ME 639

INTRODUCTION TO ROBOTICS

Assignment 2

Submitted by:

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CONTENTS

1.	Question 1	1
2.	Question 2	2
3.	Question 3	4
4.	Question 4	6
5.	Question 5	8
6.	Question 6	10
7.	Question 7	13
8.	Question 8	15
9.	Question 9	17
10.	Question 10	18
11.	References	20

91

The prove
$$\rightarrow$$
 R S(a) R^T = S(Re)

Set $a = \begin{bmatrix} \alpha \\ \beta \\ -8 \end{bmatrix}$, $R = Rz, \theta^{2} \begin{bmatrix} 1 & 0 & 0 \\ 0 & us \theta & -sin \theta \\ 0 & un \theta & us \theta \end{bmatrix}$

$$S(a) = \begin{bmatrix} 0 & -8 & \beta \\ -8 & 0 & -\alpha \\ -\beta & \alpha & 0 \end{bmatrix}, RT = \begin{bmatrix} 1 & 0 & 0 \\ 0 & us \theta & sin \theta \\ 0 & -sin \theta & us \theta \end{bmatrix}$$

Re $= \begin{bmatrix} 1 & 0 & 0 \\ 0 & us \theta & -sin \theta \\ 0 & sin \theta & us \theta \end{bmatrix}$

$$Ra = \begin{bmatrix} 1 & 0 & 0 \\ 0 & us \theta & -sin \theta \\ 0 & sin \theta & us \theta \end{bmatrix}$$

$$Ra = \begin{bmatrix} 1 & 0 & 0 \\ 0 & us \theta & -sin \theta \\ 0 & sin \theta & us \theta \end{bmatrix}$$

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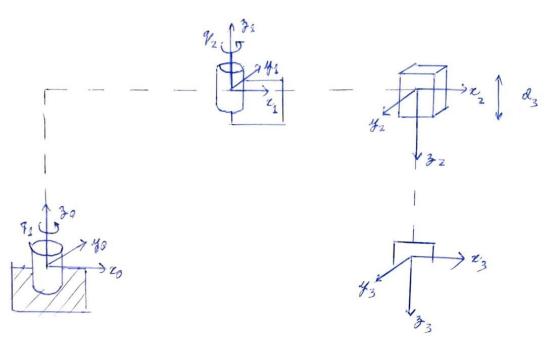
$$Ra = \begin{bmatrix} 1 & 0 & 0 \\ 0 & sin \theta & us \theta \\ 0 & sin \theta & us \theta \end{bmatrix}$$

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$$Ra = \begin{bmatrix} 1 & 0 & 0 \\ 0 & sin \theta & us \theta \\ 0 & sin \theta & us \theta \end{bmatrix}$$

$$Ra = \begin{bmatrix} 1 & 0 & 0 \\ 0 & sin \theta & us \theta \\ 0 & sin \theta & us$$





Here,
$$R_3 = \begin{bmatrix} 0 \\ -e_3 \end{bmatrix}$$
, $R_2 = R_3, 0 = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

$$d_2 = \begin{bmatrix} 0 \\ e_2 \\ -e_3 \end{bmatrix}$$
, $R_3 = R_3, q_2 = \begin{bmatrix} \cos q_2 & -\sin q_2 & 0 \\ \sin q_2 & \cos q_2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

$$d_1^2 = \begin{bmatrix} 0 \\ e_1 \\ 0 \end{bmatrix}$$
, $R_0^2 = R_3, q_2 = \begin{bmatrix} \cos q_2 & -\sin q_1 & 0 \\ \sin q_1 & \cos q_2 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

Maw,
$$H_0^2 = \begin{bmatrix} R_0^2 & d_0^2 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos q_1 & -\sin q_1 & 0 & 0 \\ \sin q_1 & \cos q_2 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_{1}^{2} = \begin{bmatrix} R_{1}^{2} & R_{1}^{2} \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos q_{2} & -\sin q_{2} & 0 & 0 \\ \sin q_{2} & \cos q_{2} & 0 & \ell_{1} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$H_{2}^{3} = \begin{bmatrix} R_{2}^{3} & d_{2}^{3} \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & l_{2} \\ 0 & 0 & 1 & -l_{3} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 2 \\ y \\ 3 \end{bmatrix} = \begin{bmatrix} \cos q_1 & -i \cos q_2 & 0 & 0 \\ i \cos q_1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos q_2 & -i \sin q_2 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -d_3 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Source Code: (Link to GitHub)

```
import numpy as np
Program to calculate the end effector position vector for an RRP SCARA robot.
Parameters:
q1 = Angle of Joint 1
q2 = Angle of Joint 2
d3 = Extension length of the robot arm
11 = Length of Link 1
12 = Length of Link 2
def scara_fwd_kin(q1, q2, 11, 12, d3):
   x = 11 * np.cos(q1) + 12 * np.cos(q1 + q2)
   y = 11 * np.sin(q1) + 12 * np.sin(q1 + q2)
   z = d3
   return x, y, z
11 = float(input("Enter length of Link 1 (m): "))
12 = float(input("Enter length of Link 2 (m): "))
q1 = np.radians(float(input("Enter angle of Joint 1 (deg): ")))
q2 = np.radians(float(input("Enter angle of Joint 2 (deg): ")))
d3 = float(input("Enter extension length (m): "))
x, y, z = scara_fwd_kin(q1, q2, l1, l2, d3)
print("\nEnd effector position :")
print("x = ", str(x)," m, y = ", str(y), " m, z = ", str(z), " m")
input()
```

Output:

```
Enter length of Link 1 (m): 2
Enter length of Link 2 (m): 2
Enter angle of Joint 1 (deg): 30
Enter angle of Joint 2 (deg): 45
Enter extension length (m): 1

End effector position:
x = 2.249688897773919 m, y = 2.9318516525781364 m, z = 1.0 m
```

Source Code: (Link to GitHub)

```
import numpy as np
Program to calculate the end effector position vector for an RRP Stanford
robot.
Parameters:
q1 = Angle of Joint 1
q2 = Angle of Joint 2
11 = Length of Link 1
12 = Length of Link 2
13 = Length of link 3
d3 = Linear displacement
def stanford_fwd_kin(q1, q2, l1, l2, l3, d3):
    P3 = np.array([13, 0, 0, 1])
    H_01 = np.array([
                         [np.cos(q1), np.sin(q1), 0, 0],
                         [-np.sin(q1), np.sin(q1), 0, 0],
                         [0, 0, 1, 0],
                         [0, 0, 0, 1]
                    ])
    H_12 = np.array([
                         [np.cos(q2), -np.sin(q2), 0, 0],
                         [0, 0, -1, 0],
                         [np.sin(q2), np.cos(q2), 0, \overline{11}],
                         [0, 0, 0, 1]
                    1)
    H_23 = np.array([
                         [1, 0, 0, 12 + d3],
                         [0, 1, 0, 0],
                        [0, 0, 1, 0],
                         [0, 0, 0, 1]
                    ])
    P0 = np.dot(np.dot(np.dot(H_01, H_12), H_23), P3)
    return P0
```

```
11 = float(input("Enter length of Link 1 (m): "))
12 = float(input("Enter length of Link 2 (m): "))
13 = float(input("Enter length of Link 3 (m): "))
q1 = np.radians(float(input("Enter angle of Joint 1 (deg): ")))
q2 = np.radians(float(input("Enter angle of Joint 2 (deg): ")))
d3 = float(input("Enter extension length (m): "))

pos = stanford_fwd_kin(q1, q2, l1, l2, l3, d3)

print("\nEnd effector position :")
print("x = ", str(pos[0])," m, y = ",str(pos[1]), " m, z = ", str(pos[2]), " m")

input()
```

Output:

```
Enter length of Link 1 (m): 2
Enter length of Link 2 (m): 2
Enter length of Link 3 (m): 2
Enter angle of Joint 1 (deg): 30
Enter angle of Joint 2 (deg): 45
Enter extension length (m): 1

End effector position:

x = 3.0618621784789726 m, y = -1.7677669529663687 m, z = 5.535533905932738 m
```

95

Set
$$x_0-4_0-3_0$$
 be the base frame

 $x_2-4_2-3_3$ be the drone trame

 $x_3-4_2-5_2$ be drone trame after first rotation

 $x_3-4_5-3_3$ be drone frame after second edution

quitted pos. of drone,

Timit =
$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Tiest rot" of from ,

$$R_{1} = R_{2,30} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos 30^{\circ} & -\sin 30^{\circ} & 0 \\ 0 & \sin 30^{\circ} & \cos 30^{\circ} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

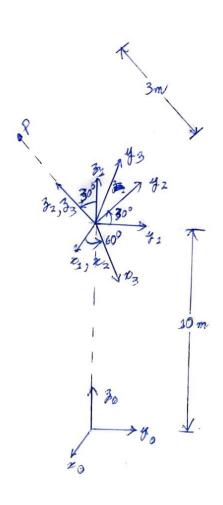
Second not " of drone,

$$R_{2} = R_{3,60}^{\circ} = \begin{bmatrix} \cos 60^{\circ} & -\sin 60^{\circ} & 0 & 0 \\ \sin 60^{\circ} & \cos 60^{\circ} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Bes. of obstacle relative to drove,

! Position of obstacle w. a. v. Base frame, Peace = Tinia R. R. Parone

$$\Rightarrow P_{base} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 10 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \frac{1}{3}/2 & \frac{1}{3}/2 & 0 \\ 0 & 0 & \frac{1}{3}/2 & \frac{1}{3}/2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{1}{3}/2 & \frac{1}{3}/2 & 0 & 0 \\ 0 & 0 & \frac{1}{3}/2 & \frac{1}{3}/2 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{1}{3}/2 & \frac{1}{3}/2 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 &$$





1. Planstany yearson

Pros!

- · Afters high torque in a compact size.
- . They have low backlash and high obsidency.
- · lan handle both low and high speed applications.

lons :

- · Complicated design and manufacturing.
- · shey we costly.
- · May dissipate large amounts of heat, so may need looking:

Mage;

- · Robotie erms .
- · Humanoid robots.

20 Spur Gearbon

Pros!

- · Simple and cost effective design,
- · whey have high efficiency.

lons;

- · Surger in sigs than other types of gentlenes with nimited tokque ratings.
- · lamost bandle very high torques.

. Usage :

- · loweyer belts.
- · simple robotic vehicles,

3. Eyeloidal Gearbox

Pros :

- · lan transmit high amounts of tarques
- · lan handle shock loads,
- · Relatively compact in sign.

lons!

- . Sower efficiency than planetery and spar gentones.
- · Balancing is sifficult.

Menge!

- · Industrial cutomation.
- · Robotic manipulators.

4. Worm Gearbon

Pros!

- · High reduction rations.
- · self booking property :
- · Onecise linear motion passible.

eons;

- · sower efficiency sue to soliding contact.
- · generate more heat.

Mage!

- · Robot may joints .
- · butomatic doors.

gearboxes in promes

gentlemes are frequently used in dromes, dromes are usually bitted with brushless DC motors (BLDC), which have high speed but low torque. For the propellers to be able to lift the drome and control it, shey should to produce enough thrust. To exhicuse this, a gearbox can be used to increase output torque while decreasing notational speeds hence the motor can run at a speed where it has the highest afficiency, while also providing adequate thrust. Moreover, the gearbox allows when when specially and more efficiency.

Q7 Justian of SCARA monipulator

From DH coordinate frame assignment, the A-medices

$$A_{1} = \begin{bmatrix} \cos q_{1} & -\sin q_{1} & 0 & e_{1} \cos q_{1} \\ e \cos q_{1} & \cos q_{1} & 0 & e_{1} \sin q_{1} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_{2} = \begin{bmatrix} \cos q_{2} & \sin q_{2} & 0 & l_{2} \cos q_{2} \\ \sin q_{2} & -\cos q_{2} & 0 & l_{2} \sin q_{2} \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_{3} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & d_{3} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$A_{4} = \begin{bmatrix} \cos q_{11} & -\sin q_{12} & 0 & 0 \\ \sin q_{12} & \cos q_{12} & 0 & 0 \\ 0 & 0 & 1 & d_{12} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

there, joints 1, 2, and 4 are nevolute and joint 3 is poismatic, and on - on is parallel to 33.

The Gordian is of the form;

$$\int_{0}^{\infty} \int_{0}^{\infty} \left(\sigma_{1} - \sigma_{0} \right) \qquad \int_{0}^{\infty} \int_{1}^{\infty} \left(\sigma_{1} - \sigma_{1} \right) \qquad \int_{0}^{\infty} \int_{0}^{\infty} \int_{0}^{\infty} \left(\sigma_{1} - \sigma_{1} \right) \qquad \int_{0}^{\infty} \int_{0}^{\infty} \left[e_{1} \cos \varphi_{1} + e_{2} \cos \left(q_{1} + q_{2} \right) \right] \\
e_{2} \sin \varphi_{1} \qquad \int_{0}^{\infty} \left[e_{1} \cos \varphi_{1} + e_{2} \cos \left(q_{1} + q_{2} \right) \right] \\
e_{3} \cos \varphi_{1} + e_{2} \cos \left(q_{1} + q_{2} \right) \\
e_{4} \cos \varphi_{1} + e_{2} \sin \left(q_{1} + q_{2} \right) \\
e_{5} \cos \varphi_{1} + e_{2} \sin \left(q_{2} + q_{2} \right) \\
e_{5} \cos \varphi_{1} + e_{3} \sin \left(q_{2} + q_{3} \right) \\
e_{5} \cos \varphi_{2} + e_{3} \sin \left(q_{2} + q_{3} \right) \\
e_{5} \cos \varphi_{1} + e_{3} \sin \left(q_{2} + q_{3} \right) \\
e_{5} \cos \varphi_{2} + e_{3} \sin \left(q_{3} + q_{3} \right) \\
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e_{5} \cos \varphi_{3} + e_{5} \cos \varphi_{3} + e_{5} \cos \left(q_{3} + q_{3} \right) \\
e_{7} \cos \varphi_{3} + e_{7} \cos \varphi_{3} + e_{7} \cos \left(q_{3} + q_{3} \right) \\
e_{7} \cos \varphi_{3} + e_{7} \cos \varphi_{3} + e_{7} \cos \left(q_{3} + q_{3} \right) \\
e_{7} \cos \varphi_{3} + e_{7} \cos \varphi_{3} + e_{7} \cos \left(q_{3} + q_{3} \right) \\
e_{7} \cos \varphi_{3} + e_{7} \cos \varphi_{3} \right) \\
e_{7} \cos \varphi_{3} + e_{7} \cos \varphi_{3$$

Men, 30 = 32 = k, 2= 33 = -k

: Jacobian of SCARA manipulator is:

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{1} + q_{2})} \frac{e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{2} \cos (q_{2} + q_{2})} \frac{\partial}{\partial e_{3}}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{3} \cos (q_{1} + q_{2})}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{3} \cos (q_{1} + q_{2})}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{3} \cos (q_{1} + q_{2})}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{3} \cos (q_{1} + q_{2})}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{3} \cos (q_{1} + q_{2})}$$

$$\int_{0}^{\infty} \frac{e_{1} \sin q_{1} - e_{2} \sin (q_{1} + q_{2})}{e_{3} \cos (q_{1} + q_{2})}$$

$$\int_{0}^{\infty} \frac{e_{1} \cos (q_{1} - q_{2})}{e_{3} \cos (q_{1} - q_{2})}$$

$$\int_{0}^{\infty} \frac{e_{1}$$

Source Code: (Link to GitHub)

```
import numpy as np
Program to calculate the manipulator Jacobian for an RRP SCARA robot.
Parameters:
q1 = Angle of Joint 1
q2 = Angle of Joint 2
d3 = Extension length of the robot arm
11 = Length of Link 1
12 = Length of Link 2
def scara_jacobian(q1, q2, l1, l2, d3):
    jacobian = np.array([
                           [-11 * np.sin(q1) - 12 * np.sin(q1 + q2), -12 *
np.sin(q1 + q2), 0],
                           [11 * np.cos(q1) + 12 * np.cos(q1 + q2), 12 *
np.cos(q1 + q2), 0],
                           [0, 0, -d3],
                           [0, 0, 0],
                           [0, 0, 0],
                           [1, 1, 1]
                        ])
    return jacobian
11 = float(input("Enter length of Link 1 (m): "))
12 = float(input("Enter length of Link 2 (m): "))
q1 = np.radians(float(input("Enter angle of Joint 1 (deg): ")))
q2 = np.radians(float(input("Enter angle of Joint 2 (deg): ")))
d3 = float(input("Enter extension length (m): "))
jacobian = scara_jacobian(q1, q2, l1, l2, d3)
print("\nJacobian matrix for SCARA robot:")
print(jacobian)
input()
```

Output:

```
Enter length of Link 1 (m): 2
Enter length of Link 2 (m): 2
Enter angle of Joint 1 (deg): 30
Enter angle of Joint 2 (deg): 45
Enter extension length (m): 1
Jacobian matrix for SCARA robot:
[[-2.93185165 -1.93185165 0.
 2.2496889
              0.51763809 0.
                         -1.
  0.
              0.
              0.
  0.
                          0.
   0.
              0.
                          0.
   1.
               1.
                          1.
```

99

Jacobian of RRR Plener manipulator

Here, the Jacobian & of the form

$$\frac{e_{1} (x q_{2} + e_{2} (x q_{2} + q_{2}) + e_{3} (x q_{1} + q_{2} + q_{3})}{e_{3} = e_{1} (x q_{1} + e_{2} (x q_{2} + q_{2}) + e_{3} (x q_{1} + q_{2} + q_{3})}$$

unit vectors,

$$30 = 31 = 32 = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

as They're all parallel to go axis.

?: Justian of RRR Planer manipulator is:

$$\int_{-2}^{-2} \frac{s_{1}}{s_{1}} - \frac{l_{2}}{s_{12}} \frac{s_{123}}{s_{123}} - \frac{l_{2}}{s_{123}} \frac{s_{123}}{s_{123}} - \frac{l_{3}}{s_{123}} \frac{s_{123}}{s_{23}} - \frac{l_{3}}{s_{23}} \frac{s_{123}}{s_{23}} - \frac{l_{3}}{s_{23}} \frac{s_{123}}{s_{23}} - \frac{l_{3}}{s_{23}} \frac{s_{123}}{s_{23}} - \frac{l_{3}}{s_{23}} \frac{s_{$$

Source Code: (Link to GitHub)

```
import numpy as np
Program to calculate the manipulator Jacobian for an RRR Planar robot.
Parameters:
q1 = Angle of Joint 1
q2 = Angle of Joint 2
q3 = Angle of Joint 3
11 = Length of Link 1
12 = Length of Link 2
13 = Length of Link 3
def rrr_planar_jacobian(q1, q2, q3, l1, l2, l3):
    jacobian = np.array([
                           [-11 * np.sin(q1) - 12 * np.sin(q1 + q2) - 13 *
np.sin(q1 + q2 + q3), -12 * np.sin(q1 + q2) - 13 * np.sin(q1 + q2 + q3), -13 *
np.sin(q1 + q2 + q3)],
                           [11 * np.cos(q1) + 12 * np.cos(q1 + q2) + 13 *
np.cos(q1 + q2 + q3), 12 * np.cos(q1 + q2) + 13 * np.cos(q1 + q2 + q3), 13 *
np.cos(q1 + q2 + q3)],
                           [0, 0, 0],
                           [0, 0, 0],
                           [0, 0, 0],
                           [1, 1, 1]
                        ])
    return jacobian
11 = float(input("Enter length of Link 1 (m): "))
12 = float(input("Enter length of Link 2 (m): "))
13 = float(input("Enter length of Link 3 (m): "))
q1 = np.radians(float(input("Enter angle of Joint 1 (deg): ")))
q2 = np.radians(float(input("Enter angle of Joint 2 (deg): ")))
q3 = np.radians(float(input("Enter angle of Joint 3 (deg): ")))
jacobian = rrr_planar_jacobian(q1, q2, q3, l1, l2, l3)
print("\nJacobian matrix for RRR Planar robot:")
print(jacobian)
input()
```

Output:

```
Enter length of Link 1 (m): 2
Enter length of Link 2 (m): 2
Enter length of Link 3 (m): 2
Enter angle of Joint 1 (deg): 30
Enter angle of Joint 2 (deg): 45
Enter angle of Joint 3 (deg): 60
Jacobian matrix for RRR Planar robot:
[[-4.34606521 -3.34606521 -1.41421356]
  0.83547534 -0.89657547 -1.41421356
               0.
  0.
                           0.
  0.
               0.
                           0.
                           0.
   0.
               0.
   1.
               1.
                           1.
```

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