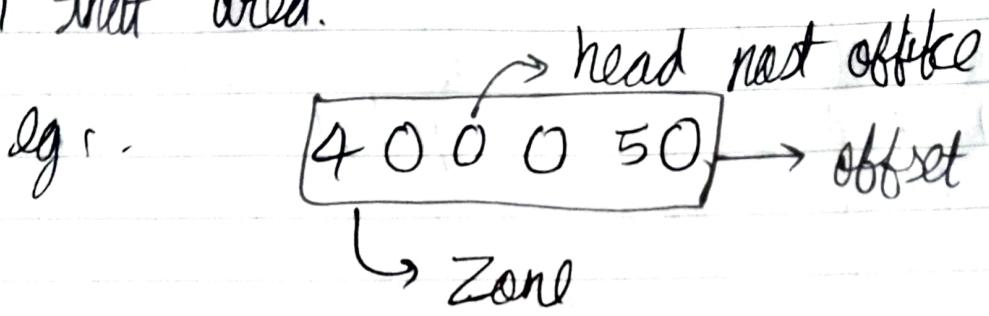
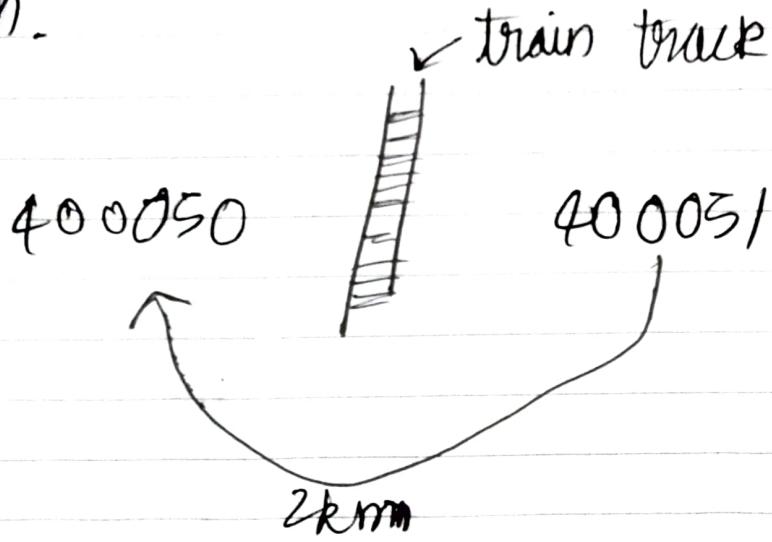


Google Maps Algorithm

Earlier Pincode / Zipcode sys was used \rightarrow assign each area based on that ~~root~~ root office in that area.



eg:- customer in 400051 shop in 400050 order comes along another path & not disp. path.



\therefore Our sys should satisfy the foll. criteria:

- GOAL 1)** Measurable dist b/w any 2 pts. ~~for this we need~~
- i) uniformity in the way nos. are assigned to loc's
 - ii) Granularity in our scalable sys. i.e. we should be able to break areas further into smaller & smaller areas.

(GOAL 2) Proximity :- eg:- find nearby loca's from a user.

for meeting goals

M-1

no rule
for
assignment
dist used
for
proximity

$$\therefore \text{Euclidean dist} = \sqrt{\sum(r_i - r_j)^2}$$

Problem

→ you gotta check and store dist of all pts in your region ~~all~~

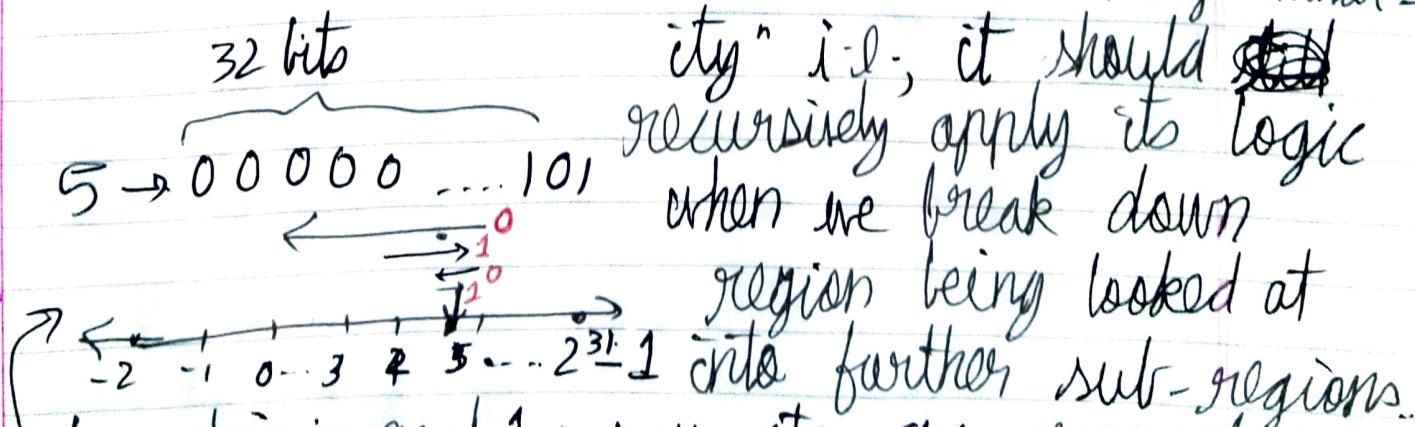
as size of region grows, this algo has a really bad TC ($O(N)$) and doesn't work very efficiently

M-2 :

for achieving goal 1 → find a smart way to assign nos to points in region

for achieving goal 2 → use a data struc., on which, if you do a range query, you get proximity of 2 pts

also, this data struc. should have "scalable granularity" i.e., it should recursively apply its logic when we break down



for achieving goal 1 → how pts. are represented

say we have a no. = 5-685

→ Q:- 5-685 [6]

Date: _____
M T W T F S S

For 4th decimal place, we add 1 more bit/group of bits i.e. we allocate 32 mem. in computer

In computer, we have
2 data types → 32 bit datatype
64 bit datatype

each data type represents a range of nos.
not the exact no.

i.e. $\frac{10}{3}$ is stored on 32-bit as $3.333333333 < \frac{10}{3}$

< 3.333333334

∴ you have a small "error range" where your actual no. lies in

∴ You can think of this as a way to find a small range of nos.

On no. line when we do a binary search, doing the bits of this no., the more the decimals i.e. more powerful datatype (64 instead of 32) the more accurate your no. is to the actual no. i.e. error range starts gettin smaller & smaller

∴ we can use this sys. to represent nos. on a map as well.

64 bits → { 32 bits for X-axis, 32 bits for Y-axis
a = error range in number stored here b = error range in no. stored here }

Error area = $a \times b = \boxed{a \times b}$ \rightarrow the square on which your loc' needs to lie

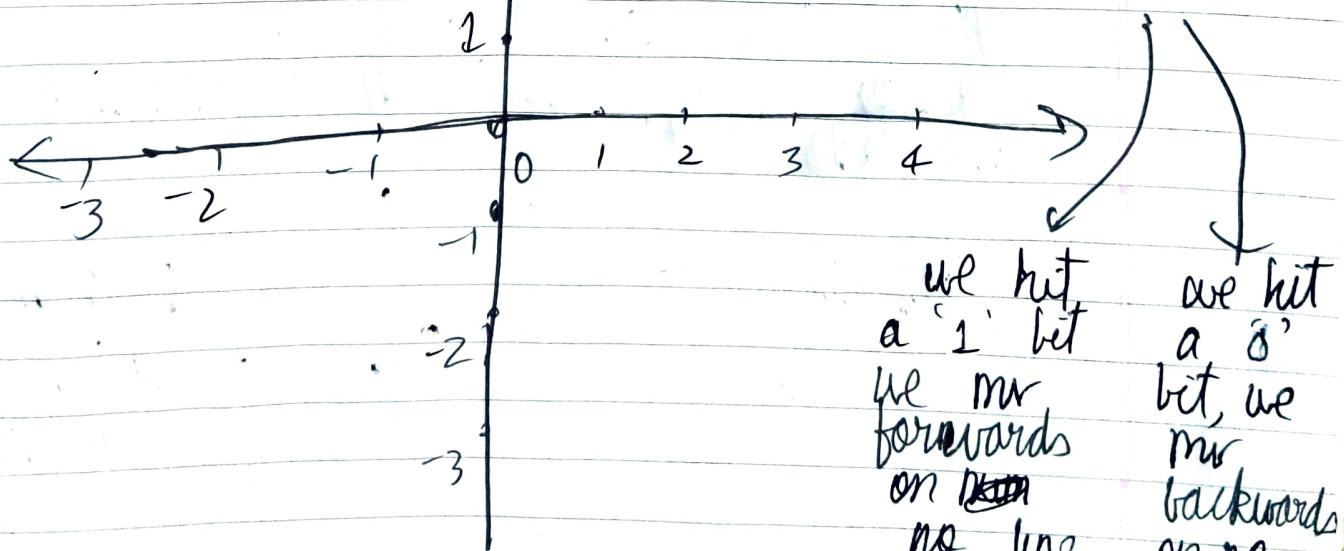
How to search for nos. in a 2-D plane

Now we hr. smartly assigned x, y coords to each pt s.t. if 2 pts are close their leading bits will match

e.g.: - if 2 pts ^{x-words} are represented as 110000 and 110001, wrt. they are quite close by in x-dir

Now pt looks like on a 2D plane

e.g.: $\rightarrow (10, 3)$ $\xrightarrow[\text{same logic}]{\text{X, Y accs are both no. lines}}$ so to locate a pt we start from MSB and move towards LSB s.t.



we hit a '1' bit
we move forwards on no. line.
we hit a '0' bit
we move backwards on no. line.

we get 1 of 4 movements in x, y dir' by reading bits simultaneously

32 bit no → 1st bit → sign → 0 for +ve
 8 bits → exponent
 23 bits → fracⁿ

Q: - MSB 32 bits → 32 decisions of ↑ ↓

10 → 000000.....0001010 2 moment
 3 → 000000.....0000111

$$(2^{31}-1, 2^{31})$$

In each such moment you ↓ by lots nos. and in the next step, you ↓ by exactly $\frac{1}{2}$ the value/nos.

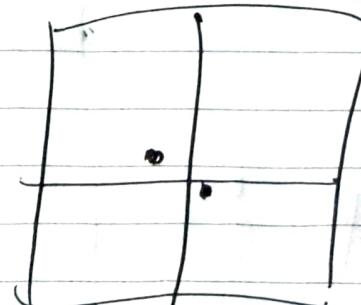
↓ after sometime

$$(2^{31}-1, 2^{31}-1)$$

$$(10, 3)$$

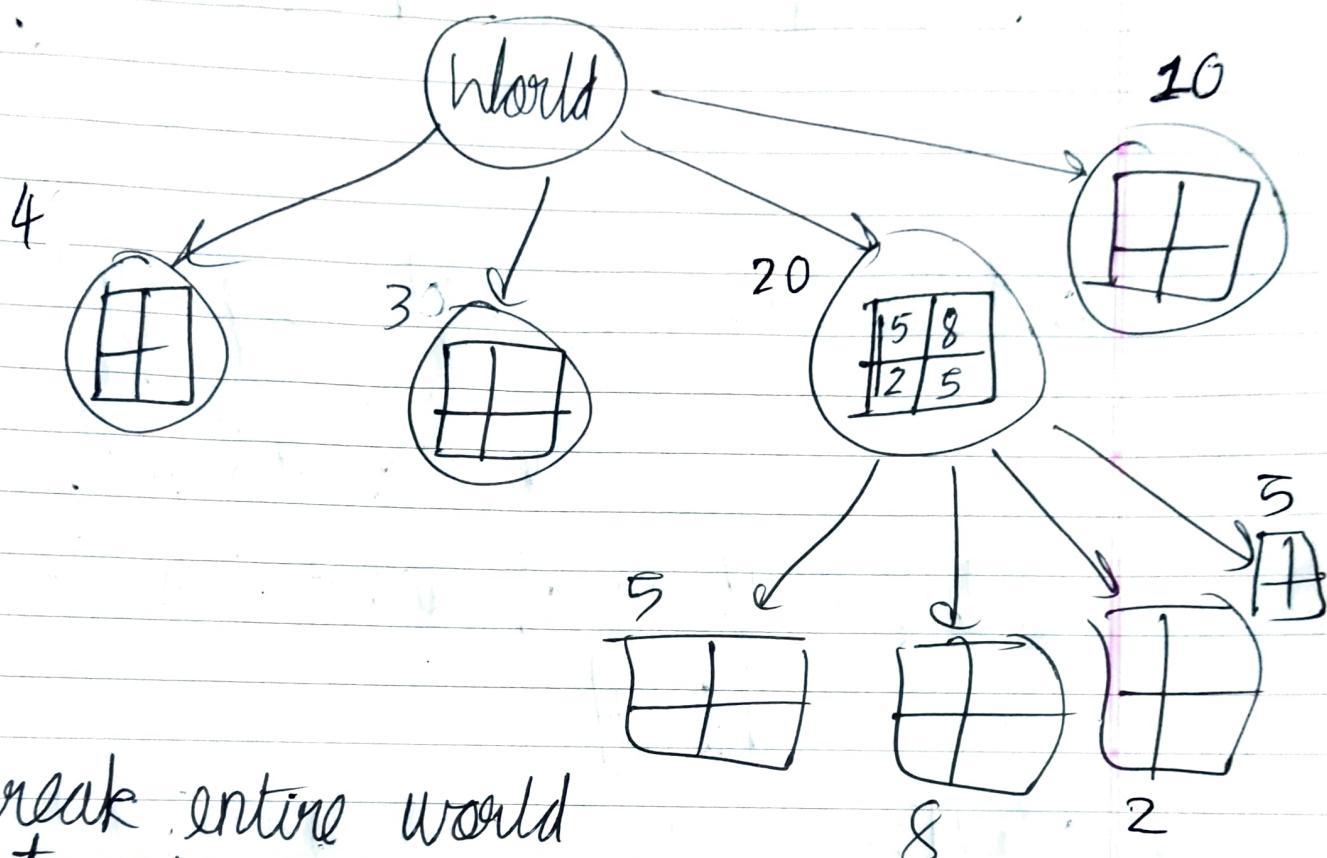
∴ If 2 pts have 1st 13 MSBs as same → then those nos. will be close by in this 2D version → preceding nos determine the quad we looking at

Case a



proximity is high but there's a mismatch

① Data Struct. 1 → Quad-tree



Break entire world

into regions → go as deep as app requires

Eg 1:- Resp breaking down till there's a 1 km radius "curr loca" places nearby

Eg 2:- can split even based on no. of loca's in a square. i.e. split of no. of loca's in a sq. is > 17

Problem → tree can be really skewed.

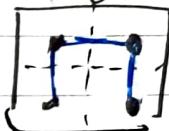
→ 2D plane → we don't have algos that are really efficient at finding which pts. lie in a range (range based query)

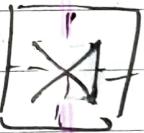
Range query can be done really well in 1-D plane (eg:- interval, segment trees)

$\log N$ T.C. for search

\therefore Our aim \rightarrow Convert 2-D planes' pts to be represented on a 1-D line so we can easily perform "range queries" on pts.

Soln \rightarrow Usage of Hilbert Curve (a fractal)

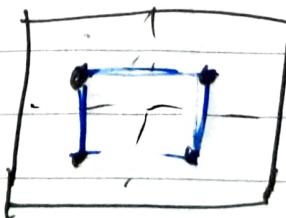


could've also used curves like  , 

but in Hilbert curve, len. of curve is min. so ~~change~~ chance of overlap is ~~also~~ during proximity calc. is also min (more proximity onto last)

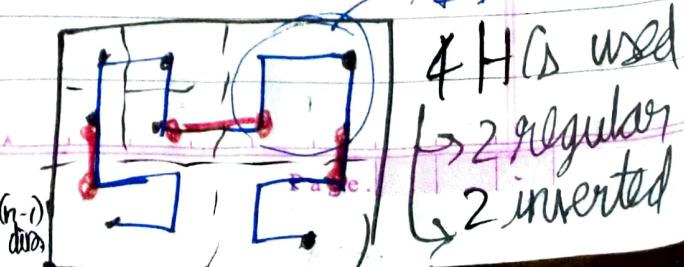
\therefore We can easily take all pts in 2-D plane and represent em all on a 1-D line ~~and~~ (our Hilbert curve) and

1D-HC } for a single grid
7 }
 }



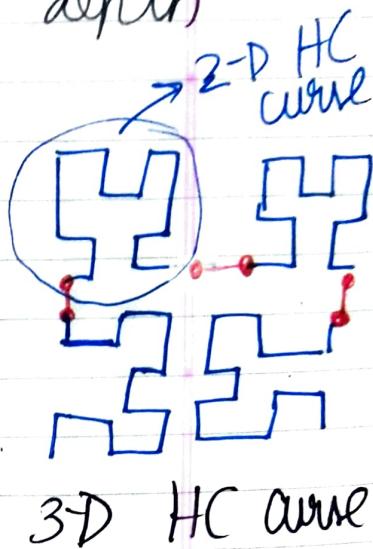
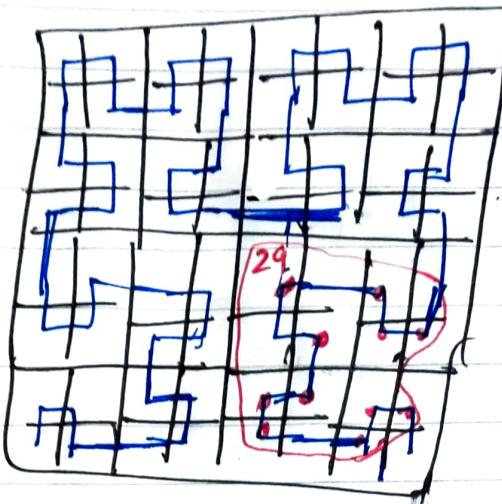
1 Hilbert curve(HC)
used

2D-HC } for a slightly complex
5 } grid / each time you
 } go a fractal dimension
 } deeper add & invert HCs of $(\frac{n}{2})$



∴ Now we get an infinitely recursive process (of representing 2D plane pts on 1D line) that can go to any arbitrary depth

Ex:- 3



∴ Recursive formula → ① Say you go n^{th} level deep

Caveat discussed earlier is also minimized as dim of HC ↑

② Use 4 curves of $(n-1)^{\text{th}}$ level → 2 regular → 2 inserted

③ Connect these 4 curves

3 really cool facts abt this kinda soln.

① It is a ^{2-D} space filling recursive curve

② It is scalably granular. (i.e. posⁿ of a pt. on a curve doesn't change much when ~~grid that the curve~~ curve dim ↑ i.e. grids are more finely divided)

③ Once you set a pt., you can do ± threshold to get all pts in close proximity