An Automatic Finite-Sample Robustness Metric: Can Dropping a Little Data Make a Big Difference?

Ryan Giordano (rgiordan@mit.edu)¹ January 2022

¹With coauthors Rachael Meager (LSE) and Tamara Broderick (MIT)

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The conclusions of one's statistical analysis may depend on only a **small** fraction of the data, even for highly significant results in correctly specified models.

We provide a **generally applicable tool** to detect such sensitivity. Our methods are **efficiently and automatically computable**, and come with **finite-sample accuracy guarantees** and **clear intuition**.

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	Beta (SE)
Original result	-4.55 (5.88)

The original conclusion: No evidence that microcredit is effective...

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Outline

- Why and when might you care about sensitivity to data dropping?
- How does our approximation work, and when is it accurate?
 - (A formalization of the problem and the class of estimators we study.)
- Examine real-life examples of analyses: some sensitive, some not. (The results may defy your intuition.)
- What kinds of analyses are sensitive to data dropping?
 - (Including comparison to standard errors and gross-error robustness.)

Dropping data: Motivation

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Would you be concerned if you could **reverse your conclusion** by removing a **small proportion** (say, 0.1%) of your data? Not always! But sometimes, surely yes.

Thinking without random noise can be helpful.

Suppose you have a farm, and want to know whether your average yield is greater than 170 bushels per acre. At harvest, you measure 200 bushels per acre.

- Scenario one: If your yield is greater than 170 bushels per acre, you
 make a profit.
 - Don't care about sensitivity to small subsets
- Scenario two: You want to recommend your farming methods to a friend across the valley.
 - Might care about sensitivity to small subsets

For example, often in economics:

- Small fractions of data are missing not-at-random,
- Policy population is different from analyzed population,
- We report a convenient summary (e.g. mean) of a complex effect,
- Models are stylized proxies of reality.

Formalizing the question.

Ordinary least squares

A data point d_n has regressors x_n and response y_n : $d_n = (x_n, y_n)$.

The estimator $\hat{\theta} \in \mathbb{R}^p$ satisfies:

$$\hat{\theta} := \arg\min_{\theta} \frac{1}{2} \sum_{n=1}^{N} \left(y_n - \theta^T x_n \right)^2$$

$$\Leftrightarrow \sum_{n=1}^{N} \left(y_n - \hat{\theta}^T x_n \right) x_n = 0.$$

Make a qualitative decision using:

- ullet A particular component: $heta_k$
- The end of a confidence interval: $\theta_k + \frac{1.96}{\sqrt{N}} \hat{\sigma}(\hat{\theta})$

Z-estimators

We observe N data points d_1, \ldots, d_N (in any domain).

The estimator $\hat{\theta} \in \mathbb{R}^p$ satisfies:

$$\sum_{n=1}^N G(\hat{\theta},d_n)=0_P.$$

 $G(\cdot, d_n)$ is "nice," \mathbb{R}^p -valued. E.g. OLS, MLE, VB, IV &c.

Make a qualitative decision using $\phi(\hat{\theta})$ for a smooth, real-valued ϕ .

Question: Can we make a big change in $\phi(\hat{\theta})$ by dropping $\lfloor \alpha N \rfloor$ datapoints, for some small proportion α ?

Which estimators do we study?

We have N data points d_1,\ldots,d_N , a quantity of interest $\phi(\hat{ heta})$, and

$$\sum_{n=1}^N G(\hat{\theta},d_n)=0_P.$$

Question: Can we make a big change in $\phi(\hat{\theta})$ by dropping $\lfloor \alpha N \rfloor$ datapoints, for some small proportion α ? **Two big problems:**

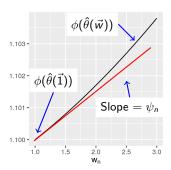
- \bullet There are ${N\choose |\alpha N|}$ sets to check. (Huge even for $\alpha\ll 1.)$
- Evaluating $\hat{\theta}$ re-solving the estimating equation.
 - E.g., re-computing the OLS estimator.
 - Other examples are even harder (VB, machine learning)

An approximation is needed!

Which estimators do we study?

$$\hat{\theta} := \vec{\theta} \text{ such that } \sum_{n=1}^{N} G(\vec{\theta}, d_n) = 0_P.$$

W, W2 ...

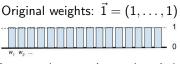


The slopes $\psi_n := \frac{\partial \phi(\hat{\theta}(\vec{w}))}{\partial \vec{w}_n} \Big|_{\vec{1}}$ are values of the **empirical influence** function [Hampel, 1986]. We call them "influence scores."

Second-order derivatives control the error of the linear approximation.

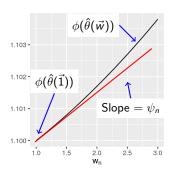
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$$\hat{\theta}(\vec{w}) := \vec{\theta}$$
 such that $\sum_{n=1}^{N} \vec{w}_n G(\vec{\theta}, d_n) = 0_P$.



Leave points out by setting their elements of \vec{w} to zero.





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Problem: How large can you make $\phi(\hat{\theta}(\vec{w}))$ leaving out no more than $\lfloor \alpha N \rfloor$ points? **Combinatorially hard!**

To simplify the search over \vec{w} , we form the Taylor series approximation:

$$\phi(\hat{\theta}(\vec{w})) \approx \phi^{\text{lin}}(\vec{w}) := \phi(\hat{\theta}(\vec{1})) + \sum_{n=1}^{N} \psi_n(\vec{w}_n - 1)$$

Approximate solution: How large can you make $\phi^{\text{lin}}(\vec{w})$ leaving out no more than $|\alpha N|$ points? **Easy!**

The most influential points for $\phi^{\text{lin}}(\vec{w})$ have the most negative ψ_n .

The ψ_n are automatically computable using the **implicit function** theorem and automatic differentiation.

We provide finite-sample theory showing that

$$\left|\phi(\hat{\theta}(\vec{w})) - \phi^{\text{lin}}(\vec{w})\right| = O\left(\left\|\frac{1}{N}(\vec{w} - \vec{1})\right\|_{2}^{2}\right) = O(\alpha) \text{ as } \alpha \to 0.$$

Procedure:

① Compute the "original" estimator, $\hat{\theta}(\vec{1})$ and $\phi(\hat{\theta}(\vec{1}))$.

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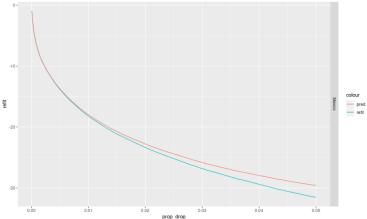
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- **3** Report non-robustness if $\phi^{\text{lin}}(\vec{w}^*) \phi(\hat{\theta}) = -\sum_{n=1}^{\lfloor \alpha N \rfloor} \psi_{(n)} \geq \Delta$.

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- **Optional:** Compute $\hat{\theta}(\vec{w}^*)$, and verify that $\phi(\hat{\theta}(\vec{w}^*)) \phi(\hat{\theta}) \geq \Delta$.

Mexico example:

See ${\tt microcredit_profit_sandbox.R.}$



Selected experimental results.

Study case	Original estimate (SE)	Target change	Refit estimate	Observations dropped
Mexico	-4.549 (5.879)	Sign change Significance change Significant sign change	0.398 (3.194) -10.962 (5.565)* 7.030 (2.549)*	1 = 0.01% $14 = 0.08%$ $15 = 0.09%$

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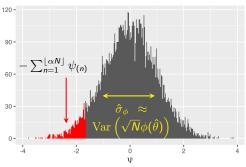
Table: Medicaid profit results [Finkelstein et al., 2012]

What makes an estimator non-robust? A tail sum.

We show that
$$\phi^{\text{lin}}(\vec{w}^*) - \phi(\hat{\theta}) = -\sum_{n=1}^{\lfloor \alpha N \rfloor} \psi_{(n)} =: \hat{\sigma}_{\phi} \hat{\mathcal{T}}_{\alpha}$$
 where

- ullet The "noise" $\hat{\sigma}_{\phi}^2
 ightarrow \mathrm{Var}(\sqrt{N}\phi)$
 - $\hat{\sigma}_{\phi}^2=$ is the robust "sandwich" variance estimator [Hampel, 1986]
- The "shape" $\hat{\mathscr{T}}_{\alpha} \leq \sqrt{\alpha(1-\alpha)}$ determined by ψ_n distribution

Influence score histogram (N = 10000, α = 0.05)



Example.

Report non-robustness if:

$$\phi^{\mathrm{lin}}(\vec{w}^*) - \phi(\hat{\theta}) = \hat{\sigma}_{\phi} \hat{\mathscr{T}}_{\alpha} \geq \Delta \qquad \Leftrightarrow \qquad \frac{\Delta}{\hat{\sigma}_{\phi}} \leq \hat{\mathscr{T}}_{\alpha}.$$

The **signal to noise ratio** $\frac{\Delta}{\hat{\sigma}_{\phi}}$ determines sensitivity to data dropping.

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Let's analyze with $\alpha = 0.01 = 1\%$.

$$\begin{array}{llll} \phi(\hat{\theta}) = & -0.029 & (\text{Increase QOI by defn}) & \Delta = & 0.029 \\ \hat{\sigma}_{\phi} = & 0.766 & (\text{Noise}) & \frac{1}{\sqrt{N}}\hat{\sigma}_{\phi} = & 0.005 & (\text{SE}) \\ \hat{\mathcal{T}}_{\alpha} = & 0.046 & (\text{Shape}) & \frac{1.96}{\sqrt{N}} = & 0.0128 & \rightarrow 0 \text{ as } N \rightarrow \infty \\ \hat{\mathcal{T}}_{\alpha}\hat{\sigma}_{\phi} = & 0.035 & (\text{Data dropping sensitivity}) & \frac{1.96}{\sqrt{N}}\hat{\sigma}_{\phi} = & 0.010 & (\text{SE sensitivity}) \end{array}$$

The noise is much larger than the signal \Rightarrow Sensitive to data dropping.

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Corollary: To robustify, reduce the noise or increase the signal.

Other forms of robustness

We proceeded as follows:

- Took presence of datapoints as a model input,
- Formed an automatically-computable differential approximation,
- Provided theory by analyzing higher-order derivatives,
- Studied its effectiveness in problems with open-access data.

Presence of datapoints is only one model input of many!

- Prior sensitivity in Bayesian nonparametrics [Giordano et al., 2021]
- Model sensitivity of MCMC output [Gustafson, 2000, Giordano et al., 2018]
- Cross-validation [Giordano et al., 2019, Wilson et al., 2020]
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- Frequentist variances of MCMC posteriors (in progress)

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- We can quickly and automatically find an approximate influential set which is accurate for small sets.
- Robustness to removing small sets is principally determined by the signal to noise ratio.
- In the present work, we studied data dropping. But we provide a framework for studying many other robustness questions, both to data and model perturbations.

Links and references

Tamara Broderick, Ryan Giordano, Rachael Meager (alphabetical authors) "An Automatic Finite-Sample Robustness Metric: Can Dropping a Little Data Change Conclusions?"

https://arxiv.org/abs/2011.14999

Open-source software:

R package zaminfluence https://github.com/rgiordan/zaminfluence Python package vittles https://github.com/rgiordan/vittles

Some related content can be found on my blog: https://rgiordan.github.io/

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