HW3

October 21, 2021

1 ouputs summary

```
****** Threshold for considering word as unknown is 2 ******

****** Vocabulary size 23183 ******

****** < unk > occurence count 20011 *******

***** Size of emission dictionary 30303 *****

****** Size of transition dictionary 1392 ******

GREEDY sentence wise accuracy 93.20391642320469

GREEDY word wise accuracy 93.51132293121243

VITERBI sentence wise accuracy 94.42883547709638

VITERBI word wise accuracy 94.76883613623946
```

```
[1]: import csv
import pandas as pd
from collections import defaultdict
import json
```

```
[2]: vocab = defaultdict(int)
                                                         # gives default value 0 tou
     \rightarrownew elements
     pos_freq = defaultdict(int)
     first tags = set()
     train_data = []
     pos_tags = []
     sentence = []
     sentences_count = 0
     with open('data/train', newline='') as csvfile: # read train file line by_
         spamreader = csv.reader(csvfile, delimiter='\t')
         for row in spamreader:
             try:
                 if len(sentence)==0:
                     first tags.add(row[2])
                 vocab[row[1].strip()]+=1
```

```
pos_freq[row[2].strip()]+=1
            sentence.append(row[1].strip())
                                                       # append words to a get a
 \rightarrowsentence
            pos_tags.append(row[2].strip())
                                                       # append pos tags to get !!
 →corresponding pos tags
        except:
            if len(row)>0:
                                                       # catch if a proper_
 → sentence had an error while reading
                print(row)
            sentences_count+=1
                                                        # count number of
 \rightarrow sentences
            train_data.append([sentences_count, sentence, pos_tags])
            sentence = []
                                                       # reset everything for
→ taking in next new sentence
            pos_tags = []
            # count sentences
            #use pos tags not words row[2]
    train_data.append([sentences_count, sentence,pos_tags])
train_df = pd.DataFrame(train_data,columns = ['sentence_number', 'words',__
```

[3]: train_df

```
[3]:
            sentence number
                                                                            words \
                              [Pierre, Vinken, ,, 61, years, old, ,, will, j...
                              [Mr., Vinken, is, chairman, of, Elsevier, N.V...
     1
     2
                             [Rudolph, Agnew, ,, 55, years, old, and, forme...
     3
                              [A, form, of, asbestos, once, used, to, make, ...
     4
                              [The, asbestos, fiber, ,, crocidolite, ,, is, ...
                              [After, San, Francisco, Mayor, Art, Agnos, spo...
     38213
                      38214
     38214
                      38215
                              [And, the, county, of, Los, Angeles, placed, i...
                              [Two, Los, Angeles, radio, stations, initiated...
     38215
                      38216
     38216
                      38217
                              [The, Los, Angeles, Red, Cross, sent, 2,480, c...
     38217
                      38217
                             [It, is, also, pulling, 20, people, out, of, P...
     0
            [NNP, NNP, ,, CD, NNS, JJ, ,, MD, VB, DT, NN, ...
            [NNP, NNP, VBZ, NN, IN, NNP, NNP, ,, DT, NNP, ...
     1
     2
            [NNP, NNP, ,, CD, NNS, JJ, CC, JJ, NN, IN, NNP...
            [DT, NN, IN, NN, RB, VBN, TO, VB, NNP, NN, NNS...
     3
     4
            [DT, NN, NN, ,, NN, ,, VBZ, RB, JJ, IN, PRP, V...
            [IN, NNP, NNP, NNP, NNP, VBD, IN, NN, IN,...
     38213
     38214
            [CC, DT, NN, IN, NNP, NNP, VBD, PRP$, NNS, CC,...
     38215
            [CD, NNP, NNP, NN, NNS, VBD, NNP, NNP, NN, NNS...
```

```
38217 [PRP, VBZ, RB, VBG, CD, NNS, IN, IN, NNP, NNP, ...
     [38218 rows x 3 columns]
\lceil 4 \rceil: thres = 1
     output text = "vocab.txt"
     res = sum(v if v <= thres else 0 for k, v in vocab.items())</pre>
                                                                  \# cound_{\square}
     → the number of words under threshold
     vocab = {key:val for key, val in vocab.items() if val > thres}
                                                                             #__
     → thresholding the vocabulary
     vocab = dict(sorted(vocab.items(), key=lambda x: x[1], reverse= True)) #__
     ⇒sorting the dictionary
     vocab = {'< unk >':res, **vocab}
                                                                      # appending <__
     \rightarrow unk > as the first elem of dictionary
     i=0
     with open('vocab.txt', 'w') as f:
         for k,v in vocab.items() :
             f.write("%s\t%s\n"%(k,i,v))
             #fix unknowns tags
     pos_freq["< * >"] = sentences_count
[5]: print("***** Threshold for considering word as unknown is 2 ******\n")
     print("***** Vocabulary size ",len(vocab),"*****\n")
     print("***** < unk > occurence count ",res, "******\n")
    ***** Threshold for considering word as unknown is 2 *****
    ***** Vocabulary size 23183 *****
    ***** < unk > occurence count 20011 ******
[6]: transition_cnt = defaultdict(float)
     emission_cnt = defaultdict(float)
     for idx, (_, words, pos_tags) in train_df.iterrows():
         prev = "< * >"
         for word, pos_tag in zip(words, pos_tags):
             try:
                 transition_cnt[(prev, pos_tag)] += 1  # insert (Prev_POS, POS)_
      → to dictionary or add count
```

38216 [DT, NNP, NNP, NNP, VBD, CD, NNS, ,, CD, ...

```
if word in vocab:
                     emission_cnt[(pos_tag, word)] += 1 # insert (POS, word) to;;
     \rightarrow dictionary or add count
                 else:
                                                             # if word has <
      → threshold occurrence
                     emission_cnt[(pos_tag,'< unk >')]+=1
                                                              # insert (POS,
     → <unk>) to dictionary or add count
                 prev = pos_tag
             except:
                 print("error bantu")
[7]: print(list(emission_cnt.items())[:10])
     print(list(transition_cnt.items())[:10])
    [(('NNP', 'Pierre'), 6.0), (('NNP', 'Vinken'), 2.0), ((',', ','), 46476.0),
    (('CD', '61'), 25.0), (('NNS', 'years'), 1130.0), (('JJ', 'old'), 213.0),
    (('MD', 'will'), 2962.0), (('VB', 'join'), 40.0), (('DT', 'the'), 39517.0),
    (('NN', 'board'), 297.0)]
    [(('< * >', 'NNP'), 7563.0), (('NNP', 'NNP'), 33139.0), (('NNP', ','), 12131.0),
    ((',', 'CD'), 987.0), (('CD', 'NNS'), 5502.0), (('NNS', 'JJ'), 995.0), (('JJ',
    ','), 1717.0), ((',', 'MD'), 490.0), (('MD', 'VB'), 7541.0), (('VB', 'DT'),
    5661.0)]
[8]: transition = defaultdict(float)
     emission = defaultdict(float)
     for key,value in transition_cnt.items():
         #transition[key] = (value +1) /(pos_freq[key[0]] + len(pos_freq))
         transition[key] = (value) /(pos_freq[key[0]])
     for key,value in emission_cnt.items():
         \#emission[key] = (value +1)/(pos\_freq[key[0]] + len(vocab))
         emission[key] = (value)/pos_freq[key[0]]
     print(list(emission.items())[:10])
     print(list(transition.items())[:10])
    [(('NNP', 'Pierre'), 6.84868961738654e-05), (('NNP', 'Vinken'),
    2.2828965391288468e-05), ((',', ','), 0.9999139414802065), (('CD', '61'),
    0.0007168253240050465), (('NNS', 'years'), 0.019530237301024905), (('JJ',
    'old'), 0.003613599348534202), (('MD', 'will'), 0.3138709335593939), (('VB',
    'join'), 0.0015693044058221193), (('DT', 'the'), 0.5016439225642653), (('NN',
    'board'), 0.0023287907538381922)]
    [(('< * >', 'NNP'), 0.1978962241934218), (('NNP', 'NNP'), 0.3782645420509543),
    (('NNP', ','), 0.13846908958086018), ((',', 'CD'), 0.021234939759036144),
    (('CD', 'NNS'), 0.15775891730703062), (('NNS', 'JJ'), 0.017196978862406887),
```

```
(('JJ', ','), 0.029129343105320303), ((',', 'MD'), 0.010542168674698794),
     (('MD', 'VB'), 0.7990886934407121), (('VB', 'DT'), 0.22209580603397544)]
 [9]: print("**** Size of emission dictionary ",len(emission),"*****\n")
      print("***** Size of transition dictionary ",len(transition),"*****\n")
     ***** Size of emission dictionary 30303 *****
     ***** Size of transition dictionary 1392 *****
[10]: transition str = dict((",".join(k), v) for k,v in transition.items())
      →converting to string keys for json file
      emission_str = dict((",".join(k), v) for k,v in emission.items())
                                                                                   #__
      →converting to string keys for json file
      hmm = {"transition": transition str, "emission": emission str}
      with open("hmm.json", "w") as outfile:
          json.dump(hmm, outfile)
[11]: dev_data = []
      sentence = []
      pos_tags = []
      sentence_count = 1
      with open('data/dev', newline = '') as tsvfile:
                                                                                  #__
       →read dev file line by line
          csv reader = csv.reader(tsvfile, delimiter = '\t')
          for row in csv reader:
              try:
                  sentence.append(row[1])
                  pos_tags.append(row[2])
              except:
                  dev_data.append([sentence_count, sentence, pos_tags])
                  sentence_count += 1
                  sentence = []
                  pos_tags = []
          dev_data.append([sentence_count, sentence,pos_tags])
      dev df = pd.DataFrame(dev data,columns = ['sentence number', 'words', |
      → 'pos_tags'])
      dev df
                                                                          words \
[11]:
            sentence_number
      0
                          1 [The, Arizona, Corporations, Commission, autho...
      1
                          2 [The, ruling, follows, a, host, of, problems, ...
      2
                          3 [The, Arizona, regulatory, ruling, calls, for,...
      3
                          4 [The, company, had, sought, increases, totalin...
      4
                          5 [The, decision, was, announced, after, trading...
```

```
[But, if, the, board, rejects, a, reduced, bid...
      5522
                        5523
      5523
                        5524
                               [The, pilots, could, play, hardball, by, notin...
      5524
                        5525
                               [If, they, were, to, insist, on, a, low, bid, ...
      5525
                               [Also, ,, because, UAL, Chairman, Stephen, Wol...
                        5526
      5526
                        5527
                               [That, could, cost, him, the, chance, to, infl...
                                                        pos_tags
             [DT, NNP, NNP, NNP, VBD, DT, CD, NN, NN, NN, I...
      0
      1
             [DT, NN, VBZ, DT, NN, IN, NNS, IN, NNP, NNP, ,...
      2
             [DT, NNP, JJ, NN, VBZ, IN, $, CD, CD, IN, JJ, ...
      3
             [DT, NN, VBD, VBN, NNS, VBG, $, CD, CD, ,, CC,...
      4
                             [DT, NN, VBD, VBN, IN, NN, VBD, .]
            [CC, IN, DT, NN, VBZ, DT, VBN, NN, CC, VBZ, TO...
      5522
            [DT, NNS, MD, VB, NN, IN, VBG, PRP, VBP, JJ, T...
      5523
      5524
            [IN, PRP, VBD, TO, VB, IN, DT, JJ, NN, IN, ,, ...
      5525
             [RB, ,, IN, NNP, NNP, NNP, CC, JJ, NNP, N...
      5526
            [DT, MD, VB, PRP, DT, NN, TO, VB, DT, NN, CC, ...
      [5527 rows x 3 columns]
[12]: import numpy as np
      import random
      def greedy_decoding(df):
            correct_matches = 0
             total\_words = 0
            with open('greedy.out', 'w') as tsvfile:
              prev_tag = '< * >'
                                                                     # start position tag_
       \rightarrow as prev tag
              predicted_tags = []
              sentence accuracies = []
              total_accuracy = 0
              total_correct = 0
              deno = 0
              num = 0
              small_no = 0.00000001
                                                                    # giving a very small_
       \rightarrowprobability to non existent proabilities to preserve matched emission /
       \hookrightarrow transition probabilities
              for idx, (_, words, pos_tags) in df.iterrows(): # loop through the_
       \rightarrow data
                                                                    # keep track of
                   predicted_tags = []
       →predicted_tags so far
```

start with prev tagu

prev_tag = '< * >'

→as star position tag

```
for word in words:
                                                         # go word by word in_
\rightarrow the sentence
              max_p = 0
                                                        # variable to keep
→ track of max probability seen so far
              best_tag = random.choice(list(first_tags)) # randomly_
→ choose a start POS tag
              for pos_tag in pos_freq.keys():
                                                        # check probabilties_
→ of each plausible tag
                   if word not in vocab:
                       word = '< unk >'
                                                        # qive < unk > 
→ frequency value for words not seen
                   if (prev_tag, pos_tag) in transition.keys() and (pos_tag,__
→word) in emission.keys():
                       p = (transition[(prev_tag, pos_tag)] +small_no) *__
elif (pos_tag, word) in emission.keys() :
                                                                   # if_{\square}
\rightarrowemission is found and transition is not matched
                       #p = (emission[(pos_tag, word)] ) * 1/
→ (pos_freq[pos_tag]+len(pos_freq)) # trying smoothing
                       p = ((emission[(pos_tag, word)] +small_no) * small_no)
                   elif (prev_tag, pos_tag) in transition.keys() : # if_
→transition exits and emission match isnt found
                       #p = (transition[(prev_taq, pos_taq)]) * 1/
→ (pos_freq[prev_taq]+len(vocab)) # trying laplace smoothing
                       p = ((transition[(prev_tag, pos_tag)]+small_no) *__
              # multiply by small probablity
⇒small no)
                   else:
                       #p = 1/(pos_freq[pos_taq]+len(pos_freq)) * 1/
\rightarrow (pos_freq[prev_tag]+len(vocab))
                      p = small no * small no
                                                                    # update
                   if p > max_p:
→best probability found
                          max_p = p
                          best_tag = pos_tag
               \#if \ max_p == 0:
               # best_tag = max(pos, key=pos.get)
               predicted_tags.append(best_tag)
                                                                   # add the
⇒best_found tag to the predicted tags list
```

```
prev_tag = best_tag
                                                                      # update_
 →prev tag as curr predicted tag
            correct_matches = np.sum(np.array(pos_tags) == np.
→array(predicted_tags)) # calculate number of tags correctly predicted
            total_correct += correct_matches
            deno +=len(pos_tags)
            accuracy = correct_matches/len(pos_tags)
            #print(accuracy)
            #print(pos_tags, predicted_tags)
            total_accuracy += accuracy
            num+=1
            sentence_accuracies.append(accuracy)
            predicted_tags.append(predicted_tags)
            for word, pos_tag in zip(words, predicted_tags):
                idx += 1
                print ("%d\t%s\t%s" % (idx, word, pos_tag), file=tsvfile)
            print ("", file=tsvfile)
        print(total_accuracy, num)
       print("GREEDY sentence wise accuracy", total_accuracy/num*100)
       print("GREEDY word wise accuracy", total_correct/deno*100)
greedy_decoding(dev_df)
```

5151.380460710523 5527 GREEDY sentence wise accuracy 93.20391642320469 GREEDY word wise accuracy 93.51132293121243

```
[16]: def viterbi_decoding(df):
        predicted_tags = []
                               # save the predicted tags
        sentence_accuracies = [] # append the sentence accuracies
        total_accuracy = 0  # add up total accuracy
        num = 0
                               # count number of sentences
        total correct = 0
        deno = 0
        small no = 0.00000001
        with open('viterbi.out', 'w') as tsvfile:
                                                        # open the .out file
            for idx, (_, words, pos_tags) in df.iterrows(): # read the df line__
      \hookrightarrow by line
                  predicted_tags = []
                                                        # reset for every
      →new sentence
                  T = len(words)
```

```
N = len(pos_freq.items())
               viterbi = [[0]*(T) for _ in range(N)]
               path_tracker = [[0]*(T) for _ in range(N)]
               for i in range(0,len(path_tracker)):
                  path_tracker[i][0] = -1
               for t, word in enumerate(words): # for each timestamp_
\rightarrow, word in words
                  if word not in vocab:
                                                         # if word is not in_
\rightarrow vocab give it < unk > tag
                       word = '< unk >'
                  for s1, pos tag in enumerate(pos freq.keys()): # for___
→ every state, current tag
                       if pos_tag == '< * >':
                          pass
                       elif t == 0:
                                                            # handle first
→word separately
                          if ('< * >', pos_tag) in transition.keys() and__
viterbi[s1][0] = (transition[('< * >',__
→pos_tag)]+small_no) * (emission[(pos_tag, word)]+small_no)
                              path tracker[s1][0] = -1 # to track end_1
→when backtracking to find the path
                       else:
                          for s2, prev_tag in enumerate(pos_freq.keys()): #__
→ for every possible prev state, prev tag
                              if prev tag == '< * >':
                                                                          #
\rightarrow ignore start symbol tag
                                  pass
                              elif (prev_tag, pos_tag) in transition.keys()__
→and (pos_tag, word) in emission.keys():
                                  p = viterbi[s2][t-1]*_{\sqcup}
→(transition[(prev_tag, pos_tag)]+small_no) * (emission[(pos_tag, __
→word)]+small no)
                                                                      # save
                                  if p > viterbi[s1][t]:
→ the best transition probability in the the viterbi table
                                      viterbi[s1][t] = p
                                      path_tracker[s1][t] = s2 # save_
→best prev pos in this path
               best_path_p = 0
               best_path_index = 0
               for i in range(N):
                                                                       # find_
→ the best path start by looking at the last column in viterbi table
                   if viterbi[i][T-1] > best_path_p:
                      best_path_p = viterbi[i][T-1]
```

```
best_path_index = i
                best_path = []
                t = T-1
                pos_list = list(pos_freq.keys())
                while best_path_index != -1 and t!=-1:
    # backtrack to find the path that gave the best probability
                    best_path.append(pos_list[best_path_index])
                    #print("index", best_path_index)
                    best_path_index = path_tracker[best_path_index][t]
                    t -= 1
                if len(best_path) == 0:
                    print("best path not found")
                best_path = best_path[::-1]
                                                                          #__
 →reverse the best path tags found by backtracking
                correct_matches = np.sum(np.array(pos_tags) == np.
→array(best_path)) # count correct matches for accuracy calculations
                total_correct += correct_matches
                deno+=len(pos tags)
                accuracy = correct_matches/len(pos_tags)
                sentence accuracies.append(accuracy)
                predicted_tags.append(best_path)
                total_accuracy += accuracy
                n_{11}m+=1
                idx = 0
                for word, pos_tag in zip(words, best_path):
                    idx += 1
                    print ("%d\t%s\t%s" % (idx, word, pos_tag), file=tsvfile)
                print ("", file=tsvfile)
    print("VITERBI sentence wise accuracy", total_accuracy/num*100)
    print("VITERBI word wise accuracy ", total_correct/deno*100)
viterbi_decoding(dev_df)
```

VITERBI sentence wise accuracy 94.42883547709638 VITERBI word wise accuracy 94.76883613623946

```
[17]: test_data = []
sentence = []
pos_tags = []
```

```
sentence count = 1
      with open('data/test', newline = '') as tsvfile:
                                                                                     #__
       →read test file line by line
          csv_reader = csv.reader(tsvfile, delimiter = '\t')
                                                                                     #__
       ⇒create sentences df like train data
          for row in csv_reader:
              try:
                  sentence.append(row[1])
              except Exception as e:
                  test_data.append([sentence_count, sentence])
                  sentence count += 1
                  sentence = []
                  pos_tags = []
          test_data.append([sentence_count, sentence])
      test_df = pd.DataFrame(test_data,columns = ['sentence_number', 'words'])
      test_df
[17]:
            sentence number
                                                                            words
      0
                           1 [Influential, members, of, the, House, Ways, a...
      1
                           2 [The, bill, ,, whose, backers, include, Chairm...
                           3 [The, bill, intends, to, restrict, the, RTC, t...
      2
      3
                           4 ['`, Such, agency, ', self-help, ', borrowing,...
                          5 [The, complex, financing, plan, in, the, S&L, ...
      5457
                       5458 [Says, Peter, Mokaba, ,, president, of, the, S...
      5458
                       5459 [They, never, considered, themselves, to, be, ...
                              [At, last, night, 's, rally, ,, they, called, ...
      5459
                       5460
      5460
                       5461 [``, We, emphasize, discipline, because, we, k...
                       5462 ['`, We, want, to, see, Nelson, Mandela, and, ...
      5461
      [5462 rows x 2 columns]
[18]: import numpy as np
      import random
      def greedy_decoding_test(df):
            with open('greedy.out', 'w') as tsvfile:
              prev_tag = '< * >'
                                                                   # start position tag_
       \rightarrow as prev tag
```

predicted_tags = []
sentence_accuracies = []

total accuracy = 0

```
small_no = 0.0000001
                                                            # qiving a very small_
\rightarrowprobability to non existent proabilities to preserve matched emission /_{\sqcup}
\hookrightarrow transition probabilities
       for idx, (_, words) in df.iterrows(): # loop through the data
           predicted tags = []
                                                            # keep track of
\rightarrowpredicted_tags so far
           prev_tag = '< * >'
                                                            # start with prev tag_
\rightarrowas star position tag
           for word in words:
                                                            # go word by word in
\rightarrow the sentence
               max_p = 0
                                                            # variable to keep_
→track of max probability seen so far
               best_tag = random.choice(list(first_tags))
                                                                  # randomly
→ choose a start POS tag
               for pos_tag in pos_freq.keys():
                                                   # check probabilties_
→ of each plausible tag
                    if word not in vocab:
                        word = '< unk >'
                                                            # qive < unk >
→ frequency value for words not seen
                    if (prev_tag, pos_tag) in transition.keys() and (pos_tag, __
→word) in emission.keys():
                        p = (transition[(prev_tag, pos_tag)]+small_no) *__
→(emission[(pos_tag, word)]+small_no)
                    elif (pos_tag, word) in emission.keys() :
                                                                       # if_{\square}
→emission is found and transition is not matched
                        p = (emission[(pos_tag, word)] + small_no) * small_no
                    elif (prev tag, pos tag) in transition.keys(): # if exits
→ and emission match isnt found
                       p = (transition[(prev_tag, pos_tag)]+ small_no) * __
\hookrightarrowsmall_no
                        p = small_no * small_no
                    if p > max_p:
                                                                          # update
\rightarrow best probability found
                            max_p = p
                            best_tag = pos_tag
               predicted_tags.append(best_tag)
                                                                          # add
→ the best found tag to the predicted tags list
```

```
prev_tag = best_tag  # update

prev tag as curr predicted tag

predicted_tags.append(predicted_tags)
    idx = 0
    for word, pos_tag in zip(words, predicted_tags):
        idx += 1
        print ("%d\t%s\t%s" % (idx, word, pos_tag), file=tsvfile)
    print ("", file=tsvfile)

greedy_decoding_test(test_df)
```

```
[20]: def viterbi_decoding_test(df):
          prev_tag= '< * >'
                                     # start position tag as prev tag
          predicted_tags = [] # save the predicted tags
          sentence_accuracies = [] # append the sentence accuracies
          total_accuracy = 0
          num = 0
          small_no = 0.00000001
                                                               # open the .out file
          with open('viterbi.out', 'w') as tsvfile:
   for idx, (_, words) in df.iterrows():
                                                                  # read the df line_
       \rightarrowby line
                       predicted tags = []
                       T = len(words)
                       N = len(pos_freq.items())
                       viterbi = [[0]*(T) for _ in range(N)]
                       path_tracker = [[0]*(T) for _ in range(N)]
                       for i in range(0,len(path_tracker)):
                           path_tracker[i][0] = -1
                       for t, word in enumerate(words): # for each timestamp u
       \hookrightarrow, word in words
                           if word not in vocab:
                                                                   # if word is not in_
       \rightarrow vocab give it < unk > tag
                               word = '< unk >'
                           for s1, pos_tag in enumerate(pos_freq.keys()): # for_
       → every state, current tag
                               if pos_tag == '< * >':
                                   pass
                               elif t == 0:
                                                                       # handle first_
       \rightarrow word separately
```

```
if ('< * >', pos_tag) in transition.keys() and__
→ (pos_tag, word) in emission.keys():
                               viterbi[s1][0] = (transition[('< * >',__
→pos_tag)] +small_no) * (emission[(pos_tag, word)]+small_no)
                               path_tracker[s1][0] = -1 # to track end__
→when backtracking to find the path
                       else:
                           for s2, prev_tag in enumerate(pos_freq.keys()): #__
→ for every possible prev state, prev tag
                               if prev_tag == '< * >':
                                                                            #__
\rightarrow ignore start symbol tag
                                   pass
                               elif (prev_tag, pos_tag) in transition.keys()__
→and (pos_tag, word) in emission.keys():
                                   p = viterbi[s2][t-1]*(transition[(prev_tag,__
→pos_tag)]+small_no) * (emission[(pos_tag, word)]+small_no)
                                   if p > viterbi[s1][t]:
                                                                         # save
→ the best transition probability in the the viterbi table
                                       viterbi[s1][t] = p
                                       path_tracker[s1][t] = s2
                                                                        # save
→best prev pos in this path
               best_path_p = 0
               best_path_index = 0
               for i in range(N):
                                                                         # find
the best path start by looking at the last column in viterbi table
                   if viterbi[i][T-1] > best_path_p:
                       best_path_p = viterbi[i][T-1]
                       best_path_index = i
               best_path = []
               t = T-1
               pos_list = list(pos_freq.keys())
               while best path index !=-1 and t!=-1:
   # backtrack to find the path that gave the best probability
                   best_path.append(pos_list[best_path_index])
                   best_path_index = path_tracker[best_path_index][t]
                   t -= 1
               if len(best_path) != len(words) :
                   print("best path not found")
               best path = best path[::-1]
                                                                         #__
→reverse the best path tags found by backtracking
```

```
idx = 0
for word, pos_tag in zip(words, best_path):
    idx += 1
    print ("%d\t%s\t%s" % (idx, word, pos_tag), file=tsvfile)
    print ("", file=tsvfile)
viterbi_decoding_test(test_df)
```

[]: