



# **EM600 - Engineering Economics and Cost Analysis**

## ***Lecture 08: Inflation***

- References:
  - Park, Chan S. Contemporary Engineering Economics. New Jersey: Pearson Prentice Hall, 2006 (Chapter 11)
  - Ganguly, A. Engineering Economics Using Excel. New Jersey: SSE, 2008

After completing this module you should understand the following:

- Introduction to Inflation
- Measuring / assessing inflation
- Equivalence calculation under inflation (real, constant, actual dollars)
- Impact of inflation on capital projects

- Key Definitions: (Chan S. Park)
  - Inflation:
    - *The rate at which the general level of prices and goods and services is rising and subsequently, purchasing power is falling.*
  - Deflation:
    - *Opposite to inflation.*
    - *Gain in purchasing power.*
    - *Not covered in this lecture, inflation is far more realistic to our every day lives.*

- Key Definitions: (Chan S. Park)
  - Measuring Inflation:
    - Consumer Price Index (CPI):
      - *Is an inflationary indicator that measures the change in the cost of a fixed basket of products and services.*
      - *The CPI compares the cost of a sample “market basket” of goods and services in a specific period relative to the cost of the same “market basket” in an earlier reference period. This reference period is known as the base period.*
    - Producer Price Index (PPI):
      - *Is an inflationary indicator published by the U.S. Bureau of Labor Statistics to evaluate wholesale price levels in the economy.*

- Key Definitions: (Chan S. Park)
  - Measuring Inflation:
    - Average Inflation Rate ( $f$ ):
      - *a single rate that accounts for the effect of varying yearly inflation rates over a period of several years.*
    - General Inflation Rate ( $\bar{f}$ )
      - *the **average** inflation rate calculated based on the CPI for all items in the market basket. The market interest rate is expected to respond to this inflation rate.*
    - Specific Inflation Rate ( $f_j$ )
      - *This rate is based on the CPI specific to segment  $j$  of the economy. Focuses on the future cost estimation of a particular item e.g. labor.*

- Average inflation rate ( $f$ )
  - Example 1:
    - Calculate the average inflation for a 5 year period with the following details:
      - Base price (year 1),  $P = \$150$
      - Inflation rates:
        - » Year 1 = 2.90%
        - » Year 2 = 3.76%
        - » Year 3 = 5.91%
        - » Year 4 = 2.78%
        - » Year 5 = 6.38%



- Average inflation rate ( $f$ )

- Example 1:

- Step 1: Calculate the price at the end of the 5<sup>th</sup> year,  $F$

- Use the compounding method

$$F = P(1+i)^N = P(1+f)^N \quad \dots \dots \text{eqn (1)}$$

$$F = P(F/P, i, N) = P(F/P, f, N) \quad \dots \dots \text{eqn (2)}$$

where,  $i$  = interest rate;  $f$  = average inflation rate

In this case  $f$  varies each year, therefore,

$$F = P(1+f_1)(1+f_2)(1+f_3)(1+f_4)(1+f_5)$$

$$F = \$100(1+0.029)(1+0.0376)(1+0.0591)(1+0.0278)(1+0.0638)$$

$$F = \$185.46$$



- Average inflation rate ( $f$ )
  - Example 1:
    - Step 2: Calculate the overall average inflation rate,  $f$ 
      - Use the compounding method

$$F = P(1 + i)^N = P(1 + f)^N \quad \dots \dots \text{eqn (1)}$$

$$F = P(F/P, i, N) = P(F/P, f, N) \quad \dots \dots \text{eqn (2)}$$

where,  $i$  = interest rate;  $f$  = average inflation rate for  $N$  periods

Rearranging eqn (1) yields,

$$f = \left( \frac{F}{P} \right)^{1/N} - 1$$

$$f = \left( \frac{\$185.46}{\$150} \right)^{1/5} - 1 = 4.34\%$$

- General inflation rate ( $\bar{f}$ )
  - In terms of the CPI, the general inflation rate can be defined as follows:

$$\bar{f} = \left[ \frac{CPI_n}{CPI_0} \right]^{1/n} - 1$$

where,

$\bar{f}$  = general inflation rate

$CPI_n$  = consumer price index at the end of period n

$CPI_0$  = consumer price index for the base period

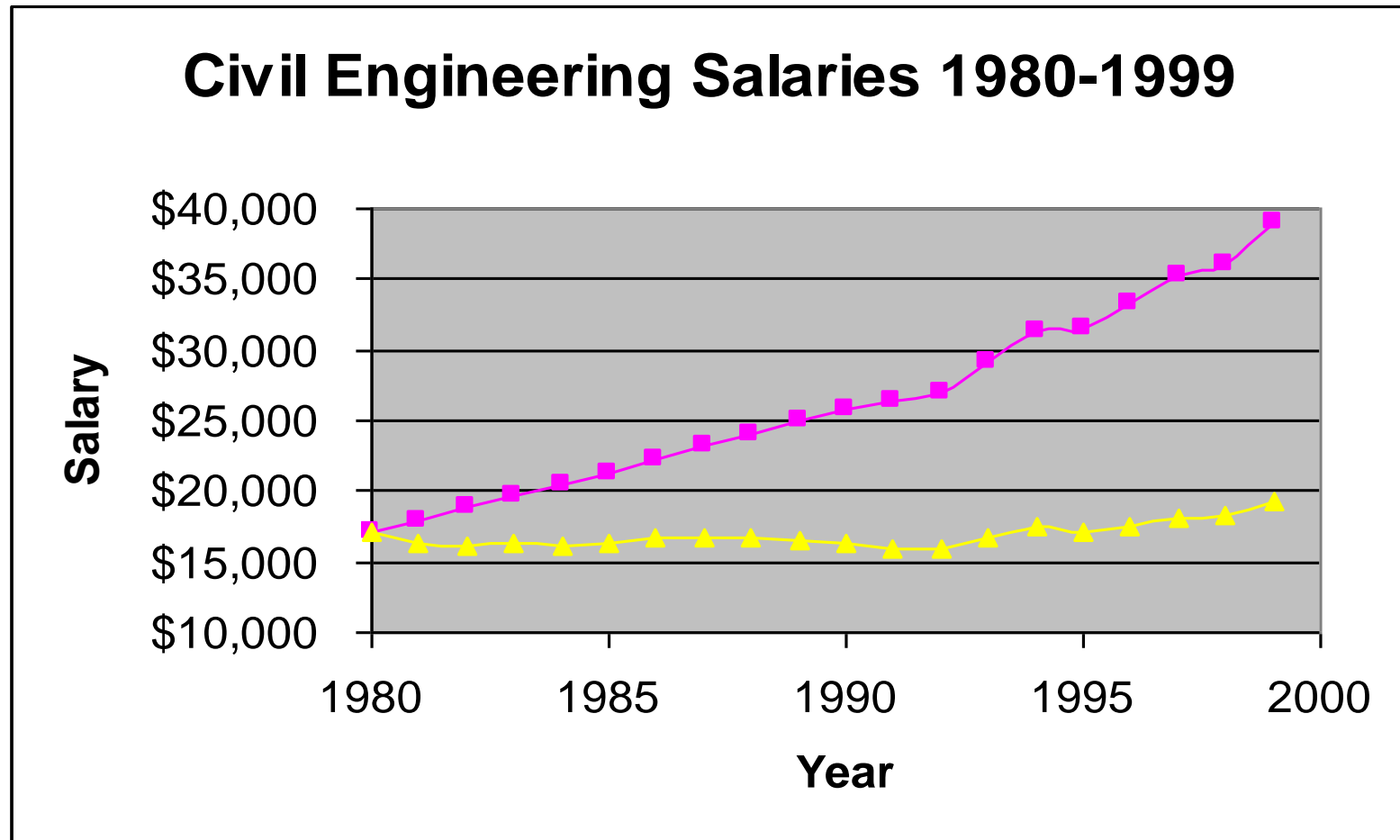
- Knowing the CPI values for 2 consecutive years, the annual general inflation rate is:

$$\bar{f}_n = \frac{CPI_n - CPI_{n-1}}{CPI_{n-1}} = \text{general inflation rate for period n}$$

- Actual versus Constant Dollars
  - Definitions: (Chan S. Park)
    - Actual Dollars ( $A_n$ )
      - *The cash flow measured in terms of dollars at the time of the transaction.*
      - *Out-of-pocket dollars paid at the time of purchasing goods and services.*
      - *Estimates of future cash flows for year  $n$  that take into account any anticipated changes in amounts caused by the effects of inflation or deflation.*
      - *Also known as: Current dollars.*

- Actual versus Constant Dollars
  - Definitions: (Chan S. Park)
    - Constant Dollars ( $A'_n$ )
      - *Represents constant purchasing power that is independent of the passage of time.*
      - *Used to adjust for the effects of inflation.*
      - *Also known as: Base-year, Nominal or Real dollars.*

- Actual versus Constant Dollars



- Actual versus Constant Dollars

- Conversion equations:

- **Constant to Actual Dollars**

$$A_n = A'_n (1 + \bar{f})^n = A'_n (F/P, \bar{f}, n)$$

- **Actual to Constant Dollars**

$$A'_n = \frac{A_n}{(1 + \bar{f})^n} = A_n (P/F, \bar{f}, n)$$

- **where,**

$A_n$  = Actual - dollar expression for the cash flow at the end of year n

$A'_n$  = Constant - dollar expression for the cash flow at the end of year n

$\bar{f}$  = General inflation rate

Note:

If the future price of a specific cash flow element ( $j$ ) is not expected to follow the general inflation rate ( $\bar{f}$ ), the average inflation rate ( $f_j$ ) applicable to that cash flow element should be used instead.

- Equivalence Calculations under Inflation
  - Two different interest rates involved
    - Inflation free interest rate,  $i'$
    - Market interest rate,  $i$
  - Two methods of analysis
    - Constant-dollar analysis (Inflation free interest rate,  $i'$ )
    - Actual-dollar analysis (Market interest rate,  $i$ )
  - Three common cases for the nature of project cash flows
    - Case 1: All cash flow elements are estimated in constant dollars
    - Case 2: All cash flow elements are estimated in actual dollars
    - Case 3: Some cash flow elements estimated in constant dollars, others in actual dollars

- Market & Inflation-Free Interest Rates
  - Inflation-free interest rate ( $i'$ )
    - *Estimate of the true earning power of money when the inflation effects have been removed.*
    - *Also known as: Real Interest Rate or MARR without inflation.*
  - Market interest rate ( $i$ )
    - *Takes into account the combined effects of earning power (earning value of capital) and purchasing power (inflation and deflation).*
    - *Also known as: Inflation Adjusted MARR or MARR with inflation.*
    - *Used to evaluate investment projects.*
    - *In the absence of inflation,  $i = i'$*



- Case 1: Constant-Dollar Analysis
  - All cash flow elements in constant dollars
  - Use  $i'$  as the interest rate to find the equivalent worth.

$$P_n = \frac{A'_n}{(1+i')^n} = A'_n (P/F, i', n)$$

where,

$P_n$  = the present worth equivalent of the constant dollar amount ( $A'_n$ ) at  $i'$ , occurring in year  $n$

- Case 1: Constant-Dollar Analysis
  - Constant dollar analysis is common in the evaluation of many long-term public projects, because government do not pay income taxes.
  - For private sector, income taxes are levied based on the taxable income in actual dollars, the actual dollar analysis is more common.

- Case 1: Constant-Dollar Analysis

- Example 2:

- Assume the following cash flow data for JoeRx, a manufacturer of an anti-inflammatory drug for their first 5 years in business:

Period, $n$	Net Cash Flow in Constant Dollars
0	-\$350,000
1	\$125,000
2	\$145,000
3	\$160,000
4	\$185,000
5	\$172,500



- With a 15% inflation-free rate of return ( $i'$ ) calculate the present worth of the cash flow series in constant dollars.

- Case 1: Constant-Dollar Analysis
  - Example 2:

Period, n	Net Cash Flow in Constant Dollars	(P/F, 15%, n)
0	-\$350,000	-
1	\$125,000	0.8696
2	\$145,000	0.7561
3	\$160,000	0.6575
4	\$185,000	0.5718
5	\$172,500	0.4972



$$PW = -P + \sum_{n=1}^N A'_n (P/F, i', n)$$

$$PW = -\$350,000 + \$125,000(P/F, 15\%, 1) + \$145,000(P/F, 15\%, 2) \\ + \$160,000(P/F, 15\%, 3) + \$185,000(P/F, 15\%, 4) + \$172,500(P/F, 15\%, 5)$$

$$PW = -\$350,000 + \$125,000(0.8696) + \$145,000(0.7561) \\ + \$160,000(0.6575) + \$185,000(0.5718) + \$172,500(0.4972)$$

$$PW = \$165,085$$

- Case 2: Actual-Dollar Analysis
  - All cash flow elements in actual dollars
  - Use  $i$  as the interest rate to find the equivalent worth.
  - Two Methods:
    - Deflation Method:
      - 1. Convert actual dollars into equivalent constant dollars by discounting by the general inflation rate (common purchasing power)
      - 2. Use  $i'$  to find the equivalent present worth (consider the earning power)
    - Adjusted Discount Method:
      - Combines steps 1 and 2 of the deflation method.
      - Performs deflation and discounting in one step using the market interest rate ( $i$ ).

- Case 2: Actual-Dollar Analysis
  - Deflation Method
    - Example 3:
      - Assume the following cash flow data:

Period, $n$	Net Cash Flow in Actual Dollars
0	-\$95,000
1	\$39,000
2	\$41,500
3	\$27,250
4	\$33,750
5	\$61,000



- Calculate the equivalent constant dollars if the general inflation rate ( $\bar{f}$ ) is 4% per year.
- With a 12% inflation-free rate of return ( $i'$ ) calculate the present worth of the cash flow series in constant dollars.

- Case 2: Actual-Dollar Analysis
  - Deflation Method
    - Example 3:
      - Calculate the equivalent constant dollars if the general inflation rate ( $\bar{f}$ ) is 4% per year.

Period, n	Net Cash Flow in Actual Dollars	(P/F,4%,n)	Net Cash Flow in Constant Dollars
0	-\$95,000	-	-\$95,000
1	\$39,000	0.9615	\$37,499
2	\$41,500	0.9246	\$38,371
3	\$27,250	0.8890	\$24,225
4	\$33,750	0.8548	\$28,850
5	\$61,000	0.8219	\$50,136

- Case 2: Actual-Dollar Analysis
  - Deflation Method
    - Example 3:

– With a 12% inflation-free rate of return ( $i'$ ) calculate the present worth of the cash flow series.

Period, $n$	Net Cash Flow in Constant Dollars	$(P/F, 12\%, n)$
0	-\$95,000	-
1	\$37,499	0.8929
2	\$38,371	0.7972
3	\$24,225	0.7118
4	\$28,850	0.6355
5	\$50,136	0.5674



$$PW = -P + \sum_{n=1}^N A'_n (P/F, i', n)$$

$$PW = -\$95,000 + \$37,499(P/F, 12\%, 1) + \dots + \$50,136(P/F, 12\%, 5)$$

$$PW = -\$95,000 + \$37,499(0.8929) + \dots + \$50,136(0.5674)$$

$$PW = \$33,096$$



- Case 2: Actual-Dollar Analysis
  - Adjusted Discount Method
    - The market interest rate ( $i$ ) reflects both the earning power and the purchasing power.
    - The market interest rate ( $i$ ) is therefore a function of:
      - $\bar{f}$ , general inflation rate
      - $i'$ , inflation - free interest rate
    - and can be expressed as:
$$i = i' + \bar{f} + i' \bar{f}$$

- Case 2: Actual-Dollar Analysis

- Adjusted Discount Method

- Since the market rate ( $i$ ) reflects both the earning power and the purchasing power,

$$P_n = \frac{A_n}{(1+i)^n} = A_n (P/F, i, n)$$

where,

$P_n$  = the present worth equivalent of the constant dollar amount ( $A_n$ ) at  $i$ , occurring in year  $n$

- Case 2: Actual-Dollar Analysis

- Adjusted Discount Method

- Example 4:

- Assume the same cash flow data for example 3:

Period, n	Net Cash Flow in Actual Dollars
0	-\$95,000
1	\$39,000
2	\$41,500
3	\$27,250
4	\$33,750
5	\$61,000



- With a general inflation rate ( $\bar{f}$ ) of 4% per year and a 12% inflation-free rate of return ( $i'$ ) calculate the present worth of the cash flow series.

- Case 2: Actual-Dollar Analysis
  - Adjusted Discount Method
    - Example 4:
      - Calculate the market interest rate ( $i$ ) with,
        - » general inflation rate ( $\bar{f}$ ) of 4%
        - » inflation-free rate of return ( $i'$ ) of 12%
$$i = i' + \bar{f} + i' \bar{f}$$
$$i = 12\% + 4\% + (12\% \times 4\%)$$
$$i = 16.48\%$$

- Case 2: Actual-Dollar Analysis
  - Adjusted Discount Method

- Example 4:

- With a 16.48% market interest rate of return ( $i$ ) calculate the present worth of the cash flow series.

Period, $n$	Net Cash Flow in Actual Dollars	$(P/F, 16.48\%, n)$
0	-\$95,000	-
1	\$39,000	0.8585
2	\$41,500	0.7371
3	\$27,250	0.6328
4	\$33,750	0.5432
5	\$61,000	0.4664



$$PW = -P + \sum_{n=1}^N A_n (P/F, i, n)$$

$$PW = -\$95,000 + \$39,000(P/F, 16.48\%, 1) + \dots + \$61,000(P/F, 16.48\%, 5)$$

$$PW = -\$95,000 + \$39,000(0.8585) + \dots + \$61,000(0.4664)$$

$$PW = \$33,097$$

- Case 3: Mixed-Dollar Analysis
  - All cash flow elements should be converted into the same dollar units
    - Converted to **constant** dollars = use the inflation-free interest rate ( $i'$ ) when calculating the equivalent present worth.
    - Converted to **actual** dollars = use the market interest rate ( $i$ ) when calculating the equivalent present worth.

- ***Effects of Inflation on Project Cash Flows:***

- Two areas of focus:
  - Depreciation expenses
  - Interest expenses
- Why focus on these areas?
  - Always given in actual dollars (with inflation), therefore, they are essentially immune to the effects of inflation.

- ***Effects of Inflation on Projects with Depreciable Assets***

- Example 5: (Chan S. Park, example 11.8)

- Refer to example 1, Lecture 7
- Project: Installation of a new computer system
- Financial Data:
  - Investment: \$125,000
  - Project life: 5 years
  - Salvage value: \$50,000
  - Annual labor savings (Annual Revenues): \$100,000
  - Annual manufacturing costs:
    - » Labor: \$20,000
    - » Materials: \$12,000
    - » Overhead: \$8,000
  - Depreciation method: 7-year MACRS
  - Income tax rate: 40%
  - Inflation-free interest rate ( $i'$ ): 15%



- ***Effects of Inflation on Projects with Depreciable Assets***
  - Example 5: (Chan S. Park, example 11.8)
    - PW in the absence of inflation: \$43,153
    - Using the deflation method:
      - Determine the PW of the project if the general inflation rate ( $\bar{f}$ ) during the next 5 years is expected to increase by 5% annually.

- ***Effects of Inflation on Projects with Depreciable Assets***
  - Example 5: (Chan S. Park, example 11.8)
    - Identify the items in the Income Statement and Cash Flow Statement that are impacted by the general inflation rate:
      - Income Statement:
        - » Revenues
        - » Expenses
          - » Labor
          - » Material
          - » Overhead
      - Cash Flow Statement:
        - » Salvage
          - » Will also have an impact on the gains tax

- ***Effects of Inflation on Projects with Depreciable Assets***

- Example 5: (Chan S. Park, example 11.8)

- Notes:

- The items identified in the previous slide are all the cash flow elements assumed to be in constant dollars.
  - » These need to be converted to actual dollars
  - » Depreciation expenses are not included
- The Net Cash Flows (operating activities and investment activities) are in actual dollars.
  - » These need to be converted to constant dollars before the PW can be calculated.
- General inflation rate of 5% is assumed to apply to each of the identified cash flow elements on the previous slide starting in year 1

- **Example 5: (Chan S. Park, example 11.8)**
  - **Income Statement**

<b>YEAR:</b>	$\bar{f}$	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>
<b>Revenues</b>	<b>5%</b>	\$105,000	\$110,250	\$115,763	\$121,551	\$127,628
<b>Expenses:</b>						
Labor	<b>5%</b>	\$21,000	\$22,050	\$23,153	\$24,310	\$25,526
Material	<b>5%</b>	\$12,600	\$13,230	\$13,892	\$14,586	\$15,315
Overhead	<b>5%</b>	\$8,400	\$8,820	\$9,261	\$9,724	\$10,210
Depreciation		\$17,863	\$30,613	\$21,863	\$15,613	\$5,581
<b>Taxable Income</b>		\$45,137	\$35,537	\$47,595	\$57,317	\$70,996
<b>Income Taxes (40%)</b>		\$18,055	\$14,215	\$19,038	\$22,927	\$28,398
<b>Net Income</b>		\$27,082	\$21,322	\$28,557	\$34,390	\$42,598

- **Example 5: (Chan S. Park, example 11.8)**
  - **Cash Flow Statement**

<b>YEAR:</b>	$\bar{f}$	<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>
<b>Operating Activities:</b>							
Net Income			\$27,082	\$21,322	\$28,557	\$34,390	\$42,598
Depreciation			\$17,863	\$30,613	\$21,863	\$15,613	\$5,581
<b>Investment Activities:</b>							
Investment		-\$125,000					
Salvage	5%						\$63,814
Gains Tax							-\$12,138
<b>Net Cash Flow (Actual Dollars)</b>		-\$125,000	\$44,945	\$51,935	\$50,419	\$50,003	\$99,855

- **Example 5: (Chan S. Park, example 11.8)**
  - **Income Statement Notes**
    1. Revenues =  $\$100,000 \times (1 + 5\%)^n$
    2. Labor =  $\$20,000 \times (1 + 5\%)^n$
    3. Material =  $\$12,000 \times (1 + 5\%)^n$
    4. Overhead =  $\$8,000 \times (1 + 5\%)^n$
  - **Cash Flow Statement Notes**
    1. Salvage Value =  $\$50,000 \times (1 + 5\%)^n$
    2. Gains tax increases as salvage value has increased due to conversion to actual dollars from constant dollars.

- Example 5: (Chan S. Park, example 11.8)**

Period, n	Net Cash Flow in Actual Dollars	(P/F, 5%, n)	Net Cash Flow in Constant Dollars	(P/F, 15%, n)
0	-\$125,000	-	-\$125,000	-
1	\$44,945	0.8658	\$42,804	0.8696
2	\$51,935	0.7496	\$47,106	0.7561
3	\$50,419	0.6490	\$43,554	0.6575
4	\$50,003	0.5619	\$41,138	0.5718
5	\$99,855	0.4865	\$78,239	0.4972

$$PW = -P + \sum_{n=1}^N A'_n (P/F, i', n)$$

$$PW = -\$125,000 + \$42,804(P/F, 15\%, 1) + \dots + \$78,239(P/F, 12\%, 5)$$

$$PW = -\$125,000 + \$42,804(0.8696) + \dots + \$78,239(0.4972)$$

$$PW = \$38,899$$



- Note:** The adjusted-discount method can also be used here.

- ***Effects of Multiple Inflation Rates on Project Cash Flows***

- Methodology:

- Apply the same methodology as in example 5.
- In this case, where inflation rates are given for specific elements, apply them to those elements.
- Use the general rate of inflation and the inflation-free interest rates to calculate the PW using either,
  - The deflation method, or
  - The adjusted-discount method

as previously shown

- Refer to Chan S. Park, example 11.9



- ***Effects of Borrowed Funds under Inflation***

- Notes:

- Loan repayment is based on a historical contract amount.
- Debt payment size **does not** change with inflation.
- Future payments are calculated based on year-0 dollars.
- Under the effect of inflation, the constant-dollar costs of both interest and principal repayments on a debt are reduced.

- Summary:

- Borrowers repay historical loan amounts with dollars of decreased purchasing power, reducing the debt-financing cost.

- ***Effects of Borrowed Funds under Inflation***
  - Example 6: (Chan S. Park, example 11.10)
    - Recall example 5
    - Assume a debt ratio of 0.5.
      - \$62,500 borrowed
    - Debt borrowed at an annual interest rate of 15.5%.
    - General Inflation Rate ( $\bar{f}$ ) = 5%
    - Calculate the loan repayment schedule
      - In actual dollars
      - In constant dollars
    - What is the borrowers gain in constant dollars?

# • *Effects of Borrowed Funds under Inflation*

## – Example 6: (Chan S. Park, example 11.10)

- Calculate annual loan repayment in actual dollars:

	A	B
1	P, amount borrowed	\$62,500
2	i	15.50%
3	N	5
4	AE	\$18,866

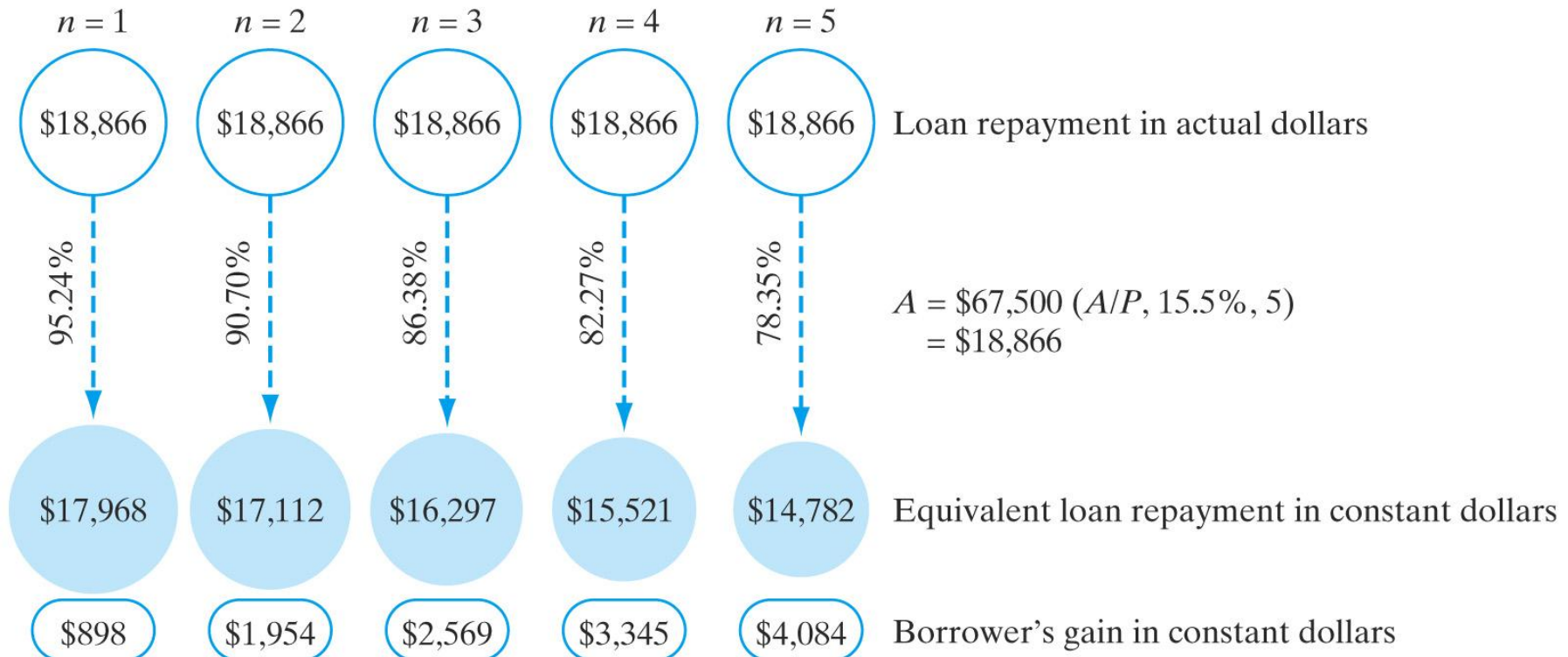
	A	B
1	P, amount borrowed	\$62,500
2	i	15.50%
3	N	5
4	=PMT(B2,B3,-B1,,)	

- Loan repayment breakdown:

Year	Beginning Balance	Interest Payment	Principal Payment	Ending Balance
1	\$62,500	\$9,688	\$9,178	\$53,322
2	\$53,322	\$8,265	\$10,601	\$42,720
3	\$42,720	\$6,622	\$12,244	\$30,476
4	\$30,476	\$4,724	\$14,142	\$16,334
5	\$16,334	\$2,532	\$16,334	\$0

# • **Effects of Borrowed Funds under Inflation**

– Example 6: (Chan S. Park, example 11.10)



**Equivalent Loan repayment cash flows measured in year-0 dollars and borrowers gain over the life of the loan (Chan S. Park, Figure 11.3)**

- ***Effects of Inflation on Return on Investment***

- Notes:

- Unless revenues are sufficiently increased to keep pace with inflation, tax effects and/or a working capital drain result in lower rate of return or lower NPW.
- Under inflation, true (real) rate of return should be based on constant dollars.
- Under inflation, if the rate of return is calculated based on actual dollars, the real rate of return can be calculated

as: 
$$i' = \frac{1+i}{1+\bar{f}} - 1 \quad \text{where,}$$

$i'$  = the real rate of return based on constant dollars

$i$  = the market rate of return based on actual dollars

$\bar{f}$  = general rate of inflation

- Effects of Inflation on Return on Investment: No Inflation**

**MARR = 20%**

**IRR' = 21.88%**

**The investment is acceptable.**

	0	1	2	3	4
Income statement:					
Revenues		\$ 24,500	\$ 24,500	\$ 24,500	\$ 24,500
Expenses					
O&M		10,000	10,000	10,000	10,000
Depreciation		10,000	13,333	4,445	2,222
Taxable income		4,500	1,167	10,055	12,278
Income taxes (40%)		1,800	467	4,022	4,911
Net income		\$ 2,700	\$ 700	\$ 6,033	\$ 7,367
Cash flow statement:					
Operating activities					
Net income		2,700	700	6,033	7,367
Depreciation		10,000	13,333	4,445	2,222
Investment activities					
Machine center	\$ (30,000)				
Salvage					0
Gains tax					0
Net cash flow					
(in actual dollars)	\$ (30,000)	\$ 12,700	\$ 14,033	\$ 10,478	\$ 9,589

**Example 11.11 (Chan S. Park, Table 11.5)**

- Effects of Inflation on Return on Investment: Inflation**

**MARR = 20%**

**IRR' = 19.40%**

**The investment  
is no longer  
acceptable.**

	0	1	2	3	4
Income statement:					
Revenues		\$26,950	\$29,645	\$32,610	\$35,870
Expenses					
O&M		11,000	12,100	13,310	14,641
Depreciation		10,000	13,333	4,445	2,222
Taxable income		5,950	4,212	14,855	19,007
Income taxes (40%)		<u>2,380</u>	<u>1,685</u>	<u>5,942</u>	<u>7,603</u>
Net income		\$ 3,570	\$ 2,527	\$ 8,913	\$11,404
Cash flow statement:					
Operating activities					
Net income		3,570	2,527	8,913	11,404
Depreciation		10,000	13,333	4,445	2,222
Investment activities					
Machine center	\$(30,000)				
Salvage					0
Gains tax					<u>0</u>
Net cash flow					
(in actual dollars)	\$(30,000)	\$13,570	\$15,860	\$13,358	\$13,626
Net cash flow					
(in constant dollars)	\$(30,000)	\$12,336	\$13,108	\$10,036	\$ 9,307

*Note: PW(20%) = \$(321); IRR (actual dollars) = 31.34%; IRR' (constant dollars) = 19.40%.*



- ***Effects of Inflation on Working Capital***

- Notes:

- Known as working capital drain, the cost of working capital increases in an inflationary environment.
- Additional cash must be invested to maintain new price levels.
- Additional working capital requirements can significantly reduce a project's rate of return.



- Effects of Inflation on Working Capital: No Inflation**

**MARR = 20%**

**IRR' = 20.88%**

**The investment is acceptable.**

Case 1: Without Inflation	0	1	2	3	4
Income statement:					
Revenue		\$ 24,500	\$ 24,500	\$ 24,500	\$ 24,500
Expenses					
O&M		10,000	10,000	10,000	10,000
Depreciation		10,000	13,333	4,445	2,222
Taxable income		4,500	1,167	10,055	12,278
Income taxes (40%)		1,800	467	4,022	4,911
Net income		\$ 2,700	\$ 700	\$ 6,033	\$ 7,367
Cash flow statement:					
Operating activities					
Net income		2,700	700	6,033	7,367
Depreciation		10,000	13,333	4,445	2,222
Investment activities					
Machine center	\$ (30,000)				
Working capital	(1,000)				1,000
Salvage					0
Gains tax					0
Net cash flow					
(in actual dollars)	\$ (31,000)	\$ 12,700	\$ 14,033	\$ 10,478	\$ 10,589

*Note: PW(20%) = \$499; IRR' = 20.88%.*

- Effects of Inflation on Working Capital: Inflation**

**MARR = 20%**

**IRR' = 18.09%**

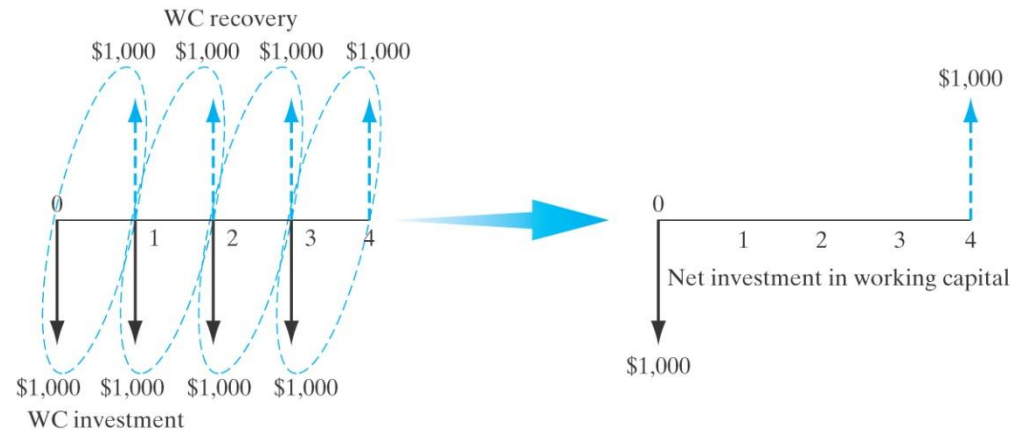
**The investment  
is no longer  
acceptable.**

Case 2: With Inflation (10%)	0	1	2	3	4
Income statement:					
Revenue		\$ 26,950	\$ 29,645	\$ 32,610	\$ 35,870
Expenses					
O&M		11,000	12,100	13,310	14,641
Depreciation		10,000	13,333	4,445	2,222
Taxable income		5,950	4,212	14,855	19,007
Income taxes (40%)		2,380	1,685	5,942	7,603
Net income		\$ 3,570	\$ 2,527	\$ 8,913	\$ 11,404
Cash flow statement:					
Operating activities					
Net income		3,570	2,527	8,913	11,404
Depreciation		10,000	13,333	4,445	2,222
Investment activities					
Machine center	\$ (30,000)				
Working capital	(1,000)	(100)	(110)	(121)	\$ 1,331
Salvage					0
Gains tax					0
Net cash flow (in actual dollars)	\$ (31,000)	\$ 13,470	\$ 15,750	\$ 13,237	\$ 14,957
Net cash flow (in constant dollars)	\$ (31,000)	\$ 12,245	\$ 13,017	\$ 9,945	\$ 10,216

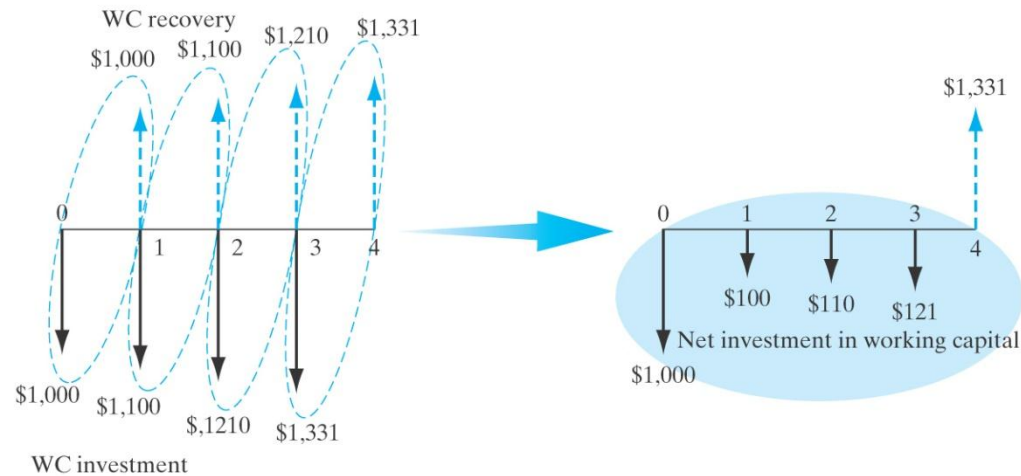
Note:  $PW(20\%) = \$ (1,074)$ ;  $IRR$  (actual dollars) = 29.89%;  $IRR'$  (constant dollars) = 18.09%.

**Example 11.12 (Chan S. Park, Table 11.7)**

- Effects of Inflation on Working Capital:**



(a) Without inflation



(b) With inflation

**Working Capital Requirements under inflation (Chan S. Park, example 11.12; figure 11.4)**

