external vertices of $H_1$	$P_u$	$P_v$	$P_z$
v, w, z	(u,w)	(v)	(z)
u, w, z	(u)	(v,w)	(z)
u, v, w	(u)	(v)	(z,w)