

Workbook for

JUST ENOUGH ALGEBRA

Dr. Suzanne Dorée
Professor of Mathematics
Augsburg College

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Chapter 1

Practice exercises for Variables

1.1 Variables and functions

1. A 32 pound bag of dog food costs \$29.97, but a 8 pound bag costs \$11.28.

(a) Identify and name the variables, including the units.

price

(b) Which is dependent and which is independent?

price

(c) What might a 16 pound bag of dog food cost? Explain the reasoning behind your guess.

2. Rent in the Riverside Neighborhood is expected to increase 7.2% each year. Average rent for an apartment is currently \$830 per month. *Story also appears in 3.4 #3*

(a) Identify and name the variables, including the units.

(b) Explain the dependence using a sentence of the form “___ is a function of ___”

(c) Which number is a constant in this story: the percent increase (7.2) or the apartment rent (830)?

(d) What is the average rent expected to be in 1 year? In 2 years? In 3 years? Note that

$$7.2\% = \frac{7.2}{100} = 7.2 \div 100 = .072$$

Try figuring it out.

3. Round each number to the precision indicated.

For a discussion of rounding, see Prelude: approximation

- (a) My calculations show I'll need a cross brace around 9.388 feet long. I don't want to buy a board that's too short, so round up to the nearest foot.

odd
example

- (b) Gas mileage is usually rounded down to the nearest one decimal place. What is the gas mileage for a car measured as getting 42.812 miles per gallon? What about a car getting 23.09 miles per gallon?

8-2

- (c) The original budget estimates for the new community center addition were rounded to the nearest hundred (that means ending in 00), so we want to round our bid of \$148,214.79 to the nearest hundred.

- (d) The population estimate was 4.2 million people, but revised estimates suggests 4,908,229 people. Report the revised estimate rounded appropriately.

4. It's about time! In each story, time is one (or both) of the variables. Identify name the variables, including units and dependence. *Stories also appear in 1.1 #5*

(a) The Nussbaums planted a walnut tree years ago when they first bought their house. The tree was 5 feet tall then and has grown around 2 feet a year.

(b) After his first beer, Stephen's blood alcohol content (BAC) was already .04 and as he continued to drink, his BAC level rose 45% per hour.

Story also appears in 2.4 #11 and 3.4 #1

(c) If McKenna drives 60 mph (miles per hour), it takes her 20 minutes on the highway to get between exits, but when traffic is bad it can take her an hour.

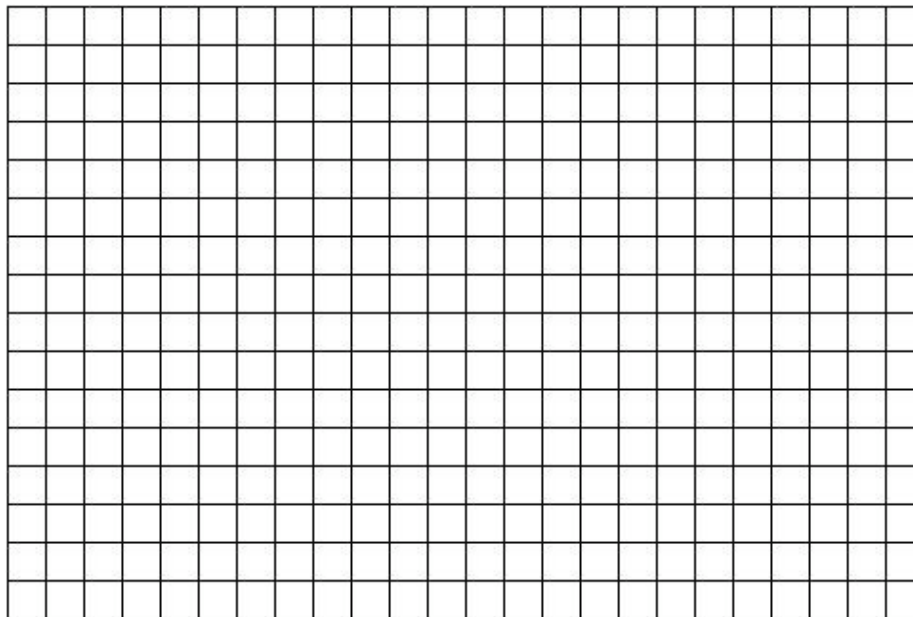
(d) The sun set at 6:00 p.m. today and I heard on the radio that it sets about 2 minutes earlier each day this time of year. *Hint: measure the sunset time in minutes after 6:00 p.m.*

1.2 Tables and graphs

1. My grandfather had \$200 in savings bonds that matured in 1962 when he gave them to me. The bonds continue to earn interest at a fixed rate so I have yet to cash them in. The table shows some values. *Story also appears in 5.3 #1*

year	1962	1970	1980	1990	2000	2010
Y	0	8	18	28	38	48
B	200.00	318.77	570.87	1,022.34	1,830.85	3,278.77

- (a) What do Y and B stand for? Include the units and dependence.
- (b) What were the savings bonds worth in 1970?
- (c) When were the savings bonds worth \$1,022.34?
- (d) Approximately when were the savings bonds worth \$1,500?
- (e) What do you expect the savings bonds will be worth in 2020?
- (f) Graph the function using the information given in the table.



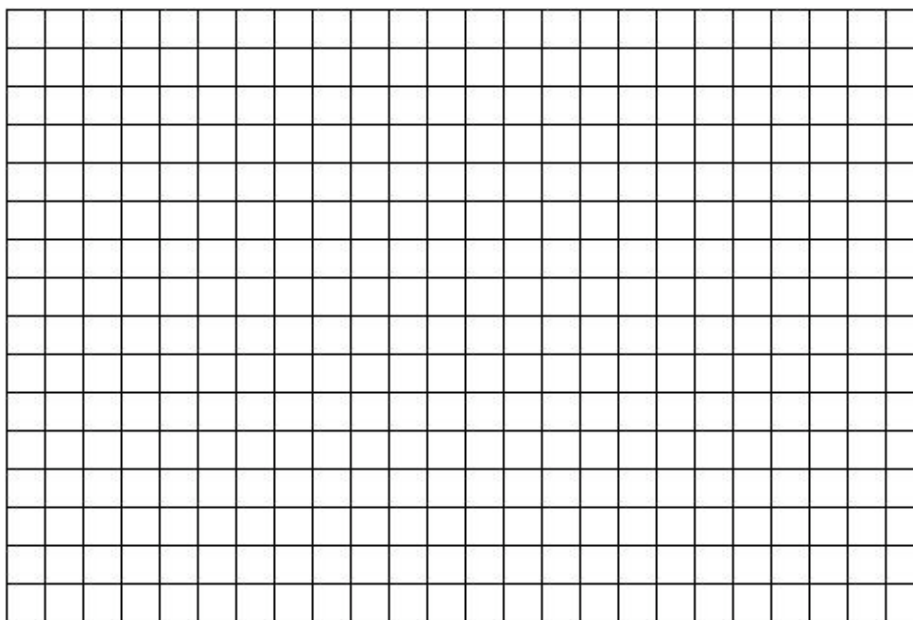
- (g) Use the graph to check your answers to the questions.

2. How cold is it? It's not just the air temperature, but also the wind, that governs how cold it feels outside. At an air temperature of 10°F with no wind it feels like an honest 10°F . Cold but manageable. But add a 30 miles per hour wind and brrr, it feels like it's -12°F (12 below zero). We say the “wind chill” of 10°F with a 30 mph wind is -12°F . The table lists the wind chill at 10°F for various wind speeds.

Wind (mph)	0	5	10	15	20	25	30	35	40	45	50	55	60
Wind chill ($^{\circ}\text{F}$)	10	1	-4	-7	-9	-11	-12	-14	-15	-16	-17	-18	-19

Source: National Weather Service *Story also appears in 2.1 #10*

- (a) At an air temperature of 10°F with a 20 mph wind, what's the wind chill?
- (b) A “cold advisory” is issued whenever the wind chill falls below 0°F . How fast does the wind need to be at an air temperature of 10°F to issue a cold advisory?
- (c) Between a wind chill of 0°F and -15°F , schools in our district are open but kids can't go outside for recess. What's the corresponding range of wind speeds at an air temperature of 10°F ?
- (d) Draw a graph showing how wind chill depends on wind speed and use it to check your answers. Extend the vertical axis both above and below the horizontal axis so you can scale for the negative numbers.

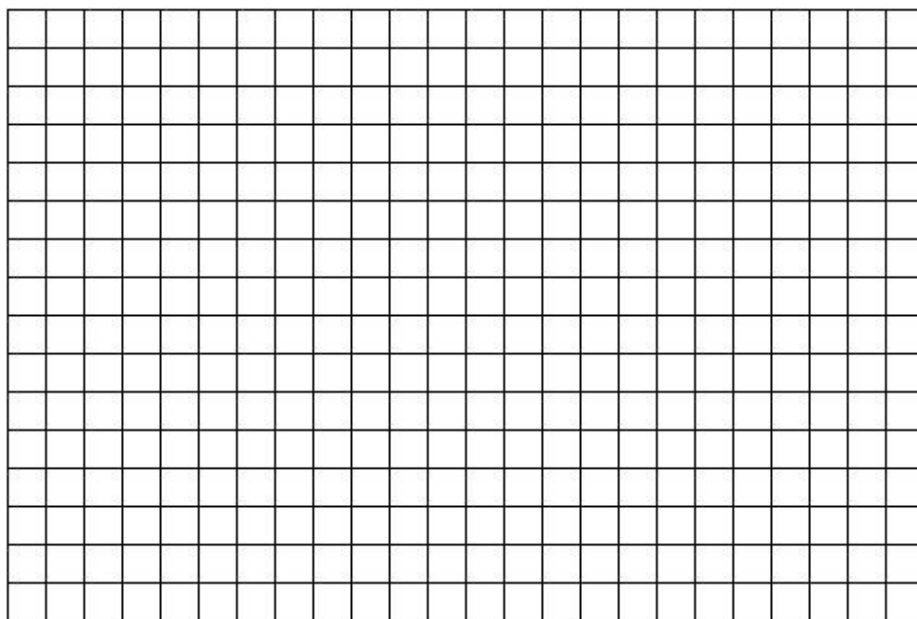


3. Anthony and Christina are trying to decide where to hold their wedding reception. The Metropolitan Club costs \$1,300 down and \$92 per person.

2 m a y h c

Σ Story also appears in 1.3 #2 and 3.2 #3

- Identify and name the variables, including units.
- Explain the dependence using a sentence of the form “___ is a function of ___”
- Make a table of showing the cost for 20, 50, 75, 100, or 150 people.
- If Tony and Tina’s budget is \$8,000, how many people can they invite to their wedding reception? Give a rough estimate from your table.
- Graph the function.



- Does your estimate agree with your graph? If not, revise.
- Can you figure out from the story exactly how many guests Tony and Tina can invite to their wedding reception and stay within their \$8,000 budget?

4. A mug of coffee costs \$3.45 at Juan's favorite cafe.

Story also appears in 2.1 #4 and 4.2 #2

13-1

- (a) Juan buys coffee on the way to work everyday for a month. Let's say that's 22 workdays. What does that cost?

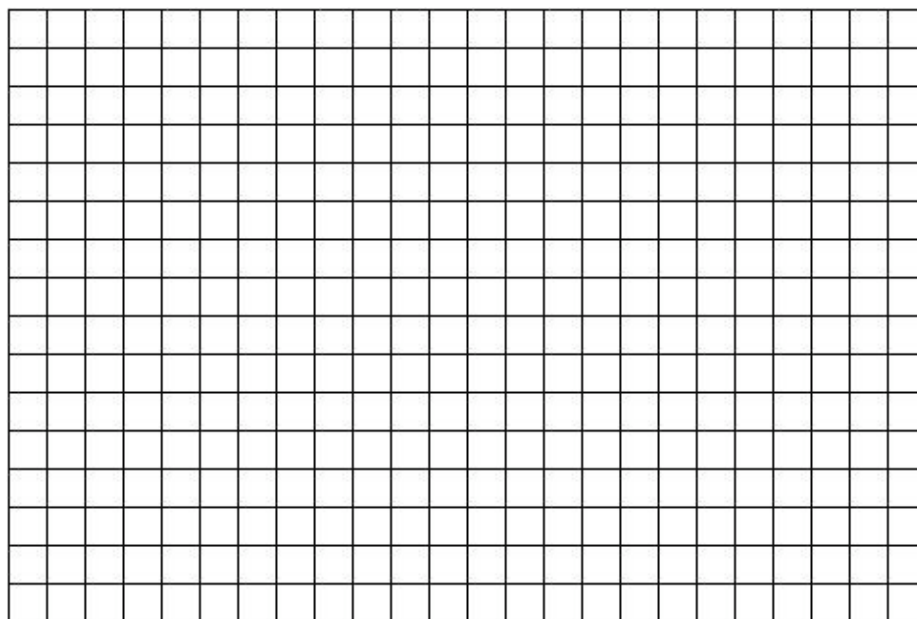
- (b) If Juan buys a discount card for \$10, then a mug costs \$2.90 instead. What will it cost Juan for a month if he buys the card? Include that \$10 in the cost.

- (c) Does the card pay for itself within the month? That means, is the total with the card (including the \$10 for the card) less than the total without the card?

- (d) Complete the table, where M is the number of mugs of coffee Juan buys and T is the total cost, in dollars.

M	0	10	22	50
T (regular)				
T (with card)				

- (e) Draw a graph illustrating both functions.



- (f) What does the point where the two lines cross mean in terms of the story?

This is a bit messy

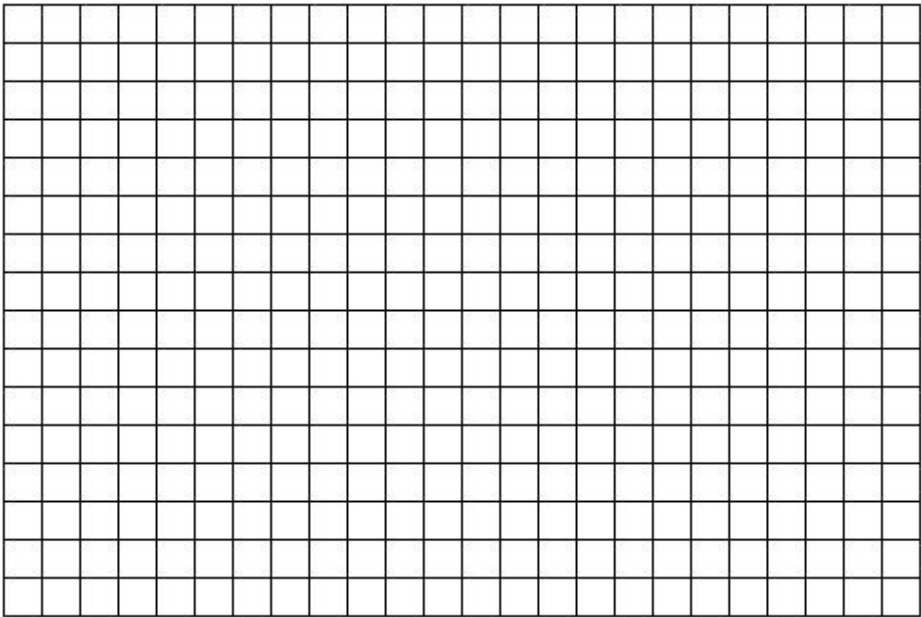
1.3 Rate of change

1. Sweet Rose Bakery makes sheet cakes and cupcakes. Here are their price sheets.

Serves	10	20	50		Serves	12	24	48
Cake (\$)	11.95	19.95	40.95		Cupcakes (\$)	6.95	13.90	27.80

- (a) Calculate the rate of change for cake prices, in \$/person, if there are between 10 and 20 people. Repeat for between 20 and 50 people.
- (b) Calculate the rate of change for cupcake prices, in \$/person, if there are between 12 and 24 people. Repeat for between 24 and 48 people.
- (c) Draw a graph showing both options. Connect each curve smoothly.

14-1



- (d) What about the cupcake graph confirms that the rate of change for cupcakes is constant? Any idea why it is constant?
- (e) What about the sheet cake graph confirms that the rate of change for cakes is not constant? Any idea why it is not constant?



2. Anthony and Christina are trying to decide where to hold their wedding reception. The Metropolitan Club costs \$1,300 down and \$92 per person.

Story also appears in 1.2 #3 and 3.2 #3

- (a) Make a table showing the cost for 20, 50, 75, or 100 people.

- (b) Calculate the extra cost for each additional person between 20 and 50 people.

- (c) Calculate the extra cost for each additional person between 75 and 100 people.

- (d) What do you notice?

- (e) Explain why the graph of this cost function is a line.

- (f) Is the cost function increasing, decreasing, or neither?

3. Rashad measured his heart rate several times after football practice, while he was cooling down. Right after practice his heart rate was 178 beats per minute. Two minutes later, it had dropped to 153 beats per minute, and by ten minutes after practice had ended it was down to 120 beats per minute.
- (a) Make a table showing how Rashad's heart rate changed.
 - (b) Identify the variables, including units and dependence.
 - (c) How quickly was Rashad's heart rate dropping during the first two minutes following practice? *Hint: the units are beats per minute per minute. Looks funny, but that's what it is.*
 - (d) How quickly was his heart rate dropping during the next time period?
 - (e) Rashad does not like hitting the showers until his heart rate is closer to normal, or at least below 100. He usually waits 15 minutes after practice. Do you think that's long enough? Explain.
 - (f) Did Rashad's heart rate increase, decrease, or neither?

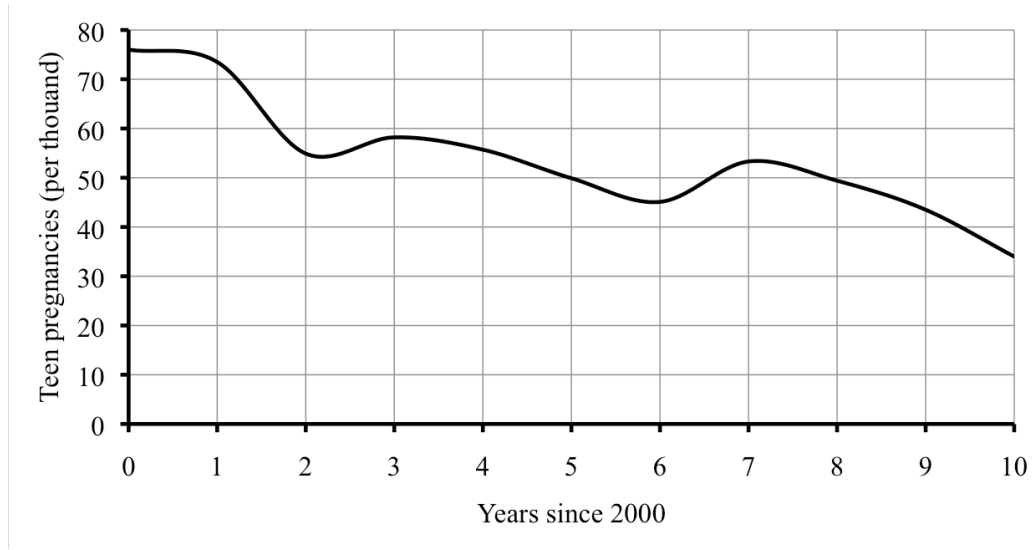
1.3. RATE OF CHANGE

births per

17

4. Teen pregnancy rates for Minneapolis (per thousand teens) are summarized in the graph and table. Minnesota Department of Health

Year	1999	2000	2001	2002	2003	2004	2005	2006	2007	2008	2009
Teen preg	76.0	73.5	54.9	58.2	55.7	49.9	45.1	53.3	49.4	43.5	34.0



- (a) What was the teen pregnancy rate (per thousand teens) in 2003?
- between 2002 + 2003?
- (b) Did the teen pregnancy rate increase or decrease in 2003?
- (c) The teen pregnancy rate has usually been decreasing, but during a couple of years it actually increased. Which years were those?
- (d) When did the teen pregnancy rate first fall below 60 (per thousand teens)?
- (e) How fast was the teen pregnancy rate dropping between 2002 and 2005? How does that compare to 2006 to 2009?

1.4 Units

1. (a) Compare centimeters (cm) and inches, using that $1 \text{ inch} \approx 2.54 \text{ cm}$
 - i. Which is longer: 1 inch or 1 centimeter?
 - ii. Kamari is shopping at an internationally-based retail store. She's looking at a curtain rod that will project 10 cm from the wall. What is that in inches?
 - iii. She also wants a basket to fit on her bookcase, so no more than 1 foot wide or deep. How many cm are in a foot?
- (b) Compare meters (m) and yards using that $1 \text{ yard} \approx .9144 \text{ m}$
 - i. Which is longer: 1 yard or 1 meter?
 - ii. Princeton was watching the Olympics and noticed everything was measured in meters. He's curious how long a football field (100 yards) is in meters.
 - iii. Kamari found a really big bath towel she likes. It's 1 meter wide and 1.5 meters long. What are the dimensions in inches? Use that $1 \text{ yard} = 3 \text{ feet}$.
- (c) Compare kilometers (km) and miles using that $1 \text{ mile} \approx 1.609 \text{ km}$
 - i. Which is longer: 1 mile or 1 kilometer?
 - ii. This weekend Princeton and Kamari are doing a 5K run. How many miles long is that? Note: **5K** is short for 5 kilometers.
 - iii. Princeton is actually in training for a marathon. How many kilometers is that? Note: a **marathon** is approximately 26.2 miles.

-
2. (a) Yesterday Cameron worked for 2 hours and 15 minutes (that's 2:15) and then went home and studied for 7 hours and 57 minutes (that's 7:57). Convert each time into decimal hours.
- (b) Ephriam works at a plant that produces very delicate electronic switches. He measured the lifetime for one switch at 4.18 hours. Another had lifetime 19.50 hours. Convert each time into hours and minutes. *That means H:MM format.*
- (c) Phillip measured his office using a digital measure. One wall is 21.8 feet. The other is 10.2 feet. How long is each wall measured in the more usual feet and inches?
- (d) The couch Stetson wanted to buy is 92" long and 44" tall. Convert the length and height to feet and inches.
- (e) Abdi volunteers at a food bank. He noticed that the shelf on the back wall was bowing so he measured its length at 12'5". The formula for load needs the length written as a decimal. Convert the length to a decimal number of feet.

3. Some people say we should drink 8 glasses of water (or other liquids) every day where a glass is defined as 8 (liquid) ounces.

- (a) Ingrid uses a 20 ounce unbreakable plastic bottle. How many of those does she need to drink ~~a~~ day?

each

- (b) Siri carries around a insulated water bottle that holds .6 liters. How many of those does she need to drink ~~a~~ day? Use that 1 liter \approx 1.057 quarts and 1 quart = 32 (liquid) ounces.

- (c) To meet the recommendation, how much water would one person drink in a year? Give the answer in gallons. Use 1 gallon = 4 quarts.

-
4. Jenna is studying in Finland this term and rented an older car to drive.
- (a) Gas prices in Finland were 1.658 €/liter. What's the equivalent price in \$/gal? Use $1 \text{ €} \approx \$1.23$. The symbol € stands for euro.
- (b) Her car holds 62 liters of gasoline in its tank. How many gallons is that? Use that $1 \text{ liter} \approx 1.057 \text{ quarts}$ and $1 \text{ gallon} = 4 \text{ quarts}$.
- (c) What would it cost, in euros, for a tank full of gas? In dollars?
- (d) Her car gets 7.6 km/liter. Convert to miles per gallon (mpg). Use $1 \text{ liter} \approx 1.057 \text{ quarts}$ and $1 \text{ gallon} = 4 \text{ quarts}$.
- (e) Jenna learns that no matter what the road signs might say, the maximum speed limit in Finland in winter is never more than 100 km/hr. How fast is that in miles per hour (mph)?

1.5 Metric prefixes and scientific notation

1. Souksavanh is setting up a patient's intravenously (IV) medication. She sets the drip at 42 drops/minute. The drip chamber size is 20 drops/mL.

- (a) Souk needs to know a few conversions.
- How many milliliters (mL) are in a liter?
 - How many microliters (μL) are in a liter?
 - How many milligrams (mg) are in a gram?

Use these numbers to answer the following questions.

- (b) At what rate is the IV fluid being delivered to Souk's patient? Answer in mL/min.

- (c) How fast is the drip measured in $\mu\text{L}/\text{sec}$?

- (d) If the drip bag holds 1 liter, how long will it take the drip to run? Express your answer in hours & minutes.

- (e) The concentration of medication is 1.7 mg/mL. How much medication is in the 1 liter bag? Convert your answer to grams. Explain what you notice.

- (f) At what rate is the medication being delivered to Souk's patient? Answer in grams/min.

2. The list shows the (approximate) mass of the planets in our solar system.

Earth	5.972×10^{24} kg
Jupiter	1.899×10^{27} kg
Mars	6.417×10^{23} kg
Mercury	3.302×10^{23} kg
Neptune	1.024×10^{26} kg
Saturn	5.685×10^{26} kg
Uranus	8.681×10^{25} kg
Venus	4.868×10^{24} kg

Source: Wikipedia (Solar System)

- (a) Write the mass of Earth and the mass of Mars in standard decimal notation. Which is heavier?
- (b) List the planets from heaviest (largest mass) to lightest (smallest mass).
- (c) The mass of astronomical bodies are sometimes measured in **Jupiter mass** abbreviated M_J where $1M_J = 1.899 \times 10^{27}$ kg. Express Earth's mass in M_J .
Because \times and \div are at the same level in the order of operations, you need to put parentheses around each number in scientific notation before dividing.

3. Edgar recently changed the cleaning bag on his vacuum cleaner. He became curious about how many particles of dust were in the bag. Jackson did a little research online and found out that the mass of a dust particle is .000 000 000 753 kilograms.

(The strange-looking spaces are to help you see that there are 9 zeros in the number.)

(a) Write the mass of a dust particle in scientific notation.

(b) Express the mass of a dust particle in each of the following units:

i. grams

ii. milligrams (mg)

iii. micrograms (μg)

iv. nanograms (ng) where

$$\mathbf{nano} = 1 \text{ in a billion} = .000\,000\,001 = 10^{-9}$$

- (c) Edgar determined that the full vacuum bag weighed 5 pounds. How many dust particles were in the bag? (I'm sneezing already.) Use 1 kilogram \approx 2.2 pounds. Express your answer in scientific notation.

4. The GDP (gross domestic product) of the United States was approximately \$15,596 billion in 2011 and the population of the United States was approximately .313 billion that year.

Source: U.S. Bureau of Economic Analysis, U.S. Census Bureau

- (a) That's a strange way to write the population. A more natural unit would be millions. Rewrite the population in millions of people.

0.313

- (b) Rewrite the population in people, both in normal decimal notation (that means with all the 0s) and in scientific notation.

- (c) That's also a strange way to write the GDP. A more natural unit would be **trillions** where

$$1 \text{ trillion} = 1,000,000,000,000$$

Rewrite the GDP in trillions of dollars.

- (d) Rewrite the GDP in dollars, both in normal decimal notation and in scientific notation.

- (e) Calculate the GDP **per capita** (meaning per person) by dividing the GDP in dollars by the population in people. Express your answer in \$/person.

- (f) For practice, repeat your calculation using the numbers in scientific notation.

Because \times and \div are at the same level in the order of operations, you need to put parentheses around each number in scientific notation before dividing.

Chapter 2

Practice exercises for Equations

2.1 A first look at linear equations

1. A truck hauling bags of grass seed pulls into a weigh station along the highway. Trucks are weighed to determine the amount of highway tax owed. This particular truck weighs 3,900 pounds when it's empty. Each bag of seed it carries weighs 4.2 pounds. For example, a truck is carrying 1,000 bags of grass seed weighs

$$3,900 \text{ pounds} + \frac{4.2 \text{ pounds}}{\text{bag}} * 1,000 \text{ bags} = 3,900 + 4.2 \times 1,000 = 8,100 \text{ pounds}$$

In official trucking lingo, we say the **curb weight** of 3,900 pounds plus the **load weight** of 4,200 pounds results in a **gross weight** of 8,100 pounds. So, now you know.

Story also appears in 3.1#1 and 3.2 #1

- (a) Calculate the gross weight of the truck if it contains 2,000 bags of grass seed.

f c n s e

- (b) Name the variables, including units, and write an equation showing how the gross weight of the truck is a function of the number of bag seed it contains.

- (c) Identify the slope and intercept, along with their units, and explain what each means in terms of the story.

Define a pallet?

- (d) How much does the truck weigh if it is carrying 12 pallets of grass seed bags, where each pallet holds 96 bags of seed?

over
what period
of time?

2. The water in the local reservoir was 47 feet deep but there's been so little rain that the depth has fallen 18 inches a week. Officials are worried if dry conditions continue the reservoir will not have enough water to supply the town.

Story also appears in 3.2 #10

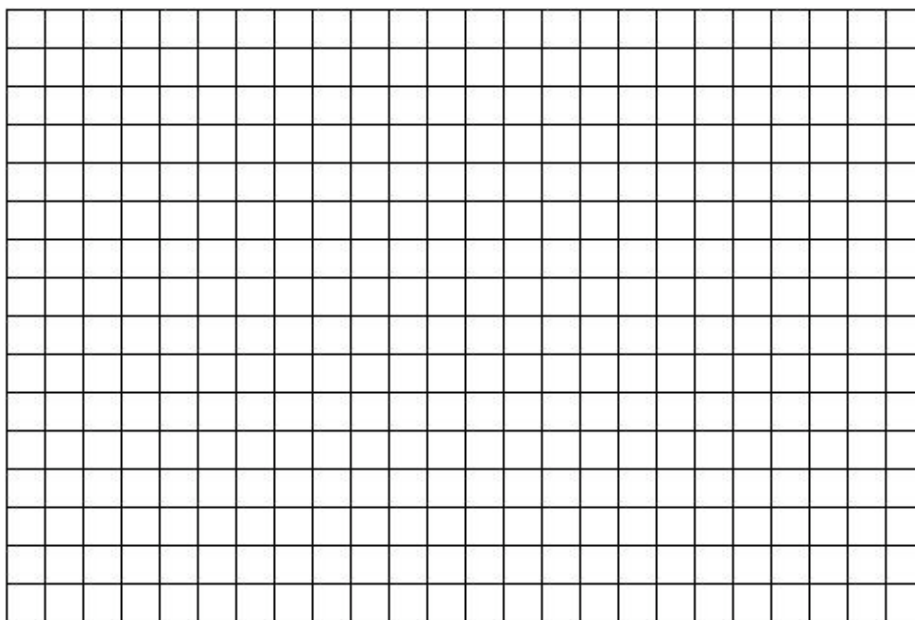
- (a) Name the variables and write an equation relating them. Don't forget to write 18 inches in feet first.

to first
convert 18 inches to feet.

- (b) Identify the slope and intercept, along with their units, and explain what each means in terms of the story.

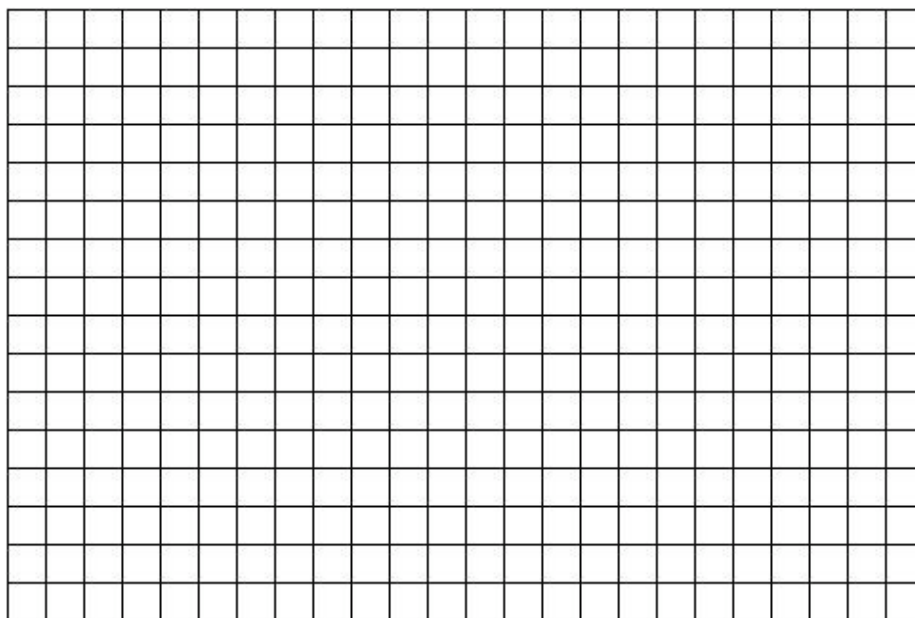
- (c) Make a table of values showing the projected depth of the reservoir after 1 week, 5 weeks, 10 weeks, and 20 weeks if the current trend continues.

- (d) Draw a graph illustrating the function.



3. Sadly, my bank account balance is $-\$2,189.57$. What happened is I spent too much so bank extended me a line of credit, essentially a loan. Each month I plan to pay back the interest for that month plus an extra \$250. Even when the loan is paid off, I plan to deposit \$250 per month to save. *Story also appears in 3.2#7*

- (a) Name the variables and write an equation relating them. Ignore the interest.
- (b) Identify the slope and intercept, along with their units, and explain what each means in terms of the story.
- (c) Make a table of values showing the projected account balance now, after 4 months, and at the end of a year.
- (d) Draw a graph showing how my account balance changed in a year's time.



- (e) About how many months will it take to pay off my line of credit?

-
4. A mug of coffee costs \$3.45 at Juan's favorite cafe, unless he buys their discount card for \$10 in which case a mug cost \$2.90. *Story also appears in 1.2 #4 and 4.2 #2*
- (a) Name the variables, including units.
- (b) Write an equation describing how the total cost depends on how many mugs of coffee Juan buys without the discount card.
- (c) Write an equation describing how the total cost depends on how many mugs of coffee Juan buys if he does buy the discount card.
- (d) How would the equation change if the cafe offer a new annual membership card that cost \$50 but entitles Juan to buy coffee for only \$1 per cup all year?

2.2 A first look at exponential equations

1. The comprehensive fee is \$37,000 at a local private college and is expected to increase 5.8% per year.

(a) Calculate the annual growth factor.

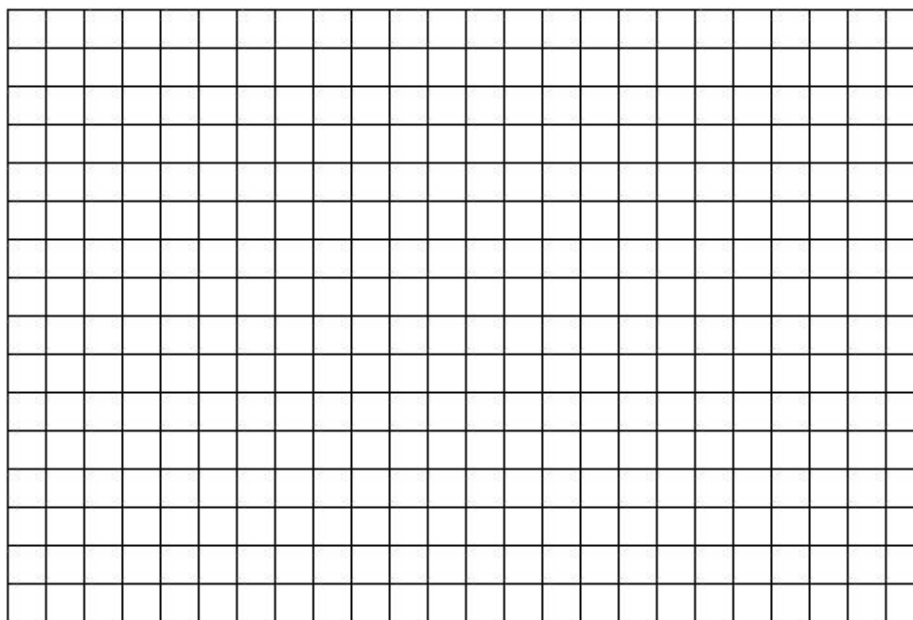
(in \$/year)

(b) What do you expect the tuition to be in five years?

(c) Name the variables, including units, and write an equation describing the dependence.

(d) Make a table of values showing the comprehensive fee now, in 5 years, 10 years, 20 years, and 50 years (even though that's not realistic).

(e) Draw a graph illustrating the function.



least they

2. Bunnies, bunnies, everywhere. In my neighborhood at least. They eat the tops of my tulips in early spring and my lilies all summer long. The most recent count back in 2007 estimated 1,800 rabbits in my neighborhood. Rabbits multiply quickly and with few natural predators in the city, the rabbit population increases rapidly. One estimate was 13% per year. *Story also appears in 5.1#3*

(a) Name the variables.

(b) Calculate the annual growth factor.

(c) What does this story suggest the rabbit population was in 2010? In 2013?

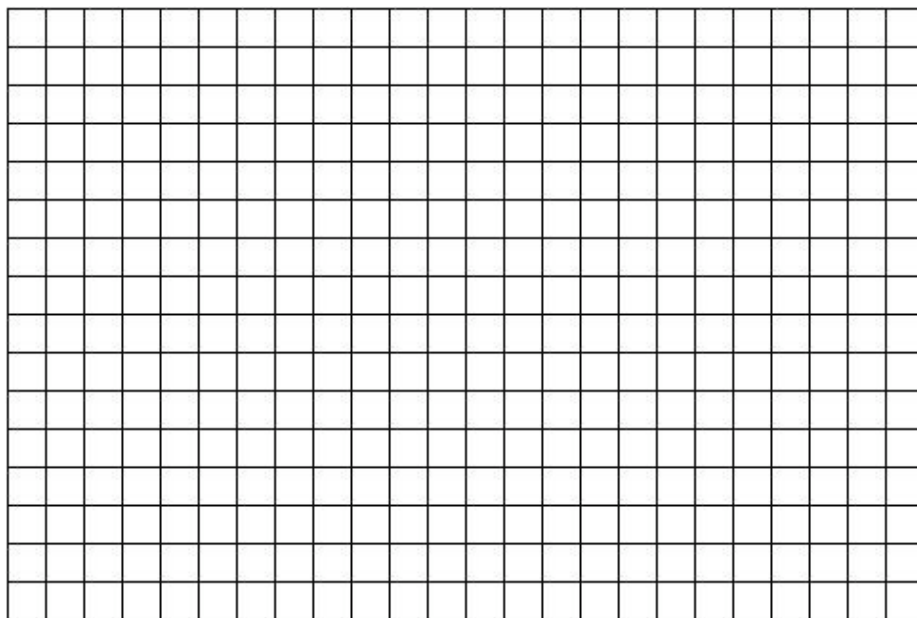
(d) Write an equation relating the variables.

3. A flu virus has been spreading through the college dormitories. Initially 8 students were diagnosed with the flu, but that number has been growing 6% per day.

Story also appears in 5.1 #2 and 5.5 #9

- (a) Calculate the daily growth factor and use it to write an equation describing the spread of the virus. Don't forget to name the variables too.

- (b) Make a table and graph for the six weeks following the initial diagnosis.



-
4. My savings account earns a modest amount of interest, the equivalent of .75% annually. I have \$12,392.18 in the account now.
- (a) How much interest will I earn this year?
 - (b) What will my balance be in three years, assuming I neither deposit nor withdraw money?
 - (c) Name the variables and write an equation relating them.
 - (d) What would the equation be if I moved all of my money into a certificate of deposit earning the equivalent of .92%?
 - (e) What would the equation be if I moved \$10,000 into that certificate of deposit, and kept the rest in savings?
Hint: to get the total balance, add the amount in each account.

2.3 Using equations

1. Monty plans to start cultivating orchids. He knows that they are fragile plants and estimates that there is a probability P that each plant will survive. He will consider his greenhouse a success if at least nine of the ten orchids survive. According to probability theory, the probability Monty's greenhouse will be a success G is given by the equation

$$G = 10P^9 - 9P^{10}$$

Technically this equation assumes that the success of the orchids are “independent” which might not be the case.

- (a) If the orchids are 100% perfect (with probability $P = 1$ of surviving), then what is the probability of a successful greenhouse? Explain how your answer is to be expected.
 - (b) If the orchids are complete duds (with probability $P = 0$ of surviving), then what is the probability of a successful greenhouse? Explain how your answer is to be expected.
 - (c) Make a table showing the probability of a successful greenhouse if the likelihood of each orchid surviving is 0%, 50%, 80%, 90%, 95%, or 100%.
That means with probabilities $P = 0, .5, .8, .9, .95, 1$
 - (d) Draw a graph of the function. SU NOTE Follow up is in Approx Solns
2. “Rose gold” is a mix of gold and copper. Suppose we have 2 grams of an alloy that is equal parts gold and copper. We plan to add G grams of pure gold to it to create a lighter color. If P is the percentage of gold in the resulting alloy, then

$$P = 100 \left(\frac{1 + G}{2 + G} \right)$$

For example, if we add .4 grams of pure gold, then $G = .4$ and so the percentage is

$$P = 100 \left(\frac{1 + .4}{2 + .4} \right) = 100 \times (1 + .4) \div (2 + .4) = 58.3333333 \dots \approx 58.3\%$$

- (a) Calculate the percentage of gold in the alloy if we add 1 or 2 grams of pure gold.
 - (b) Fill in the missing values
- | | | | | | | | | | | | |
|-----|------|----|------|----|------|-----|-----|------|------|-----|-----|
| G | 0 | .2 | .4 | .6 | .8 | 1.0 | 1.2 | 1.4 | 1.6 | 1.8 | 2.0 |
| P | 50.0 | | 58.3 | | 64.3 | | | 70.6 | 72.2 | | |
- (c) Draw a graph illustrating the function.
 - (d) What do you think happens to the percentage of gold as we add more and more pure gold? Try adding 10 grams, and then try adding 100 grams to check.
3. Our investment club has been tracking the performance of a biofuel company's stock over the past year. Using an econometrics software package, we found the equation

$$V = .00004W^3 + .01W^2 - .9W + 31$$

which describes the value of each share of stock $\$V$ as a function of the week W , starting exactly one year ago.

- (a) Complete the following table of values (and check the values already entered):

W	0	13	26	39	52
V	31.00	21.08			16.86

- (b) According to the table, what is the value of the stock when we began tracking it? What is it worth now?
- (c) We're thinking of buying some stock now, and selling it in 10 weeks. Does the equation say that's a good idea? Figure out how much money we earn (or lose) per share on the deal. *Hint: 10 weeks from now is not $W = 10$ because we started counting weeks one year ago.*
- (d) Do you want to buy a stock when it's increasing or decreasing in value? SU NOTE Follow up is in Approx Solns
4. **FOUR** Valerie plans to do a 3-day 50-mile walk to raise money for breast cancer research, in honor of her aunt who's a survivor. Valerie's friends and co-workers have pledged a total of \$93 per mile.
- (a) Valerie hopes to walk all 50 miles. If so, how much money will she raise?
- (b) She might have to stop sooner, however. Name variables and write an equation showing how the money Valerie raises is a function of how far she is able to walk.
- (c) How many hours will Valerie need to walk if she's able to keep a pace of 3.2 miles per hour?
- (d) Name the new variables and write a new equation showing how the time it takes Valerie to walk depends on her speed.
- (e) Good news. Valerie walked the full 50 miles at a pace of 3.2 miles per hour. Way to go, girl! How much money did she raise each hour? *Use your answers from earlier to find \$ and hours. Then divide to get \$/hour.*

2.4 Approximating solutions of equations

1. The size of a round pizza is often described by its diameter (distance across). Assuming a 16-inch diameter pizza serves four people, and with a little geometry to help us out, we calculated that a pizza of diameter D inches serves P people where

$$P = .015625D^2$$

- (a) Confirm that a 16-inch pizza serves four people.
- (b) According to the equation, how many people does a 12-inch pizza serve? A 14-inch pizza?
- (c) Use successive approximation to estimate the size of a personal pizza (to the nearest inch). *“Personal” means serving one person.*
- (d) What super-size should a pizza be to serve 6 people? Now find the answer to the nearest $\frac{1}{10}$ inch. Not that pizza crust is actually that precise.

Story also appears in 3.3# x

2. The gas tank of a car is typically designed to hold enough fuel to drive 350 miles. For example, hybrid that gets 50 miles per gallon (mpg) would need a gas tank that holds 7 gallons, but a RV (recreational vehicle) that gets only 10 miles per gallon would need a gas tank that holds 35 gallons.
 - (a) Name the variables including units. The way the story is stated, the size tank is a function of the fuel efficiency.
 - (b) Write an equation describing this function.
 - (c) My Honda Accord’s tank holds about 16 gallons. Approximate the corresponding fuel efficiency to one decimal place.
 - (d) My ex-husband’s Honda Civic’s tank holds only 13 gallons. Approximate the corresponding fuel efficiency to one decimal place.

Story also appears in 3.3 #3

3. **2.3#3** Our investment club has been tracking the performance of a biofuel company’s stock over the past year. We found the equation

$$V = .00004W^3 + .01W^2 - .9W + 31$$

which describes the value of each share of stock $\$V$ as a function of the week W , starting exactly one year ago.

- (a) The stock was worth \$31 a year ago when we started tracking. Now, one year later, it’s worth \$16.86 but is on the rise again. Use successive approximation to estimate when it will return to \$31 in value. *Report your answer in time from now.*
- (b) Looking back over the past year, how low did the value of the stock get? Use successive approximation to estimate to the nearest dollar.

4. **FOUR** After China, India, and the United States, the next five most populous countries (in 2011) are Indonesia, Brazil, Pakistan, Nigeria, and Bangladesh. Their projected growth rates and corresponding equation are listed below. Here Q is the population measured in millions (not billions) and Y is the years since 2011.

4 th	Indonesia	pop. 248 million	growth rate 1.04%	$Q = 248 * 1.0104^Y$
5 th	Brazil	pop. 205 million	growth rate 1.10%	$Q = 205 * 1.0110^Y$
6 th	Pakistan	pop. 190 million	growth rate 1.55%	$Q = 190 * 1.0155^Y$
7 th	Nigeria	pop. 170 million	growth rate 2.55%	$Q = 170 * 1.0255^Y$
8 th	Bangladesh	pop. 161 million	growth rate 1.58%	$Q = 161 * 1.0158^Y$

- Which of these countries is projected to have the largest population in 2020? In 2030? In 2050?
- Explain why Bangladesh's population will not overtake Nigeria's, assuming these projections are accurate.
- Approximately when will Brazil's population top 500 million? Will Nigeria get there first?

2.5 Finance formulas

1. Use the indicated formulas to help Kanya figure out her finances.
 - (a) Kanya deposited \$2,500 in a money market account that earned 7% interest compounded monthly. Use the COMPOUND INTEREST FORMULA to calculate her account balance after 4 years.
 - (b) What is the equivalent APR on Kanya's money market account? Use the EQUIVALENT APR FORMULA.
 - (c) Kanya puts \$400 a month in her retirement account that amazingly also earns 7% interest compounded monthly. Use the FUTURE VALUE ANNUITY FORMULA to determine how much Kanyai will have in her retirement account in 28 years.
 - (d) Kanya would really like to buy a new hybrid car that sells for \$23,500. Sadly Kanyai's credit rating is not very good, so the best the dealership offers is a loan at – you guessed it – 7% interest compounded monthly. Use the LOAN PAYMENT FORMULA to calculate her monthly car payments on a six year loan.
2. Tim and Josh are saving for their kids' college in fifteen years. The account pays the equivalent of 5.4% interest compounded monthly (taking into consideration various tax incentives).
 - (a) Make a table showing how much they will have after fifteen years if every month they contribute \$100, \$500, or \$1,000. Use the FUTURE VALUE ANNUITY FORMULA.
 - (b) Tim's parents decide to put \$15,000 into the account right now. How much will that add to the value in fifteen years? Use the COMPOUND INTEREST FORMULA.
3. Use the EQUIVALENT APR FORMULA to find the APR for each of the following published interest rates (compounded monthly) offered by recent credit card companies.
 - (a) 9% (b) 12.8% (c) 20.19%
4. **FOUR** Cesar and Eliana are looking at three different houses to buy. The first, a large new townhouse, for \$240,000. The second, a small but charming bungalow, for \$260,000. The third, a large story house down the block, for \$280,000.
 - (a) Calculate the monthly payment for each house for a 30-year mortgage at 3.5% interest compounded monthly. Use the LOAN PAYMENT FORMULA.
 - (b) Describe the affect of paying \$20,000 more at this interest rate.

Chapter 3

Practice exercises for Solving equations

3.1 Solving linear equations

1. **2.1 #1** A truck hauling bags of grass seed pulls into a weigh station along the highway. This particular truck weighs 3,900 pounds when it's empty. Each bag of seed it carries weighs 4.2 pounds. We found earlier that an equation for this function is

$$W = 3,900 + 4.2B$$

where W is the gross weight of the truck, in pounds, and B is the number of bags of grass seed.

- (a) Set up and solve an equation to determine the number of bags of grass seed being carried by the truck with gross weight of 14,500 pounds.
- (b) Do the same for a truck with gross weight 8 tons. *A ton is 2,000 pounds*

SU NOTE Revisited in 3.2

2. Is laughter really the best medicine? A study was conducted to determine the impact of watching comedy videos on anxiety levels in seniors with early stages of dementia. Health care professionals measured anxiety levels on a scale of 1 to 5 before and after the study. Levels averaged 4.3 before the study. There was no significant change in patients who watched a fish tank (the "control") during the study. For those patients who watched the comedy videos there was a noticeable difference, and it increased with the hours of comedy watched. Anxiety levels fell an average of .098 (on the 1 to 5 scale) for each hour of comedy watched.
 - (a) Make a table showing average anxiety levels in a patient who watched comedy videos for 0 hours (control group), 2 hours, 10 hours, and 20 hours.
 - (b) Use successive approximation to guess the number of hours watching comedy needed to lower the average anxiety level below 2 (on that scale of 1 to 5).
 - (c) Name the variables and write an equation relating them. Anxiety is measured on a unitless scale.
 - (d) Solve your equation to determine the number of hours watching comedy needed to lower the average anxiety level below 2.
3. Lizbeth wants to send her mom truffles for mother's day. It cost $\$C$ to send a box of T truffles where

$$C = 1.90T + 7.95$$

- (a) Make a table of values showing the charges for a box of 8 truffles, 12 truffles, or 30 truffles.
- (b) What are the units on 1.90 and what does it mean in the problem?
- (c) What are the units on 7.95 and what does it mean in the problem?
- (d) Draw a graph illustrating the cost of sending truffles.
- (e) If Lizbeth was charged \$53.55 for the box of truffles she sent her mom, how many truffles were there? *Set up and solve an equation to answer the question.*

4. The local burger joint by my house had a promotion this August where they reduced the price of a bacon double cheeseburger by 2¢ for each degree in the temperature. The equation we found was

$$B = 7.16 - .02H$$

where B is the price of the bacon double cheeseburger and H measures how hot it is, in °F. Set up and solve an equation to find the temperature in each situation.

- (a) Ronald paid \$5.34 for a bacon double cheeseburger on Tuesday. How hot was the temperature that day?
- (b) What was the high temperature on Sunday when Wendy bought a bacon double cheeseburger for only \$5.70?
- (c) Leroy is holding out for a \$5 burger. What temperature will make Leroy's wish to come true?

3.2 Solving linear inequalities

1. **2.1 #1 and 3.1 #1** A truck hauling bags of grass seed pulls into a weigh station along the highway. The gross weight of the truck, $\$W$ pounds depends on the number of bags of grass seed B according to the equation

$$W = 3,900 + 4.2B$$

- (a) Determine the maximum number of bags of grass seed that the truck can carry and stay under the state's 18,000 pound gross weight limit. Set up and solve an inequality.
- (b) Earlier we found these values. Fill in your answer to (a) in the table and use these values to graph the function.

B	0	1,000	2,000	18,000
W	3,900	8,100	12,300	

- (c) Since we used the answer to (a) to draw our graph, how can we use the graph to check that the answer to (a) make sense? *Hint: what shape should the graph be?*
2. The altitude, A feet above ground, of an airplane M minutes after it begins its descent is given by the equation $A = 32,000 - 1,200M$. Answer each question by evaluating; setting up and solving an equation; or setting up and solving an inequality, whichever is most appropriate.
- (a) At what altitude does the plane begin its descent?
- (b) How fast is the airplane descending?
- (c) What is the airplane's altitude 3 minutes into its descent? 8 minutes? 20 minutes? Display your answers in a table.
- (d) Draw a graph illustrating the function.
- (e) For how many minutes is the airplane above 20,000 feet?
- (f) The airplane might be asked to go into a **holding pattern** (that means flying in a circle instead of landing) when it's between 6,000 and 14,000 feet up. When will the plane be in that altitude range?
- (g) How long does it take the airplane to land (assuming it's not asked to go into a holding pattern)?
3. **1.2 #3** Anthony and Christina are trying to decide where to hold their wedding reception. For each possible site, write an equation and solve an inequality to calculate the number of guests they can afford on their \$8,000 budget. Use T for the total cost of their wedding reception (in dollars) and G for the number of guests.
- (a) The Metropolitan Club costs \$1,300 down and \$92 per person.
equation:
number of guests:

- (b) Black Elk Park charges \$500 to rent the pavilion and the family can bring in picnic food for \$65 per person.

equation:

number of guests:

- (c) The Dabbling Duck Inn charges \$1,400 and \$80 per person for their local specialties.

equation:

number of guests:

- (d) Pranzo Ristorante has only a \$300 room rental fee but averages \$145 per person, including wine.

equation:

number of guests:

4. One variety of blueberry plant yields an average of 130 blueberries per season but there's quite a bit of variability from plant to plant. One measure of this variability is called the standard deviation, which is approximated at 16.4 berries. Given a plant yielding B blueberries, we can calculate how usual or unusual that is by computing its **standard Z -score** using the equation

$$Z = \frac{B - 130}{16.4}$$

For example, a plant yielding $B = 130$ blueberries has standard Z -score of 0. A plant yielding $B = 173$ blueberries has standard Z -score of

$$Z = \frac{173 - 130}{16.4} = (\underline{173} - 130) \div 16.4 = .671875 \approx .67$$

Notice that we needed parentheses around the top (numerator) of our fraction to correct for the order of operations because we want the subtraction to be calculated before the division. (The standard order of operations is the other way around.) Answer each question by evaluating; setting up and solving an equation; or setting up and solving an inequality, whichever is appropriate.

- (a) Calculate the standard Z -score of a plant yielding 240 blueberries.
- (b) If the standard Z -score for a plant is $-.7$, what is the corresponding yield? *Hint: the negative standard Z -score tells us the answer is below average.*
- (c) A standard Z -score above 1.96 is considered extraordinarily plentiful. What yields of blueberries would be considered extraordinarily plentiful?
- (d) A standard Z -score between -1 and $+1$ are considered ordinary. What yields of blueberries are considered ordinary?

3.3 Solving power equations (and roots)

1. **2.4#1** A pizza of diameter D inches serves P people where

$$P = 0.015625D^2$$

- (a) Show how to solve the equation to find the size of a personal pizza. Means serves one person.
 - (b) What super-size should a pizza be to serve 6 people? Show how to solve the equation to find the answer.
2. The weight of a wood cube (W ounces) is a function of the length of the side (E inches) according to the equation

$$W = .76E^3$$

- (a) How much does a 2-inch cube weigh? A 3-inch cube?
 - (b)
3. **2.4 #2** The gas tank of a car is typically designed to hold enough fuel to drive 350 miles. For example, a hybrid that gets 35 miles per gallon (mpg) would need a gas tank that holds 10 gallons, but a RV (recreational vehicle) that gets only 10 miles per gallon would need a gas tank that holds 35 gallons. We saw earlier that the size tank, G gallons is a function of the fuel efficiency, F mpg according to the equation

$$G = \frac{350}{F}$$

- (a) My Honda Accord's tank holds about 16 gallons. According to the equation, what is the corresponding fuel efficiency? *Set up and solve the equation. Start solving by multiplying both sides by F . There is no power, so you won't have to take a root.*
 - (b) My ex-husband's Honda Civic's tank holds only 13 gallons. According to the equation, what is the corresponding fuel efficiency. *Set up and solve the equation.*
4. Moose bought a commemorative football jersey for \$250 fourteen years ago. Now he's planning to sell it and is interested in what the effective return on his investment might be for various prices. The equation is

$$J = 150g^{12}$$

where $\$J$ is the current value of the jersey and g is the annual growth factor. The effective return is r where $r = g - 1$ and is normally written as a percentage. Find the effective return if the current value is

(a) \$290

(b) \$350

(c) \$400

For each part, first solve for g , then calculate r , and write as a percentage.

3.4 Solving exponential equations (and logs)

1. After his first beer, Stephen's blood alcohol content (BAC) was already .04 and as he continued to drink, his BAC level rose 45% per hour. The equation is

$$S = .04 * 1.45^H$$

where S is Stephen's BAC and H is the time, measured in hours.

- (a) Make a table showing Stephen's BAC at the start of the problem and the next four hours.
- (b) At a BAC of .10 it is illegal for Stephen to drive. Set up and solve an equation to find when that will happen. Answer to the nearest minute.
- (c) At a BAC of .20, Stephen will become confused and disoriented and is at risk to black out and choke on his own vomit. Hopefully he'll stop drinking before that happens. At the rate he's going, when would that be? Set up and solve an equation to find when that will happen. Answer to the nearest minute.

Story also appears in 2.4 #11 and 3.4 #1

2. Chlorine is often used to disinfect water in swimming pools. From an initial Chlorine concentration of 2.5 ppm, the amount drops as the swimming pool is used according to the equation

$$C = 2.5(.975)^H$$

where C = amount of Chlorine (ppm) and H = time used (hours).

- (a) Make a table of values showing the concentration of Chlorine initially and after the swimming pool is used for 3 hours, 10 hours, 15 hours, and 25 hours.
- (b) Draw a graph illustrating the function.
- (c) Chlorine concentrations below 1.5 ppm do not disinfect properly. When the concentration falls below 1.5 ppm, more Chlorine needs to be added to the swimming pool water. According to your graph, after approximately how many hours of use will more Chlorine need to be added?
- (d) Show how to use successive approximate to calculate when the Chlorine concentration will fall below 1.5 ppm.
- (e) Show how to solve the equation to calculate when the Chlorine concentration will fall below 1.5 ppm.

REVISIT 5.3 #3

3. **1.1 #2** Rent in the Riverside Neighborhood is expected to increase 7.2% each year. Average rent for an apartment is currently \$830 per month. Earlier we identified the variables as R for the monthly rent (in \$) and Y for the years.
 - (a) Find the annual growth factor.
 - (b) Write an equation showing how rent is expected to change.

- (c) Use successive approximation to determine when rent will pass \$1,000/month. Display your work in a table. Round to the appropriate year.
- (d) Show how to solve the equation to calculate when rent will pass \$1,000/month. Display your work in a table. Round to the appropriate year.
- (e) Solve again to determine when rent will reach double what it is now, namely \$1,660/month, assuming this trend continues.

Story also appears in 3.4 #3

4. Goldie the goldfish, Pinches the lobster, Quackers the duck, Speedy the turtle . . . Expectations back in 1994 were that first generation Beanie Babies toys made would increase in value according to the equation

$$B = 6(1.08)^Y$$

where B is the value of Beanie Babies (in \$) and Y is the years since 1994.

- (a) If expectations were correct, what was a Beanie Baby toy worth in the year 2004? What was it worth in 2010?
- (b) According to your equation, when will Beanie Babies made in 1994 be worth over \$100? *Report the actual year.*
- (c) Show how you can solve the equation to find the answer.
- (d) Because of the recession, the value actually slowed a bit starting in 2004. The revised equation is

$$B = 12.95 * 1.072^T$$

where now T is measured from 2004 instead. What is the revised estimate for 2010 and when will it be worth over \$100? Solve an equation to answer. *Report the actual year.*

REVISIT 5.3

3.5 Solving quadratic equations

1. A high-jumper jumps so that the height, H feet, of the point on his back that must clear the bar after T seconds is given by the equation

$$H = 3.5 + 16T - 16T^2$$

SU PROVIDE GRAPH

- (a) When would the high-jumper hit the ground (if there weren't a pit)? **Ouch!** Use the QUADRATIC FORMULA to find the answer.
 - (b) The high jump pit is 2 feet off the ground. When does the high-jumper land in the pit? Use the QUADRATIC FORMULA to find the answer.
 - (c) How high a bar can the high-jumper clear? Find the maximum height of that point above ground by evaluating at $T = \frac{-b}{2a}$.
2. The number of people visiting national parks each year has been increasing for many years. The number of annual visits is approximated by the equation

$$N = .0913Y^2 - 1.7Y + 10.1$$

where N is number of annual visits, in millions, and Y is the year since 1920.

- (a) Calculate the missing values in the table.

Y	0	5	10	15	20	25	30
V	10		2	5	13		41

- (b) Draw a graph of the function
 - (c) According to this equation, in what year is the number of annual visits the smallest? For that year, what were the number of visits?
 - (d) Explain why N never equals 0.
 - (e) So, what actually happens when you try to use the QUADRATIC FORMULA to solve for $N = 0$?
 - (f) In what year did the number of visitors first pass 700 million in a year? Estimate the value from your graph. Then set up and solve a quadratic equation.
3. The profit $\$P$ from selling M tanks of milk is described by the equation

$$P = -2M^2 + 2000M - 80,000$$

- (a) Complete the following table showing the profit of selling tanks of milk.

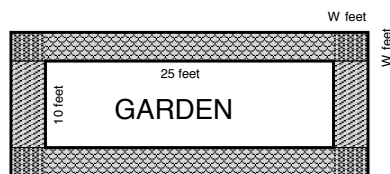
M	0	100	200	300	400	500	600	700	800	900
P			240,000	340,000		420,000	400,000		240,000	100,000

- (b) Explain why negative numbers make sense in this problem.

- (c) Draw a graph showing how the profit depends on the amount of milk sold.
- (d) How much milk must be sold for the company to “break even” (means having \$0 profit.)? Set up and solve a quadratic equation to answer the question.
- (e) Does your answer agree with your table and graph? Explain.
- (f) How many tanks of milk would they need to sell to keep profits over \$400,000?
Your answer should be in the form of an inequality.
4. **2.3#6, then 2.4 #12** Urban community gardens are catching on. What was once an abandoned lot down the block is now a thriving 10'×25' vegetable and berry garden for the neighborhood. One of the neighbors works for a landscaper who has volunteered to donate some gravel to make a path around the garden that's 3 inches deep and the same width all around. The amount of gravel we need (G cubic feet) is given by the equation

$$G = W^2 + 17.5W$$

where W is the width of the path in feet.



- (a) If the landscaper donates 60 cubic feet of gravel, how wide a path can they build?
Set up and solve a quadratic equation to find the answer to two decimal places in feet. Then convert your answer into inches.
- (b) Gravel is measured by the “yard,” which is short for cubic yard. There are 27 cubic feet in 1 cubic yard. If the landscaper donates three yards of gravel, how wide a path can they build? *Set up and solve a quadratic equation to find the answer to two decimal places in feet. Then convert your answer into inches.*
- (c) What would it mean to solve the equation to find where $G = 0$? Can you tell what the answer is from the equation (without actually solving)?

Chapter 4

Practice exercises for A closer
look at linear equations

4.1 Modeling with linear equations

1. A solar heating system costs approximately \$30,000 to install and \$150 per year to run. By comparison, a gas heating system costs approximately \$12,000 to install and \$700 per year to run.
 - (a) What is the total cost for installing and running a gas heating system for 30 years?
 - (b) Write a linear equation showing how the total cost for a gas heating system depends on the number of years you run it.
 - (c) Write a linear equation showing how the total cost for a solar heating system depends on the number of years you run it.
 - (d) How many years of a solar heating system could you get for the cost of a gas heating system lasting 30 years (your answer to part (a))? Set up and solve an equation. SU NOTE Revisit in 4.2
2. Since the Amazon Kindle was released in February 2009, the price has been decreasing at a constant rate. In fact, in February 2011, a blogger developed the following equation representing the price P of the Kindle in the months M since it was released in February 2009:

$$P = 359 - 12M$$

- (a) Make a table of values for the Kindle price initially, 10 months, and 25 months since February 2009.
 - (b) What does the 359 mean in the story and what are its units?
 - (c) What does the 12 mean in the story and what are its units?
 - (d) Draw a graph illustrating the dependence.
 - (e) Approximately how many months after February 2009 is the price of the Kindle expected to be \$200?
 - (f) I will purchase a Kindle if the price falls below \$100. When will the price fall below that level? Set up and solve an inequality to find the answer.
 - (g) If you can believe what you read in blogs, Amazon will soon be giving away the Kindle for free, since they make money on the book sales themselves. When would that happen, according to our equation?
3. **2.1 #5** Earlier we were comparing plumbers and found the following options. In each equation, the plumber charges \$ P for H hours of work.

Plumber Equation	James $P = 50 + 120H$	Jo $P = 45 + 55H$	Mario $P = 90H$	Luigi $P = 150$
0 hours	\$50	\$45	\$0	\$150
2 hours	\$290	\$155	\$180	\$150
4 hours	\$530	\$265	\$360	\$150

- (a) Use the points given to plot each of the four lines on the same set of axes. Label each line with the plumber's name.
 - (b) What do you notice about Luigi's line?
 - (c) List the plumbers in order from steepest to flat as shown on the graph. What does that mean in terms of the story?
 - (d) Now list the plumbers in order from smallest to largest intercept. How can you see that on the graph? What does that mean in terms of the story?
4. Which of these functions are linear? NEED TABLES
- (a) SAVINGS ACCOUNT, 1.2 #1 then 5.3 again
 - (b) AHMED's virbunum, 4.2 #3
 - (c) Rose gold 2.3 #2
 - (d) pizza 2.4 # 1
 - (e) oil change 4.5 #7

4.2 Systems of linear equations

1. Madison want to buy a new car and have narrowed it down to two models: the Toyota Prius, priced at \$26,100, or the Volkswagen Jetta, priced at \$23,700. Annual fuel costs for the Toyota Prius are currently \$1,100. For the Jetta, annual fuel costs are currently \$1,800. The total cost of each car will depend on how many years she keeps it.
 - (a) Name the variables.
 - (b) Write a linear equation for the total cost (including purchase price and fuel costs) of the Prius and write another linear equation for the total cost of the Jetta, each as a function of how long she keeps it. Assume fuel costs stay at current levels. (Don't know if that's realistic, but it's the best information we have.)
 - (c) Make a table comparing the total cost for each car if she keeps it 3, 5, or 10 years.
 - (d) Set up and solve a system of linear equations to determine the **payoff time**, or the number of years for which the total costs of each car are equal.
 - (e) Based on what you've learned, **fill in the blank**.

The more expensive Toyota Prius pays off if Madison is going to keep it for ___ years or more.

2. **1.2 #4 and 2.1 #4** Juan's favorite coffee shop sells a discount card. Without the card his coffee costs \$3.45 per mug. If he purchases a card for \$10.00, then Juan can buy the coffee for \$2.90 per cup. If we let C represent the number of cups of coffee he buys and T represent the total cost in dollars, then the equations are: SU SEE REWORDING IN 1.2 MUGS!!

$$\text{No Card: } T = 3.45C$$

$$\text{With Card: } T = 10 + 2.90C$$

- (a) Compare the total costs with and without the card to buy 0, 10, 20, or 30 cups of coffee.

Cups	0	10	20	30
With Card				
No Card				

- (b) Draw a graph showing both options.
- (c) According to your graph, what is the **break even** time? *That means the number of cups of coffee for which the total costs with or without the discount card are equal.*

- (d) Set up and solve a system of linear equations to determine the exact break even time.
- (e) Describe in words what you've learned about whether or not Juan should purchase the discount card.
3. (4.1 #4) Ahmed planted two shrubs in the backyard on May 1. The virburnum was 16.9 inches tall and expected to grow .4 inches each week this summer. The weigela was 20.3 inches tall but only expected to grow .2 inches per week this summer. If we let S represent the total height of the shrub in inches after W weeks, then the equations are:

$$\textbf{Virburnum: } S = 16.9 + .4W$$

$$\textbf{Weigela: } S = 20.3 + .2W$$

- (a) Compare the height of the shrub on the given dates.

date	May 1	June 12	July 10	Sept 4
W	0	6	10	18
S (virburnum)	16.9	19.3	20.9	24.1
S (weigela)	20.3	21.5	22.3	23.9

- (b) When will the shrubs be the same height? Continue successive approximation to find the answer to the nearest week.
- (c) Set up and solve an equation to find the day when the two shrubs are the same height. Report the actual calendar date.
4. The **supply** of flour is the amount of flour produced. It depends on the price of flour. A high price encourages producers to make more flour. If the price is low, they tend to make less of it. The dependence of the supply of flour S (in loads) on the price P (in \$/ pound) is given by the equation

$$\textbf{Supply: } S = .8P + .5$$

The **demand** of flour is the amount of flour consumers want to buy. It also depends on the price of flour. If flour sells for a high price, then consumers will buy less. If flour sells for a low price instead, then consumers will buy more. The dependence of the demand of flour D (in loads) on the price P (in \$/pound) is given by the equation

$$\textbf{Demand: } D = 1.5 - .4P$$

The **equilibrium price** of flour is the price where the supply equals the demand.

- (a) What happens if flour is priced at \$1.00/pound? That is, how much flour will be produced and how much will consumers want?
- (b) What happens if flour is priced at \$0.50/pound? That is, how much flour will be produced and how much will consumers want?

- (c) Graph each dependence on the same set of axes. What is the equilibrium price, approximately, according to your graph?
- (d) Set up and solve an equation to find the equilibrium price of flour.
- (e) When more of a product is produced than consumers want to buy, we have a **surplus** of the product. For practice, set up and solve an inequality to find the range of price values for which there will be a surplus of flour.
- (f) When less of a product is produced than consumers want to buy, we have a **shortage** of the product. For practice, set up and solve an inequality to find the range of price values for which there will be a shortage of flour.

4.3 Intercepts and direct proportionality

1. Each of the two stories, below, involve how temperature changes over time. Best to not call either variable T , so use H for the time in hours and D for the temperature in $^{\circ}\text{F}$. In each case, time should be measured from the start of the story.
 - (a) It was really cold at 8:30 this morning when Raina arrived at the office. Luckily the heating system warms things up very quickly, 4°F per hour. By 11:00 a.m. it was a very comfortable 72°F .
 - i. Figure out what the temperature was at 8:30 a.m.
 - ii. Write an equation illustrating the function.
 - (b) While 72°F is a perfectly good temperature for an office, not so for ballroom dancing. When Raina arrived for her practice at 5:30 that evening, she began to sweat before she even took the floor. Turns out the air conditioner had been running since 4:00 p.m. but it only cools down the room 3°F per hour.
 - i. Figure out what the temperature was at 4:00 p.m.
 - ii. Write an equation illustrating the function.
2. Maryn is very happy. After tallying in this month's hours, her interior design business is finally showing a profit. She has logged a total of 471 billable hours at \$35 per hour since she started her business. Accounting for start up costs, her net profit is totals \$2,194.
 - (a) What were Maryn's start up costs?
 - (b) Identify the slope and intercept (including their units and sign) and explain what each means in terms of the story.
 - (c) Calculate what Maryn's profits will be once she has logged a total of 1,000 hours.
 - (d) Name the variables and write an equation relating them.
 - (e) Graph the function.
3. For each story, find the initial weight of the person and use it to write an equation showing how the person's weight W pounds depends on the time, W weeks.
 - (a) Jerome has gained weight since he took his power training to the next level ten weeks ago, at the rate of around 1 pound a week. He now weighs 198 pounds.
 - (b) Vanessa's doctor put her on a sensible diet and exercise plan to get her back to a healthy weight. She would need to lose an average of 1.25 pounds a week to reach her goal weight of 148 pounds in a year (which is 52 weeks).
 - (c) After the past 6 weeks of terrible migraine headaches, Carlos is down to 158 pounds. He's lost 4 pounds a week.
 - (d) Since she's been pregnant, Zoe has gained the recommended $\frac{1}{2}$ pound per week. Now 30 weeks pregnant and 168 pounds, she wonders if she'll ever see her feet again.

4. Each story describes a situation that we're assuming is linear. Decide whether it is directly proportional or not. If not, identify what the intercept would mean in the story.
- (a) The price of a bag of sweet potatoes depends on how many pounds of sweet potatoes are in the bag.
 - (b) The price of a bag of tortillas depends on how many tortillas are in the bag.
 - (c) The time it takes to vacuum a rug depends on the area of the rug.
 - (d) The time it takes to wash dishes depends on how many dirty dishes there are.
 - (e) The amount of laundry detergent I have left depends on how many loads of laundry I did.

4.4 Slopes

1. Jana is making belts out of leather strips and a metal clasp. An extra short length belt (as shown in the picture) is 24.5 inches long and includes 7 leather strips. An extra long length belt (not shown) is 37.3 inches long and includes 13 leather strips. Each belt includes one metal clasp that is part of the total length. All belts use the same clasp.



- (a) Name the variables, including units.
 - (b) Display the information from the story in a table.
 - (c) How long is each leather strip?
 - (d) How long is the metal clasp?
 - (e) Write an equation relating the variables.
 - (f) Solve your equation to find the number of leather strips in a extra extra long length belt that's 43.7 inches long?
2. The local ski resort is trying to set the price for season passes. They know from past experience that they will sell around 12,000 passes if the season ticket price is \$380. If the price is \$400, they will sell fewer, perhaps only 10,000 passes. You can assume this decrease in demand is linear.
 - (a) Display the information from the story in a table. Notice that ticket price is the independent variable.
 - (b) How many fewer people purchase season passes for every dollar increase in the price?
 - (c) Find the intercept. Explain why this number does not make sense in the problem.
 - (d) Write an equation for the function, using T for the ticket price, in dollars, and D for the demand (number of tickets sold).
 - (e) How many season passes will they sell if the price is reduced to \$355?
 - (f) The amount of **revenue** (money they take in) depends both on the ticket price and the number of tickets sold. The equation is $R = TD$, where R is the revenue, in dollars. Calculate the revenue when ticket prices are \$355, \$380, and \$400. *That means multiply the ticket price T times the number of tickets sold D in each case listed.* Of these three prices, which yields the most revenue?
 3. For Harland's Oscar party he ordered 70 chicken wings for a total cost of \$51.25. For their Super Bowl bash he had 125 wings delivered for \$83.70. Pricing is based on a fixed cost per chicken wing plus a delivery charge.
 - (a) What does each chicken wing cost?
 - (b) What is the delivery charge?

- (c) Write an equation describing how the price depends on the number of wings ordered. Don't forget to name the variables.
 - (d) For his birthday party, Harland has \$100 budgeted for chicken wings (including delivery). How many wings can he have delivered? Show how to solve your equation.
 - (e) Graph and check.
4. Boy, am I out of shape. Right now I can only “press” about 15 pounds. (“Press” means lift weight off my chest. Literally.) Years ago I was able to press 90 pounds and I would love to get back there again. My trainer says that if I challenge myself I should be able to press 50 pounds by the end of 10 weeks. For the sake of this problem, assume that I can increase the weight I press by a fixed amount each week.
- (a) Write an equation for my trainer's projection. Include naming variables. *Hint: you know the intercept.*
 - (b) According to your equation when will I be able to press (at least) 90 pounds again? Set up and solve an inequality.
 - (c) Draw a graph illustrating the function.
 - (d) I am skeptical. I don't think I'll be able to press 50 pounds by the end of 10 weeks. More than 15 pounds, sure, but 50 seems too ambitious. Will the revised slope be larger or smaller? *Hint: try sketching in a possible revised line on your graph assuming that after 10 weeks I will press much less than 50 pounds.*
 - (e) Will the revised projections mean I'll reach that 90-pound goal sooner or later? Explain. *Hint: extend your graph.*

4.5 Fitting lines to data

SU smoothe out these problems – NOT WELL WRITTEN!!!

1. Mulki is considering investing in a company's stock. She looked up a few values.

Day	0	300	500
Value (\$)	23.19	37.00	48.10

- (a) Calculate the rate at which the stock prices changed during the first 300 days.
 - (b) Calculate the rate at which the stock prices changed from Day 300 to Day 500.
 - (c) Is this growth linear?
 - (d) Draw a scatter plot of the points. SU NOTE SU half sheet is fine
 - (e) Draw in a line that through the points for Day 300 and Day 500. Label this line #1. Explain why that line does not fit the data well.
 - (f) Draw in a line that fits the data better. It does not need to go through any of the points exactly. Label that line #2.
2. The table shows the GPA (grade point average) of ten students compared to the number of hours per week each student works at a part time job. The variables we used are H for the time worked at job (hours / week) and G for the grades GPA (on scale of 0.0 to 4.0)

H	0	0	10	12	14	15	16	18	20	20
G	3.72	3.91	3.43	2.79	3.08	2.62	2.44	3.17	3.00	2.55

- (a) Make a scatter plot of the points. Start the G -axis at 2.0.
 - (b) Find the equation of the line that goes through the first and last point listed. Notice that you know the intercept. Draw this line on your graph and label it B.
 - (c) Use your equation to figure out what you would expect the GPA of a student working a 30 hour per week job to be.
 - (d) The best fitting line from statistics has equation $G = 3.7597 - .0551H$. Make a table of values for this equation using $H = 0, 10, 20$ hours. Use that table of values to graph your line. Label it C.
 - (e) Compare the two lines.
 - (f) According to line C, what's the most hours a student should work to be able to maintain a 3.5 GPA? Solve an equation, and check on your graph.
3. Mia and Mandi and opened a candy shop this January. The table shows their monthly sales profit. Except for some seasonal fluctuation, Mia and Mandi generally expect your profits to rise steadily while their business is getting established.

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug
Sales Profit (\$)	3,394	4,702	3,683	4,840	5,632	4,432	4,649	4,590

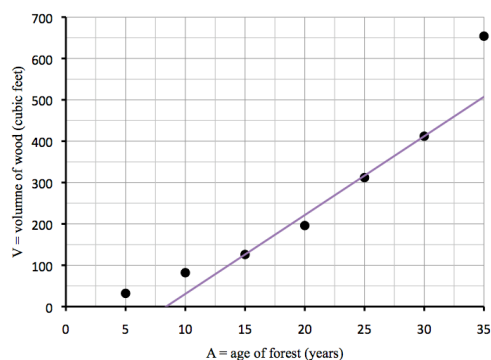
- (a) Name the variables.
- (b) Make a scatter plot. Instead of starting at \$0, begin the profit axis at \$3,000 instead.
- (c) Write an equation for the line through January and August. Add this line (#1) to your graph. This line is too low.
- (d) Write an equation for the line through March and July. Add this line (#2) to your graph. This line is too steep.
- (e) Neither of these lines go anywhere near the data for February, April, and May, because those are outliers. Any idea why those months had much higher candy sales than the other months?
- (f) What does each equation give as an estimate for September's sales?
- (g) Explain why Mia and Mandi should not use your lines to estimate October's sales.

4. The following table shows the total volume of wood, V cubic feet, in managed forests of different ages, A years.

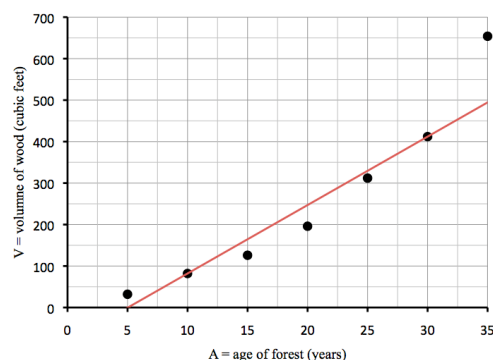
A	5	10	15	20	25	30	35
V	32	82	126	196	312	412	654

For each line drawn, decide if it's a good fit or not. If not, explain why.

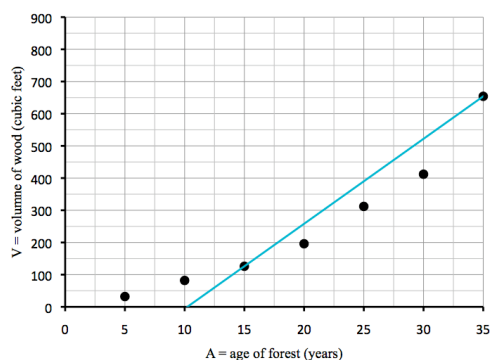
(a) LINE A



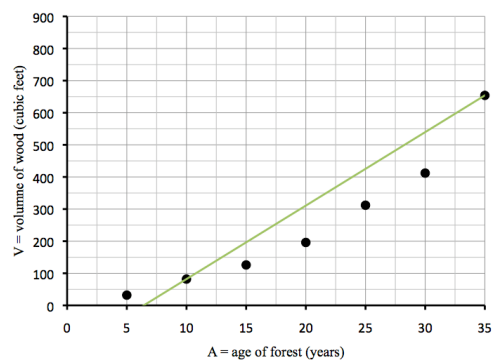
(b) LINE B



(c) LINE C



(d) LINE D



Chapter 5

Practice exercises for A closer
look at exponential equations

5.1 Modeling with exponential equations

1. The population of Buenos Aires, Argentina in 1950 was estimated at 5.0 million and expected to grow at 1.8%.
 - (a) Name the variables.
 - (b) What is the annual growth factor?
 - (c) Write an equation estimating the population of Buenos Aires.
 - (d) Make a table of values showing the population of Buenos Aires every 20th year from 1950 to 2030, according to the equation.
 - (e) By how many people has the population been increasing during each 20 year period? Add these calculations to your table. *Notice how this answer changes because the rate of change is not constant.*
 - (f) The actual population of Buenos Aires in the year 2000 was around 12.6 million and by 2010 it was around 15.2. (This now includes a larger surrounding area as the city has spread beyond historical limits.) How does that compare to the estimates?

SU NOTE source: Mongabay.com

2. **2.2 #3** A flu virus has been spreading through the college dormitories. Initially 8 students were diagnosed with the flu, but that number has been growing 6% per day. Earlier we found the equation

$$N = 8 * 1.06^D$$

where D is the number of days (since the first diagnosis) and N is the total number of students who had the flu. There are 1,094 students currently living in the dorms.

- (a) Make a table and graph for the six weeks following the initial diagnosis. (If you did this earlier, you may look back at that graph instead.)
 - (b) Use successive approximations to estimate when the number of infected students reaches 100.
 - (c) Use the LOG DIVIDES FORMULA to solve your equation.
 - (d) What is a realistic domain? That means, for how many days do you think this model is reasonable? SU NOTE Follow up in 5.5
3. Bunnies, bunnies, everywhere. Earlier we found the equation

$$B = 1,800 * 1.13^Y$$

where B is the number of bunnies and Y is the years since 2007.

- (a) Make a table showing the number of bunnies (according to the equation) in 2007, 2010, 2013, and 2020.
 - (b) Draw a graph showing how the bunny population grew.

- (c) Approximately when will the bunny population pass 5,000, according to this equation? Guess from the graph. Then, check and refine your answer using successive approximation (if necessary).
- (d) Show how to solve your equation to get the answer.

FROM 2.2 #2

4. Carbon dioxide is a greenhouse gas in our atmosphere. Increasing carbon dioxide concentrations are related to global climate change. In 1980, the carbon dioxide concentration was 338 parts per million carbon dioxide (that is on average, one million molecules of air contained 338 molecules of carbon dioxide). At that time it was assumed that carbon dioxide concentrations would increase .42% per year.
- (a) Name the variables including units.
 - (b) Assuming the growth is exponential as predicted, write an equation that describes the dependence.
 - (c) The carbon dioxide concentration in 2008 was 385 parts per million. Is that count higher or lower than predicted from your equation? Explain.
 - (d) Does that mean that carbon dioxide increased at a higher or lower rate than .42%? Explain.

5.2 Exponential growth and decay

1. A signal one unit strong is sent down a fiber optic cable. It decreases by 2% each mile it travels.
 - (a) Make a table showing the strength of the signal of the first five miles.
 - (b) Name the variables, including units, and write an equation relating them.
 - (c) The signal will need a booster when it has fallen to under .75 units. How far along the cable should the booster be placed? Set up and solve an equation.
 - (d) Draw a graph illustrating the relationship.
 - (e) What's the half-life (or should we say half-distance) of a signal? That means, how far can it travel without dropping below 50%? (That won't actual happen because we'd boost the signal.) Again, set up and solve an equation.
2. A recent news report stated that cell phone usage is growing exponentially in developing countries. In one small country, 50,000 people owned a cell phone in the year 2000. At that time it was estimated that usage would increase at 1.4% percent per year.
 - (a) Name the variables including units.
 - (b) Assuming the growth is exponential, write an equation for the function.
 - (c) At this rate, how many years would it take for the number of people owning a cell phone to double? That's called the **doubling time**. Show how to set up and solve an equation to find the answer.
 - (d) In 2011, about 682,000 people owned a cellphone. Is that count higher or lower than predicted from your equation? Explain.
 - (e) Based on the 2011 data, would you say that cell phone usage was growing slower or faster than 1.4%?
3. If you have a heart attack and your heart stops beating, the amount of time it takes paramedics to restart your heart with a defibrillator is critical. According to a medical report, each minute that passes decreases your chance of survival by 10%. Assume that this statement means the decrease is exponential and that the survival rate is 100% if the defibrillator is used immediately.
 - (a) Name the variables and write an equation.
 - (b) If it takes the paramedics 2 minutes to use the defibrillator, what is your survival rate?
 - (c) When does the survival rate drop below 50%? Use successive approximation to estimate to the nearest minute. Display your work in a table.
 - (d) Solve your equation.

source: American Red Cross

4. You and two buddies each invite 10 people to “like” your online group. Suppose everyone accepts and then they each invite 10 people. And then everyone accepts and they each invite 10 people. And so on. Of course, there is likely to be substantial overlap, but for the moment pretend that there isn’t.
- (a) There are 3 friends to start. They each invite 10 in the first round, so a total of 30 new people “like” your online group. How many new people “like” your group in the second round? The third?
 - (b) Name the variables and write an equation showing how the total number of new people increases in each round.
 - (c) Draw a graph showing the number of new people in each of the first six rounds.
 - (d) What is the total number of people who “like” your online group after six rounds.
Hint: add
 - (e) Comment on why our assumption is unrealistic.

SU NOTE Su revisit logistic

5.3 Growth factors

1. In 1962, my grandfather had savings bonds that matured to \$200. He gave those to my mother to keep for me. These bonds have continued to earn interest at a fixed, guaranteed rate so I have yet to cash them in. The table lists the value at various times since then.

year	1962	1970	1980	1990	2000	2010
Y	0	8	18	28	38	48
B	200.00	318.77	570.87	1,022.34	1,830.85	3,278.77

- (a) Use the GROWTH FACTOR FORMULA to find the annual growth factor for the time period from 1962 to 1970.
- (b) Repeat for 1970 to 1980. What do you notice? What in the story told you that would happen?
- (c) Write an equation for the value of bonds over time.
- (d) Use your equation to check the information for 1990, 2000, and 2010.
- (e) In what year will the bond be worth over \$5,000?
- (f) Draw a graph using the data in the table, but not your answer to part (e). Include another year that is later than your answer to (e).
- (g) Does your answer to (e) agree with your graph? If not, fix what's incorrect.

Story also appears in 1.2 #1

2. Have you read stories in the news about archaeological digs and some specimen (like bones) are found that date back thousands of years? How do scientists know how old something is? There are many ways, but one uses the idea of radioactive decay. After a person or animal dies, the carbon-14 that was in their body very slowly begins to change to carbon-12. So, by comparing how much carbon-14 is in the specimen to how much would have been in the person or animal when they were living, scientist can get a pretty good idea how long it's been dead. Clever, huh? (Actually it's so clever that Willard Libby won the Nobel Prize in Chemistry for it in 1960.) Turns out the key information to know is that the half-life of carbon-14 is about 5,730 years. For the purpose of this problem, suppose some specimen is found that Assume that should have contained 300 milligrams of carbon-14 when alive.

- (a) Find the annual "growth" factor.
- (b) Name the variables and write an equation describing the dependence.
- (c) How many milligrams of carbon-14 should remain after 1,000 years? After 10,000 years? After 100,000 years?
- (d) Draw a graph that shows up to 10,000 years.
- (e) How many milligrams of carbon-14 should remain after 1 million years? Explain the answer your calculator gives you.

- (f) If the specimen is determined to have 100 milligrams of carbon-14, how old is it? (That is, approximately how long ago did it die?) Display your work in a table.
- (g) Solve the equation exactly.
3. For each equation, find the growth rate(s) (percent increase or percent decrease) and state the units. (For example, something might “grow 2% per year” while something else might “drop 7% per hour”)

- (a) **3.4 #4** Beanie babies toys were expected to increase in value according to the equation

$$B = 6(1.08)^Y$$

where B is the value of Beanie Babies (in \$) and Y is the years since 1994. Later estimates were revised to

$$B = 12.95 * 1.072^T$$

where now T is measured from 2004 instead.

- (b) **3.4 #2** Chlorine is often used to disinfect water in swimming pools. From an initial Chlorine concentration of 2.5 ppm, the amount drops as the swimming pool is used according to the equation

$$C = 2.5(.975)^H$$

where C = amount of Chlorine (ppm) and H = time used (hours).

4. Find the annual growth factor and growth rate for each of the following stories.
- (a) Donations to the food shelf have increased 35% per year for the past few years.
- (b) People picking up food at the food shelf has increased exponentially too, from 120 per week in 2005 to 630 per week in 2011.
- (c) The crime rate has dropped 3% each year recently.
- (d) The creeping vine taking over my lawn doubles in area each year.
- (e) Attendance at parent volunteer night has done so well it has doubled every 3 years.
- (f) The new stop sign has decreased accidents exponentially, from 40 in 2008 to 17 in 2013.

5.4 Linear vs. exponential models

1. My parents bought the house I grew up in for \$35,000 and sold it 40 years later for \$342,000. True story. (It was before the housing bubble burst.)

First, assume the value of the house increased exponentially.

- (a) Calculate the annual growth factor.
- (b) In this model, by what percentage did the house value increase each year?
- (c) Write an exponential equation showing how the value of the house increased. Don't forget to name the variables, including units.
- (d) Check that your equation gives the correct sold value.

Next, assume the value of the house increased linearly instead.

- (e) In this model, by what fixed amount did the house value increase each year?
Hint: calculate the slope.
 - (f) Write a linear equation showing how the value of the house increased.
 - (g) Check that your equation gives the correct sold value.
2. The number of manufacturing jobs in the state has been declining for decades. In 1970, there were 1.2 million such jobs in the state but by 2010 there were only .6 million such jobs. Write J for the number of manufacturing jobs (in millions) and Y for the years since 1970.

First, assume the number of jobs decreased linearly.

- (a) Calculate the slope.
- (b) Write a linear equation showing how the number of jobs declined.
- (c) Check that your equation gives the correct value for 2010.

Next, assume the number of jobs decreased exponentially instead.

- (d) Calculate the growth factor.
- (e) Write an exponential equation showing how the number of jobs declined.
- (f) Check that your equation gives the correct value for 2010.

Now, compare the models.

- (g) Complete the table of values.

year	1970	1990	2010	2020	2030
Y	0	20	40	50	60
J (if linear)					
J (if exponential)					

- (h) Draw a graph showing both models.

3. In December 2010, the popular mobile app game Angry Birds had 50 million downloads. Six months later (May 2011), the game had 200 million downloads. Let D denote the number of downloads of Angry Birds (in millions) and M the months since December 2010.
 - (a) Suppose that the number of downloads have been increasing at a *constant rate each month*. What type of equation is suggested here? Write that equation and use it to estimate the number of downloads in November 2011 (when $M = 11$)
 - (b) Suppose that the number of downloads have been increasing at a *fixed percentage each month*. What type of equation is suggested here? Write that equation and use it to estimate the number of downloads in November 2011 (when $M = 11$)
4. Bus fares are up to \$2.25 per ride during rush hour. Two different plans of increasing fares are being debated: 10¢ per year or 2.5% per year.
 - (a) Make a table comparing these two plans over the next decade. A **decade** is ten years.
 - (b) Draw a graph showing both options.
 - (c) As a city council representative, you want to support the plan that your constituents prefer. If most of your constituents ride the bus, which plan should you support?
 - (d) If most of your constituents are members of the same union as the bus drivers (who count on solid earnings from the bus company to keep their jobs), then which plan should you support?
 - (e) Which type of equation is being suggested in each plan?
 - (f) Write the equations. Don't forget to name the variables, including units.

5.5 Logistic and other growth models

1. Corn farmers say that their crop is healthy if it is “knee high by the Fourth of July.” An equation that relates the height H (in inches) of the corn crop as it matures is the following, where D is days since May 1:

$$W = 106 - 100 * .989^D$$

- (a) According to this equation, how high is corn expected to be on the Fourth of July (day 64)? Is that “knee high”? Let’s say that’s 18 inches tall.
 - (b) These days with stronger corn from cross-breeding and various seed technologies, the rule ought to be modified to “chest high.” Let’s say that’s 52 inches tall. According to this equation, on approximately what date is the corn projected to be that tall? Use successive approximation to answer.
 - (c) The particular corn matures in approximately 110 days (by August 19). How tall will it be then?
 - (d) Draw a graph of the function.
2. An alternative equation for corn height is

$$C = \frac{200}{1 + 70 * .965^D}$$

- (a) According to this new equation, how high is corn expected to be on the Fourth of July (day 64)? Is that “knee high” (18 inches tall)?
 - (b) According to this new equation, on approximately what date is the corn projected to be “chest high” (52 inches tall)? Use successive approximation to answer.
 - (c) The particular corn matures in approximately 110 days (by August 19). How tall will it be then?
 - (d) Add the graph of this function to your graph of the original function.
3. Following the 2011 Japanese earthquake and tsunami there was concern of radiation leaking from nuclear power plants. A monitoring station near the Fukushima Daiichi recorded radiation according to the following equation, where R is radiation measured in milliSieverts (mSv for short) and T is time in hours:

$$R = \frac{.162}{1 + 3,319 * .3127^T}$$

- (a) How much radiation was detected at the start (0 hours)? After 24 hours? 48 hours?
- (b) At how many mSv did radiation levels level off?
- (c) A typical person is exposed to around 2.4 mSv in a year. How many is that in a day? (Use 365 days/year.)

- (d) Did the detected radiation exceed normal (at its highest value where it leveled off)? If so, by how many times normal? *That means divide your answer to (b) by your answer to (c).*
4. Jason works at a costume shop selling Halloween costumes. The shop is busiest during the fall before Halloween. An equation that describes the number of daily visitors V the shop receives D days from August 31 is the following:

$$V = \frac{430}{1 + 701 * .81^D}$$

an alternative equation is

$$V = 700 - 690 * .985^D$$

- (a) Make a table showing what each equations projects for August 31, September 15, September 30, October 15, October 25, October 28, October 31
- (b) Graph both functions on the same set of axes.
- (c) Which function is more consistent with a major advertising campaign that aired starting the first week of September? Explain.

Notes

8-2

Using the word "addition" here is distracting?

13-1

What is his total cost of coffee?

14-1

Graphing price or rate of change?