  $q^* := \operatorname{argmin}_{q \in \mathcal{Q}} \operatorname{KL}(q||p)$  for an unknown target p. What should  $\mathcal{Q}$  be?

 $\mathsf{Variational} \ \mathsf{inference} \ (\mathsf{VI}) \ \mathsf{finds} \ q^* := \mathrm{argmin}_{q \in \mathcal{Q}} \ \mathsf{KL} \left( q || p \right) \ \mathsf{for} \ \mathsf{an} \ \mathsf{unknown} \ \mathsf{target} \ p.$ 

What should  ${\mathcal Q}$  be?

Classical VI takes a simple Q. Then  $p \notin Q$ , but you get computational benefits!

Variational inference (VI) finds  $q^* := \operatorname{argmin}_{q \in \mathcal{Q}} \operatorname{KL}(q||p)$  for an unknown target p.

What should  ${\mathcal Q}$  be?

Classical VI takes a simple Q. Then  $p \notin Q$ , but you get computational benefits!

But when  $p \notin \mathcal{Q}$ , can get poor posterior approximations even in simple cases.

What to do?

Variational inference (VI) finds  $q^* := \operatorname{argmin}_{q \in \mathcal{Q}} \operatorname{KL}(q||p)$  for an unknown target p.

What should Q be?

Classical VI takes a simple Q. Then  $p \notin Q$ , but you get computational benefits!

But when  $p \notin \mathcal{Q}$ , can get poor posterior approximations even in simple cases.

#### What to do?

- 1. Don't care ("machine learning")
  - Evaluate by other criteria than poterior approximations (e.g. prediction)
  - Maybe fine for some machine learning tasks

Variational inference (VI) finds  $q^* := \operatorname{argmin}_{q \in \mathcal{Q}} \operatorname{KL}(q||p)$  for an unknown target p.

What should Q be?

Classical VI takes a simple Q. Then  $p \notin Q$ , but you get computational benefits!

But when  $p \notin \mathcal{Q}$ , can get poor posterior approximations even in simple cases.

#### What to do?

- 1. Don't care ("machine learning")
  - Evaluate by other criteria than poterior approximations (e.g. prediction)
  - Maybe fine for some machine learning tasks
- 2. Make Q more expressive ("modern VI")
  - Strong theoretical guarantees
  - High computational cost!

Variational inference (VI) finds  $q^* := \operatorname{argmin}_{q \in \mathcal{Q}} \operatorname{KL}(q||p)$  for an unknown target p.

What should Q be?

Classical VI takes a simple Q. Then  $p \notin Q$ , but you get computational benefits!

But when  $p \notin \mathcal{Q}$ , can get poor posterior approximations even in simple cases.

#### What to do?

- 1. Don't care ("machine learning")
  - Evaluate by other criteria than poterior approximations (e.g. prediction)
  - Maybe fine for some machine learning tasks
- 2. Make Q more expressive ("modern VI")
  - Strong theoretical guarantees
  - High computational cost!
- 3. Try to capture important properties of p with simple  $\mathcal Q$ 
  - Begins with understanding how things go wrong (this paper!)
  - Hope to have our cake and eat it too (e.g. marginals and easy computation)
  - Much harder! But important, with big potential benefits

I would love to see more work like this!