#### **Chapter 1 checkpoint!**

Hello and welcome to your first checkpoint! Here come six questions, one about each of the learning targets from Chapter 1. This is your scorecard:

Learning target:	P1	P2	L1	L2	L3	L4
Your confidence level						
before starting (0-5):						
Your confidence level						
after the quiz (0-5):						
The mark you earned	Success!	Success!	Success!	Success!	Success!	Success!
	Revise!	Revise!	Revise!	Revise!	Revise!	Revise!
on this attempt:	Try again!					

Before anything else, please do the following:

- Rank your confidence from 0-5 on each of the learning targets. 5 means "I could teach a whole class about this;" 0 means "I am genuinely not sure I have heard these words before."
- Rip all the pages apart.
- Write your name on this page and on each of the other pages of the quiz.

Then do the quiz! Some reminders:

- Open notes, closed computer.
- If you need more room to write, use the back of the same learning target page, or ask me for some scratch paper.
- Read the questions carefully and make sure you're answering each part.
- Show all your work and explain all your thinking!

When you are done:

- Rank your confidence from 0-5 on each of the learning targets. 5 means "I absolutely nailed that question for sure;" 0 means "oof, I definitely didn't get that one."
- Make double sure your name is on every page, including any scratch paper.
- Hand in your work, separated by learning target.

Have fun and do your best! I believe in u ♡

#### Learning target P1, version 1

Consider the following proposition:

For all natural numbers n, if  $n^2$  is even, then n is even.

Is the following claimed proof valid? Use Toulmin analysis to decide.

*Proof.* Consider any  $n \in \mathbb{N}$ . Assume that  $n^2$  is even.

By definition,  $n^2 = 2k$  for some  $k \in \mathbb{N}$ .

Let's take square roots of each side giving us  $\sqrt{n^2} = \sqrt{2k}$ .

Simplifying,  $n = \sqrt{2k}$ .

Multiplying by 2 top and bottom inside the square root,  $n = \sqrt{\frac{2 \cdot 2k}{2}}$ .

So, 
$$n = \sqrt{\frac{4 \cdot k}{2}}$$
.

Pulling 4 out of the square root,  $n = 2 \cdot \sqrt{\frac{k}{2}}$ .

Let 
$$m = \sqrt{\frac{k}{2}}$$
.

Thus n = 2m.

Therefore, n is an even number.

So, our theorem is proved.

#### Learning target P2, version 1

The following definitions are extremely made up and don't mean anything (but they look fun!).

**Definition**: A function is *viscous* if its geodesic curvature  $\gamma(f)$  is nonzero.

**Definition**: A function is *laminar* if its intrinsic cofunction  $\tilde{f}$  is differentiable.

Consider the following proposition: Every laminar function is viscous.

1. Write a proof framework for a *direct* proof of this proposition.

2. Write a proof framework for a proof by contrapositive.

3. Write a proof framework for a *proof by contradiction*.

4. (Bonus!) If for some reason you did not believe this proposition was true (and thus that none of these proof frameworks is appropriate), how would you show it?

## Learning target L1, version 1

Consider these two very similar-looking statements:

$$\exists x \in \mathbb{Z} \ \forall y \in \mathbb{Z}, x + y = 0$$

$$\forall y \in \mathbb{Z} \ \exists x \in \mathbb{Z}, x + y = 0$$

1. Translate both statements into human words.

2. Precisely one of these two statements is true. Which is it, and why? (Moral: the order of quantifiers is super important.)

#### Learning target L2, version 1

Write each of the following statements in "if..., then ..." form. (Note that some of them are true and some of them are not.)

- 1. Every continuous function is differentiable.
- 2. A shape is a square only if it is a rectangle.
- 3. Cooking is necessary for eating salmon.
- 4. All dogs go to heaven.
- 5. (The converse of "all dogs go to heaven".)
- 6. (The inverse of "all dogs go to heaven".)
- 7. (The contrapositive of "all dogs go to heaven".)

## Learning target L3, version 1

Simplify each of the following:

1. 
$$\neg (P \rightarrow Q)$$

2. The negation of the **converse** of  $P \rightarrow Q$ 

3. 
$$\neg((P \rightarrow Q) \lor (Q \rightarrow P))$$

4. 
$$\neg \exists x \forall y (\neg O(x) \lor E(y))$$
.

### Learning target L4, version 1

I wonder how the implication sign distributes over the logical connectives  $\vee$  and  $\wedge$ .

1. Are the statements  $P \to (Q \lor R)$  and  $(P \to Q) \lor (P \to R)$  logically equivalent? Use a truth table to decide.

2. What about the statements  $P \to (Q \land R)$  and  $(P \to Q) \land (P \to R)$ ? Make another truth table.

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# Learning target G1, version 1

Fill in the blank boxes.

A	djacency table	Vertex set and edge set	Drawing
vertex	adjacent to		
$\overline{a}$	b, d		
b	$\begin{vmatrix} a, c, d, e, f \\ b, g \end{vmatrix}$		
c	b, g		
d	a, b, e		
e	b, d, f		
f	b, e, g		
g	c, f		

## Learning target G2, version 1

Two of the graphs on the previous page are isomorphic.

- 1. Figure out which two,
- 2. provide a relabeling between them,
- 3. and convince me that the relabeling respects the edges.