MATH 201 Fall 2025

PS4: Interpreting, using, estimating derivatives and second derivatives - Answer key qr

1. (1.5.5.7)

- (a) If a patient takes a dose of 50 mL of a drug, their body temperature will go up by like 0.75 degrees F.
- (b) deg F per mL
- (c) At a dosage of 50 mL, if the patient takes *one more* mL, they'll experience 0.02 degrees F *less* of temperature change.

2. (1.5.5.9)

- (a) $AV_{[40000,55000]} \approx -0.153$ dollars per mile.
- (b) $h'(55000) \approx -0.147$ dollars per mile. If the car has been driven 55000 miles, for each additional mile driven, we expect its value to drop by like 15 cents.
- (c) Probably h'(30000) < h'(80000) (but |h'(30000)| > |h'(80000)|). Negative numbers are annoying.
- (d) h(m) is always decreasing and always c.u. and probably tends to zero. h'(m) is always negative and probably also tends to zero. (therefore it is c.d.)

3. (1.6.6.12)

(a)
$$h'(4.5) \approx 14.3$$

 $h'(5) \approx 21.2$
 $h'(5.5) \approx 23.9$

- (b) $h''(5) \approx 9.6$
- (c) acceleration; (feet per second) per second
- (d) 0 < t < 2, and then 6 < t < 10.