# The Lime Instruction Set Manual

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### Introduction

The philosophy behind our design prioritizes short and uniformly sized instructions that are executed in a single clock cycle. We have tried to create an architecture that achieves this with minimal difficulty for the programmer. Our architecture sometimes requires the programmer to use multiple instructions for actions that would require only one in other architectures, but we believe this inconvenience is worth the compact and simple instructions.

Despite the small size of our 16-bit instructions, we can still handle immediate that are up to 16 bits using our special UI register. This ensures that our architecture does not sacrifice performance for uniform instruction sizes and can access 16-bit addressed memory and use large immediate in operations. For convenience, many of our instructions maximize the small portion of the immediate that is part of the instruction, so the UI register does not need to be changed for most operations.

## Performance

#### Introduction

Performance measurement is crucial for evaluating the effectiveness of the Lime architecture. In this section, we discuss the metrics, methodology, and tools used to assess the performance of our processor.

### **Performance Metrics**

The lime structure utilized multi cycle design and greatly utilized the two edges of clock signal, which leads to a better performance over RISC-V on some algorithm.

# Registers

## Programmable Registers

Register	Name	Description	Saver
x0	ra	Return address	Caller
x1	sp	Stack pointer	Callee
x2	s0	Saved register	Callee
x3	t0	Temporary register	Caller
x4	t1	Temporary register	Caller
x5	t2	Temporary register	Caller
x6	a0	Procedure argument (and return)	Caller
x7	a1	Procedure argument	Caller

# **Special Registers**

## Non-Programmable Registers

Register	Name	Description
UI	Upper Immediate	For storing the most significant 13 bits of large immediate using lui instruction. They can then be used in 2RI instructions giving the least significant 3 bits as the immediate. This special register belongs to immediate generator.

# Memory

# Memory Allocation

Stack							
↓							
<b>↑</b>							
' '							
Dynamic Data							
Static Data							
Text							
Reserved							

## Register-Transfer Level (RTL) Component

## **Naming Convention**

The naming convention for RTL (Register-Transfer Level) components follows a systematic pattern to ensure clear and consistent identification of signals. This pattern involves specifying three key aspects for each signal: its type, direction, and name.

#### Direction

The signal name includes information about the direction of each signal, differentiating between inputs and outputs. Inputs that receive external data are denoted by the prefix  $input_{-}$ , while outputs that represent the results or data produced by the component are denoted by the prefix  $output_{-}$ .

#### Component

The signal name includes information about component. For instance, signals associated with Arithmetic Logic Unit (ALU) operations are labeled with prefixes such as *input\_ALU\_* or *output\_ALU\_*, indicating their connection to the ALU functionality.

#### Purpose

The signal name includes information about the purpose. This extra detail enhances understanding of each signal's role and functionality within the RTL component. For instance, the first ALU input is represented by *input\_ALU\_A*.

By following this systematic pattern, the naming convention not only improves readability but also provides crucial information about the role and characteristics of each signal in the RTL component. This approach promotes maintainability and ease of understanding for developers working with the hardware description of the component.

## RTL Summary

Components	Inputs	Outputs	Multicycle RTL Symbols
ALU	input_ALU_A[15: 0] input_ALU_B[15: 0] input_ALU_ALUOp[2: 0]	output_ALU[15: 0] output_ALU_Zero[0: 0] output_ALU_negative[0: 0]	ALU(operation, input_A, input_B)
Memory	input_mem_write[0:0] input_mem_addr[15:0] input_mem_data[15:0] CLK[0:0]	output_mem_data[15:0]	mem[address]
Immediate Generator	input_imm[15: 0] CLK[0: 0]	output_imm[15:0]	imm[15: 0] UI[12: 0]
Control	$input\_control[6:0]$	output_control_branch[0:0] output_control_memRead[0:0] output_control_ALUOp[2:0] output_control_memWrite[0:0] output_control_ALUSrc[0:0] output_control_regWrite[0:0] output_control_branchType[1:0]	None (not used in RTL)
Program Counter	input_PC_PCWrite input_PC_newPC CLK[0:0]	output_PC[15:0]	PC[15:0]
Programmable Register File	input_reg_readA_address[2:0] input_reg_readB_address[2:0] input_reg_write[0:0] input_reg_write_value[15:0] input_reg_write_address[2:0] CLK[0:0]	output_reg_A[15:0] c[15:0]	Reg[index]
Instruction Register	input_IR_Instru[15:0] input_IR_write[0:0] CLK[0:0]	<pre>output_IR_Control[6:0]   output_IR_RegA[3:0]   output_IR_RegB[3:0]   output_IR_RegD[3:0]   output_IR_Imm[15:0]</pre>	IR[end: start] IR = mem[PC]
Simple Register	input_SR[15: 0] CLK[0: 0]	output_SR[15:0]	A B MDR ALUOut

### Arithmetic Logic Unit (ALU)

#### Inputs:

- input\_ALU\_A[15:0]: 16-bit input representing the first operand for the ALU.
- **input\_ALU\_B[15:0]**: 16-bit input representing the second operand for the ALU.
- **input\_ALU\_ALUOp[2:0]**: 3-bit input specifying the ALU operation code.

### Outputs:

- **output\_ALU[15:0]**: 16-bit output representing the result of the ALU operation.
- **output\_ALU\_Zero[0:0]**: Single-bit output indicating whether the ALU result is zero (0) or not.
- **output\_ALU\_negative[0:0]**: Single-bit output indicating whether the ALU result is negative or not.

#### Behavior:

- The ALU performs operations based on input\_ALUOp, including addition, subtraction, bit shifts, logical AND/OR/XOR, multiplication, and special calculation.
- Output flags indicate if the result is zero or negative.

#### Multicycle RTL Symbols:

 ALU(operation, input\_A, input\_B): Output of ALU with given operation and inputs.

- Test all operations with arbitrary inputs to ensure correct behavior.
- Test all operations with edge cases (max, min, and zero values).
- Test flag functionality during subtraction operation.
- Ensure all operations complete within the cycle before the greatest possible delay.

### Memory

### Inputs:

- **input\_mem\_write[0:0]**: Single-bit input indicating when a write instruction is enabled.
- **input\_mem\_addr[15:0]**: 16-bit input representing the memory address for read or write operations.
- **input\_mem\_data[15:0]**: 16-bit input representing the data to be written into the memory when a write instruction is enabled.
- **CLK[0:0]**: Clock signal.

#### Outputs:

• **output\_mem\_data[15:0]**: 16-bit data from the memory at the specified address.

#### Behavior:

- On the rising edge of the clock (CLK), reads 16-bit data at the memory address specified by **input\_mem\_addr** and outputs it to **output\_mem\_data**.
- If input\_mem\_write is 1, writes data from input\_mem\_data to the address specified by input\_mem\_addr.

### Multicycle RTL Symbols:

• mem[address]: the 16 bit value at this memory address

- Test read and write operations for arbitrary memory addresses with arbitrary data.
- Ensure proper timing on read and write operations (should take one cycle).

### Immediate Generator (IG)

#### Inputs:

- **input\_imm[15:0]**: 16-bit input of the instruction for the immediate to be parsed.
- **CLK[0:0]**: Clock signal.

#### Outputs:

• **output\_imm[15:0]**: 16-bit output representing the immediate value generated by the Immediate Generator.

#### Behavior:

- Generates a 16-bit immediate value based on the opcode.
- For 2RI instructions, appends a 3-bit immediate in the instruction to the upper 13 bits of the upper immediate register.
- For lui instructions, stores the 13-bit immediate value in the instruction in its upper immediate register for later use.

#### Multicycle RTL Symbols:

- IG[15:0]: the output of immediate generator (the 16 bit calculated immediate)
- UI[12:0]: the value stored in the UI register that is used for immediate in 2RI instruction types

- Test for proper interpretation of instructions for all instruction formats.
- Validate correct immediate concatenation for RI types.
- Ensure proper sign extension when applicable.
- Verify proper timing, ready for ALU and PC applications in the same cycle the instruction is available.
- Ensure *lui* instruction takes only one cycle.

#### Control

#### Inputs:

• input\_control[6:0]: The opcode + funct4.

#### Outputs:

- **output\_control\_branch[0:0]**: 1 if it's a branch instruction, 0 otherwise.
- **output\_control\_memRead[0:0]**: 1 if reading from memory, 0 otherwise.
- **output\_control\_ALUOp[2:0]**: ALU operation (+, -, and, or, ...).
- **output\_control\_memWrite[0:0]**: 1 if writing to memory, 0 otherwise.
- **output\_control\_ALUSrc[0:0]**: 1 if using immediate, 0 otherwise.
- output\_control\_regWrite[0:0]: 1 if the instruction involves writing to a register,
   0 otherwise.
- **output\_control\_branchType[1:0]**: Specifies the type of branch instruction based on two bits (00 for beq, 01 for blt, 10 for bne, 11 for bge).

#### Behavior:

- Interprets the 3 opcode bits of the instruction to know what bits are what.
- If necessary, reads func4 bits to determine the appropriate ALU operation and sends this to the ALU.

### Multicycle RTL Symbols:

• None (not used in RTL).

- Test for proper interpretation of opcode and func4.
- Validate proper control signal output for every instruction.
- Ensure proper timing (control signals should be available shortly after the instruction is available).

## **Program Counter**

#### Inputs:

- **input\_PC\_PCWrite**: A flag indicating whether the Program Counter (PC) will be updated.
- **input\_PC\_newPC**: The new value for the Program Counter (PC).
- **CLK[0:0]**: The clock signal.

#### Outputs:

• **output\_PC[15:0]**: The value of the Program Counter, representing the address of the instruction.

#### Behavior:

- On the falling edge of the clock (CLK), if the input\_PC\_PCWrite flag is asserted, the PC undergoes an update.
- The PC's value is set to the new value specified by input\_PC\_newPC.
- If the **input\_PC\_PCWrite** flag is not asserted, the Program Counter (PC) remains unchanged, maintaining its current value.

### Multicycle RTL Symbols:

• PC[15:0]: The instruction address value held in PC.

- Test for proper incrementing of the Program Counter.
- Validate correct jumping/branching behavior.
- Ensure proper PC output.
- Test for edge cases (max/min values) to verify robustness.
- Validate that the PC is ready by the end of the last cycle for all instructions.

### Programmable Register File

#### Inputs:

- **input\_reg\_readA\_address[2:0]**: 3-bit address specifying the register location for reading Operand A.
- **input\_reg\_readB\_address[2:0]**: 3-bit address specifying the register location for reading Operand B.
- **input\_reg\_write[0:0]**: Single-bit signal to enable the write operation to the register.
- **input\_reg\_write\_value[15:0]**: 16-bit value to be written into the register when a write operation is enabled.
- **input\_reg\_write\_address[2:0]**: 3-bit address specifying the register location for writing data when **reg\_write** is enabled.
- **CLK[0:0]**: Single-bit clock signal used to synchronize read and write operations in the programmable register.

### Outputs:

- **output\_reg\_A[15:0]**: 16-bit output representing the data read from Register A.
- **output\_reg\_B[15:0]**: 16-bit output representing the data read from Register B.

#### Behavior:

- On the rising edge of the clock (CLK), if the reg\_set[0:0] input is 1, the register corresponding to the value of register\_id[0:2] is set to the input\_value[0:15].
- The **output\_value[15:0]** is set to the value of the register corresponding to **register\_id[0:2]**.

### Multicycle RTL Symbols:

• **Reg[index]**: The value of the register at this index.

- Test for writing arbitrary values to every register.
- Validate reading values from every register.
- Ensure proper timing on all registers for read and write (outputs should be ready in time for ALU to finish in that cycle).

## **Instruction Register**

#### Inputs:

- input\_IR\_Instru[15:0]: 16-bit input bus for storing the instruction data.
- **input\_IR\_write[0:0]**: Single-bit control signal indicating whether to write data into the instruction register.
- **CLK[0:0]**: Clock signal.

#### Outputs:

- **Output\_IR\_Control[6:0]**: 7-bit output signifying the opcode and func4 of the current instruction fetched from the Instruction Register (IR) [6:0]. Sent to the control module.
- **Output\_IR\_RegA[3:0]**: 3-bit output sourced from the Instruction Register (IR) [12:10], utilized in 3R and 2RI types to determine the address of register r1. Sent to the Programmable Register File.
- Output\_IR\_RegB[3:0]: 3-bit output obtained from the Instruction Register (IR) [9:7], employed in 3R types to specify the address of register r2. Sent to the Programmable Register File.
- Output\_IR\_RegD[3:0]: 3-bit output, extracted from the Instruction Register (IR) [12:10], used in 3R, 2RI, UJ, and RI types to identify the address of register rd. Sent to the Programmable Register File.
- **Output\_IR\_Imm[15:0]**: 16-bit output derived from the complete instruction in the Instruction Register (IR) [15:0]. Sent to the Immediate Generator.

#### Behavior:

- On the rising edge of the clock (CLK), receives a 16-bit instruction through the **input[15:0]** wire if **input\_ir\_write[0:0]** equals 1.
- Decodes the opcode and outputs it through output\_opcode.
- Identifies addresses for A and B, putting them to output\_reg\_A and output\_reg\_B.
- Sets the destination register address to **output\_reg\_dest**.

### Multicycle RTL Symbols:

- **IR[end:start]**: The respective bits of the instruction.
- IR=mem[PC]: Fetching the instruction at the address indicated by PC.

- Test for proper fetching of the instruction.
- Validate proper splitting of the instruction and sending it out.
- Ensure proper timing (instruction should be ready after the first cycle for all instructions).

## Simple Register

#### Inputs:

- input\_SR[15:0]: Input that updates every cycle.
- **CLK[0:0]**: Single-bit clock signal used to synchronize read and write operations in the register.

#### Outputs:

output\_SR[15:0]: Outputs the value in the register.

#### Behavior:

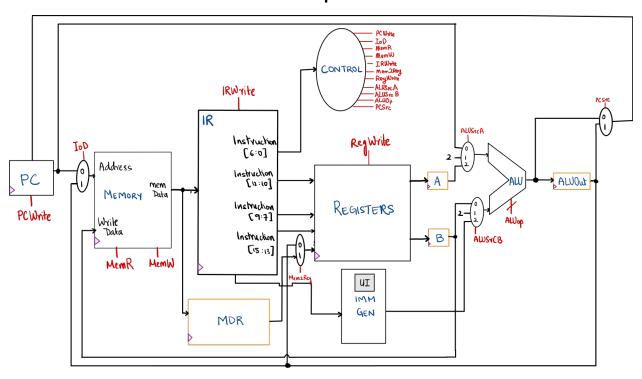
- On the falling edge of the clock (CLK), the register is set to the **input[15:0]**.
- The output is always the value currently in the register.

#### Multicycle RTL Symbols:

- **A**: Register storing the value for the next clock cycle, serving as input A for the ALU.
- **B**: Register storing the value for the next clock cycle, serving as input B for the ALU.
- MDR: Memory Data Register, storing data fetched from memory.
- ALUOut: Output of the Arithmetic Logic Unit (ALU).

- Test for reading of input.
- Validate outputting value.
- Ensure proper timing.

# Datapath



▶ 7ime Signal

## Instructions

## Core Instruction Formats

All our instructions are 16 bits.

All memory addresses are 16 bits.

All 8 programmable registers have 16-bit values and 3-bit identifiers.

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	Type Name
rd	rd r1 r2				fun	c 4			opcod	e		3R type				
imr	mmediate [ 12 : 0 ] opcode														L type with a special register	
rd			r1			imn [ 2 :		ate	fun	c 4			opcod	e		2RI type
rd immediate [ 9 : 0 ] opcode												UJ type				
rd	rd immediate [ 5 : 0 ] func 4										opcod	e		RI type		

## Instruction RTL

Cycles	3 <i>R</i>	RI	2RI	lw/sw									
1			PC = ALU(+, PC, 2) IR = Mem([PC]) ALUOut = ALU(+, PC)	C,2)									
2	A = Reg[IR[12:10]] $B = Reg[IR[9:7]]$												
3	$\begin{array}{l} ALUOut \\ = ALU(ALUOp, A, B) \end{array}$	ALUO1 = ALU	ut I(ALUOp, A, IG([9:7]))	ALUOut = ALU(2+, A, IG([9:7]))									
4	4) Reg[IR[15:	13]] =	ALUOut	lw: MDR = Mem[ALUOut] sw: Mem[ALUOut] = Reg(IR[15:13])									
5				lw: Reg(IR[15:13]) = MDR									

Cycles	jalr	Branch	jal	lui
1		PC = ALU(+, PC, 2) IR = Mem([PC]) ALUOut = ALU(+, PC, 2)		
2	Reg(IR[15:13]) = ALUOut $PC = ALU(*,2,IG([9:7]))$	A = Reg[IR[12:10]] B = Reg[IR[15:13]]	PC = ALU(*,2,IG([12:3]))	
3		ALUOut = ALU(2+, PC, IG([9:7]))		
4		If (A branchType B) PC = ALUOut		

## Table of Instructions

## 3R Type

15	14	13	3	12	11	10	9	8	7	6	5	4	3	2	1	0	Type Name
rd				r1			r2			fund	c 4			opcod	e		3R type

Instructio		Instruction				
n	Name	Type	func 4	Opcode	Description	Note
add	add	3 <i>R</i>	0000	000	R[rd] = R[r1] + R[r2]	
sub	subtract	3 <i>R</i>	0001	000	R[rd] = R[r1] - R[r2]	
and	and	3 <i>R</i>	0010	000	R[rd] = $R[r1] & R[r2]$	
or	or	3 <i>R</i>	0011	000	$R[rd] = R[r1] \mid R[r2]$	
xor	xor	3 <i>R</i>	0100	000	$R[rd]$ = $R[r1] ^ R[r2]$	
sll	shift left logical	3 <i>R</i>	0101	000	R[rd] = R[r1] < < R[r2]	
srl	shift right logical	3 <i>R</i>	0110	000	R[rd] = R[r1] > $ > R[r2]$	
sla	shift left arithmeti c	3 <i>R</i>	0111	000	R[rd] = R[r1] < < R[r2]	sign extends
sra	shift right arithmeti c	3 <i>R</i>	1000	000	R[rd] = R[r1] > $ > R[r2]$	sign extends

# 2RI Type

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	Type Name
	rd			r1		imn		ate		fur	ıc 4		opcod	e		2RI type

Instruc		Instr	func	Opcod		
tion	Name	Туре	4	е	Description	Note
addi	ADD Immediat e	2RI	0000	001	R[rd] = R[r1] + OR(UI, imm)	
xori	XOR Immediat e	2RI	0001	001	$R[rd] = R[r1]^OR(UI, imm)$	
ori	OR Immediat e	2RI	0010	001	R[rd] = R[r1]   OR(UI, imm)	
andi	AND Immediat e	2RI	0011	001	R[rd] = R[r1] & OR(UI,imm)	
subi	SUB Immediat e	2RI	0100	001	R[rd] = R[r1] - OR(UI, imm)	
slli	Shift Left Logical Imm	2RI	0101	001	R[rd] = R[r1] < < OR(UI, imm)	
srli	Shift Right Logical Imm	2RI	0110	001	R[rd] = R[r1] > > OR(UI, imm)	
srai	Shift Right Arith Imm	2RI	0111	001	R[rd] = R[r1] > OR(UI, imm)	
lw	Load Word	2RI	1000	001	R[rd] = M[2 * (R[r1] + OR(UI, imm))]	

SW	Store Word	2RI	1001	001	M[2 * (R[r1] + OR(UI, imm))] = R[rd]	multiplied by 2
jalr	Jump And Link Reg	2RI	1010	001	R[rd] = PC + 2; PC = R[rs1] + OR(UI, imm)	multiplied by 2
beq	Branch if equal	2RI	1011	001	if(R[rd] == R[r1]) PC+= 2 * OR(UI, imm)	PC relative and multiplied by 2
blt	Branch if less than	2RI	1100	001	if(R[rd] < R[r1]) PC+= 2 * OR(UI, imm)	PC relative and multiplied by 2
bne	Branch if	2RI	1101	001	if(R[rd]! = R[r1]) PC+= OR(UI,imm)	PC relative and multiplied by 2
bge	Branch if greater or equal	2RI	1110	001	$if(R[rd] \ge R[r1])$ PC+= 2 * OR(UI, imm)	

# RI Type

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	Type Name
rd			imr	ned	iate	[5:	0]		fun	c 4			opcod	e		RI type

Instruction	Name	Instr Typ e	func 4	Oncode	Description	Note
mstruction	Ivairie		Turic 4	Opcode	Description	INOLE
inc	Increment Immediate	RI	0000	010	R[rd] = $R[rd]$ - $SE(imm)$	
dec	Decrement Immediate	RI	0001	010	R[rd] = R[rd] - SE(imm)	
slipl	Shift Left in Place logical	RI	0010	010	R[rd] = R[rd] < < SE(imm)	
sripl	Shift Right in Place logical	RI	0011	010	R[rd] = R[rd] > SE(imm)	
slipa	Shift Left in Place arithmetic	RI	0100	010	R[rd] = R[rd] < < SE(imm)	Sign Extend s
sripa	Shift right In Place arithmetic	RI	0101	010	R[rd] = R[rd] > > SE(imm)	Sign Extend s
set	Set	RI	0110	010	R[rd] = SE(imm)	Sign Extend s

## L Type

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	Type Name
im	medi	iate	[ 12	: 0 ]									opcod	е		L type with a special register

Instructio n	Name	Instr Type	func 4	Opcod e	Description	Note
lui	load Upper Immediat e	L	-	011	UI = immediate[12:0]	sets non- programable UI (upper immediate) register to be used with 2RI instructions

# UJ Type

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0	Type Name
rd			imr	ned	iate	[9:	0]						opcod	е		UJ type

Instruc tion	Name	Instr Type	func 4	Opcod e	Description	Note
jal	Jump and Link	UJ	-	100	PC = 2 * imm[9:0]	moves execution to the instruction at address 2*(immediate 9:0)

# **Assembly Examples**

## while loop

## C Code

```
    int main () {
    int a = 5;
    while(a < 20) {</li>
    a++;
    }
    return a;
    }
```

## Assembly Code

Address	Assembly	Machine Code	Comment
	main:		
0x0000	addi a0, a0, 5	110 110 101 0000 001	//a = 5
0x0002	addi t0, t0, 7	011 011 111 0000 001	// t0 = 7
	loop:		
0x0004	bge a0, t0, loop_end	110 011 [011] 1110 001	// if (a < 7)
0x0006	addi a0, a0, 1	110 110 001 0000 001	// a + +
0x0008	jal t1, loop	100 [0 0000 0010]100	
	loop_end:		
0x000A	jal t1, 0(ra)	100 000 000 1010 001	// return a

## **Array Access**

C code:

```
1. int main(){
   2. int[] array = int[20];
   3. for(int i=0; i < array.length; <math>i++){
   4.
5. }
           array[i]=array[i] * 2
   6. }
Assembly Code:
main:
      lui [array address]
loop:
      bgt t0
set t0, 0 //t0 is i
      lw t1, 0(t0)
      inc t1
                   //inciment t1
      jal a0, loop
```

## Recursion

## C code:

```
    int simpleRecursion(int n) {
    if (n == 0) {
    return 1;
    }
    else {
    return simpleRecursion(n - 1);
    }
```

## Assembly code

Address	Assembly	Machine Code	Comment
	simpleRecursion:		
0x0000	subi sp, sp, 2	001 001 010 0100 001	
0x0002	sw ra, 0(sp)	000 001 000 1001 001	
	// Base case: if n == 0, return 1		
0x0004	addi t0, t0, 0	110 110 000 0000 001	
		110 011 [101] 1011	
0x0006	beq a0, t0, base_case	001	
	<ul><li>// Recursive case: return simpleRecursion(n</li><li>- 1)</li></ul>		
0x0008	subi a0, a0, 1	101 101 001 0100 001	
0x000A	jal ra, simpleRecursion	000 [0 0000 0101] 100	
0x000C		000 110 000 1000 001	
0x000E	jal ra, end_recursion	000 [0 0000 0010] 100	
	base_case:		
0x0010	addi a0, a0, 1 // Return 1 for the base case	110 110 001 0000 001	

	end_recursion:		
0x0012	lw ra, 0(sp)	001 001 000 1000 001	
0x0014	add sp, sp, 2	001 001 010 0000 001	
0x0016	jalr t1, 0(ra)	100 000 000 1010 001	

## relPrime and Euclid's Algorithm

#### C Code

```
1. // Find m that is relatively prime to n.
int relPrime(int n)
3. {
4.
    int m;
5.
6.
     m = 2;
7.
     while (\gcd(n, m) != 1) \{ // n \text{ is the input from the outside world } \}
8.
9.
      m = m + 1;
10. }
11.
12. return m;
13.}
14.
15. // The following method determines the Greatest Common Divisor of a and b
16. // using Euclid's algorithm.
17. int gcd(int a, int b)
18. {
19. if (a == 0) {
20. return b;
21. }
22.
23. while (b != 0) {
24. if (a > b) {
25. a = a - b;
26. } else {
27. b = b - a;
28. }
29. }
30.
31. return a;
32.}
```

## Assembly Code

Address	Assembly	Machine Code	Comment
	relPrime:		
0x0000	lui 0	000000000000000011	// Make Sure UI is Set to 0
0x0002	subi sp, sp, 4	001 001 100 0100 001	// Increase Stack by -4 Bytes for 2 16-Bit Values
0x0004	sw ra, 0(sp)	000 001 000 1001 001	// Save Return Address
0x0006	sw a0, 1(sp)	110 001 001 1001 001	// Store n in the Second Part of the Stack (Note: sw Multiplies Imm by 2)
0x0008	set a1, 2	111 000010 0110 010	// Set m = 2
0x000A	set s0, 1	010 000001 0110 010	// Set s0 = 1
	loop:		
0x000C	jal ra, gcd	000 [0 0000 1111] 100	// Jump to gcd Function, Result in a0
0x000E	beq a0, s0, exit_loop	110 010 [100] 1011 001	// If gcd = 1, Exit the Loop
0x0010	lw a0, 1(sp)	000 110 001 1000 001	// Else, prepare for next gcd calling, set a0 = n
0x0012	addi a1, a1, 1	111 111 001 0000 001	// Increment m: m = m + 1
0x0014	jal t0, loop	011 [000000110] 100	// Next Iteration
	exit_loop:		
0x0016	addi a0, a1, 0	110 111 000 0000 001	// Set Return Value to m
0x0018	lw ra, 0(sp)	001 001 000 1000 001	// Load Return Address from Stack
0x001A	addi sp, sp, 4	001 001 100 0000 001	// Restore Stack
0x001C	jalr t0, 0(ra)	011 000 000 1010 001	// Return to Caller
	gcd:		// gcd Function Label (a=a0, b=a1)
0x001E	set t0, 0	011 000000 0110 010	// t0 = 0
0x0020	bne a0, t0, gcd_loop	110 011 [011] 1101 001	// If a != 0, Skip to Loop
0x0022	add a0, a1, t0	110 111 011 0000 000	// set b as a return value
0x0024	jalr t0, 0(ra)	011 000 000 1010 001	// Return b if a = 0
	gcd_loop:		
0x0026	bne a1, t0, gcd_end	111 011 [110] 1101 001	// if $b == 0$ , end loop
0x0028	bge a0, a1, greater	110 111 [011] 1110 001	// If a > b, jump to greater
0x002A	sub a1, a1, a0	111 111 110 0001 000	// b = b - a
0x002C	jal t0, gcd_loop	110 [000001101] 100	// Next Iteration
	greater:		
0x002E	sub a0, a0, a1	110 110 111 0001 000	// a = a - b

0x0030	jal t0, gcd_loop	011 [000001101] 100	// Next Iteration
	gcd_end		// gcd_end Label
0x0032	jalr t0, 0(ra)	011 000 000 1010 001	// back to caller