

# 1 Disinhibitory signaling enables flexible coding of top-down 2 information

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## 7 Abstract

8 Recent studies have proposed employing biologically plausible recurrent neural networks (RNNs)  
9 to investigate flexible decision-making in the brain. However, the mechanisms underlying the  
10 integration of bottom-up sensory inputs and temporally varying top-down factors (such as task  
11 instructions and selective attention) remain poorly understood, both within the context of these  
12 models and the brain. To address this knowledge gap, we trained biologically inspired RNNs on  
13 complex cognitive tasks that require adaptive integration of these factors. Through comprehensive  
14 analyses of RNNs and neural activity from mouse primary visual cortex, we show that sensory  
15 neurons in low-level areas possess the remarkable ability to multiplex and dynamically combine  
16 both bottom-up and top-down information via local inhibitory-to-inhibitory connections. Our  
17 results shed light on the role of disinhibitory circuits in the intricate interplay between bottom-up  
18 and top-down factors to enable flexible decision processes.

## 19 Introduction

20 Successfully navigating complex environments requires neural systems to efficiently encode and  
21 process incoming sensory inputs alongside contextual cues and task goals [1–3]. This capacity to  
22 integrate across different sources of information allows the brain to dynamically convert identical  
23 sensory inputs into diverse behavior in a context-dependent manner. Sensory inputs can be under-  
24 stood as bottom-up signals with regards to their encoding within lower cortical areas. In contrast,  
25 top-down factors refer to information regarding behavioral relevance of each stimulus, prior expec-  
26 tations about sensory statistics, and task contexts which provide guidelines for how the encoded  
27 sensory information should be interpreted and mapped onto behavior [4–8].

28 The ability to rapidly adapt to temporally varying top-down factors is a hallmark of cognitive  
29 flexibility and has been primarily attributed to the frontoparietal networks and medial temporal  
30 lobes [9–15]. However, the extent to which lower cortical areas contribute to this adaptive process is  
31 not well understood. Past works have shown that responses within sensory areas could be modulated  
32 by top-down signals such as selective attention [16–25], and that non-sensory information such as  
33 memory content can be decoded from activity within sensory areas [26–29]. Yet, it remains poorly  
34 understood how these neural codes complement computations that take place in higher cortical  
35 areas. This knowledge gap highlights the need for deeper insight into the computational principles  
36 and circuit mechanisms that enable flexible information processing for adaptive behavior.

37 In nature, where identical stimuli elicit diverse responses, inhibition may be a key mechanism  
38 in averting conflicting behaviors. This ensures the selection of appropriate sensorimotor mapping,  
39 aligning behavioral outcomes with the current task contexts rather than being driven solely by the  
40 stimuli. This account of inhibition as a modulatory mechanism, crucial for shaping task-optimized  
41 behavior, has been supported by past studies demonstrating the role of inhibition for the integration  
42 of top-down factors within the cortical hierarchy [17, 30–32]. In addition, discoveries of specialized  
43 sensory microcircuits that rely on inhibitory-to-inhibitory connections among local interneurons  
44 further highlight the importance of inhibitory function in flexible information processing [33–36].  
45 Notably, disinhibitory circuits have been proposed as key in facilitating top-down modulation of  
46 sensory coding [37–40], highlighting the plastic nature of neural codes within lower cortical areas.  
47 This account underscores the flexibility of neural codes along the cortical hierarchy and suggests a

48 potential mechanism for sensory multiplexing [41, 42].

49 Models based on recurrent neural networks (RNNs) of continuous-variable firing rate units have  
50 been widely used to provide computational explanations of experimental findings and to investigate  
51 neural correlates of cognitive functions, including sensory discrimination and working memory [9,  
52 43–49]. However, these studies primarily examine scenarios in which task goals and contextual cues  
53 remain fixed over time. This results in the models basing their responses largely on bottom-up  
54 processes such that the generated behaviors are mainly governed by the encoding of sensory inputs.

55 This approach may not fully capture the dynamics of the natural environment, where top-down  
56 information about current task demands is consistently present, exerting continuous influence on  
57 how we optimize the conversion of sensory inputs into appropriate behaviors. Importantly, these  
58 top-down factors, including selective attention, task contexts, and prior knowledge, can exhibit dis-  
59 tinct temporal structures, imposing varied but complementary guiding rules on how sensory input  
60 should be processed. This results in temporally rich and highly dynamic decision-making, a phe-  
61 nomenon that has proven challenging to investigate in artificial neural network models, including  
62 RNNs. Neglecting to account for the nuanced dynamics of top-down factors and their temporal  
63 influence limits our understanding of how neural systems efficiently integrate bottom-up and top-  
64 down signals to consistently produce optimal behavior. Additionally, we can gain better insights  
65 into this dynamic process through modifying the architecture of past models to incorporate several  
66 fundamental properties inherent in biological neural networks. These constraints, such as heteroge-  
67 nous neuronal timescales, cortical hierarchies, and the balance between inhibitory and excitatory  
68 connections, can offer valuable insights into the functionality of neural networks and the types of  
69 computations they can perform [50–53].

70 To address these knowledge gaps, we designed dynamic decision-making tasks that require  
71 seamless integration of bottom-up sensory inputs with top-down factors. These tasks included  
72 diverse top-down signaling with varying temporal dynamics as well as orthogonal manipulation  
73 of bottom-up and top-down signals. By training biologically plausible RNNs on these tasks and  
74 parsing the trained networks, we show that disinhibitory circuit motifs governed by inhibitory-to-  
75 inhibitory connections are critical for the intricate interplay between the two essential components  
76 of decision processes. By extending our model to incorporate the functional cortical hierarchy, we

77 further demonstrate that feedback signaling from higher-level areas and selective local inhibition  
78 enable lower-level areas to differentially process identical sensory inputs in a context-dependent  
79 manner. Moreover, we tested our model predictions using publicly available data recorded from  
80 the mouse primary visual cortex [54] and confirmed that local inhibitory-to-inhibitory connections  
81 within the visual cortex play an integral role in encoding top-down information.

82 Our results offer mechanistic insights into the dynamic integration of top-down and bottom-up  
83 signals during flexible information processing in a biological context. Within this comprehensive  
84 theoretical framework, we elucidate the computational principles employed by RNN models to  
85 flexibly utilize distinct top-down signals for guiding the analysis of sensory input, thereby optimizing  
86 behavior.

## 87 Results

88 **Recurrent neural network (RNN) model and dynamic decision-making tasks.** To un-  
89 derstand the cortical computations required for flexibly and optimally integrating bottom-up and  
90 top-down information, we employed a biologically plausible recurrent neural network (RNN) model  
91 consisted of continuous-variable firing units (model schematic shown in Fig. 1a right; see *Methods*)  
92 and trained the model to perform novel dynamic decision-making tasks (Fig. 1a,b). We utilized a  
93 gradient descent approach to train the RNN model, optimizing the recurrent connectivity weights,  
94 readout output weights, and synaptic decay time constants (see *Methods* for details). In addition,  
95 Dale's principle was enforced using the weight parametrization method introduced in [43].

96 These RNNs were employed to execute flexible decision-making tasks designed to achieve several  
97 distinct objectives. The first aim was to investigate how identical sensory inputs might be processed  
98 differently depending on distinct top-down inputs. These tasks also allowed for the independent  
99 manipulation of both bottom-up and top-down inputs. Lastly, the task incorporated separate  
100 stimulus modalities, each providing independent sources of top-down information. To meet these  
101 criteria in task design, we modified the classic delayed match-to-sample (DMS) task, commonly  
102 used in experimental studies [55–59], to develop one-modality DMS and two-modality DMS tasks.

103 For the one-modality DMS task (Fig. 1a), the RNN model received one stream of input stimulus  
104 signal (bottom-up) containing two sequential stimuli separated by a delay period. Each stimulus

105 was set to either +1 or -1. The model additionally received a task cue signal (top-down), indicating  
106 whether the network should employ the pro- or anti-DMS stimulus-response mapping. For the pro-  
107 DMS task (a task cue of +1 during the instruction period), the network was required to generate  
108 an output of +1 if the signs of the two stimuli matched, and -1 otherwise. For the anti-DMS  
109 (a task cue of -1 during the instruction period), the network was required to generate a negative  
110 output if the signs of the two stimuli were the same, and a positive output otherwise. The task cue  
111 was given either before (*early instruction*; 150-400 ms) or after the first stimulus (*late instruction*;  
112 650-900 ms; Fig. 1a).

113 Critically, in nature, not all aspects of sensory input are relevant to the task at hand (i.e., one-  
114 modality DMS task). To effectively navigate this, organisms rely on additional top-down signals,  
115 such as selective attention, alongside direct task signals to optimize decisions. To study this more  
116 complex scenario, we developed the two-modality DMS task by incorporating two streams of input  
117 stimulus signals (bottom-up; modality 1 and modality 2) and an attention cue (top-down) which  
118 instructs the model which stimulus modality is behaviorally relevant on a given trial and thus  
119 should be attended to (Fig. 1b; see *Methods*). An attention signal of -1 during the instruction  
120 period informs the model to focus on modality 1 while ignoring modality 2, and vice versa for a +1  
121 attention cue signal. The task cue manipulation is identical to that used in the one-modality DMS  
122 task. Similar to the one-modality task, the timing of the instruction period was manipulated such  
123 that task and attention cues were delivered either before (*early instruction*) or after the presentation  
124 of the first stimulus (*late instruction*).

125 For each decision task (one-modality DMS and two-modality DMS), we trained 20 RNNs to  
126 perform the task with high accuracy (> 95%; see *Methods*). For the one-modality DMS, the models  
127 performed the task accurately regardless of the timing of the instruction window (Fig. 1c). The  
128 model performance on the two-modality DMS was lower when the top-down cues were provided  
129 early ( $p < 0.001$ , two-sided Wilcoxon rank-sum test Fig. 1c). This can be attributed to the  
130 model's requirement to retain both the task and attention signals for a longer duration in the  
131 early instruction condition.

132 **Dynamic encoding of top-down information by RNNs.** After training RNNs to perform  
133 the dynamic decision tasks, we next investigated the effects of the top-down factors (task and

134 attention cues) on the network dynamics. To visualize RNN dynamics in response to distinct  
135 external inputs of both bottom-up and top-down signals under various conditions, we plotted  
136 the kinetic energy landscape (see *Methods*) of a representative RNN. This was achieved by using  
137 two principal components (Fig. 2a,b; see *Methods*). The kinetic energy landscape provides a useful  
138 guideline for understanding RNNs as dynamical systems. It offers a visual summary that illustrates  
139 how external inputs shape the structure of fixed points and “slow” points (local minima in the  
140 energy landscape) as well as neural trajectories within the state space [60–62]. Therefore, seeking  
141 to identify these fixed and “slow” points in the two-dimensional energy landscape enabled us to  
142 gain insight into how the task and attention signals influenced the RNN network dynamics.

143 We hypothesized that the presence of top-down cues would condition network dynamics even  
144 before the arrival of the bottom-up sensory inputs. In addition, we postulated that opposing cues  
145 would correspondingly lead to separable shifts in fixed point structure, which we first visualized  
146 through the energy landscape of the network during the first instruction period (150-400 ms, see  
147 Fig. 1a). For the one-modality DMS task, the energy landscape of the example RNN model  
148 displayed an area with an inverted U-shape where the kinetic energy was notably low (darker  
149 blue area in Fig. 2a). The local minimum of the landscape stayed around the center of this U-  
150 shaped profile during the period before the first stimulus presentation when the task cue was not yet  
151 presented (*no instruction*). However, when the task cue was presented early (*early instruction*), the  
152 local minimum shifted to the left and to the right for the pro- and anti-DMS condition, respectively  
153 (Fig. 2a).

154 For the two-modality DMS task, the energy landscape again revealed a U-shaped region char-  
155 acterized by a low-energy profile (dark blue in Fig. 2b). Consistent with what we observed in the  
156 one-modality task, the local minimum was situated at the center of the low energy structure during  
157 the first instruction period for late instruction trials, where no task or attention cues were yet  
158 presented (*no instruction*). Analyzing different combinations of the task and attention cue signals  
159 displayed distinct local minima points along the low-energy profile. For instance, the local minima  
160 corresponding to the pro-DMS signal were positioned to the right of the no-instruction minima.  
161 Along this pro-DMS “arm” of the energy trajectory, two local minima were observed: one corre-  
162 sponding to the modality-one attention signal and the other to the modality-two attention signal.

163 These results suggest that network dynamics shift as a function of the combination of top-down  
164 attention and task signals, in a dissociable manner even before the sensory inputs arrive.

165 Subsequently, we performed a quantitative fixed point search analysis [60] for different values  
166 of external input to the network during the first instruction period (150-400 ms, Fig. 1a). During  
167 this time, the network could receive either a pro-DMS, an anti-DMS, or no task cue (i.e., *late*  
168 *instruction* trials). We plotted network trajectories as well as fixed points discovered for each  
169 of these conditions in the principal component space, for the representative RNN performing the  
170 one-modality (Fig. 2c) and the two-modality DMS tasks (Fig. 2d). We observed that the presence  
171 and content of top-down signals given to the network not only altered its trajectories in the state  
172 space but also affected its fixed point structure. The network performing the two-modality DMS  
173 task exhibited a branching pattern that reflected symmetrical top-down coding across attended  
174 modalities for each task cue condition (anti- vs. pro-DMS).

175 To further examine network dynamics as a function of distinct top-down and bottom-up in-  
176 formation, we performed a manifold discovery analysis, utilizing the CEBRA method [63]. This  
177 approach enables latent structure discovery and has the advantage of conditioning latent structure  
178 discovery over variables of interest. Here, we performed an unsupervised analysis with regards to  
179 all task covariates except for time. This ensured that adjacent time points were mapped to closer  
180 points in latent space and that smooth latent dynamics were obtained. This method allowed us to  
181 determine the latent trajectory bifurcations in the state space following presentation of stimuli and  
182 top-down cues in the network performing the one-modality DMS (i.e., one-modality RNN; Fig. 2e)  
183 and the two-modality DMS tasks (i.e., two-modality RNN; Fig. 2f-i). In the one-modality RNN,  
184 the trajectories during the first instruction period were separated into three pathways correspond-  
185 ing to the pro-DMS cue signal (light green and light purple in Fig. 2e), anti-DMS cue signal (dark  
186 green and dark purple in Fig. 2e), and the absence of the task cue instruction (i.e. late instruction  
187 condition; gray in Fig. 2e). The pro-DMS and anti-DMS pathways were then further bifurcated  
188 based on the identity of the first stimulus during the first stimulus period. For the two-modality  
189 RNN, we observed similar latent trajectories for the attended modality (Fig. 2f). However, the bi-  
190 furcations driven by the identity of the first stimulus were not as well separated in the unattended  
191 modality (Fig. 2g). This pattern held true across pro- and anti-DMS trials, which exhibited qualita-

192 tively similar bifurcations (Fig. 2h,i). These findings were further confirmed by the cross-temporal  
193 discriminability analysis, which revealed that the identity of the first stimulus of the attended  
194 modality was more robustly encoded throughout the trial duration compared to the unattended  
195 modality (Fig. 2j–m; see *Methods*). Linear support vector machine (SVM) decoding analysis also  
196 revealed that the top-down cue signals were robustly encoded by the RNN models (Extended Data  
197 Fig. 1; see *Methods* for more details). These results suggest that lower-dimensionality represen-  
198 tations of network dynamics sufficiently capture the network’s flexibility in encoding stimuli in a  
199 context-dependent manner, depending on stimulus relevance, as flexibly determined by top-down  
200 cues.

201 **Inhibitory units play a critical role in both encoding and maintaining top-down infor-**  
202 **mation.** After establishing the model’s capacity for flexible encoding of top-down information, we  
203 next investigated the relative contributions of excitatory and inhibitory units in facilitating this  
204 process. Through dissection of the RNNs performing the one-modality and two-modality DMS  
205 tasks, we found that the optimized synaptic decay time constants for the excitatory units were  
206 significantly larger compared to the time constants of the inhibitory units ( $p < 0.001$ , two-sided  
207 Wilcoxon rank-sum test, Fig. 3a,b).

208 Building on these findings, which indicate distinct roles for excitatory and inhibitory units,  
209 we conducted a series of linear support vector machine (SVM) decoding analyses. These analyses  
210 aimed to decode the task cue identity (anti- vs. pro-DMS) from the activity of excitatory and  
211 inhibitory units within RNNs engaged in the one-modality DMS task (see *Methods*). While the  
212 task cue identity could be readily decoded from the activities of both excitatory and inhibitory  
213 units following the cue presentation on early instruction trials, the SVM decoding accuracy was  
214 significantly higher for the inhibitory units throughout the trial duration ( $p < 0.05$ , 2-sample KS  
215 test, Bonferroni corrected across time; Fig. 3c). We observed similar trends for RNNs performing  
216 the two-modality DMS task (Fig. 3d). In these models, the inhibitory units also exhibited stronger  
217 maintenance of the attention signal compared to the excitatory units (Fig. 3e). Interestingly,  
218 decoding performance for stimulus identity was higher in inhibitory units for both the attended  
219 and unattended modalities, when compared to excitatory units (Fig. 3f,g).

220 Given these findings that highlight the distinct role of inhibitory units on maintaining task-

221 related information, we next investigated their network-level implications through the functional  
222 connectivity patterns of inhibitory units. More specifically, we measured the functional closeness  
223 centrality of all units in each network across time (see *Methods*). Assuming that correlations  
224 between activation rates over time establish a metric of distance between units, it follows that  
225 units with greater centrality emerge as potential candidates for serving as functional hubs in their  
226 respective networks. While both excitatory and inhibitory units increased in centrality following  
227 the top-down cue presentation (*early instruction*) for the RNNs performing the one-modality and  
228 two-modality DMS tasks, the average centrality was higher for the inhibitory units after the onset  
229 of task and attention cue presentation ( $p < 0.05$ , two-sided 2-sample KS-test, Fig. 3h,i). Comparing  
230 the distribution of the centrality measure from individual units in the one-modality RNNs before  
231 (at 145 ms) and after (at 395 ms) the first instruction period on early instruction trials revealed  
232 that the centrality values of inhibitory units were distributed more widely post-instructions. This  
233 finding indicates the formation of inhibitory functional connectivity hubs following the top-down  
234 cue presentation (Fig. 3j,k). Taken together, these results suggest a central role for inhibitory units  
235 in encoding task-specific top-down information, as well as stimulus identity.

236 **Inhibitory-to-inhibitory connections carry top-down information.** Given the crucial role  
237 of inhibitory units in encoding and sustaining top-down signals, we next investigated the neural cir-  
238 cuity surrounding these inhibitory units to further elucidate their contribution to the maintenance  
239 of task-specific top-down information.

240 Lesioning inhibitory connections to inhibitory units selective for the anti-DMS task cue (by  
241 reducing synaptic weights by 50%; see *Methods*) in a representative RNN trained to perform the  
242 one-modality DMS task resulted in the disruption of anti-DMS task signaling (Fig. 4a). Conse-  
243 quently, the network exhibited a tendency to perform the pro-DMS task irrespective of the task  
244 cue presented. By visualizing the neural dynamics of this lesioned RNN using CEBRA [63], we  
245 confirmed that the neural trajectories were no longer separated by the task cue condition during  
246 the first instruction period in early instruction trials (Fig. 4b).

247 Motivated by these findings, we employed a systematic approach where we lesioned synaptic  
248 connections based on task cue selectivity (pro- vs. anti-DMS) and unit type (excitatory vs. in-  
249 hibitory) for the one-modality DMS task. We found that disrupting inhibitory-to-inhibitory ( $I \rightarrow I$ )

250 connections led to profound impairment in task performance (Fig. 4c top;  $**p < 0.01$ ,  $***p < 0.001$   
251 by two-sided Wilcoxon rank-sum test). Disrupting similarly tuned inhibitory connections impaired  
252 performance in both pro- and anti-DMS trials ( $Ia \rightarrow Ia$  and  $Ip \rightarrow Ip$  in Fig. 4c top;  $**p < 0.01$ ,  
253  $***p < 0.001$  by two-sided Wilcoxon rank-sum test). However, lesioning oppositely tuned  $I \rightarrow I$   
254 connections resulted in greater impairment in one type of task trials ( $Ia \rightarrow Ip$  and  $Ip \rightarrow Ia$  in  
255 Fig. 4c top;  $**p < 0.01$ ,  $***p < 0.001$  by two-sided Wilcoxon rank-sum test). We also observed  
256 significant changes in task performance when the  $I \rightarrow E$  connections were lesioned (Fig. 4c bot-  
257 tom;  $**p < 0.01$ ,  $***p < 0.001$  by two-sided Wilcoxon rank-sum test). The effects of lesioning task  
258 cue-specific connections were similar in the RNN models trained to perform the two-modality task  
259 (Fig. 4d,e). In addition,  $I \rightarrow I$  connections also carried attention cue-specific information in RNNs  
260 performing the two-modality DMS task (Fig. 4f,g).

261 These findings suggest that inhibitory-to-inhibitory connections are essential for integrating  
262 context-defining top-down information.

263 **Two-module RNN model with hierarchical organization.** Recent empirical studies have  
264 shown that inhibitory-to-inhibitory connections within early sensory areas receive strong task-  
265 specific and context-based modulation by higher cortical areas [37, 54, 64].

266 Based on our results thus far, which underscore the significance of  $I \rightarrow I$  connections in contex-  
267 tual coding, we next investigated whether inhibitory-to-inhibitory connections in low-level sensory  
268 areas would emerge as a critical target for task-oriented top-down modulation in our model. To  
269 accomplish this, we developed a two-module RNN model inspired by the cortical hierarchy. In this  
270 model, the first module (sensory module) is modeled after the early sensory cortex and receives  
271 the stimulus input signal only (Fig. 5a). The first module subsequently conveys the processed  
272 sensory signal to the second, non-sensory module through exclusively feedforward excitatory con-  
273 nections. Given previous findings from animal studies that showed lack of long-range feedforward  
274 inhibitory connections ([31]), we trained our two-module RNNs to perform the one-modality DMS  
275 task without intermodule feedforward inhibitory projections. The second module of the model, de-  
276 signed after higher cortical areas, receives the task cue signal (Fig. 5a). Using this architecture, we  
277 trained 20 two-module RNNs to perform the one-modality DMS task. On average, the two-module  
278 RNNs took longer to learn the one-modality task compared to the one-module networks (mean  $\pm$

279 stdev,  $38,571 \pm 6,306$  trials for the one-module RNNs vs.  $55,221 \pm 10,187$  trials for the two-module  
280 RNNs; Extended Data Fig. 2).

281 To investigate if the two-module RNNs processed the task cue signal in a manner similar to that  
282 observed in the one-module RNNs, we characterized the kinetic energy landscape and performed the  
283 fixed-point analysis on the two-module networks during the first instruction period (150-400 ms; see  
284 *Methods*). Similar to the landscape and energy minima seen in the one-module RNNs (Fig. 2a), we  
285 observed an inverted U-shaped energy landscape and displacement of energy minima as a function  
286 of the task cue identity (Fig. 5b). In addition, the fixed point analysis revealed a line attractor  
287 structure which was also displaced based on the task cue signal presented to the network (Fig. 5c).  
288 These results suggest that network trajectories are conditioned by a systematic shift in fixed point  
289 structure, which is brought about by the presence of distinct top-down signals in the form of task  
290 instructions.

291 Characterizing the synaptic decay dynamics of the two-module RNNs revealed slower excitatory  
292 dynamics in the non-sensory module compared to the sensory module (Fig. 5d;  $p < 0.001$  by  
293 two-sided Wilcoxon rank-sum test). The inhibitory units exhibited the opposite trend (Fig. 5e;  
294  $p < 0.001$ , two-sided Wilcoxon rank-sum test). Investigating the average synaptic connection  
295 strength revealed strong excitatory connections within the sensory module and from non-sensory  
296 to sensory modules (Fig. 5f;  $p < 0.001$ , Kruskal-Wallis test followed by Dunn's multiple comparison  
297 test). Interestingly, the average inhibitory signaling was the strongest within the non-sensory  
298 module (Fig. 5g;  $p < 0.001$ , Kruskal-Wallis test followed by Dunn's multiple comparison test).  
299 Both  $I \rightarrow E$  and  $I \rightarrow I$  connections within the non-sensory module were significantly stronger than  
300 their counterparts in the sensory module (Extended Data Fig. 3). These findings are consistent  
301 with previous empirical evidence suggesting increased inhibitory strength and diversity along the  
302 cortical hierarchy [53, 65].

303 Linear SVM decoding analyses in the two-module RNNs showed that the task signals were more  
304 readily decodable from the inhibitory units than from the excitatory units in both sensory and non-  
305 sensory modules (Fig. 5h,i; see Extended Data Fig. 4 for the non-sensory module results,  $p < 0.05$ ,  
306 two-sided KS test with Bonferroni corrected across time). Most notably, the SVM decodability of  
307 the task signal decayed slower for the inhibitory units compared to the excitatory units in both

308 modules.

309 **Inhibitory-to-inhibitory connections in both sensory and non-sensory modules encode**

310 **top-down information.** Analyzing the neural trajectories of an example two-module RNN during

311 the first stimulus period for early instruction trials revealed trajectory grouping based on the task

312 cue identity (Fig. 6a). Lesioning  $I \rightarrow I$  connections in both sensory and non-sensory modules by

313 reducing the weights by 50% abolished this top-down modulation (Fig. 6b), mirroring the results

314 observed in the one-module RNN (Fig. 4b). Lesioning other synaptic connections (i.e.,  $E \rightarrow E$ ,

315  $E \rightarrow I$ ,  $I \rightarrow E$ ) did not lead to disruption of the top-down information encoding. Thus, these results

316 suggest that the hierarchical, two-module RNNs also rely on inhibitory-to-inhibitory connections

317 to encode contextual information.

318 Performing a systematic lesioning analysis, similar to the one utilized for the one-module RNNs

319 in Figure 4, demonstrated the importance of inhibitory units with opposite tuning to the task cue

320 (i.e., anti- vs. pro-DMS) in the sensory module for reliably encoding the task signal (Fig. 6c). In

321 addition, disrupting  $I \rightarrow I$  connections within the non-sensory module severely impaired the task

322 performance of all the RNNs, confirming that top-down information is primarily encoded by  $I \rightarrow I$

323 connections in the non-sensory module (Fig. 6d). Lesioning feedback inhibitory connections had

324 minimal influence on the task performance (Fig. 6e,f).

325 These results suggest that the task cue information is encoded by  $I \rightarrow I$  synapses in the non-

326 sensory module. What is even more unexpected is that the top-down information is transmitted to

327 the sensory module via feedback connections and encoded by  $I \rightarrow I$  connections within the sensory

328 module (Fig. 6a). Although some connections did not reach statistical significance, based on the

329 observed trend, it is likely that  $I \rightarrow E$  connections play a significant role in transmitting top-down

330 information from the non-sensory module to the sensory module (Fig. 6f).

331 **Disinhibitory circuits in mouse primary visual cortex and RNN sensory module en-**

332 **code top-down information.** Building on the findings from the previous section, which indicate

333 the role of sensory areas in encoding both stimulus-driven (bottom-up) and task-related (top-down)

334 information, we proceeded to test our hypothesis. Specifically, we proposed that cortical  $I \rightarrow I$  con-

335 nections within early sensory processing regions represent top-down information via feedback from

336 higher cortical areas. To investigate this, we analyzed a publicly available experimental data which

337 demonstrated the capability of the mouse primary visual cortex (V1) in representing contextual in-  
338 formation [54]. This electrophysiology dataset was collected with a linear array recording electrode  
339 covering all layers of V1 and preprocessed with standard filtering and spike sorting pipelines.

340 In this study, during V1 activity recording, mice were trained to identify the location of a salient  
341 grating visual pattern (“figure”) that stood out from the visual background (“ground”) [54]. These  
342 patterns were distinguished based on either orientation, phase, or texture (Fig. 7a). Crucially,  
343 in each of these conditions, the sensory inputs chosen to fall within the exact receptive fields of  
344 the recorded neurons remained strictly identical in both the figure and background conditions  
345 (see *Methods*). This implies that any observed difference in figure versus ground coding within  
346 V1 neurons representing these receptive fields would stem from coding dependent on top-down  
347 feedback. This mirrors our approach in configuring our RNNs to process identical bottom-up  
348 sensory information under varying contexts informed by top-down cues. Therefore, any disparity  
349 in neural activity observed across conditions in the mouse dataset would be attributed to the  
350 context indicated by stimulus regions outside of the measured neural receptive field.

351 First, we tested whether the activity of V1 neurons could differentiate between figure and ground  
352 conditions, even when the sensory information within their receptive fields remained identical. A  
353 successful figure vs. ground decodability would be an evidence for feedback from regions outside  
354 receptive fields into the measured V1 sites. Performing a linear SVM decoding analysis on the  
355 V1 activity to decode the condition label (figure vs. ground) revealed that the V1 responses were  
356 modulated by the task context (Fig. 7b;  $p < 0.05$ , permutation test, Bonferroni corrected). The  
357 high decoding accuracy indicates that feedback signals from regions outside the receptive fields  
358 robustly modulate V1 activity in response to information about task context.

359 In sensory cortical areas, including V1, vasoactive intestinal peptide-expressing (VIP) interneu-  
360 rons send inhibitory projections to somatostatin-positive (SST) interneurons. This forms micro-  
361 circuitry characterized by inhibitory-to-inhibitory connections, similar to the  $I \rightarrow I$  connections  
362 observed in the sensory module of our two-module RNN model (Fig. 5a). Leveraging the experi-  
363 ments within the dataset where VIP interneurons of mouse V1 were optogenetically silenced, we  
364 analyzed the role of VIP neurons in figure-background discrimination. Through the SVM decoding  
365 analysis, we observed a decrease in decoding accuracy following optogenetic silencing of V1 VIP neu-

366 rons ( $p < 0.05$ , one-sided Kolmogorov-Smirnov test, Bonferroni corrected; Fig. 7c). These results  
367 demonstrate the importance of intact inhibitory-inhibitory projections for successfully encoding  
368 top-down information in V1 circuits.

369 We next utilized CEBRA [63] to analyze the neural dynamics of the sensory module in an  
370 example two-module RNN model during the first stimulus presentation in early instruction trials  
371 of the one-modality DMS task. The recovered latent space revealed distinct neural trajectories  
372 delineated by the task cue signal (Fig. 7d). The trajectories were initially divided into two arms  
373 based on the identity of the task cue (light green and light purple vs. dark green and dark purple  
374 trajectories in Fig. 7d). Within each arm, the trajectories were further separable by the first  
375 stimulus identity (+1 or -1). Removing all the inhibitory-to-inhibitory connections within the  
376 sensory module abolished the effects of the task signal in the sensory module (Fig. 7e). These results  
377 highlight a convergence between theoretical models and experimental evidence for the importance  
378 of feedback into lower sensory areas in coding top-down information.

379 Performing the cross-temporal discriminability analysis on the sensory module across all 20  
380 trained two-module RNNs demonstrated that the task cue identity could be reliably decoded,  
381 providing additional confirmation of the top-down modulation imposed by the non-sensory module  
382 (Fig. 7f; see *Methods*). When the sensory  $I \rightarrow I$  connections were removed, the task cue identity  
383 could not be decoded as reliably as in the intact model (Fig. 7f), indicating the crucial role of these  
384 connections in facilitating top-down modulation within the network architecture.

385 **Introducing retro-cue condition elicits shift in strategy.** Identifying relevant sensory stimuli  
386 and determining the timing of their relevance is often dynamic in the real world. To better capture  
387 this, we modified the two-modality DMS task by introducing a retro-cue condition as illustrated  
388 in Figure 8a. The task still involves two streams of stimuli (modality 1 and modality 2) along  
389 with the task cue (pro- and anti-DMS). In this task version, the task cue was fixed to be given  
390 before the first stimulus; see *Methods*). Notably, in this modified version, the attention cue may be  
391 presented before the first stimulus (*early instruction*), after the first stimulus (*late instruction*), or  
392 after the second stimulus (*retro-cue*), as depicted in Figure 8a. This modification provides a more  
393 nuanced exploration of attentional processes by allowing flexibility in the timing of attention cue  
394 presentation.

395 We trained 20 one-module RNNs to perform this modified two-modality DMS task. We then  
396 compared the resulting network dynamics for the case where top-down cues (both task and attention  
397 cue signals) were given before the first stimulus against the dynamics observed from the RNNs  
398 trained for the original two-modality DMS task (Fig. 2). Applying CEBRA to an example RNN  
399 trained for the modified two-modality DMS task revealed that the trajectories for the attended  
400 modality closely resembled those obtained from the example RNN trained for the original two-  
401 modality DMS (i.e., compare Fig. 8b with Fig. 2f). The trajectories were initially distinguished by  
402 the task cue (pro- vs. anti-DMS). Subsequently, each task “arm” bifurcated based on the identity of  
403 the attended first stimulus (Fig. 8b). Interestingly, in the case of pro-DMS, where the unattended  
404 first stimulus had an identity of +1, the trajectories diverged based on the identity of the attended  
405 first stimulus (illustrated by the green trajectories in Fig. 8c). This stands in stark contrast to the  
406 trajectories observed in the RNN model performing the original two-modality DMS task, where  
407 the trajectories of the unattended modality were unaffected by the attended modality (Fig. 2g).  
408 In other words, the introduction of the retro-cue condition to the two-modality task forced the  
409 RNNs to maintain not only the attended but also the unattended stimuli throughout the trial  
410 period. This is further underscored by the robust temporal discriminability of the first stimulus of  
411 the unattended modality across the three attention cue conditions (i.e., early, late, and retro cue  
412 conditions) in the 20 RNNs trained for the modified two-modality DMS task (Fig. 8d–f; compare  
413 these to Fig. 2l,m).

414 Overall, introducing the retro-cue condition resulted in the RNN model employing a different  
415 strategy to flexibly prioritize and maintain relevant information throughout the task execution.

## 416 Discussion

417 The present study provides a unique set of cognitive tasks that require flexible stimulus-response  
418 mapping and enable investigation into the interaction between bottom-up and top-down signaling.  
419 By constructing and training biologically constrained recurrent neural networks (RNNs) on these  
420 tasks, we elucidate and propose possible neural mechanisms essential for such flexible information  
421 processing and cognitive control. Importantly, we show that selective inhibition plays a central  
422 role in shaping network dynamics during context-dependent decision-making. Moreover, through  
423 the utilization of hierarchically structured RNN models (i.e., two-module RNNs) and data from  
424 the mouse primary visual cortex, we demonstrate the involvement of selective inhibition in encod-  
425 ing top-down information within early sensory areas. Together, these findings offer a complete  
426 computational and empirical account for the role of top-down feedback into lower level sensory  
427 areas.

428 Previous experimental and computational studies have highlighted the significance of disin-  
429 hibitory circuits governed by inhibitory-to-inhibitory signaling in performing high-level cognitive  
430 functions [33, 40, 66–68]. For instance, disinhibitory effects exerted by vasoactive intestinal pep-  
431 tide-expressing (VIP) and somatostatin-positive interneurons (SST) in higher-level cortical areas,  
432 such as the prefrontal cortex, have been shown to be critical for working memory and social memory  
433 [52, 69]. While recent animal studies have started to explore how these mechanisms are utilized for  
434 other cognitive functions [70–72], the role of inhibitory-to-inhibitory connections in facilitating flex-  
435 ible cognitive switching remains poorly understood. This ambiguity is primarily attributed to the  
436 lack of computational models incorporating relevant biological constraints, coupled with scarcity of  
437 cognitive tasks that allow for orthogonal manipulation of sensory and temporally varying top-down  
438 signals. To bridge this gap, we trained RNNs composed of model neurons to perform cognitive tasks  
439 requiring adaptive switching. Through several computational analyses, including lesion studies, we  
440 demonstrate that a subset of  $I \rightarrow I$  synapses naturally emerge in our model to adeptly map sensory  
441 information into context-dependent decisions. Consistent with our findings, recent animal studies  
442 have identified disinhibitory circuit motifs facilitating flexible routing of sensory information [33,  
443 37, 38, 54, 72].

444 Particularly noteworthy are our findings that  $I \rightarrow I$  connections within the sensory module of

445 our two-module RNN model encode top-down information, and that these connections are necessary  
446 for context-dependent mapping of the sensory information. Furthermore, we reported that feedback  
447 signals from higher-level cortical areas contribute to emergence of these  $I \rightarrow I$  connections in early  
448 sensory areas. These findings indicate a hierarchical organization of inhibitory circuits involved in  
449 encoding and processing top-down information. In support of this, Kirchberger et al. demonstrated  
450 the critical role of feedback inputs from higher visual areas in generating context-dependent signals  
451 in the mouse primary visual cortex through optogenetic manipulation [54]. While the authors  
452 observed reduced context-encoding upon optogenetic silencing of excitatory neurons in the higher  
453 visual cortex [54], the specific circuitry underlying these feedback projections warrants further  
454 investigation.

455 The possibility that aspects of complex computations, typically ascribed to higher cortical areas,  
456 may also occur in lower-level areas challenges the prevailing notion of the cognitive limitations of  
457 lower-level areas. Building in representational redundancies throughout cortical hierarchies allows  
458 for complex computations to occur in both lower sensory areas and higher-level areas [25, 41,  
459 42]. This mechanism enhances the robustness of representations and facilitates efficient processing,  
460 enabled by top-down feedback signals guiding multiplexing in sensory areas.

461 Building on the insights gained from this study, future directions could explore whether similar  
462 circuit mechanisms are employed across various cognitive domains, potentially uncovering universal  
463 circuit motifs underlying flexible sensory processing and cognitive control across various contexts.  
464 Furthermore, enhancing the biological realism of computational models and RNNs by incorpo-  
465 rating spiking model neurons and biologically plausible learning rules could unveil other neural  
466 mechanisms based on precise timing-based computations. Finally, validating our experimentally  
467 testable hypotheses and predictions using neural data from both non-human primates and humans,  
468 particularly epilepsy patients with depth electrodes implanted for seizure monitoring and potential  
469 intervention, represents a crucial future direction. This step would provide an improved under-  
470 standing of representational redundancies within cortical networks and help identify compensatory  
471 mechanisms that preserve flexible computation in networks disrupted by disorders. Additionally,  
472 these insights will inform the development of targeted interventions and therapeutic strategies for  
473 neurological disorders that impair sensory processing and cognitive control.

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## 671 Author contributions

672 R.K. and N.R. conceived and designed the research; T.G.A., R.K., and N.R. analyzed data; T.G.A.,  
673 R.K., and N.R. wrote the manuscript.

## 674 Declaration of interests

675 The authors declare no competing interests.

## 676 Methods

677 **Continuous-rate recurrent neural network (RNN) model.** In this study, we constructed the  
678 following continuous-variable recurrent neural network (RNN) model:

$$\tau \frac{dx}{dt} = -x(t) + wr(t) + w_{in}u(t) \quad (1)$$

$$r(t) = \sigma(x(t)) = \frac{1}{1 + \exp(-x(t))} \quad (2)$$

$$o(t) = w_{out}r(t) + b \quad (3)$$

679 where  $\tau \in \mathbb{R}^{1 \times N}$  refers to the synaptic time constants,  $x \in \mathbb{R}^{N \times T}$  denotes the synaptic current  
680 variable from from  $N$  units across  $T$  time points. By applying a sigmoid nonlinearity, we estimated  
681 the firing rates  $r \in \mathbb{R}^{N \times T}$  based on the synaptic current values ( $x$ ). The connection weights from  
682 the time-varying inputs ( $u \in \mathbb{R}^{N_{in} \times T}$ ;  $N_{in}$ , the number of input channels) to the network were  
683 represented by the weight matrix  $w_{in} \in \mathbb{R}^{N \times N_{in}}$ . Additionally,  $w \in \mathbb{R}^{N \times N}$  contains connection  
684 weights between the  $N$  units.

685 To compute the network output ( $o \in \mathbb{R}^{1 \times T}$ ), we linearly combined all the firing rates specified  
686 by the output connection weight matrix,  $w_{out} \in \mathbb{R}^{1 \times N}$ , along with the constant bias term,  $b$ . The  
687 network size ( $N$ ) was set to 1000 for all the networks.

688 For the one-modality DMS task, the input signals ( $u$ ) contained three channels: two channels  
689 for the two sequential stimuli and one channel for the task cue signal (Fig. 1a). For the two-modality  
690 DMS task,  $u$  contained 6 channels, corresponding to two stimulus modalities (two channels for each  
691 modality), one channel for the task cue signal, and another one for the attention cue (Fig. 1b).  
692 For the one-module RNNs,  $u$  was projected to all the units in the network. However, for the  
693 two-module RNNs, the stimulus signals were injected into the first 200 units, while the task and  
694 attention cues were provided to the second module comprising 800 units (Fig. 5a).

695 For the two-module RNN model, the recurrent connectivity weight matrix ( $w$ ) was constrained  
696 to remove the feedforward inhibitory connections from the first module (first 200 units; sensory  
697 module) to the second module (non-sensory module) by applying a binary mask.

698 **Training and task details.** The dynamics in Eq. (1) were discretized using the first-order Euler  
699 approximation method and using the step size ( $\Delta t$ ) of 5 ms:

$$\mathbf{x}_t = \left(1 - \frac{\Delta t}{\tau}\right) \mathbf{x}_{t-1} + \frac{\Delta t}{\tau} (\mathbf{w} \mathbf{r}_{t-1} + \mathbf{w}_{in} \mathbf{u}_{t-1}) \quad (4)$$

700 where  $\mathbf{x}_t = \mathbf{x}(t)$ . Given that the units in this network model communicate through differentiable  
701 and continuous signals, a gradient-descent supervised method, known as backpropagation through  
702 time (BPTT; [73]), was employed to train our RNNs to perform cognitive tasks. Specifically, the  
703 trainable parameters of the model included  $\mathbf{w}$ ,  $\tau$ ,  $\mathbf{w}_{out}$ , and  $b$ . We used Adam (adaptive moment  
704 estimation) optimization algorithm to update these parameters. The learning rate was set to 0.01,  
705 and the TensorFlow default values were used for the rest of the parameters including the first  
706 and second moment decay rates. To further impose biological constraints, we enforced Dale's  
707 law (uniform neurotransmitter release characteristics within separate excitatory and inhibitory  
708 neurons) using methods similar to those implemented in previous studies ([43, 49, 74]). To adhere  
709 to empirical findings regarding the ratio of excitatory and inhibitory neurons observed in the brain,  
710 each RNN consists of 80% excitatory and 20% inhibitory units (i.e., E-I ratio of 80/20; [30, 75,  
711 76]).

712 Importantly, instead of fixing the synaptic decay constant ( $\tau$ ) to a fixed value for all the units,  
713 we optimized the parameter for each unit. The parameter was trained to range from 20 ms to  
714 125 ms to model heterogeneous synaptic dynamics of different receptors in the cortex [77, 78]. We  
715 initialized the synaptic decay time constant parameter ( $\tau$ ) using

$$\tau = \sigma(\mathcal{N}(0, 1)) \tau_{step} + \tau_{min} \quad (5)$$

716 where  $\sigma(\cdot)$  is the sigmoid function and  $\mathcal{N}(0, 1)$  refers to the standard normal Gaussian distribution.  
717  $\tau_{min} = 20$  ms and  $\tau_{step} = 105$  ms were used to constrain the parameter to range from 20 ms to  
718 125 ms.

719 Our model training was deemed successful if the following two criteria were satisfied within the  
720 first 70,000 epochs: 1) loss value (defined as the root mean squared error between the network  
721 output and target signals)  $< 7$ ; and 2) task performance  $> 95\%$  for the one-modality DMS task

722 and > 85% for the two-modality DMS task. If the network did not meet the criteria within the first  
723 70,000 epochs, the training was terminated. For each successfully trained RNN, we simulated 400  
724 trials for the one-modality task and 1,000 trials for the two-modality task, randomizing each trial  
725 to contain one possible combination of instruction order, top-down cues, and stimulus identities.  
726 Using these criteria, we trained 20 RNNs for each task.

727 *One-modality DMS task.* For the one-modality DMS task, the trial duration was set to 350 steps  
728 with 5 ms step size, and the input matrix ( $\mathbf{u} \in \mathbb{R}^{3 \times 350}$ ) contained two input channels for the two  
729 sequential stimuli (Stim 1 and Stim 2 in Fig. 1a). The third channel was used to deliver the task cue  
730 signal. The first channel was employed to present Stim 1 (lasting 250 ms) at 400 ms, and the second  
731 channel delivered Stim 2 (lasting 250 ms) 250 ms after the offset of the first stimulus. During the  
732 stimulus period, the input channel was set to either -1 or +1. For the early instruction condition,  
733 the task cue channel was set to either -1 or +1 from 150 ms to 400 ms. For the late instruction  
734 condition, the task cue channel was adjusted to -1 or +1 during the delay period, spanning from  
735 650 ms to 900 ms.

736 *Two-modality DMS task.* The input matrix for the two-modality task contained 6 input channels  
737 ( $\mathbf{u} \in \mathbb{R}^{6 \times 350}$ ). The initial two channels were employed to present two sequential stimuli for the  
738 first modality, whereas the subsequent two channels delivered stimuli for the second modality. The  
739 fifth channel was dedicated for the task cue signal, while the last channel was used to present the  
740 attention cue. For the early instruction condition, both task and attention signals were delivered at  
741 150 ms. For the late instruction condition, the task and attention signals were presented at 650 ms.

742 *Modified two-modality DMS task.* For the modified version of the two-modality DMS task (Fig. 8),  
743 the input matrix closely resembled that of the standard two-modality task (see above). The trial  
744 duration for this variant was reduced to 250 steps (1,250 ms), and the stimulus window was also  
745 shortened to 125 ms. In this task, the task cue signal was always delivered before the first stimulus  
746 at 125 ms. However, the attention cue signal was randomly delivered either before the first stimulus  
747 (*early instruction*), after the first stimulus at 375 ms (*late instruction*), or after the second stimulus  
748 at 625 ms (*retro-cue*).

749 **SVM decoding and state space analyses.** We performed decoding on RNN activity with a  
750 5-fold cross-validated linear support vector machine analysis (SVM; *sklearn* function SVC). Given  
751 a trained RNN model, we first generated firing rate timecourses ( $\mathbf{r}$  in Eq. (3)) of 1,000 units across  
752 1,000 simulated trials. Next, the data were randomly sampled for instruction order (early vs.  
753 late), stimulus identity (+1 vs. -1), and top-down task signals (pro-DMS vs. anti-DMS; as well  
754 as attended vs. unattended for the RNNs performing two-modality DMS). The SVM classifier was  
755 trained on the firing activities from either excitatory or inhibitory units and then tested on the  
756 left-out trials to distinguish each of the signals of interest.

757 To characterize the network dynamics in response to distinct external inputs, we performed a  
758 fixed-point analysis [60] using the FixedPointFinder toolbox [61]. This method involves numerically  
759 minimizing a proxy energy function derived from the RNN update equations to identify fixed points  
760 and subsequently obtaining linearized dynamics around these points to describe their behavior. In  
761 our case, this is equivalent to minimizing  $q(x)$ , defined from the RNN dynamics of Eq. (1):

$$q(x) = \frac{1}{2} \left| \frac{dx}{dt} \right|^2 = \frac{1}{\tau} (-\mathbf{x}(t) + \mathbf{w}\mathbf{r}(t) + \mathbf{w}_{in}\mathbf{u}(t)) \quad (6)$$

762 We repeated this search for every set of external inputs  $u(t)$ , which included null inputs for  
763 late instruction trials, task cue (pro-DMS vs. anti-DMS), and attention cues (for the two-modality  
764 DMS).

765 For each optimization run, we randomly selected 200 out of the 1000 simulated trials to create  
766 initial conditions for the optimizer. From each trial, one initial condition was generated by taking  
767 the 1000-dimensional system state at the end of the first instruction period. Each optimization  
768 run had the following parameters: number of iterations = 30000; initial learning rate = 0.1; outlier  
769 distance scale = 10; unique tolerance = 10. The outlier distance scale servesd as a cutoff distance  
770 for discarding outlier putative fixed points, measured from the centroid of the vector of initial  
771 conditions. The unique tolerance is the numerical precision used to determine if two fixed points  
772 are unique. Fixed points that were too close to previously identified ones were discarded. Two  
773 fixed points were considered unique if their distance exceeded this threshold.

774 To visualize the fixed points and RNN neural trajectories, we plotted them in principal com-

775 ponent space spanned by the top three principal components extracted from the average activities  
776 during the first instruction period. In addition, we visualized the entire landscape of the energy  
777 function  $q(x)$  in the top two principal components during the first instruction period along with  
778 their respective energy minima for each external input  $u(t)$  condition (Fig. 2a,b; Fig. 5b).

779 **CEBRA analysis.** To visualize network dynamics and analyze the impact of top-down signaling  
780 on RNN dynamics, we applied unsupervised manifold discovery CEBRA [63] on the 1,000 simulated  
781 trials of representative RNN models during the first instruction and first stimulus periods. This  
782 method is capable of uncovering latent structures in multidimensional dynamical datasets, either  
783 unsupervised or conditioned on specific variables of interest. Throughout this study, we conducted  
784 unsupervised latent structure discovery based solely on the temporal sequence of data points across  
785 the entire dataset, without considering trial conditions, tasks, or stimulus identities. More specifi-  
786 cally, we utilized the default model parameters for the ‘offset10-model’ architecture, using a batch  
787 size of 256, time offsets of 10, learning rates of  $3e - 4$ , and cosine as the distance measure.

788 **Cross-temporal discriminability analysis.** In addition to the SVM decoding analysis (see  
789 above), we also quantified the amount of information encoded by each unit within RNNs using  
790 cross-temporal discriminability analysis ([79–81]). For Figure 2j–m, the firing rate estimate time  
791 courses of each unit for each first stimulus identity were initially divided into two splits (odd vs.  
792 even trials) and averaged across trials within each split. Subsequently, for each unit in each split, the  
793 difference in the average firing rates between the two conditions based on the first stimulus identity  
794 (i.e., +1 and -1) was computed. Next, Pearson’s correlation coefficient between the two splits was  
795 calculated. The discriminability score was then obtained by applying Fisher’s  $z$ -transformation.  
796 This process was carried out separately for the attended modality (Fig. 2j,k) and the unattended  
797 modality (Fig. 2l,m). For Figure 7f, the first stimulus identity was fixed to -1, and the discrim-  
798 inability of the task cue signal was computed using the two task cue identities (pro- vs. anti-DMS).  
799 The diagonal values of the discriminability matrices are shown. For Figure 8d–f, similar procedures  
800 to those employed for Figure 2j–m were implemented.

801 **Centrality measure.** We utilized a functional closeness centrality measure to determine the cen-  
802 trality of each unit within RNNs. For this, we first defined a functional distance metric  $d_{i,j}$  between  
803 unit  $i$  and  $j$  a network, based on the absolute of the Pearson correlation ( $\rho$ ) between their synaptic

804 current activity over time, denoted as  $x_i$  and  $x_j$ :

$$d_{i,j} = 1 - |\rho(x_i, x_j)| \quad (7)$$

805 This function ensures that unit pairs that are more predictive of each other's activity, either  
806 via positive or negative correlation, have a distance function closer to 0, while unit pairs with weak  
807 correlations have a distance function closer to 1.

808 Next, we used the complete distance matrix as the edge distances between nodes in a graph and  
809 employed the Python package *networkx* [82] to compute the network closeness centrality measure  
810  $C_i$  for each unit  $i$  from all  $n$  units:

$$C_i = \frac{n - 1}{\sum_{j=1}^{n-1} S(i, j)} \quad (8)$$

811 Here,  $S(i, j)$  represents the shortest path distance between two units  $i$  and  $j$ , computed utilizing  
812 the distance matrix  $d_{i,j}$  via Dijkstra's algorithm with the distance attributes as edge weights.

813 **Identifying task and attention cue selective units.** To identify unit selective for pro-DMS vs.  
814 anti-DMS task signals, we first generated 400 trials for the one-modality DMS and 1,000 trials for  
815 the two-modality DMS. We next extracted firing rate estimates of all units in each of the trained  
816 RNNs. Then, the trials and firing rate estimates were sorted based on the early task cue signal,  
817 separating them into pro-DMS and anti-DMS groups. For each unit, we averaged the firing rate  
818 estimates during the first instruction window for each trial. Subsequently, we performed the one-  
819 sided Wilcoxon rank-sum statistical test on the average firing rates from the two task groups for  
820 each unit. Units with significantly higher average firing rates in the pro-DMS group compared to  
821 the anti-DMS group were classified as pro-DMS selective units. Similar procedures were performed  
822 to identify attention-selective units for the two-modality RNNs.

823 **Lesioning analyses.** For Figure 4 and Figure 6, trained synaptic connections were lesioned sys-  
824 tematically to identify specific connections important for encoding and maintenance of top-down  
825 information. For each trained network, connections were initially classified into four subgroups:  
826  $I \rightarrow I$  (inhibitory units inhibiting other inhibitory units),  $I \rightarrow E$  (inhibitory units inhibiting ex-  
827 citatory units),  $E \rightarrow I$  (excitatory units exciting inhibitory units), and  $E \rightarrow E$  (excitatory units

828 exciting other excitatory units). Within each subgroup, connections were further categorized based  
829 on their selectivity for the task and attention cue signal (see above). The selective connections were  
830 then lesioned by reducing their strength by 50%.

831 **Experimental data.** To further characterize the impact of top-down signaling over information  
832 processing, we utilized publicly available experimental data on the role of recurrent processing in  
833 the activity of mouse primary visual cortex [54]. In this task, mice had to determine the location  
834 of a salient grating visual pattern which contrasted from a visual background, distinguishing them  
835 based either on the orientation, the phase, or the texture of the grating pattern. For the purposes  
836 of our analyses, we averaged results across orientation, phase, and texture conditions. Target  
837 patterns could appear either in the right or left visual field, prompting mice to indicate their  
838 locations by licking a spout on the corresponding side to receive water or milk droplets as rewards.  
839 Crucially, neural recordings and stimuli were set up in such a way that image contents falling within  
840 the receptive fields of the recorded neurons were strictly identical in the figure and background  
841 conditions. Thus, any difference in neural activity measured across conditions was caused by the  
842 context indicated by image regions outside of the measured neural receptive field.

843 We first sought to determine whether V1 activity contained information distinguishing target  
844 grated stimuli from non-target grated backgrounds even when the sensory input within receptive  
845 fields was identical. This would indicate that feedback from regions outside receptive fields into  
846 the measured V1 sites. For this analysis, neural activity consisted of multiunit activity from 198  
847 recording sites in 13 different V1 electrode penetrations in 6 awake mice. To determine which  
848 information was contained in V1 multiunit activity, we performed a 4-fold cross-validated linear  
849 SVM decoding analysis (MATLAB function fitcsvm), for figure versus background labels from 0.5 s  
850 before to 1 s after stimulus presentation, utilizing activity in separate channels as features. To  
851 obtain a null distribution for decoding accuracy, we generated 1,000 random label permutations  
852 and performed the same decoding analysis.

853 Furthermore, we leveraged an additional analysis using the aforementioned dataset. Specifically,  
854 we determined whether activity of inhibitory neurons in V1 is necessary for figure versus background  
855 discrimination, as predicted by the central role of inhibitory neurons in our modeling approach.  
856 The analysis contained multiunit activities of different subgroups of inhibitory interneurons in

857 V1: vasoactive intestinal peptide-expressing (VIP) and somatostatin-positive interneurons (SST).  
858 In addition, the dataset also contains recordings when VIP or SST neurons were optogenetically  
859 inhibited (see [54] for more details).

860 Using this dataset, we decoded figure versus background labels from V1 multiunit activity with  
861 a 4-fold cross-validated linear SVM, both with and without optogenetic VIP suppression. We then  
862 compared decoding accuracy between the laser-on and laser-off conditions by performing a two-  
863 sample one-sided Kolmogorov-Smirnov (KS) test for whether accuracy was larger in trials without  
864 laser suppression. We performed KS tests within the laser delivery time window (250 ms to 500 ms)  
865 and Bonferroni corrected p-values across different time bins.

866 **Statistical analyses.** All RNNs trained in the present study were randomly initialized (with  
867 random seeds) before training. Nonparametric statistical methods were employed throughout the  
868 study. In figures containing boxplots, two-sided Wilcoxon rank-sum or signed-rank tests were  
869 performed to ascertain statistically significant differences between two groups.

870 Following linear SVM decoding and functional centrality analyses, we aimed to determine  
871 whether decoding accuracy or functional centrality values were higher in excitatory or inhibitory  
872 neurons. To achieve this, we utilized the `scipy.stats` function `kstest` and performed two-sided  
873 Kolmogorov-Smirnov (KS) tests across all time bins and Bonferroni corrected for the number of  
874 tested time bins. Similarly, we performed Bonferroni corrected one-sided KS tests across time to  
875 specifically test the hypothesis that decoding accuracies in V1 would decrease following optogenet-  
876 ical silencing.

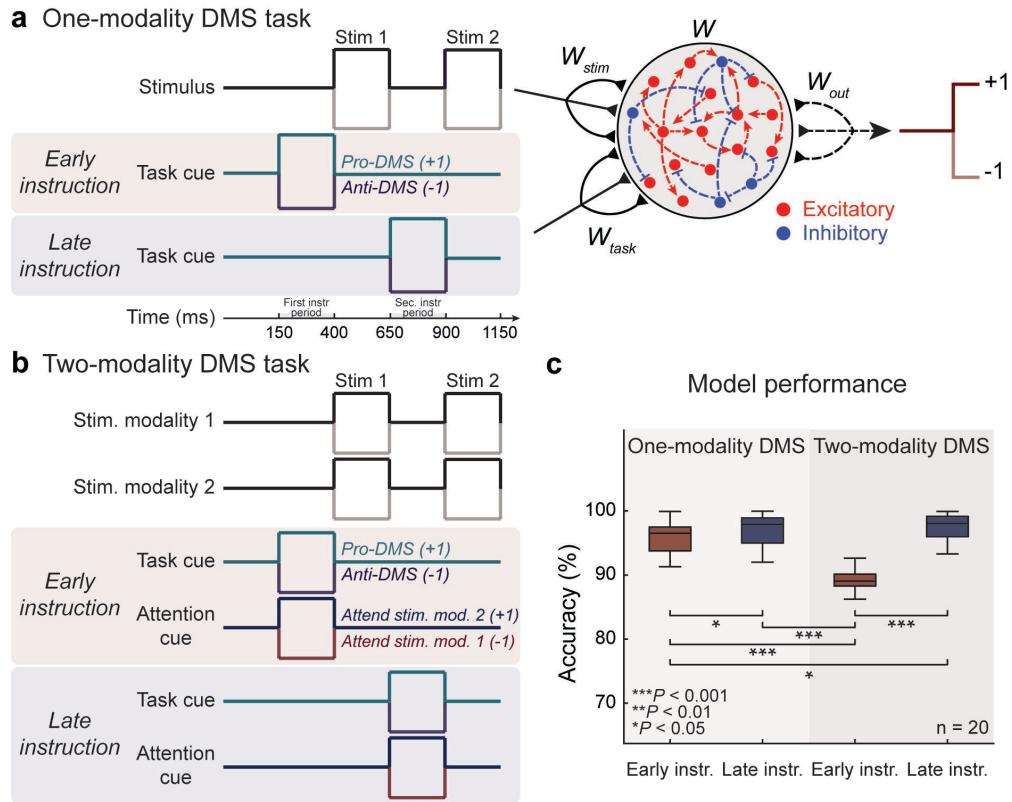
877 For cross-temporal discriminability analyses, we performed binomial tests and Bonferroni cor-  
878 rected for the number of tests to determine whether each decoding accuracy value was higher than  
879 chance. Assuming a false positive rate of 5%, and a Bernoulli process to generate significant decod-  
880 ing events at this rate, the number of instances  $S$  falsely classified as significant within a population  
881 of size  $N$  is given by a binomial distribution:  $S \sim \text{binomial}(N, 0.05)$ . Accordingly, we derived a  
882 binomial p-value for the probability of obtaining an observed sensitive instance count  $K$  larger than  
883 expected by chance, using the cumulative binomial distribution:  $p = 1 - \text{binomialCDF}(K, N, 0.05)$ .

884 **Code availability**

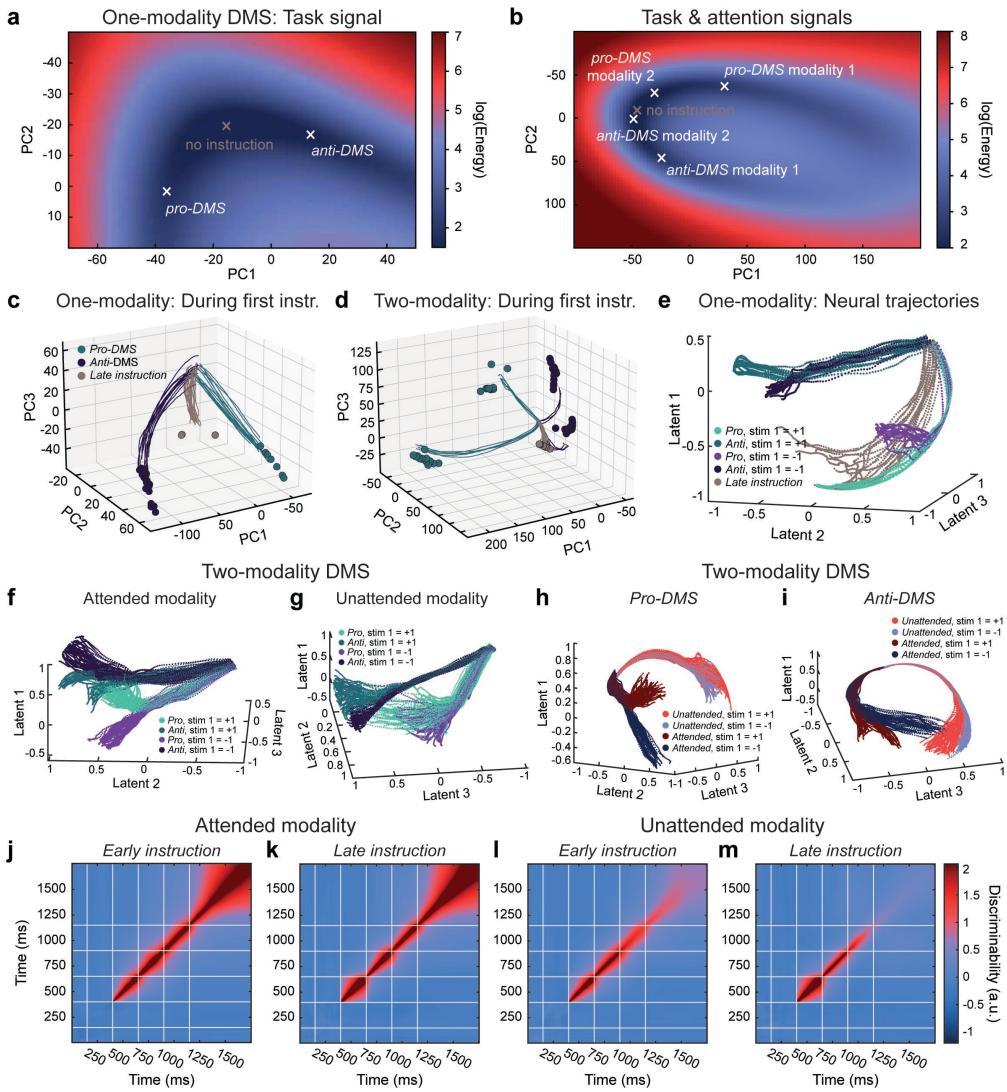
885 The code for the analyses performed in this study will be made available upon acceptance for  
886 publication.

887 **Data availability**

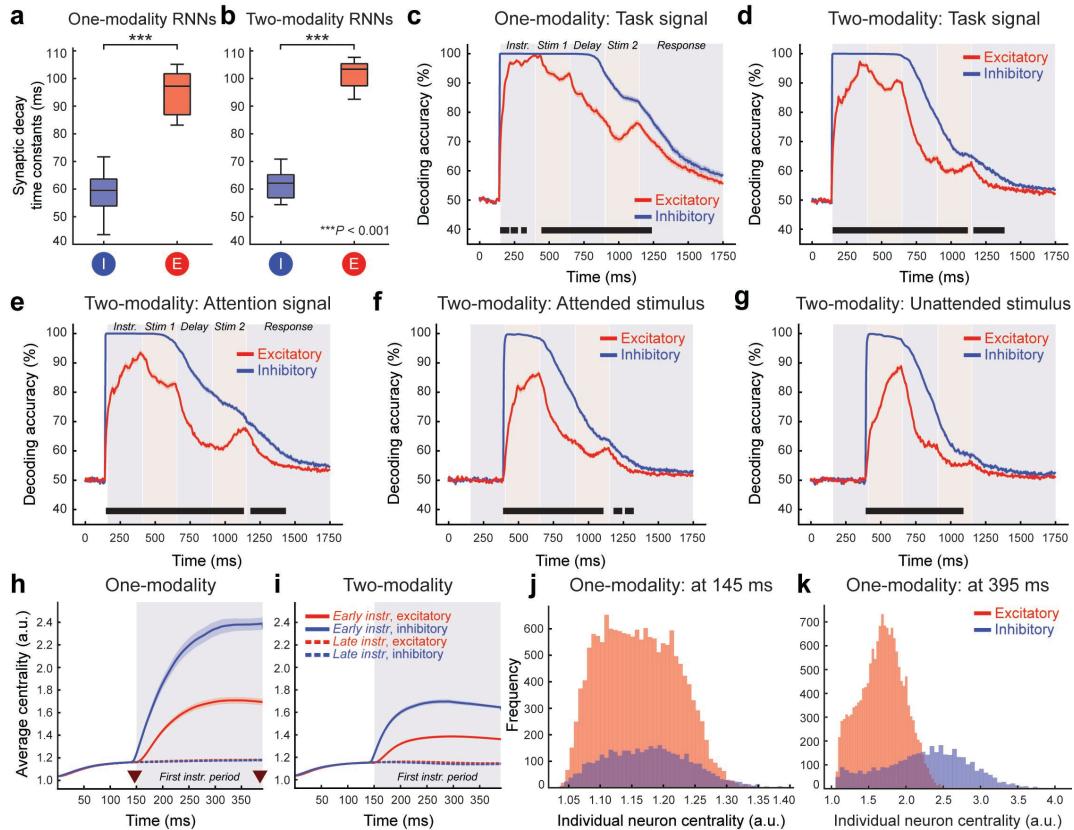
888 The trained RNN models used in the present study will be deposited as MATLAB-formatted data  
889 in Open Science Framework upon acceptance for publication.



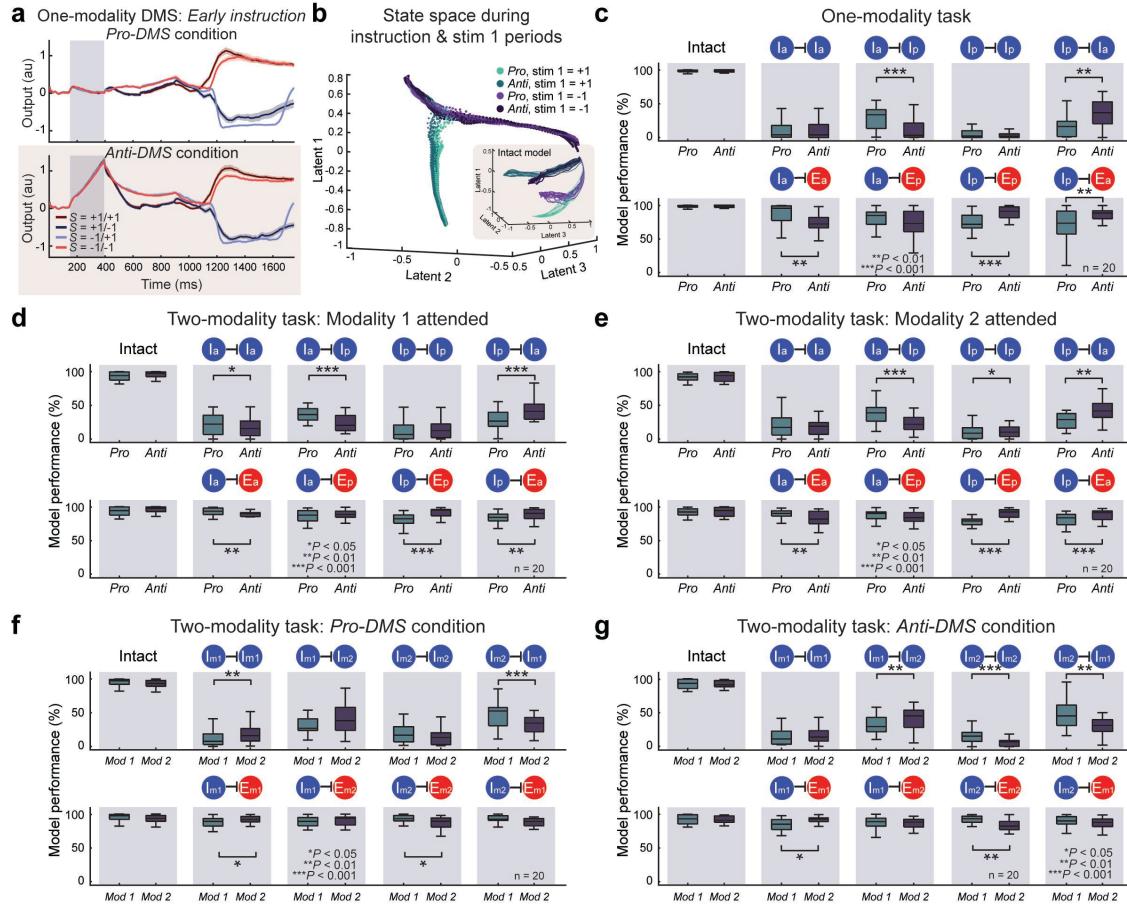
**Fig. 1 | Dynamic decision-making tasks and model schematic.** **a.** Schematic of a one-modality DMS task with sequential stimuli separated by a delay period. A task cue, indicating the stimulus-response mapping, is presented either before (*early instruction*) or after stimulus 1 (*late instruction*). The recurrent neural networks (RNNs) generate an output of +1 or -1 for matched and mismatched trials, respectively (*pro-DMS*; and vice versa for *anti-DMS*). The schematic of the RNN model shown on the right. **b.** Schematic of a two-modality DMS task where each stimulus comprises two modalities. In addition to the task cue, an attention cue is presented on each trial, indicating the modality on which the RNNs need to perform the DMS task. The task and attention cues are presented either before (*early instruction*) or after stimulus 1 (*late instruction*). The trial timing for both one- and two-modality DMS tasks is depicted in **a**. **c.** Testing performance of the trained RNNs on the DMS tasks. The average accuracy of the trained RNNs is presented, with statistical comparisons computed using two-sided Wilcoxon rank-sum tests. Boxplot: central lines, median; bottom and top edges, lower and upper quartiles; whiskers,  $1.5 \times$  interquartile range; outliers are not plotted. \* $p < 0.05$ ; \*\* $p < 0.01$ ; \*\*\* $p < 0.001$



**Fig. 2 | Flexible incorporation of task and attention signals.** **a.** Heat map of kinetic energy in an example RNN performing the one-modality DMS task during the first instruction period (150-400 ms; Fig. 1a). Background heat maps belong to the late instruction condition. The middle cross indicates the local energy minimum during the first instruction period for the late instruction condition (*no instruction*), while the left and right crosses indicate the new local energy minima for the pro- and anti-DMS conditions, respectively. **b.** Same as **a**, for an example RNN performing the two-modality DMS task. Legend: pro-task modality 1, pro-DMS and first modality attended; pro-task modality 2, pro-DMS and second modality attended; anti-task modality 1, anti-DMS and first modality attended; anti-task modality 2, anti-DMS and second modality attended. **c.** Individual trial one-modality RNN trajectories in principal component space during the first instruction period. Principal component projections of fixed points are included. Trial top-down cue conditions are divided into pro-DMS (teal), anti-DMS (dark blue) or no instructions (gray). **d.** Same as **c**, for a two-modality RNN. **e.** Latent space one-modality RNN trajectories during the first instruction and first stimulus periods (150-650 ms; Fig. 1a) for all combinations of top-down cues and stimulus identities. **f.** Same as **e**, for a two-modality RNN, highlighting the attended stimulus modality. **g.** Same as **e**, for a two-modality network, highlighting the unattended stimulus modality. **h.** Latent space two-modality RNN trajectories for pro-DMS trials, splitting trajectories by the identity of attended versus unattended stimuli. **i.** Same as **h**, for anti-DMS trials. **j-k.** Temporal discriminability for the first stimulus identity of the attended modality when the attention signal is given early (**j**) or late (**k**). The task signal was fixed to anti-DMS. **l-m.** Temporal discriminability for the first stimulus identity of the unattended modality when the attention signal is given early (**l**) or late (**m**). The task cue was fixed to anti-DMS.

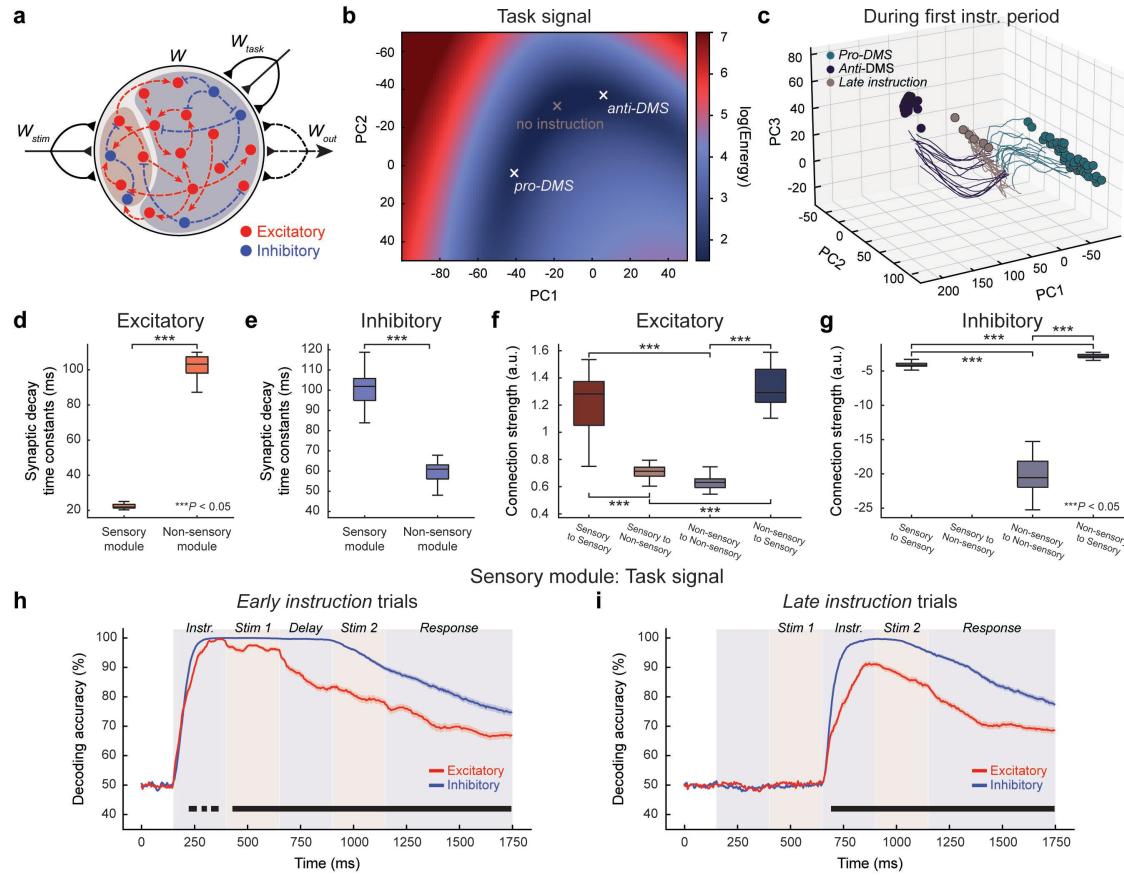


**Fig. 3 | Inhibitory units robustly maintain top-down signals and establish functional connectivity hubs.** **a-b.** Average synaptic decay time constants of inhibitory (blue) and excitatory (red) units in one-modality RNNs (**a**) and two-modality RNNs (**b**). **c.** SVM decodability of the task signal from inhibitory (blue) and excitatory (red) units from the one-modality RNNs. **d.** SVM decodability of the task signal from inhibitory (blue) and excitatory (red) units from the two-modality RNNs. **e.** SVM decodability of the attention signal from inhibitory (blue) and excitatory (red) units from the two-modality RNNs. **f.** SVM decodability of the attended first stimulus identity from inhibitory (blue) and excitatory (red) units from the two-modality RNNs. **g.** SVM decodability of the unattended first stimulus identity from inhibitory (blue) and excitatory (red) units from the two-modality RNNs. Black bars indicate significant differences between excitatory and inhibitory units ( $p < 0.05$ , two-sided KS test). **h.** Average functional connectivity centrality for all inhibitory (blue) and excitatory (red) units, across all one-modality RNNs, in early (solid) or late (dashed) instruction trials. Arrows indicate start and end of the first instruction period. Shaded areas indicate standard error of the mean. **i.** Same as **h**, for two-modality RNNs. **j.** Histogram of functional connectivity values for all units in all one-modality networks at the beginning of the first instruction period. **k.** Same as **j**, at the end of the instruction period. Boxplot: central lines, median; bottom and top edges, lower and upper quartiles; whiskers,  $1.5 \times$  interquartile range; outliers are not plotted. \*\*\* $p < 0.001$  by two-sided Wilcoxon rank-sum test.

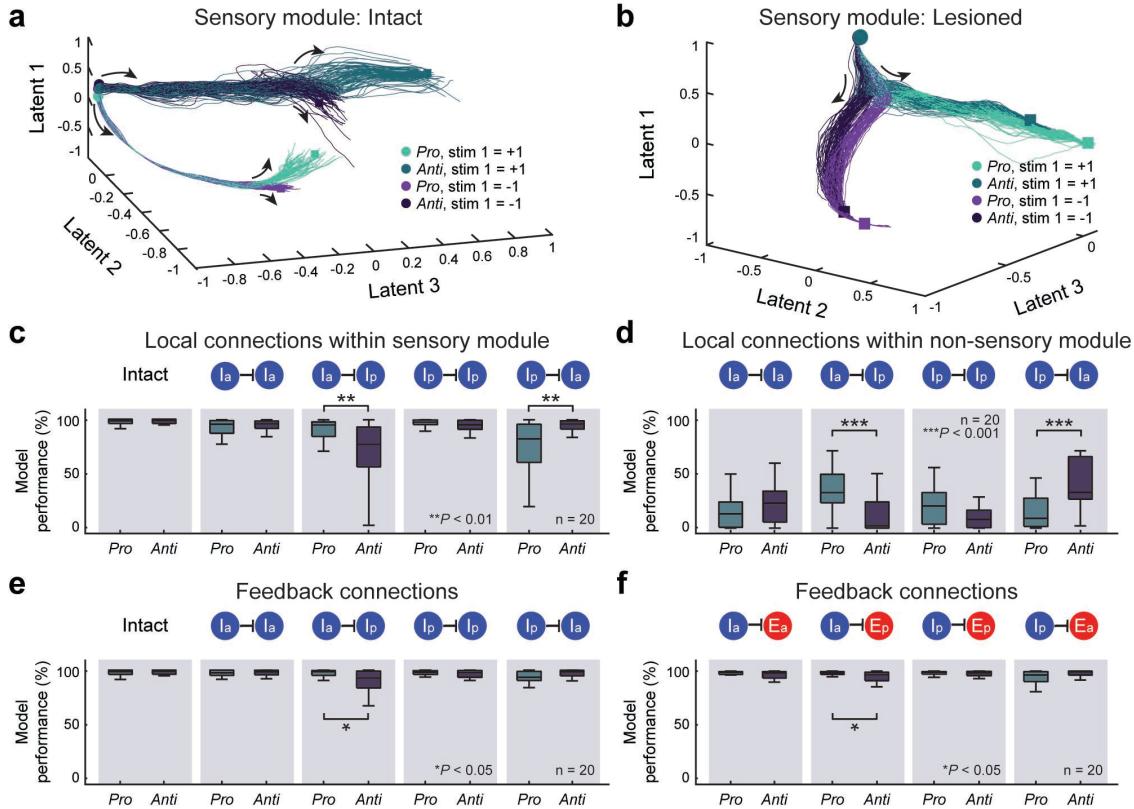


**Fig. 4 | Inhibitory-to-inhibitory connections primarily encode task and attention cue signals.**

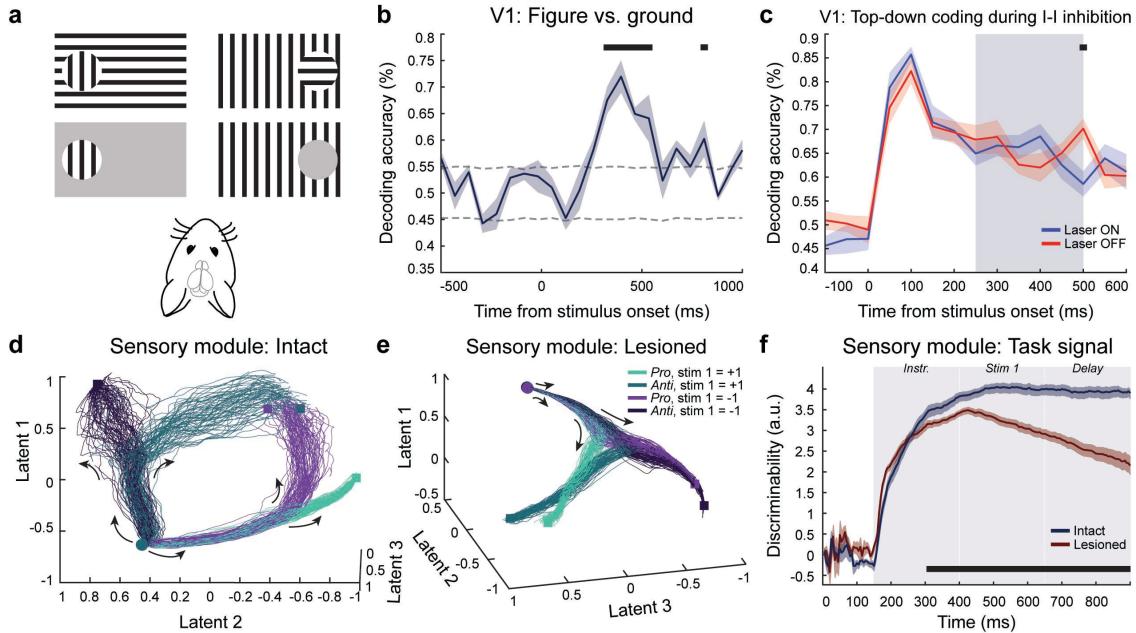
**a.** Reducing incoming inhibitory synaptic weights to inhibitory units selective to the anti-DMS cue by 50% in an example one-modality RNN led to the network performing the pro-DMS even when the anti-DMS cue was given (bottom). **b.** CEBRA neural trajectories of the lesioned model shown in **a** during the first instruction and first stimulus periods. Inset, trajectories from the intact network (identical to Fig. 2e). **c.** Performance of all 20 RNNs trained to perform the one-modality task when task-specific inhibitory-to-inhibitory ( $I \rightarrow I$ ; top) or inhibitory-to-excitatory ( $I \rightarrow E$ ; bottom) synaptic weights were reduced by 50%. **d.** Performance of all 20 RNNs trained to perform the two-modality DMS when task-specific  $I \rightarrow I$  (top) or  $I \rightarrow E$  (bottom) synaptic weights were reduced by 50% when modality 1 was attended. **e.** Same as **d**, when modality 2 was attended. **f.** Performance of all 20 RNNs trained to perform the two-modality DMS when modality-specific  $I \rightarrow I$  (top) or  $I \rightarrow E$  (bottom) synaptic weights were reduced by 50% when the task signal was fixed to pro-DMS. **g.** Same as **f**, when the task was fixed to anti-DMS.  $I_a$ , inhibitory units preferring anti-DMS cue;  $I_p$ , inhibitory units preferring pro-DMS cue;  $E_a$ , excitatory units preferring anti-DMS cue;  $E_p$ , excitatory units preferring pro-DMS cue;  $I_{m1}$ , inhibitory units preferring modality-1 attention cue;  $I_{m2}$ , inhibitory units preferring modality-2 attention cue;  $E_{m1}$ , excitatory units preferring modality-1 attention cue;  $E_{m2}$ , excitatory units preferring modality-2 attention cue. Boxplot: central lines, median; bottom and top edges, lower and upper quartiles; whiskers,  $1.5 \times$  interquartile range; outliers are not plotted. \* $p < 0.05$ , \*\* $p < 0.01$ , \*\*\* $p < 0.001$  by two-sided Wilcoxon rank-sum test.



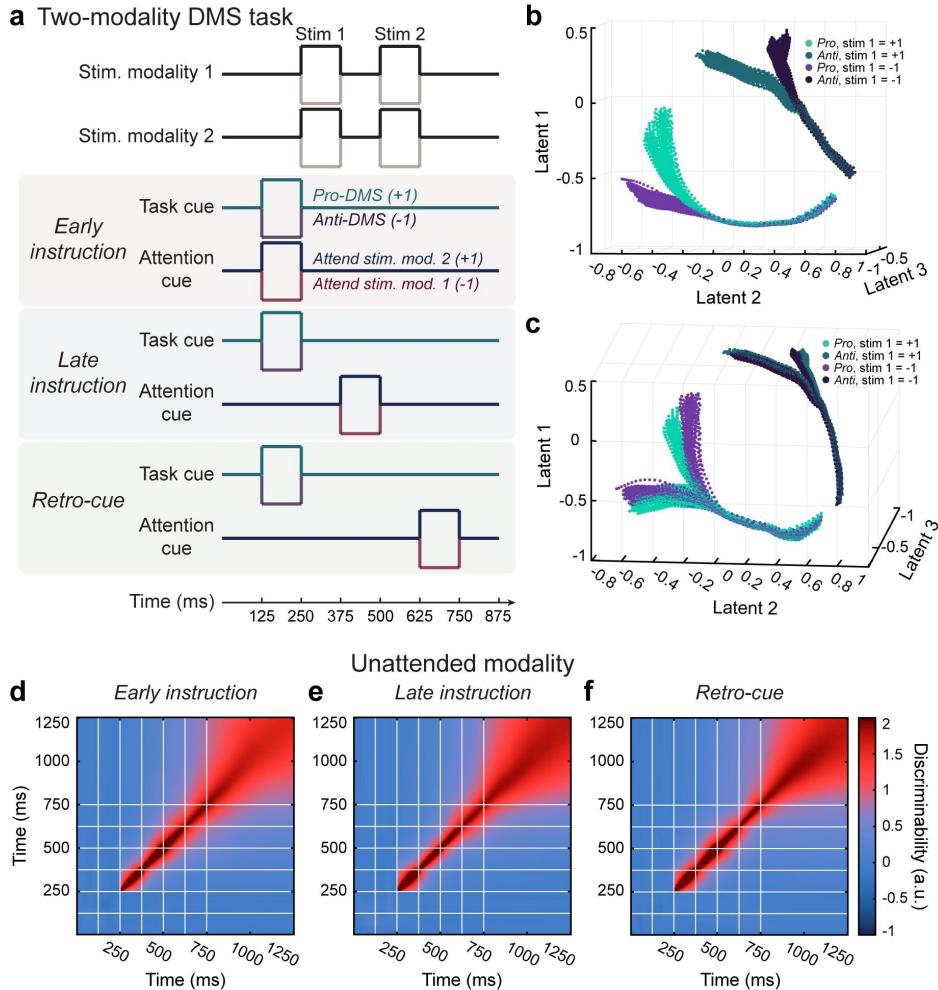
**Fig. 5 | Dynamic coding and emergence of hierarchical inhibitory organization in two-module RNNs.** **a.** Schematic of the two-module RNN model trained to perform the one-modality DMS task. The sensory module (red shade) contains 200 units and the non-sensory module (blue shade) contains 800 units. The sensory module receives the input stimulus signal, while the non-sensory module receives the task cue signal. There are no feedforward inhibitory projections from the sensory module to the non-sensory module. **b.** Heat map of kinetic energy in an example one-modality two-module RNN during the first instruction period. The middle cross indicates the local energy minimum for the late instruction condition (*no instruction*), while the left and right crosses indicate the new local energy minima for the pro- and anti-DMS conditions, respectively. **c.** Individual trial two-modality RNN trajectories in principal component space during the first instruction period. Principal component projections of fixed points are included. Trial task cues are divided into pro-DMS (teal), anti-DMS (dark blue) or no instructions (gray). **d-e.** Average synaptic decay time constants of excitatory units (**d**) and inhibitory units (**e**) in the sensory and non-sensory modules from 20 two-module RNN models trained to perform the one-modality DMS task. **f-g.** Comparison of average excitatory (**f**) and inhibitory (**g**) synaptic connection strengths within and between the sensory and non-sensory modules. **h.** Average decoding accuracy in early instruction trials for pro- vs. anti-DMS signal in the sensory module of two-module networks, including either excitatory (red) or inhibitory (blue) units. Shaded areas indicate standard error of the mean. Black bars indicate significant differences between excitatory and inhibitory units ( $p < 0.05$ , two-sided KS test). **i.** Same, for late instruction trials. Boxplot: central lines, median; bottom and top edges, lower and upper quartiles; whiskers,  $1.5 \times$  interquartile range; outliers are not plotted. \*\*\* $p < 0.001$  by two-sided Wilcoxon rank-sum test (**d** and **e**) or Kruskal-Wallis test followed by Dunn's multiple comparison test (**f** and **g**).



**Fig. 6 |  $I \rightarrow I$  connections in both sensory and non-sensory modules contribute to task cue encoding.** **a.** CEBRA neural trajectories during the first instruction and first stimulus periods from an example two-module RNN. **b.** CEBRA trajectories during the first instruction and first stimulus periods from the same RNN model shown in **a**, but with  $I \rightarrow I$  connections lesioned. **c-d.** Performance of all 20 two-module RNNs trained to perform the one-modality DMS task when task-specific  $I \rightarrow I$  connection strengths within the sensory module (**a**) or within the non-sensory module (**b**) were reduced by 50%. **e-f.** Performance of all 20 two-module RNNs trained to perform the one-modality task when task-specific  $I \rightarrow I$  connection strengths (**c**) or  $I \rightarrow E$  (**d**) from the non-sensory to the sensory module were reduced by 50%. Boxplot: central lines, median; bottom and top edges, lower and upper quartiles; whiskers,  $1.5 \times$  interquartile range; outliers are not plotted. \* $p < 0.05$ , \*\*\* $p < 0.001$  by two-sided Wilcoxon rank-sum test.

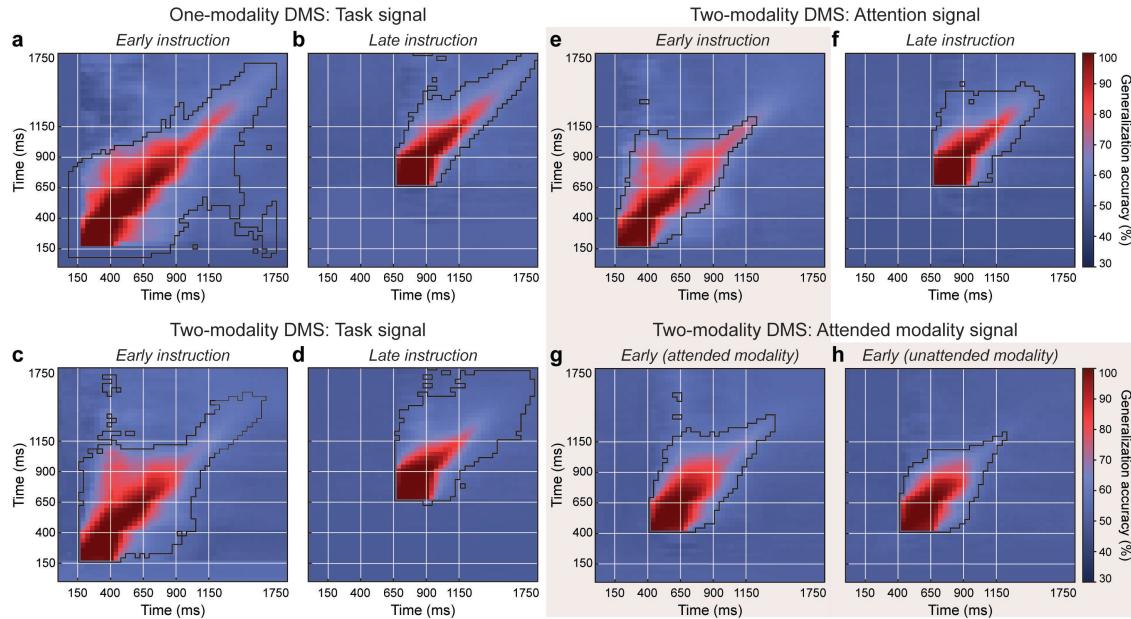


**Fig. 7 | Top-down encoding in mouse V1 and RNN sensory module.** **a.** Task summary. In the orientation condition, mice viewed an orientation pattern as either part of a figure (top left) or as part of the background (top right). Phase and texture detection conditions (not shown) were also included in the analysis. In control trials (bottom row), mice must contrast a target against a gray background which did not require figure-ground segregation. This design ensured that the same sensory information within receptive fields could possess different contextual meanings (figure vs. ground). Reproduced from [54]. **b.** SVM decoding of top-down figure vs. ground signal from V1 neurons, holding sensory input constant. Black bars indicate significant decoding ( $p < 0.05$ , random permutation test). Dashed lines indicate 95% confidence intervals from permutations. **c.** SVM decoding of top-down signal during optogenetic I-I inhibition in V1, in laser on (blue) and laser off (red) trials. Gray bar indicates laser on time window. Black bar indicates significant difference in decoding across conditions ( $p < 0.05$ , one-sided KS test). **d.** CEBRA trajectories within the sensory module of an example two-module RNN during the first stimulus period when the task signal was presented early. **e.** Same as **d** but when the connections from the non-sensory module to the sensory module were completely removed. **f.** Comparison of average within-time temporal discriminability for the first stimulus identity across 20 trained, two-module RNNs under two conditions: one with intact connections including feedback and the other without feedback (lacking connections from non-sensory to sensory modules).

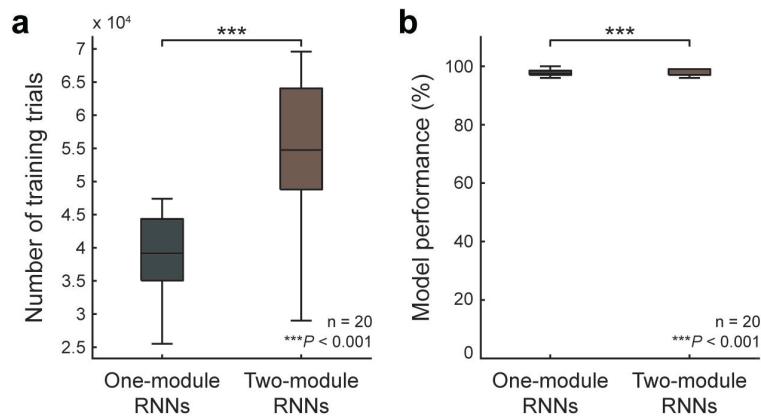


**Fig. 8 | Retro-cue signal forces the model to maintain both unattended and attended sensory signals.** **a.** Schematic of a modified version of the two-modality DMS task which includes a retro attention cue signal. The task cue signal was always given early (before the onset of the first stimulus), while the attention cue was given before the first stimulus (*early instruction*), during delay (*late instruction*), or after second stimulus (*retro-cue*). **b.** CEBRA trajectories during the first instruction and first stimulus periods for the attended modality when the attention cue signal was given early (example RNN). **c.** Same as **b** but for the unattended modality. **d-f.** Average temporal discriminability of the first stimulus identity of the unattended modality when the attention cue was given early (**d**), late (**e**), or after the second stimulus (**retro**; **f**).

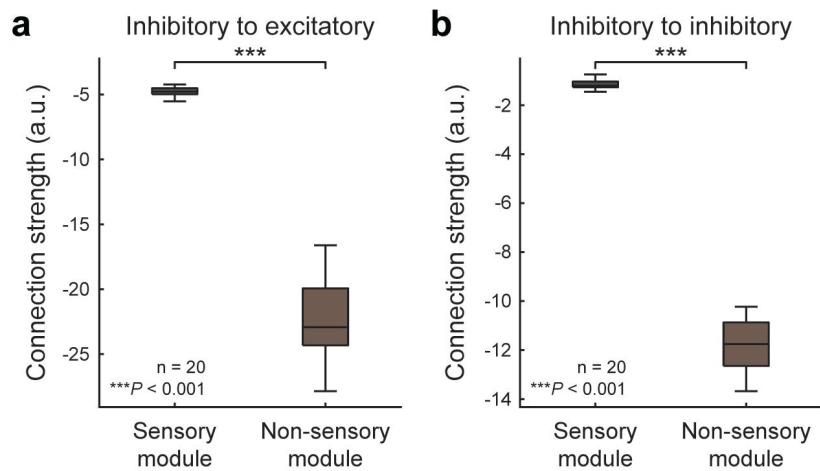
## Extended Data Figures



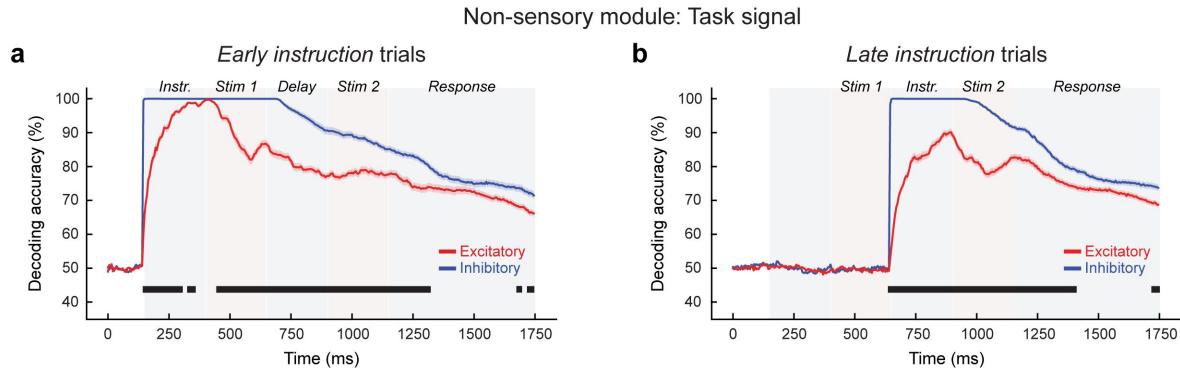
**Extended Data Fig. 1 |** Temporal encoding of top-down signals during DMS tasks. Cross-temporal decodability of task and attention signals is shown as the average generalization accuracy for each pair of training/testing time windows. Highlighted boundaries indicate significant decoding accuracy,  $p < 1e - 20$ , binomial test, Bonferroni corrected. White lines denote the reference event of each trial period (task and attention cues, stimulus onsets, response). **a.** One-modality DMS, task signal, early instruction. **b.** Same, for late instruction. **c.** Two-modality DMS, task signal, early instruction. **d.** Same, for late instruction. **e.** Two-modality DMS, attention signal, early instruction **f.** Same, for late instruction. **g.** Two-modality DMS, attended modality signal, early instruction, attended modality. **h.** Same, for unattended modality. **i.** One-modality DMS, stimulus identity. **j.** Two-modality DMS, stimulus identity, stimulus modality 1. **k.** Same, for stimulus modality 2.



**Extended Data Fig. 2 | Training two-module RNNs takes longer for the one-modality DMS compared to the one-module RNNs.** **a.** Comparison of the number of training trials required for training between the one-module and two-module RNNs, with 20 RNNs trained for each case. **b.** Both one-module and two-module RNNs achieved high accuracy in performing the one-modality DMS task (mean $\pm$ stdev; 97.7 $\pm$ 1.3% for the one-module model; 97.6 $\pm$ 1.2% for the two-module model). Boxplot: central lines, median; bottom and top edges, lower and upper quartiles; whiskers,  $1.5 \times$  interquartile range; outliers are not plotted.  $***p < 0.001$  by two-sided Wilcoxon rank-sum test.



**Extended Data Fig. 3 | Comparison between  $I \rightarrow E$  and  $I \rightarrow I$  connection strength in two-module RNNs.**  $I \rightarrow E$  (a) and  $I \rightarrow I$  (b) connections were significantly stronger within the non-sensory module than the sensory module. Boxplot: central lines, median; bottom and top edges, lower and upper quartiles; whiskers,  $1.5 \times$  interquartile range; outliers are not plotted. \*\*\* $p < 0.001$  by two-sided Wilcoxon rank-sum test.



**Extended Data Fig. 4 | Decoding task signals in non-sensory module of two-module RNNs.** **a.** Average decoding accuracy in early instruction trials for pro- vs. anti-DMS signal in the non-sensory module of two-module networks, including either excitatory (red) or inhibitory (blue) units. Shaded areas indicate standard error of the mean. Black bars indicate significant differences between excitatory and inhibitory units ( $p < 0.05$ , two-sided KS test). **b.** Same, for late instruction trials.