```
In [1]:
        import pandas
                                                            pd
                                                   as
         import numpy
                                                   as
                                                            np
         import matplotlib.pyplot
                                                   as
                                                            plt
                IPython.display
         from
                                                   import
                                                           display
         from
                pylab
                                                           rcParams
                                                   import
         from
                datetime
                                                            datetime, timedelta
                                                   import
         from
                pandas.tseries.offsets
                                                   import BDay
         from statsmodels.tsa.stattools
                                                   import
                                                            adfuller
         from statsmodels.tsa.stattools
                                                   import
                                                            pacf
         from statsmodels.tsa.stattools
                                                   import
                                                            acf
         from statsmodels.graphics.tsaplots
                                                   import
                                                            plot pacf
         from statsmodels.graphics.tsaplots
                                                   import plot_acf
         from statsmodels.graphics.gofplots
                                                   import
                                                           qqplot
         from statsmodels.tsa.seasonal
                                                   import seasonal decompose
         from
                statsmodels.tsa.api
                                                            ExponentialSmoothing, Holt
                                                   import
         from statsmodels.tsa.arima.model
                                                   import
                                                            ARIMA
         from sklearn.metrics
                                                   import
                                                           mean_squared_error
         import warnings
        warnings.filterwarnings('ignore')
        %matplotlib inline
         import itertools
 In [2]:
        plt.rcParams['figure.figsize'] = 12,8
 In [3]:
        df = pd.read_csv('retail_sales.csv')
        df.head()
Out [3]:
                   ds
                           у
        0 1992-01-01 146376
         1 1992-02-01
                      147079
        2 1992-03-01
                     159336
        3 1992-04-01 163669
        4 1992-05-01 170068
 In [4]:
        df.head(),df.tail()
Out [4]: (
                  ds
        0 1992-01-01
                     146376
           1992-02-01
                     147079
        2 1992-03-01
                     159336
        3 1992-04-01 163669
        4 1992-05-01
                     170068.
                    dς
        288 2016-01-01
                       400928
        289
             2016-02-01
                       413554
        290 2016-03-01 460093
         291
             2016-04-01
                       450935
        292 2016-05-01 471421)
 In [5]:
        date = pd.date_range(start='1992/01/01',end='2016/05/01',freq=BDay())
        date
'2016-04-18', '2016-04-19', '2016-04-20', '2016-04-21', '2016-04-22', '2016-04-25', '2016-04-26', '2016-04-27', '2016-04-28', '2016-04-29'],
                    dtype='datetime64[ns]', length=6348, freq='B')
```

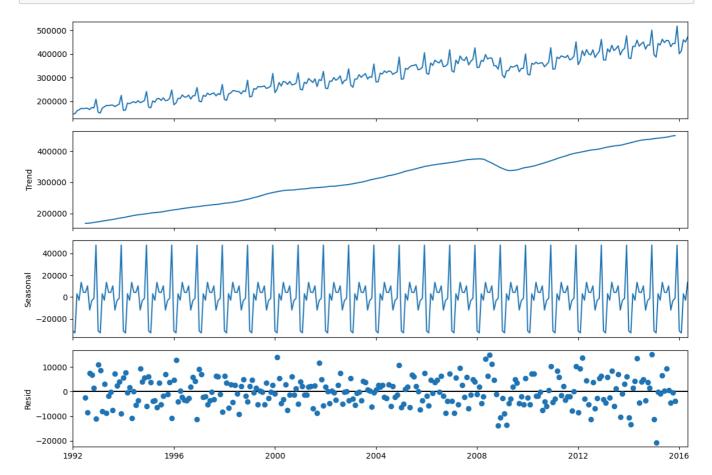
```
In [6]:
        df['time_stamp'] = pd.to_datetime(df['ds'],format='%Y-%m-%d')
        df = df.set_index('time_stamp')
        df = df.drop('ds',axis=1)
        df.head()
Out [6]:
                         у
         time_stamp
         1992-01-01
                    146376
         1992-02-01
                    147079
         1992-03-01
                    159336
         1992-04-01
                    163669
         1992-05-01
                    170068
 In [7]:
        df.plot()
        plt.show()
                   - у
         500000
         450000
                                   400000
         350000
         300000
         250000
         200000
         150000
                    1994
                                       1999
                                                         2004
                                                                            2009
                                                                                               2014
                                                        time_stamp
 In [8]:
        df.isnull().sum()
Out [8]: y 0 dtype: int64
In [9]:
        df.describe()
Out [9]:
        count
               293.000000
               308971.310580
         mean
               86084.323897
          std
               146376.000000
          min
          25%
               234503.000000
```

50%

314051.000000

75% 375795.000000 **max** 518253.000000

```
In [10]: decompose_add = seasonal_decompose(df,model='add')
    decompose_add.plot()
    plt.show()
```



```
In [11]: decompose_mul = seasonal_decompose(df,model='mul')
    decompose_mul.plot()
    plt.show()
```

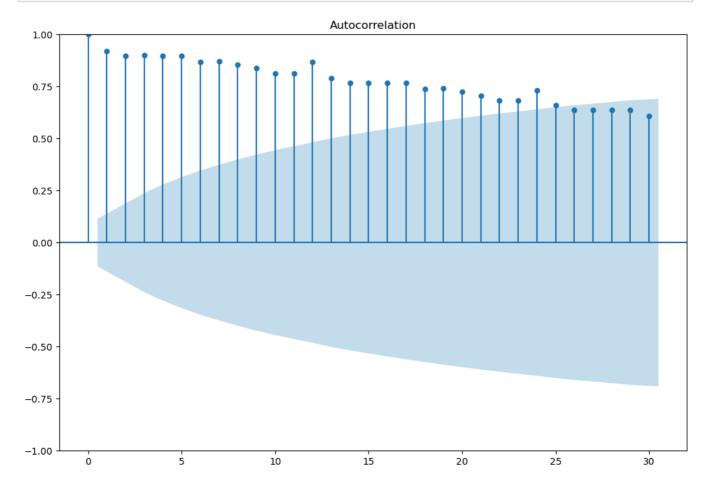
```
who had a factor of the forting and a factor of the forting and the factor of the fact
                             500000
                             400000
                             300000
                             200000
                             400000
                        300000
                             200000
                                  1.15
                                  1.10
                                  1.05
                                  1.00
                                  0.95
                                  0.90
                                    1.0
                                     0.8
                                Po.0
                                    0.4
                                    0.2
                                     0.0
                                                                                  1996
                                                                                                                            2000
                                                                                                                                                                                                                                                          2012
                                                                                                                                                                                                                                                                                                     2016
                                       1992
                                                                                                                                                                      2004
                                                                                                                                                                                                                2008
In [12]:
                        observation_df = df.values
                        result_df = adfuller(observation_df)
                        print(f"ADF test statistics: {result_df[0]}")
                        print(f"p_value: {result_df[1]}")
                        print(f"Used lags: {result_df[2]}")
                        print(f"Number of observations: {result_df[3]}")
                        for key,value in result_df[4].items():
                                     print(f"{key}: {value}")
                        print(f"IC best: {result_df[5]}")
                      ADF test statistics: -0.6443250505938629
                      p_value: 0.8606486181958646
                      Used lags: 15
                      Number of observations: 277
                      1%: -3.4541800885158525
5%: -2.872031361137725
                      10%: -2.5723603999791473
                      IC best: 5671.009371066914
In [13]: df_diff = df.diff(periods=1).dropna()
                        observation_diff = df_diff.values
                        result_diff = adfuller(observation_diff)
                        print(f"ADF test statistics: {result_diff[0]}")
                        print(f"p_value: {result_diff[1]}")
                        print(f"used lags: {result_diff[2]}")
                        print(f"Number of observations: {result_diff[3]}")
                        for key,values in result_diff[4].items():
                                     print(f"{key}: {values}")
                        print(f"IC Best: {result_diff[5]}")
```

ADF test statistics: -3.437937154315123 p_value: 0.009731610960261502 used lags: 14 Number of observations: 277 1%: -3.4541800885158525

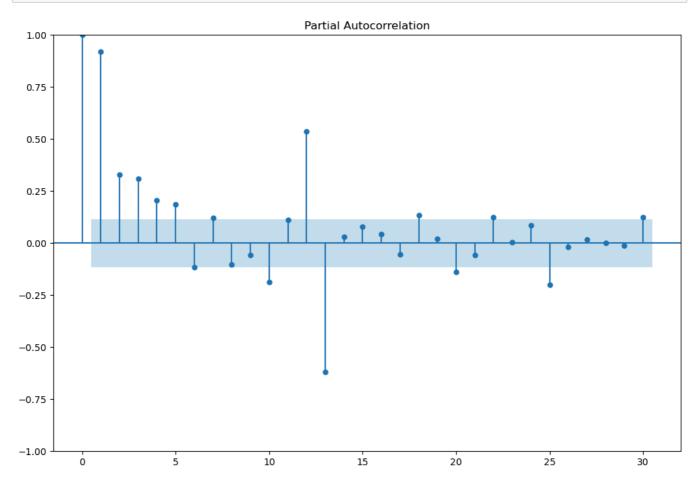
5%: -2.872031361137725

10%: -2.5723603999791473 IC Best: 5649.985617927769

In [14]: plot_acf(df,lags=30)
 plt.show()

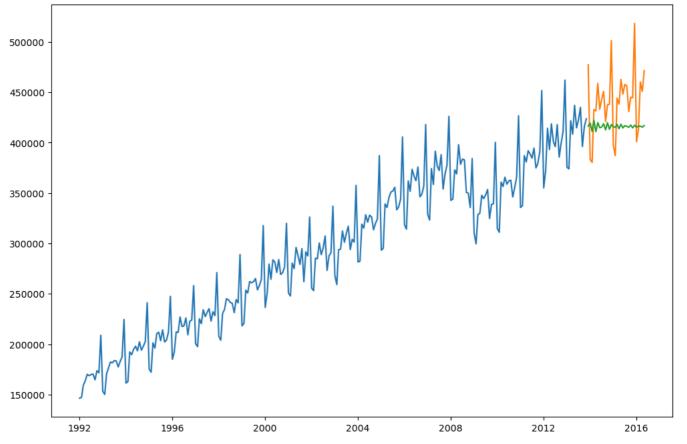


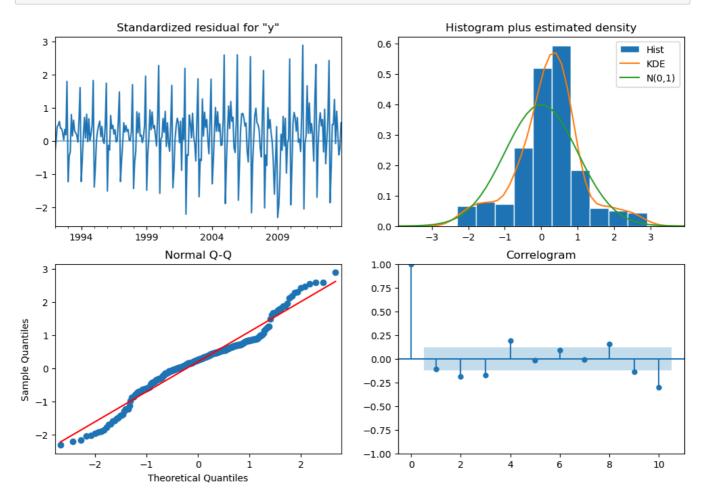
In [15]: plot_pacf(df,lags=30)
 plt.show()



```
In [16]: df.head(),df.tail()
Out [16]: (
         time stamp
         1992-01-01
                    146376
         1992-02-01
                   147079
         1992-03-01
                   159336
         1992-04-01 163669
         1992-05-01 170068,
         time_stamp
                   400928
         2016-01-01
         2016-02-01 413554
         2016-03-01 460093
         2016-04-01 450935
         2016-05-01 471421)
 In [17]:
         train_set = datetime(2013,11,1)
         test\_set = datetime(2016, 5, 1)
         train = df[:train_set]
         test = df[train_set+timedelta(days=1):test_set]
In [18]:
         train.shape,test.shape
Out [18]: ((263, 1), (30, 1))
In [19]: train.isnull().sum()
Out [19]: y
        dtype: int64
In [20]: p = q = range(0,4)
         d = range(0,2)
         pdq = itertools.product(p,d,q)
         arima_model = []
         for i in pdq:
             model = ARIMA(train,order=i)
              result_arima = model.fit()
              arima_model.append((i,result_arima.aic))
In [21]:
         frame = pd.DataFrame(arima_model,columns=['param','aic'])
 In [22]:
         frame.sort_values(by='aic',ascending=True).head()
Out [22]:
              param
                             aic
         27 (3, 0, 3) 6000.167826
         19 (2, 0, 3) 6012.776444
         15 (1, 1, 3) 6014.462657
         23 (2, 1, 3) 6015.041477
         11 (1, 0, 3) 6015.902494
 In [23]:
         model_arima = ARIMA(train,order=(3,0,3))
         result_arima_1 = model_arima.fit()
         print(result arima 1.summary())
                                    SARIMAX Results
        Dep. Variable:
                                            No. Observations:
                                                                           263
                                                                     -2992.084
                            ARIMA(3, 0, 3)
        Model:
                                            Log Likelihood
        Date:
                           Wed, 19 Feb 2025
                                            AIC
                                                                      6000.168
                                  22:07:04
                                                                      6028.745
        Time:
                                            BIC
                                01-01-1992
                                            HQIC
                                                                      6011.652
        Sample:
                               - 11-01-2013
        Covariance Type:
        [0.025
                             std err
                                                   P>|z|
                                                                      0.975]
                       coef
```

```
const
                  2.94e+05 1.41e-09 2.08e+14
                                               0.000
                                                       2.94e+05
                                                                2.94e+05
                                   -12.999
                           0.050
                                               0.000
        ar.L1
                   -0.6535
                                                         -0.752
                                                                  -0.555
                                              0.000
                                    35.956
                   0.7872
                             0.022
                                                         0.744
        ar.L2
                                                                   0.830
                                     17.986
                             0.048
                   0.8660
                                               0.000
                                                         0.772
                                                                   0.960
        ar.L3
        ma.L1
                   1.0641
                             0.079
                                     13.476
                                               0.000
                                                         0.909
                                                                   1.219
                                     -5.842
                   -0.4956
                            0.085
                                               0.000
                                                        -0.662
        ma.L2
                                                                  -0.329
                   -0.7968
                              0.072
                                     -11.056
                                                0.000
                                                         -0.938
                                                                   -0.656
        ma.L3
                4.862e+08 1.36e-10 3.58e+18
        sigma2
                                               0.000
                                                      4.86e+08
                                                               4.86e+08
        ______
        Ljung-Box (L1) (Q):
                                       3.03 Jarque-Bera (JB):
                                                                       12.21
        Prob(Q):
                                       0.08
                                           Prob(JB):
        Heteroskedasticity (H):
                                       2.11
                                            Skew:
                                                                        -0.10
        Prob(H) (two-sided):
                                       0.00
                                            Kurtosis:
                                                                        4.04
        ______
        Warnings:
        [1] Covariance matrix calculated using the outer product of gradients (complex-step).
        [2] Covariance matrix is singular or near-singular, with condition number 4.51e+33. Standard errors may be unstable.
In [24]:
        from sklearn.metrics import root_mean_squared_error
In [25]:
        class Evaluate:
             def Rmse(y_true,y_pred):
                 return root_mean_squared_error(y_true,y_pred)
             def Mape(y_true,y_pred):
                 return np.mean((np.abs(y_true-y_pred))/y_true)*100
In [26]:
        arima_pred = result_arima_1.forecast(len(test))
In [27]:
        Evaluate.Rmse(test['y'],arima_pred)
Out [27]: 38866.408528879765
In [28]:
        Evaluate.Mape(test['y'],arima_pred)
Out [28]: 7.309302838308487
In [29]:
        plt.plot(train)
        plt.plot(test)
        plt.plot(arima_pred)
        plt.show()
```





In [31]: model_exp = ExponentialSmoothing(train, trend='additive', seasonal='additive', initialization
 result_exp = model_exp.fit()
 print(result_exp.summary())

```
Seasonal:
                                                                                                                 Additive
                                                                                                                                               AICC
                                                                                                                                                                                                                                  4633.613
                           Seasonal Periods:
                                                                                                                                                                                                            Wed, 19 Feb 2025
                                                                                                                                 12
                                                                                                                                               Date:
                           Box-Cox:
                                                                                                                         False
                                                                                                                                               Time:
                                                                                                                                                                                                                                   22:07:05
                           Box-Cox Coeff.:
                                                                                                   coeff
                                                                                                                                                                code
                                                                                                                                                                                                                 optimized
                           smoothing_level
                                                                                                              0.5000000
                                                                                                                                                                                   alpha
                                                                                                                                                                                                                                                True
                           smoothing_trend
                                                                                                                       0.0001
                                                                                                                                                                                      beta
                                                                                                                                                                                                                                                True
                                                                                                             0.3250000
                                                                                                                                                                                                                                                True
                           smoothing_seasonal
                                                                                                                                                                                    gamma
                           initial_level
                                                                                                           1.6654e+05
                                                                                                                                                                                         1.0
                                                                                                                                                                                                                                                True
                           initial_trend
                                                                                                              972.51187
                                                                                                                                                                                                                                                True
                           initial_seasons.0
                                                                                                            -24263.224
                                                                                                                                                                                                                                                 True
                           initial_seasons.1
                                                                                                            -24717.464
                                                                                                                                                                                                                                                True
                                                                                                            -1087.3281
                                                                                                                                                                                                                                                True
                           initial_seasons.2
                           initial_seasons.3
                                                                                                            -2654.0052
                                                                                                                                                                                                                                                True
                           initial_seasons.4
                                                                                                              6487.0990
                                                                                                              3994.2552
                           initial_seasons.5
                                                                                                                                                                                                                                                 True
                           initial seasons.6
                                                                                                              739.52604
                                                                                                                                                                                                                                                True
                           initial_seasons.7
                                                                                                             4860.1094
                                                                                                                                                                                                                                                True
                           initial_seasons.8
                                                                                                            -4216.2552
                                                                                                                                                                                                                                                True
                           initial_seasons.9
                                                                                                            -193.24479
                                                                                                                                                                                                                                                 True
                           initial_seasons.10
                                                                                                              2540.8698
                                                                                                                                                                                      s.10
                                                                                                                                                                                                                                                True
                                                                                                              38509.661
                           initial_seasons.11
                                                                                                                                                                                                                                                True
   In [32]:
                             pred_exp = result_exp.forecast(len(test))
   In [33]:
                             plt.plot(train)
                             plt.plot(test)
                             plt.plot(pred_exp)
                             plt.show()
                              500000
                                                                                     Jahahan Jahahan Jahahan Jahan 
                              450000
                              400000
                              350000
                              300000
                              250000
                              200000
                              150000
                                                         1992
                                                                                                   1996
                                                                                                                                              2000
                                                                                                                                                                                         2004
                                                                                                                                                                                                                                   2008
                                                                                                                                                                                                                                                                             2012
                                                                                                                                                                                                                                                                                                                        2016
   In [34]:
                             Evaluate.Rmse(test['y'],pred_exp)
Out [34]: 8054.220053734076
  In [35]:
                             Evaluate.Mape(test['y'],pred_exp)
Out [35]: 1.456057930754873
   In [36]:
```

Model:

Trend:

Optimized:

ExponentialSmoothing

resuduals = test['y'].values - pred_exp.values

SSE

AIC

BIC

True

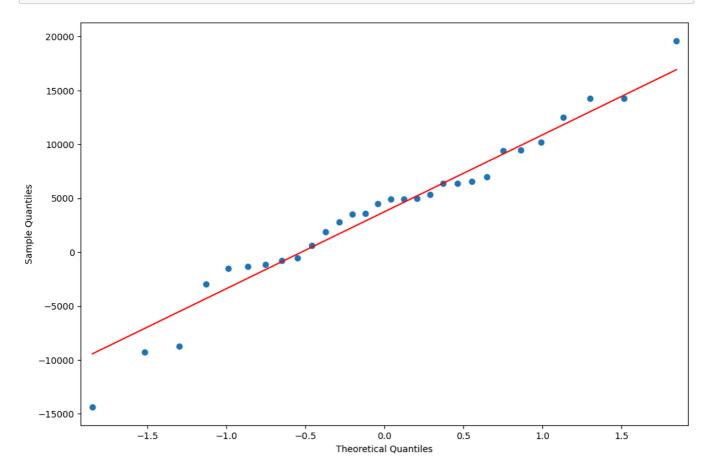
Additive

10327972264.770

4630.810

4687.964

```
In [37]: qqplot(resuduals,line='s')
plt.show()
```



In [38]: model_exp_tune = ExponentialSmoothing(train['y'],trend='add',seasonal='mul',seasonal_perio
 result_exp_tune = model_exp_tune.fit()
 print(result_exp_tune.summary())

```
ExponentialSmoothing Model Results
```

| Dep. Variable: | У | No. Observations: | 263 |
|-------------------|---|-------------------|------------------|
| Model: | ExponentialSmoothing | SSE | 9936302247.368 |
| Optimized: | True | AIC | 4620.642 |
| Trend: | Additive | BIC | 4677.796 |
| Seasonal: | Multiplicative | AICC | 4623.445 |
| Seasonal Periods: | 12 | Date: | Wed, 19 Feb 2025 |
| Box-Cox: | False | Time: | 22:07:06 |
| Box-Cox Coeff.: | None | | |
| ========== | ======================================= | | |
| | coeff | code | ontimized |

| | coeff | code | optimized |
|-------------------------------|------------|-------|-----------|
| smoothing_level | 0.5000000 | alpha | True |
| smoothing_trend | 0.0001 | beta | True |
| smoothing_seasonal | 0.2750000 | gamma | True |
| initial_level | 1.6654e+05 | 1.0 | True |
| initial_trend | 972.51187 | b.0 | True |
| <pre>initial_seasons.0</pre> | 0.8743406 | s.0 | True |
| <pre>initial_seasons.1</pre> | 0.8715923 | s.1 | True |
| <pre>initial_seasons.2</pre> | 0.9938863 | s.2 | True |
| <pre>initial_seasons.3</pre> | 0.9869043 | s.3 | True |
| <pre>initial_seasons.4</pre> | 1.0320753 | s.4 | True |
| <pre>initial_seasons.5</pre> | 1.0201988 | s.5 | True |
| <pre>initial_seasons.6</pre> | 1.0045706 | s.6 | True |
| <pre>initial_seasons.7</pre> | 1.0248818 | s.7 | True |
| <pre>initial_seasons.8</pre> | 0.9773991 | s.8 | True |
| initial_seasons.9 | 0.9998626 | s.9 | True |
| <pre>initial_seasons.10</pre> | 1.0129029 | s.10 | True |
| <pre>initial_seasons.11</pre> | 1.2013853 | s.11 | True |
| | | | |

```
In [40]:
        final_pred = result_final.forecast(30)
In [41]:
        plt.plot(train)
        plt.plot(test)
        plt.plot(final_pred)
        plt.show()
                        500000
        450000
        400000
        350000
        300000
        250000
        200000
        150000
                1992
                           1996
                                     2000
                                                2004
                                                           2008
                                                                      2012
                                                                                 2016
                                                                                           2020
In [42]:
        new = pd.DataFrame(final_pred,columns=['pred'])
        new.head()
Out [42]:
                          pred
                  454690.460806
        2016-06-01
        2016-07-01
                  460684.693340
        2016-08-01
                  466657.798203
        2016-09-01
                  438619.823755
```

2016-10-01

In []:

452555.354617