

# Thesis Title VB QMC... Entanglement...

by

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I hereby declare that I am the sole author of this thesis. This is a true copy of the thesis, including any required final revisions, as accepted by my examiners.

I understand that my thesis may be made electronically available to the public.

## **Abstract**

In this thesis we present...

## Acknowledgements

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