DLUTIONS

Approximating solutions of equations - Practice exer-2.4 cises

1. The size of a round pizza is described by its diameter (distance across). Assuming a 16-inch diameter pizza serves four people, and with a little geometry to help us out, we calculated that a pizza of diameter D inches serves P people where

$$P = .015625D^2$$

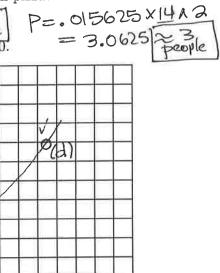
Story also appears in 3.3 #1 and 4.1 #3

(a) Confirm that a 16-inch pizza serves four people.

P=.015625
$$\Re 16^3$$
 =.015625 $\times 16^4$

(b) How many people does a 12-inch pizza serve? A 14-inch pizza?

$$P = .015625 \times 18 \land 2 = 2.25 \approx 2$$
 (c) Graph the function. Include what happens when $D = 0$.



diameter pizza (d) A personal pizza is sized to serve one person. Use successive approximation to estimate the diameter of a personal pizza to the nearest inch.

12

10

8

D	0	12	8
P	0	2	A
VSI	IDM	high	yes:

a

6

5

2

= B inches

14

16

18

(e) What diamter should an extra large pizza be to serve 6 people? Answer to the nearest 1/10 inch.

1	in		10.	19	19 <	197	19.6
	16	20	10		1100	1 10 1	
D	4	6.25	5,0625	5,640	5.941	6.063	6.0025
VSG	low	high	bw	low	low	high	

219.6 inches

2. Suppose a car gas tank is designed to hold enough fuel to drive 350 miles. (That's fairly average.) A hybrid car with fuel efficiency of 50 miles per gallon (mpg) would only need a 7 gallon gas tank, but a recreational vehicle that gets only 10 mpg would need a 35 gallon gas tank.

Story also appears in 3.3 #3

5-7

(a) Name the variables including units. The way the story is stated, the size tank is a function of the fuel efficiency.

50 mpg * 7 gal = 350mi

(b) Write an equation describing this function. $f \not \star G = 350 \implies \boxed{G = \frac{350}{F}}$

check: $\frac{350}{50} = 7\sqrt{\frac{350}{10}} = 35\sqrt{\frac{350}{10}}$

(c) My Honda Accord's tank holds about 16 gallons. Approximate the corresponding

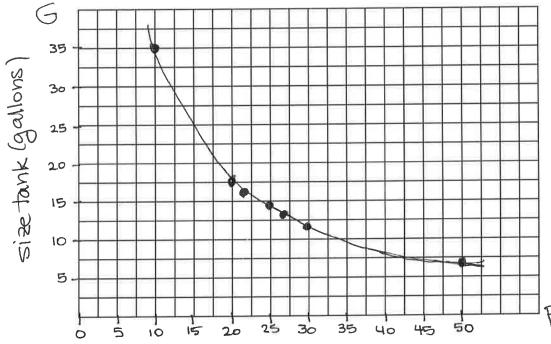
fuel effici	ency to on	e decimal	place.				-	121 91.
FI	120	25	23	21	21	21.5	21.8	21.1
16	17.5	14	15.2	15.9	16.6	16.27	16.05	15.98
V516	high	low	IOW	low	high	high	high	low
	11	1		18	10 1	1 A		11

(d) My ex-husband's Honda Civic's tank holds only 13 gallons. Approximate the

12.96	12110	high		
10 01	10 111	12 21	13.061	12,011
27	26			
	27	27 26	20 20	27 26 26.5 26.8

≈26.9 Mpg

(e) Draw a graph showing how the size tank depends on the fuel efficiency



assorted values:

F G 7 35 17.5 16 25 11.7 26.9 13

fuel efficiency (mpg)

3. Monty hopes to grow or chids but they are fragile plants. He will consider his greenhouse a success if at least nine of the ten or chids survive. Assuming the or chids each survive at rate S, the probability his greenhouse is a success, P, is given by

$$P = 10S^9 - 9S^{10}$$

Story also appears in 2.3 #3

remember to plug in . 8 both places for S

(a) Monty can buy orchids each with survival rate of S = .8. Is that enough to give probability $P \ge .8$ of a successful greenhouse?

No, S=.8 is not enough. In fact, it's not close to enough.

(b) What quality of orchids would Monty need to have probability $P \geq .8$ of a successful greenhouse? Answer to two decimal places.

To have P > . B, you'd need each orchid to have survival rate 5 2.92

(c) What quality of orchids would Monty need to have probability $P \geq .95$ of a successful greenhouse? Answer to three decimal places.

To have P≥.95, you'd need each orchid to have survival vate S≈.964

4. After China, India, and the United States, the next five most populous countries (in 2011) are Indonesia, Brazil, Pakistan, Nigeria, and Bangladesh. Their projected growth rates and corresponding equation are listed below. Here Q is the population Source: CIA Factbook measured in millions and Y is the years since 2011.

$4^{ m th}$	Indonesia	pop. 248 million	growth rate 1.04%	$Q = 248 * 1.0104^{Y}$
$5^{ m th}$	Brazil	pop. 205 million	growth rate 1.10%	$Q = 205 * 1.0110^{Y}$
$6^{ m th}$	Pakistan	pop. 190 million	growth rate 1.55%	$Q = 190 * 1.0155^{Y}$
$7^{ m th}$	Nigeria	pop. 170 million	growth rate 2.55%	$Q = 170 * 1.0255^{Y}$
$8^{ m th}$	Bangladesh	pop. 161 million	growth rate 1.58%	$Q = 161 * 1.0158^{Y}$

(a) Which of these cou 2030? In 2050? Y	ntries is projected to Y= 2020 2020	have the largest por Y=19	pulation in 202 Y= 39 2050	Indonesia in 2020 and
Indonesia	(272.2)	(301.9)	371.3	- shill in 2030.
Brazil	226.2	252,4	314.7	
Pakistan	218.2	254.5	346.2	- Nigeria
Nigeria	213.2	274.3	(453.9)	in 2050
Bangladesh	105.4	216.9	296.1	

(b) Explain why Bangladesh's population will not overtake Nigeria's, assuming these projections are accurate.

Bangladesh's population is smaller than Nigeria's and it's growing slower, so it can never overtake Nigeria's population.

(c) Approximately when will Brazil's population top 500 million? Will Nigeria get there first? Display your work in a table.

Brazil 39 50 100 70 80 85 83 82 81
$$V$$
 39 50 100 70 80 85 83 82 81 V 39 50 100 V 401.9 519.5 508.3 502.7 497 V 500 V 100 V high V 100 V high V 100 V high V 100 V high V 100 V 100