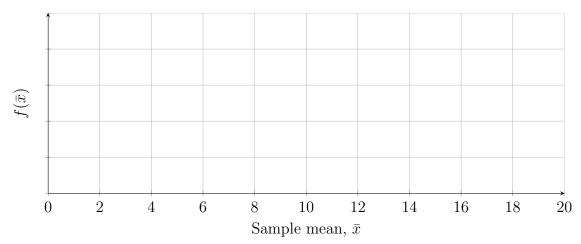
STEVENS INSTITUTE OF TECHNOLOGY

SYS-601 Practice Exam #2

2.1Statistical Sampling

- (a) Which of the following do random sampling methods seek to eliminate?
 - (A) Sampling error

- (C)Human bias
- (B) Correlation between samples
- (D)All of the above
- (b) Which situation generally recommends the use of Student's t distribution to compute confidence intervals on mean?
 - (A) Large number of samples
- (C)Normal population distribution
- (B) Unknown population std. deviation
- (D) None of the above
- (c) If a random variable X has a normal distribution f(x) with population mean $\mu = 10$ and standard deviation $\sigma = 3$, which of the following describes the distribution of the sample mean \bar{X} for N = 100 samples?
 - (A)
- $\bar{X} \sim \text{normal}(\mu_{\bar{x}} = 10, \sigma_{\bar{x}} = 3)$ (C) $\bar{X} \sim \text{normal}(\mu_{\bar{x}} = 0, \sigma_{\bar{x}} = 1)$
 - $\bar{X} \sim \text{normal}(\mu_{\bar{x}} = 10, \sigma_{\bar{x}} = 0.3)$ (B)
- (D) None of the above
- (d) Sketch the distribution shape $f(\bar{x})$ for the sample mean in the space below.



- (e) If a random variable X has a normal distribution f(x) with population mean $\mu = 10$ and variance $\sigma^2 = 9$, which of the following describes the distribution of the sample variance s^2 for N = 100 samples?
 - (A) $11 \cdot s^2 \sim \text{chi}(k = 9)$ (C) $11 \cdot s^2 \sim \text{chi}(k = 99)$
 - (B) $s^2 \sim \text{chi}2(k=9)$ (D) None of the above
- (f) Assume a normally-distributed population has standard deviation $\sigma = 3$. How many samples would be required to estimate the population mean with a 99% chance of being within 0.3 units of the true value?

N =

2.2 Hypothesis Testing

| (8 | $\mathbf{a})$ | Which of | of the | following | statements | is | incorrect? |
|----|---------------|----------|--------|-----------|------------|----|------------|
|----|---------------|----------|--------|-----------|------------|----|------------|

- (A) The acceptable probability of making a Type I error is set by parameter α .
- (B) A Type I error means a true null hypothesis was rejected.
- (C) A Type II error means a false null hypothesis was not rejected.
- (D) Statistical methods minimize the chance of Type I and Type II errors.
- (b) What is the best interpretation of a *p*-value?
 - (A) Probability of a Type I error. (C) Prob. of a true null hypothesis.
 - (B) Probability of a Type II error. (D) Prob. of a false null hypothesis.
- (c) Pokémon Go is a popular mobile game produced by Niantic. A large user community attempts to reverse-engineer various gameplay mechanics by collecting data and performing statistical analysis.

A dataset collected by Redditor CarolinaCapsFan in February 2017¹ investigates item drop rates. Out of N=1756 samples, they report the sample drop rate of Potions to be $\bar{x}=149/1756=0.0849$ and the sample standard deviation, approximated by a Bernoulli Trial, is $s=\sqrt{\bar{x}(1-\bar{x})}=\sqrt{0.0849\cdot0.9151}=0.279$.

Perform a statistical test to check if the Potion drop rate during February 2017 was equal to a hypothesized value of $\mu^* = 0.10$. Report the test statistic and p-value.

Test statistic: p =

(d) Explain the meaning of results in (c) above to someone unfamiliar with statistics.

(e) A second dataset collected by Redditor Crawnic in August 2016^2 gathered N=9976 samples, reporting a sample drop rate of Potions to be $\bar{x}=760/9976=0.0762$ and the sample standard deviation is approximately $s=\sqrt{0.0762\cdot0.9238}=0.265$.

 $^{^{1}} https://www.reddit.com/r/TheSilphRoad/comments/5vqjyc/pokestop_drop_rates_in_gen_2_lvl_31_7_days_511/$

²https://www.reddit.com/r/TheSilphRoad/comments/4whv63/3207_pokestops_data/

Perform a statistical test to check if the Potion drop rate during August 2016 and February 2017 were equal. Report the test statistic and p-value. (Hint: feel free to assume the sample standard deviations are close to true population standard deviations.)

(ii)

Test statistic: p =

(f) Explain the meaning of results in (e) above to someone unfamiliar with statistics.

- (g) Match each scenario with the best corresponding class of hypothesis test.
 - Check if the variance of one normally- (i) distributed population is less than $\sigma^* = 9$.

(A) z Test

Check if the means of two related populations are unequal.

- (B) Paired t Test
- Check if the variances of two normally- (iii) distributed populations are unequal.
- (C) χ^2 Test
- Check if the mean of one population is greater than $\mu^* = 10$ using 100 samples.
- (D) F Test

2.3 Experimental Analysis

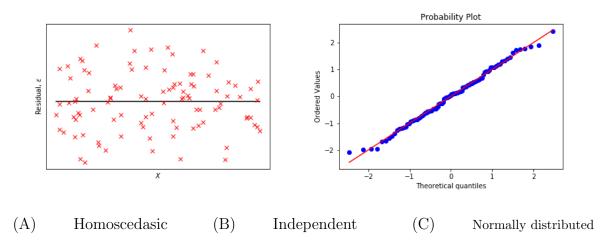
| (a) | Which of the following is not a key principle of rigorous experimental design? | | | | |
|-----|--|------------------------------------|-------|---|--|
| | (A) | Randomization | (C) | One factor at a time | |
| | (B) | Replication | (D) | Blocking variables | |
| (b) | (b) Why may a full factorial experiment not be desirable? | | | | |
| | (A) | Cannot detect interaction effects | (C) | Results dependent on intuition | |
| | (B) | Requires too many trials | (D) | Cannot isolate multiple factors | |
| (c) | (c) On which statistical test is analysis of variation (ANOVA) based? | | | | |
| | (A) | F test for difference in variances | (C) | χ^2 test for population variance | |
| | (B) | t test for difference in means | (D) | z test for population mean | |
| (d) | Blogger Juan De Dios Santos collected data in Pokémon Go for nine days dur August 2016 including information about item drops ³ . Out of $N=886$ samples, reports the sample drop rate of Potions to be $\bar{x}=65/886=0.0733$. Does the addit of a third dataset help understand if the Potion drop rate varies across players? The three datasets are presented in the supplied file potion_drops.csv. Calculate the following statistics using an appropriate ANOVA method. For ease | | | os ³ . Out of $N=886$ samples, he $5/886=0.0733$. Does the addition p rate varies across players? potion_drops.csv. ate ANOVA method. For ease of | |
| | analysis, compiled datasets for the three Pokémaniacs are available via Canvas. Sorter samples only record 0 or 1 to determine if a Potion was dropped at a Pokéstop. | | | | |
| | SSC | C = | MSC = | = | |
| | SSE | $\mathcal{E} =$ | MSE = | = | |
| (e) | Perform a statistical hypothesis test to check if at least one of the three players has different Potion drop rate. Report the test statistic and p -value. | | | 1 0 | |
| | Test s | statistic: | p | = | |

 $^{^3 \}verb|https://github.com/juandes/PokemonGo9DaysAnalysis|$

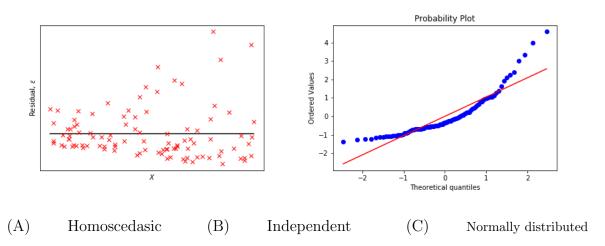
(f) Explain the meaning of results to someone unfamiliar with statistics.

2.4 Regression Analysis

- (a) Which statement regarding linear regression models is **incorrect**?
 - (A) Regression implies causality between independent and dependent variables.
 - (B) Forward selection and backward elimination methods will both produce the same multiple regression model.
 - (C) Unhealthy residuals indicate the linear assumption is invalid.
 - (D) Coefficient values are calculated to minimize the sum of squares of error between observations and predictions.
- (b) Assess the health of the following simple regression model via its residual scatter (left) and probability (right) plots and mark **all** applicable properties.



(c) Assess the health of the following simple regression model via its residual scatter (left) and probability (right) plots and mark **all** applicable properties.



(d) Blogger Juan De Dios Santos collected data about the Pokémon he caught in Pokémon Go for nine days during August 2016⁴. During this time period, he caught 60 Pidgey (a small bird) and recorded their combat power (CP), health points (HP), height (meters), and weight (kilograms).

The dataset is presented in the supplied file Pidgey.csv.

Develop a multiple regression model to predict Pidgey CP as a function of HP, height, and weight as follows:

$$\hat{y}_{\text{CP}} = \beta_0 + \beta_1 \cdot x_{\text{HP}} + \beta_2 \cdot x_{\text{height}} + \beta_3 \cdot x_{\text{weight}}$$

Report the fitted coefficient values, their statistical significance, and explain the meaning of results for each coefficient.

| Coef. | Value | Statistically | Meaning of Results |
|-----------|-------|---------------|--------------------|
| | | Significant? | |
| | | | |
| | | | |
| β_0 | | Yes | |
| | | No | |
| | | | |
| | | | |
| β_1 | | Yes | |
| /~ 1 | | No | |
| | | 110 | |
| | | | |
| | | 37 | |
| β_2 | | Yes | |
| | | No | |
| | | | |
| | | | |
| β_3 | | Yes | |
| | | No | |
| | | | |

 $^{^4 {\}tt https://github.com/juandes/PokemonGo9DaysAnalysis}$

2.5 Categorical and Non-parametric Statistics

They can accommodate ordinal, interval, or ratio sample data.

(a) Which statement regarding non-parametric statistics is **incorrect**?

(A)

| | (B) | They are based on sample rank rather than magnitude. | | | | | | |
|---|--|--|------------|----------------------------|----------------|--------------------------------|--|--|
| | (C) They are out-of-date compared to parametric statistics. | | | | | catistics. | | |
| | (D) | They are n | not widely | available in | spreadsheet to | ols. | | |
| (b) | Which st | Which statement regarding the chi-squared goodness of fit test is incorrect ? | | | | | | |
| | (A) | It can acco | ommodate | e any type of sample data. | | | | |
| | (B) Choosing how samples are binned into categories does not change res | | | | | | | |
| | (C) No category should have zero expected observations. | | | | | | | |
| | (D) | It can be u | sed to che | eck if data f | ollow a mathem | atical distribution. | | |
| (c) | Match ea | ach non-par | ametric st | atistic with | the correspond | ing parametric version. | | |
| | Friedma | an Test | | (i) | (A) |) t Test | | |
| | Kruskal | l-Wallis Tes | t | (ii) | (B) |) Paired t Test | | |
| | Mann-V | Whitney U | Test | (iii) | (C) |) Pearson's Correlation | | |
| | Spearma | an's Rank C | orrelation | (iv) | (D) |) One-way ANOVA | | |
| | Wilcoxo | n Matched l | Pairs Test | (v) | (E) | Two-way ANOVA | | |
| (d) Some players of Pokémon Go are concerned that the current game mechanic players living in urban areas more than those in rural areas. The following (survey of 300 players shows the number of responses with negative, neutral, and sentiment for players living in urban and rural locations. | | | | | | eas. The following (fictional) | | |
| | O_{ij} | Negative | Neutral | Positive | | | | |
| | Urban | 25 | 128 | 92 | | | | |
| | Rural | 14 | 28 | 13 | | | | |
| | Record the expected number of observations below assuming player location and resentiment are independent. | | | | | | | |
| | E_{ij} | Negativ | ve | Neutral | Positive | | | |
| | Urban | | | | | | | |
| | Rural | | | | | | | |
| | - | | | | | | | |

| (e) Perform a statistical test to evaluat | te whether player location and review sentiment are |
|---|---|
| independent. Report the test statis | stic and p -value. |
| | |
| | |
| Test statistic: | p = |

(f) Explain the meaning of results to someone unfamiliar with statistics.